

## Homework 3, Question 3b

Rachel M. Smith

07 December 2016

---

### Data Descriptives

R

```
dat <- read.csv("data/states_new.csv")
dat <- dat[, c("Q3", "Q7", "Q8")]
dat <- na.omit(dat)
id <- seq(1:nrow(dat))
dat <- cbind(id, dat)
```

---

### Multiple Logistic Regression Model

R

```
library(MASS)
fit <- polr(factor(Q8) ~ Q3 + Q7 + Q3*Q7, data = dat, contrasts = NULL, method = "probit")
library("AER")
print(coeftest(fit))
```

z test of coefficients:

	Estimate	Std. Error	z value	Pr(> z )
Q3	0.0442	0.0453	0.97	0.3296
Q7	1.4158	0.3637	3.89	0.000099
Q3:Q7	-0.0436	0.0320	-1.36	0.1742
0 1	0.1869	0.4902	0.38	0.7030
1 2	1.8536	0.5582	3.32	0.0009

—

Signif. codes: 0 "0.001" 0.01 "0.05" 0.1 "1"

R

```

CI.b <- confint(fit, trace = FALSE)

OR <- exp(coef(fit))
CI <- confint(fit)

CIb <- cbind(coef(fit), CI.b)
CIb.labs <- c("***$\beta$", dimnames(confint(fit))[[2]])
CIb <- rbind(CIb.labs, round(CIb, 4))
dimnames(CIb)[[1]][1] <- " "
dimnames(CIb)[[2]] <- c(" ", "$CI_{\beta}$", " ")

## odds ratios and 95% CI ##
ORCI <- exp(cbind(coef(fit), CI))
ORCI.labs <- c("***$\Phi$", dimnames(confint(fit))[[2]])
ORCI <- rbind(ORCI.labs, round(ORCI, 4))
dimnames(ORCI)[[1]][1] <- " "
dimnames(ORCI)[[2]] <- c(" ", "$CI_{\Phi}$", " ")

library(lmtest) ## "lrtest()" ##
lrchsqr <- lrtest(fit)[2, -3]
lrchsqr <- lrchsqr[, c(2, 1, 3, 4)]
names(lrchsqr) <- c("Log Likelihood", "_df_", "$\chi^2$", "_p_")

library(pscl)
rsq <- pR2(fit)["McFadden"]
rsq[[1]]

0.2064

# names(rsq) <- c("McFadden's Pseudo-$R^2$")
# rsq.perc <- (rsq[2]*100)

```

---

### Model Fit Indices

Table 1: Likelihood Ratio  $\chi^2$ ,  $R^2$ , &  $G^2$

	Log Likelihood	$df$	$\chi^2$	$p$
2	-45.5	2	18.79	0.0003027

R

```
kable(CIb, align = rep('r', ncol(CIb)),
      caption = "Logistic Regression Coefficients ( $\beta$ ) \&
      Corresponding Confidence Intervals (_CI_)")
```

Table 2: Logistic Regression Coefficients ( $\beta$ ) &  
Corresponding Confidence Intervals (CI)

	$CI_{\beta}$		
	$\beta$	2.5 %	97.5 %
Q3	0.0442	-0.0442	0.1334
Q7	1.4158	0.7295	2.1616
Q3:Q7	-0.0436	-0.1066	0.0195

```
kable(ORCI, align = rep('r', ncol(ORCI)),
      caption = "Logistic Regression Odds Ratios ( $\Phi$ ) \&
      Corresponding Confidence Intervals (_CI_) [note]" ) %>%
      add_footnote("Confidence intervals are based on the logistic regression
      model's profiled log-likelihood function,
      rather than the standard errors",
      threeparttable = TRUE)
```

Table 3: Logistic Regression Odds Ratios ( $\Phi$ ) &  
Corresponding Confidence Intervals (CI) <sup>1</sup>

	$CI_{\Phi}$		
	$\Phi$	2.5 %	97.5 %
Q3	1.0451	0.9567	1.1427
Q7	4.1198	2.074	8.6851
Q3:Q7	0.9574	0.8989	1.0197

**Note:**

<sup>1</sup> Confidence intervals are based on the logistic regression  
model's profiled log-likelihood function,  
rather than the standard errors

ORDINAL PROBIT REGRESSION SUMMARY. An ordinal probit regression model was tested predicting whether states' batterer intervention program (BIP) standards were gender inclusive ( $Q8$ ) by the size of state standards' committees ( $Q3$ ), whether processes were in place for assessing BIPs' feedback about the standards ( $Q7$ ), and the interaction of these two predictors ( $Q3 \times Q7$ ). The predictors collectively accounted for a significant amount of variance in the outcome, likelihood ratio  $\chi^2(2) = 18.79, p < .001$ . However, only  $Q7$  significantly predicted  $Q8$ ,  $b = 1.42, SE = .36, p < .001$ ; such that a one unit increase in  $Q7$  was associated with approximately 34% increases in  $Q8$ . Overall, the model accounted for 21% of the variance in reported baseline income adequacy (*Mcfadden's pseudo- $R^2$*  = 0.2064).

COMPARISON WITH CUMULATIVE LOGISTIC MODEL. The above described ordinal probit regression analysis findings are starkly different from the originally tested logistic regression model, such that the effects of  $Q7$  are distinguishable in the probit model whereas they were not in the logistic regression model.