Empirical Analysis of the Role of Energy in Economic Growth

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Abstract

****** Add abstract *******

Keywords: economic growth, energy, cobb-douglas, CES, LINEX

Caleb, put your LaTeX code here.

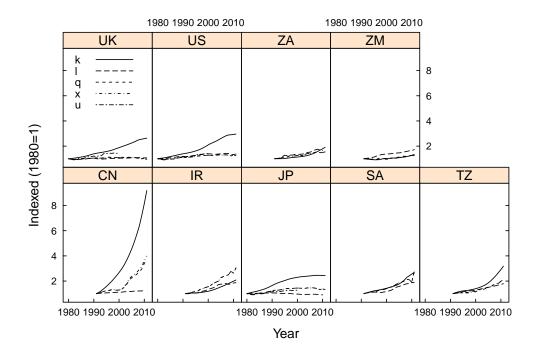
```
createCountryFactorsGraph <- function(countryName){</pre>
  dataTable <- loadData(countryName)</pre>
  graphType <- "1"</pre>
  lineTypes <- c(1, 5, 2, 4, 6) #line types. See http://en.wikibooks.org/wiki/R_Pa
  lineWidths \leftarrow c(1, 1, 1, 1, 1) #line widths
  colors <- c("black", "black", "black", "black", "black") #line and point colors</pre>
  lineSpec <- list(lty=lineTypes, lwd=lineWidths, col=colors)</pre>
  graph <- xyplot(iCapStk+iLabor+iQ+iX+iU ~ Year, data=dataTable,</pre>
                   type=graphType,
                   par.settings = list(superpose.line = lineSpec),
                   key=list(text=list(c("k", "l", "q", "x", "u")),
                             type=graphType,
                             lines=lineSpec,
                             columns=1, x=0.0, y=0.98),
                   scales=list(cex=1.0, #controls text size on scales
                                tck=-0.5), #controls tick mark length
                   ylab="Indexed (1980=1)")
```

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```
return(graph)
createFactorsLatticeGraph <- function(countryName){</pre>
  dataTable <- loadData(countryName)</pre>
  graphType <- "1"</pre>
  lineTypes <- c(1, 5, 2, 4, 6) #line types. See http://en.wikibooks.org/wiki/R_Pa
  lineWidths \leftarrow c(1, 1, 1, 1, 1) #line widths
  colors <- c("black", "black", "black", "black", "black") #line and point colors</pre>
  lineSpec <- list(lty=lineTypes, lwd=lineWidths, col=colors)</pre>
  graph <- xyplot(iCapStk+iLabor+iQ+iX+iU ~ Year | Country, data=dataTable,</pre>
                   type=graphType,
                   par.settings = list(superpose.line = lineSpec),
                   key=list(text=list(c("k", "l", "q", "x", "u")),
                             type=graphType,
                             cex=0.85,
                             lines=lineSpec,
                             columns=1, x=0.01, y=0.92),
                   scales=list(cex=0.75, #controls text size on scales
                                tck=-0.5), #controls tick mark length
                   ylab="Indexed (1980=1)")
 return(graph)
createGDPComparisonGraph <- function(countryName){</pre>
  dataTable <- loadData(countryName)</pre>
  graphType <- "1"</pre>
  lineTypes <- c(1) #line types. See http://en.wikibooks.org/wiki/R_Programming/Gi
  lineWidths <- c(1) #line widths
  colors <- c("black") #line and point colors</pre>
  lineSpec <- list(lty=lineTypes, lwd=lineWidths, col=colors)</pre>
  graph <- xyplot(iGDP ~ Year, data=dataTable,</pre>
                   key=list(text=list(c("GDP")),
                             type=graphType,
                             lines=lineSpec,
                             columns=1, x=0.0, y=0.98),
                   type=graphType,
```

```
par.settings = list(superpose.line = lineSpec),
                   scales=list(cex=1.0, #controls text size on scales
                                tck=-0.5), #controls tick mark length
                   ylab="Indexed (1980=1)")
  return(graph)
# createGDPComparisonGraph <- function(countryName){</pre>
    dataTable <- loadData(countryName)</pre>
#
    graphType <- "1"</pre>
    colors <- c("black", "black", "black", "black") #line and point colors</pre>
#
    lineWidths \leftarrow c(1, 1, 1, 1) #line widths
    lineTypes <- c(1, 5, 2, 4) #line types. See http://en.wikibooks.org/wiki/R_Pro
#
    lineSpec <- list(lty=lineTypes, lwd=lineWidths, col=colors)</pre>
#
    pointSpec <- list(col=colors)</pre>
    graph <- xyplot(iGDP ~ iYear, data=dataTable,</pre>
#
#
                     key=list(text=list(c("GDP")),
#
                               type=graphType,
#
                               lines=lineSpec,
#
                               columns=1, x=0.0, y=0.98),
#
                     type=graphType,
#
                     par.settings = list(superpose.line = lineSpec),
# #
                                            superpose.symbol = pointSpec),
#
                     scales=list(cex=1.0, #controls text size on scales
                                  tck=-0.5), #controls tick mark length
#
#
                     ylab="Indexed (1980=1)")
#
    return(graph)
#
#
# }
createFactorsLatticeGraph("All")
```



```
#createGDPComparisonGraph("US")
#createCountryFactorsGraph("US")
#lapply(countries, createCountryFactorsGraph)
```

1. Cobb-Douglas Without Energy

countryName is a string containing the 2-letter abbreviation for the country, e.

```
# returns a vector of data for the Cobb-Douglas model.
# First item is the +95% CI on all parameters
# Second item contains the parameter estimates
\# Third item is the -95% CI on all parameters
# Each row has names: lambda, alpha, beta, gamma, corresponding to the parameters
cobbDouglasData <- function(countryName){</pre>
  # Load the data that we need.
  dataTable <- loadData(countryName)</pre>
  # Establish guess values for alpha and lambda.
  lambdaGuess <- 0.0 # guessing lambda = 0 means there is no technological progres
  alphaGuess <- 0.3 # a typical value for alpha, the coefficient on capital stock
  # Runs a non-linear least squares fit to the data. We've replaced beta with 1-al
 modelCD <- nls(iGDP ~ exp(lambda*iYear) * iCapStk^alpha * iLabor^(1 - alpha),</pre>
                  algorithm = "port",
                 start = list(lambda=lambdaGuess, alpha=alphaGuess),
                  lower = list(lambda=-Inf, alpha=0),
                  upper = list(lambda=Inf, alpha=1),
                 data=dataTable)
  # Checks validity of the model. AIC stands for Akaike's Information Criterion.
  aicCD <- AIC(modelCD, k=2)
  #print(aicCD)
  summaryCD <- summary(modelCD) # Gives the nls summary table.</pre>
  #print(summaryCD)
  ciCD <- confint(modelCD, level = ciLevel); ciCD # Displays confidence intervals</pre>
  # Calculate beta and its confidence interval and report it.
  alpha <- as.numeric(coef(modelCD)["alpha"])</pre>
  beta <- 1.0 - alpha
  beta.est <- deltaMethod(modelCD, "1 - alpha"); beta.est # Estimates beta and its
  # Now calculate a confidence interval on beta
```

```
dofCD <- summaryCD$df[2]; dofCD # Gives the degrees of freedom for the model.
  tvalCD <- qt(ciHalfLevel, df = dofCD); tvalCD</pre>
  betaCICD <- with(beta.est, Estimate + c(-1.0, 1.0) * tvalCD * SE); betaCICD # G
  #print(coef(modelCD))
  # Combine all estimates and their confidence intervals into data frames with int
  estCD <- data.frame(lambda = coef(modelCD)["lambda"], alpha = coef(modelCD)["alp</pre>
  #print(estCD)
  row.names(estCD) <- "CD"</pre>
  row.names(estCD) \leftarrow "Cobb-Douglas: $y = e^{{\lambda t}}k^{{\lambda t}}l^{{\lambda t}} = e^{{\lambda t}}k^{{\lambda t}}
  # The [1] subscripts pick off the lower confidence interval
  lowerCD <- data.frame(lambda = ciCD["lambda","2.5%"], alpha = ciCD["alpha", "2.5</pre>
  row.names(lowerCD) <- "- 95% CI"
  # The [2] subscripts pick off the lower confidence interval
  upperCD <- data.frame(lambda = ciCD["lambda", "97.5%"], alpha = ciCD["alpha", "97.5%"]
  row.names(upperCD) <- "+ 95% CI"
  # Now create the data for a table.
  dataCD <- rbind(upperCD, estCD, lowerCD)</pre>
  #print(dataCD)
  return(dataCD)
# Creates a LaTeX printable table from the Cobb Douglas data. This function first
# countryName is a string containint the 2-letter abbreviation for the country, e
# returns a printable LaTeX table from xtable.
cobbDouglasTable <- function(countryName){</pre>
  dataCD <- cobbDouglasData(countryName)</pre>
  colnames(dataCD) <- c("$\\lambda$", "$\\alpha$", "$\\beta$", "$\\gamma$")</pre>
  tableCD <- xtable(dataCD, caption=paste(countryName, "Cobb-Douglas, 1980-2011",
  #print(tableCD)
  return(tableCD)
```

```
}
```

```
Waiting for profiling to be done...
```

print(tablesCD[["US"]], caption.placement="top")

Table 1: US Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0116	0.34	0.79	
CD	0.0102	0.27	0.73	0.0
- 95% CI	0.0087	0.21	0.66	

Table 2: UK Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0303	1.12	1.24	
CD	0.0097	0.44	0.56	0.0
- 95% CI	-0.0104	-0.25	-0.13	

print(tablesCD[["JP"]], caption.placement="top")

Table 3: JP Cobb-Douglas, 1980-2011

	\$\lambda\$		<u> </u>	\$\gamma\$
+95% CI	0.0081	0.61	0.56	
CD	0.0048	0.52	0.48	0.0
- 95% CI	0.0014	0.44	0.39	

print(tablesCD[["ZA"]], caption.placement="top")

Table 4: ZA Cobb-Douglas, 1980-2011

		0	/	
	\$\lambda\$	\$\alpha\$	$\Delta $	\$\gamma\$
+ 95% CI	0.0022	0.73	0.54	
CD	0.0008	0.60	0.40	0.0
- 95% CI	-0.0007	0.46	0.26	

print(tablesCD[["CN"]], caption.placement="top")

Table 5: CN Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0779	1.32	0.89	
CD	0.0188	0.71	0.29	0.0
- 95% CI	-0.0405	0.11	-0.32	

print(tablesCD[["SA"]], caption.placement="top")

Table 6: SA Cobb-Douglas, 1980-2011

		0	,	
	\$\lambda\$	\$\alpha\$	$\Delta \$	\$\gamma\$
+ 95% CI	-0.0087	0.68	0.78	
CD	-0.0123	0.45	0.55	0.0
- 95% CI	-0.0159	0.21	0.32	

print(tablesCD[["IR"]], caption.placement="top")

Table 7: IR Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0045	0.70	0.51	
CD	0.0039	0.60	0.40	0.0
- 95% CI	0.0032	0.49	0.30	

print(tablesCD[["TZ"]], caption.placement="top")

Table 8: TZ Cobb-Douglas, 1980-2011

	\$\lambda\$		/	\$\gamma\$
+ 95% CI	0.0068	0.95	0.50	
CD	0.0015	0.73	0.27	0.0
- 95% CI	-0.0039	0.50	0.05	

print(tablesCD[["ZM"]], caption.placement="top")

[#] According to http://cran.r-project.org/web/packages/xtable/vignettes/xtableGalle

 $[\]mbox{\tt\#}$ be able to use the "sanitize.text.function" parameter to allow markup in column

[#] line is not working at the present time. --MKH, 18 Jan 2012.

[#] print(tableCD, caption.placement="top", sanitize.text.function = function(x) $\{x\}$)

Table 9: ZM Cobb-Douglas, 1980-2011

	\$\lambda\$	\$\alpha\$	\$\beta\$	\$\gamma\$
+ 95% CI	0.0280	1.57	-0.25	
CD	0.0249	1.41	-0.41	0.0
- 95% CI	0.0218	1.25	-0.57	

2. Cobb-Douglas With Energy

We can force α , β , and γ to be in [0,1] by a reparameterization:

$$a \in [0, 1], b \in [0, 1], \alpha = \min(a, b), \beta = |b - a|, \gamma = 1 - \max(a, b)$$

2.1. Cobb-Douglas with Q

Note that the anlaysis of ZA is taking a long time here. Need to figure out why CDqTables <- lapply(countries, cobbDouglasEnergyTable, energyType="Q")

```
print(CDqTables[["US"]], caption.placement="top")
print(CDqTables[["ZA"]], caption.placement="top")

# According to http://cran.r-project.org/web/packages/xtable/vignettes/xtableGallef
# be able to use the "sanitize.text.function" parameter to allow markup in column
# line is not working at the present time. --MKH, 18 Jan 2012.
# print(tableCDe, sanitize.text.function = function(x){x})
#print(tableAll, caption.placement="top")
```

2.2. Cobb-Douglas With X

Note that the anlaysis of ZA is taking a long time here. Need to figure out why CDxTables <- lapply(countries, cobbDouglasEnergyTable, energyType="X")

```
print(CDxTables[["US"]], caption.placement="top")
print(CDxTables[["ZA"]], caption.placement="top")
```

2.3. Cobb-Douglas With U

```
CDuTables <- lapply(countries, cobbDouglasEnergyTable, energyType="U")
```

```
print(CDuTables[["US"]], caption.placement="top")
print(CDuTables[["ZA"]], caption.placement="top")
```

3. CES

```
cesData <- function(countryName, energyType){</pre>
  energyColumnName <- paste("i", energyType, sep="")</pre>
  # Load the data that we need.
  dataTable <- loadData(countryName)</pre>
  # Establish guess values for phi beta, zeta, lambda_L and lambda_E.
  phiGuess <- -20
  betaGuess <- 0.5 # a typical value for beta (exponent on labor)
  zetaGuess <- 0.0004 # a small value
  lambda_LGuess <- 0.007 #assuming no technical progress on the labor-capital port
  lambda_EGuess <- 0.008 #assuming no technical progress on the energy portion of
  # Runs a non-linear least squares fit to the data with constraints
  modelCES <- nls(iGDP ~ ((1-zeta) * (exp(lambda_L*iYear) * iCapStk^(1-beta) * iLa
                           + zeta*(exp(lambda_E*iYear) * iQ)^phi)^(1/phi),
                   algorithm = "port",
                   control = nls.control(maxiter = 500, tol = 1e-06, minFactor = 3
                                          printEval = FALSE, warnOnly = FALSE),
                   start = list(phi=phiGuess, beta=betaGuess, zeta=zetaGuess, lamb
                                 lambda_E=lambda_EGuess),
                   lower = list(phi=-Inf, beta=0, zeta=0, lambda_L=-Inf, lambda_E=
                   upper = list(phi=0, beta=1, zeta=1, lambda_L=Inf, lambda_E=Inf)
                   data=dataTable)
  aicCES <- AIC(modelCES, k=2) # Checks validity of the model. AIC stands for Akar
  print(aicCES)
  # Gives the nls summary table
```

```
summaryCES <- summary(modelCES) # Gives the nls summary table
print(summaryCES)
# Provides confidence intervals on phi, beta, zeta, lambda_L, and lambda_E. But,
ciCES <- confint(modelCES, level = ciLevel)</pre>
print(ciCES)
# Get the estimate for alpha
beta <- as.numeric(coef(modelCES)["beta"])</pre>
alpha <- 1.0 - beta
alpha.est <- deltaMethod(modelCES, "1 - beta") # Estimates alpha and its standar
print(alpha.est)
# Now calculate a confidence interval on alpha
dofCES <- summaryCES$df[2]</pre>
print(dofCES) # Gives the degrees of freedom for the model.
tvalCES <- qt(ciHalfLevel, df = dofCES); tvalCES
# Get confidence intervals for each parameter in the model
alphaCICES <- with(alpha.est, Estimate + c(-1.0, 1.0) * tvalCES * SE) # CI on al
print(alphaCICES)
# Assemble the data into data frames for the table.
estCES <- data.frame(phi = coef(modelCES)["phi"], alpha = alpha,</pre>
                     beta = coef(modelCES)["beta"], zeta = coef(modelCES)["zeta"]
                     lambda_L = coef(modelCES)["lambda_L"], lambda_E = coef(modelCES)
row.names(estCES) <- paste("CES with ", energyType, sep="")</pre>
#print(estCES)
# The [1] subscripts pick off the lower confidence interval
lowerCES <- data.frame(phi = ciCES["phi","2.5%"], alpha = alphaCICES[1],</pre>
                        beta = ciCES["beta", "2.5%"], zeta = ciCES["zeta", "2.5%"
                        lambda_L = ciCES["lambda_L", "2.5%"], lambda_E = ciCES["]
row.names(lowerCES) <- "- 95% CI"
# The [2] subscripts pick off the lower confidence interval
upperCES <- data.frame(phi = ciCES["phi", "97.5%"], alpha = alphaCICES[2],
                       beta = ciCES["beta", "97.5%"], zeta = ciCES["zeta", "97.5
                       lambda_L = ciCES["lambda_L", "97.5%"], lambda_E = ciCES["]
row.names(upperCES) <- "+ 95% CI"
```

```
# Now create the data for a table.
 dataCES <- rbind(upperCES, estCES, lowerCES)</pre>
 print(dataCES)
 return(dataCES)
 #xyplot( resid(modelCESQ) ~ fitted(modelCESQ) )
 #histogram( ~resid(modelCESQ) )
 #qqmath( ~resid(modelCESQ) )
# Creates a LaTeX printable table from the CES data. This function first calls centered
# countryName is a string containint the 2-letter abbreviation for the country, e
# energyType is a string to be used in table captions reprsenting the type of ener
# returns a printable LaTeX table from xtable.
cesTable <- function(countryName, energyType){</pre>
 dataCESe <- cesData(countryName, energyType)</pre>
 tableCESq <- xtable(dataCESe, caption=paste(countryName, ", 1980-2011.", sep="")
3.1. CES with Q
```

```
countryName <- "US"
energyType <- "Q"
tableCESq <- cesTable(countryName, energyType)</pre>
[1] -194
Formula: iGDP ~ ((1 - zeta) * (exp(lambda_L * iYear) * iCapStk^(1 - beta) *
    iLabor^beta)^phi + zeta * (exp(lambda_E * iYear) * iQ)^phi)^(1/phi)
Parameters:
          Estimate Std. Error t value Pr(>|t|)
```

```
phi
        -3.96e+01 2.43e+01
                               -1.63 0.1144
beta
         6.09e-01 3.45e-02
                               17.64 2.4e-16
zeta
         2.09e-06 1.32e-05
                               0.16 0.8758
lambda_L 7.98e-03
                    6.68e-04
                               11.95 2.8e-12
lambda_E 8.57e-03
                    2.48e-03
                                3.45
                                       0.0018
Residual standard error: 0.0105 on 27 degrees of freedom
Algorithm "port", convergence message: relative convergence (4)
Waiting for profiling to be done...
                      97.5%
            2.5%
              NA -10.290831
phi
beta
        0.514667
                   0.665371
zeta
              NA
                         NA
lambda_L 0.006428
                  0.009152
lambda_E 0.000715
                   0.012468
        Estimate
                      SE
         0.3911 0.03453
1 - beta
[1] 27
[1] 0.3202 0.4619
             phi alpha
                                    zeta lambda_L lambda_E
                          beta
+ 95% CI
          -10.29 0.4619 0.6654
                                     NA 0.009152 0.012468
CES with Q -39.64 0.3911 0.6089 2.085e-06 0.007979 0.008570
- 95% CI
              NA 0.3202 0.5147
                                    NA 0.006428 0.000715
#CESqTables <- lapply(countries, cesTable, energyType="Q")</pre>
```

```
print(tableCESq, caption.placement="top")
```

```
#print(CESqTables[["US"]], caption.placement="top")
#print(CESqTables[["ZA"]], caption.placement="top")
```

Table 10: US, 1980-2011.

	phi	alpha	beta	zeta	lambda_L	lambda_E
+ 95% CI	-10.3	0.46	0.67		0.00915	0.01247
CES with Q	-39.6	0.39	0.61	0.000002	0.00798	0.00857
- 95% CI		0.32	0.51		0.00643	0.00071