

# chinooksalmonLimit5to10CSilt model summary

## Contents

<b>Overview</b> . . . . .	2
<b>Variables:</b> . . . . .	2
<b>Components:</b> . . . . .	4
<b>Model equation:</b> . . . . .	4
<b>Global sensitivity and uncertainty analysis:</b> . . . . .	4
<b>Model uncertainty</b> . . . . .	4
<b>Model sensitivity</b> . . . . .	6
Original model . . . . .	7
Arithmetic mean model . . . . .	8
Geometric mean model . . . . .	9
Limiting factor model . . . . .	10
Multiplicative model . . . . .	11
Summary of influential variables . . . . .	12
References . . . . .	13

## Overview

This document summarizes the results of a global sensitivity and uncertainty analysis for the **chinook-salmonLimit5to10CSilt** habitat suitability index (HSI) model for *Oncorhynchus tshawytscha*. Metadata for the model is stored in the `ecorest` package in R.

The original documentation for this model can be found here<sup>1</sup>.

Sub-model: **Riverine limiting factor model for Chinook Salmon habitat with temperatures greater than 5C and less than or equal to 10C during the egg and pre-emergent yolk sac fry period and fines less than or equal to 0.8mm in size (silt)**

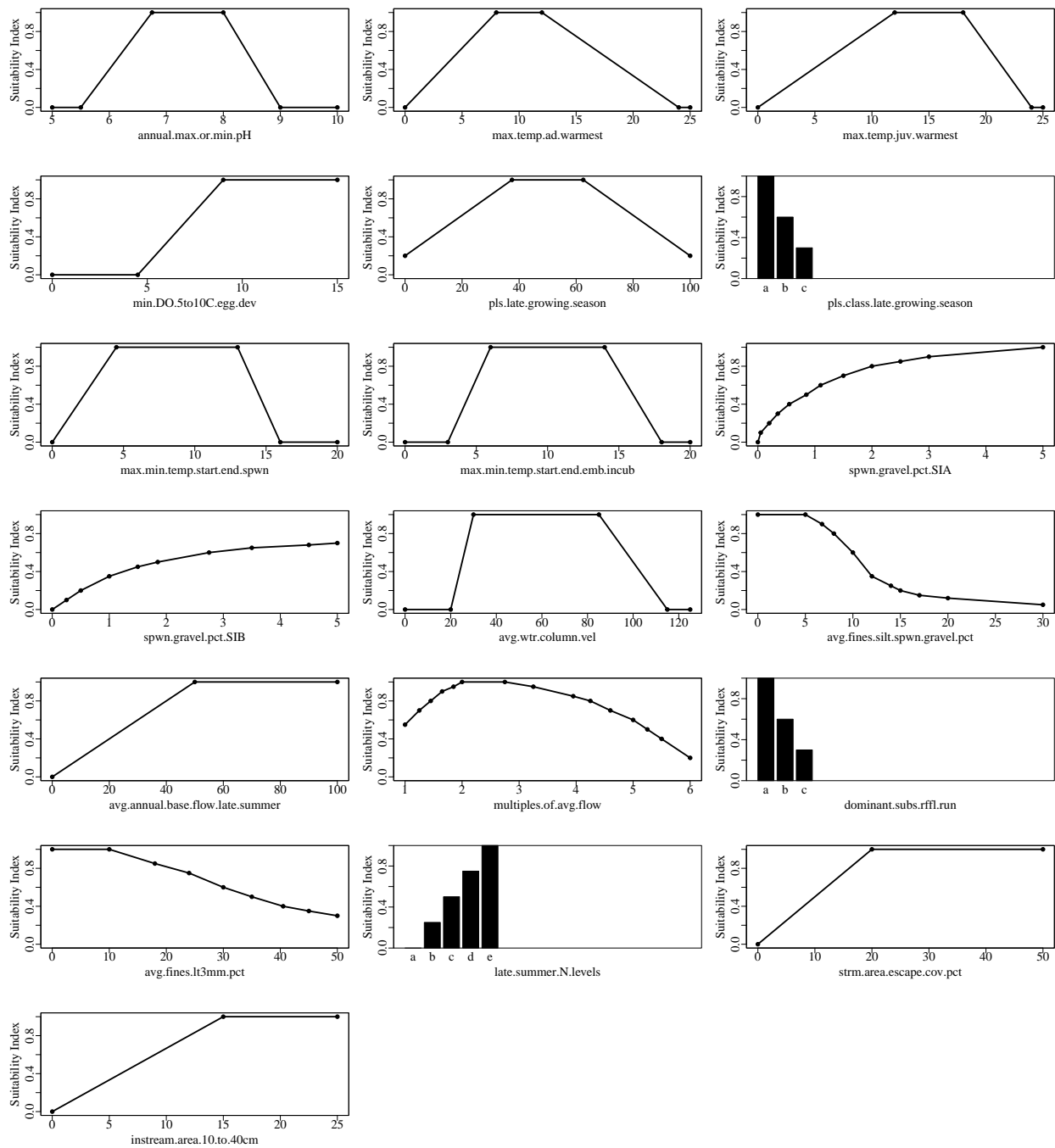
The `chinooksalmonLimit5to10CSilt` model is comprised of **19** variables and **3** components.

## Variables:

**Table 1.** SIV variables included in the `chinooksalmonLimit5to10CSilt` model. Type indicates whether a variable is numeric or categorical and breakpoints indicates the number of distinct breakpoints in suitability graphs.

	Variable name	Type	Breakpoints
SIV1	annual.max.or.min.pH.SIV	numeric	6
SIV2	max.temp.ad.warmest.SIV	numeric	5
SIV2B	max.temp.juv.warmest.SIV	numeric	5
SIV3	min.DO.5to10C.egg.dev.SIV	numeric	4
SIV4	pls.late.growing.season.SIV	numeric	4
SIV5	pls.class.late.growing.season.SIV	categorical	3
SIV6	max.min.temp.start.end.spwn.SIV	numeric	5
SIV7	max.min.temp.start.end.emb.incub.SIV	numeric	6
SIV8	spwn.gravel.pct.SIA.SIV	numeric	12
SIV8B	spwn.gravel.pct.SIB.SIV	numeric	10
SIV9	avg.wtr.column.vel.SIV	numeric	6
SIV10	avg.fines.silt.spwn.gravel.pct.SIV	numeric	11
SIV11	avg.annual.base.flow.late.summer.SIV	numeric	3
SIV12	multiples.of.avg.flow.SIV	numeric	15
SIV13	dominant.subs.rffl.run.SIV	categorical	3
SIV14	avg.fines.lt3mm.pct.SIV	numeric	9
SIV15	late.summer.N.levels.SIV	categorical	5
SIV16	strm.area.escape.cov.pct.SIV	numeric	3
SIV17	instream.area.10.to.40cm.SIV	numeric	3

<sup>1</sup><https://ecolibrary.sec.usace.army.mil/resource/75cc3ca3-1110-4ef6-fa99-142f99a846eb>



**Figure 1.** Suitability index graphs for variables included in the chinooksalmonLimit5to10CSilt model in ecorest.

## Components:

**Table 2.** Components included in the chinooksalmonLimit5to10CSilt model in ecoREST.

	Component	Equation
CE	Embryo component	$\min(\text{SIV3}, \text{SIV6}, \text{SIV7}, (\text{SIV8} + \text{SIV8B})/2, \text{SIV9}, \text{SIV10}, \text{SIV11}, \text{SIV12}, \text{na.rm=T})$
CJ	Juvenile component	$\min(\text{SIV1}, \text{SIV2B}, \text{SIV3}, \text{SIV4}, \text{SIV5}, \text{SIV11}, \text{SIV12}, \text{SIV13}, \text{SIV14}, \text{SIV15}, \text{SIV16}, \text{SIV17}, \text{na.rm=T})$
CA	Adult component	$\min(\text{SIV1}, \text{SIV2}, \text{SIV3}, \text{SIV4}, \text{SIV5})$

## Model equation:

The equation to calculate an overall HSI index for the chinooksalmonLimit5to10CSilt model is:

$$\min(\text{CA}, \text{CE}, \text{CJ})$$

According to our classification, this model's format is: **limiting factor**

## Global sensitivity and uncertainty analysis:

We ran global sensitivity and uncertainty analyses on the chinooksalmonLimit5to10CSilt model using the sensobol package in R (Puy et al. 2022). The following parameters were used for the sensobol analysis:

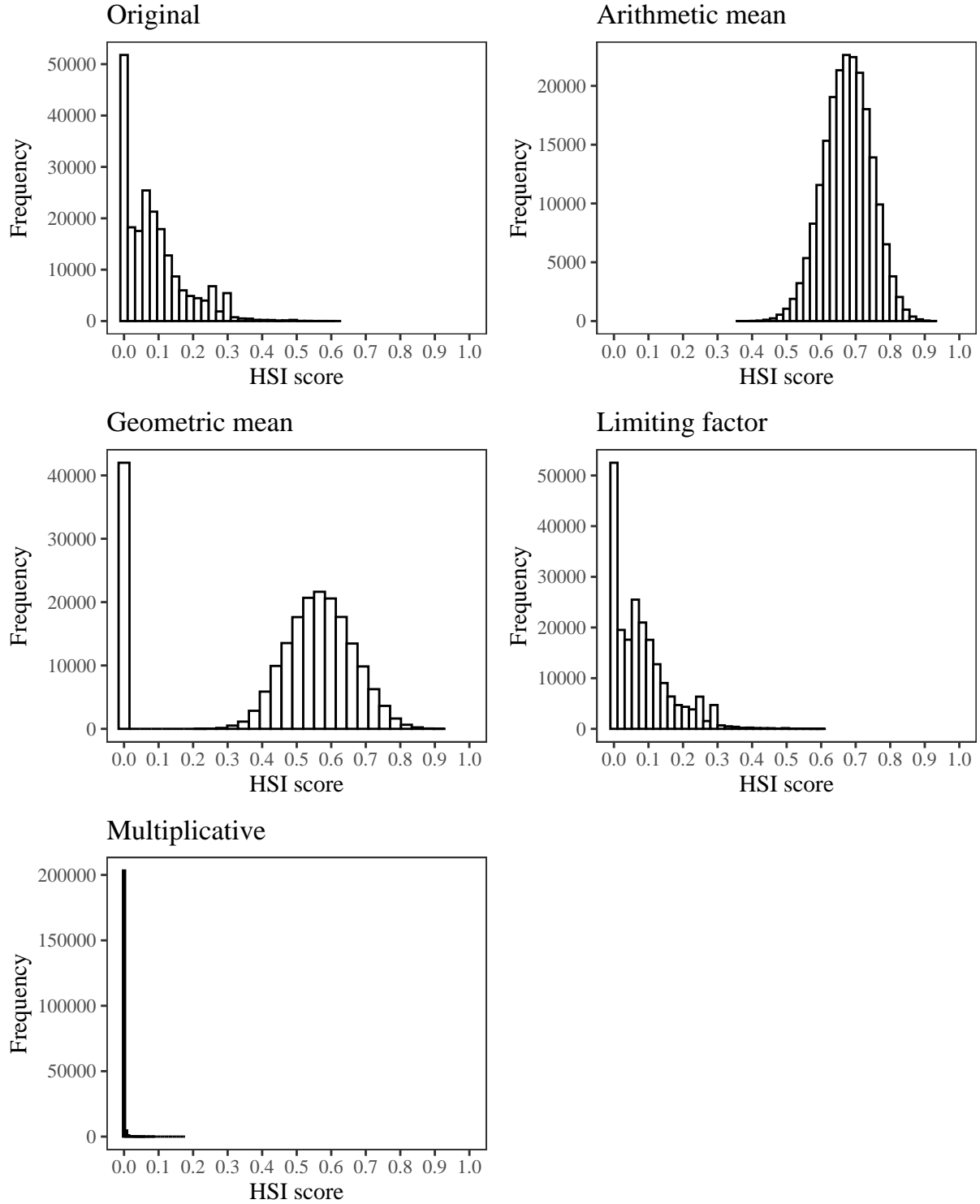
**Table 3.** Parameters and settings used for sensobol sensitivity and uncertainty analyses.

Parameter	Equation	Value
Number of input variables (M)	-	19
Base sample size (n)	-	10000
Number of model evaluations (N)	$n \cdot (M+2)$	210000
First order estimator	See Puy et al. (2022)	Saltelli
Total order estimator	See Puy et al. (2022)	Jansen
Number of bootstrap replications	-	1000
Sampling scheme	-	Quasi-random
Matrices	-	A, B, AB

We ran a sensitivity and uncertainty analysis for the chinooksalmonLimit5to10CSilt model using the original equation outlined in the documentation from Raleigh et al. (1986) and using arithmetic mean, geometric mean, limiting factor, and multiplicative equations to contrast the results across different equation structures.

## Model uncertainty

We ran the chinooksalmonLimit5to10CSilt model using 210000 combinations of its SIV variables, which were sampled from a uniform distribution spanning the range of possible values listed in the chinooksalmonLimit5to10CSilt documentation. We limited the range of possible values for each parameter to the range in which the SIV values were greater than zero to prevent HSI score distributions with primarily zero values.



**Figure 2.** Empirical distributions of HSI scores for the chinooksalmonLimit5to10CSilt model using the original limiting factor model equation from Raleigh et al. (1986), and an arithmetic mean, geometric mean, limiting factor, and multiplicative structure incorporating all SIV variables. Note differences in the y axis.

We assumed a uniform distribution for all parameters because we evaluated all ecores models in batch. Should you decide to run your own sensitivity analysis, this assumption should be evaluated independently for each parameter in the model.

**Table 4.** Quantiles from the empirical distribution of HSI scores for the original chinook-salmonLimit5to10CSilt model structure, an arithmetic mean equation, a geometric mean equation, a limiting factor equation, and a multiplicative equation structure.

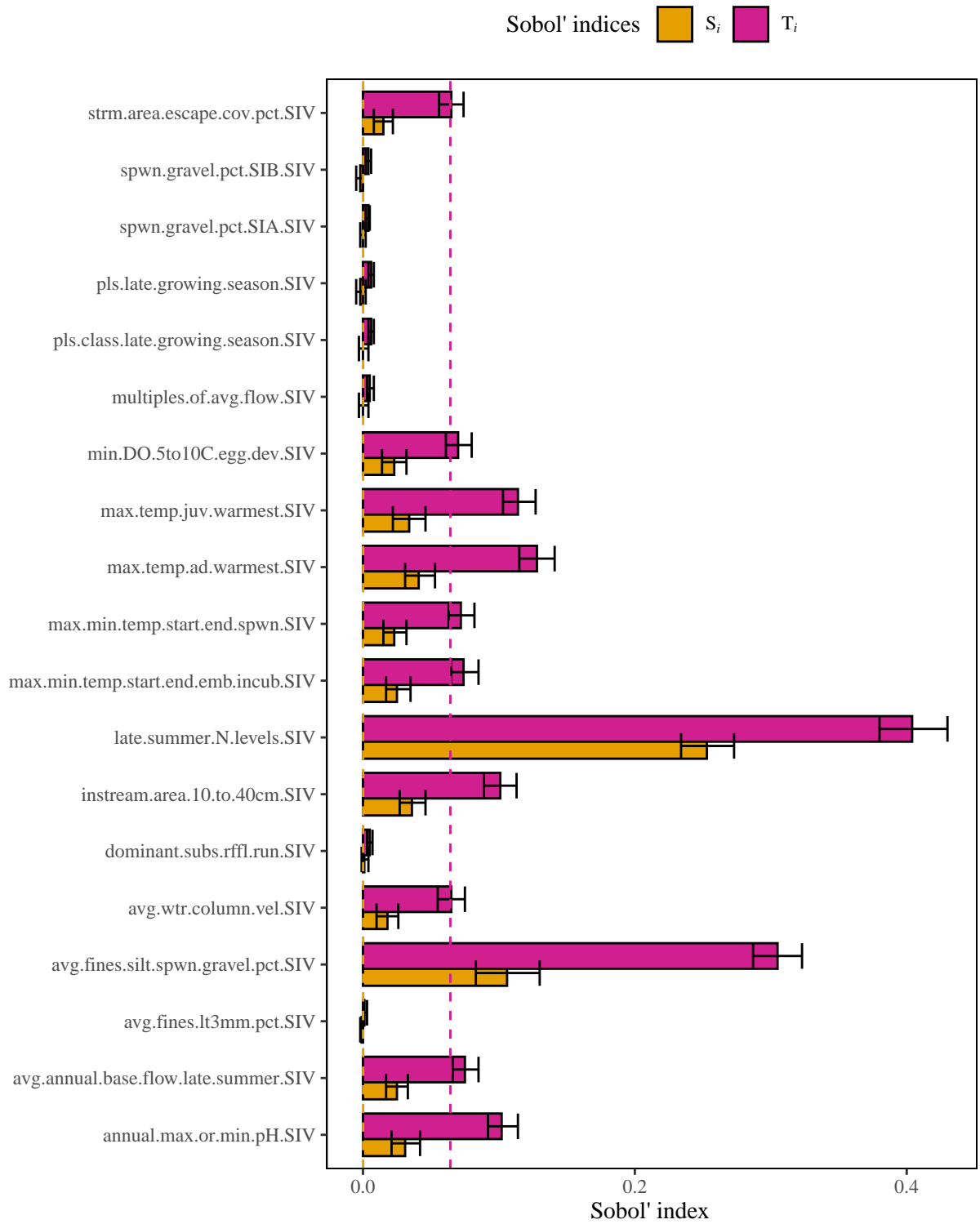
	1%	2.5%	5%	25%	50%	75%	95%	97.5%	99%	100%
Original	0.00	0.00	0.00	0.01	0.07	0.13	0.26	0.30	0.33	0.62
Arithmetic	0.51	0.54	0.56	0.63	0.68	0.72	0.79	0.81	0.83	0.92
Geometric	0.00	0.00	0.00	0.42	0.54	0.61	0.72	0.75	0.78	0.91
Limiting	0.00	0.00	0.00	0.01	0.06	0.12	0.25	0.30	0.32	0.60
Multiplicative	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.17

The empirical distribution of the original chinooksalmonLimit5to10CSilt model has a coefficient of variation (CV) of **1.002**, while the arithmetic mean model has a CV of **0.102**, the geometric mean model has a CV of **0.533**, the limiting factor model has a CV of **1.011**, and the multiplicative model has a CV of **6.077**. Hence, the **Multiplicative** model is the most uncertain, while the **Arithmetic mean** model is the least uncertain.

### Model sensitivity

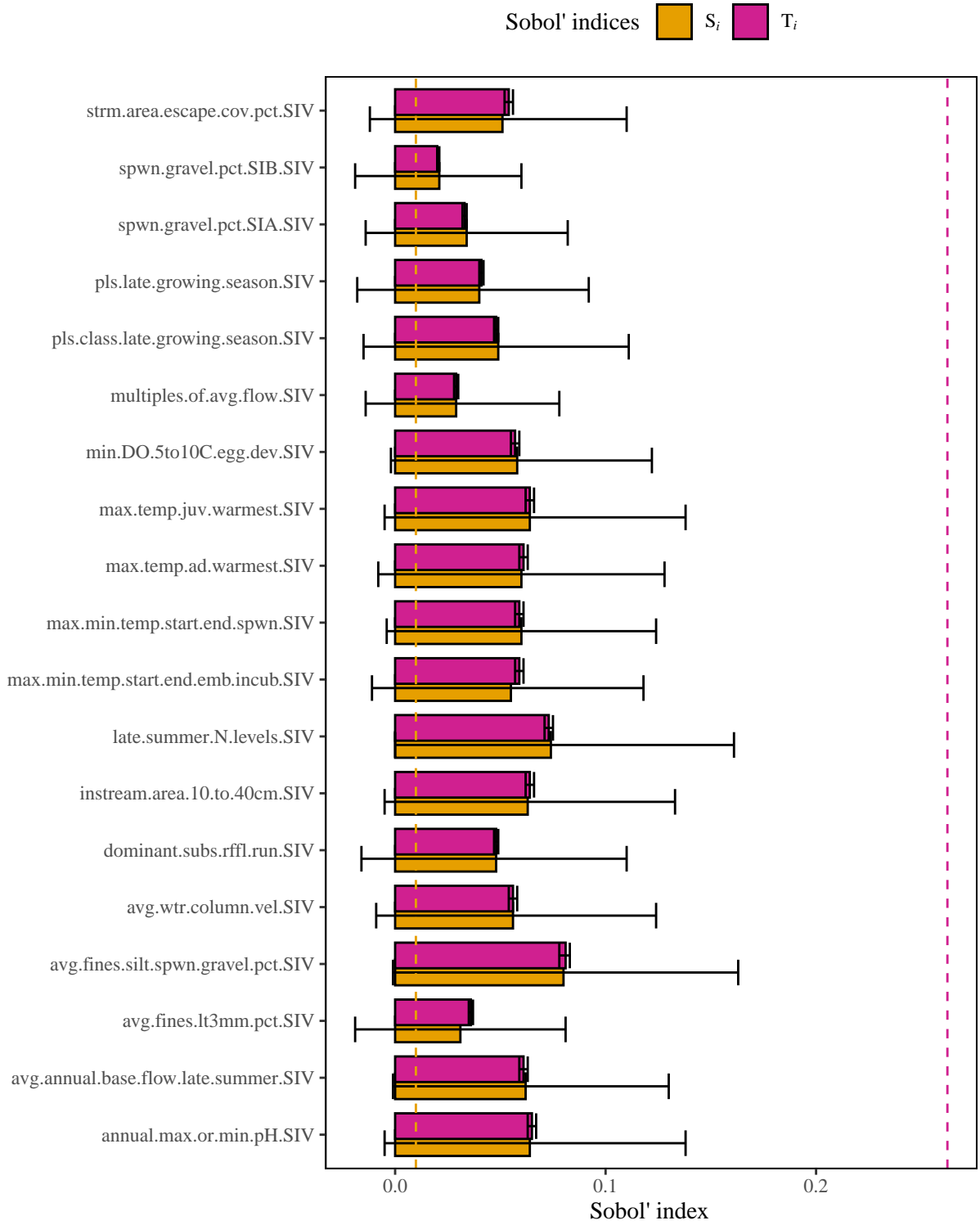
Below are the results of the global sensitivity analysis for the chinooksalmonLimit5to10CSilt model using the original equation, an arithmetic mean, a geometric mean, a limiting factor, and a multiplicative model structure. The sensobol package uses variance-based sensitivity metrics, so the model’s sensitivity to a given parameter is a measure of how much variance in the HSI score decreases in response to that parameter being fixed (Puy et al. 2022). For each parameter, the observed changes in the variance of the HSI score can be described with a first order sensitivity index ( $S_i$ ) that accounts for the influence of a single parameter of interest on variance in HSI, or with a total order index ( $T_i$ ) that accounts for the influence of a single parameter on its own and in combination with all other parameters (*i.e.*, interactions) (Puy et al. 2022). We can compare the 95% confidence intervals for the first and total order indices to a dummy parameter, which represents a parameter that has no influence on the variance in a model’s output. While an uninfluential variable should theoretically have an  $S_i$  and  $T_i$  of zero, small approximation errors can lead variables to have a non-zero influence on a model’s output (Puy et al. 2022). If the confidence interval of the  $S_i$  and  $T_i$  index for a given parameter overlaps the confidence interval of the dummy parameter, we can deduce that the parameter has a negligible effect on variance in HSI scores, both on its own and in combination with all other variables.

## Original model



**Figure 3.** Results of a sensitivity analysis for the chinooksalmonLimit5to10CSilt model based on the original limiting factor model outlined in Raleigh et al. (1986). Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

## Arithmetic mean model



**Figure 4.** Results of a sensitivity analysis for the chinooksalmonLimit5to10CSilt model based on an arithmetic mean structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

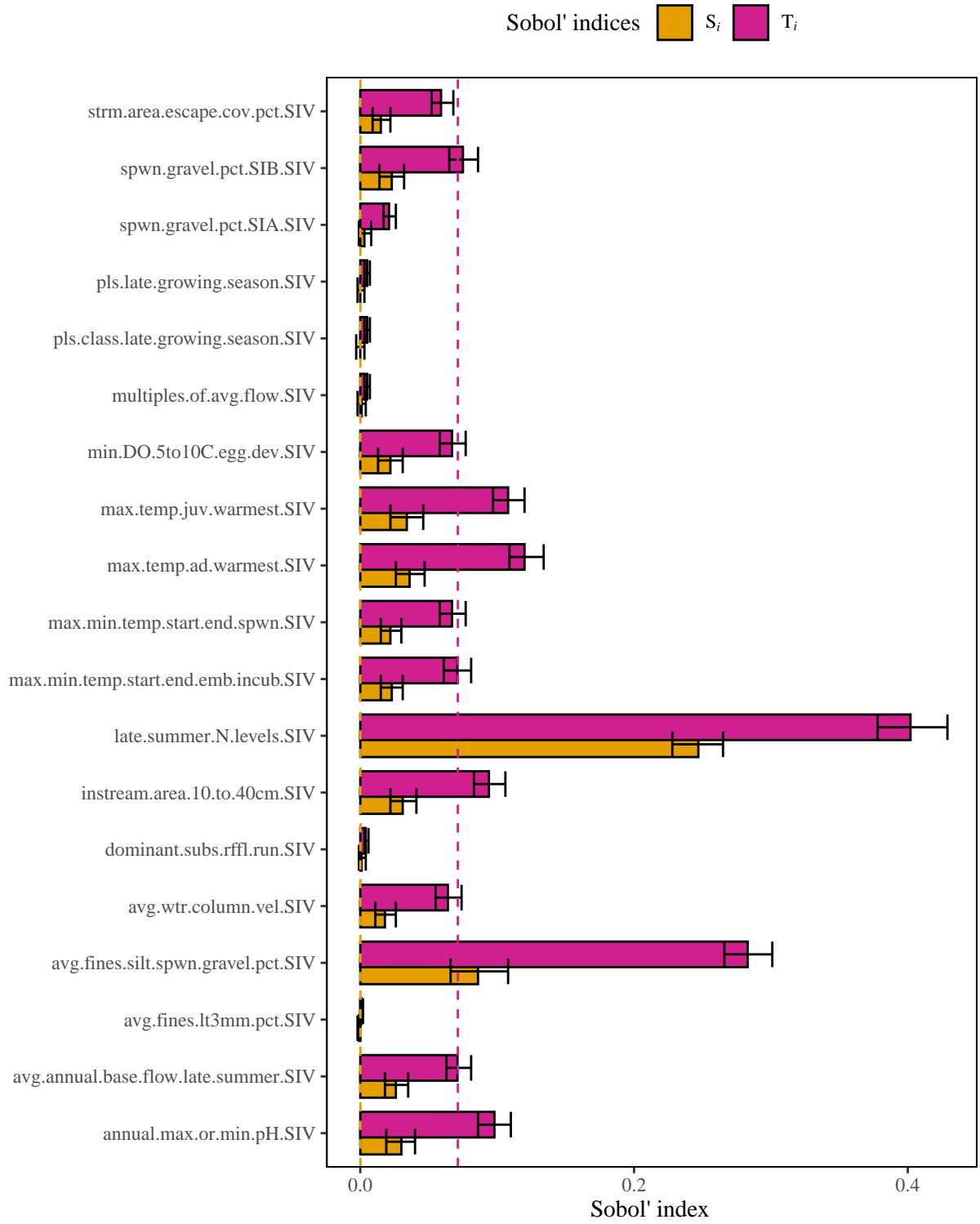


## Geometric mean model



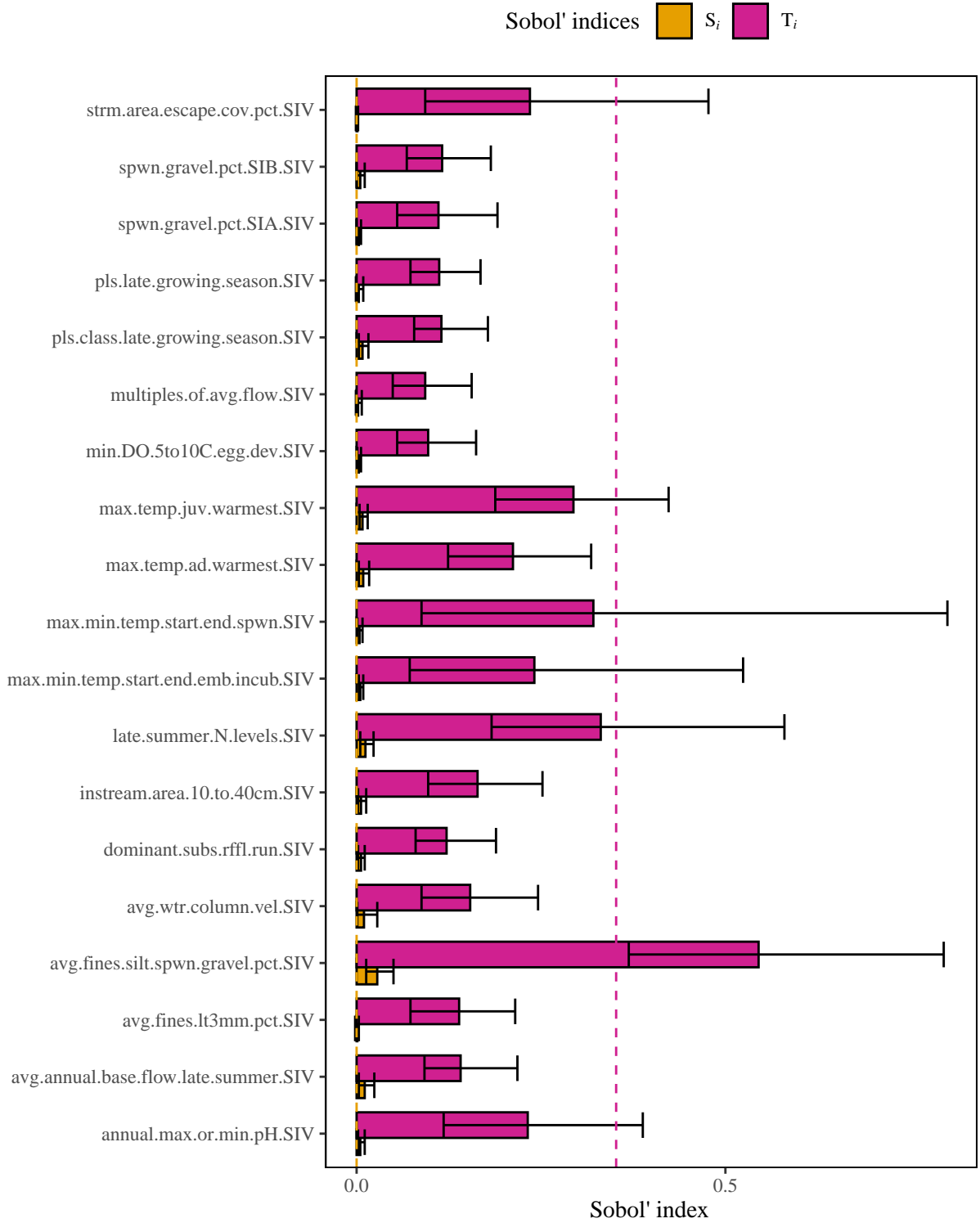
**Figure 5.** Results of a sensitivity analysis for the chinooksalmonLimit5to10CSilt model based on a geometric mean structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

## Limiting factor model



**Figure 6.** Results of a sensitivity analysis for the chinooksalmonLimit5to10CSilt model based on a limiting factor structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

## Multiplicative model



**Figure 7.** Results of a sensitivity analysis for the chinooksalmonLimit5to10CSilt model based on a multiplicative mean structure. Dashed lines represent baseline numerical approximation error for  $S_i$  and  $T_i$  (*i.e.*, dummy variables).

## Summary of influential variables

**Original model** In the **original chinooksalmonLimit5to10CSilt** model, **12 of 19** variables are influential and **late.summer.N.levels.SIV** has the highest first order sensitivity. In addition, **late.summer.N.levels.SIV** has the highest total order sensitivity.

### Un-influential variables in original model:

pls.late.growing.season.SIV  
pls.class.late.growing.season.SIV  
spwn.gravel.pct.SIA.SIV  
spwn.gravel.pct.SIB.SIV  
multiples.of.avg.flow.SIV  
dominant.subs.rffl.run.SIV  
avg.fines.lt3mm.pct.SIV

**Arithmetic mean model** In the **arithmetic mean chinooksalmonLimit5to10CSilt** model, **0 of 19** variables are influential and **avg.fines.silt.spwn.gravel.pct.SIV** has the highest first order sensitivity. In addition, **avg.fines.silt.spwn.gravel.pct.SIV** has the highest total order sensitivity.

### Un-influential variables in arithmetic mean model:

annual.max.or.min.pH.SIV  
max.temp.ad.warmest.SIV  
max.temp.juv.warmest.SIV  
min.DO.5to10C.egg.dev.SIV  
pls.late.growing.season.SIV  
pls.class.late.growing.season.SIV  
max.min.temp.start.end.spwn.SIV  
max.min.temp.start.end.emb.incub.SIV  
spwn.gravel.pct.SIA.SIV  
spwn.gravel.pct.SIB.SIV  
avg.wtr.column.vel.SIV  
avg.fines.silt.spwn.gravel.pct.SIV  
avg.annual.base.flow.late.summer.SIV  
multiples.of.avg.flow.SIV  
dominant.subs.rffl.run.SIV  
avg.fines.lt3mm.pct.SIV  
late.summer.N.levels.SIV  
strm.area.escape.cov.pct.SIV  
instream.area.10.to.40cm.SIV

**Geometric mean model** In the **geometric mean chinooksalmonLimit5to10CSilt** model, **13 of 19** variables are influential and **late.summer.N.levels.SIV** has the highest first order sensitivity. In addition, **late.summer.N.levels.SIV** has the highest total order sensitivity.

### Un-influential variables in geometric mean model:

pls.late.growing.season.SIV  
pls.class.late.growing.season.SIV  
spwn.gravel.pct.SIA.SIV  
multiples.of.avg.flow.SIV  
dominant.subs.rffl.run.SIV  
avg.fines.lt3mm.pct.SIV

**Limiting factor model** In the **limiting factor chinooksalmonLimit5to10CSilt** model, **13 of 19** variables are influential and **late.summer.N.levels.SIV** has the highest first order sensitivity. In addition, **late.summer.N.levels.SIV** has the highest total order sensitivity.

**Un-influential variables in limiting factor mean model:**

```
pls.late.growing.season.SIV
pls.class.late.growing.season.SIV
spwn.gravel.pct.SIA.SIV
multiples.of.avg.flow.SIV
dominant.subs.rffl.run.SIV
avg.fines.lt3mm.pct.SIV
```

**Multiplicative model** In the **multiplicative mean chinooksalmonLimit5to10CSilt** model, **13 of 19** variables are influential and **avg.fines.silt.spwn.gravel.pct.SIV** has the highest first order sensitivity. In addition, **avg.fines.silt.spwn.gravel.pct.SIV** has the highest total order sensitivity.

**Un-influential variables in multiplicative model:**

```
pls.late.growing.season.SIV
spwn.gravel.pct.SIA.SIV
spwn.gravel.pct.SIB.SIV
multiples.of.avg.flow.SIV
avg.fines.lt3mm.pct.SIV
strm.area.escape.cov.pct.SIV
```

## References

1. McKay S, D Hernandez-Abrams, and K Cushway. 2024. ecorest: conducts analyses informing ecosystem restoration decisions. R package version 2.0.0, <https://CRAN.R-project.org/package=ecorest>.
2. Puy, A, S Lo Piano, A Saltelli, and SA Levin. 2022. sensobol: an R package to compute variance based sensitivity indices. *Journal of Statistical Software* 102(5):1-37. doi: 10.18637/jss.v102.i05
3. Raleigh, RF, WJ Miller, and PC Nelson. 1986. Habitat suitability index models and instream flow suitability curves: chinook salmon. *U.S. Fish Wildl. Serv. Biol. Rep.* 82(10.122). 64 pp.