

## WAEP Semester One Examination, 2020

Question/Answer booklet



ection Two:
↑ TINU
NETHODS
<b>SOITAMEHTAN</b>

Calculator-assumed

Time allowed for this section Reading time: Working time:	ten minutes one hundred minutes	Number of additional answer booklets used (if applicable):	
Your nar			
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WA student number: In figures			

## Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet (retained from Section One)

### To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

drawing instruments, templates, notes on two unfolded sheets of A4 paper, Special items:

Computer Algebra System (CAS) calculators, are permitted in this ATAR and up to three calculators, which can include scientific, graphic and

course examination

### Important note to candidates

it to the supervisor before reading any further. you do not have any unauthorised material. If you have any unauthorised material with you, hand No other items may be taken into the examination room. It is your responsibility to ensure that

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# CALCULATOR-ASSUMED

## Structure of this paper

001	IstoT				
92	86	100	13	13	Section Two: Calculator-assumed
32	25	09	8	8	Section One: Calculator-free
Percentage for a point of the contraction of the co	Marks available	Working time (minutes)	Number of questions to be snswered	Number of questions available	Section

3

### Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
   Do not use erasable or gel pens.
- 3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any required to receive full marks. If you repeat any question, ensure that you cancel the required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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**CALCULATOR-ASSUMED** 

Section Two: Calculator-assumed

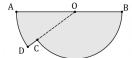
65% (98 Marks)

This section has  ${\bf thirteen}$  questions. Answer  ${\bf all}$  questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (5 marks)

Shape AOBCDA below consists of sector BOC of circle centre O joined to sector DOA of a different circle, also centre O. AB is a straight line of length 65 cm, arc AD is 12 cm long and  $\angle AOD = 0.32$  radians.



(a) Determine the length OA.

(2 marks)

(b) Determine the area of the shape.

(3 marks)

Solution

$$A_{DOA} = \frac{1}{2} \times 37.5^{2} \times 0.32$$
= 225

Let *OB* = *r*

$$r = 65 - 37.5$$
= 27.5

$$A_{BOC} = \frac{1}{2} \times 27.5^{2} (π - 0.32)$$
= 1067
$$Area = 225 + 1067$$
= 1 292 cm<sup>2</sup>

Specific behaviours
✓ area of sector *DOA*

See next page

√ radius and angle of sector BOC

✓ area of shape

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Question number: Supplementary page METHODS UNIT 1 20 CALCULATOR-ASSUMED

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Determine the probability that

both events occur.

Question 11

(6 marks)

(2 marks)

**METHODS UNIT 1** 

Question 21

(8 marks)

(2 marks)

A squad of 6 cyclists is to be chosen at random from 17 applicants. 3 of applicants live in Tasmania, 6 live in WA and the rest live in Queensland.

a) Determine the number of different squads that can be chosen.

Solution  $\binom{17}{6} = 12376$ 

19

Specific behaviours

✓ indicates use of combination formula

✓ correct number

(b) Determine the number of different squads that can be chosen that

(i) include all the Tasmanians.

(2 marks)

(2 marks)

(2 marks)

Solution  $\binom{3}{3}\binom{14}{3} = 1 \times 364$  = 364

Specific behaviours

✓ indicates correct method

✓ correct number

i) include an equal number of cyclists from each of the states.

Solution  $\binom{3}{2}\binom{6}{2}\binom{8}{2} = 3 \times 15 \times 28$  = 1260

Specific behaviours

✓ indicates correct method✓ correct number

(iii) have at least 5 cyclists from Queensland.

Solution

 $\binom{8}{5}\binom{9}{1} + \binom{8}{6}\binom{9}{0} = 56 \times 9 + 28 \times 1$ = 504 + 28= 532

Specific behaviours

√ indicates correct method

✓ correct number

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Solution  $P(Y|X) = \frac{P(X \cap Y)}{P(X)} \Rightarrow P(X \cap Y) = 0.2 \times 0.1 = 0.02$ 

Specific behaviours

✓ indicates use of conditional formula
 ✓ correct probability

Two events are such that P(X) = 0.2, P(Y) = 0.5 and P(Y|X) = 0.1.

(b) at least one event occurs.

(2 marks)

Solution  $P(X \cup Y) = P(X) + P(Y) - P(X \cap Y) = 0.2 + 0.5 - 0.02 = 0.68$ 

Specific behaviours

✓ indicates use of rule✓ correct probability

(c) neither event occurs.

(1 mark)

Solution  $P(\overline{X} \cap \overline{Y}) = 1 - P(X \cup Y)$  = 1 - 0.68 = 0.32Specific behaviours  $\checkmark \text{ correct probability}$ 

(d) X occurs given that Y has occurred.

curred.

Solution  $P(X|Y) = \frac{P(X \cap Y)}{P(Y)}$   $= \frac{0.02}{0.5}$  = 0.04

Specific behaviours

✓ correct probability

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(1 mark)

End of questions

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CALCULATOR-ASSUMED

(8 marks)

Question 12

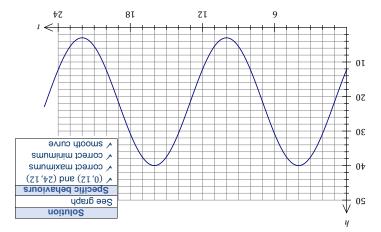
the wheel begins to move is given by  $h = 21.5 - 18.5 \cos (\frac{\pi}{3} + \frac{1\pi}{3})$ . The height above ground level, h m, of a seat on a steadily rotating Ferris wheel t minutes after

Determine the initial height of the seat. (1 mark)

√ correct height Specific behaviours  $m \ 22.21 = (0)$ hSolution

(4 marks)

Graph the height of the seat against time on the axes below.



Determine (c) BE CUT OFF

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(8 marks)

(1 mark)

the maximum height above ground reached by the seat.

√ correct height Specific behaviours  $m 0 = x_{MM} h$ Solution

above ground level. the time taken, to the nearest second, for the seat to first reach a height of 4 m

(S marks)

(s 292) s 22 m 9 = 3 $52 = 00 \times 75.0$  $75.6 = 3 \Leftarrow 4 = 3$ Solution

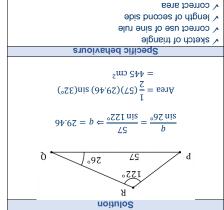
√ time to nearest second √ time as decimal Specific behaviours

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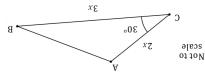
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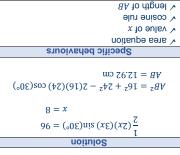
Question 20 CALCULATOR-ASSUMED METHODS UNIT 1

Determine the area of triangle PQR when  $\angle PQR = 26^\circ$ ,  $\angle PRQ = 122^\circ$  and PQ = 57 cm. (s)



Determine the length of AB. The area of triangle ABC is  $96 \text{ cm}^2$ ,  $\angle ACB = 30^\circ$  and  $\angle BC = 3AC$  as shown in the diagram.





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CALCULATOR-ASSUMED

(1 mark)

Question 13 (6 marks)

The graph y = f(x), where  $f(x) = x^2 + bx + c$  has a turning point at (2, -7).

State the equation of the line of symmetry for the graph of y = f(x).

	•				•	•
	S	olut	ion			
		x =	2			
Spe	ecifi	c be	havi	oui	'S	
✓ corre	ect e	quat	ion			

Determine the value of the constant b and the value of the constant c. (3 marks)

Solution	
$f(x) = (x-2)^2 - 7$	
$=x^2-4x+4-7$	
b = -4	
_	
c = -3	
0 " 1 1 .	
Specific behaviours	
✓ writes f(x) in squared form	
√ value of b	
√ value of c	

(c) The graph of y = f(x) is translated 3 units to the left and 2 units upwards. Determine the equation of the resulting curve. (2 marks)

	Solution
1	New turning point at $(2-3, -7+2) = (-1, -5)$ .
E	Equation is $y = (x+1)^2 - 5 = x^2 + 2x - 4$
	Specific behaviours
,	✓ identifies new turning point
,	✓ correct equation (either form)

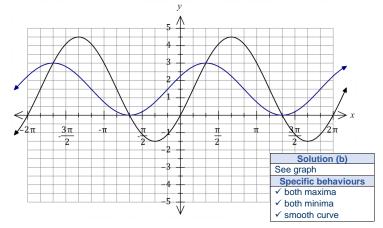
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Question 19

(8 marks)

The graph of  $y = a + b \sin(x - c)$  is drawn below, where a, b and c are positive constants.



Determine the value of a, the value of b and the value of c, where  $c < \pi$ . (3 marks)

;	Solution	
a = 1.5,	b = 3,	$c = \frac{\pi}{6}$
Specif	fic behavio	ours
√ value of a		
✓ value of b		
✓ value of c		

(b) On the same axes, draw the graph of  $y = a + \frac{b}{2}\sin(x + c)$ . (3 marks)

(c) Solve  $b \sin(x - c) = \frac{b}{2} \sin(x + c)$  for  $-\pi \le x \le \pi$ . (2 marks)

Using intersection of graphs:
$2\pi$ $\pi$
$x = -\frac{1}{3}, \qquad x = \frac{1}{3}$
3 3
Specific behaviours
√ a correct solution, anywhere
✓ two solutions as given

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### (9 marks) 4r noiteauD

observed that n(D) = 140, n(S) = 53 and  $n(S \cap D) = 10$ . they had a driver's licence (event D) and whether they wore spectacles (event S), it was When a random sample of 173 people from a university were classified according to whether

(a) Determine

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(i) ·(<u>S</u>)u

 $n(\vec{S}) = 173 - 53 = 120$ Solution

√ correct number Specific behaviours

(1 mark)

(1 mark)

 $(S \cap G)n$  (ii)

√ correct number Specific behaviours  $E_{4} = 01 - E_{6} = (Q \cap Q)n$ Solution

Determine the probability that a randomly chosen person from the sample

(S marks)

does not have a driver's licence.

 $191.0 \approx \frac{88}{871} = (\overline{a})q$ 8 = 173 - 140 = 33Solution

Specific behaviours

✓ denominator √ numerator

(S marks)

wears spectacles given that they have a driver's licence.

Specific behaviours  $708.0 \approx \frac{6 \text{ ft}}{6 \text{ ft}} = \frac{(6 \text{ ft})n}{(6 \text{ ft})n} = (6 \text{ ft})q$ Solution

√ denominator √ numerator

See next page

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The attendance of Cleo at the next work social is independent of the attendance of CALCULATOR-ASSUMED

(3 marks) next work social. anyone else. Determine the probability that none of the three named people attend the

√ correct probability √ uses independence rule  $\checkmark P(\overline{A} \cap \overline{B})$ Specific behaviours  $(28.0 - 1) \times 2.0 =$  $(\overline{\lambda})^q \times (\overline{a} \cap \overline{h})^q = (\overline{\lambda} \cap \overline{a} \cap \overline{h})^q$ Since event C is independent: 5.0 =8.0 - 1 = $P(\overline{A} \cap \overline{B}) = P(\overline{A} \cup \overline{B})$ Solution

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### CALCULATOR-ASSUMED

Does the sample provide any indication of possible independence of events S and D?
 Justify your answer.
 (3 marks)

10

Yes, since  $P(S) = \frac{53}{173} \approx 0.306$  and  $P(S|D) \approx 0.307$ , it can be seen that the probability that a person wears spectacles barely changes given that they also have a driver's licence. Hence the events are likely to be independent.

### Specific behaviours

- √ calculates P(S)
- ✓ compares with P(S|D)
- ✓ explains why independence indicated

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CALCULATOR-ASSUMED

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**METHODS UNIT 1** 

Question 18

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(9 marks)

The probabilities that Alf, Bess and Cleo will attend the next work social are P(A) = 0.7, P(B) = 0.55 and P(C) = 0.85 respectively. It is also known that  $P(A \cap B) = 0.45$ .

(a) Determine  $P(A \cup B)$ .

(2 marks)

Solution  $P(A \cup B) = 0.7 + 0.55 - 0.45$  = 0.8

Specific behaviours

✓ uses probability rule✓ correct probability

(b) Describe, in the context of this question, the event (A ∩ B̄) ∪ (Ā ∩ B) and calculate the probability that it happens. (3 marks

Solution

The event means that either Alf or Bess but not both attend the next social.

$$P(A \cap \overline{B}) = 0.7 - 0.45 = 0.25$$
  
 $P(\overline{A} \cap B) = 0.55 - 0.45 = 0.1$   
 $P = 0.25 + 0.1 = 0.35$ 

### Specific behaviours

- √ description
- ✓ one correct part probability
- ✓ correct answer

(c) State, with justification, whether events A and B are mutually exclusive. (1 mark)

Solution

No, since  $P(A \cap B) \neq 0$ .

Specific behaviours

√ uses probability rule for ME events

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.(0.5.0)A polynomial of degree 3 passes through the points with coordinates (0,4),(-2,0),(2,0) and (8 marks)

11

(4 marks)

Determine the equation of the polynomial in expanded form.

z = v $(2.0-)(2-)(2)b = 4 \leftarrow 0 = x$ Use 4th point:  $(2.0 - x)(2 - x)(2 + x)b = \emptyset$ Using roots:

Solution

 $(2.0 - x)(2 - x)(2 + x)2 = \emptyset$ Exband:

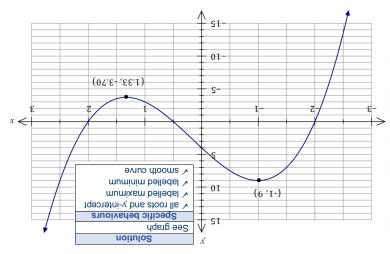
 $4 + x8 - x^2 - x^2 = x^2 = x^2 + 4$ 

√ factored form using roots Specific behaviours

✓ substitutes fourth point

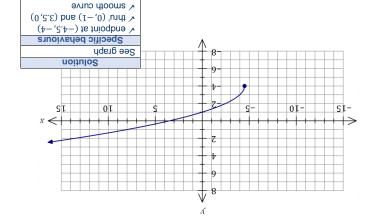
√ correct expanded form  $\checkmark$  correct value of  $\alpha$ 

(4 marks) turning points. Draw the graph of the polynomial on the axes below, indicating the coordinates of all



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> (3 marks) Draw the graph of y = f(2x) on the axes below. (c) CALCULATOR-ASSUMED ÞΙ METHODS UNIT 1



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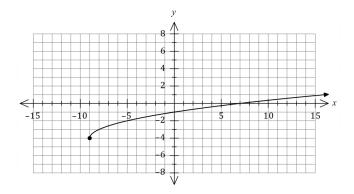
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(3 marks)

The graph of y = f(x) is drawn below, where  $f(x) = \sqrt{x + a} + b$ .

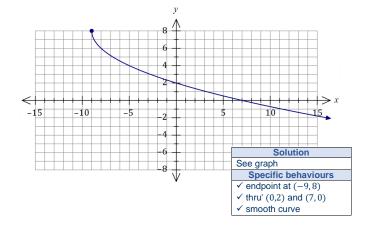
**CALCULATOR-ASSUMED** 



Determine the value of the constant a and the value of the constant b. (2 marks)

Solution			
$a = 9, \qquad b = -4$			
Specific behaviours			
value of a			
value of b			

Draw the graph of y = -2f(x) on the axes below.



12 Question 16 (7 marks)

A counter is randomly drawn from bag A, replaced and then a second counter randomly drawn from the same bag. Determine the probability that the second counter drawn is

Bag *A* contains 6 red and 4 blue counters. Bag *B* contains 3 red and 5 blue counters.

blue.

Solution

Specific behaviours √ correct probability

A counter is randomly drawn from bag  $\mathcal{B}$ , **not** replaced and then a second counter is randomly drawn from the same bag. Determine the probability that the second counter (3 marks)

drawn is red.

Solution

$$P(BR) = \frac{5}{8} \times \frac{3}{7} = \frac{15}{56}$$

$$P(RR \cup BR) = \frac{6+15}{56} = \frac{21}{56} \left( = \frac{3}{8} = 0.375 \right)$$

### Specific behaviours

- √ uses tree or indicates correct method
- √ either branch correct
- √ correct probability
- A counter is randomly drawn from bag A, its colour noted and then placed in bag B. A second counter is then randomly drawn from bag B. Determine the probability that this counter is the same colour as the first counter drawn.

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Solution	
$P(RR) = \frac{6}{10} \times \frac{4}{9} = \frac{24}{90}$	
$P(BB) = \frac{4}{10} \times \frac{6}{9} = \frac{24}{90}$	
$P(RR \cup BB) = \frac{24 + 24}{90} = \frac{48}{90} \ \left( = \frac{8}{15} = \frac{8}{15} \right)$	= 0.53)

- Specific behaviours
- √ uses tree or indicates correct method
- √ either branch correct
- √ correct probability

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