browntroutCompLtoe10C model summary

Contents

Overview

This document summarizes the results of a global sensitivity and uncertainty analysis for the **browntrout-CompLtoe10C** habitat suitability index (HSI) model for *Salmo trutta*. Metadata for the model is stored in the ecorest package in R.

The original documentation for this model can be found here[1].

Sub-model: **Compensatory limiting factor model for riverine or lacustrine habitats with temperatures less than or equal to 10 degrees Celsius**
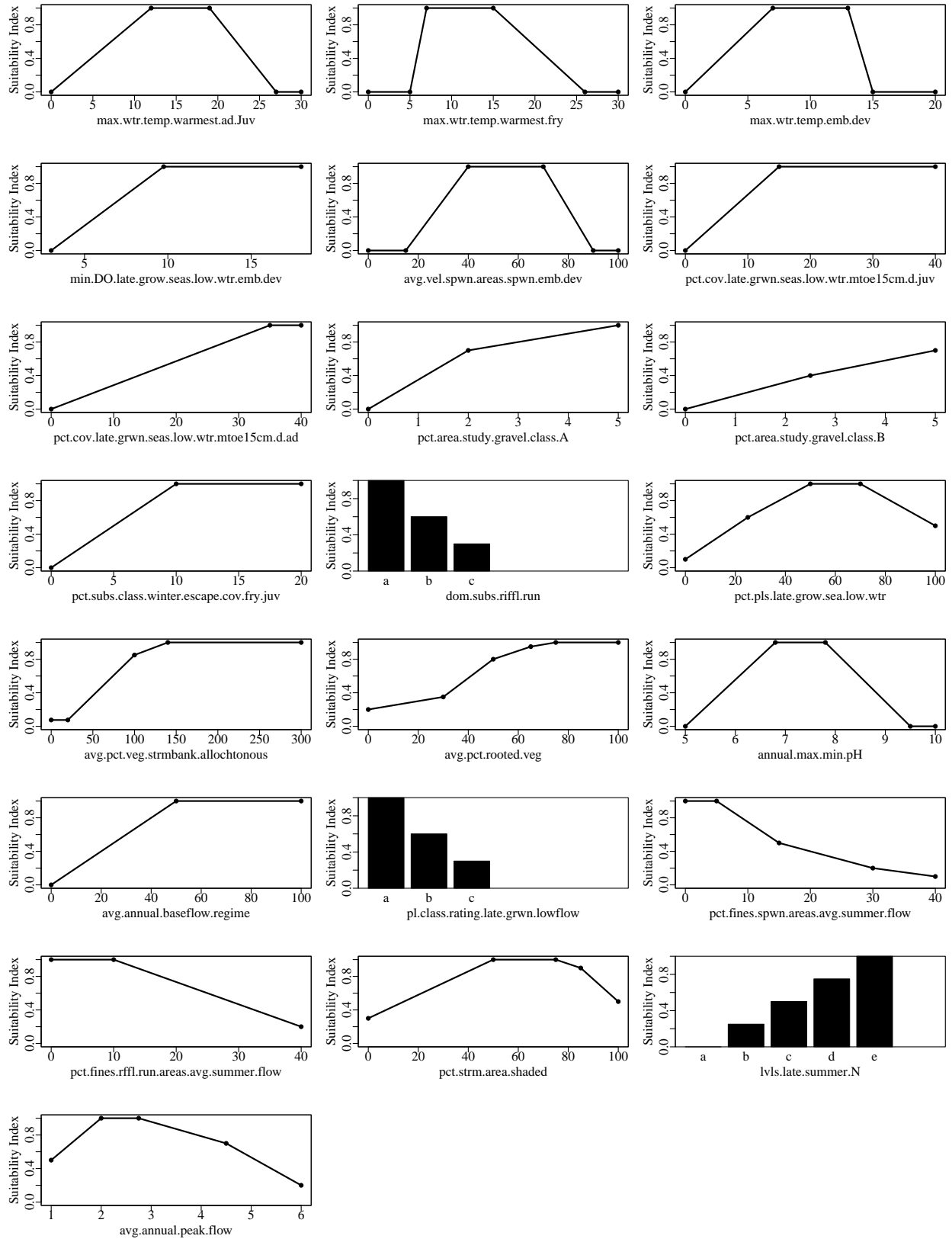
The browntroutCompLtoe10C model is comprised of **22** variables and **5** components.

Variables:

Table 1. SIV variables included in the browntroutCompLtoe10C model. Type indicates whether a variable is numeric or categorical and breakpoints indicates the number of distinct breakpoints in suitability graphs.

	Variable name	Type	Breakpoints
SIV1	max.wtr.temp.warmest.ad.Juv.SIV	numeric	5
SIV1B	max.wtr.temp.warmest.fry.SIV	numeric	6
SIV2	max.wtr.temp.emb.dev.SIV	numeric	5
SIV3	min.DO.late.grow.seas.low.wtr.emb.dev.SIV	numeric	3
SIV4	avg.vel.spwn.areas.spwn.emb.dev.SIV	numeric	6
SIV5	pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.juv.SIV	numeric	3
SIV5B	pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.ad.SIV	numeric	3
SIV6	pct.area.study.gravel.class.A.SIV	numeric	3
SIV6B	pct.area.study.gravel.class.B.SIV	numeric	3
SIV7	pct.subs.class.winter.escape.cov.fry.juv.SIV	numeric	3
SIV8	dom.subs.riffl.run.SIV	categorical	3
SIV9	pct.pls.late.grow.sea.low.wtr.SIV	numeric	5
SIV10	avg.pct.veg.strmbank.allochtonous.SIV	numeric	5
SIV11	avg.pct.rooted.veg.SIV	numeric	6
SIV12	annual.max.min.pH.SIV	numeric	5
SIV13	avg.annual.baseflow.regime.SIV	numeric	3
SIV14	pl.class.rating.late.grwn.lowflow.SIV	categorical	3
SIV15	pct.fines.spwn.areas.avg.summer.flow.SIV	numeric	5
SIV15B	pct.fines.rffl.run.areas.avg.summer.flow.SIV	numeric	3
SIV16	pct.strm.area.shaded.SIV	numeric	5
SIV17	lvls.late.summer.N.SIV	categorical	5
SIV18	avg.annual.peak.flow.SIV	numeric	5

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[1]https://ecolibrary.sec.usace.army.mil/resource/f99ca1c7-b4ac-4cf7-f07d-2f17290376fa

Figure 1. Suitability index graphs for variables included in the browntroutCompLtoe10C model in ecorest.

Components:

Table 2. Components included in the browntroutCompLtoe10C model in ecorest.

	Component	Equation
COT	Other component	min(SIV1,SIV1B,SIV3,SIV12,SIV13,SIV8,SIV10,SIV15B,SIV11,SIV16,SIV17,SIV18,na.rm=T)
CE	Embryo component	ifelse(SIV4<=0.3|((SIV6+SIV6B)/2)<=0.3|SIV15<=0.3,min(SIV2,SIV3,SIV4,((SIV6+SIV6B)/2),SIV15),ifelse(SIV4==((SIV6+SIV6B)/2) & SIV4==SIV15,min(SIV2,SIV3,((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),((SIV4+((SIV6+SIV6B)/2)+SIV15)/3)),ifelse(SIV4==((SIV6+SIV6B)/2) & SIV4<SIV15,min(SIV2,SIV3,((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),SIV15),ifelse(SIV4==SIV15 & SIV4<((SIV6+SIV6B)/2),min(SIV2,SIV3,((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),((SIV6+SIV6B)/2),((SIV4+((SIV6+SIV6B)/2)+SIV15)/3)),ifelse(((SIV6+SIV6B)/2)==SIV15 & ((SIV6+SIV6B)/2)<SIV4,min(SIV2,SIV3,SIV4,((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),((SIV4+((SIV6+SIV6B)/2)+SIV15)/3)),ifelse(min(SIV4,((SIV6+SIV6B)/2),SIV15)==SIV4,min(SIV2,SIV3,((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),((SIV6+SIV6B)/2),SIV15),ifelse(min(SIV4,((SIV6+SIV6B)/2),SIV15)==((SIV6+SIV6B)/2),min(SIV2,SIV3,SIV4,((SIV4+((SIV6+SIV6B)/2)+SIV15)/3),SIV15),min(SIV2,SIV3,SIV4,((SIV6+SIV6B)/2),((SIV4+((SIV6+SIV6B)/2)+SIV15)/3)))))))))
CJ	Juvenile component	ifelse(SIV9<=0.3|SIV14<=0.3,min(SIV5,SIV9,SIV14),ifelse(SIV9==SIV14,min(SIV5,((SIV14+SIV9)/2),((SIV14+SIV9)/2)),ifelse(SIV9<=SIV14,min(SIV5,((SIV14+SIV9)/2),SIV14),min(SIV5,SIV9,((SIV14+SIV9)/2)))))
CFr	Fry component	min(SIV7,SIV9,SIV15B)
CA	Adult component	ifelse(SIV9<=0.3|SIV14<=0.3,min(SIV5B,SIV9,SIV14),ifelse(SIV9==SIV14,min(SIV5B,((SIV14+SIV9)/2),((SIV14+SIV9)/2)),ifelse(SIV9<=SIV14,min(SIV5B,((SIV14+SIV9)/2),SIV14),min(SIV5B,SIV9,((SIV14+SIV9)/2)))))

Model equation:

The equation to calculate an overall HSI index for the browntroutCompLtoe10C model is:

min(CA,CJ,CFr,CE,COT)

According to our classification, this model's format is: **author-specified**

Global sensitivity and uncertainty analysis:

We ran global sensitivity and uncertainty analyses on the browntroutCompLtoe10C model using the sensobol package in R (Puy et al. 2022). The following parameters were used for the sensobol analysis:

Table 3. Parameters and settings used for sensobol sensitivity and uncertainty analyses.

Parameter	Equation	Value
Number of input variables (M)	-	22
Base sample size (n)	-	10000
Number of model evaluations (N)	n*(M+2)	240000
First order estimator	See Puy et al. (2022)	Saltelli
Total order estimator	See Puy et al. (2022)	Jansen
Number of bootstrap replications	-	1000
Sampling scheme	-	Quasi-random
Matrices	-	A, B, AB

We ran a sensitivity and uncertainty analysis for the browntroutCompLtoe10C model using the original equation outlined in the documentation from Raleigh et al. (1986) and using arithmetic mean, geometric mean, limiting factor, and multiplicative equations to contrast the results across different equation structures.

Model uncertainty

We ran the browntroutCompLtoe10C model using 240000 combinations of its SIV variables, which were sampled from a uniform distribution spanning the range of possible values listed in the browntroutCompLtoe10C documentation. We limited the range of possible values for each parameter to the range in which the SIV values were greater than zero to prevent HSI score distributions with primarily zero values.
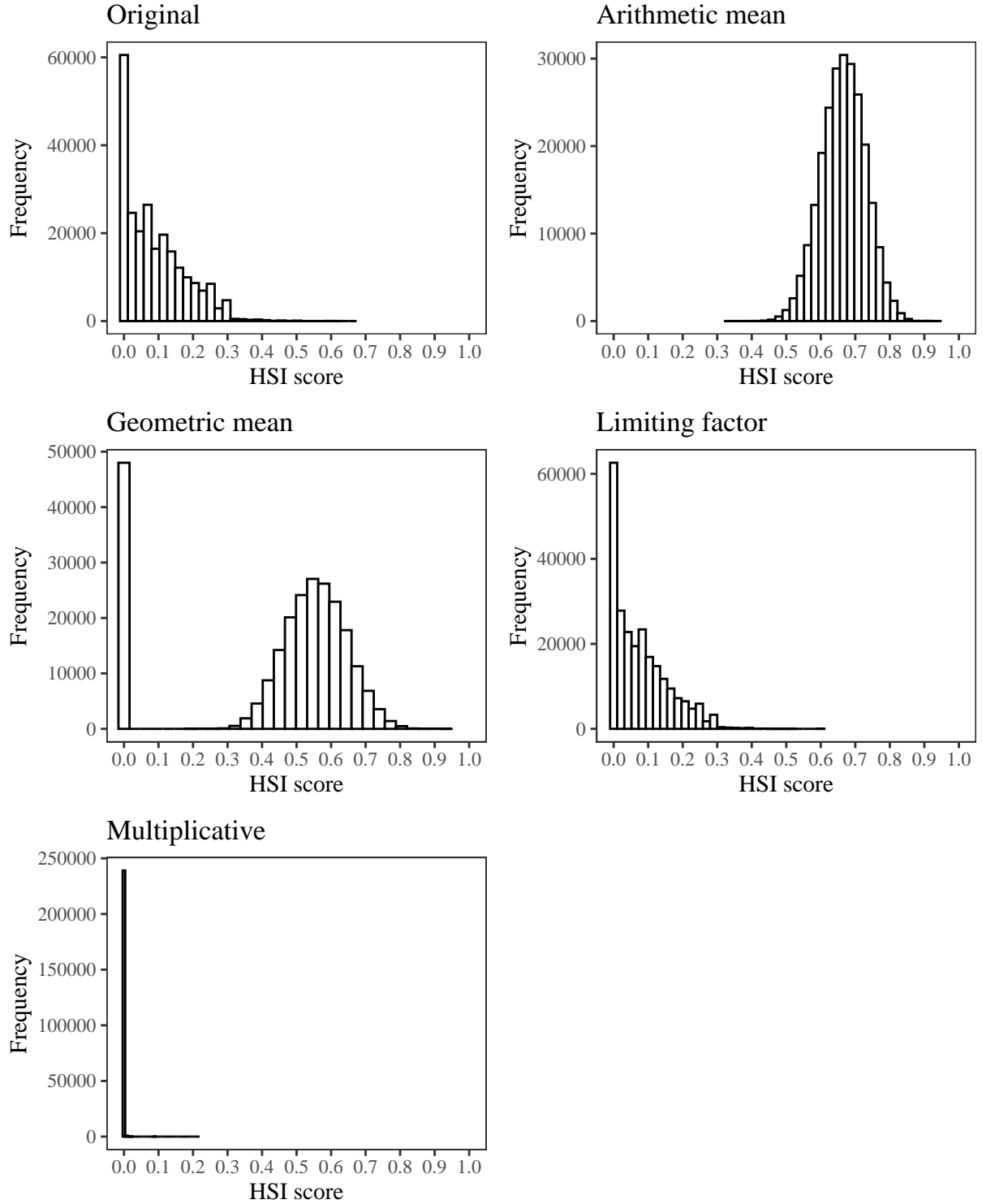
Figure 2. Empirical distributions of HSI scores for the browntroutCompLtoe10C model using the original author-specified model equation from Raleigh et al. (1986), and an arithmetic mean, geometric mean, limiting factor, and multiplicative structure incorporating all SIV variables. Note differences in the y axis.

We assumed a uniform distribution for all parameters because we evaluated all ecorest models in batch. Should you decide to run your own sensitivity analysis, this assumption should be evaluated independently for each parameter in the model.

Table 4. Quantiles from the empirical distribution of HSI scores for the original browntroutCompLtoe10C model structure, an arithmetic mean equation, a geometric mean equation, a limiting factor equation, and a multiplicative equation structure.

	1%	2.5%	5%	25%	50%	75%	95%	97.5%	99%	100%
Original	0.00	0.00	0.00	0.01	0.07	0.14	0.25	0.29	0.30	0.66
Arithmetic	0.51	0.54	0.56	0.62	0.67	0.71	0.77	0.79	0.81	0.94
Geometric	0.00	0.00	0.00	0.42	0.53	0.60	0.69	0.72	0.75	0.93
Limiting	0.00	0.00	0.00	0.01	0.06	0.12	0.24	0.27	0.30	0.60
Multiplicative	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.22

The empirical distribution of the original browntroutCompLtoe10C model has a coefficient of variation (CV) of **0.962**, while the arithmetic mean model has a CV of **0.096**, the geometric mean model has a CV of **0.53**, the limiting factor model has a CV of **1.007**, and the multiplicative model has a CV of **12.852**. Hence, the **Multiplicative** model is the most uncertain, while the **Arithmetic mean** model is the least uncertain.

Model sensitivity

Below are the results of the global sensitivity analysis for the browntroutCompLtoe10C model using the original equation, an arithmetic mean, a geometric mean, a limiting factor, and a multiplicative model structure. The sensobol package uses variance-based sensitivity metrics, so the model's sensitivity to a given parameter is a measure of how much variance in the HSI score decreases in response to that parameter being fixed (Puy et al. 2022). For each parameter, the observed changes in the variance of the HSI score can be described with a first order sensitivity index (S_i) that accounts for the influence of a single parameter of interest on variance in HSI, or with a total order index (T_i) that accounts for the influence of a single parameter on its own and in combination with all other parameters (*i.e.*, interactions) (Puy et al. 2022). We can compare the 95% confidence intervals for the first and total order indices to a dummy parameter, which represents a parameter that has no influence on the variance in a model's output. While an uninfluential variable should theoretically have an S_i and T_i of zero, small approximation errors can lead variables to have a non-zero influence on a model's output (Puy et al. 2022). If the confidence interval of the S_i and T_i index for a given parameter overlaps the confidence interval of the dummy parameter, we can deduce that the parameter has a negligible effect on variance in HSI scores, both on its own and in combination with all other variables.
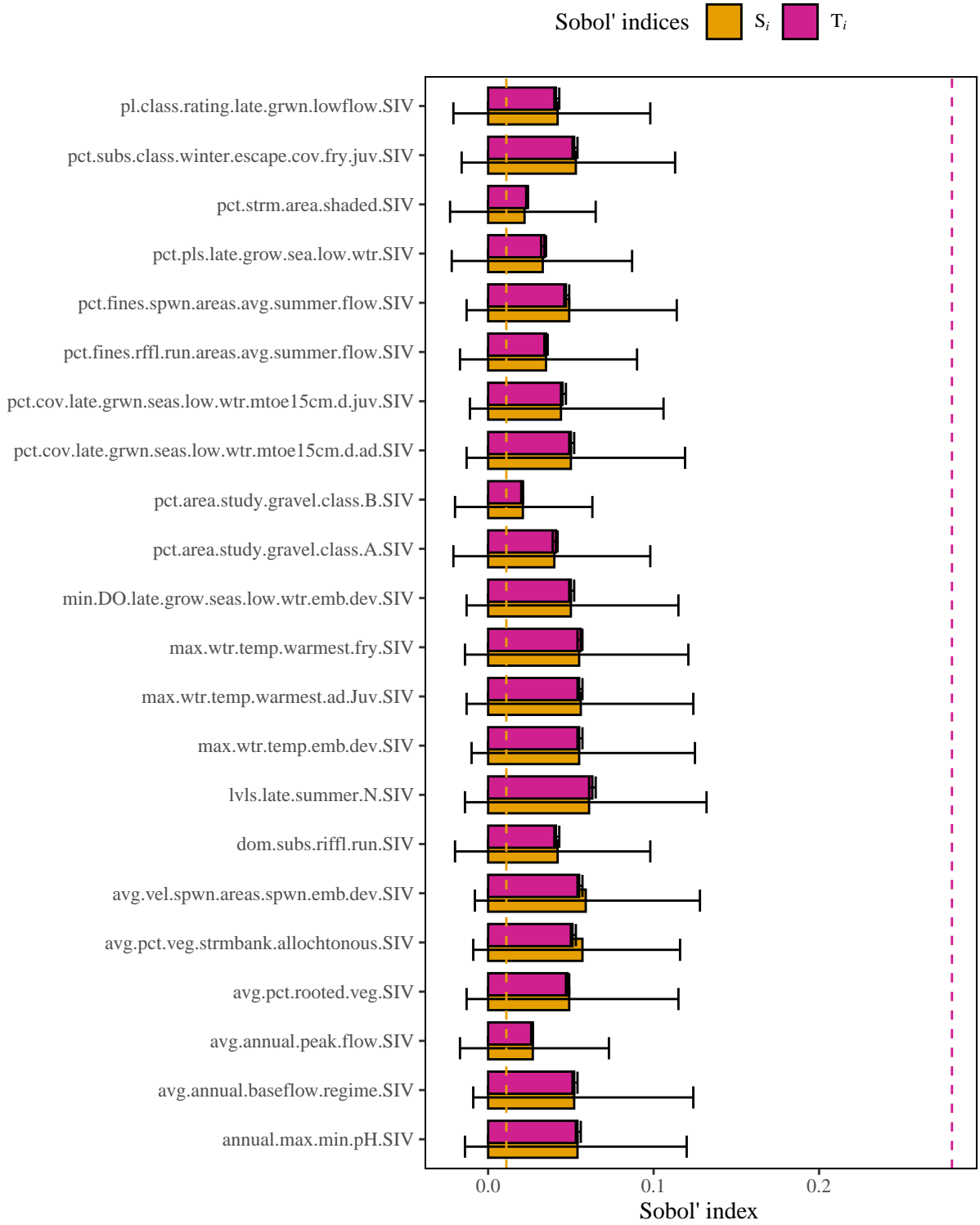
Original model
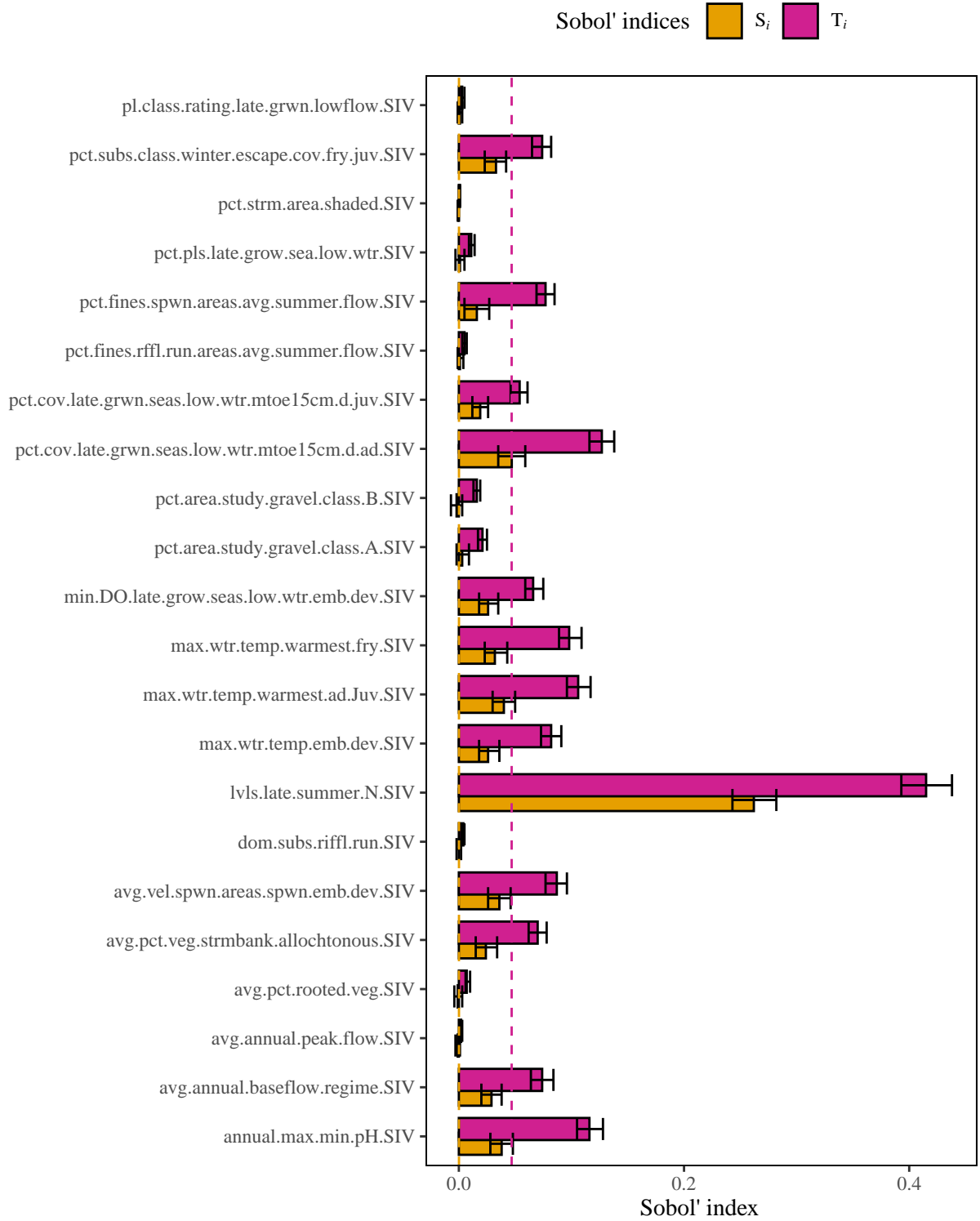
Figure 3. Results of a sensitivity analysis for the browntroutCompLtoe10C model based on the original author-specified model outlined in Raleigh et al. (1986). Dashed lines represent baseline numerical approximation error for S_i and T_i (*i.e.*, dummy variables).

Arithmetic mean model
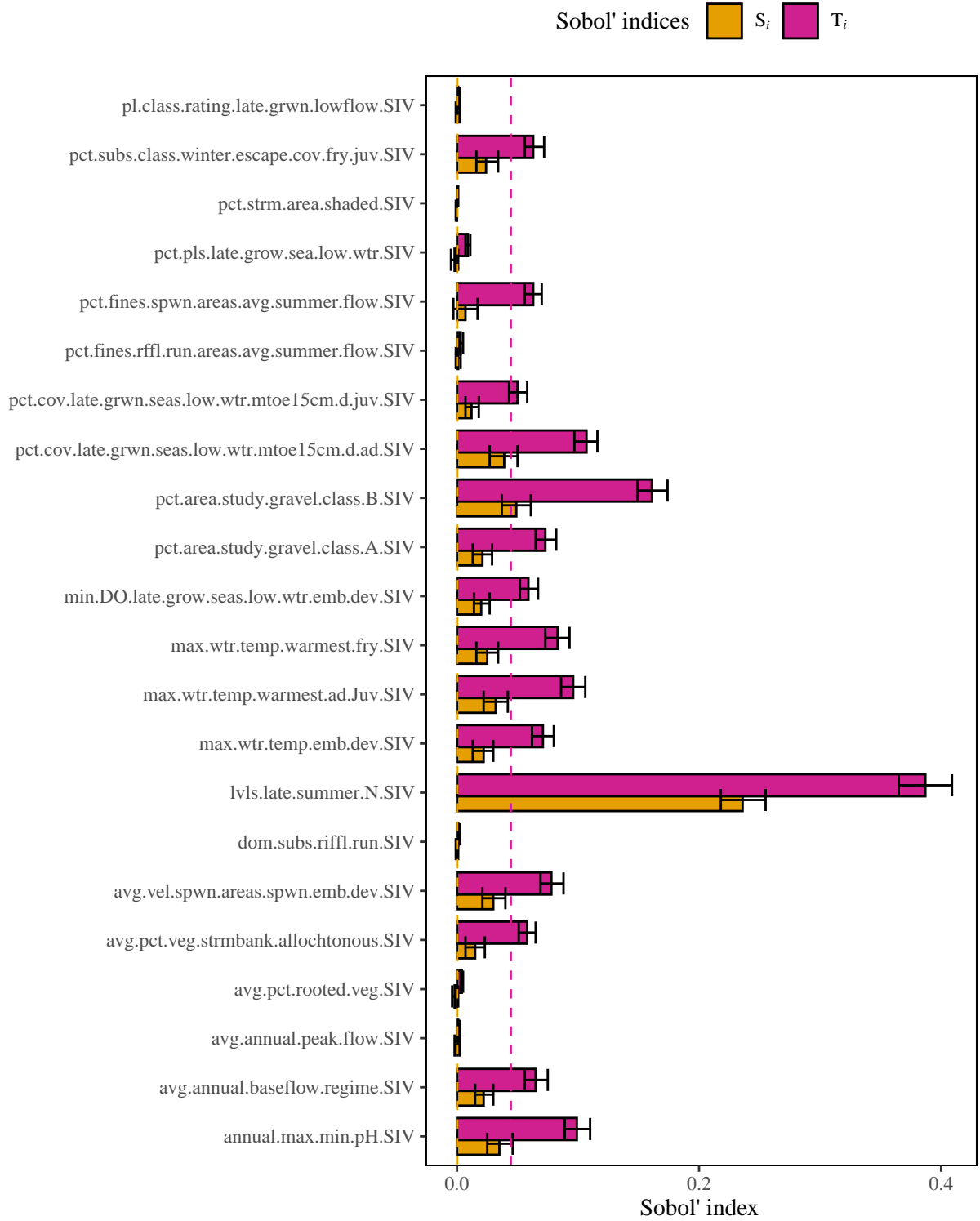

Figure 4. Results of a sensitivity analysis for the browntroutCompLtoe10C model based on an arithmetic mean structure. Dashed lines represent baseline numerical approximation error for S_i and T_i (*i.e.*, dummy variables).

Geometric mean model

Figure 5. Results of a sensitivity analysis for the browntroutCompLtoe10C model based on a geometric mean structure. Dashed lines represent baseline numerical approximation error for S_i and T_i (*i.e.*, dummy variables).

Limiting factor model

Figure 6. Results of a sensitivity analysis for the browntroutCompLtoe10C model based on a limiting factor structure. Dashed lines represent baseline numerical approximation error for S_i and T_i (*i.e.*, dummy variables).
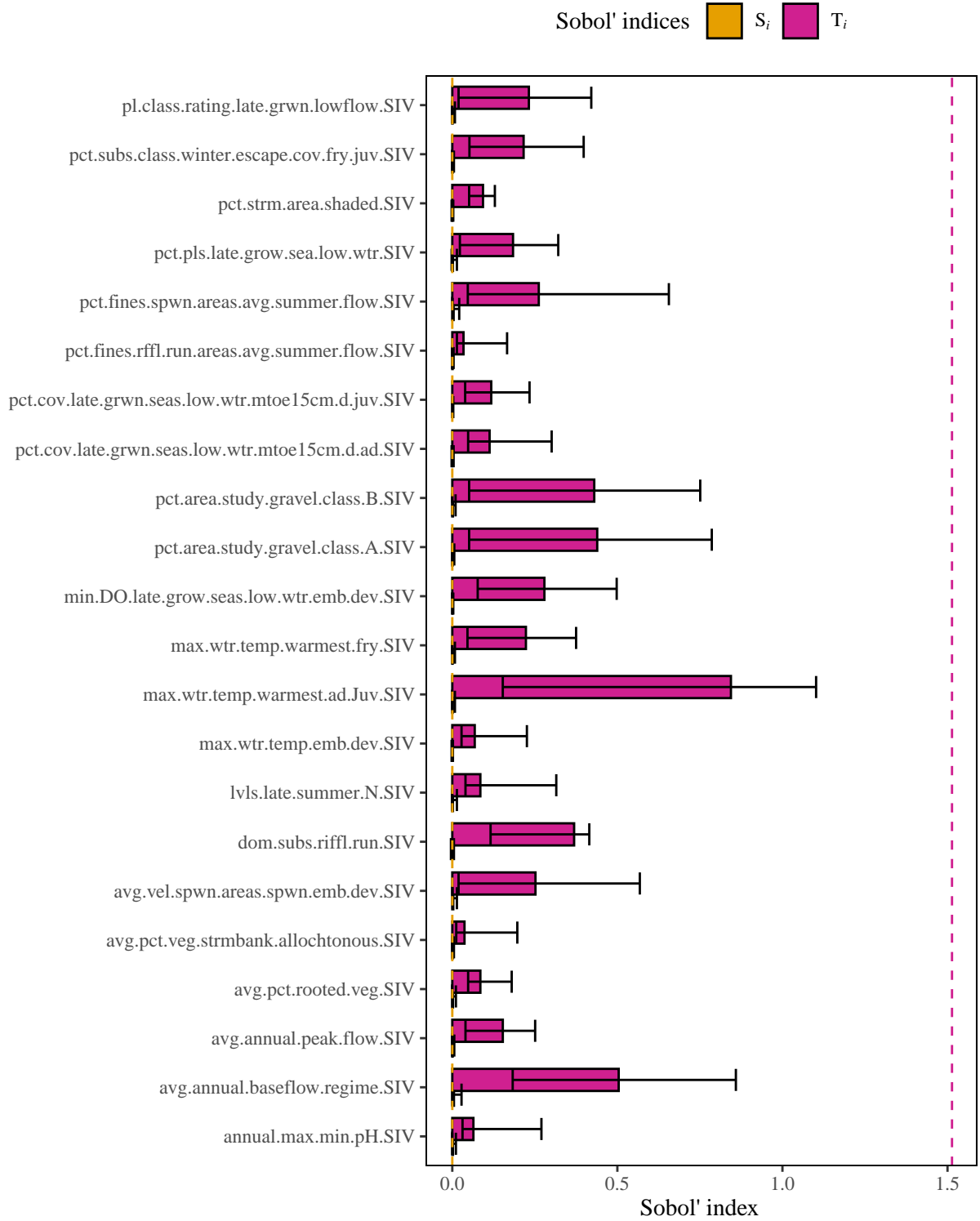
Multiplicative model

Figure 7. Results of a sensitivity analysis for the browntroutCompLtoe10C model based on a multiplicative mean structure. Dashed lines represent baseline numerical approximation error for S_i and T_i (*i.e.*, dummy variables).

Summary of influential variables

Original model   In the **original browntroutCompLtoe10C** model, **13 of 22** variables are influential and **lvls.late.summer.N.SIV** has the highest first order sensitivity. In addition, **lvls.late.summer.N.SIV** has the highest total order sensitivity.

Un-influential variables in original model:

```
pct.area.study.gravel.class.A.SIV
pct.area.study.gravel.class.B.SIV
dom.subs.riffl.run.SIV
pct.pls.late.grow.sea.low.wtr.SIV
avg.pct.rooted.veg.SIV
pl.class.rating.late.grwn.lowflow.SIV
pct.fines.rffl.run.areas.avg.summer.flow.SIV
pct.strm.area.shaded.SIV
avg.annual.peak.flow.SIV
```

Arithmetic mean model   In the **arithmetic mean browntroutCompLtoe10C** model, **0 of 22** variables are influential and **lvls.late.summer.N.SIV** has the highest first order sensitivity. In addition, **lvls.late.summer.N.SIV** has the highest total order sensitivity.

Un-influential variables in arithmetic mean model:

```
max.wtr.temp.warmest.ad.Juv.SIV
max.wtr.temp.warmest.fry.SIV
max.wtr.temp.emb.dev.SIV
min.DO.late.grow.seas.low.wtr.emb.dev.SIV
avg.vel.spwn.areas.spwn.emb.dev.SIV
pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.juv.SIV
pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.ad.SIV
pct.area.study.gravel.class.A.SIV
pct.area.study.gravel.class.B.SIV
pct.subs.class.winter.escape.cov.fry.juv.SIV
dom.subs.riffl.run.SIV
pct.pls.late.grow.sea.low.wtr.SIV
avg.pct.veg.strmbank.allochtonous.SIV
avg.pct.rooted.veg.SIV
annual.max.min.pH.SIV
avg.annual.baseflow.regime.SIV
pl.class.rating.late.grwn.lowflow.SIV
pct.fines.spwn.areas.avg.summer.flow.SIV
pct.fines.rffl.run.areas.avg.summer.flow.SIV
pct.strm.area.shaded.SIV
lvls.late.summer.N.SIV
avg.annual.peak.flow.SIV
```

Geometric mean model   In the **geometric mean browntroutCompLtoe10C** model, **7 of 22** variables are influential and **lvls.late.summer.N.SIV** has the highest first order sensitivity. In addition, **lvls.late.summer.N.SIV** has the highest total order sensitivity.

Un-influential variables in geometric mean model:

```
max.wtr.temp.warmest.fry.SIV
max.wtr.temp.emb.dev.SIV
```

```
min.DO.late.grow.seas.low.wtr.emb.dev.SIV
pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.juv.SIV
pct.area.study.gravel.class.A.SIV
pct.subs.class.winter.escape.cov.fry.juv.SIV
dom.subs.riffl.run.SIV
pct.pls.late.grow.sea.low.wtr.SIV
avg.pct.rooted.veg.SIV
avg.annual.baseflow.regime.SIV
pl.class.rating.late.grwn.lowflow.SIV
pct.fines.spwn.areas.avg.summer.flow.SIV
pct.fines.rffl.run.areas.avg.summer.flow.SIV
pct.strm.area.shaded.SIV
avg.annual.peak.flow.SIV
```

Limiting factor model In the **limiting factor browntroutCompLtoe10C** model, **15 of 22** variables are influential and **lvls.late.summer.N.SIV** has the highest first order sensitivity. In addition, **lvls.late.summer.N.SIV** has the highest total order sensitivity.

Un-influential variables in limiting factor mean model:

```
dom.subs.riffl.run.SIV
pct.pls.late.grow.sea.low.wtr.SIV
avg.pct.rooted.veg.SIV
pl.class.rating.late.grwn.lowflow.SIV
pct.fines.rffl.run.areas.avg.summer.flow.SIV
pct.strm.area.shaded.SIV
avg.annual.peak.flow.SIV
```

Multiplicative model In the **multiplicative mean browntroutCompLtoe10C** model, **2 of 22** variables are influential and **avg.annual.baseflow.regime.SIV** has the highest first order sensitivity. In addition, **max.wtr.temp.warmest.ad.Juv.SIV** has the highest total order sensitivity.

Un-influential variables in multiplicative model:

```
max.wtr.temp.warmest.ad.Juv.SIV
max.wtr.temp.warmest.fry.SIV
max.wtr.temp.emb.dev.SIV
min.DO.late.grow.seas.low.wtr.emb.dev.SIV
pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.juv.SIV
pct.cov.late.grwn.seas.low.wtr.mtoe15cm.d.ad.SIV
pct.area.study.gravel.class.A.SIV
pct.area.study.gravel.class.B.SIV
pct.subs.class.winter.escape.cov.fry.juv.SIV
dom.subs.riffl.run.SIV
pct.pls.late.grow.sea.low.wtr.SIV
avg.pct.veg.strmbank.allochtonous.SIV
avg.pct.rooted.veg.SIV
annual.max.min.pH.SIV
avg.annual.baseflow.regime.SIV
pl.class.rating.late.grwn.lowflow.SIV
pct.fines.rffl.run.areas.avg.summer.flow.SIV
pct.strm.area.shaded.SIV
lvls.late.summer.N.SIV
avg.annual.peak.flow.SIV
```

References

1. McKay S, D Hernandez-Abrams, and K Cushway. 2024. ecorest: conducts analyses informing ecosystem restoration decisions. R package version 2.0.0, https://CRAN.R-project.org/package=ecorest.
2. Puy, A, S Lo Piano, A Saltelli, and SA Levin. 2022. sensobol: an R package to compute variance based sensitivity indices. Journal of Statistical Software 102(5):1-37. doi: 10.18637/jss.v102.i05
3. Raleigh, RF, LD Zuckerman, and PC Nelson. 1986. Habitat suitability index models and instream flow suitability curves: Brown trout, revised. US Fish and Wildlife Service. 82(10.124) 65 pp