# $mink Palu Forested Or Shrub More 405 ha\ model\ summary$

# Contents

Overview
Variables:
Components:
Model equation:
Global sensitivity and uncertainty analysis:
Model uncertainty
Model sensitivity
Original model
Arithmetic mean model
Geometric mean model
Limiting factor model
Multiplicative model
Summary of influential variables
References

#### Overview

This document summarizes the results of a global sensitivity and uncertainty analysis for the **minkPalu-ForestedOrShrubMore405ha** habitat suitability index (HSI) model for *Mustela vison*. Metadata for the model is stored in the ecorest package in R.

The original documentation for this model can be found here<sup>1</sup>.

 $\operatorname{Sub-model}$ : Palustrine forested wetland or shrub wetland cover types with area greater than or equal to  $\operatorname{405ha}$ 

The minkPaluForestedOrShrubMore405ha model is comprised of  ${\bf 4}$  variables and  ${\bf 2}$  components.

#### Variables:

**Table 1.** SIV variables included in the minkPaluForestedOrShrubMore405ha model. Type indicates whether a variable is numeric or categorical and breakpoints indicates the number of distinct breakpoints in suitability graphs.

	Variable name	Type	Breakpoints
SIV1	surface.wtr.present.all.yr.SIV	numeric	4
SIV2	${\it tree.can.cov.SIV}$	numeric	3
SIV3	shrub.can.cov.SIV	numeric	3
SIV4	emergent.veg.can.cov.SIV	numeric	4

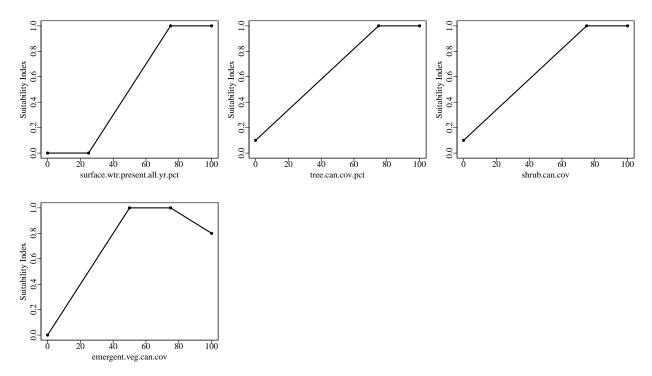


Figure 1. Suitability index graphs for variables included in the minkPaluForestedOrShrubMore405ha model in ecorest.

 $<sup>^{1}</sup> https://ecolibrary.sec.usace.army.mil/resource/adcd8e6b-26d7-408d-e383-2abb2fecec44$ 

#### Components:

Table 2. Components included in the minkPaluForestedOrShrubMore405ha model in ecorest.

Component		Equation
CCF CW	Food cover component Water component	$ \min(1,(SIV2+SIV3+SIV4)) $ SIV1

#### Model equation:

The equation to calculate an overall HSI index for the mink PaluForestedOrShrubMore405ha model is:  $\min(\text{CCF},\text{CW})$ 

According to our classification, this model's format is: author-specified

#### Global sensitivity and uncertainty analysis:

We ran global sensitivity and uncertainty analyses on the minkPaluForestedOrShrubMore405ha model using the sensobol package in R (Puy et al. 2022). The following parameters were used for the sensobol analysis:

**Table 3.** Parameters and settings used for sensobol sensitivity and uncertainty analyses.

Parameter	Equation	Value
Number of input variables (M) Base sample size (n) Number of model evaluations (N) First order estimator Total order estimator	- n*(M+2) See Puy et al. (2022) See Puy et al. (2022)	4 10000 60000 Saltelli Jansen
Number of bootstrap replications Sampling scheme Matrices	- -	1000 Quasi-random A, B, AB

We ran a sensitivity and uncertainty analysis for the minkPaluForestedOrShrubMore405ha model using the original equation outlined in the documentation from Allen (1986) and using arithmetic mean, geometric mean, limiting factor, and multiplicative equations to contrast the results across different equation structures.

#### Model uncertainty

We ran the minkPaluForestedOrShrubMore405ha model using 60000 combinations of its SIV variables, which were sampled from a uniform distribution spanning the range of possible values listed in the minkPaluForestedOrShrubMore405ha documentation. We limited the range of possible values for each parameter to the range in which the SIV values were greater than zero to prevent HSI score distributions with primarily zero values.

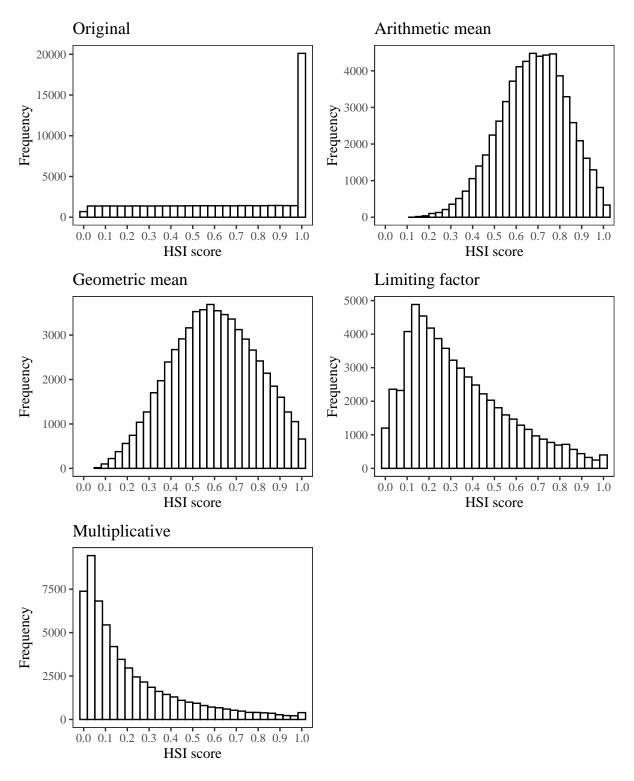


Figure 2. Empirical distributions of HSI scores for the minkPaluForestedOrShrubMore405ha model using the original author-specified model equation from Allen (1986), and an arithmetic mean, geometric mean, limiting factor, and multiplicative structure incorporating all SIV variables. Note differences in the y axis.

We assumed a uniform distribution for all parameters because we evaluated all ecorest models in batch. Should you decide to run your own sensitivity analysis, this assumption should be evaluated independently for each parameter in the model.

**Table 4.** Quantiles from the empirical distribution of HSI scores for the original minkPaluForestedOr-ShrubMore405ha model structure, an arithmetic mean equation, a geometric mean equation, a limiting factor equation, and a multiplicative equation structure.

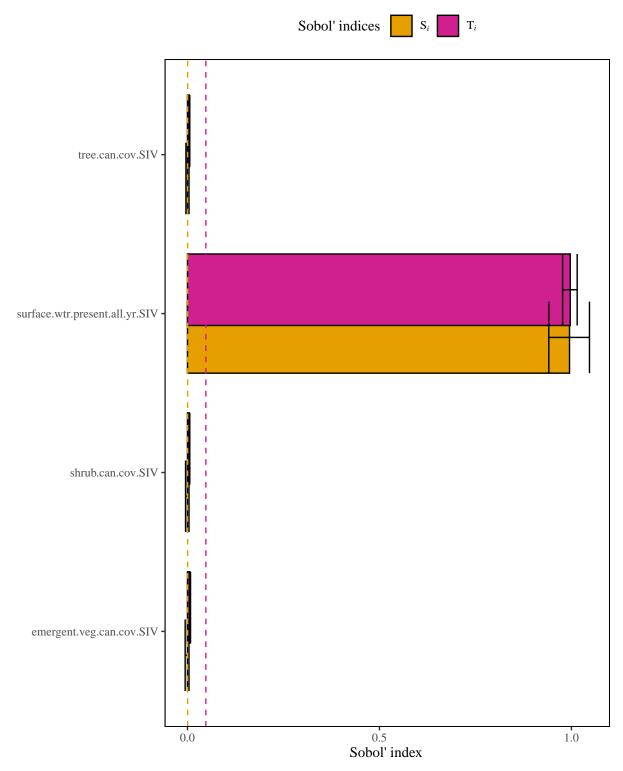
	1%	2.5%	5%	25%	50%	75%	95%	97.5%	99%	100%
Original	0.02	0.04	0.08	0.37	0.74	1.00	1.00	1.00	1.00	1
Arithmetic	0.30	0.36	0.41	0.58	0.69	0.79	0.93	0.96	0.99	1
Geometric	0.17	0.22	0.27	0.46	0.60	0.74	0.92	0.96	0.99	1
Limiting	0.01	0.02	0.04	0.16	0.28	0.47	0.80	0.87	0.95	1
Multiplicative	0.00	0.00	0.01	0.04	0.13	0.31	0.72	0.84	0.95	1

The empirical distribution of the original minkPaluForestedOrShrubMore405ha model has a coefficient of variation (CV) of **0.5**, while the arithmetic mean model has a CV of **0.228**, the geometric mean model has a CV of **0.326**, the limiting factor model has a CV of **0.679**, and the multiplicative model has a CV of **1.064**. Hence, the **Multiplicative** model is the most uncertain, while the **Arithmetic mean** model is the least uncertain.

#### Model sensitivity

Below are the results of the global sensitivity analysis for the minkPaluForestedOrShrubMore405ha model using the original equation, an arithmetic mean, a geometric mean, a limiting factor, and a multiplicative model structure. The sensobol package uses variance-based sensitivity metrics, so the model's sensitivity to a given parameter is a measure of how much variance in the HSI score decreases in response to that parameter being fixed (Puy et al. 2022). For each parameter, the observed changes in the variance of the HSI score can be described with a first order sensitivity index ( $S_i$ ) that accounts for the influence of a single parameter of interest on variance in HSI, or with a total order index ( $T_i$ ) that accounts for the influence of a single parameter on its own and in combination with all other parameters (*i.e.*, interactions) (Puy et al. 2022). We can compare the 95% confidence intervals for the first and total order indices to a dummy parameter, which represents a parameter that has no influence on the variance in a model's output. While an uninfluential variable should theoretically have an  $S_i$  and  $T_i$  of zero, small approximation errors can lead variables to have a non-zero influence on a model's output (Puy et al. 2022). If the confidence interval of the  $S_i$  and  $T_i$  index for a given parameter overlaps the confidence interval of the dummy parameter, we can deduce that the parameter has a negligible effect on variance in HSI scores, both on its own and in combination with all other variables.

### Original model



**Figure 3.** Results of a sensitivity analysis for the minkPaluForestedOrShrubMore405ha model based on the original author-specified model outlined in Allen (1986). Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

#### Arithmetic mean model

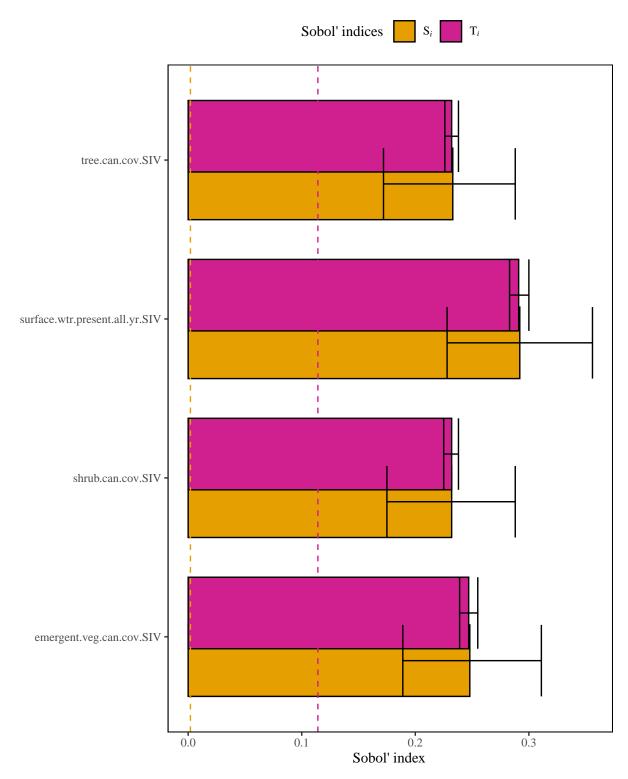


Figure 4. Results of a sensitivity analysis for the minkPaluForestedOrShrubMore405ha model based on an arithmetic mean structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (i.e., dummy variables).

#### Geometric mean model

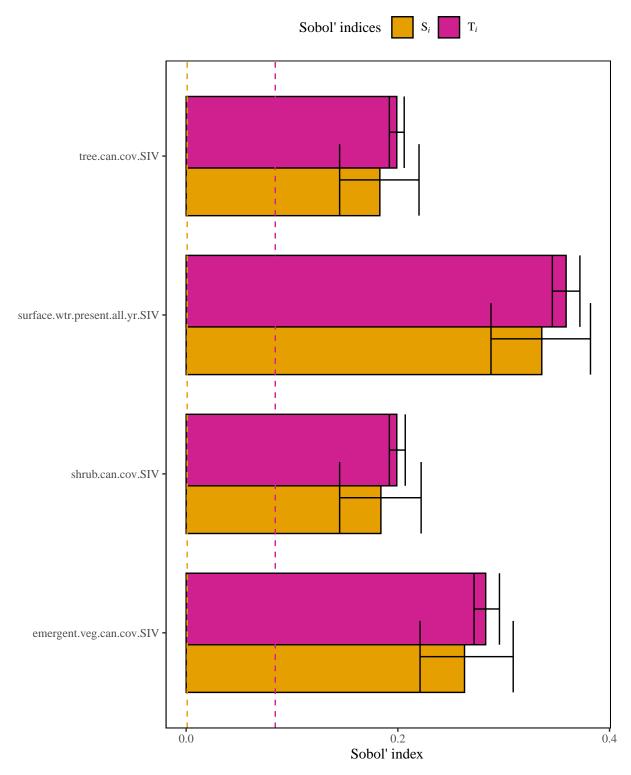
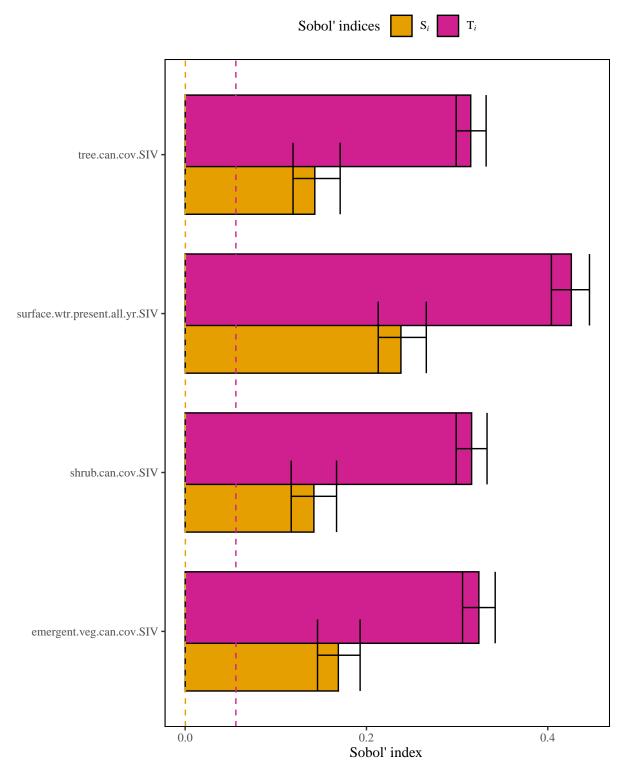


Figure 5. Results of a sensitivity analysis for the minkPaluForestedOrShrubMore405ha model based on a geometric mean structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (i.e., dummy variables).

# Limiting factor model



**Figure 6.** Results of a sensitivity analysis for the minkPaluForestedOrShrubMore405ha model based on a limiting factor structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

# Multiplicative model

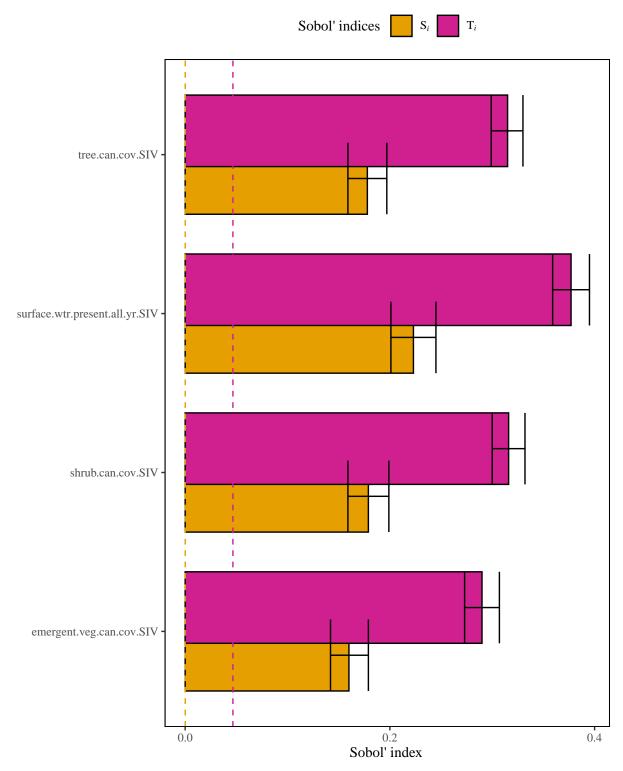


Figure 7. Results of a sensitivity analysis for the minkPaluForestedOrShrubMore405ha model based on a multiplicative mean structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

#### Summary of influential variables

Original model In the original minkPaluForestedOrShrubMore405ha model, 1 of 4 variables are influential and surface.wtr.present.all.yr.SIV has the highest first order sensitivity. In addition, surface.wtr.present.all.yr.SIV has the highest total order sensitivity.

Un-influential variables in original model:

```
tree.can.cov.SIV
shrub.can.cov.SIV
emergent.veg.can.cov.SIV
```

Arithmetic mean model In the arithmetic mean minkPaluForestedOrShrubMore405ha model, 4 of 4 variables are influential and surface.wtr.present.all.yr.SIV has the highest first order sensitivity. In addition, surface.wtr.present.all.yr.SIV has the highest total order sensitivity.

Un-influential variables in arithmetic mean model:

None

Geometric mean model In the geometric mean minkPaluForestedOrShrubMore405ha model, 4 of 4 variables are influential and surface.wtr.present.all.yr.SIV has the highest first order sensitivity. In addition, surface.wtr.present.all.yr.SIV has the highest total order sensitivity.

Un-influential variables in geometric mean model:

None

Limiting factor model In the limiting factor minkPaluForestedOrShrubMore405ha model, 4 of 4 variables are influential and surface.wtr.present.all.yr.SIV has the highest first order sensitivity. In addition, surface.wtr.present.all.yr.SIV has the highest total order sensitivity.

Un-influential variables in limiting factor mean model:

None

Multiplicative model In the multiplicative mean minkPaluForestedOrShrubMore405ha model, 4 of 4 variables are influential and surface.wtr.present.all.yr.SIV has the highest first order sensitivity. In addition, surface.wtr.present.all.yr.SIV has the highest total order sensitivity.

Un-influential variables in multiplicative model:

None

#### References

- 1. Allen, AW. 1986. Habitat suitability index models: mink, revised. U.S. Fish Wildl. Serv. Biol. Rep. 82(10.127). 23 pp. [First printed as: FWS/OBS-82/10.61, October 1983.]
- 2. McKay S, D Hernandez-Abrams, and K Cushway. 2024. ecorest: conducts analyses informing ecosystem restoration decisions. R package version 2.0.0, https://CRAN.R-project.org/package=ecorest.
- 3. Puy, A, S Lo Piano, A Saltelli, and SA Levin. 2022. sensobol: an R package to compute variance based sensitivity indices. Journal of Statistical Software 102(5):1-37. doi: 10.18637/jss.v102.i05