\upphi nit Methods Unit \upphi

Calculator Free Logarithm Laws and Solving Equations

Time: 45 minutes Total Marks: 45 Your Score: / 45



Question One: [2, 2, 2, 2 = 8 marks] \mathbf{CE}

Express each of the following as a single logarithm:

2 log 3 + log 2 - log 6

(a)

$$2\log_x y - 3\log_x y + 6$$
 (d)

(p)
$$(\log x)_3 \div (\log x)_5 + \log x_5$$

Question Two: [3, 3, 3 = 9 marks] CF

Evaluate each of the following showing full working:

$$3\log_2 6 - \log_2 27$$

(a)

$$\frac{\log 135 - \log 5}{\log 3^2}$$
 (c)

Question Three: [1, 3 = 4 marks] CF

$$\log x = y$$
 , where $\stackrel{X}{=}$ is positive, express each of the following in terms of $\stackrel{Y}{=}$.

$$\log x^2$$
 (a)

$$\log xm^3 - 3\log m$$
 (b)

CE

Question Four: [2, 3, 3, 3, 3, 3, 4, 3 = 24 marks]

Solve each of the following equations, showing all working.

(a)

$$0 \not = \frac{\bar{\epsilon}}{\bar{\epsilon}} \chi \Delta \mathbf{1} + \frac{\bar{\epsilon}}{\bar{\epsilon}} \chi \delta$$

0=8 gol + x gol

 $1.00001 = \frac{1.0001}{10001}$

 $SI = {}^{I+x}E$

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 $x = 5 - \ln 50$ 02 nl = x - 2 $\int_{0}^{\infty} 02 \, dx = \ln 20$ $6_{5-x} = 50$ (y) 26^{2-x} =100 $\frac{\log 3}{\log 4} = x$ gol = pgol x**√** E= ***⊅ 7-**≠ _x**t y** =3 y =−2 **√** 0 = (3 + 2)(3 - 2) $\lambda = 0 = 0 - \lambda - 2\lambda$ $\mathrm{rst}\ \lambda = \mathrm{d}_{\times}$ 0 = 9 - 4 - 4 = 0 $2 \operatorname{Sol} E + \operatorname{Sol} = \operatorname{Sgol} xz - 2 \operatorname{Sol} x$ $2 \operatorname{Sol} E + \operatorname{Sgol} = (\operatorname{2gol} z - 2 \operatorname{gol})x$ $2 \operatorname{gol} E + \operatorname{2gol} = (\operatorname{2gol} z - 2 \operatorname{gol})x$ $\frac{2 \operatorname{gol} E + \operatorname{2gol}}{\operatorname{2gol} E + \operatorname{2gol}} = x$ $x \log 2 - 3 \log 2 = 2x \log 5 + 3 \log 5$ $2\log(1+x) = 2\log(2-x)$ $\Sigma_{x-3} = \Sigma_{2x+1}$ Mathematics Methods Unit 4

$$2^{x-3} = 5^{2x+1}$$
 (f)

$$4^{2x} - 4^x - 6 = 0$$
 (g)

$$5e^{2-x} = 100$$
 (h)

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Mathematics Methods Unit 4

$$(x+1)\log 3 = \log 12$$

$$x+1 = \frac{\log 12}{\log 3}$$

$$x+1 = \frac{\log 12}{\log 3}$$

$$x = \frac{\log 12}{\log 3} - 1$$

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SOLUTIONS Calculator Free Logarithm Laws and Solving Equations

Time: 45 minutes Total Marks: 45 Your Score: / 45



Question One: [2, 2, 2, 2 = 8 marks] OF

Express each of the following as a single logarithm:

$$= \log^{x} \frac{\lambda}{\lambda} + \log^{x} x_{\theta}$$

$$= \log^{x} \lambda_{3} - \log^{x} \lambda_{3} + 2\log^{x} x$$

$$= \log^{\alpha} m_{3}u_{4} - \log^{\alpha} u_{4} - \log^{\alpha} t_{2}$$

$$= \int_{0}^{2} x^{3} \operatorname{ol}(x)^{3} + \operatorname$$

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Question Four: [2, 3, 3, 3, 3, 4, 3 = 24 marks] CF

Solve each of the following equations, showing all working.

(a)
$$\int_{0}^{2} 64 = 2$$

$$\int_{0}^{2} 64$$

$$\int_{0}^{2} = 64$$

Mathematics Methods Unit 4

$$2 = \frac{1}{6}x$$

$$8 = x$$

$$9 = 8 \text{ sgol} + x \text{ sgol}$$

$$0 = 2 \text{ sgol} + x \text{ sgol}$$

$$S = S = X$$

$$S = S = X$$

$$S = S = X$$

$$x = \frac{152}{1}$$

$$\frac{100^{4x}}{10^{4x}} = 10000^{x-1}$$

$$10^{4x+4}$$

$$10^{6x+4}$$

$$10^{$$

$$3^{x+1} = 12$$

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Question Two: [3, 3, 3 = 9 marks] CF

Evaluate each of the following showing full working:

$$1.5\log_84$$

(b)

$$=\log_{8}(\sqrt{4})^{3} \checkmark$$

$$=\log_{8} 8 \checkmark$$

$$=1 \checkmark$$

$$\frac{\log 135 - \log 5}{\log 3^2}$$

(c)

$$= \frac{\log 27}{2\log 3}$$

$$= \frac{\log 3^3}{2\log 3}$$

$$= \frac{3\log 3}{2\log 3}$$

Question Three:

CF

 $\log x = y$, where is positive, express each of the following in terms of .

$$\log x^{2}$$
(a)
$$=2\log x$$

$$=2y \checkmark$$

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Mathematics Methods Unit 4

(b)
$$\log xm^3 - 3\log m$$

$$= \log x + 3\log m - 3\log m$$

$$= y \qquad \checkmark$$