```
Binomial Tests
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Setting Things Up in R
source("SETUP.R")
options(width = 70)
knitr::opts_chunk$set(
    tidy = FALSE,
    echo = TRUE,
    cache = FALSE,
    fig.keep = 'high',
    fig.show = 'asis',
    results = 'asis',
    # autodep = T,
    Rplot = TRUE,
    \underline{dev} = 'pdf',
    fig.path = 'graphics/reuters/rplot_',
    fig.width = 7,
    fig.asp = 1,
    out.width = "\\linewidth",
    collapse = TRUE
library(foreign) ## read.spss() ##
library(car) ## recode() ##
dat <- read.spss("data/reuters.sav", to.data.frame = TRUE)</pre>
dat <- within(dat, {recode(response, c("1=0", "2=1", "3=2"))})</pre>
```

Notes on the R-code above: SETUP.R is the default R-script I source in the "setup" code-chunk¹ at the beginning of all R markdown documents. It contains global arguments for loading commonly used packages, setting options, and defining various R-object utilities and functions. I also use this script as a record of functions I create while working in R. The script is heavily commented throughout for explanatory purposes, as well as for giving credit where it is due (I've tried to keep up with all of the R-code, LaTex, and R markdown sources, but may have missed some along the way).

AFTER SOURCING SETUP.R and setting a few output options (options() & opts_chunk\$set()), I load the {foreign} and {car} packages for the read.spss() and recode() functions, respectively. Then I read in (read.spss()) the Reuters polling dataset, "reuters.sav" and store

¹ see help(package = knitr)

it in R as a dataframe named "dat". Finally, I re-code the values for the "dat\$response" variable, using the {car} package's recode() function to undo default numeric values 1,2,3 and label values.

Data-Cleaning & Preparation

A few things need to happen to help optimize the information we put into and get out of the binomial hypothesis testing for the polling data. Specifically, I want set all values of "other" to "NA" in dat\$response, then drop all "NA" values since the analysis is only interested in responses for the two major candidates (i.e., Clinton and Trump).

However, there are also some existing "NAs" in "dat\$party", which need to be re-coded as well to avoid excluding rows with acceptable data values in dat\$response.



Risna <- function(x) **sum(is.na**(x))

Getting a count of NA values in the original dataframe ## sapply(dat, Risna)

id	response	party	partmiss	ind
О	О	377	О	О

```
R.na <- function(x, v = 0){
    ## x = object to be manipulated,
    ## v = value to assign to NAs ##
    x <- ifelse(is.na(x), v, x)</pre>
    return(x)
    }
```

Table 2: Summary information for 'party' data column before recoding NAs

M	0.42
SD	0.49
Min	0.00
Max	1.00

Note: This last recoding step seems unneccessary to me. I included it here based on Jason Newsom's code and in-class explanation, but when I run the rest of the analysis below without recoding, the results are the same. Is there a specific situation in which setting a discrete variable's values to '0, 1, 2, ...', versus '1, 2, 3, ...' is consequential to the analysis? Or is this a matter of personal preference for coding discrete variables? I think it would make more logical sense to me if, in this case, '0' strictly reflected 'No Response', but that is not the case here, as '0' reflects both 'Other' and 'No Response'. Further, should 'Other' responses not be coded as separate from 'No Response', given that an 'Other' response is absolutely qualitatively distinct from 'No Response'?

See Newsom 2016-CDA Handout-4

Note that the common method for binomial tests in R is to use exact.test = TRUE, which is actually the most conservative approach and also no ideal for binomial tests. Use prop.test() for approximate tests. (source: Jason Newsom)

sapply(), apply(), and vapply() are great function to get to know if you find yourself doing a ton of data cleaning/mining.

R.na(): "If x = NA (is.na()), replace xwith v, otherwise leave x alone."

t. ——

```
unique(dat$party)

o, 1 and _ _

dat$party <- sapply(dat$party, R.na, v = 99)
unique(dat$party)

o, 1 and 99</pre>
```

Table 3: Summary information for 'party' data column *after* recoding NAs

M 24.59 SD 42.42 Min 0.00 Max 99.00 NAs 0.00

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dat\$response <- recode_factor(dat\$response,</pre>

"other/no opinion" = NA_character_)

see "recode_factor()" in the {dplyr} package
dat <- na.omit(dat)</pre>

sapply(dat, R.isna) ## bye-bye NAs! ... again ##

id	response	party	partmiss	ind
0	О	0	О	О

```
## but this time we only lost data for rows with NA
```

in dat\$response (but we did lose ALL of the data

for those rows, as these were removed from the

dataframe entirely, though the original datafile remains untouched).

Now the data are, in my opinion, ready for analysis.

Single-Sample Binomial Tests: Differences in proportions of (non-"other") polling responses.

```
levels(dat$response)
  Trump and Clinton
poll.t <- table(dat$response)</pre>
## Why not make a table of the poll response counts for each candidate? ... ##
```

Table 5: Frequency Table of Polling Data

Response	Frequency
Trump	554
Clinton	677

DEFINITION OF A CONVENIENCE FUNCTION FOR THE BINOMIAL TEST. I'm combining the prop.test() & binom.test() functions ({pkg:stats}) because I think it's kind of ridiculous that there is not already a combined function for these. I also don't particularly enjoy the default output format for either of these functions, so I'm breaking the function writing rule of simplicity (AKA: "Curly's Law") and implementing some formatting tasks within the function as well.

Arguments (R.binom_test()):

- p. The target proportion to be tested against the null hypothesis (H_0 ; π_0 ; see pi0 below). Synonymous Arguments: x in prop.test() & binom.test().
- N. The size of the sample from which 'p' is taken. Synonymous Arguments: n in prop.test() & binom.test(). Synonymous Arguments: n in prop.test() & binom.test().
- pi0. [Default = 0.5]. A vector of probabilities of success corresponding to the value(s) in p. These probabilities represent the null hypothesis value (H_0 ; π_0) against which p is to be tested. Synonymous Arguments: p & conf.level (inverse) in prop.test() & binom.test().
- exact. Logical [Default = FALSE]. Should the the hypothesis be tested using an exact binomial test (i.e., binom.test()). If FALSE (the

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default), a test of equal or given proportions, depending on the lengths of p and pi0 is conducted using prop.test()
```

- correct. Logical Default = FALSE]. Synonymous with the correct
 argument in prop.test().
- digits. [Default = 2]. Number of digits to use when rounding
 (round()) the final output values (does not influence the test calculation).
- Additional arguments to be passed to either prop.test() or binom.test(), depending on the value set for exact (e.g., alternative).

Value (R.binomTest()): Returns a data.frame object containing the
values returned by either prop.test() or binom.test(), depending
on the value set for exact.

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```
R.binom_test <- function(p, N, pi0 = 0.5, exact = FALSE, correct = FALSE,
                         digits = 2, \ldots){
    if (exact) { ## Hypothesis Testing
        BT <- stats::binom.test(x = p, n = N, p = pi0, ...)
        }
        else {
            BT <- stats::prop.test(x = p, n = N, p = pi0,
                                   correct = correct, ...)
    ## The rest deals with formatting the output ##
        BT$data.name <- paste0(p, " out of ", N, " null probability ",
                               BT$null.value)
        ## Above, I modified the default output value for *.test$data.name
            ## to print the actual data values, rather than the object
            ## names the values are stored under (see output below) ##
        BTCI <- paste0(round(BT$conf.int[[1]], digits = digits), ", ",
                       round(BT$conf.int[[2]], digits = digits))
        BT$p.value <- round(BT$p.value, digits = 7)
        BT.df <- data.frame(c(BT[c("alternative",
                                    "null.value",
                                    "parameter",
                                    "estimate",
                                    "statistic",
                                    "p.value")],
                              BTCI))
        row.names(BT.df) <- NULL</pre>
        return(BT.df)
}
```

Approximate Test (prop. test())

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```
pt <- R.binom_test(\underline{p} = poll.t["Clinton"], \underline{N} = nrow(dat), \underline{pi0} = 0.5) ## ... Now we know where values for prop.test() came from :) ## ## There's more than one way to do that, by the way, but ## creating the table will come in handy later on too. ##
```

Table 6: 1-sample proportions test without continuity correction: 677 out of 1231

H_1	π_0	df	р	χ2	p-value	CI
two.sided	0.5	1	0.55	12	0.0005	0.52, 0.58

Exact Test (binom.test())



```
et <- R.binom_test(\underline{p} = poll.t["Clinton"],

\underline{N} = nrow(dat), \underline{pi0} = 0.5,

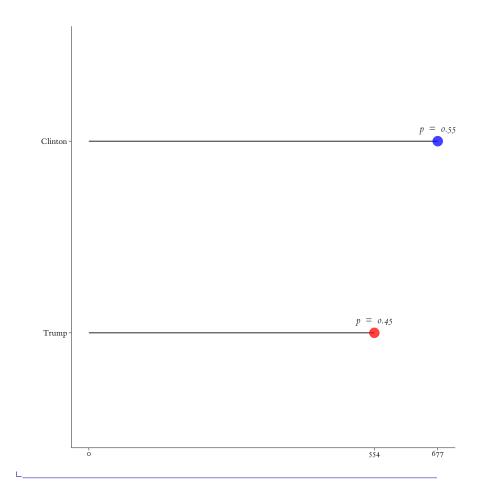
\underline{exact} = TRUE)
```

Table 7: 1-sample *exact* binomial test with continuity correction: 677 *out of* 1231

H_1	π_0	n_{trials}	p	$n_{successes}$	p-value	CI
two.sided	0.5	1231	0.55	677	0.0005	0.52, 0.58



```
poll.df <- as.data.frame(poll.t)</pre>
names( poll.df) <- c("Response", "Frequency")</pre>
poll.df$N <- rep(x = nrow(dat), times = nrow(poll.df))
n <- poll.df[, 2]</pre>
electpal <- c("red", "blue")</pre>
electpal <- sapply(electpal, adjustcolor, alpha = 0.75, <u>USE.NAMES = FALSE</u>)
bpoll <- ggplot( poll.df, aes(x = Frequency, y = Response)) +
    geom\_segment(aes(yend = Response), xend = 0, colour = mypal[20]) +
    geom\_point(\underline{size} = 5, aes(\underline{colour} = Response)) +
    scale_colour_manual(values = electpal, guide = FALSE) +
    labs(y = "", \underline{x} = "") + thm_tft(\underline{xline} = TRUE, yline = TRUE)
bpoll2 <- bpoll + scale_x_continuous(breaks = c(0, n),
                                        limits = c(0, max(n))
bpoll2 + geom_text(vjust = -1.5, hjust = 0.5, stat = 'identity',
                    position = 'identity', colour = mypal[19],
                    size = rel(4), aes(family = "ETBembo",
                                         fontface = "italic",
                                         label = paste("p = ",
                                                         round(n/ poll.df$N,
                                                                digits = 2))))
```



See Newsom 2016-CDA Handout-3

z-Score Test

Here we are taking one of the favorability proportions (i.e. "sucess proportions") and comparing it to the Null Hypothesis (H_0) represented by π_0 (i.e., 0.50).²

$$z = \frac{0.55 - 0.5}{\sqrt{\frac{0.5(1 - 0.5)}{1231}}} \Rightarrow \frac{0.05}{\sqrt{\frac{0.5(0.5)}{1231}}} \Rightarrow \frac{0.05}{\sqrt{\frac{0.25}{1231}}} \Rightarrow \frac{0.05}{\sqrt{0}} \Rightarrow \frac{0.05}{0.0143}$$
$$z = 3.5086$$

z-Score Test: Lower and Upper Confidence Limits

Confidence limits are calculated by the favorability proportion (p) \pm the $z_{critical}$ value multiplied by the standard error of the estimate $(SE_{\pi}).$

$$LCL_z = p - (1.96)(0.0142) \Rightarrow p - 0.0278 \Longrightarrow \textbf{0.5222}$$
 $UCL_z = p + (1.96)(0.0142) \Rightarrow p + 0.0278 \Longrightarrow \textbf{0.5778}$ $CI_z = \textbf{0.52}$

z-Score Test Margin of Error (ME_z)

$$ME_z = \frac{(0.5222 - 0.5778)}{2}(100) \Rightarrow \frac{(-0.0556)}{2}(100) \Rightarrow (-0.0278)(100)$$

 $ME_z = -2.7792$

Goodness-of-Fit Tests (χ^2)

Table 8: Summary of Known Values and Parameters for Pearson's χ^2 Goodness-of-Fit Test

N
$$n_{Clinton}^{\dagger}$$
 n_{Trump}^{\dagger} $z_{critical}$ $(df = 1)$
1231 677 554 3.84

Evaluate the observed χ^2 value to the χ^2 distribution ($f_k(x)$).

$$z = \frac{p - \pi_0}{SE_{\pi}}$$

$$SE_{\pi} = \sqrt{\frac{\pi_0(1 - \pi_0)}{n}}$$

$$CI = p \pm (z_{critical})(SE_{\pi})$$

$$CI_z = p \pm (z_{critical})(SE_{\pi})$$

$$z_{critical} = 1.96$$

$$p = 0.55$$

$$ME_z = \left(\frac{CI_z^+ - CI_z^-}{2}\right) (100)$$

$$\chi^2 = \Sigma \frac{(O_i - Ei)^2}{E_i}$$

$$O_1 = 677$$

$$O_2 = 554$$

$$E_i = \frac{(O_1 + O_2)}{2}$$

The χ^2 test's flexibility allows for additional comparison analyses. The Likelihood Ratio χ^2 is similar to the pearson χ^2 .

$$E_i = \frac{(677 + 554)}{2} \Rightarrow \frac{(1231)}{2}$$

$$E_i = 615.5$$

$$\chi^{2} = \frac{(677 - 615.5)^{2}}{615.5} + \frac{(554 - 615.5)^{2}}{615.5}$$

$$\Rightarrow \frac{(61.5)^{2}}{615.5} + \frac{(-61.5)^{2}}{615.5}$$

$$\Rightarrow \frac{(3782.25)}{615.5} + \frac{(3782.25)}{615.5}$$

$$\Rightarrow 6.145 + 6.145$$

$$\chi^2 = 12.29$$

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³ Note: This document was created using R-v3.3.2 R Core Team, R, and the following R-packages: base-v3.3. R Core Team, R, bibtex-vo.4. Francois, Bibtex, car-v2.1. Fox and Weisberg, An R Companion to Applied Regression, dplyr-vo.5. Wickham and Francois, Dplyr, DT-vo.2. Xie, DT, extrafontvo.17. Chang, Extrafont, ggplot2-v2.1. Wickham, Ggplot2, knitcitations-v1.o. Boettiger, knitcitations, knitr-v1.14. Xie, Dynamic Documents with R and Knitr, pander-vo.6. Daroczi and Tsegelskyi, Pander, papaja-vo.1. Aust and Barth, Papaja, plyr-v1.8. Wickham, "The Split-Apply-Combine Strategy for Data Analysis.", rmarkdown-v1.1. Allaire et al., rmarkdown, scales-vo.4. Wickham, Scales, tidyr-vo.6. Wickham, Tidyr, ggthemes-v3.2. Arnold, Ggthemes, gtablevo.2. Wickham, Gtable, kableExtra-vo.o. Zhu, KableExtra, tufte-vo.2. Xie and Allaire, Tufte, devtools-v1.12. Wickham and Chang, Devtools, highlight-vo.4. Francois, Highlight, sysfonts-vo.5. Qiu and others, Sysfonts, and showtext-vo.4. Qiu, Showtext

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