

Spring 2021 6.884 Computational Sensorimotor Learning Assignment 1

In this assignment, we will learn about multi-armed and contextual bandits. You will need to [answer the bolded questions](#) and [fill in the missing code snippets \(marked by ****TODO****\)](#).

There are 255 total points in this assignment, scaled to be worth 6.25% of your final grade.

Setup

Ignore the following skeleton code (imports, plotting).

```
In [17]: %matplotlib inline
import numpy as np
import random
import time
import os
import gym
import json
import matplotlib.pyplot as plt
import matplotlib as mpl
import seaborn as sns
import pandas as pd

from copy import deepcopy
from tqdm.notebook import tqdm
from dataclasses import dataclass
from typing import Any
mpl.rcParams['figure.dpi'] = 100
```

```
In [19]: # some util functions
def plot(logs, x_key, y_key, legend_key, **kwargs):
    nums = len(logs[legend_key].unique())
    palette = sns.color_palette("hls", nums)
    if 'palette' not in kwargs:
        kwargs['palette'] = palette
    ax = sns.lineplot(x=x_key, y=y_key, data=logs, hue=legend_key, **kwargs)
    return ax

def set_random_seed(seed):
    np.random.seed(seed)
    random.seed(seed)

# set random seed
seed = 0
set_random_seed(seed=seed)
```

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Multi-armed bandits

Let us define a multi-armed bandit scenario with 10 arms. There are two slightly different formulations that are useful:

- Stochastic Case: Each arm has a reward of 1, with probability $p \in [0, 1]$.
- Deterministic Case: Each arm has a reward $r \in [0, 1]$, but the same reward is obtained for every pull.

In this assignment, we will work through the stochastic case. The same insights would apply to the deterministic scenario with variable rewards or even to stochastic setups with variable rewards.

To define our bandit, we arbitrarily select probabilities p for each arm and save them as `probs`.

```
In [22]: numArms = 10
         set_random_seed(1000)
         probs = [np.random.random() for i in range(numArms)]
         print(probs)

[0.6535895854646095, 0.11500694312440574, 0.9502828643490245, 0.4821914014279
982, 0.8724745351820353, 0.21233268092271995, 0.040709624769089126, 0.3971944
613457058, 0.23313219734837998, 0.8417407242530616]
```

We then define an environment to evaluate different agent strategies.

```
In [23]: #To simulate a realistic Bandit scenario, we will make use of the BanditEnv.
         @dataclass
         class BanditEnv:
             probs: np.ndarray # probabilities of giving positive reward for each arm

             def step(self, action):
                 # Pull arm and get stochastic reward (1 for success, 0 for failure)
                 return 1 if (np.random.random() < self.probs[action]) else 0
```

```
In [24]: #Code for running the bandit environment.
@dataclass
class BanditEngine:
    probs: np.ndarray
    max_steps: int
    agent: Any

    def __post_init__(self):
        self.env = BanditEnv(probs=self.probs)

    def run(self, n_runs=1):
        log = []
        for i in tqdm(range(n_runs), desc='Runs'):
            run_rewards = []
            run_actions = []
            self.agent.reset()
            for t in range(self.max_steps):
                action = self.agent.get_action()
                reward = self.env.step(action)
                self.agent.update_Q(action, reward)
                run_actions.append(action)
                run_rewards.append(reward)
            data = {'reward': run_rewards,
                    'action': run_actions,
                    'step': np.arange(len(run_rewards))}
            if hasattr(self.agent, 'epsilon'):
                data['epsilon'] = self.agent.epsilon
            run_log = pd.DataFrame(data)
            log.append(run_log)
        return log
```

```
In [25]: #Code for aggregating results of running an agent in the bandit environment.
def bandit_sweep(agents, probs, labels, n_runs=2000, max_steps=500):
    logs = dict()
    pbar = tqdm(agents)
    for idx, agent in enumerate(pbar):
        pbar.set_description(f'Alg:{labels[idx]}')
        engine = BanditEngine(probs=probs, max_steps=max_steps, agent=agent)
        ep_log = engine.run(n_runs)
        ep_log = pd.concat(ep_log, ignore_index=True)
        ep_log['Alg'] = labels[idx]
        logs[f'{labels[idx]}'] = ep_log
    logs = pd.concat(logs, ignore_index=True)
    return logs
```

Credits: The code for Multi-Arm Bandits is inspired from

- https://github.com/ShangtongZhang/reinforcement-learning-an-introduction/blob/master/chapter02/ten_armed_testbed.py (https://github.com/ShangtongZhang/reinforcement-learning-an-introduction/blob/master/chapter02/ten_armed_testbed.py)
- <https://github.com/lilianweng/multi-armed-bandit/blob/master/solvers.py> (<https://github.com/lilianweng/multi-armed-bandit/blob/master/solvers.py>)

Oracle Agent

The best agent we could possibly build is one that has access to all the necessary information to make an optimal decision, even if that information would not be available in a real world problem. We call this an "oracle agent."

Imagine you were to build an Oracle agent for the stochastic multi-armed bandits problem defined by `probs`. What reward would you get from this agent in expectation?

```
In [26]: ##### TODO: find the maximum return with privileged information about the reward distribution [5pts] #####
# oracle_decision = np.argmax(probs)
oracleReward = max(probs)
#####
print (f'Max possible reward {oracleReward}')
```

Max possible reward 0.9502828643490245

Random Agent

That's pretty high reward! However, let's say that we don't have access to `probs`, and that the only information we can learn about the environment is through interaction. This is more akin to a real world bandits problem.

One baseline agent we should construct is one that chooses a random action at every timestep. Fill in the `TODO` in the below agent code to implement this behavior.

```
In [27]: #As a baseline, lets first construct a baseline agent that chooses a random ac
tion at every timestep.
#We will measure how much better we can do.
@dataclass
class RandomAgent:
    num_actions: int

    def __post_init__(self):
        self.reset()

    def reset(self):
        self.t = 0
        self.action_counts = np.zeros(self.num_actions, dtype=np.int) # action
counts n(a)
        self.Q = np.zeros(self.num_actions, dtype=np.float) # action value Q
(a)

    def update_Q(self, action, reward):
        pass

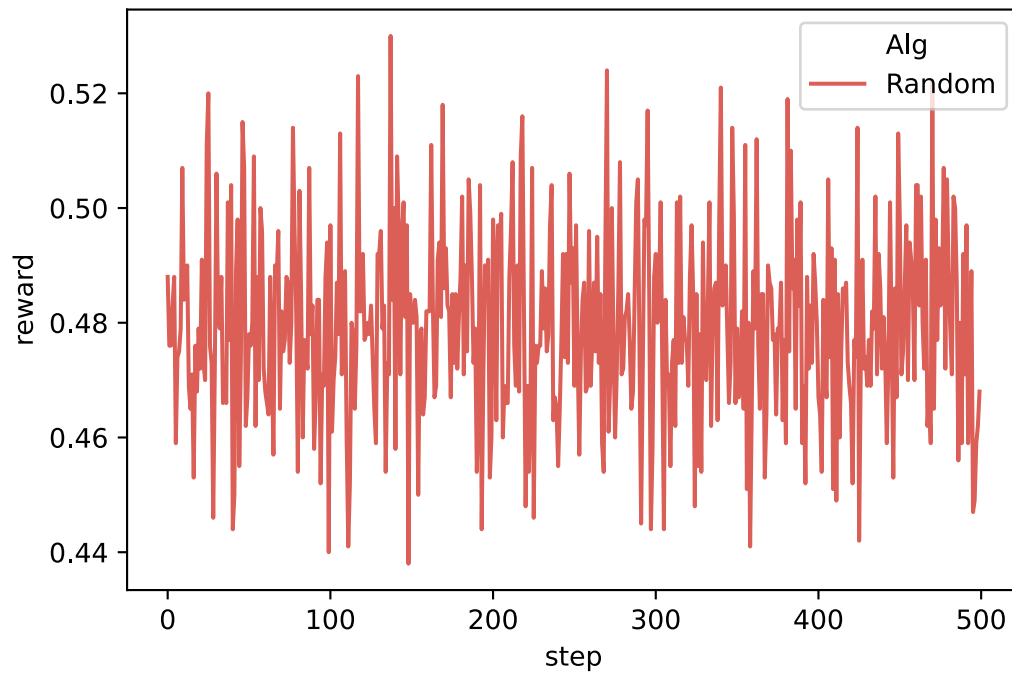
    def get_action(self):
        self.t += 1
        ##### TODO: get a random action index [5pts]####
        selected_action = np.random.randint(low = 0, high = self.num_actions)
# placeholder
        #####

    return selected_action
```

```
In [28]: #Create the random agent.
agent = RandomAgent(num_actions=len(probs))
'''
In order to measure average behavior of the agent, we are going to run the age
nt
multiple times and compute the mean reward. The number of runs will be denoted
by the variable `n_runs`. The default value is set to 1000, but feel free to r
educe it
it if its taking too much time.
'''
n_runs = 1000
logs = bandit_sweep([agent], probs, ['Random'], n_runs=n_runs)
```

```
In [29]: plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', ci=None)
```

```
Out[29]: <matplotlib.axes._subplots.AxesSubplot at 0x20bc878ceb0>
```



```
In [30]: np.mean(probs)
```

```
Out[30]: 0.47986550181870297
```

```
In [31]: ##### TODO: plot the reward curve of a random agent, and the average reward of
all arms [5pts]#####
logs
#####
```

Out[31]:

	reward	action	step	Alg
0	0	9	0	Random
1	1	2	1	Random
2	0	8	2	Random
3	0	4	3	Random
4	0	5	4	Random
...
499995	0	6	495	Random
499996	0	8	496	Random
499997	1	4	497	Random
499998	1	4	498	Random
499999	1	0	499	Random

500000 rows × 4 columns

Analyzing the Results:

- On the x-axis is the number of steps taken by the agent.
- On the y-axis is the average reward after i steps.

The reward obtained by the random agent is far less than the oracle agent. Regret is defined as the difference between the the reward collected by oracle and the agent under consideration. In the above example, regret is about 0.35.

Note: that if you use a different random seed to run experiments, you might get a slightly different value of regret. Treat this as a ball park figure.

Explore First Agent

In the class we discussed an algorithm to solve bandits where,

- For the first N (defined as `max_explore` in the code) steps the agent takes random actions.
- The agent identifies the best arm based on these N steps and then only chooses the best arm.

We will now implement this agent below. Fill in the missing code in `update_Q` and `get_action`. We will store the average reward for each action in the variable `self.Q`, and the count of how many times we've taken each action in `self.action_counts`.

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```

In [32]: #Lets now construct the explore first agent
@dataclass
class ExploreFirstAgent:
    num_actions: int
    max_explore: int

    def __post_init__(self):
        self.reset()

    def reset(self):
        self.t = 0
        self.action_counts = np.zeros(self.num_actions, dtype=np.int) # action
counts n(a)
        self.Q = np.zeros(self.num_actions, dtype=np.float) # action value Q
(a)

    def update_Q(self, action, reward):
        # Update Q action-value given (action, reward)
        # HINT: Keep track of how good each arm is
        ##### TODO: update Q value [5pts] #####
        if self.t <= self.max_explore:
            self.action_counts[action] += 1
            self.Q[action] = (self.Q[action]*(self.action_counts[action]-1) +
reward)/self.action_counts[action]

        #####

    def get_action(self):
        self.t += 1
        ##### TODO: get action [5pts] #####
        if self.t <= self.max_explore:
            selected_action = np.random.randint(low = 0, high = self.num_actio
ns)
        else:
            selected_action = np.random.choice(np.where(self.Q == self.Q.max
())[0])
        #####

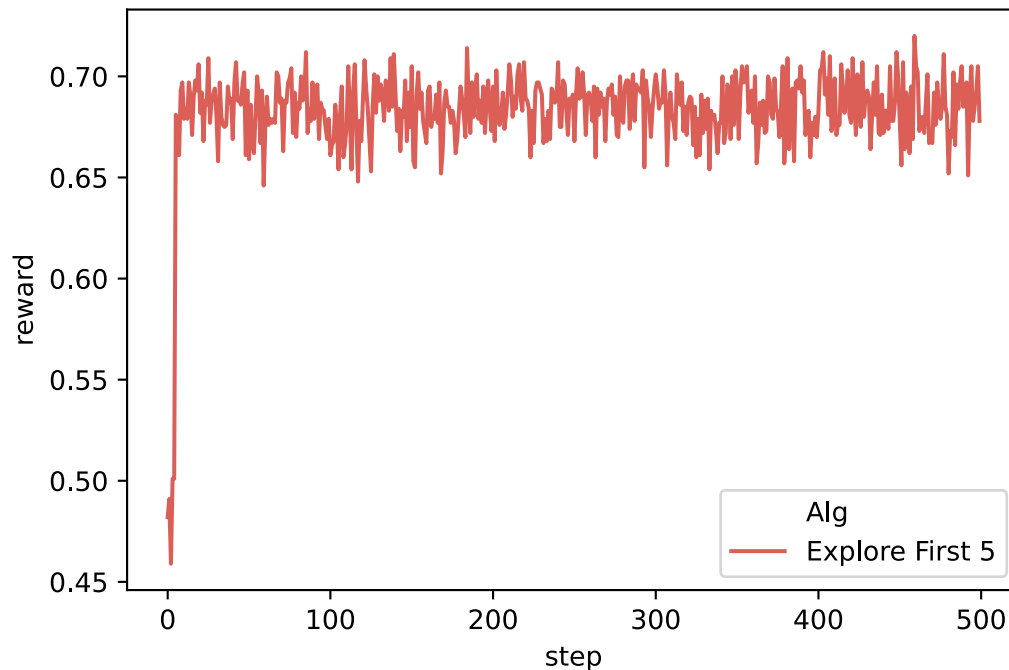
        return selected_action

```

Great! Now we'll instantiate the engine, and run it with $N = 5$ (five steps of exploration, followed by entirely greedy policy).


```
In [33]: agent = ExploreFirstAgent(num_actions=len(probs), max_explore=5)
logs = bandit_sweep([agent], probs, ['Explore First 5'], n_runs=1000, max_steps=500)

ax = plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', ci=None)
```



```
In [34]: plt.show()
```

Explore First v.s. Random Agent

The results clearly show that the explore first agent performs better than the random agent. However, it still performs much worse than the oracle. How can we improve our performance?

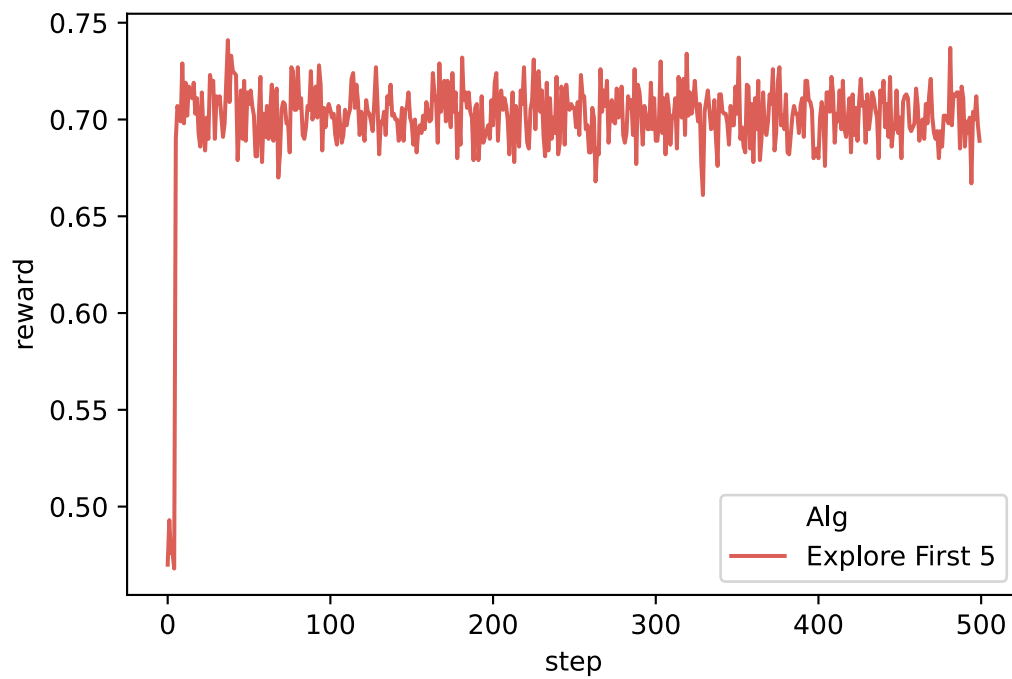
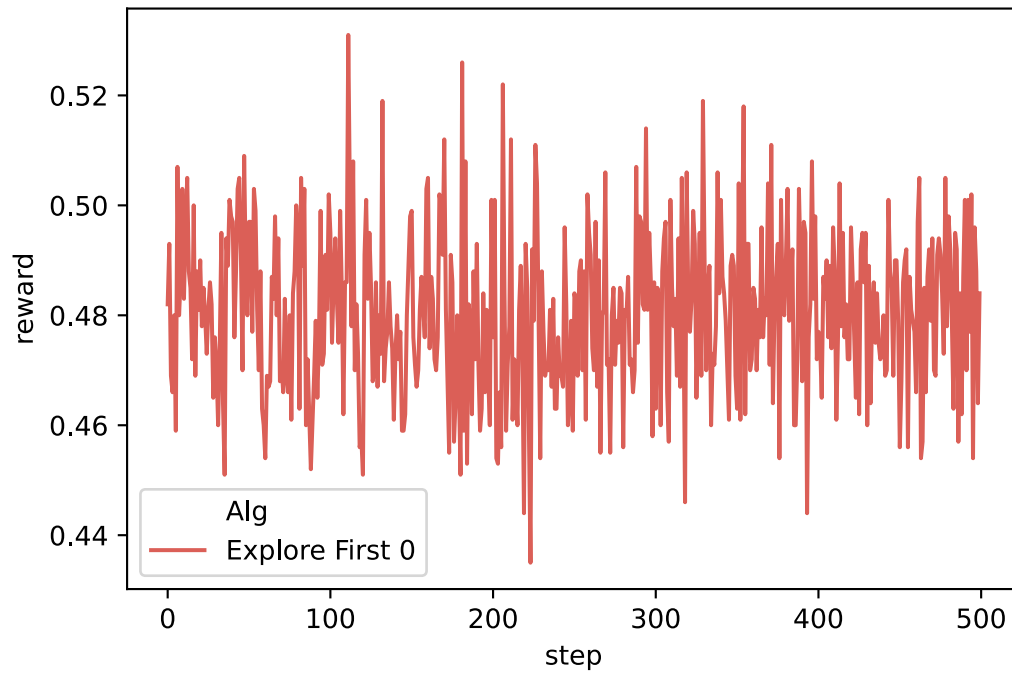
If there are 10 possible actions but the agent only explores for 5 steps, then it is likely it won't find the best arm. Thus, the policy will be suboptimal. Let's see what happens when we allow the agent to explore for more steps.

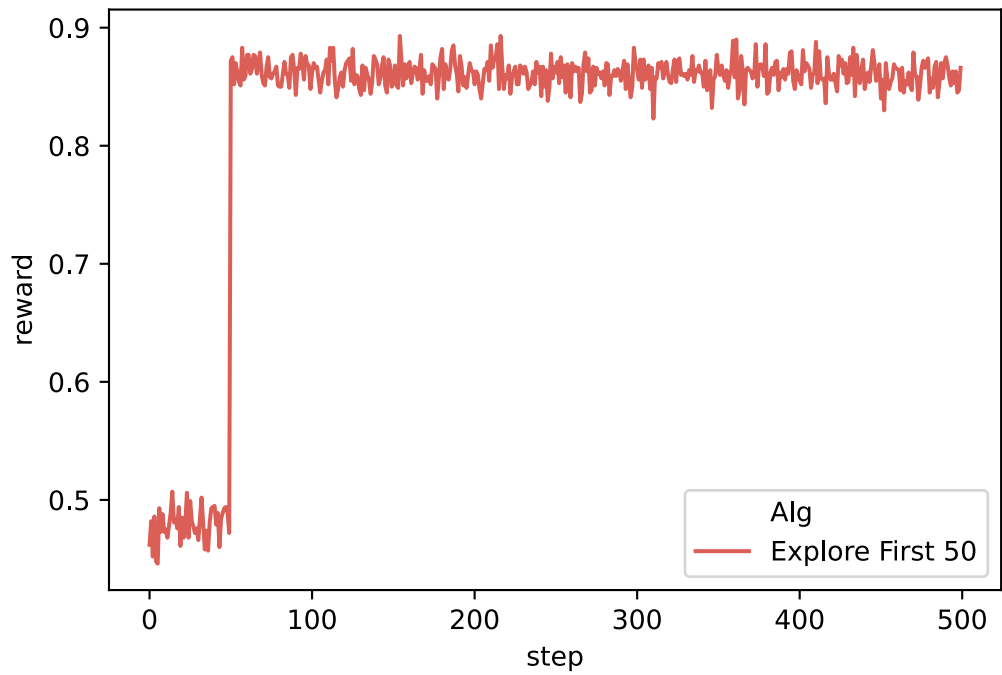
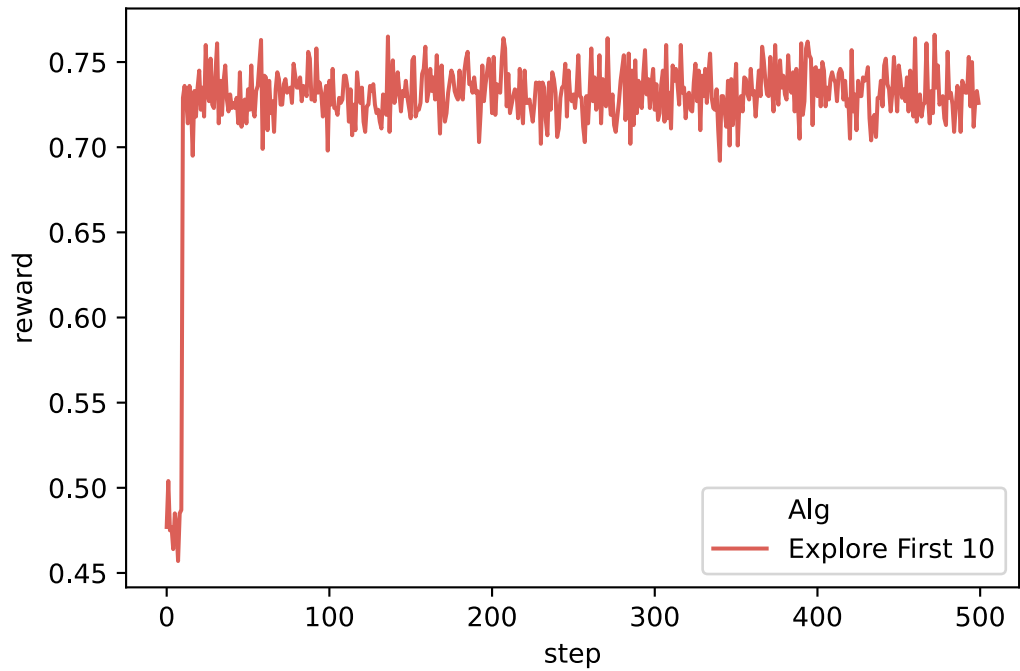
```

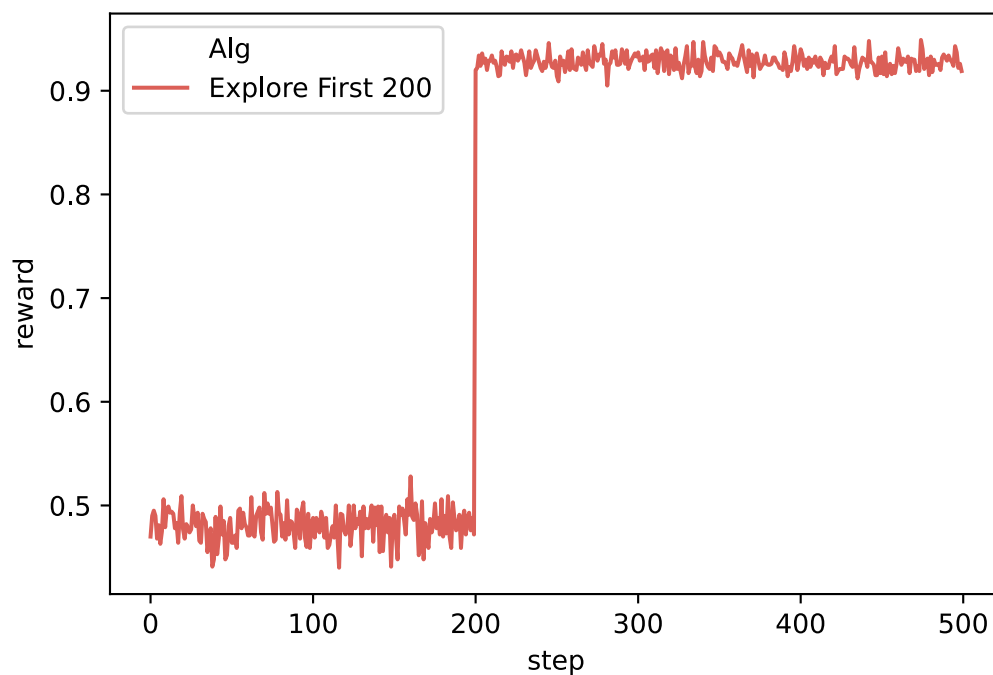
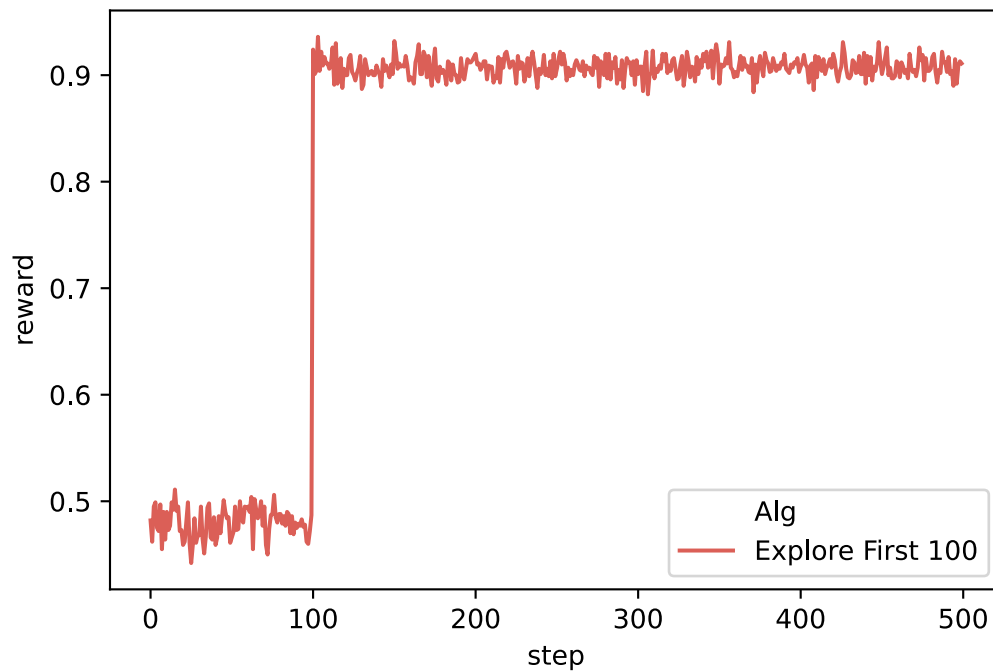
In [35]: '''
What happens if we allow the agent to explore for only 5, 10, 50, 100, 200 steps respectively?
'''

max_explore_steps = [0, 5, 10, 50, 100, 200]
n_runs = 1000
#### TODO: run ExploreFirstAgent with different max_explore steps, and plot the reward curves [10pts]####
for max_explore in max_explore_steps:
    agent = ExploreFirstAgent(num_actions=len(probs), max_explore = max_explore)
    logs = bandit_sweep([agent], probs, ['Explore First ' + str(max_explore)],
n_runs=1000, max_steps=500)
    plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', ci=None)
    plt.show()
#####

```







Analyzing the Results

- Notice that for all agents there is a jump in performance. This corresponds to the time point when they switch from explore only to exploit mode.
- The agents that explore for 5, 10 steps are unable to accurately identify the best arm everytime. Their scores are lower than that of agents exploring for 50 or 100 steps. These agents find the optimal arm.

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UCB Agent

Rather than having a fixed delineation between exploration and exploitation, an agent should be able to figure out when to explore and when to exploit. This leads us to the UCB agent that we discussed in class.

Implement the `update_Q` and `get_action` methods for a UCB agent using the course notes.

Moving to More Realistic Scenarios

Question (5pts): It's unclear how long the agent should explore before switching to exploit mode. Can you come up with a strategy to choose a good value of `max_explore`? Can we use such a strategy to deploy a product?

Answer: A good way could be probably picking `max_explore` as to maximize the total expected rewards. In some scenarios probably it is ok to deploy a product when the action space is discrete, limited, and not change after deployment. In other scenarios there will be problematic to deploy.

```
In [36]: ##### UCB Agent #####
@dataclass
class UCBAgent:
    num_actions: int

    def __post_init__(self):
        self.reset()

    def reset(self):
        self.t = 0
        self.action_counts = np.zeros(self.num_actions, dtype=np.int) # action
counts n(a)
        self.Q = np.zeros(self.num_actions, dtype=np.float) # action value Q
(a)

    def update_Q(self, action, reward):
        # Update Q action-value given (action, reward)
        ##### TODO: Calculate the Q-value [5pts] #####
        self.action_counts[action] += 1
        self.Q[action] = (self.Q[action]*(self.action_counts[action]-1) + reward)/self.action_counts[action]

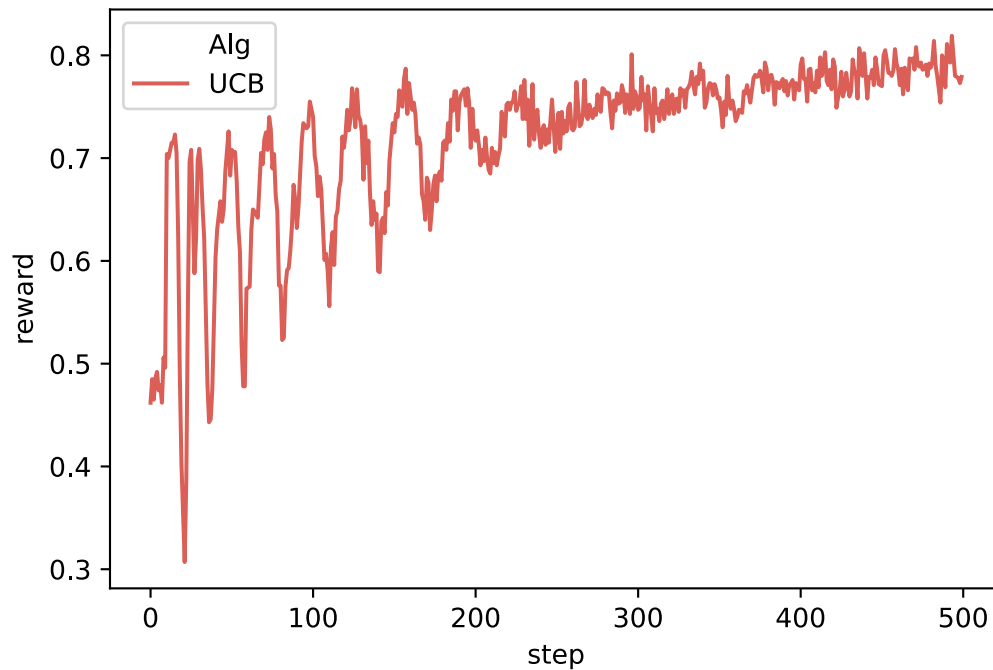
        #####

    def get_action(self):
        self.t += 1
        ## HINT: To avoid a division by zero, you can add a small delta>0 to the denominator
        ##### TODO: Calculate the exploration bonus [5pts] #####
        exploration_bonus = np.sqrt(4*np.log(self.t)/(self.action_counts+0.05)) # placeholder
        #####
        Q_explore = self.Q + exploration_bonus
        return np.random.choice(np.where(Q_explore == Q_explore.max())[0])
```

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```
In [37]: #Define the UCB Agent
agentUCB = UCBAgent(num_actions=len(probs))
#Compute Performance
logs = bandit_sweep([agentUCB], probs, ['UCB'], n_runs=1000, max_steps=500)
#Plot Performance
plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', ci=None)
```

Out[37]: <matplotlib.axes._subplots.AxesSubplot at 0x20bc8ae18b0>



UCB v/s Explore-First

Now let's compare the reward curves of the UCB agent and Explore First agent with `max_explore=5`.

Analyzing the Results

Question [5pts]: Why does the UCB algorithm learn slowly (even after 500 steps, the agent still does not reach the maximum reward)?

Answer: Because the Q-value is not constant compared with Explore-first algorithm, and with the inclusion of exploration bonus the optimal choice will possibly change over time

If you are willing to afford the risk of missing out on the optimal policy, one could terminate the exploration bonus in UCB after some time. This hybrid between UCB and Explore-First could work better for your use case. However, remember that UCB requires no tuning because it assumes no extra knowledge about the system. But, this comes at a cost -- if you have extra knowledge, you can achieve better performance than UCB! How to incorporate this knowledge depends on the nature of available information.


```

In [38]: #Now we will compare the UCB agent against the ExploreFirst Agent that only ex
         plores for 5 steps.
         ##### TODO: run both algorithms and plot the reward curves (max_explore=5) [10p
         ts] #####
         ##### use legends ['UCB', 'Explore First 5'] respectively
         ##### run each algorithm 1000 times (n_runs=1000), and max_steps=1000
         agentUCB = UCBAgent(num_actions=len(probs))
         agentfirst5 = ExploreFirstAgent(num_actions=len(probs), max_explore = 5)

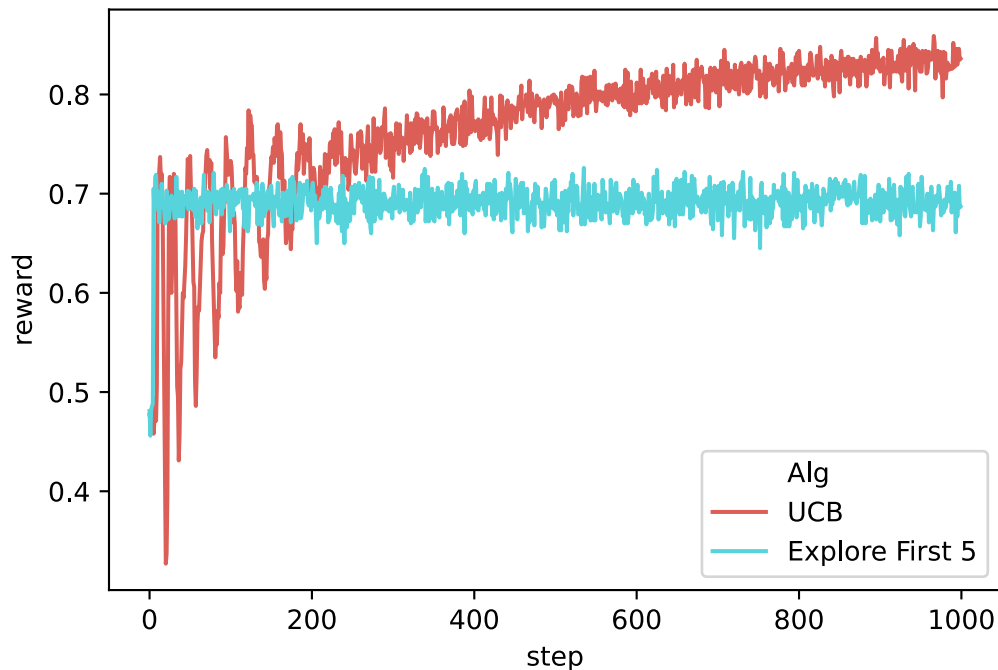
         logs = bandit_sweep([agentUCB, agentfirst5], probs, ['UCB', 'Explore First 5'
         ], n_runs=1000, max_steps=1000)

         plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', c
         i=None)

         #####

```

Out[38]: <matplotlib.axes._subplots.AxesSubplot at 0x20bc83a7a00>



Result Analysis: UCB outperforms the greedy Explore First agent that only explores for 5 steps.

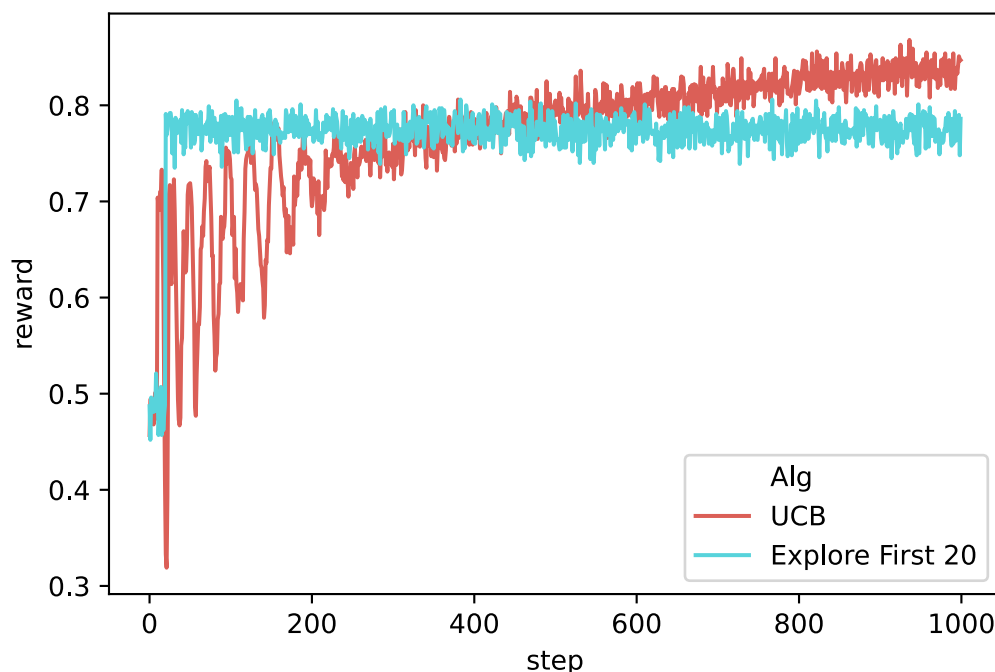
What happens if we allow the agent to explore for more steps? Run the Explore First agent for 20 steps, and compare the reward to the UCB agent.

```
In [29]: #Lets compare UCB with an agent that explores for twenty steps.
##### TODO: run both algorithms and plot the reward curves (max_explore=20) [10
pts] #####
##### use legends ['UCB', 'Explore First 20'] respectively
##### run each algorithm 1000 times (n_runs=1000), and max_steps=1000
agentUCB = UCBAgent(num_actions=len(probs))
agentfirst5 = ExploreFirstAgent(num_actions=len(probs), max_explore = 20)

logs = bandit_sweep([agentUCB, agentfirst5], probs, ['UCB', 'Explore First 2
0'], n_runs=1000, max_steps=1000)

plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', c
i=None)
#####
```

Out[29]: <matplotlib.axes._subplots.AxesSubplot at 0x2dd910cf100>



Question: In the lecture we studied that the UCB algorithm is optimal. Why then does Explore First perform better?*

Answer:

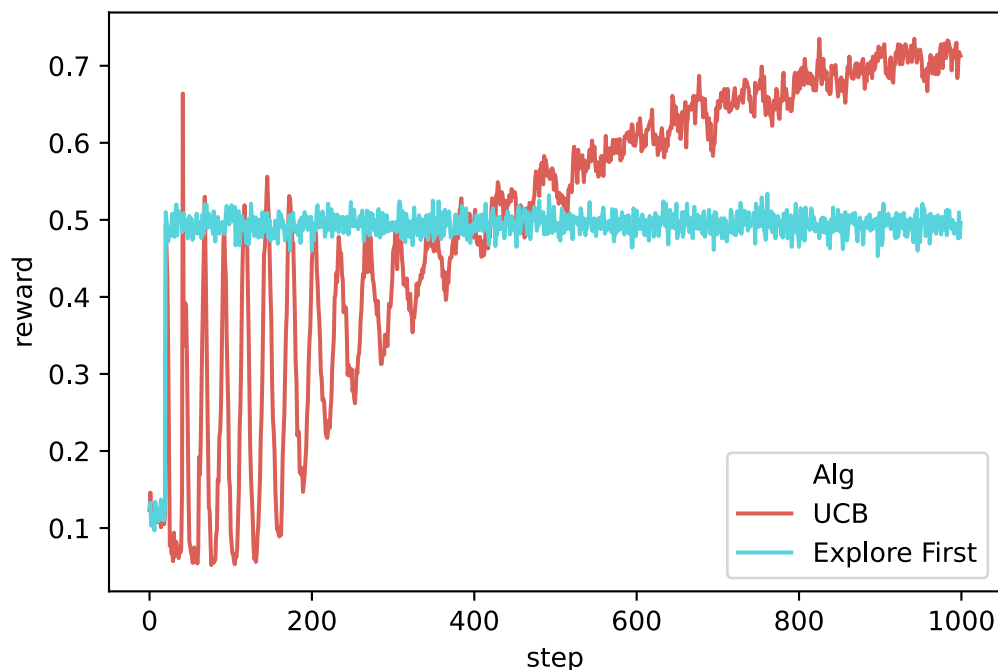
Skewed Arms Scenario:

In the previous example, the probability of each arm providing a return was sampled uniformly from $[0, 1]$. Because there were only 10 arms, and some arms had similar returns, by performing 20 random actions it is possible to find the best arm by chance. However, if the reward distributions are very skewed (e.g., only one arm returns rewards with high probability, say 0.9), or there are more arms, more actions may be necessary. In this case the initial exploration phase may not succeed at finding the best arm. Lets see this in practice below.

```
In [30]: skewedProbs = [0.1, 0.2, 0.15, 0.21, 0.3, 0.05, 0.9, 0.13, 0.17, 0.07, 0.01,
0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01, 0.01]
##### TODO: compare the reward curves of UCBAgent and ExploreFirstAgent (max_ex
plore=len(skewedProbs)) [10pts] #####
##### sweep with n_runs=1000, max_steps=1000

agentUCB = UCBAgent(num_actions=len(skewedProbs))
agentexplore = ExploreFirstAgent(num_actions=len(skewedProbs),max_explore=len(
skewedProbs))
logs = bandit_sweep([agentUCB, agentexplore], skewedProbs, ['UCB', 'Explore F
irst'], n_runs=1000, max_steps=1000)
plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', c
i=None)
#####
#####
```

Out[30]: <matplotlib.axes._subplots.AxesSubplot at 0x2dd91045fd0>



In this case, UCB performs better than *Explore First (20)*. It is because exploring for 20 steps is insufficient for this problem. This problem again illustrates that unless one has access to privileged information about the problem, UCB performs the best!

Also notice that UCB's reward is still increasing and it hasn't converged to the optimal action yet. Try varying the maximum number of steps to see when UCB converges to the optimal / oracle policy.

In other words, `max_explore` is a hyperparameter. Without "tuning" it, the method may perform well on some problem instances and poorly on others. An advantage of UCB is its lack of hyperparameters. Next, we'll consider another hyperparameter, ϵ .

Epsilon-greedy Agent

Another popular method of simultaneously exploring/exploiting is ϵ -greedy exploration. The main idea is to:

- Sample the (estimated) best action with probability $1 - \epsilon$
- Perform a random action with probability ϵ

By changing ϵ , we can control if the agent is conservative or exploratory. We will now implement this agent.

```

In [39]: ##EpsilonGreedy Agent
@dataclass
class EpsilonGreedyAgent:
    num_actions: int
    epsilon: float = 0.1

    def __post_init__(self):
        self.reset()

    def reset(self):
        self.action_counts = np.zeros(self.num_actions, dtype=np.int) # action
counts n(a)
        self.Q = np.zeros(self.num_actions, dtype=np.float) # action value Q
(a)

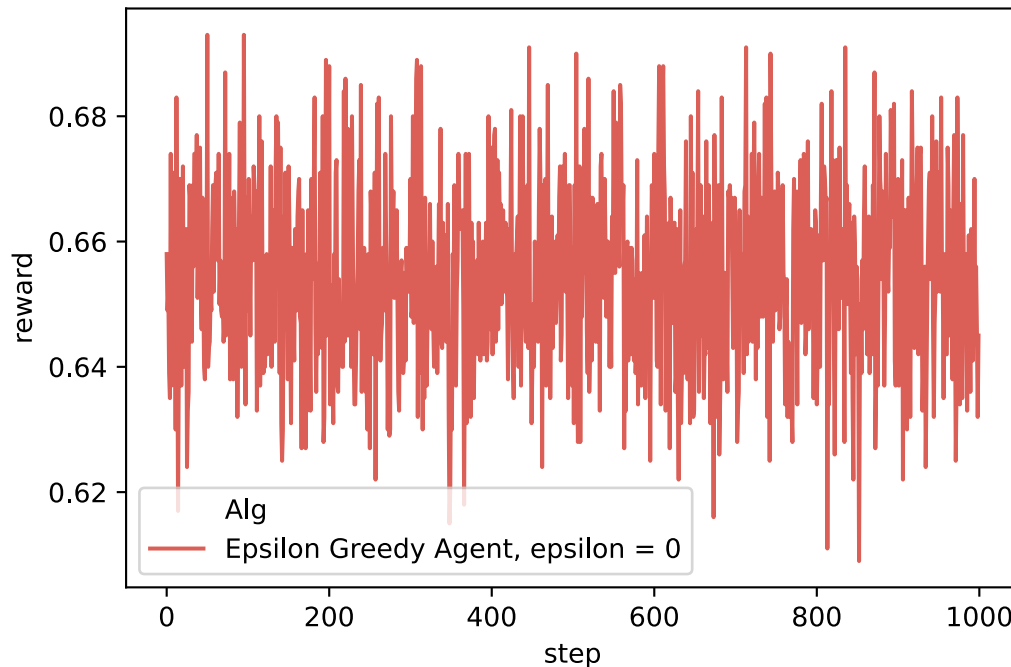
    def update_Q(self, action, reward):
        # Update Q action-value given (action, reward)
        self.action_counts[action] += 1
        self.Q[action] += (1.0 / self.action_counts[action]) * (reward - self.
Q[action])

    def get_action(self):
        # Epsilon-greedy policy
        ##### TODO: Code for exploration [5pts] #####
        if np.random.random() < self.epsilon:
            print('?')
            selected_action = np.random.randint(low = 0, high = self.num_actio
ns)
        else:
            selected_action = np.argmax(self.Q)
            #####
        return selected_action

```

```
In [43]: epsilonAgent = EpsilonGreedyAgent(num_actions=len(probs),epsilon=0)
logs = bandit_sweep([epsilonAgent], probs, ['Epsilon Greedy Agent, epsilon = '
      +str(epsilonAgent.epsilon)], n_runs=1000, max_steps=1000)
plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', ci=None)
```

Out[43]: <matplotlib.axes._subplots.AxesSubplot at 0x2dd92516880>



Analyzing Epsilon-Greedy Agents

Notice that the reward of all agents gradually increases (except for $\epsilon = 0$, which is an extremely greedy agent). Also, notice that reward is maximum for $\epsilon = 0.1$ but decreases for higher values.

Question [5pts]: Why is the reward lower for higher-values of ϵ ?

Answer: Because higher-values of ϵ means there are more steps are executed randomly instead of exploiting the information available

Question [5pts]: To overcome the issue above, one can try setting $\epsilon = 0$ after some time or adaptively changing ϵ . Can you suggest a strategy for varying ϵ with time T ?

Answer: Probably higher ϵ when T is small to explore enough and then decrease ϵ when the information is collected/the environment is explored enough

Consider: Compare ϵ -greedy with UCB and the tradeoffs.

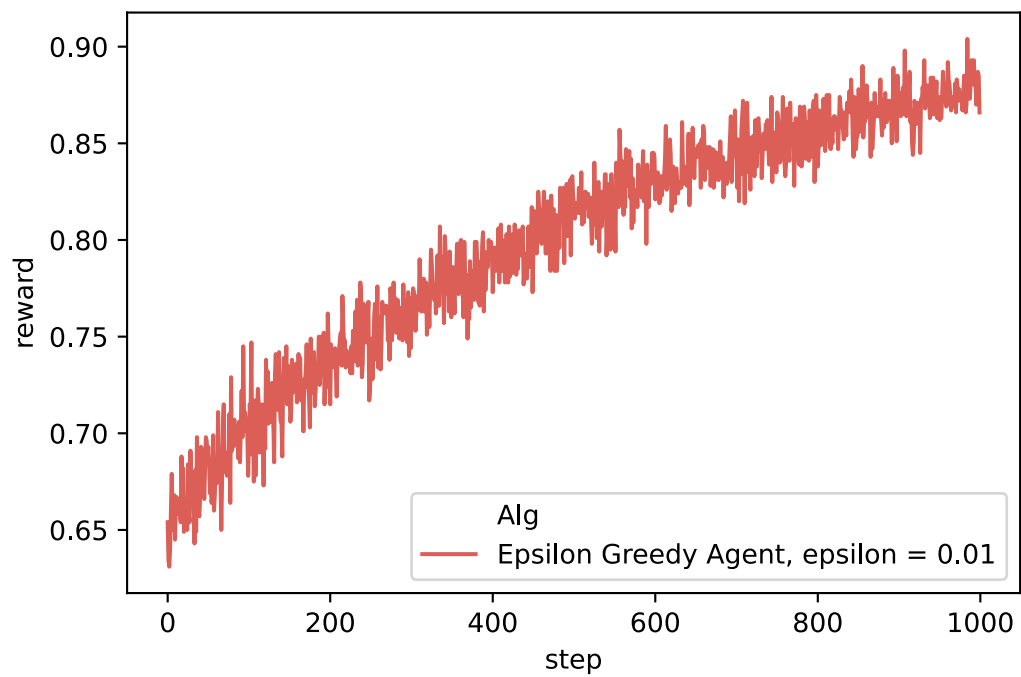
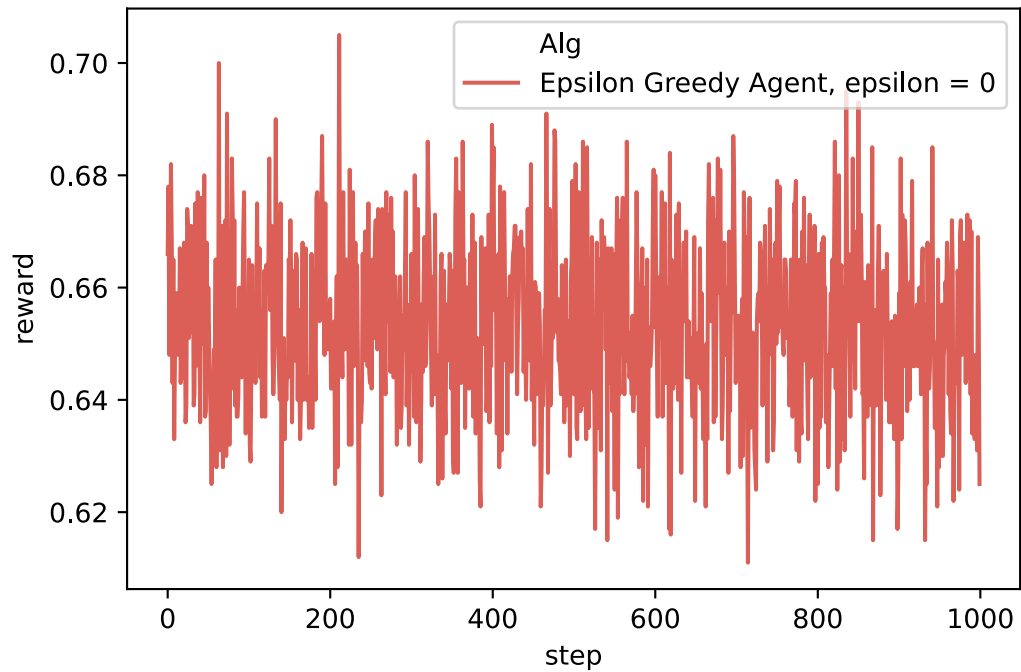
```
In [ ]: probs
```

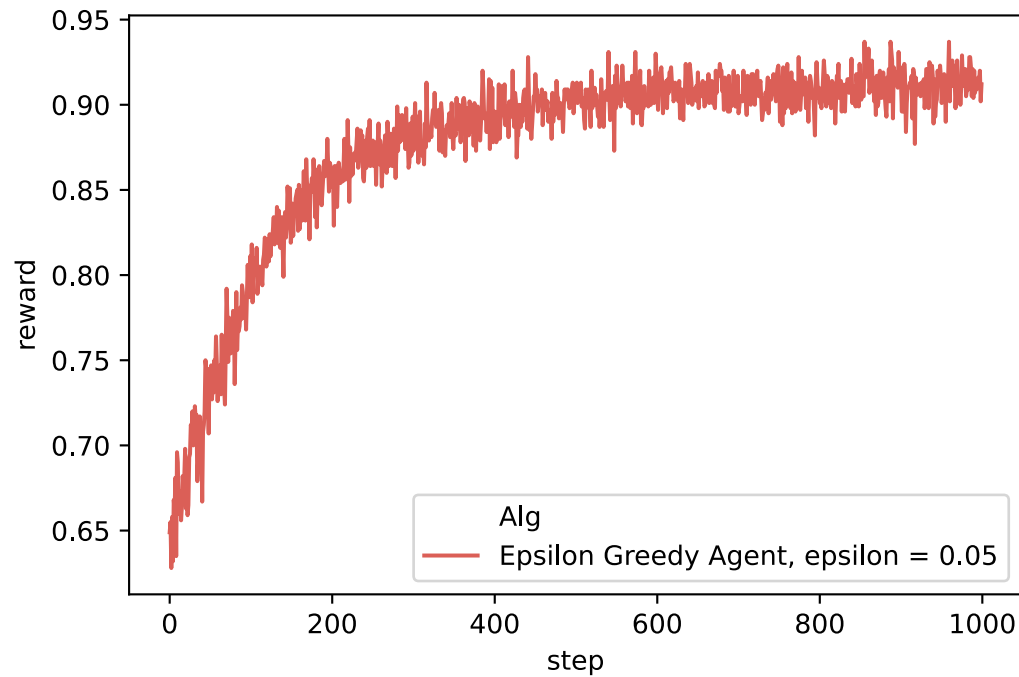
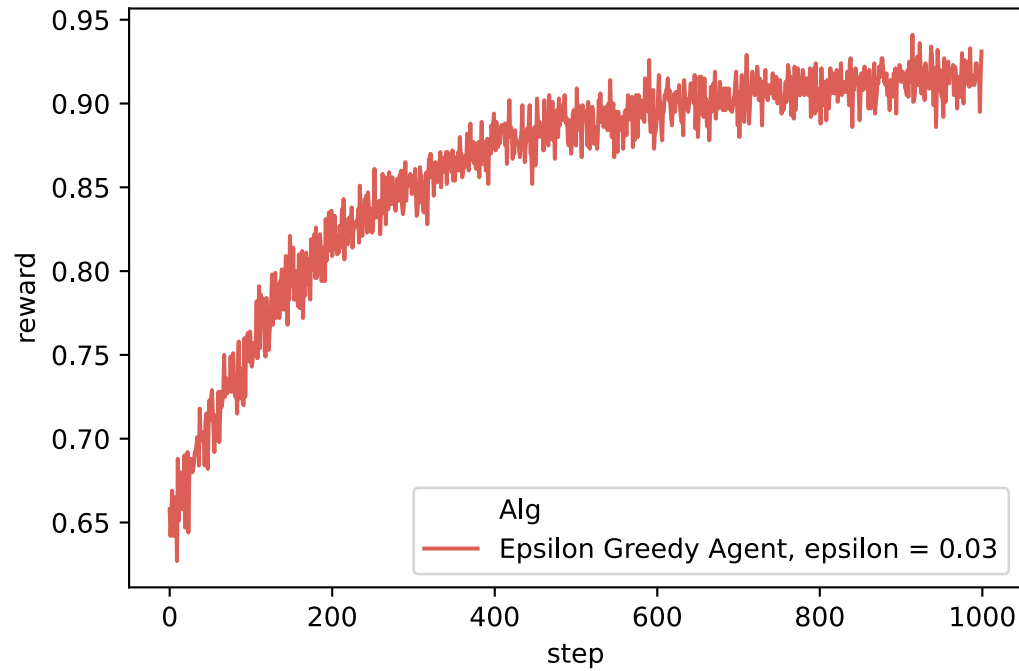
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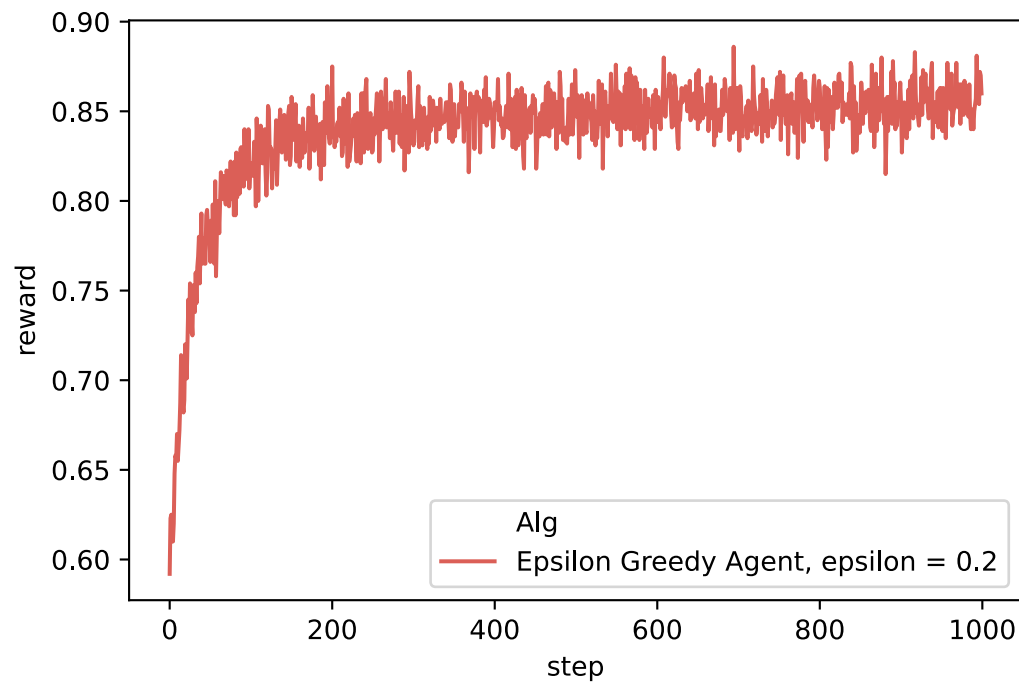
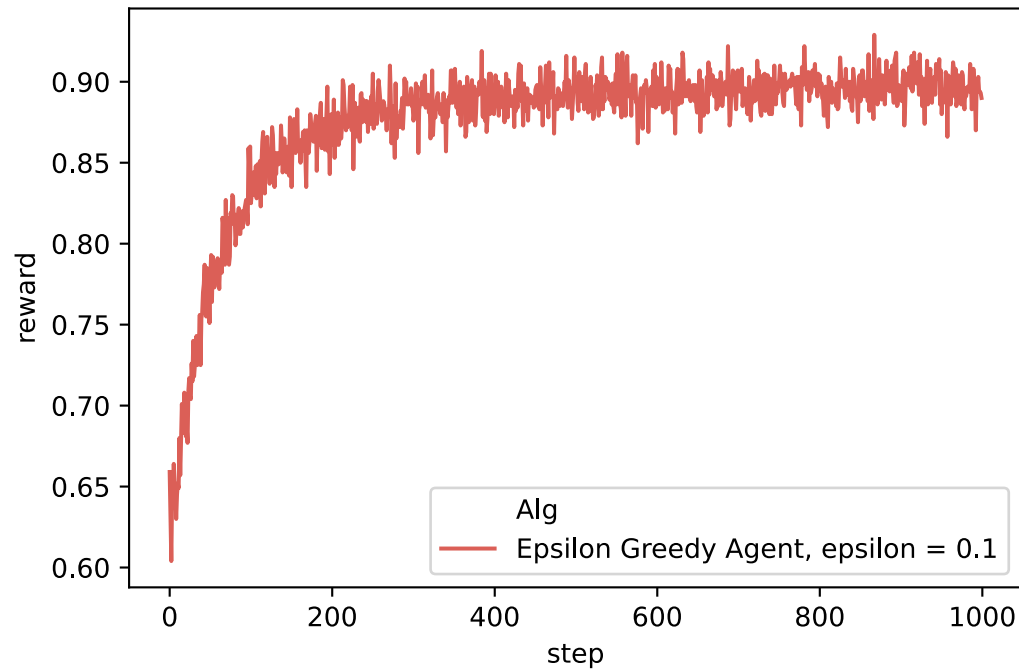
```
In [42]: ##### TODO: show reward curves of an EpsilonGreedyAgent with epsilon=[0, 0.1, 0.2, 0.4] [10pts]#####

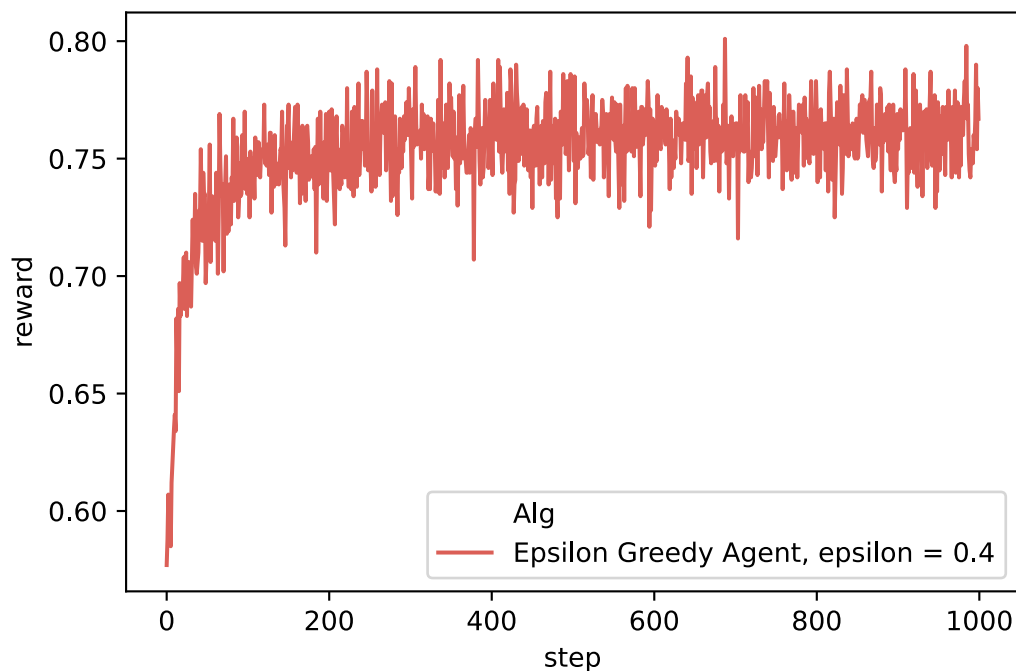
for epsilon in [0,0.01,0.03,0.05,0.1,0.2,0.4]:
    epsilonAgent = EpsilonGreedyAgent(num_actions=len(probs),epsilon=epsilon)
    logs = bandit_sweep([epsilonAgent], probs, ['Epsilon Greedy Agent, epsilon = '+str(epsilon)], n_runs=1000, max_steps=1000)
    plot(logs, x_key='step', y_key='reward', legend_key='Alg', estimator='mean', ci=None)
    plt.show()

#####
```









Contextual bandits

In this section, we will deal with contextual bandits problem. In contextual bandits, we use contextual information about the observed subject to make subject-specific decisions. The algorithm we will implement is called [LinUCB](https://arxiv.org/pdf/1003.0146.pdf) (<https://arxiv.org/pdf/1003.0146.pdf>).

As an example, imagine we have a website with 10 products that we'd like to promote. Whenever a user enters the website, the website promotes one product to the user. If the user clicks the product link, then it's a successful promotion (reward is 1). Otherwise, it's a failed promotion (reward is 0). Our goal is to optimize the click through rate (CTR), and thus optimize our \$\$\$.

We will use a dataset from [here \(http://www.cs.columbia.edu/~jebara/6998/dataset.txt\)](http://www.cs.columbia.edu/~jebara/6998/dataset.txt) to explore contextual bandits. The dataset contains a pre-logged array of shape [10000, 102]. Each row represents a data point at time step t where $t \in [0, 9999]$. The first column represents the index of the arm a_t that's chosen (10 arms in total). The second column represents the reward $r_t \in \{0, 1\}$ received for taking the selected arm. The last 100 columns represent the context feature vector.

The following code is inspired by [this code repository \(https://github.com/kfoofw/bandit_simulations\)](https://github.com/kfoofw/bandit_simulations).

[illegible]

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```
In [55]: # Load in the dataset
dataset = np.loadtxt('file.txt')
##### TODO: Load in the dataset.txt, and extract the data as a numpy array of shape [10000, 102] #####
```

```
Out[55]: (10000, 102)
```

```
In [65]: dataset[1, 2]
```

```
Out[65]: 1.0
```

```
In [56]: ##### Contextual bandit environment #####
@dataclass
class ContextualBanditEnv:
    dataset: Any
    t: int = 0

    def step(self, action):
        # if the action matches the recorded action in the dataset, it will
        # return the recorded reward in the dataset. Otherwise, it will return
        # a reward of None
        if action == self.dataset[self.t, 0]:
            reward = self.dataset[self.t, 1]
        else:
            reward = None
        self.t += 1
        return reward

    def reset(self):
        self.t = 0
```

Fill in the missing code below to implement the LinUCB agent.

```

In [2]: ##### LinUCB Agent #####
@dataclass
class LinUCBAgent:
    num_actions: int
    alpha: float
    feature_dim: int

    def __post_init__(self):
        self.reset()

    def reset(self):
        self.As = [np.identity(self.feature_dim) for i in range(self.num_actions)]
        self.bs = [np.zeros([self.feature_dim, 1]) for i in range(self.num_actions)]

    def get_ucb(self, action, state):
        ##### TODO: compute the UCB of the selected action/arm, and the context information [5pts] #####
        A = self.As[action]
        b = self.bs[action]
        theta = np.dot(np.linalg.inv(A), b)
        x = state.reshape((self.feature_dim, 1))

        p = np.dot(theta.T, x) + self.alpha * np.sqrt(np.dot(x.T, np.dot(np.linalg.inv(A), x)))
        return p[0,0]

    def update_params(self, action, reward, state):
        ##### update A matrix and b matrix given the observed reward, selected action, and the context feature #####
        if reward is None:
            return
        x = state.reshape((self.feature_dim, 1))
        self.As[action] += np.dot(x, x.T)
        self.bs[action] += reward * x
        return
        ##### TODO: update A and b matrices of the selected arm [5pts] #####

    def get_action(self, state):
        ##### find the action given the context information #####

        ##### TODO: get the UCB estimates for all actions [5pts] #####
        UCB_estimates = np.zeros(shape = self.num_actions)
        highest_ucb = -1
        candidate_arms = []

        for action in range(self.num_actions):
            UCB_estimates[action] = self.get_ucb(action, state)
            if UCB_estimates[action] > highest_ucb:
                highest_ucb = UCB_estimates[action]
                candidate_arms = [action]
            elif UCB_estimates[action] == highest_ucb:
                candidate_arms.append(action)

```

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```

        ##### TODO: choose an arm  $a_t = \arg\max_a(p_{t,a})$  with ties broken arbitrarily [5pts] #####

        selected_action = np.random.choice(candidate_arms) # placeholder

    return selected_action

```

NameError Traceback (most recent call last)

<ipython-input-2-6e871e5e759f> in <module>

```

1 ##### LinUCB Agent #####
----> 2 @dataclass
      3 class LinUCBAgent:
      4     num_actions: int
      5     alpha: float

```

NameError: name 'dataclass' is not defined

```

In [ ]: #Code for running the contextual bandit environment.
        @dataclass
        class CtxBanditEngine:
            dataset: Any
            agent: Any

            def __post_init__(self):
                self.env = ContextualBanditEnv(dataset=self.dataset)

            def run(self, n_runs=1):
                log = []
                for i in tqdm(range(n_runs), desc='Runs'):
                    # we only record the time steps when the selected arm matches the
                    arm in the pre-logged data
                    aligned_ctr = []
                    ret_val = 0
                    valid_time_steps = 0
                    self.env.reset()
                    self.agent.reset()
                    for t in tqdm(range(self.dataset.shape[0]), desc='Time'):
                        state=self.dataset[t, 2:]
                        action = self.agent.get_action(state=state)
                        reward = self.env.step(action)
                        self.agent.update_params(action, reward, state=state)
                        if reward is not None:
                            ret_val += reward
                            valid_time_steps += 1
                            aligned_ctr.append(ret_val / float(valid_time_steps))
                    data = {'aligned_ctr': aligned_ctr,
                           'step': np.arange(len(aligned_ctr))}
                    if hasattr(self.agent, 'alpha'):
                        data['alpha'] = self.agent.alpha
                    run_log = pd.DataFrame(data)
                    log.append(run_log)
                return log

```

```
In [ ]: #Code for aggregating results of running an agent in the contextual bandit environment.
def ctxbandit_sweep(alphas, dataset, n_runs=2000):
    logs = dict()
    pbar = tqdm(alphas)
    for idx, alpha in enumerate(pbar):
        pbar.set_description(f'alpha:{alpha}')
        agent = LinUCBAgent(num_actions=10, feature_dim=100, alpha=alpha)
        engine = CtxBanditEngine(dataset=dataset, agent=agent)
        ep_log = engine.run(n_runs)
        ep_log = pd.concat(ep_log, ignore_index=True)
        ep_log['alpha'] = alpha
        logs[f'{alpha}'] = ep_log
    logs = pd.concat(logs, ignore_index=True)
    return logs
```

```
In [ ]: ##### TODO: run the sweep with alpha = [0, 0.01, 0.1, 0.5] and n_runs=1 [5pts]
#####
ctxbandit_sweep(alphas = [0, 0.01, 0.1, 0.5], dataset = dataset, nruns = 1)

#####
```

```
In [ ]: plot(logs, x_key='step', y_key='aligned_ctr', legend_key='alpha', estimator='mean', ci=None)
```

Question [5pts]: What does α affect in LinUCB?

Answer:

Question [5pts]: Do the reward curves change with α ? If yes, why? If not, why not?

Answer:

```
In [ ]: ##### TODO: modify the UCB agent in the multi-armed bandits, and compare the
##### aligned_ctr curves between bandit, and contextual bandit with alpha as 0,
0.01, 0.5 [10pts] #####
```

Question [20pts]: Does LinUCB outperform UCB? If yes, explain why. If not, explain why not.

Answer:

In []: