

Pythagorean Identities

$$\sin^2 x + \cos^2 x = 1$$

$$1 + \tan^2 x = \sec^2 x$$

$$1 + \cot^2 x = \csc^2 x$$

Even/Odd Identities

$$\sin(-x) = -\sin(x)$$

$$\cos(-x) = \cos(x)$$

$$\tan(-x) = -\tan(x)$$

Co-Function Identities

$$\cos\left(\frac{\pi}{2} - x\right) = \sin(x)$$

$$\sin\left(\frac{\pi}{2} - x\right) = \cos(x)$$

$$\tan\left(\frac{\pi}{2} - x\right) = \cot(x)$$

$$\sec\left(\frac{\pi}{2} - x\right) = \csc(x)$$

$$\csc\left(\frac{\pi}{2} - x\right) = \sec(x)$$

$$\cot\left(\frac{\pi}{2} - x\right) = \tan(x)$$

Addition and Subtraction Identities

$$\begin{aligned}\sin(a + b) &= \sin(a)\cos(b) + \cos(a)\sin(b) \\ \sin(a - b) &= \sin(a)\cos(b) - \cos(a)\sin(b)\end{aligned}$$

$$\begin{aligned}\cos(a + b) &= \cos(a)\cos(b) - \sin(a)\sin(b) \\ \cos(a - b) &= \cos(a)\cos(b) + \sin(a)\sin(b)\end{aligned}$$

$$\tan(a + b) = \frac{\tan(a) + \tan(b)}{1 - \tan(a)\tan(b)}$$

$$\tan(a - b) = \frac{\tan(a) - \tan(b)}{1 + \tan(a)\tan(b)}$$

Double Angle Identities

$$\sin(2x) = 2\sin(x)\cos(x)$$

$$\cos(2x) = \cos^2(x) - \sin^2(x)$$

$$\tan(2x) = \frac{2\tan(x)}{1 - \tan^2(x)}$$

Half Angle Identities

$$\sin\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 - \cos(x)}{2}}$$

$$\cos\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 + \cos(x)}{2}}$$

$$\tan\left(\frac{x}{2}\right) = \frac{\sin(x)}{1 + \cos(x)} = \frac{1 - \cos(x)}{\sin(x)}$$

Law of Cosines

$$c^2 = a^2 + b^2 - 2ab\cos(C)$$

Law of Sines

$$\frac{a}{\sin(A)} = \frac{b}{\sin(B)} = \frac{c}{\sin(C)}$$

Triangle Area Formulas

$$\text{Area} = \frac{1}{2} ab\sin(C)$$

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

Angle Between Vectors \vec{u} and \vec{v}

$$\cos(\theta) = \frac{\vec{u} \cdot \vec{v}}{\|\vec{u}\| * \|\vec{v}\|}$$