Predmet: Mataliza 1

Ukol: 5. Verze: 1.

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Prezdivka: DN

#### zadani

$$\lim_{x \to 1} \frac{x^3 - x^2 - x + 1}{x^3 + x^2 - x - 1}$$

## reseni

$$lim_{x\to 1} \frac{(x-1)(x^2-1)}{(x+1)(x^2-1)}$$

$$lim_{x\to 1} \frac{x-1}{x+1}$$

$$\frac{1-1}{1+1} = \frac{0}{2} = 0$$

$$lim_{x\to 1} \frac{x^3 - x^2 - x + 1}{x^3 + x^2 - x - 1} = 0$$

### zadani

$$lim_{x\to 1} \frac{x^3 + x^2 - x - 1}{x^3 + 2x^2 - x - 2}$$

#### reseni

$$lim_{x \to 1} \frac{(x^2 - 1)(x + 1)}{(x^2 - 1)(x + 2)}$$

$$lim_{x \to 1} \frac{(x + 1)}{(x + 2)}$$

$$\frac{(1 + 1)}{(1 + 2)} = \frac{2}{3}$$

$$lim_{x \to 1} \frac{x^3 + x^2 - x - 1}{x^3 + 2x^2 - x - 2} = \frac{2}{3}$$

### zadani

$$\lim_{x \to -1} \frac{x^3 - x^2 - x + 1}{x^3 + x^2 - x - 1}$$

### reseni

$$lim_{x \to -1} \frac{(x-1)(x^2-1)}{(x+1)(x^2-1)}$$

$$lim_{x \to -1} \frac{(x-1)}{(x+1)}$$

$$\frac{-1-1}{(-1\pm\epsilon)+1} = \frac{-2}{0\pm\epsilon} = \pm\infty$$

$$lim_{x \to (-1)} - \frac{(x-1)}{(x+1)} = \infty$$

$$lim_{x \to (-1)} + \frac{(x-1)}{(x+1)} = -\infty$$

# zadani

$$\lim_{x\to -1} \frac{x^3+x^2-x-1}{x^3+2x^2-x-2}$$

### reseni

$$\begin{split} lim_{x \to -1} \frac{(x^2 - 1)(x + 1)}{(x^2 - 1)(x + 2)} \\ lim_{x \to -1} \frac{(x + 1)}{(x + 2)} \\ \frac{(-1 + 1)}{(-1 + 2)} &= \frac{0}{1} \\ lim_{x \to -1} \frac{x^3 + x^2 - x - 1}{x^3 + 2x^2 - x - 2} &= 0 \end{split}$$