Hale School 2012

 DMV



Question/Answer Booklet

Circle your teacher's initials

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m IIB}$

BAH GJ

WATHEMATICS 3CD Section One (Calculator Free)

Booklet 1 of 3

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Material required/recommended for this section

To be provided by the supervisor
This Question/answer booklet for Section One.
Formula sheet.

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler.

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

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Structure of this examination

		Number of questions	Working time (minutes)	Marks available
Booklet 1 This Booklet (Section 1)	Calculato r Free	9	50	50
Booklet 2 (Section 2)	Calculator Assumed	6	100	50
Booklet 3 (Section 2)		7	100	50
			Total marks	150

Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the booklet *Year 12 Information Handbook 2012*. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in the spaces provided in this Question/Answer Booklet.
- 3. Spare answer pages are provided at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning : If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued i.e. give the page number. Fill in the number(s) of the question(s) that you are continuing at the top of the page.
- 4. **Show all working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you **do not use pencil**, except in diagrams.

(a)
$$f(x) = \frac{1 - e^{-2x}}{1 + e^x}$$

$$g(x) = (3x+1)(1+x^2)^3$$
 [2 marks]

$$h(x) = \int_{1}^{2x} (1-At)^3 dt$$
 (2 marks)

 $\int_{0.5}^{1} (\sqrt{2x-1})^{-1}$

(5 marks)

(a) Evaluate

[3 marks]

(b) Determine $\int xe^{1+x^2}dx$

[2 marks]

(2 marks) **E** noitesuQ "every prime number greater than 3 is one more or less than a multiple of 6". Consider the conjecture:

(4 marks)

9 noitesup

Calculate the maximum and minimum values of $\begin{tabular}{c} χ & S = S. \end{tabular}$ $\overline{t} + \zeta X$

(a) Show that the conjecture is true for three values. [1 mark]

(q) [3 marks] Prove the conjecture.

See next page End of paper

Question 4 (5 marks)

 $\frac{1-4x}{x+12} \le 3$

Solve the inequality

Question 8 (cont)

(b) Evaluate the constants a, b and c by solving the equations in part (a).

[3 marks]

See next page See next page

(e marks) 8 noitesup

$$\frac{x-1}{1} = (x)\theta \qquad \text{pue} \qquad x \to = (x) \int_{0}^{1} dx$$

The function
$$r(x) = ax + bx^2 + \frac{c}{x}$$
 has the following properties:
• $r(x) = ax + bx^2 + \frac{c}{x}$

4a + 8b + c = 40, a + 2b - c = 0, 8b - c = 0.

- t = x nand t = x nand t = x nand t = x
- x the notion of inflection at x = -2
- Show that the constants a, b and c satisfy the simultaneous equations: **(a)**

- Determine expressions for f(g(x)) and g(f(x)).
- [2 marks]

- Evaluate f(g(0)) and g(f(0)). [2 marks]
- Determine the domain of f(g(x))

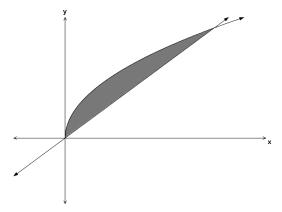
[1 mark]

Oetermine the range of P(x)[2 marks]

[3 marks]

Question 6 (6 marks)

The diagram below shows graphs of $y = \sqrt{x}$ and y = 0.5x. Find the shaded area.



Question 7 (6 marks)

Let A denote the set [1, 2, 3, ..., 999, 1000], the set of positive integers up to 1000.

(a) How many numbers in set A are not multiples of either 4 or 5 or both? [3 marks]

(b) How many numbers in set A that have at least 2 digits start and finish with the same digit? [3 marks]