

ciselne obory
 $\mathbb{N}, \mathbb{N}_0, \mathbb{Z}, \mathbb{Q}, \mathbb{R}$
castecne usporadana mnozina

- reflexe
- antisymetre
- tranzitivita

priklad 1

$x, y \subseteq \mathbb{R}$:

- $\forall x \in X \forall y \in Y x \leq y \ (x < 0 < y)$
- $\exists x \in X \exists y \in Y x \leq y \ (x=y=0)$
- $\exists x \in X \forall y \in Y x \leq y \ (\min(x) \leq \min(y))$
- $\forall x \in X \exists y \in Y x \leq y \ (\max(x) \leq \max(y))$
- $\forall y \in Y \exists x \in X x \leq y \ (\min(x) \leq \min(y))$
- $\exists y \in Y \forall x \in X x \leq y \ (\max(x) \leq \max(y))$

omezenost

$X \subseteq \mathbb{R}$ je omezena $\Leftrightarrow \exists y \in \mathbb{R}^+ \forall x \in X : -y \leq x \leq y$

jednoznacnost

$f \subseteq X \times Y$

$\forall x \in X \exists! y \in Y : f(x) = y$

omezenost funkce

maximum \neq shora omezena (napr otevreny interval)

priklad 2

$X \subseteq \mathbb{R} : \exists a, b, c \in \mathbb{R} \forall x, y \in \mathbb{X}, \in \mathbb{R} (x \neq y) \Rightarrow (a < x \& y < b \& |x - y| < c)$

omezena zdola, zhora, $c=a+b$

HW

$X \subseteq \mathbb{R}$: nekonecna t. ze

$\exists a, b, c \in \mathbb{R} : c > 0 \& \forall x, y \in \mathbb{X}, \in \mathbb{R} (x \neq y) \Rightarrow (a < x \& y < b \& |x - y| > c)$

... interval to nebude

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dukaz ze $\sqrt{2}$ neni racionalni

dukaz ze $k \in \mathbb{N}$

$\mathbb{N}^k \quad (\mathbb{N} * \mathbb{N} * \dots * \mathbb{N})$

je spocetna mnozina

$\forall a, b, \in \mathbb{R} : (a < b) \rightarrow (\exists c \in \mathbb{Q} : a < c < b)$

hledani suprema, infima a zjistovani min a max nejake mnoziny

$A = \{\frac{1}{n}, n \in \mathbb{N}\}$ sup=1, inf=0

$B = \{q \in \mathbb{Q} : q^2 < 2\}$ sup= $\sqrt{2}$, inf= $-\sqrt{2}$

$C = \{0.3, 0.33, 0.333...1/3\}$ sup=1/3, inf=0,3

sjednocovani suprema a infima

necht: $\sup(A) = a, \sup(B) = b$

$\sup(A \cup B) = \max(a, b)$

$\sup(A \cap B) = \min(a, b)$ pokud $A \cap B \neq \emptyset$

$$\sup(A + B) = (a + b)$$

$$\sup(A - B) = \sup(A) - \inf(B)$$

AG nerovnost

$$a_1, \dots, a_n \text{ in } \mathbb{R}^+ : \frac{a_1 + \dots + a_n}{n} \geq \sqrt[n]{a_1 * \dots * a_n}$$

ulohy:

$$A = \{q \in \mathbb{Q} | q < \sqrt{3}\} \quad \sup = \sqrt{3}, \inf = -\infty$$

$$B = \{\sin x | x \in (0, 2\pi)\} \quad \sup = 1, \inf = -1$$

$$C = \{\frac{n-1}{n} | n \in \mathbb{Z} \setminus \{0\}\} \quad \sup = 2, \inf = 0$$