VOIT TEST 1



MATHEMATICS METHODS Year 12 Section One: Calculator-free

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Time and marks available for this section
Reading time before commencing work:

Working time for this section:

15 minutes
15 marks

Materials required/recommended for this section
To be provided by the supervisor
This Question/Answer Booklet
Formula Sheet

To be provided by the candidate Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

correction fluid/tape, eraser, ruler, highlighters

CALCULATOR-FREE

Instructions to candidates

- 1. Write your answers in this Question/Answer Booklet.
- Answer all questions.
- 3. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

2

4. It is recommended that you do not use pencil, except in diagrams.

See next page

CALCULATOR-FREE

(7 marks)

Cuestion 1

Differentiate with respect to x. Simplify your answers. (IN FULLY FACTORISED FORM)

(2 marks)

(2 marks)

$$x \leq 200 + -(x \in 3)$$
 (as) $+(x \in 3) \leq 2$

See next page

Question 2

the value of x, in terms of a and b.

(2 marks)

Find where the equation $y=2ax^2+b^2x$ has a derivative equal to zero given that a and b are positive constants.

$$\frac{dy}{dx} = 4ax + b^2$$

$$(x = -b^2 / 4a)$$

MATHEMATICS METHODS Year 12

7

CALCULATOR-ASSUMED

Question 9

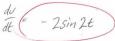
(6 marks)

A particle is in rectilinear motion and its velocity, ν , at any time t seconds is given by

$$v = \cos(2t) \, ms^{-1}$$

Determine an expression for $\frac{dv}{dt}$ the acceleration of the particle.

(1 mark)



ii) What is the velocity and the acceleration of the particle when $t = \pi$? (2 marks)

$$t = \pi , V = \cos 2\pi = 1$$

$$\frac{dV}{dt} = -2\sin 2\pi = 0$$

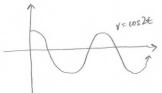
(iii) What feature of the parameter is indicated by the value of the acceleration when $t=\pi$. (1 mar

not changing

at = 0 indicates that t=TT, gives local max/min

Max value of v = cos2t is 1 : Max @ t = Tr .

(iv) During a particular second, the acceleration increases from $-1.8~ms^{-2}$ to $1.5~ms^{-2}$. Describe the velocity of the particle during this second. (1 mark)



Ace is gradient of velocity

Gradient '-' before min

't' after min

During this second, v decreasing until min.

then V increases.

End of questions

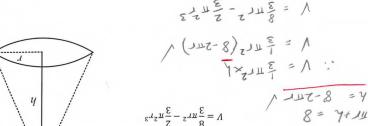
CALCULATOR-FREE

Question 3

(2, 4 marks)

for the framework, represented by the the solid lines in the diagram below. circumference of the base and the height of the cone. 8 metres of bamboo is to be used A tent in the shape of a cone is to be pitched. A bamboo frame is needed for the

(a) Show that the volume V, of the tent in terms of its radius r, is given by



in terms of π . You are not required to prove it is a maximum. (b) Determine the radius of the tent that will maximise the volume, leaving your answer

$$0 \neq 1$$

$$1 = \frac{1}{8} \times \frac{$$

End of Questions

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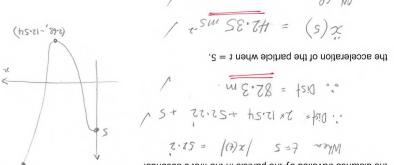
MATHEMATICS METHODS Year 12

(2,2 marks)

Question 7

second, is x meters, where: A particle moves such that its displacement from the origin 0, at time t seconds

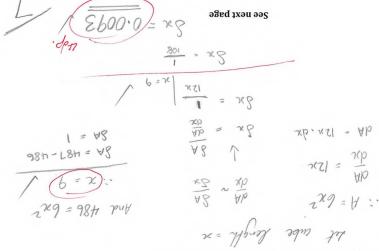
When E=5 /x(4) = 52.2 the distance travelled by the particle in the first 5 seconds. Determine: (22.75 5) $S + \frac{1}{482 - 81 - 412} = (1)x$ for $t \ge 0$.



(3 marks)

Question 8

Use calculus to approximate the small change in the side length of a cube (correct to 4 decimal places) when its area changes from $486cm^2$ to $487cm^2$



CALCULATOR-FREE

6 MATHEMATICS METHODS Year 12

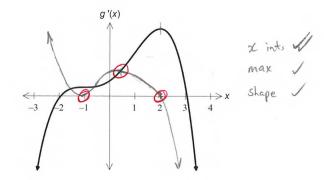
CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 12

Question 6

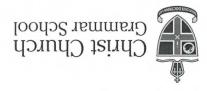
(4 marks)

The graph of y = g'(x) is sketched below. On the same axes, sketch y = g''(x).



5

UNIT TEST 1 2017



MATHEMATICS METHODS Year 12

Section Two:

Calculator-assumed

Marks available:

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30 minutes Working time for this section: Reading time before commencing work: 3 minutes Time and marks available for this section

Formula Sheet (retained from Section One) This Question/Answer Booklet To be provided by the supervisor Materials required/recommended for this section

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, To be provided by the candidate

30 marks

for use in the WACE examinations Special items: drawing instruments, templates, and up to three calculators approved

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MATHEMATICS METHODS Year 12

(2 marks)

Question 5

Consider the functions $f(x) = ax^3 + \frac{b}{x}$ with f'(1) = 9 and f''(1) = 6. Determine the

$$\int_{-\infty}^{\infty} \frac{1}{2} \int_{-\infty}^{\infty} \frac{1}{2} \int_{-\infty}^{\infty}$$

See next page

CALCULATOR-ASSUMED

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See next page

MATHEMATICS METHODS Year 12

CALCULATOR-ASSUMED

Question 4

(8 marks)

Using the rule $f(x + h) = f(x) + h \times f'(x)$ for the function $f(x) = \frac{1}{\sqrt[3]{x}}$ (4 marks) find an approximation for $\frac{1}{\sqrt[3]{105}}$ as x increases from 1 to 1.05. Your answer should

$$f(x+h) = x^{-1/3} + 0.05 \times (-1/3)x^{-1/3}$$

$$= 1 + 0.05 \times (-1/3)(1)$$

$$= 1 + \frac{1}{20} \times (-1/3)$$

$$= 1 - \frac{1}{60}$$

$$= \frac{59}{60}$$

$$= 0.983$$

For the function $f(x) = \sin(2x)$ find:

(1,3 marks)

the instantaneous rate of change when $x = \frac{\pi}{a}$

the average rate of change in terms of π over the interval $\frac{\pi}{6} \le x \le \frac{\pi}{4}$.

