

# Recommender Systems

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# Recommender Systems

- Overview **Wednesday**
- Content-based Systems **Wednesday**
- Collaborative Filtering **Friday & Saturday**
- Evaluating Recommender Systems **Friday & Saturday**

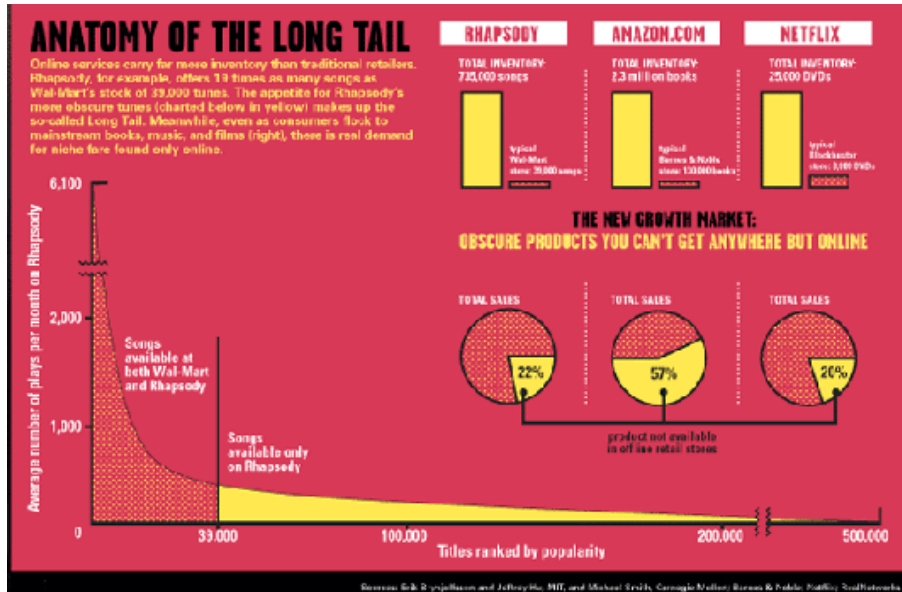
This section is based on **Jeff Ullmanns MMDS Course**

# Overview

# Long Tail Distribution

How **Into the Air** made  
**Touching the Void** a bestseller

More choices necessitates  
better filters



- Books, movies, music, news articles
- Fashion
- Bids
- People (friend recommendations of social media)

Read the Article

# Type of Recommendations

- Editorial and hand curated
  - List of favorites
  - List of "essential" items
- Simple Aggregates
  - Top 10, Most Popular, Recent Uploads
- Tailored to individual user
  - Netflix, Trendyol, Sahibinden.com...

# Formal Model

- $C$  = set of Customers
- $S$  = set of Items
- Utility Function  $u : C \times S \rightarrow R$ 
  - $R$  = set of Ratings
  - $R$  is a totally ordered set
  - e.g., 0-5 stars, real numbers in  $[0,1]$

# Totally Ordered Set

## A Short Update on Classification vs Regression

- How does it sound to compare different  $y$  values of a **regression** problem ?
  - **Rental Price:** [1000€, 10000€]
  - **Dam Capacity:** [0,100]
- How does it sound to compare different  $y$  values of a **classification** problem ?
  - **Sentiment:** Positive, Negative
  - **Image classification:** Cat, Dog

# Utility Matrix

	<i>Avatar</i>	<i>Blade Runner</i>	<i>Matrix</i>	<i>Pirates</i>
<i>Alice</i>	1		.2	
<i>Bob</i>		0.5		0.3
<i>Carol</i>	.2		1	
<i>David</i>				0.4

*Carol* ♥ *Matrix*

Extrapolating Utility Matrix



# Utility Matrix

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# Problems to Address

## 1. Building Utility Matrix

- How to collect data ?

## 2. Extrapolate unknown ratings using the known ones

- Note that **utility matrix** is highly sparse.

## 3. Evaluating extrapolation methods

- How to measure the **performance** of a recommender system ?

# Building Utility Matrix

- **Explicit**: Ask people to rate items
  - 👍 Usually gives a better estimator for a given user
  - 👎 Doesn't scale very well (think of utility matrix size) 🤔
- **Implicit**: Learn ratings from user actions
  - 👍 Much scalable
  - 👎 Defining rules might be challenging
  - 👎 How about low ratings ?
- **Explicit + Implicit**: Combine two



# Extrapolating Utility Matrix

- **Key Problem:** Matrix **U** is sparse
  - $r$  value is missing for most  $(u, s)$  pair. 🤔
  - Cold Start Problem
    - A **row** of **U** is completely empty 🤔
    - A **column** of **U** is completely empty 🤔
- **Three main approaches**
  1. Content-based
  2. Collaborative
  3. Latent factor based



# Content-based Systems

# Content-based Recommendations

**Main Idea:** Recommend items to customer  $c$  **similar** to previous items rated highly by  $c$

- **Movie**
  - Same actor(s), director, genre...
- **Website, blog, news or any document**
  - Documents with **similar** content
- **People**
  - Recommend people with many common friends, common hobbies, etc.

# Item Profiles

- For each item, create an **item profile**
- Convenient way to think of the item profile as a vector
  - One entry per feature
  - Vector might be boolean/real-valued

# Item Profiles

## How to incorporate Text Features

- **Important** words in text features
- Defining importance of a word as the combination (multiplication) of two
  - Presence of a word in a document (**tf**)
  - A word is **trivial** if it occurs in many documents (**idf**)



# Term Frequency (tf)

$f_{ij}$  = frequency of  $word_i$  in  $document_j$

🤔 We obtain **term frequency** by normalizing with **frequency of the most frequent word in that sentences.**

$$tf_{ij} = \frac{f_{ij}}{\max_k f_{kj}}$$

Refer **Term Frequency** for more term frequency calculation heuristics.

# Inverse Document Frequency (idf)

$n_i$  = Number of documents in which  $word_i$  is mentioned.

$N$  = Total number of documents.

$$idf_i = \frac{N}{n_i}$$

Refer [Inverse Document Frequency](#) for more **idf** calculation heuristics.

# Learn **tf-idf** by example

- For a simple case let's assume we have 2 text items to be profiled
  - **s1**: this<sup>1</sup> is<sup>2</sup> a<sup>3</sup> sample<sup>4</sup>
  - **s2**: this<sup>1</sup> is<sup>2</sup> another<sup>5</sup> sample<sup>4</sup>
- tf
  - $tf_{11} = \frac{1}{1}, tf_{21} = \frac{1}{1}, tf_{31} = \frac{1}{1}, tf_{41} = \frac{1}{1}, tf_{51} = \frac{0}{1}$
  - $tf_{12} = \frac{1}{1}, tf_{22} = \frac{1}{1}, tf_{32} = \frac{0}{1}, tf_{42} = \frac{1}{1}, tf_{52} = \frac{1}{1}$
- $idf_1 = \log \frac{2}{2}, idf_2 = \log \frac{2}{2}, idf_3 = \log \frac{2}{1}, idf_4 = \log \frac{2}{2}, idf_5 = \log \frac{2}{1}$
- $p(s_1) = \langle 0, 0, 1, 0, 0 \rangle$
- $p(s_2) = \langle 0, 0, 0, 0, 1 \rangle$

# Boolean Utility Matrix

- Assume customer  $c$  has watched 5 movies (remember **implicit** building of utility matrix.)
  - 2 movies featuring actor A
  - 3 movies featuring actor B
- Profile of user is  $[0.4 \ 0.6]$

# Star Rating

# Making Recommendations

- We have **user profiles**
- We have **item profiles**
- We can generate prediction by using vector similarity between two
  - $U(w_1, w_2) = \frac{w_1 w_2}{|w_1| |w_2|}$

# Pros: Content-based Approach

- No need for data on other users
- Able to recommend to users with unique tastes
- Able to recommend new & unpopular items
- Explanations for recommended items

# Cons: Content-based Approach

- Finding the appropriate feature is hard 🤔
  - Images 🤔
  - Movies 🤔
  - Music 🤔
- Overspecialization
  - Never recommends items outside user's content profile
  - Unable to exploit quality judgements of other users
- Cold-start problem for new users