Other types of locking-Snapshot locking

Bead A into All 读的时候不上锁 Bead B into Bl 读的时候不上锁 new values based on A1 and B1

Read Birds I 可能读了之后有人改了这个值,但你也不知道 any check or locks, just check the records that we need to If someone change values of A and B, inconsistency may arise write on, read records doesn't take any account into. A more relaxed lock, Reading operations are done without

write C3 to C
write D3 to D
write D3 to D
write D3 to D
commit
unlock(C and D)
e % not first modifier
C1 = C2
Unlock(C and D)
goto Loop

For optimistic lock: also slock A and slock B

throughput is very high compared to two phase locking scheme Snapshot Isolation method is used in Oracle but it will not guarantee Serializability. However, its transaction

end

Cons: It does not guarantee consistency (serializability). It executes transactions in a serial order, final output can be different if

writing locks are taken right before the 'commit' take place, hence the duration is shorter. 2.It allows multiple reading transactions run concurrently. Pros:1. Higher throughput: there is no locks on the unchanged values, hence such locking mechanism has less # of locks, and all

Other types of locking

Optimistic Locking When conflicts are rare, transactions can execute operations without managing locks and without waiting for locks - higher throughput(认为系统中没有conflict, 没有trans对一个shared resource 进行修改)

Use data without locks

Before committing

- each transaction verifies that no other transaction has modified the data (by taking appropriate locks)
- Brief locks may be needed at the end duration of locks are very short
- If any conflict found, the transaction repeats the attempt
- If no conflict, make changes and commit
- Loop内给只读的object也上锁(take read locks before commit)

of locking is very short but can force many repeated attempts due to failure of the condition. Once the condition is true – it is effectively 2 phase locking but duration

case many repeated attempts in the loop may need to be required, which changed by many transactions frequently, the conflict will arise, in which be better compared with dead lock. However, if some values are If conflict are rare, this technique is very efficient, and performance will



Unlock (all locks)

else abort

Commit Write A1 to A **Time Stamping**



time stamps are examined. If time stamp is more recent than the transaction read time the transaction is aborted. These are a special case of optimistic concurrency control. At commit,

Time Domain Versioning

Data is never overwritten a new version is created on update

<0,<V1, [t1, t2)>, <V2, [t2,t3)>, <V3,[t3,*)>

concurrency, recovery and time domain addressing. writes updates to durable media. This model of computation unifies At the commit time, the system validates all the transaction's updates and

We can track what transaction did before system down, which helps for crash recovery

Two phase locking transaction

Lock(X,A)

T2:	ntegrity constraint A+B \Rightarrow 0; A = 100; B = 100;	
T1: Loop: Read A to A1:	Integrity constraint	
T2:	constraint A+B >= 0; A = 100; B = $^{\circ}$	

Snapshot Isolation Transaction

constraint A+B >= 0; A = 100; B = 100; T2: Lock(S, A) Lock(X, B) Read A to A1; Read B to B1; B1 = B1 - 200; If (A1+B1 >= 0) Write B1 to B Commit else abort	Integrity constraint A+B >= 0: A = 100: B = 100: T1: T2: Loop: Read A to A1; Head B to B1; A3 = A1 -200; Lock(X, A) Lock(X, A) Head A to A2 if (A1 = A2) Unlock(A) Junlock(A) goto Loop goto Loop goto Loop with A3 + B1 >= 0) with A3 + B1 >= 0) With A3 + B1 >= 0 Wi	= 0; A = 100; B = 100; T2: Loop: Read A to A1; Loop: Read B to B1; B3 = B1 -200; Lock(X, B) Read B to B2 if (B1 = B2) Unlock(B) goto Loop elself (A1+ B3 >= 0) Write B3 to B
Lock(X,B) Read A to A1;	Read B to B1; A3 = A1 -200;	Read B B3 = B1
Read B to B1;	Lock(X, A)	Lock(X,
B1 = B1 -200;	Read A to A2	Read B
If $(A1 + B1 >= 0)$	if (A1 != A2)	if (B1 !=
Write B1 to B	Unlock(A)	Unlo
Commit	goto Loop	goto
else abort	elseif (A3+ B1 >= 0)	eiseir
end	Write A3 to A	Commit
Unlock (all locks)	Commit	else abort
	else abort	Unlock (all lo
	Unlock (all locks)	Officer (all locks)
(S)		
Only one transaction can commit.		

if (A1+B1 >= 0)

A1 = A1 - 200;Read B to B1; Read A to A1; Lock(S,B)

not be correct result if both trans commit. (A=-100, B=-100 for snapshot) If T1 commit, then in T2 the A1+B1 =-200<0 false, T2 cannot commit. But in snapshot final output of database will

by one if snapshot were used Inconsistency will arise if use snapshot, because the 'reading operation' has no locks. Therefore, we have to commit trans one

Other types of locks

Phantoms: They commonly occur when a transaction lock records/table but another transaction adds new records in that table

inserted some in the meantime So reading the same table twice by one transaction presents two different sets of records as the other has

Solution: 1. Predicate locks solve this problem. Rather than locking records, lock based on condition

Select * from Employee where salary > 80000

update the value within this range) this predicate range (only lock on specified range of records in table, other transaction cannot change or Another transaction will be able to insert new records in Employee table as long as the salary is not within

attributes.(要在属性值(工资)被排好序的前提下,不排序不能用) 2. Page Locks can solve this problem too. In this case, the storage should be organized based on values of

desirable condition of our database. inserting records. When we working on a certain subset of table, if the set changes or adding new records into it, then it is not a lock, and I have to manually check all list to find newly added students.) If I use phantom lock, it can prevent any other trans from the list, some more student just finish the enrollment.(In this case, I miss these new student if the system weren't used phantom When teacher wants to send emails to all students who are in the enroll list, when she is going to compose the email and send to

Time Stamping

from employee select average (salary) コ update employee set salary = salary*1.1

\$40000, T2 will be delayed until T1 finishes. But with time stamps T2 does not have to wait for If transaction T1 commences first and holds a read lock on a employee record with salary < where salary < \$40000

T1 to finish!

- Timestamp ordering assigns orders for transactions based on time of commencement
- Locking has some sort of order which is decided at object access time
- When there are many updates, two-phase locking is good as it has less aborts
- Timestamp-based methods abort immediately which may be good sometimes

Hence, there is no winner for all DBMSs for all types of data/queries.

based one. What is the implication of this difference? Briefly explain. Q What is the difference between a classical Optimistic Concurrency control mechanism versus a Snapshot Isolation-

Q What are the benefits of using snapshot isolation, compared to two-phase well-formed isolation? Also, give an example of an to frequent rollbacks, can be configured to provide stricter consistency at the cost of efficiency in high concurrency cases. so such method is unsuitable areas like banking systems where constraints involve multiple data points. In contrast, OCC is prone running concurrently, as one transaction may change the value that has been read by another transaction during their execution work may be discarded if inconsistency is detected at the end. Snapshot Isolation does not have any read locks and just check the contention system, the system may roll back frequently and many repeated attempts in the loop may be required because all application scenario where snapshot isolation can be useful over a two-phase well-formed isolation. Implication: Snapshot isolation transaction should be executed in a serial way, it cannot guarantee consistency when transactions records for writing operation, which can be seen as a more relaxed locking and tends to perform better in read-heavy systems throughput because it has short duration of locking only being taken before commit for some quick checks. Cons: In a high Ans:OCC:In validation phase, OCC add read locks (Slock) before commit.Pros: If conflicts are rare, this technique has higher

write conflicts result in transaction aborts, which is especially beneficial for applications with frequent reads and fewer writes. occasional updates by an administrator (e.g., changes to product descriptions or stock levels) have minimal impact on users' In an e-commerce platform's product catalog, especially during off-peak seasons, Snapshot Isolation offers advantages because 2PWF restricts concurrency more due to the shared lock and exclusive locks held until commit, which can limit the number of Ans: SI provides a high level of concurrency by allowing multiple transactions to read the same data without conflict. Only write decisions. Multiple users can browse products simultaneously, while the administrator can modify product information (write simultaneous transactions.

Web browsing: if one is using=>then the web is locked, others are not able browse, leading to bad experience SI is more suitable for such read-dominant applications. of blocking. In read-heavy scenarios, this can lead to delays caused by write locks, resulting in degraded performance. Therefore What kind of applications use relaxed isolation? - Have you experienced any inconsistency in reading values as users? Well-Formed Isolation, all read operations require shared locks, and write operations need exclusive locks, increasing the chance operations) without considering any reading locks, avoiding delays for users and improving system efficiency. Under Two-Phase

use degree 1, they can read concurrently at any time.) Adding product to shopping coat, everybody can add this item into cart, but only one of them will be available. (We can

sometimes, we've paid for it already, after a while we receive email saying sorry we have to return money. 1.Although multiple users can add it into cart, but only one user can pay at the end. If others have bought that previously=> then the system informs you this item is not available, and shopping cart gets updated. 2. Even

1,2 have inconsistency=>but when we actually want to write on it=> it shows us the value has been changed by

Fault tolerance by voting: at least $\frac{n+1}{2}$ for 奇数 can work, $\frac{n}{2}+1$ for 偶数

1 device is faulty, we have 9 working and we need at least 5 to agree 0 devices are faulty, we have 10 working and we need at least 6 to agree 2 devices are faulty, we have 8 working and we need at least 5 to agree

4 devices are faulty, we have 6 working and we need at least 4 to agree 3 devices are faulty, we have 7 working and we need at least 4 to agree 5 devices are faulty, we have 5 working and we need at least 3 to agree

8 devices are faulty, we have 2 working and we need both to agree 6 devices are faulty, we have 4 working and we need at least 3 to agree 7 devices are faulty, we have 3 working and we need at least 2 to agree

 Failvote (majority vote 4 9 devices are faulty, we have 1 working and we have to stop as nothing to compare!

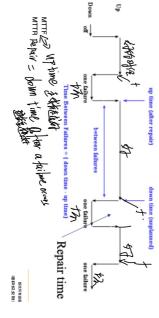
10个nodes: 至少要6个能工作,挂1,2,3,4都可以, 挂5个时候,就剩5个<6,不能工作Consider a system with modules each with MTTF of 10 years→一个坏掉的概率是1/10 (___)*(1/10)=1/5=1/MTTF. 整个系统的MTTF=5 Failvoting with 2 devices: MTTF = 10/2 = 5 years (system fails with 1 device failure) 只要有一个坏了就不行了, 整个系统坏掉的概率是

Failvoting with 3 devices: MTTF = 10/3 for the first failure + 10/2 for 2nd failure = 8.3 years

Lower availability for higher reliability (multiple modules agreeing on a value means that value is more likely to be accurate/reliable)

Supermodule:只要系统有一个存活就能工作

Module Availability measures the ratio of service accomplishment to elapsed time.



mean time to failure

 $\overline{MTTF + MTTR}$

module availability = $\frac{1}{mean time to failure + mean time to repair}$

Probability of a particular module is not available: mean time to repair

 $\overline{mean time to failure + mean time to repair} = \overline{MTTF + MTTR} = \overline{MTTF}$ MTTR(MTTR << MTTF)

Fault tolerance by voting

devices on failvote. Q: Which of the following system has higher reliability than the other? (i) System A with 4 devices on failvote (ii) System B with 5

For failvote: A: 4/2+1=3 有三个就行; For B: (5+1)/2=3 有三个就行 挂一个:A 剩3个,可以工作; B剩4个,可以工作; 挂2个:A剩2个<3,fall; B剩3个,可以工作: B更好

剩1,(1+1)/2=1 nothing to compare 剩3,(3+1)/2=2<3可以 剩2,(2)/2+1=2=2可以 剩3,(3+1)/2=2可以 剩2,(2/2)+1=2可以 剩4,(4/2)+1=3可以 (B强)

Can the system continue to operate in this scenario? Please explain your answer. Q: A failfast system has 8 devices. Assume 5 out of the 8 devices are unavailable but there are still 2 agreeing devices

system can still work. Ans: 8-5=3 available, in such case for failfast: if (3+1)/2=2 devices agree the system can work. So there are 2 agreeing devices the

Q: Which system is expected to be available more (e.g., expected to function for longer) than the other system? (i) System A with 5 devices on failfast (ii) System B with 5 devices as a supermodule

剩4, 需要4/2+1=3个,可以

剩3, 需要(3+1)/2=2个,可以

推进 ∰3 剩2, 需要2/2+1=2个,可以

剩2, 需要2/2+1=2个,可以 down

挂4个都能工作, B更强

挂2 世

Probability that (n-1) modules are unavailable, $P_{n-1} = \left(\frac{MTTR}{MTTF}\right)^{n-1}$

Probability that a particular l^{th} module fails, $P_f = \left(\frac{1}{MTTF}\right)$

Probability that the system fails with a particular ith module failing last =

$$P_f*P_{n-1} = \left(\frac{1}{MTTF}\right) \left(\frac{MTTR}{MTTF}\right)^{n-1}$$

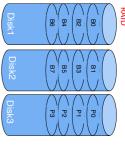
Probability that a supermodule fails due to any one of the n modules

failing last, when other (n-1) modules are unavailable $=\left(\frac{n}{MTTF}\right)\left(\frac{MTTR}{MTTF}\right)^{n-1}$

Question 9: [3 Marks]

We have seen the supermodule concept in class with repairs. Explain in your own words even when we have disks where failures per disk may happen almost every other year, a supermodule using these disks may be fault tolerant at the level of many years or even hundreds of years. Briefly explain your rationale.

enables recovery from individual disk loss supermodule's redundancy means that it can withstand multiple independent failures by storing data across disks in a way that allowing it to tolerate individual disk failures without losing data. Even though each disk might fail every other year, a one.The concept of a supermodule achieves high fault tolerance by organizing multiple disks into a redundant structure, the whole system will be improved greatly. So even if one disk failure we can use others to work and recovery the failed Ans: System can work if only one node can work, hence one disk failure would not impact the whole system, the reliability of

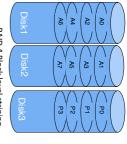


4.P0 is parity for bytes B0 and B1 so Rarely used Provides higher transfer rate as Striping takes place at byte level RAID 3 Byte level striping Bi are bytes of data of file

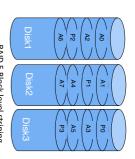
6.MTTF=1/(3p*p)= $\frac{1}{3}MTTF^2$

fail)= $\binom{5}{7}p^*p=3p^*p$

5.P(system fail)=P(two of three



3. MTTF=1/(3p*p)= $\frac{1}{3}MTTF^2$ bottlenecked by the write speed of be updated for every data write. these two disks as Parity needs to Disk3 has more writes than any of 2.Dedicated disk for parity blocks So the whole write operation gets Cons: 3和4都有,very slow writes. Pros: Provides higher throughput Striping takes place at block level RAID 4 Block level striping



RAID 5 Block level striping

all disks in parallel) 2. Provides higher throughput (read from Parity blocks are also striped

is no single disk with high # of writes, 3.slower writes but better than RAID 4 as write is better than 4,3) average equal among all 3 disks. (There and the number of write operations on Parity bits are distributed among all disks

4.MTTF=1/(3p*p)= $\frac{1}{3}MTTF^2$

has some benefits gained due to the loss of space utilization? 2 disks, (3) RAID 3 with 3 disks. Where does this lack of utilization of space go, i.e., where we can use such a configuration as it Q Which of the following RAID configurations has the lowest disk space utilization? (1) RAID 0 with 2 disks, (2) RAID 1 with

space is utilized. However, although (2) has low utilization, fault tolerance get improved a lot as its MTTF is higher. If one disk fail, we can still get whole same data from another disk. MTTF= $\frac{1}{p} * \frac{1}{p} = MTTF^2$, for (1) MTTF= $\frac{1}{2p} = \frac{1}{2}MTTF$, for (3) MTTF = Ans (2) has the lowest disk space utilization, because mirror method will store totally same data in two disk, hence only half of

$$\frac{1}{\binom{3}{2}p^2} = \frac{1}{3}(MTTF)^2$$

concern for her. She is undecided between the following two options: data. She needs high reliability, high read throughput, and cheaper option for her work, but write throughput is not a **Q** A researcher collected 10 Terabyte of data for her research. She needs to choose a RAID structure to store the

Option 1: RAID 1 with 2 disks Option 2: RAID 4 with 3 disks.

disadvantages of each option. If one of these options is clearly a more suitable choice over the other, please explain why. If not, please explain that as well. Assuming each disk has 10 Terabyte capacity and the same mean time to failure, explain the advantages and

utilization Cons: Lower MTTF compared with (1), MTTF=1/(3p*p)= $\frac{1}{3}MTTF^2$. Higher cost, we need buy 3 disks cost is high, we have to write data on two disks. For 2: Read can be done parallelly so it has higher throughput. Higher space done parallel on the two disks. 3.cost-effective as it only has two disks. Cons: lower space utilization (i.e. utilization is half), write Ans For 1 Pros: 1. mirroring pattern is more reliable (MTTF)^2, avoiding data get lost. 2.higher read throughput, read can be

Recommendation: (1) because it has higher reliability and cheaper satisfying the preference of this researcher.

RAID(Redundant Array of Independent Disks.) MTTF=1/p p是坏的概率

Different ways to combine multiple disks as a unit for fault tolerance or performance improvement

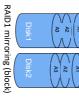
8 continuous bits = 1 byte; 4000/8000 continuous bytes = 1 block; Bit - b; byte - B; block - A



throughput ~doubles (small overhead Disks can send data parallelly, RAID0 (Block level Striping)

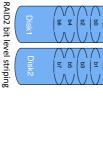
(浜半) 3.MTTF=1/(2p)=(1/2)*(1/p)=(1/2)*MTTF2.P(system fail)=P(one of disk fail)

increased vulnerability to failures (一个坏了系统就坏了) Cons: Increased vulnerability to failures Pros: Higher throughput at the cost of



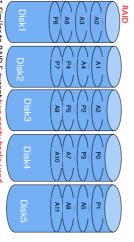
throughput (reading can be done in parallel) 1.P(system fail)=P(both two disks $2.MTTF=1/(p*p)=MTTF^2$ Pros: Provides higher read

written in disk 1 will also be written disk speed), because anything in disk2. 2.Half storage utilization (half of the total speed –i.e. single Cons: 1.lower write throughput



Provides higher transfer rate (double Striping takes place at bit level

difficult to main and read) rarely used (striping at bit level is MTTF reduced by half as in RAID 0 the single disk)



2.P(system fail)=P(three of five fail)= $\binom{5}{3}$ *P*P*P L.Similar to RAID 5 except two parity bocks used

3.MTTF=1/(10p*p*p)= $\frac{1}{10}MTTF^3$ increase substantially.

to recover the data. are computed in such way that any two disk failures can be safe times) $MTTF=1/(p^4)=(MTTF)^4$ 4.P0 and P1 are parity blocks for blocks A0, A1 and A2. These

5.All disks have similar # of writes and reading, so the

throughout is higher. failures can be sate to recover the data. Pros: Higher guarantee for fault tolerance, any two disks

Cons: Parity calculation and recovery process for RAID 6 is

much more complex.

configurations will have the best MTTF? Assume individual down) MTTF(坏一个就不行)=1/(3p)=(1/3)MTTF propability of each of disks fail is p, so MTTF for this disk is 1/p. MTTF of the disks in this question are the same. Assum the Q Given some data to be put on disks, which one of RAID (2) RAID 1 with 4 disks (for this case first disk is mirrored 3 (1) RAID 0 with 3 disks (any of the disk fail would cause system

(3) RAID 3 with 3 disks
$$\frac{\binom{3}{3}p^2}{\binom{2}{3}p^2} = \frac{3p^2}{3p^2} = \frac{(MTTF)^2/3}{(3)p^2}$$
 (4) RAID 4 with 3 disks $\frac{1}{\binom{3}{3}p^2} = \frac{1}{3p^2} = (MTTF)^2/3$

(4) RAID 4 with 3 disks
$$\frac{1}{\binom{3}{2}p^2} = \frac{1}{3p^2} = (MTTF)^2/3$$

Communication

e.g., B wants to send message ID 7 to A. In: receive; Out: send; Ack: acknowledge; If B cannot receive from A, after waiting for a while, B will send message again. Keep doing...



changes are performed, or none of them are. e.g., A transfer \$100 to B Atomicity: All changes to data are performed as if they are a single operation. That is, all the

Each block is associated with a version number. The block with the latest version number contains the most recent data. While reading - we can determine error of a disk block by its CRC. It always guarantees at least one block has consistent data. **Duplex write**: Each block of data is written in two places sequentially. If one of the writes fail, system can issue another write

Read(from hard disk to 2.Modify in main memory



Write the change to the hard 200

disk in a different block

write is check if the compare #v8 and #v9 to We can block and modify the version # 4.Write the change to original 200

write is correct latest version. We can use CRC to check if the If this step fails, we can have blue block as the correct

RAID 0 and RAID 2

- we have to wait for disk write finish to move to the other one) 1. Provides balanced I/O of disk drives (The same # of write and read operations happen at both disks. No bottleneck disk that
- Provides higher throughput (~doubles)
- 3.Reliability performance: Any disk failure will be catastrophic 4.MTTF reduces by a factor of 2
- 5.System throughput: we can read from two disks in parallel, but Higher throughput (almost double) at the cost of increased vulnerability to failures.
- 6. Storage utilization: same. For RAID1 will be 50%
- 7.Number of Disks needed: 2
- 8. Overhead difference: Striping in bit level cost more than striping in block level. In RAID 2, more dividing or partitioning overhead involved for writing operation. When we reading, we need to merge data from two disks more frequently to form meaningful data that can be displayed to users (much more overhead)

Which of the following RAID can safely recover data even for two disk failures? RAID 1 with 3 disks

Why communication reliability is important for databases?

check if the message or the input has been received correctly from automated information or other system. If input comes, some acknowledgement or message passing involved, we need to The nodes of distributed database need to communicate with each other, also input in a DB does not only from users, but also

number of operations (e.g., insertion, update or deletion) Additionally, many functionalities of DB need ensure the reliability during communication for consistency, because of huge

Data would be durable if it goes into disk, but actually why it cannot go into disk?

disk to make. Room for new page. buffer is fulln (no capacity left). In that case, process or transaction needs a new page, and we really have to write a page back to consuming and slow because of the performance issue. So the system tries to do such operation as less as possible unless the In fact, system avoid writing back to disk as long as possible. All sorts of reading and writing operations on disk are time-

better idea, speeding up the writing operation Assuming 4 changes on the same block, all these changes generate a log (4 logs). However, page still in the buffer, when it needs to be written back to disk, four changes still many writing operations. Hence logs are written frequently, having an SSD for logs is

while the disk is being recovered, Can we still get answers for queries "How many people are in income level L1"? Let's assume that a bitmap index is in memory while the hard disk became unavailable. If the system is designed to still runst

Num		, and	Num	income level	
0	John	VIC	됴	ㅁ	10100
1	Diana	WSN	12	22	01000
2	Xiaolu	WA	E	E	00001
ω	Anii	VIC	4	4	00010
4	Peter	WSN	₩.	5	00000

Yes, transaction does not have to access to the disk, as the page is store on the main memory.

memory, so that it will not go to the disk to read it. particular rows are on main memory, transaction will find them on No, because the records pointed by B+tree are on the disk. If the

Atomic Disk Write – logged write

Similar to duplex write, except one of the writes goes to a log

entire block in the disk) ideal for using log (pros: save space, record small changes; writing operations are also quicker than writing on the If just record what was the previous value, where's the changes in that entire block or when the changes happen=> Log – durable & can be read quickly. This method is very efficient if the changes to a block are small

It is also possible that multiple users using the same block, all of the operation needed to be written in logs (number of logs increase.)

is lost while storing the records. They can use multiple disks for the storage purpose if necessary. What strategies detect whether any error occurred or not? How can they still use the data if an error is detected? can they use to minimize the chance of any error while writing the data on disk? What strategies can they use to A company needs to store some sensitive medical records on disk. It is very critical that no error occurs, and no data

improving the reliability. We can use RAID1 with mirror pattern to store data, such configuration stores the same data on other disks,

to detect error. Verify whether a data in a block is correct, if not, the data with previous version number can be use the first modified version. used. Because duplex write can duplicate data in two different places on disk, hence if errors were detected we car data is written in two places sequentially. If one of the writes fail, system can issue another write. We can use CRC leading to low efficiency in logged write. Instead, we can use <mark>Duplex write</mark> to store the data on disk. Each block of When writing data from main memory to disk, it is unsuitable to use logged write as multiple disks involved,

CRC – Cvclic Redundancy Check

- Step
- 补最高次项个 0 (n 个 0) 找多项式系数
- 做 XOR (从不为 0 的那一位开始) 剩下 n 位 (结果为 m)
- 将m补在 message 后,做 XOR
- 若结果为 0,则 correct
- 111010000 111000

problems, if the original transaction using page 1 is rolled back or aborted, since page 1 has already written to disk, the system has to managed to Steal means if buffer pool is full, page 1 is chosen to evict from the buffer pool, page 1 hasn't committed but as there is no space in the buffer pool, page 1 is "forced" to be written in disk, and that caused

pages (steal it) putting on disk, making room for buffer. Forcing: to write back to disk; No force: No write on disk just put them in buffer as long as possible; Steal: Take one of the

rollback the changes done to page 1.

program | otoolologo dutus Astron 4 freshring to X411 + x3x0 + x2x1 + x1x1 + x0x1

 $X^4 + X^2 + X + 1$ original data 10100101/11100001