# Why Should We Care about Similarity of Satisfiability Problems?

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Part III
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- Feature Models
- A Matter of Size
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- Solving Similar SAT/BDD/SMT Instances
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- Time vs. Number of Selected Submodels
- Threats to Validity





# Why Should We Care about Similarity of Satisfiability Problems?

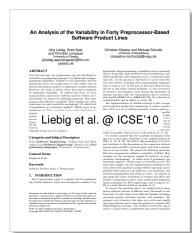
Thomas Thüm, Frederik Kanning, Stephan Mennicke, Ina Schaefer, ... FOSD Meeting 2017 in Grasellenbach, March 16, 2017

#### Part I

# Why Does Configurable Software Need Compositionality?



#### **Highly-Configurable Systems**

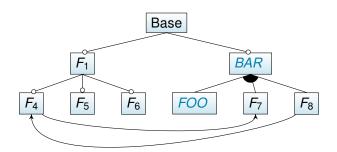








#### **Feature Models**







#### A Matter of Size



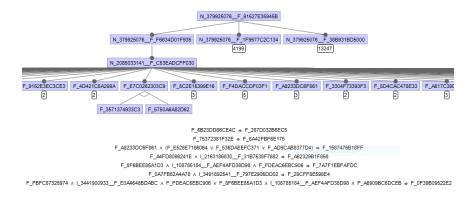
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Feature models with thousands of features are challenging





#### A Matter of Size



#### Feature models with thousands of features are challenging





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#ifdef BAR
int x = 0;
#endif
```





```
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int x = 0;
#endif
#endif
```





```
#ifdef BAR
int x = 0;
#endif
#endif
```

 $FOO \Rightarrow BAR$ ?



```
#ifdef BAR
int x = 0;
#endif

// ...
#ifdef F00
x++;
#endif
```

```
FM \models FOO \Rightarrow BAR?
```



```
#ifdef BAR
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```
\neg SAT(FM \land (FOO \Rightarrow BAR))?
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Idea: reduce size of feature model



```
#ifdef BAR
int x = 0;
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// ...
#ifdef FOO
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#endif
```

```
\overline{\mathbb{Z}} ¬SAT(FM \wedge (FOO \Rightarrow BAR)) ?
```

Idea: reduce size of feature model

- Type checking
- Parsing
- Dataflow analysis
- Model checking
- Deductive verification
- Refactoring
- Feature-model analysis
- Configuration process





#### Part II

# Compositional Analyses with Feature-Model Interfaces



## **Compositionality Principle**

$$(FOO \Rightarrow X) \land Y \land Z \land (X \Rightarrow BAR) \models FOO \Rightarrow BAR$$





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$$(FOO \Rightarrow X) \land Y \land Z \land (X \Rightarrow BAR) \models FOO \Rightarrow BAR$$

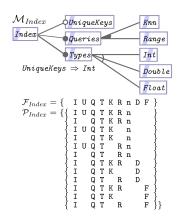
$$(FOO \Rightarrow X) \land (X \Rightarrow BAR) \models FOO \Rightarrow BAR$$



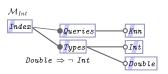


#### **Feature-Model Interfaces**

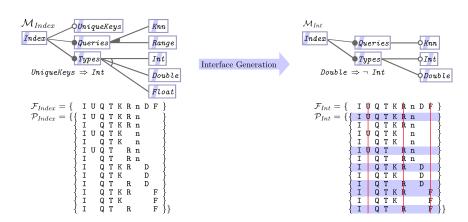
#### [ICSE'16]



Interface Generation







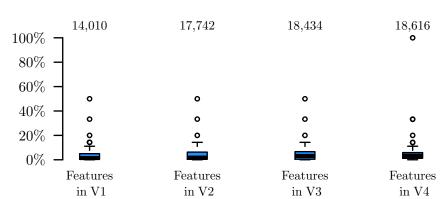
For scalability: features eliminated from propositional formulas with existential quantification





Given four monthly snapshots of an automotive feature model growing from 14k to 18k features

RQ1: How small can interfaces be compared to submodels?



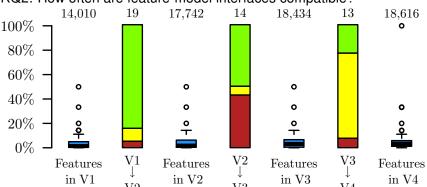




Given four monthly snapshots of an automotive feature model growing from 14k to 18k features

RQ1: How small can interfaces be compared to submodels?

RQ2: How often are feature-model interfaces compatible?







- Family-based type checking with TypeChef
- Linux kernel version 2.6.33.3 with 11,000 features
- 1,363 out of 7,760 files







- Family-based type checking with TypeChef
- Linux kernel version 2.6.33.3 with 11,000 features
- 1,363 out of 7,760 files
- 173,845 queries
- 90ms per query



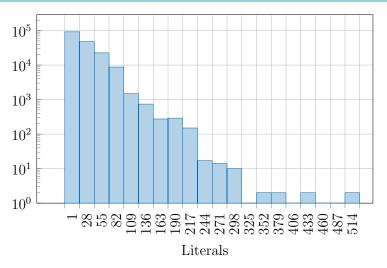


- Family-based type checking with TypeChef
- Linux kernel version 2.6.33.3 with 11,000 features
- 1,363 out of 7,760 files
- 173,845 queries
- 90ms per query
- 12s reasoning time per file
- Reasoning: 60% of type checking phase





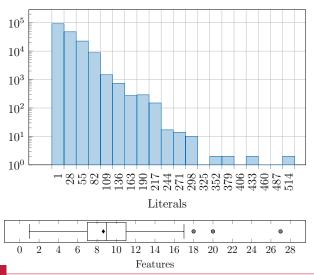
## **Literals and Distinct Features per Query**







## **Literals and Distinct Features per Query**







## **Apply Linux Queries to Automotive Feature Model**

Problem: no decomposition for Linux feature model and no domain artifacts/queries for automotive

Idea: use queries from Linux evaluation as templates

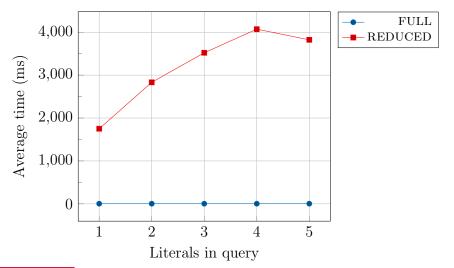
$$(\neg A \land B) \lor A \qquad \curvearrowright \qquad (\neg P \land Q) \lor P$$

Snapshot	Features	Constraints	Clauses	Submodels
1	14,010	666	237,706	44
2	17,742	914	342,935	45
3	18,434	1,300	347,557	46
4	18,616	1,369	350,287	46





# (No) Reduced Effort for Product-Line Analysis?







#### Part III

# Solving Similar SAT/BDD/SMT Instances



# **Profiling the SAT4J Implementation**

$$\neg SAT(FM \land (FOO \Rightarrow BAR))$$
 ?

⊡ <mark> </mark>	17.395 ms	(100%)
🖶 🎽 org.sat4j.core.ConstrGroup. <b>removeFrom</b> (org.sa	17.340 ms	(99,7%)
🖃 🤰 org.sat4j.minisat.core.Solver. <b>removeConstr</b>	16.724 ms	(96,196)
🕒 org.sat4j.core.Vec. <b>remove</b> (Object)	10.356 ms	(59,5%)
庄 🤰 org.sat4j.minisat.core.Solver. <b>clearLearnt</b>	2.582 ms	(14,8%)
庄 🤰 org.sat4j.minisat.constraints.cnf.BinaryClar	1.729 ms	(9,9%)
🕒 Self time	1.518 ms	(8,7%)
🕩 瀏 java.util.HashMap.get (Object)	507 ms	(2,9%)





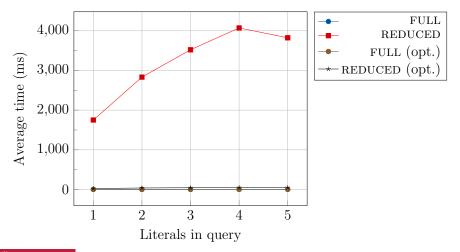
### **Profiling the SAT4J Implementation**

```
public void remove(T elem) {
 int j = 0;
  for (; this.myarray[j] != elem; j++) {
    if (j == size())
      throw new NoSuchElementException();
  System.arraycopy(this.myarray, j + 1,
  this.myarray, j, size() - j - 1);
  this.myarray[--this.nbelem] = null;
```





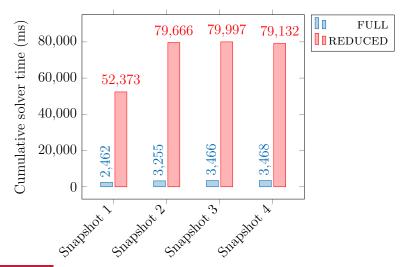
### **Effect of Our SAT4J Optimization**







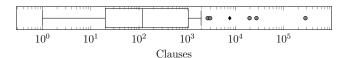
# **Cumulative Solver Time with Optimization**







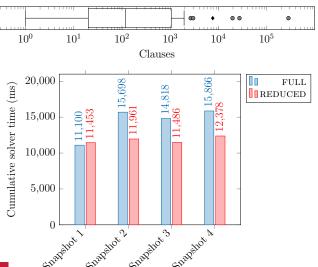
# The Influence of Large Submodels







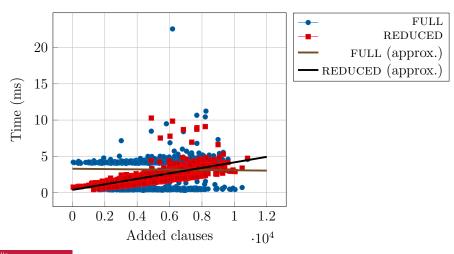
# The Influence of Large Submodels







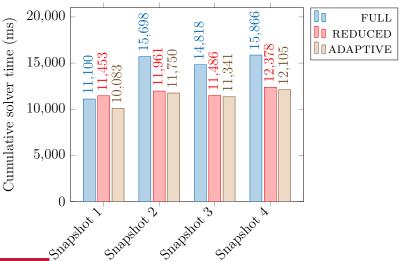
### Time vs. Added Submodel Clauses







### **Cumulative Solver Times with Threshold**







## Solving Similar SAT/BDD/SMT Instances

- SAT: similar instances not part of satisfiability contests
   ⇒ not optimized for this purpose
- BDD: no BDD for Linux, hard to join BDDs with different variable orderings
- SMT: recent developments for lightweight removal of formulas



# **How Should Superheroes Eat Cake?**





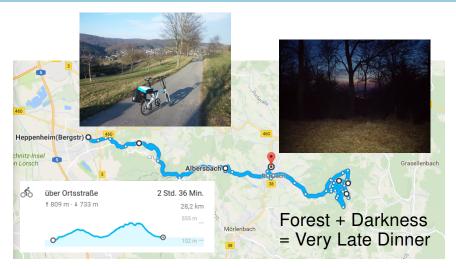
## We Should Care about Similarity of SAT Problems

- Configurable software requires to solve many similar SAT instances: consumes 60% of type checking (without parsing)
- Feature-model interfaces can significantly reduce the similar part
- Performance gain for reasoning 10–24%
- Open question: What are good decompositions of feature models?
- Open question: Are solvers ready to solve similar instances?





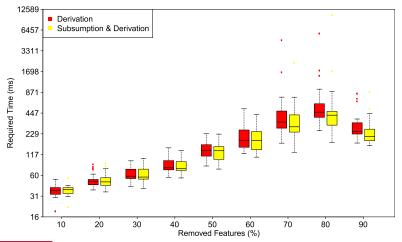
### **Experience Report: How NOT to Travel to FOSD'17**





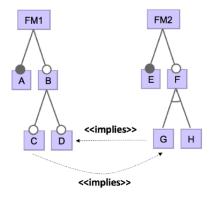


Removing x % of 18k features of an automotive feature model:

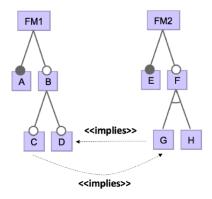






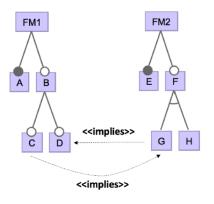


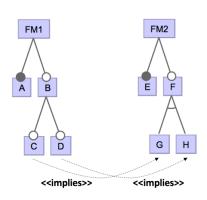




$$C \Rightarrow D$$





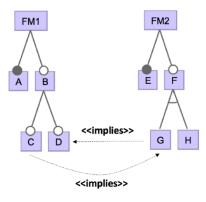


$$C \Rightarrow D$$

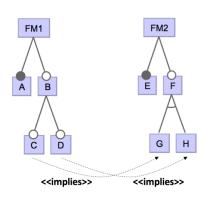


### **Make Implicit Constraints Explicit**

[FOSD'16]



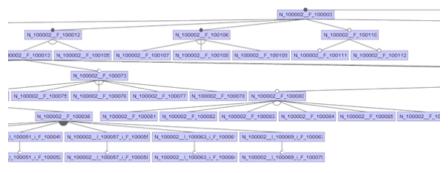
$$C \Rightarrow D$$



$$\neg C \lor \neg D$$



RQ1: How many implicit constraints exist in subtrees? Automotive feature model with 2,513 features and 2,833 constraints



Depth 1: 6 features and 12 implicit constraints

Depth 2: 25 features and 186 implicit constraints





## **Make Implicit Constraints Explicit**

[FOSD'16]

RQ2: What is the structure of implicit constraints?

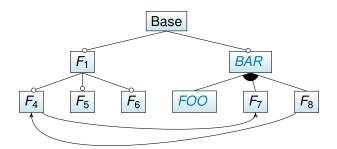
Expression	CNF Pattern	# I.C. Depth 1	# I.C. Depth 2	Overall (%)
Negation	¬ A	1	16	8,6
Implication	¬A∨B	11	18	14,6
Exclusion	¬Av¬B	-	31	15,7
Other	AvBvC	-	1	0,5
	¬Av¬BvC	-	115	58,1
	¬AvBvC	-	5	2,5

RQ3: What is the number of involved subtrees?

Depth 1: max. 4/6 partial models Depth 2: max. 5/25 partial models

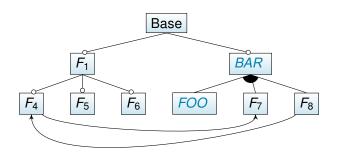








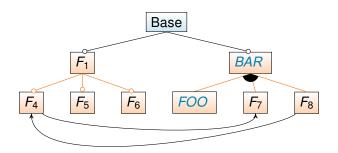




#### select subtrees



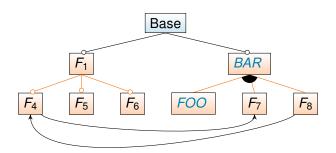




#### select subtrees



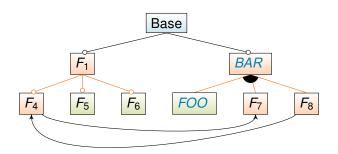




identify local features & local constraints



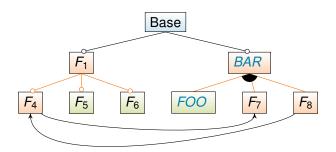




identify local features & local constraints



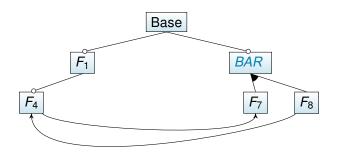




decompose model by removing local features



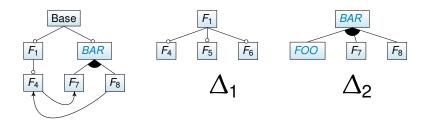




decompose model by removing local features

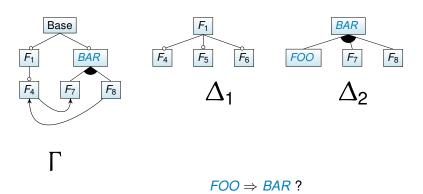






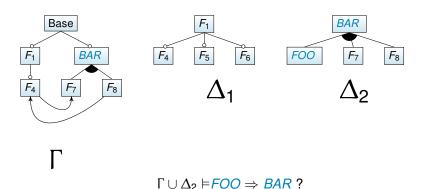






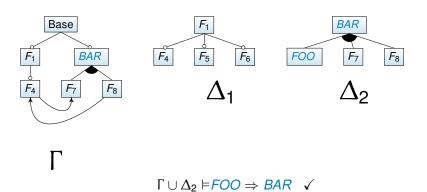




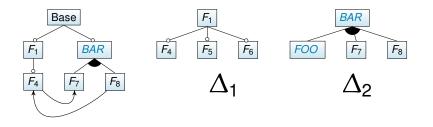










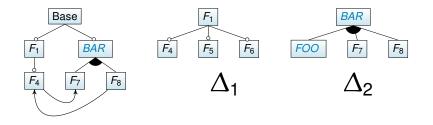


$$\Gamma \cup \Delta_2 \vDash FOO \Rightarrow BAR \checkmark$$

$$F_6 \Rightarrow Base ?$$



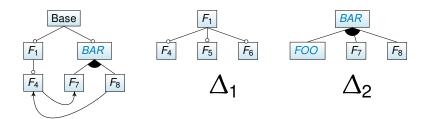




$$\Gamma \cup \Delta_2 \vDash FOO \Rightarrow BAR \checkmark$$
  
$$\Gamma \cup \Delta_1 \vDash F_6 \Rightarrow Base ?$$





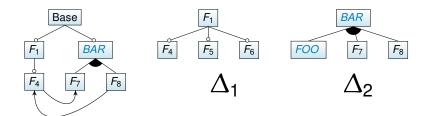


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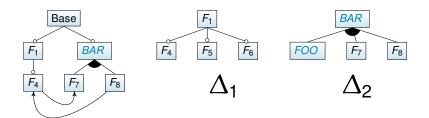
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$$\Gamma \cup \Delta_1 \vDash F_6 \Rightarrow Base \checkmark$$

$$F_1 \land F_6 \land FOO ?$$







$$\Gamma \cup \Delta_2 \vDash FOO \Rightarrow BAR \quad \checkmark$$

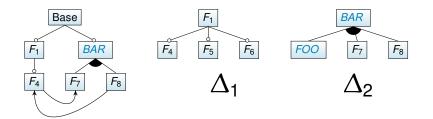
$$\Gamma \cup \Delta_1 \vDash F_6 \Rightarrow Base \quad \checkmark$$

$$\Gamma \cup \Delta_1 \cup \Delta_2 \vDash F_1 \land F_6 \land FOO ?$$





# **Compositionality with Feature-Model Interfaces**



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$$\Gamma \cup \Delta_2 \vDash FOO \Rightarrow BAR \quad \checkmark$$

$$\Gamma \cup \Delta_1 \vDash F_6 \Rightarrow Base \quad \checkmark$$

$$\Gamma \cup \Delta_1 \cup \Delta_2 \nvDash F_1 \land F_6 \land FOO \quad \checkmark$$

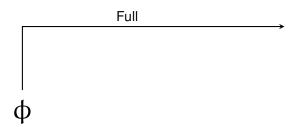






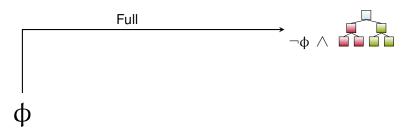






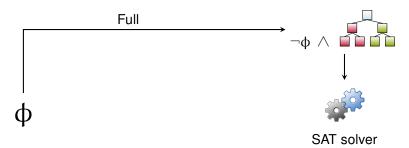




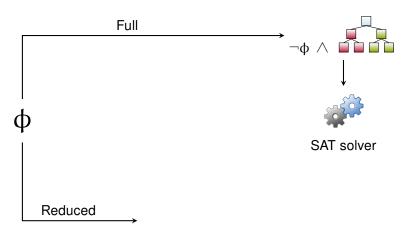






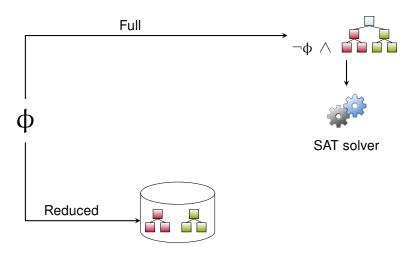






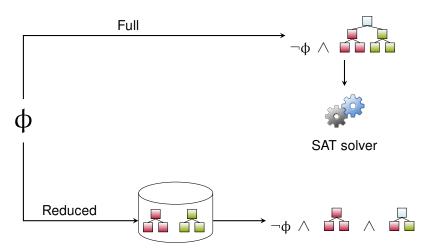






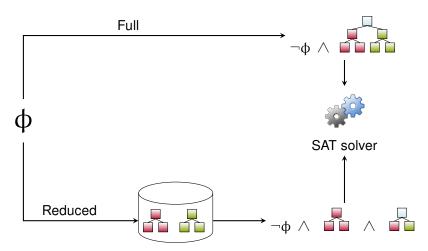






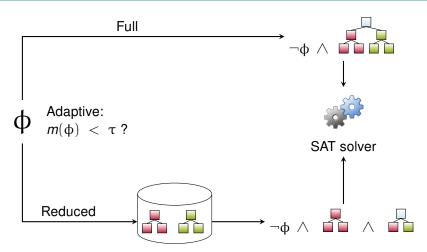






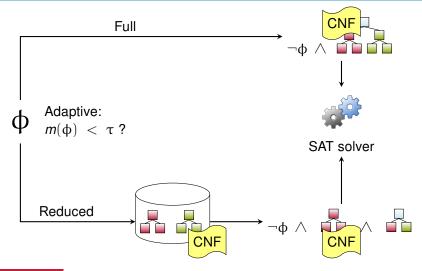
















#### **Setup for Measurements**

- Generate sets of 1,000 and 5,000 queries
- Full: pure solver time
- Reduced: selection + composition + solver times





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- Generate sets of 1,000 and 5,000 queries
- Full: pure solver time
- Reduced: selection + composition + solver times
- JVM: garbage collection & just-in-time compilation





### **Setup for Measurements**

- Generate sets of 1,000 and 5,000 queries
- Full: pure solver time
- Reduced: selection + composition + solver times
- JVM: garbage collection & just-in-time compilation
- ScalaMeter framework
  - Multiple measurements across different JVM runs
  - Warm-up runs
  - Outlier detection

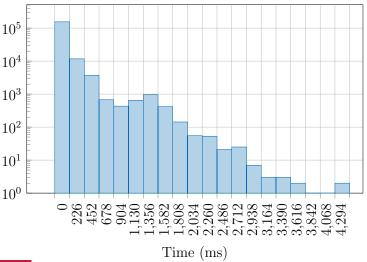








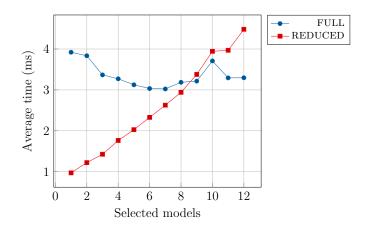
#### **Time to Solve SAT Queries**







#### **Time vs. Number of Selected Submodels**







## Threats to Validity

- Type checking
  - 1/6 of available files
  - Other analyses, product lines?







### Threats to Validity

- Type checking
  - 1/6 of available files
  - Other analyses, product lines?
- Reasoning with interfaces
  - Semi-random queries
  - Only snapshots of a single model
  - Single solver implementation
  - Isolated measurements





