Spatial autocorrelation

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Introduction

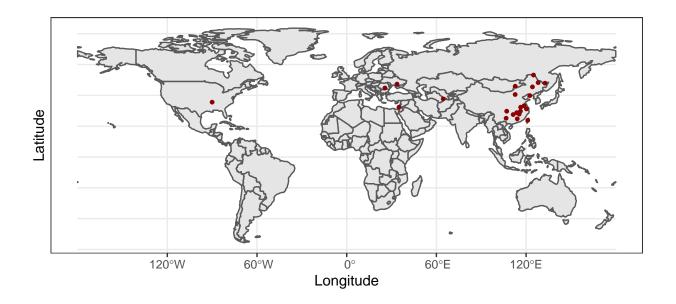
This .Rmd file is to test the spatial autocorrelation in our black carp data file, and try to find the best distance that reduces the spatial autocorrelation when doing subsampling. In this file, we:

- 1. Show the distribution of our data points on a map.
- 2. Use moran's I test to test the global spatial autocorrelation in our dataset.
- 3. Use the correlog plots to examine how spatial autocorrelation changes with distances.
- 4. Use the variogram to further test point 2.
- 5. Subsample at 250 km and 550 km, and check the local moran's I after sub-sampling to see if spatial autocorrelation has been reduced.
- 6. Conduct latitudinal stratification analysis.
- 7. Look at the Chinese dataset 17 data points.

```
library(gstat)
library(ggplot2)
library(dplyr)
library(spdep)
library(sp)
library(nlme)
library(ape)
library(MuMIn)
library(raster)
library(ncf)
library(knitr)
library(rnaturalearth)
library(sf)
## Import location data
location <- read.csv("location_no_temps.csv")</pre>
location <- unique(location) # remove duplicating locations</pre>
# Clean the data
carp <- read.csv("eddie_carp_new.csv")</pre>
carp.r <- carp %>%
  filter(sex != "male") %>% # keep the non-male data points
  distinct(location, .keep_all = TRUE) # remove all repeating locations
## Download one file to get the spatial points
# (this defines what projection to use when converting to spatial objects)
tmin.1979 <- brick("cpc/tmin.1979.nc", varname = "tmin")</pre>
```

```
## Loading required namespace: ncdf4
tmin.1979<-rotate(tmin.1979)</pre>
```

Data distribution



Calculate the residuals from the linear model

```
# Define the model
lm.annual <- lm(log(carp.r$AAM)~carp.r$AnnualTemp) # Annual temperature
lm.cold <- lm(log(carp.r$AAM)~carp.r$ColdTemp) # Cold temperature
lm.warm <- lm(log(carp.r$AAM)~carp.r$WarmTemp) # Warm temperature</pre>
```

```
# See the results
summary(lm.annual)
##
## Call:
## lm(formula = log(carp.r$AAM) ~ carp.r$AnnualTemp)
## Residuals:
       Min
                 1Q
                     Median
                                           Max
## -0.45033 -0.15088 -0.02442 0.11877 0.54619
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                                0.088922 22.796 2.7e-16 ***
## (Intercept)
                     2.027038
## carp.r$AnnualTemp -0.018853
                                0.006468 -2.915 0.00828 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2131 on 21 degrees of freedom
## Multiple R-squared: 0.288, Adjusted R-squared: 0.2541
## F-statistic: 8.495 on 1 and 21 DF, p-value: 0.008285
summary(lm.cold)
##
## Call:
## lm(formula = log(carp.r$AAM) ~ carp.r$ColdTemp)
##
## Residuals:
                 1Q
                      Median
## -0.41846 -0.12055 -0.02502 0.09514 0.57767
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                              0.04397 40.723 < 2e-16 ***
                   1.79047
## (Intercept)
## carp.r$ColdTemp -0.01190
                              0.00389 -3.059 0.00596 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.21 on 21 degrees of freedom
## Multiple R-squared: 0.3083, Adjusted R-squared: 0.2753
## F-statistic: 9.359 on 1 and 21 DF, p-value: 0.005955
summary(lm.warm)
## Call:
## lm(formula = log(carp.r$AAM) ~ carp.r$WarmTemp)
## Residuals:
##
       Min
                 10 Median
                                   3Q
                                           Max
## -0.48388 -0.15016 0.03813 0.11838 0.54909
##
## Coefficients:
```

Estimate Std. Error t value Pr(>|t|)

##

```
## (Intercept) 2.26257 0.30290 7.47 2.43e-07 ***
## carp.r$WarmTemp -0.01943 0.01262 -1.54 0.139
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2394 on 21 degrees of freedom
## Multiple R-squared: 0.1015, Adjusted R-squared: 0.05867
## F-statistic: 2.371 on 1 and 21 DF, p-value: 0.1385
```

Global spatial autocorrelation

```
## Make spatial dataframe
coords <- data.frame("long"=location[,3],"lat"=location[,2])</pre>
df <- data.frame(a = 1:nrow(location[3]))</pre>
spatial.data <- SpatialPointsDataFrame(coords,df,proj4string = tmin.1979@crs)</pre>
# Get a distance matrix from all points
dists <- spDists(spatial.data, longlat = TRUE)</pre>
## Run the Moran.I test on the residuals
Moran.annual <- Moran.I(lm.annual$residuals, dists)</pre>
Moran.cold <- Moran.I(lm.cold$residuals, dists)</pre>
global.moran <- data.frame(</pre>
  Model = c("Moran.annual", "Moran.cold"),
  Observed = c(Moran.annual$observed, Moran.cold$observed),
  Expected = c(Moran.annual$expected, Moran.cold$expected),
  sd = c(Moran.annual$sd, Moran.cold$sd),
  p.value = c(Moran.annual$p.value, Moran.cold$p.value)
kable(global.moran)
```

Model	Observed	Expected	sd	p.value
Moran.annual Moran.cold	0.0=.000	-0.0454545 -0.0454545	0.00-00-0	0.0.0

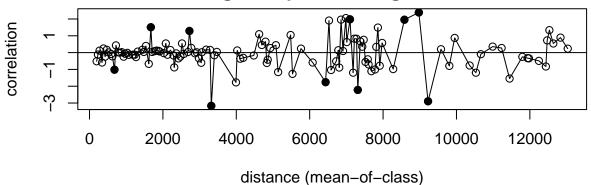
There is no global spatial autocorrelation for the entire dataset.

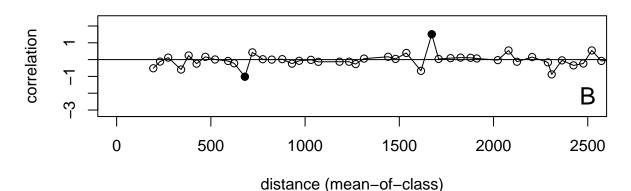
Local spatial autocorrelation

```
text(17400, min(test$correlation)+1, "A", cex=1.5)

# Reduce the distance range to 2500 km
plot(test, main="", xlim=c(0,2500))
abline(h=0)
text(2500, min(test$correlation)+1, "B", cex=1.5)
```

Annual Average Temperature Regression Residuals

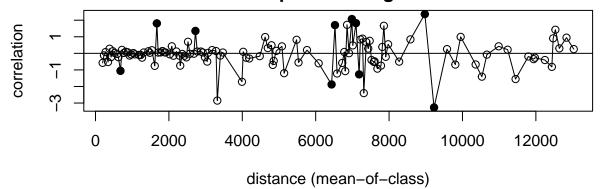


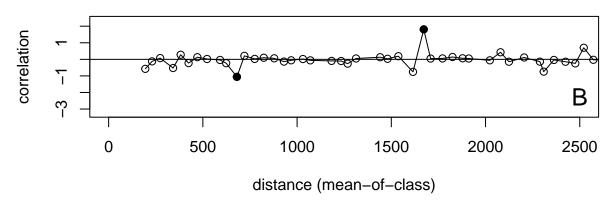


```
## 50 of 500 100 of 500 150 of 500 200 of 500 250 of 500 300 of 500 350 of 500 400 of 5
# Plot with the entire distance range
plot(test, main="Cold Quarter Temperature Regression Residuals")
abline(h=0)
text(17400, min(test$correlation)+1, "A", cex=1.5)

# Reduce the distance range to 2500 km
plot(test, main="", xlim=c(0,2500))
abline(h=0)
text(2500, min(test$correlation)+1, "B", cex=1.5)
```

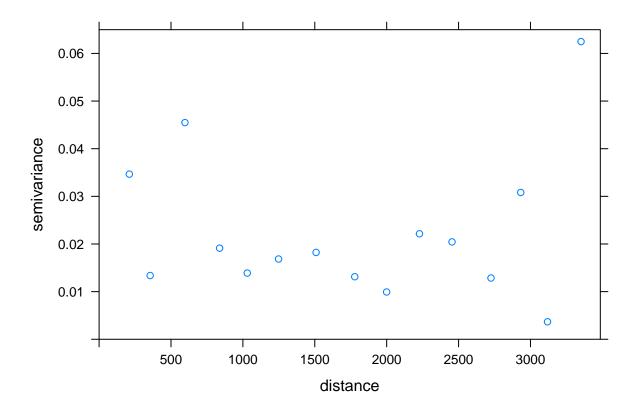
Cold Quarter Temperature Regression Residuals





In general, the correlog plots suggest that for both temperature, 600 km is a good distance to reduce local spatial autocorrelation.

Variogram

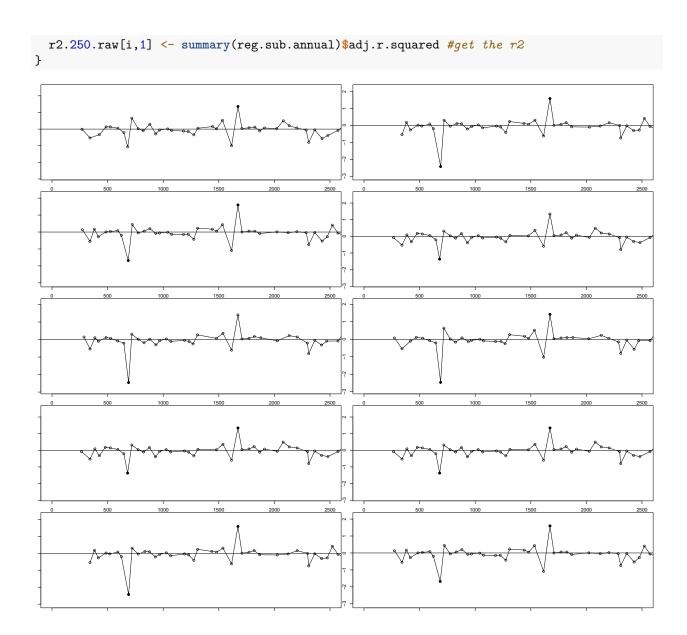


If we pick 250 km as the cutoff distance for sub-sampling, we would have 20 location points. If we pick 550 km as the cutoff distance for sub-sampling, we would have only 12 location points.

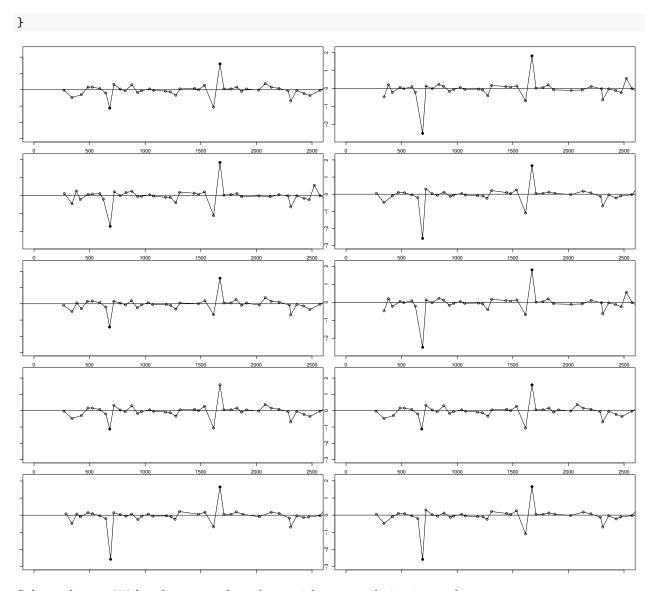
Subsampling at 250km

Here, we try to sub-sample at 250km and check the local moran's I (correlog plot) after sub-sampling.

Local moran's I - annual 250



Local moran's I - cold 250



Subsampling at 250 km does not reduce the spatial autocorrelation in our dataset.

Subsampling at 550km

Now, we try to subsample at a larger distance - 550km.

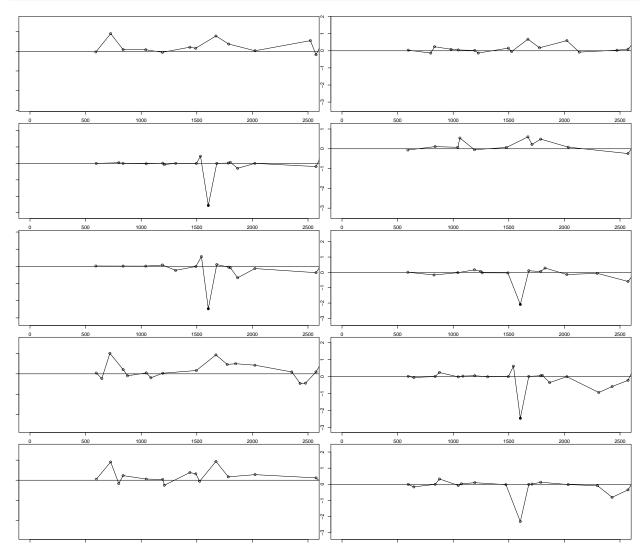
Local moran's I - annual 550

```
table(carp.r$spatial.code.550)

# Store the r2 values
r2.550.raw <- matrix(NA,10, 2)
colnames(r2.550.raw) <- c("annual","cold")

par(mfrow = c(5, 2))
par(mar=c(1,1,1,1))

## Check the local moran's results after sub-sampling</pre>
```

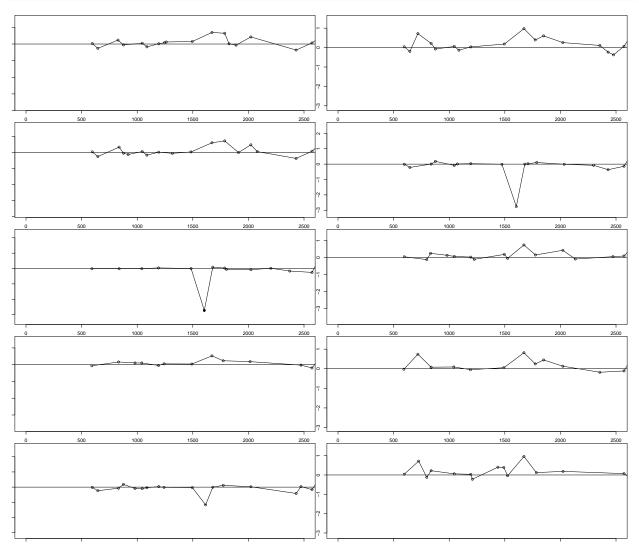


Local moran's I - cold 550

```
table(carp.r$spatial.code.550)

par(mfrow = c(5,2))
par(mar=c(1,1,1,1))

## Check the local moran's results after sub-sampling
for (i in 1:10){
```



We have seen that subsampling at 550 km would largely reduce the spatial autocorrelation in our dataset at low distances, even though we are only left with 12 data points.

Compare the r2 values

```
mean(unique(r2.550.raw[,2])))
)
kable(r2)
```

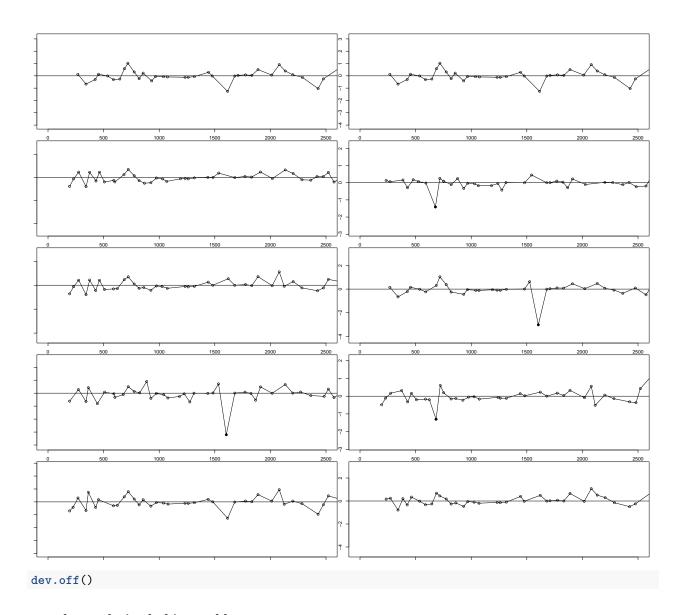
Time	Annual	Cold
Original Sub 250 Sub 550	0.2541185 0.2511585 0.1258329	$\begin{array}{c} 0.2753462 \\ 0.2714244 \\ 0.1306277 \end{array}$

However, subsampling at 550 km would reduce our R2 value as well, suggesting that the model would not fit for the sub-dataset.

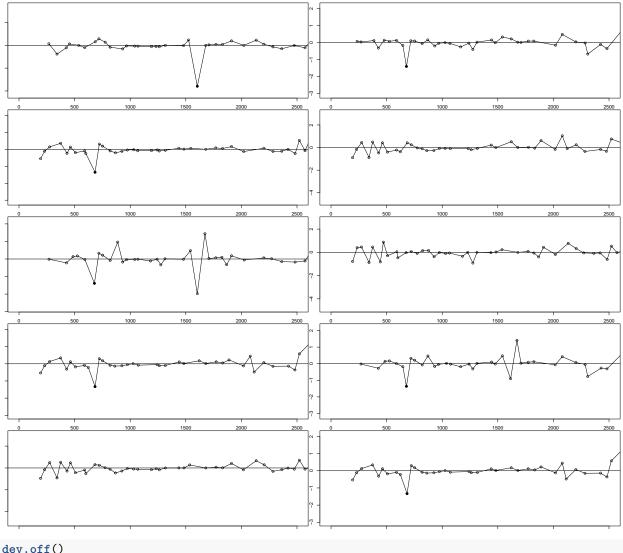
Latitudinal stratification

Now we would like to explore if stratified sub-sampling using latitude would reduce our spatial autocorrelation at low distances.

one degree latitude bin - annual



one degree latitude bin - cold



- For some subsamples, the negative autocorrelation at 550 km is reduced.
- It seems that the South Ukarine data point is the main cause that we have negative spatial autocorrelation at around 550 km. Therefore, we ought to remove this datapoint from our analyses.

Local moran's I without the South Ukarine data point

Now we would like to re-examine the local spatial autocorrelation with the South Ukarine data point removed.

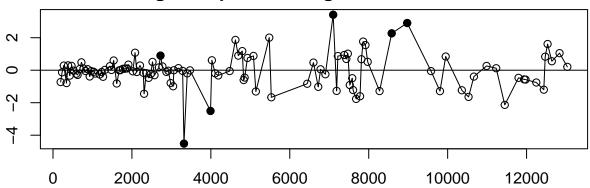
Remove the data point and construct the local moran's I

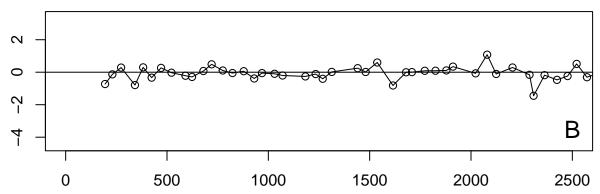
```
# Remove the data point for South Ukarine
carp.new <- carp.r[carp.r$location != "South Ukraine",]</pre>
# Define the model
lm.annual <- lm(log(carp.new$AAM)~carp.new$AnnualTemp) # Annual temperature</pre>
lm.cold <- lm(log(carp.new$AAM)~carp.new$ColdTemp) # Cold temperature</pre>
```

```
# See the results
summary(lm.annual)
##
## Call:
## lm(formula = log(carp.new$AAM) ~ carp.new$AnnualTemp)
## Residuals:
##
       Min
                 1Q
                      Median
                                           Max
## -0.42284 -0.12220 0.00157 0.10361 0.31059
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                                  0.075785 26.200 < 2e-16 ***
## (Intercept)
                       1.985591
## carp.new$AnnualTemp -0.017471
                                  0.005446 -3.208 0.00441 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1788 on 20 degrees of freedom
## Multiple R-squared: 0.3398, Adjusted R-squared: 0.3067
## F-statistic: 10.29 on 1 and 20 DF, p-value: 0.004414
summary(lm.cold)
## Call:
## lm(formula = log(carp.new$AAM) ~ carp.new$ColdTemp)
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -0.39212 -0.11672 -0.00521 0.09334 0.29909
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                                0.036336 48.560 < 2e-16 ***
## (Intercept)
                     1.764503
## carp.new$ColdTemp -0.011593
                                0.003148 -3.683 0.00147 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1699 on 20 degrees of freedom
## Multiple R-squared: 0.4041, Adjusted R-squared: 0.3743
## F-statistic: 13.56 on 1 and 20 DF, p-value: 0.001475
## Local moran's I - Annual temperature
par(mfrow=c(2,1), mar=c(2,2,2,2))
# Use the coorelog function to develop the relationship
test <- correlog(carp.new$longitude, carp.new$latitude, lm.annual$residuals,
                increment=50, resamp=500, latlon=T)
## 50 of 500 100 of 500 150 of 500 200 of 500 250 of 500 300 of 500 350 of 500 400 of 5
# Plot with the entire distance range
plot(test, main="Annual Average Temperature Regression Residuals - Removal")
abline(h=0)
text(17400, min(test$correlation)+1, "A", cex=1.5)
```

```
# Reduce the distance range to 2500 km
plot(test, main="", xlim=c(0,2500))
abline(h=0)
text(2500, min(test$correlation)+1, "B", cex=1.5)
```

Annual Average Temperature Regression Residuals – Removal



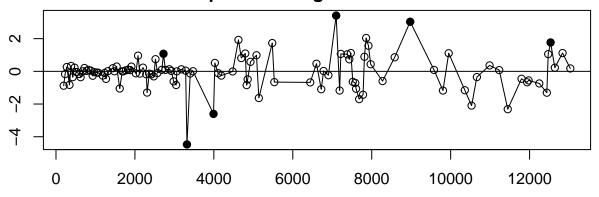


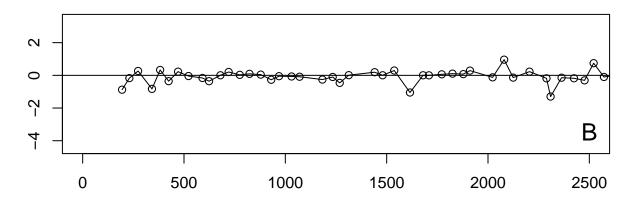
```
# Plot with the entire distance range
plot(test, main="Cold Quarter Temperature Regression Residuals - Removal")
abline(h=0)
text(17400, min(test$correlation)+1, "A", cex=1.5)

# Reduce the distance range to 2500 km
plot(test, main="", xlim=c(0,2500))
abline(h=0)
text(2500, min(test$correlation)+1, "B", cex=1.5)
```

50 of 500 100 of 500 150 of 500 200 of 500 250 of 500 300 of 500 350 of 500 400 of 5

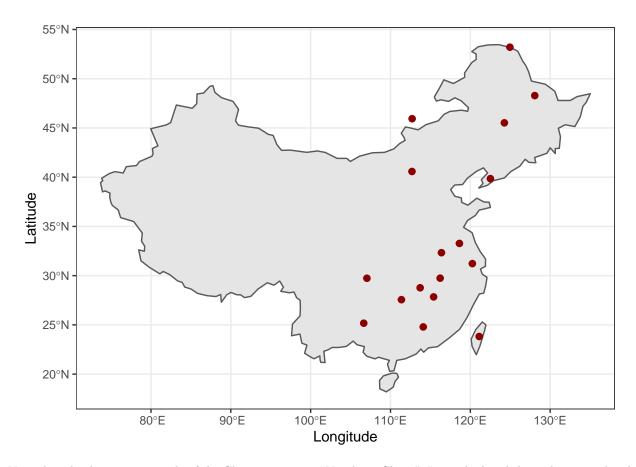
Cold Quarter Temperature Regression Residuals – Removal





China Dataset analyses

Now let's look at the datapoints in China. There are 17 datapoints.



Note that the datapoint outside of the Chinese region is "Northern China". It is calculated through geographical center.

Global moran's I

```
# Run the models
lm.annual.china <- lm(log(AAM)~AnnualTemp, data = black.china)</pre>
summary(lm.annual.china)
##
## Call:
## lm(formula = log(AAM) ~ AnnualTemp, data = black.china)
##
## Residuals:
##
        Min
                  1Q
                      Median
                                    3Q
                                            Max
   -0.21857 -0.10327 -0.01010 0.09564 0.18908
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 1.998599
                           0.057669 34.656 9.83e-16 ***
## AnnualTemp -0.019144
                           0.004173
                                    -4.588 0.000355 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1235 on 15 degrees of freedom
## Multiple R-squared: 0.5839, Adjusted R-squared: 0.5562
```

```
## F-statistic: 21.05 on 1 and 15 DF, p-value: 0.0003553
lm.cold.china <- lm(log(AAM)~ColdTemp, data = black.china)</pre>
summary(lm.cold.china)
##
## Call:
## lm(formula = log(AAM) ~ ColdTemp, data = black.china)
##
## Residuals:
##
        Min
                  1Q
                       Median
## -0.21312 -0.04385 -0.00453 0.08316 0.18188
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.755918
                           0.027736
                                       63.31 < 2e-16 ***
## ColdTemp
               -0.012452
                           0.002372
                                       -5.25 9.79e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1136 on 15 degrees of freedom
## Multiple R-squared: 0.6476, Adjusted R-squared: 0.6241
## F-statistic: 27.57 on 1 and 15 DF, p-value: 9.785e-05
## Make spatial dataframe
coords <- data.frame("long"=black.china[,14],"lat"=black.china[,13])</pre>
df <- data.frame(a = 1:nrow(black.china[14]))</pre>
spatial.data <- SpatialPointsDataFrame(coords,df,proj4string = tmin.1979@crs)</pre>
# Get a distance matrix from all points
dists <- spDists(spatial.data, longlat = TRUE)</pre>
## Run the Moran.I test on the residuals
Moran.annual <- Moran.I(lm.annual.china$residuals, dists)</pre>
Moran.cold <- Moran.I(lm.cold.china$residuals, dists)</pre>
global.moran <- data.frame(</pre>
 Model = c("Moran.annual", "Moran.cold"),
  Observed = c(Moran.annual$observed, Moran.cold$observed),
  Expected = c(Moran.annual$expected, Moran.cold$expected),
  sd = c(Moran.annual$sd, Moran.cold$sd),
  p.value = c(Moran.annual$p.value, Moran.cold$p.value)
kable(global.moran)
```

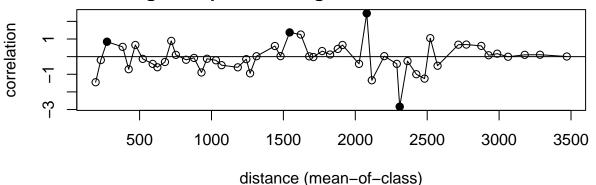
Model	Observed	Expected	sd	p.value
Moran.annual Moran.cold	-0.055177 -0.041979	0.00=0	$\begin{array}{c} 0.0494446 \\ 0.0491515 \end{array}$	

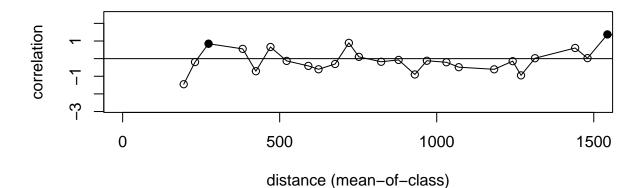
No global spatial autocorrelation in the Chinese dataset.

Local moran's I - correlog

abline(h=0)

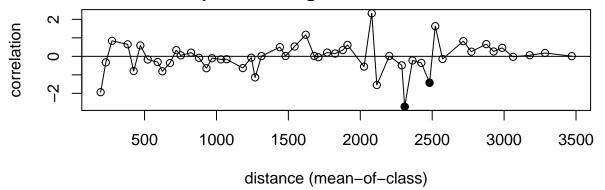
Annual Average Temperature Regression Residuals for Chinese dat

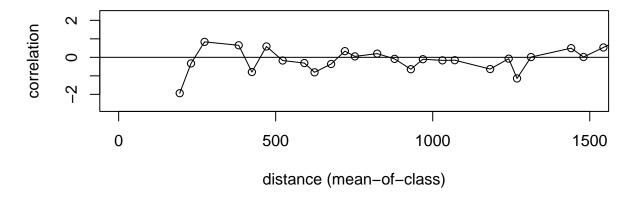




50 of 500 100 of 500 150 of 500 200 of 500 250 of 500 300 of 500 350 of 500 400 of 5

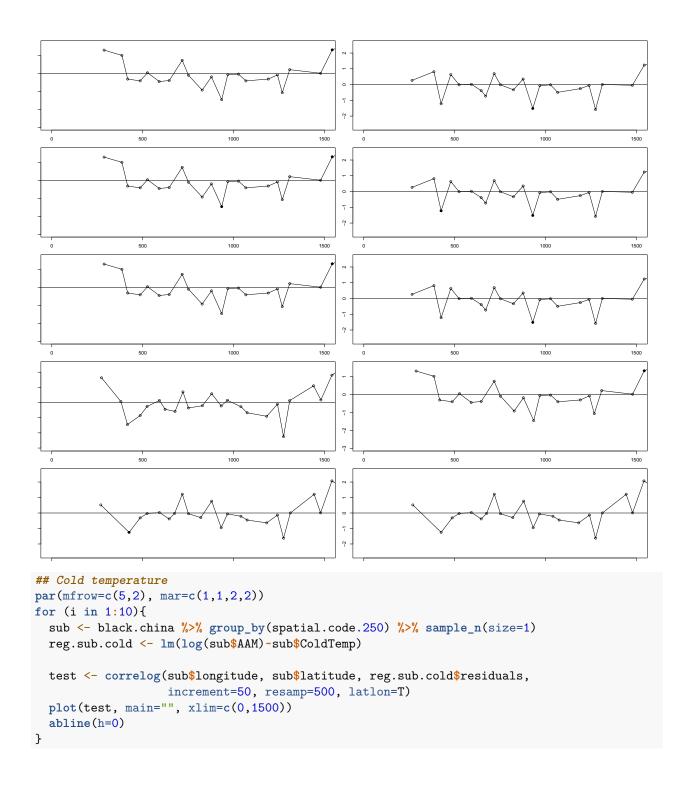
Cold Quarter Temperature Regression Residuals for Chinese data

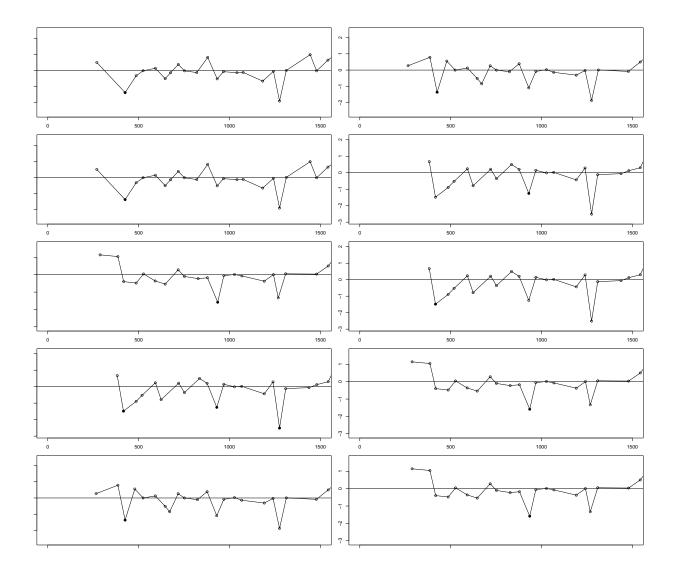




Subsample at 250km for Chinese dataset

Now we subsample at 250km to reduce spatial autocorrelation.





Conclusions

- There was no global spatial autocorrelation in the entire dataset, but when looking at local clustering, we saw a strong negative autocorrelation at around 550 km.
- We tried to subsample at 250 km, and 550 km. 220 km did not reduce the spatial autocorrelation we saw. 550 km did reduce that, but left us with too few data to fit a model.
- We then tried to subsample by latitudinal straitification. We found that the negative autocorrelation was reduced in some iterations (when South Ukarine was not selected). We hypothesized that particular datapoint is the cause.
- $\bullet\,$ We removed the SU data point and ran the local moran's I again. This time, we have no local clustering at 550 km!