

$16 \leq 90$
 $17 \leq 19$
 $\boxed{4} \ 3 \ \boxed{5} \ \boxed{7}$
 $4 \ 5 \ 7 \ 9$
 $2 \ 3 \ 9$
 $5 + 9 = 14$
 45

What's the total amount of
7 permutations with loop length
of 6?

$${}^7C_6 (6-1)!$$

$$= 7 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1$$

$$= 840$$


$${}^7C_3 \cdot 2 \cdot {}^4C_2 = \frac{7!}{3!} = 420$$

$840 + 420$

1260

$$a, b \text{ s.t. } a+b \leq n$$

$$km(a, b) =$$

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Unit 1 Specialist Mathematics Investigation 1 2023

Take-home part

Student name: _____ Teacher name: _____

Task type: Investigation take-home part

Validation test information:

Test date: Tuesday 27th March (Week 8) during your usual Specialist period

Test version: Your usual Specialist classroom

Reading Time: 5 minutes

Working Time: 40 minutes

Materials required: Calculator with CAS capability (as provided by the student)

Identified Items: Area (like those previously), areas (including extended), perimeter, conversion, Rad/Pegs, arcs, rates, highlighters

Preparation: Drawing tools (compass, straightedge, ruler) on two unlined A4 pieces of paper, and up to three calculators approved for use in the WAACE examinations

Task length: 10 minutes

Time-keeping: No, but time-allowance (noted on page 2 of validation task)

Note: All part questions worth more than 2 marks require working to obtain full marks.

Read the following, and answer the questions in the text.

Here are two mathematical exercises, and you have just got a wonderful (and mathematical) motivation. The machine will also do rearrangement operations of letters, and you have decided to call it a *permutator*. An example of a *permutator* is below:

It works as follows. Suppose you have a sequence of seven letters:

A B C D E F G

For each number n in the row of the “permutator,” letters in position n (left moved to the position n in the row of the “permutator.”) are moved to the position n in the row of the “permutator.” In this case, the letter in position 1 (position 1 of the permutator) is moved to the position 1 of the permutator, i.e., the letter A remains in position 1 of the permutator. And so on. After the permutation above is applied to the letters of the row, the arrangement looks like this:

F C A D B G E

So see, word games around you offer a magnificent invention – and start making you to feel

Sure! But you say “ye-”

Thank!!!

Yes, but you know, you have just started creating motivation in the 21st Special course, we are well prepared for the task.)

So, let's try to find out how many words could be created from the word “permutator”.

As the answer to the question is:

[illegible]

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Answer to questions in task format

Some of the answers listed include the calculation used to obtain answers; others do not. (But in the selection list, question parts worth more than 2 marks will – in total – require writing for full marks.)

- What is the total number of different permutations?
Total number = 21
5040
- How many different 7 permutations using the letters within just one pair (and hence all the other letters in the same place)?
Total number = $\frac{7!}{2!} = 21$
- How many different 7 permutations using letters within just 2 pairs?
How many ways letters within 2 pairs (leaving the other letters in the same place)?
Number (that swap letters within 2 pairs = 105
Number (that swap letters within 2 pairs = 105
- How many different 7 permutations more exactly 8 letters (leaving the other letters where they are)?
Number (that more exactly 8 letters = $\frac{8!}{2!} = 20160$
- Can you think of examples of 7 permutations which have lengths of 8, 5, 4, and 6?
Here is an example of one with length 8:
$$\begin{pmatrix} 2 & 1 & 3 & 4 & 5 & 6 & 7 \end{pmatrix}$$
- Can you think of examples of obtaining 7 permutations with a given loop length (such as 6)?
Yes, here are two examples of 7 permutations with loop length 6:
$$\begin{pmatrix} 6 & 2 & 4 & 5 & 3 & 1 & 7 \end{pmatrix}$$
$$\begin{pmatrix} 2 & 1 & 3 & 4 & 5 & 6 & 7 \end{pmatrix}$$

7. What is the total number of 7 perimeters with a long length of 11?
Total number = $(7 - 1)!$
 $= 4!$
 $= 24$
8. What is the total number of 7 perimeters with a long length of 5?
Total number = $5! = 120$
9. What is the maximum possible long length of a 7 perimeter?
Maximum possible long length = 12

7. 200 kg 30 m



$F = m$

(1.) $\frac{1}{2} F \cdot s$

(2.) F_P

$W = \Delta E$

$\Delta E_P = m \cdot g \cdot h = 200 \cdot 9.8 \cdot 30$

$= 58800$

4. A person walks up a flight of 12 stairs. Each step is 200 mm wide and 150 mm up. The person is 60 kg.

$p = 980 \text{ m}^2$

What is the work done against gravity

1.16×10^7

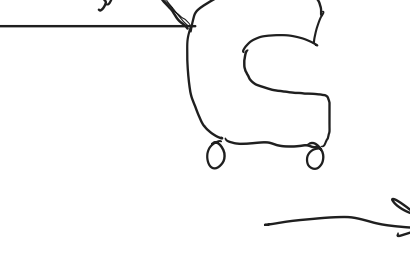
5. 2000 J 60 kg $W = F_s$ $F = m \cdot a$

$W = F_s$

$9.8 \cdot 60 = 588 \text{ N}$

$s = \frac{W}{F} = \frac{2000}{588} \approx 0.34$

6.



1200 J

15 m

F

$W = F \cdot s$ $F = \frac{W}{s}$

$\text{cm } 75 \cdot F = \frac{1}{2}$

$F = \frac{1200}{150 \cdot 75}$

$= 9.77 \times 10^3 \text{ N}$

7. 120 kg

10 cm 16 m^2

$F_g = m \cdot g = 120 \cdot 1.6 \cdot 10 = 192$

8. 800 kg $0 \rightarrow 60 \text{ m/s}$ $\frac{26.1}{s}$

$$\begin{aligned}
 P_{\text{As}} &= \frac{F}{t} = \\
 F_{\text{As}} &= a_{\text{As}} \cdot M \cdot \frac{60}{72 \cdot 74} \\
 &\approx 708.6 \text{ N} \\
 708.6 \text{ N} \\
 P &= \frac{F}{t} = \frac{F_1}{t_1} = \frac{M \cdot a \cdot s}{t} = \frac{M \cdot s \cdot s}{t \cdot t} = M \cdot \frac{1}{t} = 800 \cdot \frac{60}{72} \cdot \frac{1}{26} \\
 &= 4.09 \times 10^3 \text{ W}
 \end{aligned}$$