Empirical Analysis of the Role of Energy in Economic Growth

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Abstract

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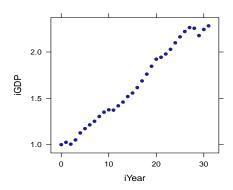
Keywords: economic growth, energy, cobb-douglas, CES, LINEX

Caleb, put your LaTeX code here.

```
createCountryGraph <- function(countryName) {
  dataTable <- loadData(countryName)
  graph <- xyplot(iGDP ~ iYear, data=dataTable)
  return(graph)
}
#graph <- createCountryGraph("US")
print(createCountryGraph("US"))</pre>
```

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1. Cobb-Douglas Without Energy

```
# Runs a non-linear least squares fit to the data. We've replaced beta with 1-al
modelCD <- nls(iGDP ~ exp(lambda*iYear) * iCapStk^alpha * iLabor^(1 - alpha),</pre>
                algorithm = "port",
                start = list(lambda=lambdaGuess, alpha=alphaGuess),
                lower = list(lambda=-Inf, alpha=0),
                upper = list(lambda=Inf, alpha=1),
                data=dataTable)
# Checks validity of the model. AIC stands for Akaike's Information Criterion.
aicCD <- AIC(modelCD, k=2)
#print(aicCD)
summaryCD <- summary(modelCD) # Gives the nls summary table.</pre>
#print(summaryCD)
ciCD <- confint(modelCD, level = ciLevel); ciCD # Displays confidence intervals</pre>
# Calculate beta and its confidence interval and report it.
alpha <- as.numeric(coef(modelCD)["alpha"])</pre>
beta <- 1.0 - alpha
beta.est <- deltaMethod(modelCD, "1 - alpha"); beta.est # Estimates beta and its
# Now calculate a confidence interval on beta
dofCD <- summaryCD$df[2]; dofCD # Gives the degrees of freedom for the model.</pre>
tvalCD <- qt(ciHalfLevel, df = dofCD); tvalCD</pre>
betaCICD <- with(beta.est, Estimate + c(-1.0, 1.0) * tvalCD * SE); betaCICD # G
#print(coef(modelCD))
# Combine all estimates and their confidence intervals into data frames with int
estCD <- data.frame(lambda = coef(modelCD)["lambda"], alpha = coef(modelCD)["alp</pre>
#print(estCD)
row.names(estCD) <- "CD"
row.names(estCD) \leftarrow "Cobb-Douglas: $y = e^{\langle t \} k^{\langle t \}} "
# The [1] subscripts pick off the lower confidence interval
lowerCD <- data.frame(lambda = ciCD["lambda","2.5%"], alpha = ciCD["alpha", "2.5</pre>
row.names(lowerCD) <- "- 95% CI"
# The [2] subscripts pick off the lower confidence interval
upperCD <- data.frame(lambda = ciCD["lambda", "97.5%"], alpha = ciCD["alpha", "97.5%"]
```

```
row.names(upperCD) <- "+ 95% CI"
 # Now create the data for a table.
 dataCD <- rbind(upperCD, estCD, lowerCD)</pre>
 #print(dataCD)
 return(dataCD)
# Creates a LaTeX printable table from the Cobb Douglas data. This function first
# countryName is a string containint the 2-letter abbreviation for the country, e
# returns a printable LaTeX table from xtable.
##
cobbDouglasTable <- function(countryName){</pre>
 dataCD <- cobbDouglasData(countryName)</pre>
 colnames(dataCD) <- c("$\\lambda$", "$\\alpha$", "$\\beta$", "$\\gamma$")</pre>
 tableCD <- xtable(dataCD, caption=paste(countryName, "Cobb-Douglas, 1980-2011",
 #print(tableCD)
 return(tableCD)
tablesCD <- lapply(countries, cobbDouglasTable)</pre>
Waiting for profiling to be done...
```

Waiting for profiling to be done...

print(tablesCD[["US"]], caption.placement="top")

Table 1: US Cobb-Douglas, 1980-2011

Table 1. 03 Cobb-Douglas, 1980-2011							
	\$\lambda\$	\$\alpha\$	$\Delta $	\$\gamma\$			
+ 95% CI	0.0116	0.34	0.79				
CD	0.0102	0.27	0.73	0.0			
- 95% CI	0.0087	0.21	0.66				

print(tablesCD[["UK"]], caption.placement="top")

Table 2: UK Cobb-Douglas, 1980-2011

	8 /					
	\$\lambda\$	\$\alpha\$	$\Delta $	\$\gamma\$		
+ 95% CI	0.0303	1.12	1.24			
CD	0.0097	0.44	0.56	0.0		
- 95% CI	-0.0104	-0.25	-0.13			

print(tablesCD[["JP"]], caption.placement="top")

Table 3: JP Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0081	0.61	0.56	
CD	0.0048	0.52	0.48	0.0
- 95% CI	0.0014	0.44	0.39	

print(tablesCD[["ZA"]], caption.placement="top")

Table 4: ZA Cobb-Douglas, 1980-2011

	\$\lambda\$ \$\alpha\$ \$\beta\$ \$\gamma\$								
	$\Lambda \$	\$\alpha\$	\$\beta\$	\$\gamma\$					
+ 95% CI	0.0022	0.73	0.54						
CD	0.0008	0.60	0.40	0.0					
- 95% CI	-0.0007	0.46	0.26						

print(tablesCD[["CN"]], caption.placement="top")

Table 5: CN Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0779	1.32	0.89	
CD	0.0188	0.71	0.29	0.0
- 95% CI	-0.0405	0.11	-0.32	

print(tablesCD[["SA"]], caption.placement="top")

Table 6: SA Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	-0.0087	0.68	0.78	
CD	-0.0123	0.45	0.55	0.0
- 95% CI	-0.0159	0.21	0.32	

print(tablesCD[["IR"]], caption.placement="top")

print(tablesCD[["TZ"]], caption.placement="top")

Table 7: IR Cobb-Douglas, 1980-2011

		0	,	
	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0045	0.70	0.51	
CD	0.0039	0.60	0.40	0.0
- 95% CI	0.0032	0.49	0.30	

Table 8: TZ Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0068	0.95	0.50	
CD	0.0015	0.73	0.27	0.0
- 95% CI	-0.0039	0.50	0.05	

print(tablesCD[["ZM"]], caption.placement="top")

Table 9: ZM Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0280	1.57	-0.25	
CD	0.0249	1.41	-0.41	0.0
- 95% CI	0.0218	1.25	-0.57	

- # According to http://cran.r-project.org/web/packages/xtable/vignettes/xtableGalle # be able to use the "sanitize.text.function" parameter to allow markup in column
- # line is not working at the present time. --MKH, 18 Jan 2012.
- # print(tableCD, caption.placement="top", sanitize.text.function = function(x){x};

2. Cobb-Douglas With Energy

We can force α , β , and γ to be in [0, 1] by a reparameterization:

$$a \in [0, 1], b \in [0, 1], \alpha = \min(a, b), \beta = |b - a|, \gamma = 1 - \max(a, b)$$

2.1. Cobb-Douglas with Q

```
# Note that the anlaysis of ZA is taking a long time here. Need to figure out why CDqTables <- lapply(countries, cobbDouglasEnergyTable, energyType="Q")
```

```
print(CDqTables[["US"]], caption.placement="top")
print(CDqTables[["ZA"]], caption.placement="top")
# According to http://cran.r-project.org/web/packages/xtable/vignettes/xtableGallef
# be able to use the "sanitize.text.function" parameter to allow markup in column
# line is not working at the present time. --MKH, 18 Jan 2012.
# print(tableCDe, sanitize.text.function = function(x){x})
#print(tableAll, caption.placement="top")
```

2.2. Cobb-Douglas With X

```
# Note that the anlaysis of ZA is taking a long time here. Need to figure out why
CDxTables <- lapply(countries, cobbDouglasEnergyTable, energyType="X")</pre>
```

```
print(CDxTables[["US"]], caption.placement="top")
print(CDxTables[["ZA"]], caption.placement="top")
```

2.3. Cobb-Douglas With U

```
CDuTables <- lapply(countries, cobbDouglasEnergyTable, energyType="U")
```

```
print(CDuTables[["US"]], caption.placement="top")
print(CDuTables[["ZA"]], caption.placement="top")
```

3. CES

```
cesData <- function(countryName, energyType){</pre>
  energyColumnName <- paste("i", energyType, sep="")</pre>
  # Load the data that we need.
  dataTable <- loadData(countryName)</pre>
  # Establish guess values for phi beta, zeta, lambda_L and lambda_E.
  phiGuess <- -20
  betaGuess <- 0.5 # a typical value for beta (exponent on labor)</pre>
  zetaGuess <- 0.0004 # a small value
  lambda_LGuess <- 0.007 #assuming no technical progress on the labor-capital port
  lambda_EGuess <- 0.008 #assuming no technical progress on the energy portion of
  # Runs a non-linear least squares fit to the data with constraints
  modelCES <- nls(iGDP ~ ((1-zeta) * (exp(lambda_L*iYear) * iCapStk^(1-beta) * iLa
                            + zeta*(exp(lambda_E*iYear) * iQ)^phi)^(1/phi),
                   algorithm = "port",
                   control = nls.control(maxiter = 500, tol = 1e-06, minFactor = 3
                                          printEval = FALSE, warnOnly = FALSE),
                   start = list(phi=phiGuess, beta=betaGuess, zeta=zetaGuess, lamb
                                 lambda_E=lambda_EGuess),
                   lower = list(phi=-Inf, beta=0, zeta=0, lambda_L=-Inf, lambda_E=
                   upper = list(phi=0, beta=1, zeta=1, lambda_L=Inf, lambda_E=Inf)
                   data=dataTable)
  aicCES <- AIC(modelCES, k=2) # Checks validity of the model. AIC stands for Akar
  print(aicCES)
  # Gives the nls summary table
  summaryCES <- summary(modelCES) # Gives the nls summary table
  print(summaryCES)
  # Provides confidence intervals on phi, beta, zeta, lambda_L, and lambda_E. But
  ciCES <- confint(modelCES, level = ciLevel)</pre>
  print(ciCES)
  # Get the estimate for alpha
  beta <- as.numeric(coef(modelCES)["beta"])</pre>
```

```
alpha <- 1.0 - beta
alpha.est <- deltaMethod(modelCES, "1 - beta") # Estimates alpha and its standar
print(alpha.est)
# Now calculate a confidence interval on alpha
dofCES <- summaryCES$df[2]</pre>
print(dofCES) # Gives the degrees of freedom for the model.
tvalCES <- qt(ciHalfLevel, df = dofCES); tvalCES</pre>
# Get confidence intervals for each parameter in the model
alphaCICES <- with(alpha.est, Estimate + c(-1.0, 1.0) * tvalCES * SE) # CI on all
print(alphaCICES)
# Assemble the data into data frames for the table.
estCES <- data.frame(phi = coef(modelCES)["phi"], alpha = alpha,</pre>
                     beta = coef(modelCES)["beta"], zeta = coef(modelCES)["zeta"]
                     lambda_L = coef(modelCES)["lambda_L"], lambda_E = coef(modelCES)
row.names(estCES) <- paste("CES with ", energyType, sep="")</pre>
#print(estCES)
# The [1] subscripts pick off the lower confidence interval
lowerCES <- data.frame(phi = ciCES["phi", "2.5%"], alpha = alphaCICES[1],
                        beta = ciCES["beta", "2.5%"], zeta = ciCES["zeta", "2.5%"
                        lambda_L = ciCES["lambda_L", "2.5%"], lambda_E = ciCES["]
row.names(lowerCES) <- "- 95% CI"
# The [2] subscripts pick off the lower confidence interval
upperCES <- data.frame(phi = ciCES["phi","97.5%"], alpha = alphaCICES[2],
                       beta = ciCES["beta", "97.5%"], zeta = ciCES["zeta", "97.8
                       lambda_L = ciCES["lambda_L", "97.5%"], lambda_E = ciCES["]
row.names(upperCES) <- "+ 95% CI"
# Now create the data for a table.
dataCES <- rbind(upperCES, estCES, lowerCES)</pre>
print(dataCES)
return(dataCES)
#xyplot( resid(modelCESQ) ~ fitted(modelCESQ) )
#histogram( ~resid(modelCESQ) )
#qqmath( ~resid(modelCESQ) )
```

```
# Creates a LaTeX printable table from the CES data. This function first calls ces
# countryName is a string containint the 2-letter abbreviation for the country, e
# energyType is a string to be used in table captions reprsenting the type of energyType
# returns a printable LaTeX table from xtable.
cesTable <- function(countryName, energyType){</pre>
 dataCESe <- cesData(countryName, energyType)</pre>
 tableCESq <- xtable(dataCESe, caption=paste(countryName, ", 1980-2011.", sep="")
3.1. CES with Q
countryName <- "US"
energyType <- "Q"</pre>
tableCESq <- cesTable(countryName, energyType)</pre>
[1] -194
Formula: iGDP ~ ((1 - zeta) * (exp(lambda_L * iYear) * iCapStk^(1 - beta) *
   iLabor^beta)^phi + zeta * (exp(lambda_E * iYear) * iQ)^phi)^(1/phi)
Parameters:
         Estimate Std. Error t value Pr(>|t|)
        -3.96e+01 2.43e+01 -1.63 0.1144
phi
beta
        6.09e-01 3.45e-02 17.64 2.4e-16
        2.09e-06 1.32e-05 0.16 0.8758
zeta
lambda_L 7.98e-03 6.68e-04 11.95 2.8e-12
lambda_E 8.57e-03 2.48e-03 3.45 0.0018
Residual standard error: 0.0105 on 27 degrees of freedom
Algorithm "port", convergence message: relative convergence (4)
```

```
Waiting for profiling to be done...
            2.5%
                     97.5%
phi
              NA -10.290831
beta
        0.514667 0.665371
zeta
              NA
lambda_L 0.006428  0.009152
lambda_E 0.000715
                  0.012468
        Estimate
                     SE
1 - beta 0.3911 0.03453
[1] 27
[1] 0.3202 0.4619
             phi alpha beta zeta lambda_L lambda_E
+ 95% CI -10.29 0.4619 0.6654
                                    NA 0.009152 0.012468
CES with Q -39.64 0.3911 0.6089 2.085e-06 0.007979 0.008570
- 95% CI
          NA 0.3202 0.5147 NA 0.006428 0.000715
#CESqTables <- lapply(countries, cesTable, energyType="Q")</pre>
```

print(tableCESq, caption.placement="top")

Table 10: US, 1980-2011.

	phi	alpha	beta	zeta	lambda_L	lambda_E
+ 95% CI	-10.3	0.46	0.67		0.00915	0.01247
CES with Q	-39.6	0.39	0.61	0.000002	0.00798	0.00857
- 95% CI		0.32	0.51		0.00643	0.00071

```
#print(CESqTables[["US"]], caption.placement="top")
#print(CESqTables[["ZA"]], caption.placement="top")
```