



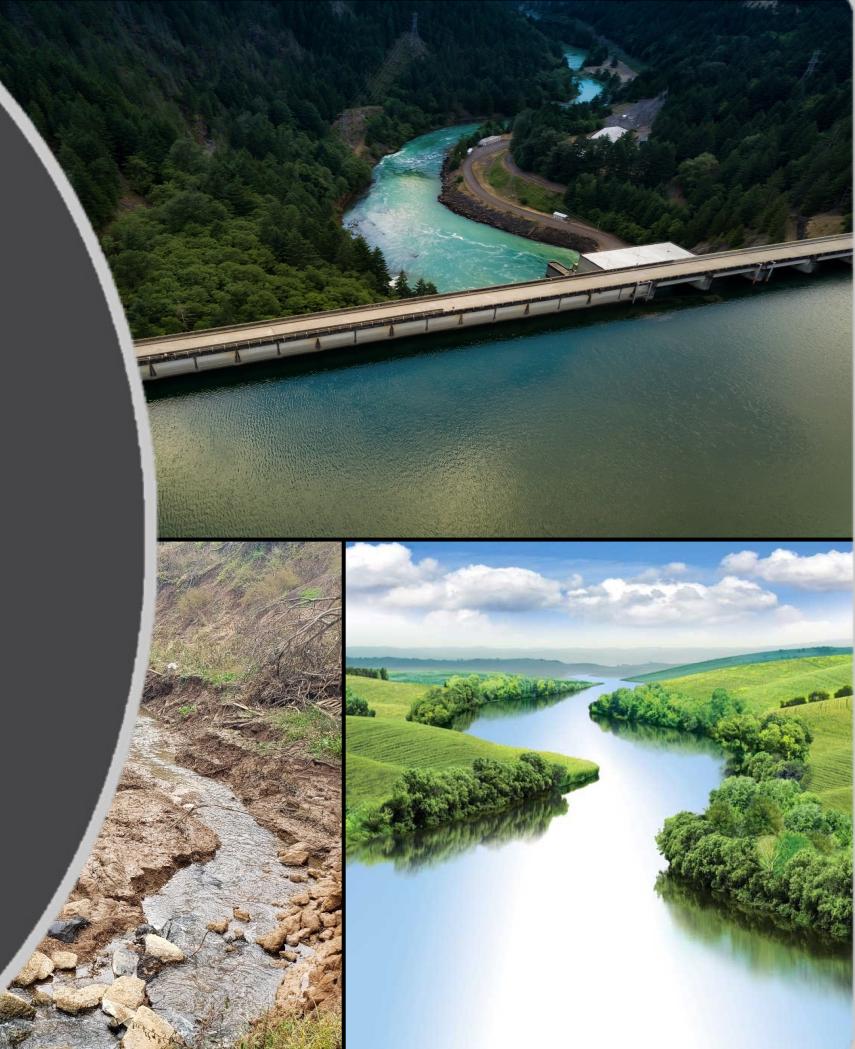
HYDRODYNAMICS MODELING

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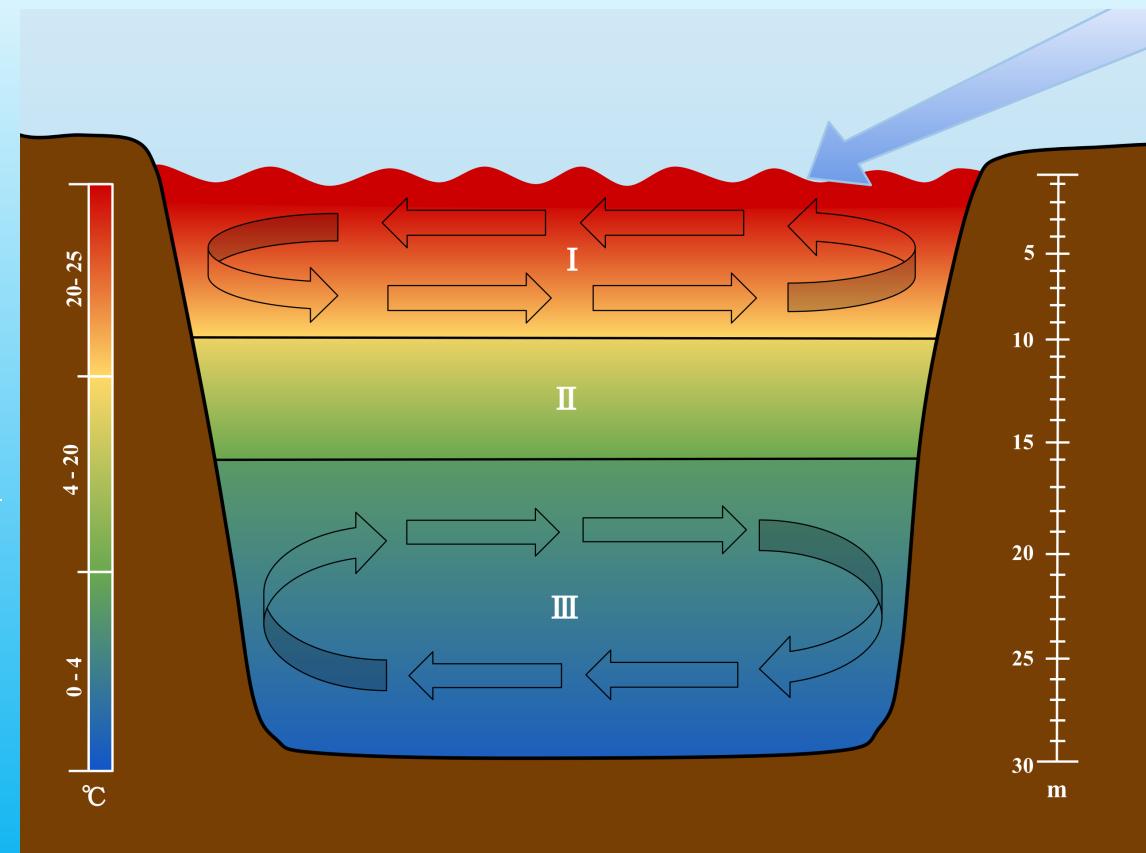
Important Hydrodynamic Processes

- Vertical stratification
- Meteorology
 - Wind forcing
 - Thermal forcing
- Water quality
 - Affects stratification
- Climate
 - Long-term effects



Vertical Stratification

- Mid-latitude lakes and reservoirs tend to thermally stratify vertically during the spring and summer. A conceptual model of their stratification divides the water body into three vertical layers:
 - The epilimnion, a warm surface layer
 - The hypolimnion, a cool bottom layer
 - The metalimnion, the layer in between the top and bottom layers. This layer is often described as the *thermocline*, where the temperature suddenly decreases sharply with depth.
- Lake stratification varies continually. It is often described by the depth and strength of the thermocline. The seasonal thermocline is characterized by the average depth and strength over a season. The diurnal thermocline varies throughout the day.



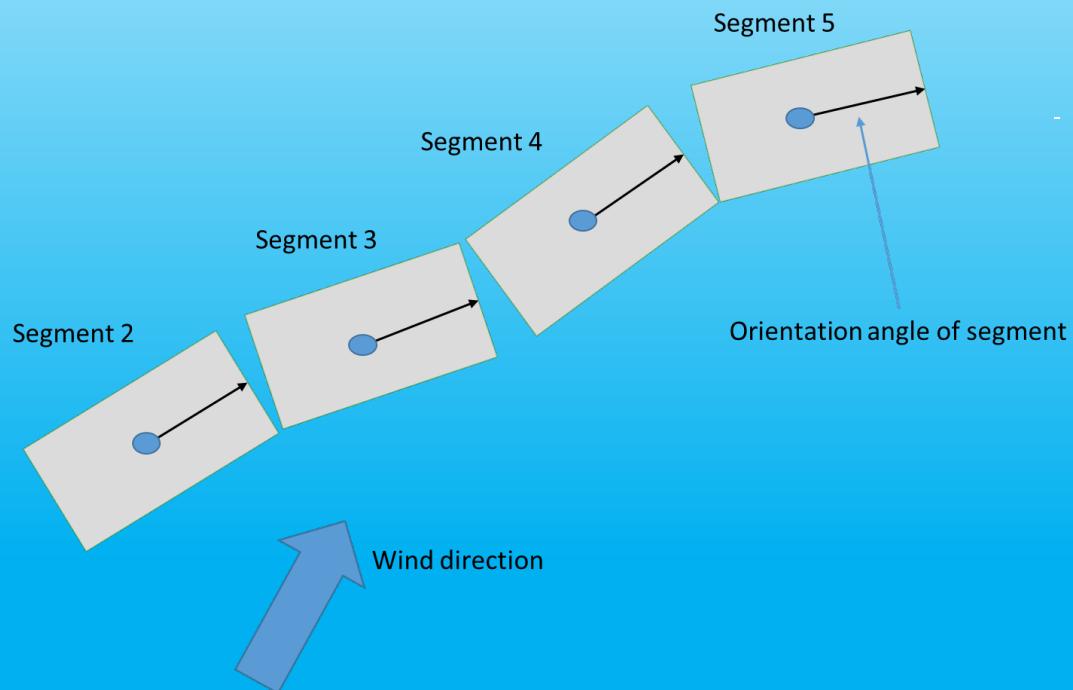
Meteorological Forcing

- The meteorology of the watershed affects several factors that control the hydrodynamics as well as the water quality of a reservoir.
 - Wind forcing: The wind flowing across the reservoir affects depth of stratification, vertical mixing, and circulation (currents across and around the water body).
 - Heat balance: The incoming (shortwave) solar radiation and outgoing radiation (longwave radiation, sensible heat, and evaporation) control the heat balance. Wind, solar radiation, and cloud cover, and relative humidity control the evaporation, the largest source of heat loss in a water body.



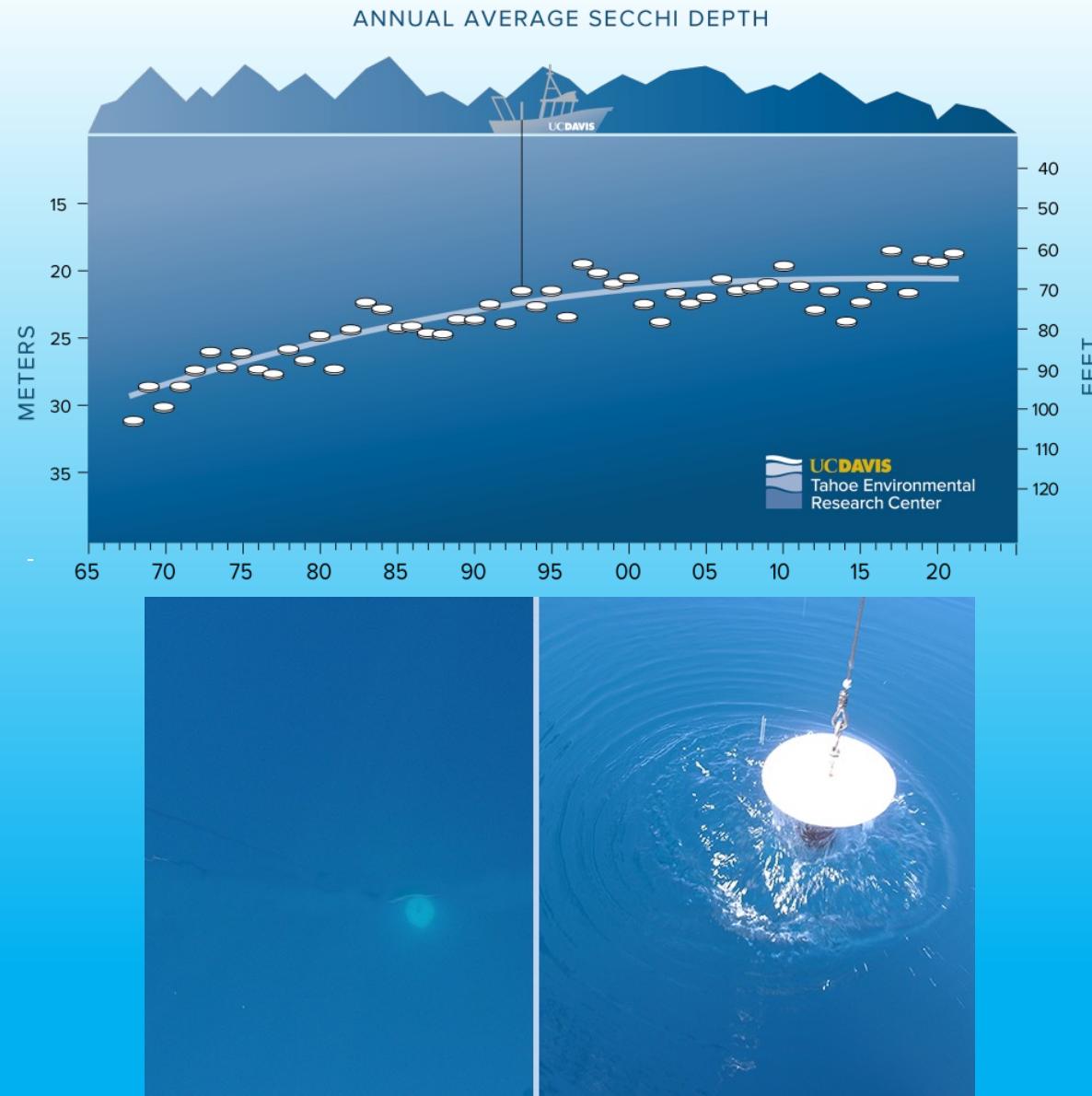
Meteorological Forcing: Wind Fetch

- The *fetch* or *fetch length* of a water body is the length of water over which wind has blown without obstruction.
- The fetch varies with the direction of the wind.
- If the fetch of the prevailing wind is aligned with the long axis of the water body, then the wind effect on mixing is at its maximum.



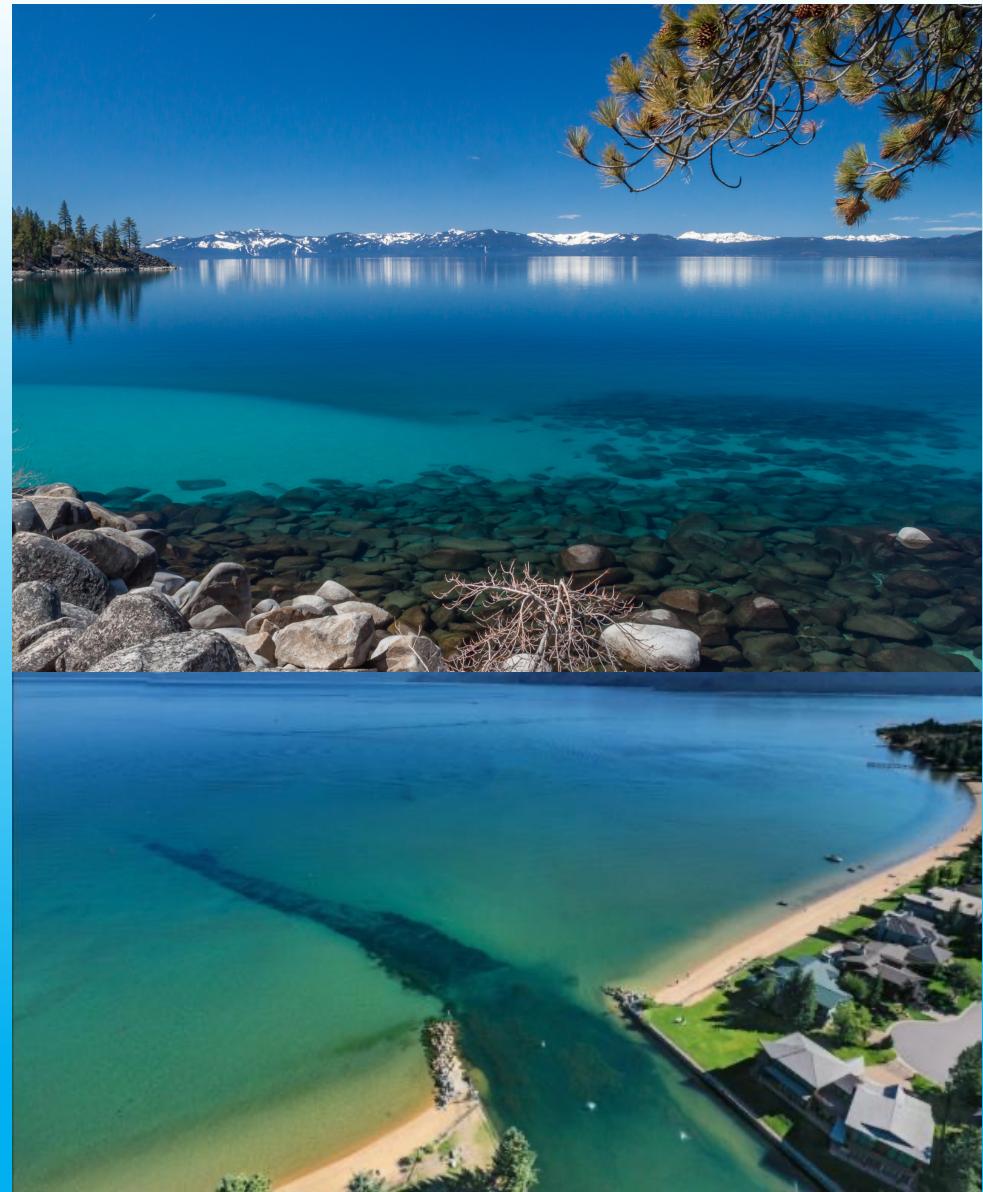
Water Quality Forcing

- Water quality affects the clarity of the water.
- Water clarity affects the depth that solar radiation penetrates the water surface.
- Clear lakes tend to have deep and relatively cool epilimnions and weak stratification.
- Turbid lakes tend to have shallow and warm epilimnions and strong stratification.



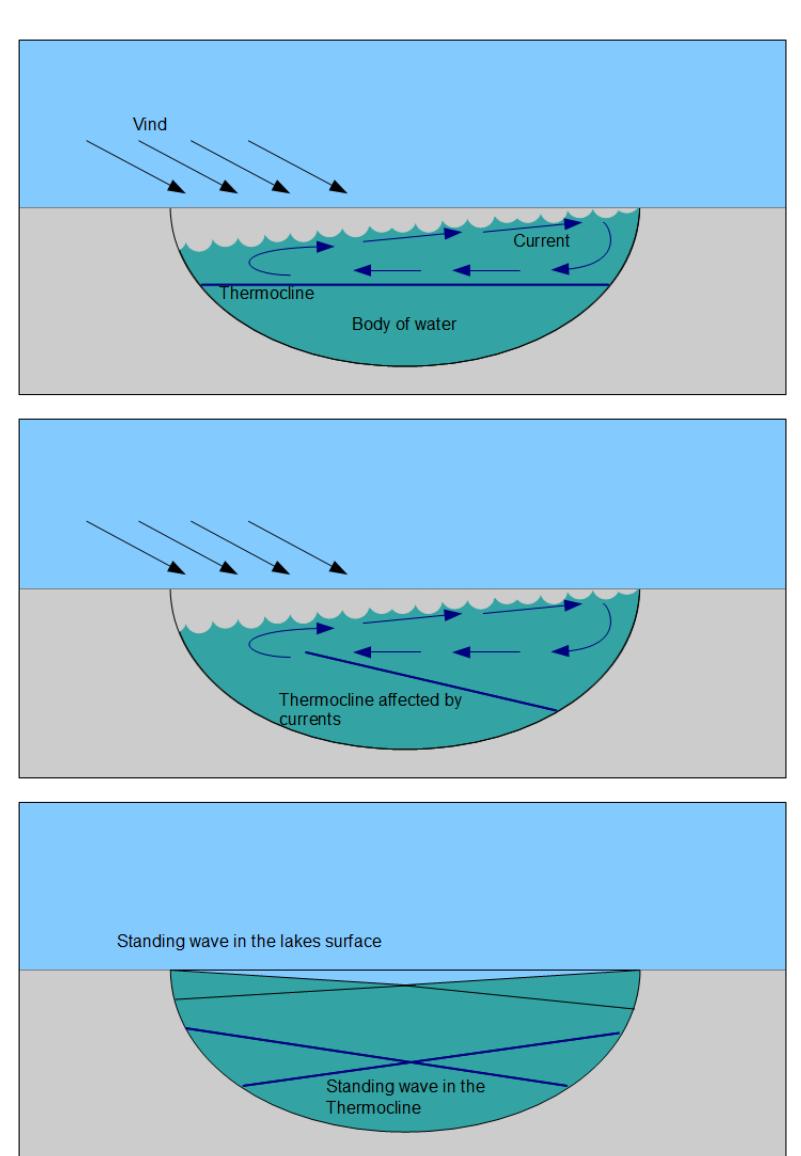
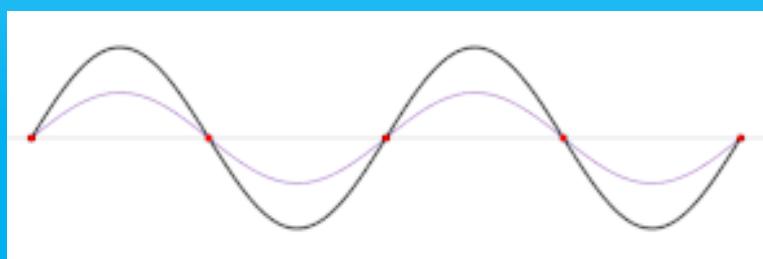
Climate Forcing

- Climate change can have a significant affect on reservoir hydrodynamics.
- As climate and water temperatures increase, while average wind forcing remains the same, the seasonal stratification will tend to strengthen. This can reduce the tendency of the reservoir to overturn (mix vertically). Poor water quality conditions can intensify in the hypolimnion.
 - Example: In Lake Tahoe, a significant quantity of phosphorus is bound with iron in the sediment. Hypoxic conditions could release the phosphorus into the water column, resulting in significant internal loading of phosphorus, increasing algae concentrations.
- On the other hand, if climate change increases the strength and frequency of occurrence of intense storms, wind forcing will affect the diurnal stratification. However, extreme precipitation can lead to increased particle inputs from runoff and erosion, which may decrease water clarity.



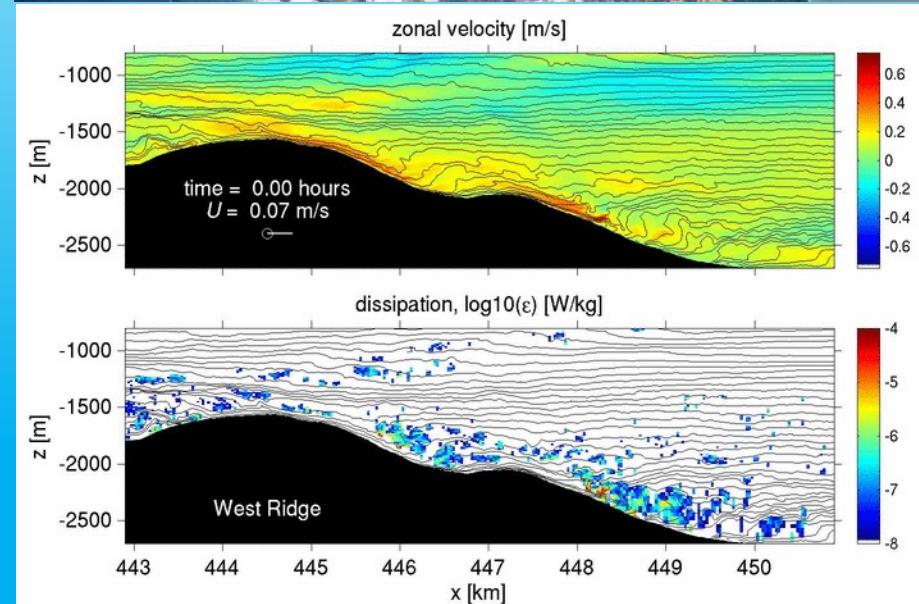
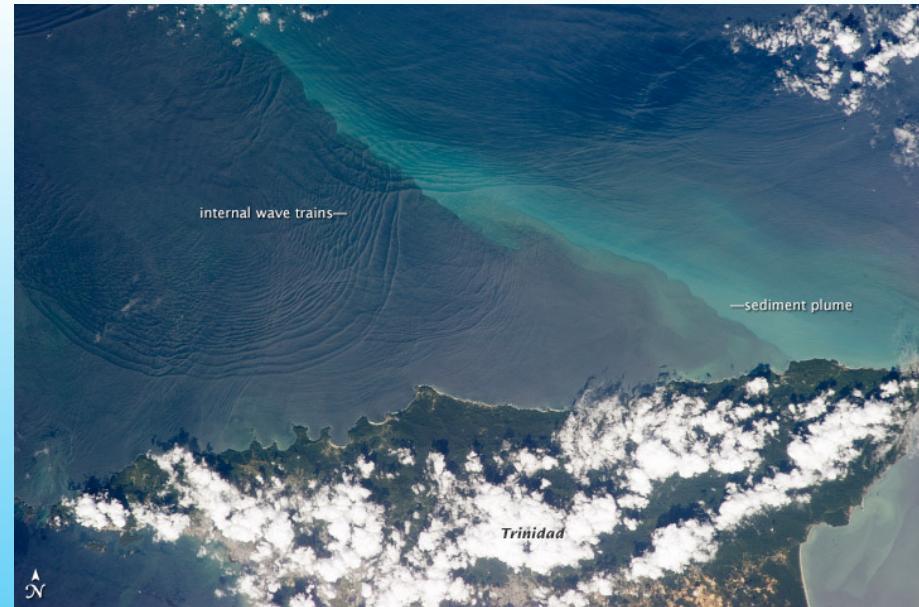
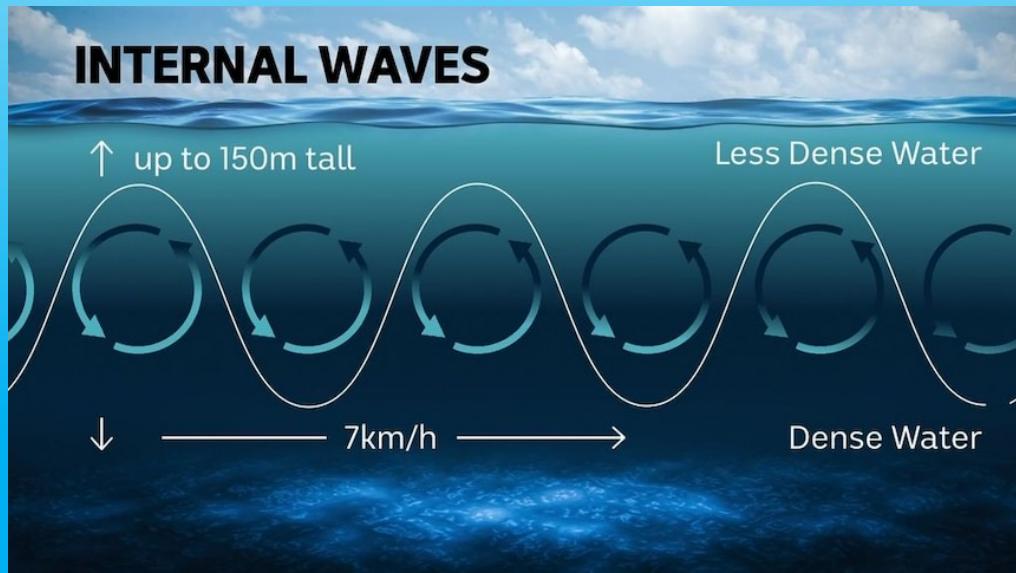
Seiches

- As wind blows across the water surface, it causes the water surface to tilt. It rises at the downwind side and lowers at the upwind side.
- The elevation change is small. For a water body with a fetch of 10 km, the maximum elevation change at the upwind end is only a few centimeters.
- When the wind slows down, the water surface tilts in the opposite direction, but it moves past the equilibrium point. This cycle results in a basin-wide standing wave, called a seiche.
- Seiches, like other surface waves are relatively fast and shallow.



Internal Waves

- The thermocline can oscillate up and down in response to seicheing, generating *internal waves*.
- The smaller the density difference between two layers of fluid, the larger and slower the waves.
- Seiches are small and fast.
- Internal waves are large and slow.
- Even though they are under the surface, they can be seen from the air and from space.



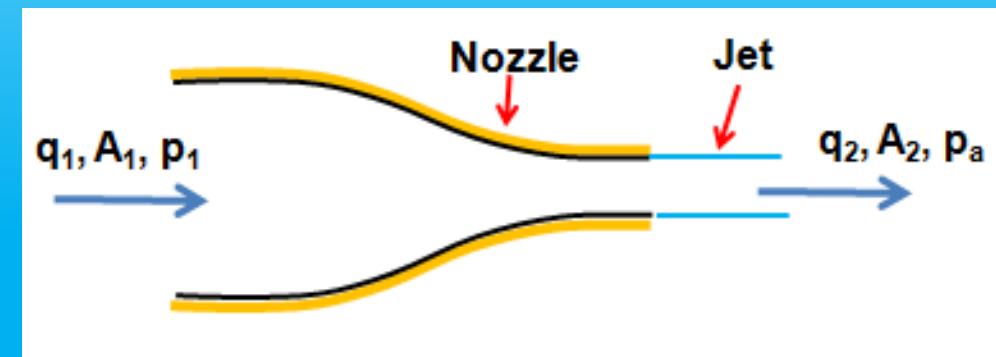
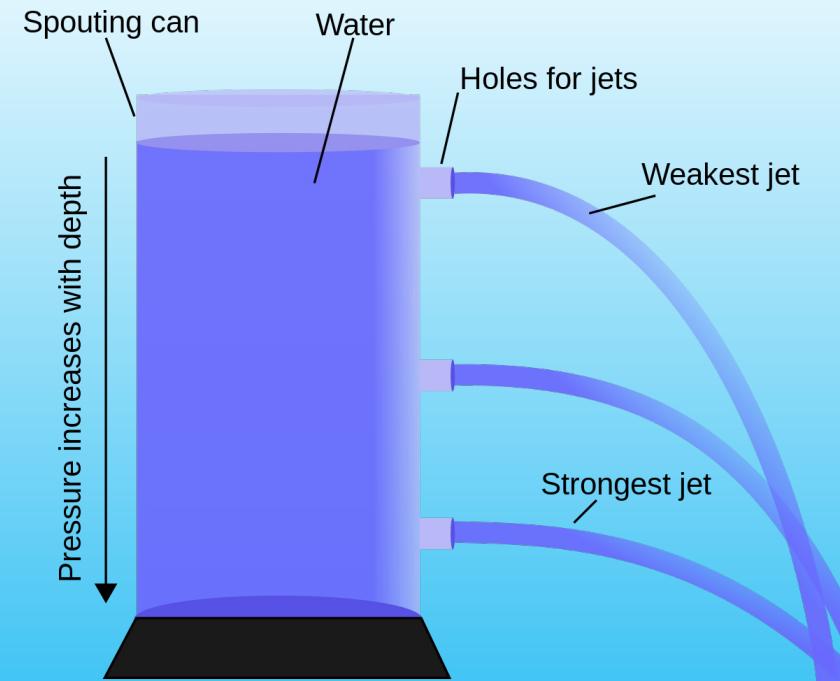
Harmful Algal Blooms

- Conditions that lead to Harmful Algal Blooms (HAB) include:
 - Warm water temperatures
 - High nutrient and algae concentrations
 - Low flows and velocities (currents, mixing)
- Climate change is expected to generally increase surface water temperatures, which will increase vertical stratification.
- These factors are expected to increase the severity and frequency of occurrence of harmful algal blooms in the future.



Introduction to Fluid Dynamics

- Important Properties:
 - Flow, Q
 - Velocity, V
 - Area, A
 - Pressure, P
 - Density, ρ
 - Height of water body: controls potential energy, H or z
 - Depth within water body: controls pressure, D or z
 - Viscosity, ν
- Three laws of conservation:
 - Conservation of Mass
 - Conservation of Momentum
 - Conservation of Energy (not covered)



Conservation of Mass: Continuity Equation

- The mass entering a system must equal the mass exiting the system, if mass does not change within the system.
- Consider the figure below, which describes an *element* of water. Think of this element as a full water tank.
- In surface water models, water is usually considered *incompressible*. Therefore, if water flows into full water tank, the same amount of water must flow out to conserve mass.
- This principle is described as the continuity equation:

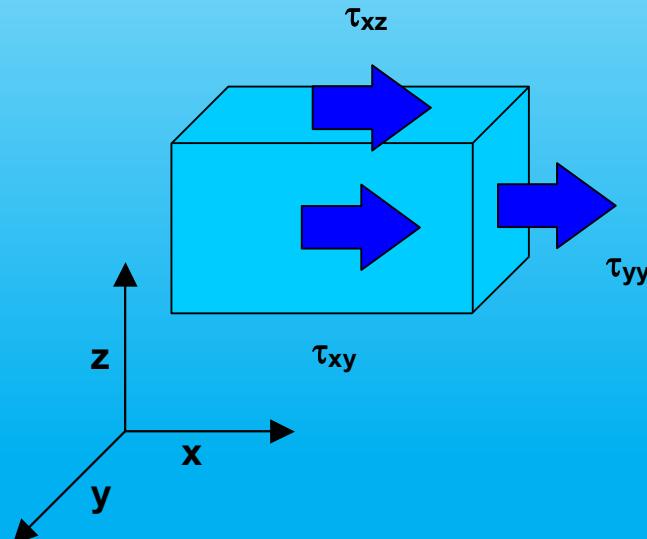
$$\frac{\partial \bar{u}}{\partial x} + \frac{\partial \bar{v}}{\partial y} + \frac{\partial \bar{w}}{\partial z} = 0$$

where:

u = x-direction velocity

v = y-direction velocity

w = z-direction velocity



Conservation of Momentum: Momentum Equations

- According to Newton's laws of motion, momentum must be conserved. Momentum is the product of the mass and velocity of an object. It takes a force to change the momentum of an object. The mass of a parcel of water (control volume) does not change. So, we focus on the change of velocity, which is *acceleration*. Force equals mass times acceleration: $F = m*a$
- Neglecting the Coriolis force*, the momentum equation in the x-direction is:

$$\frac{\partial \bar{u}}{\partial t} + \underbrace{\bar{u} \frac{\partial \bar{u}}{\partial x} + \bar{v} \frac{\partial \bar{u}}{\partial y} + \bar{w} \frac{\partial \bar{u}}{\partial z}}_{\text{unsteady acceleration}} = - \underbrace{\frac{1}{\rho} \frac{\partial \bar{p}}{\partial x}}_{\text{pressure gradient}} + \underbrace{\frac{\mu}{\rho} \left(\frac{\partial^2 \bar{u}}{\partial x^2} + \frac{\partial^2 \bar{u}}{\partial y^2} + \frac{\partial^2 \bar{u}}{\partial z^2} \right)}_{\text{viscous stresses}} + \underbrace{\frac{1}{\rho} \left(\frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xy}}{\partial y} + \frac{\partial \tau_{xz}}{\partial z} \right)}_{\text{turbulent stresses}}$$

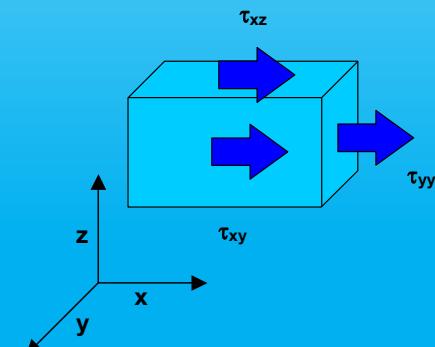
where:

τ_{xx} = turbulent shear stress acting in x direction on the x-face of control volume

τ_{xy} = turbulent shear stress acting in x direction on the y-face of control volume

τ_{xz} = turbulent shear stress acting in x direction on the z-face of control volume

μ = dynamic viscosity



Questions?

