Γ est 3

snoituditisid Isimonia Calculus of Trigonometric Functions
Discrete Random Variables

Calculator Assumed Year 12 Mathematics Methods Semester One 2018



Exceptional schooling. Exceptional students. PERTH MODERN SCHOOL

(շ ացւէշ)		Ţи	Question 1	
	45 minutes +5 minutes READING	τ∌/¯¯¯	lstoT	
Mr Change Me Change Mr Staffe Mr Staffe Mr Staffe	sheet for this section of the test.	l Calculators	_	
Mr McClelland Mrs. Carter		ed 2 nd May	Date: W	
Теясhет:		:	Name	

$\frac{^{2}ph}{\varepsilon}$	$\frac{52 + 1}{5}$	<u>ne - 1</u> E	3 <u>2a</u> 2	(x = X)d
8	7	I	0	X

Determine the value of the constant a.



Year 12 Mathematics Methods

Test 3 2018

Question 2 (8 marks)

(a) Differentiate $e^{-3x}\sin(2x)$ with respect to x, showing full working. (2 marks)

- (b) Hence find the following indefinite integral.
- $-3\int e^{-3x}\sin(2x)dx+2\int e^{-3x}\cos(2x)dx.$

And using a similar process as part (a), find the indefinite integral for

$$-3\int e^{-3x}\cos(2x)dx-2\int e^{-3x}\sin(2x)dx.$$

Year 12 Mathematics Methods

Test 3 2018

Question 6 (9	marks
---------------	-------

(a) A sample of six objects is to be drawn from a large population in which 20% of the objects are defective. Find the probability that the sample contains:

(i) three defectives. (2 marks)

(ii) fewer than three defectives. (2 marks)

(b) Another large population contains a proportion p of defective items.

(i) Write down an expression in terms of p for P, the probability that a sample of six items contains exactly two defectives. (2 marks)

(ii) By differentiating to find $\frac{dP}{dp}$, show that P is greatest when $p = \frac{1}{3}$. (3 marks)

(3 marks)

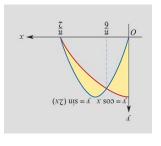
Year 12 Mathematics Methods Test $3\,2018$

(c) Use the two equations from (b) to determine $\int e^{-3x} \sin(2x) dx$.

(3 marks)

Test 3~2018

Find the area between the two curves from $0 \le x \le \frac{\pi}{2}$, showing full algebraic reasoning. (4 marks) ∂ noitesuQ



Year 12 Mathematics Methods

Year 12 Mathematics Methods

Test $3\ 2018$

Question 3 (6 marks)

Differentiate with respect to x, (show full working)

(a)
$$y = \sin^3(2x+1)$$
.

(3 marks)

Evaluate the following, showing full working.

$$\int_{6}^{2} \cos(2x) dx$$

(3 marks)

Page 4 of 7

Year 12 Mathematics Methods Test 3 2018

Question 4 (9 marks) 75% of the avocados produced by a farm are known to be first grade, the rest being second grade. Trays of 24 avocados are filled at random in a packing shed and sent to market. Let the random variable X be the number of first grade avocados in a single tray. Explain why X is a discrete random variable, and identify its probability distribution. (2 marks) Calculate the mean and standard deviation of X. (2 marks) Determine the probability that a randomly chosen tray contains 18 first grade avocados. (1 mark) more than 15 but less than 20 first grade avocados. (2 marks) In a random sample of 1000 trays, how many trays are likely to have fewer first grade than second grade avocados. (2 marks)

Page **5** of **7**

Perth Modern School