Mathematical Methods



MORKING TIME:

EQUIPMENT:

21 minutes

Polynomial Functions Practice Test

| :JATOT | 21 marks | | |
|---------------------|----------|------------|------|
| | | Percentage | |
| SECTION ONE: RESOUR | CE FREE | letoT | τς/ |
| | | Calc | 08 / |
| Name AUNE | -5015 | Non calc | 17/ |

pens, pencils, pencil sharpener, highlighter, eraser, ruler, SCSA formula sheet

Show all of your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks.

A new hospital is being planned for the consortium with between 100 and 400 beds. What number
of beds would you recommend and why?

237 beds. Mewmuse profit (tyming pointless)

e. The consortium are considering closing two smaller hospitals, with 250 and 310 beds, and replacing them with a single hospital to accommodate all their patients. Discuss whether this would be an effective strategy to increase profitability.

END OF SECTION 2

Question 1

[2,2,4 = 8 Marks]

 Find the equation of the circle drawn, you do not need to expand or simplify your answer.

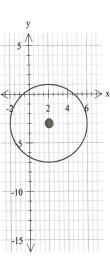
Centre at
$$(2,-3)$$

Radius of 4
 $(x-2)^2 + (y-(-3))^2 = 4^2$
 $(x-2)^2 + (y+3)^2 = 16$

b. Give the domain and the range of this circle.

domain
$$\{x: -2 \le x \le 6\}$$

range $\{y: -7 \le y \le 1\}$



c. Find the centre and radius of the circle defined by:

$$x^2 + y^2 - 8x + 6y - 24 = 0$$

Use completing the square:

$$(\chi^{2}-8\chi) + (y^{2}+6y)-24=0$$

$$((\chi-4)^{2}-16) + ((y+3)^{2}-9)-24=0$$

$$(\chi-4)^{2}+(y+3)^{2}-49=0$$

$$(\chi-4)^{2}+(y+3)^{2}=7$$
Centre at $(4,-3)$ radius=7

Question 5

[1,3,1,2,3 = 10 Marks]

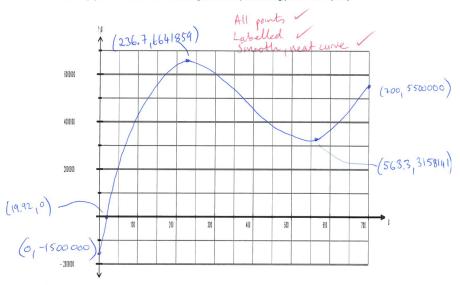
A recent study into the annual profitability, P(B), in dollars, of individual hospitals owned by a consortium found that it varied with the number of beds, B, in each hospital.

Using the model:

$$P(B) = 0.2B^3 - 240B^2 + 80000B - 1500000$$

a. What annual profit is expected if a hospital has 50 beds?

b. Graph P(B) on the axes below showing all intercepts, turning points and P(700).



c. What is the fewest number of beds a hospital needs to make a profit rather than a loss?

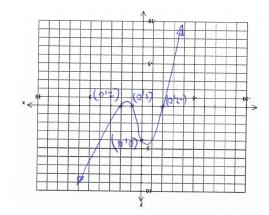


[1,1,3,2 = 7 Marks]

a. The coordinates of the point where the curve cuts the γ -axis, For the graph of $y = x^3 - x^2 - 4x + 4$, determine:

c. the coordinates of the points where the line cuts the x-axis $\chi - Z$. When the respect to $\chi - Z$.

$$(2-\chi^{+}) = (-\chi) + (-\chi) + (-\chi) = (-\chi) + (-$$



Question 4 [1,4,1,2 = 8 Marks]

the rule: The depth of water in a flask in a science experiment was measured for an eight hour period and followed

$$a = 0.44^3 - 51^2 + 161 + 161$$

a. What was the depth of water when the experiment began? Where t was the number of hours since the experiment began and d the depth of water in centimetres.

1 . moz

(01,58.40) b. In total for how many hours and minutes was the depth 10cm or more during the eight hour

and y=10, (01, 13.0) -2+ +91+275-227h-0=h ydsb

SYYZTE = 1.82 + 2 4 2 13.03 13.02 12.02720

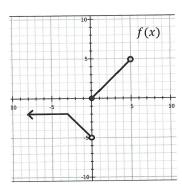
2cm. c. What was the minimum depth of water during the first eight hours? 10 Ld = 4.16

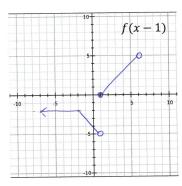
d. At what time, correct to nearest minute, was the depth a maximum during the first eight hours?

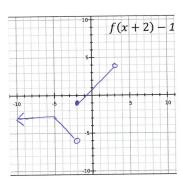
Question 3

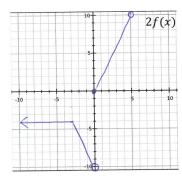
[2,2,2 = 6 Marks]

The following is the graph of f(x). On the graphs below, sketch the new graph with the transformations applied





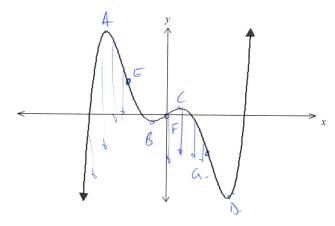




Question 3

[4,2 = 6 Marks]

The graph below is that of the curve $y = x^5 - 6x^3 + 3x$



Use your calculator to help find:

a. Find the co-ordinates of each of the turning points.

Points of influction at E(-1.342, 6.118) F(0, 0) G(-1.342, 6.118)

Concare downwards between:

$$-\infty \leq x \leq -1.342$$
.

and 123 0 4 x 4 1.342.

[3,2 = 5 Marks]

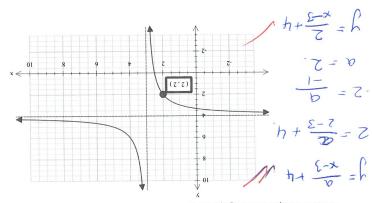
a. Describe the transformation that takes place when $y = x^3$ is changed to,

 $y = 2(3x - 4)^3 + 5$ b. The original graph contains the point (5, 125), where will this point be transformed to in the graph of

[3 Marks]

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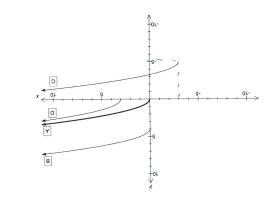
Determine the equation of the graph below.



[3 Marks]

Question 2

Graphs B, C and D are all translations (no dilations) of graph A. Write down the equations of B, C and D $\overrightarrow{x} \checkmark = \checkmark$ noiseupa sed weld blod ni nwods A dqes \Im



Graph B Graph B Graph D
$$y = \sqrt{x+3} - 5$$

Graph D $y = \sqrt{x+3} - 5$



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Polynomial Functions Practice Test



SECTION TWO: RESOURCE ALLOWED

TOTAL:

30 marks

EQUIPMENT:

pens, pencils, pencil sharpener, highlighter, eraser, ruler, SCSA formula sheet, scientific &/ or

CAS calculator, 1 A4 page of notes

WORKING TIME:

30 minutes

Show all of your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks.