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Max	Mark	Question	Max	Mark

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to candidates

Special items: null

To be provided by the candidate
Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/lapte, eraser, ruler, highlighters

Materials required/recommended for this section

Working time: fifty minutes
Reading time before commencing work: five minutes

Your Name

Your Teacher's Name

Your Name

Calculator-free

Section One:

UNITS 3 & 4

MATHEMATICS SPECIALIST

Question/Answer booklet

Semester Two Examination, 2020

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	50	34
Section Two: Calculator-assumed	11	11	100	89	66
Total					100

Instructions to candidates

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2016*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

(3 marks)

$$\int_{\pi}^{\frac{\pi}{2}} \sin(5x) \cos(5x) dx \quad \text{let } u = \sin 5x$$

(3 marks)

$$\int \cos^2(3x) dx$$

Evaluate

Question 1

Working time: 50 minutes.

- Separate pages are included at the end of this booklet. They can be used for planning your expenses and/or as additional space if required to continue an answer.

Planning: if you use the spare pages for planning, indicate this clearly at the top of the page.

Concluding: if you need to use the space to continue an answer, indicate this clearly at the top of the page.

Original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

This section has seven (7) questions. Answer all questions. Write your answers in the spaces

(50 Marks)

Question 2**(5 marks)**

Consider the function $P(z) = z^4 + 10z^2 + 9$ where z is a complex number.

a) Show that $(z + 3i)$ is a factor of $P(z)$.

(2 marks)

b) Solve for all values for $P(z) = 0$ in the form $a + bi$.

(3 marks)

Question 4

(3,3 & 1 = 7 marks)

Consider the following functions:

$$f(x) = e^{x+1}$$

$$g(x) = \frac{1}{\sqrt{x-2}}$$

$$h(x) = (x+3)^2$$

- a) Determine $f^{-1}(x)$ and its domain. (3 marks)

- b) Determine $g \circ h(x)$ and its domain. (3 marks)

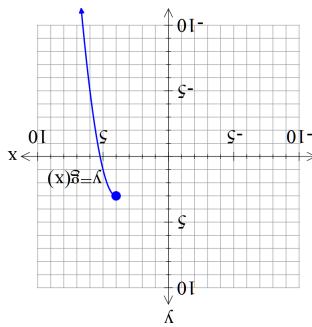
- c) Determine the solution(s), if any for $f \circ h(x) = -1$, explain. (1 mark)

(3 marks)

- b) Given that $g(x) = -2(x - 4)^2 + 3$, $x \geq 4$, determine the defining rule for $g_{-1}(x)$ and its domain.

(3 marks)

- a) Plot $y = g_{-1}(x)$ on the axes above showing all major features.



(6 marks)

Consider the function $g(x)$ which is plotted below.

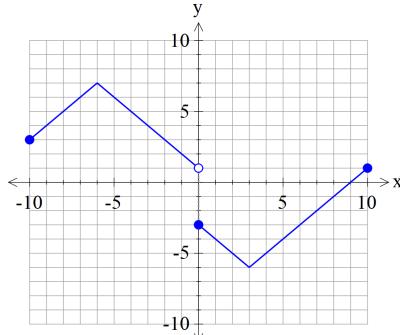
Question 5

Question 7
(6 marks)

Using the substitution $u = \sin x$, evaluate the integral $\int_{\pi}^{\frac{3\pi}{2}} -2 \cos x \, dx$. (Simplified)

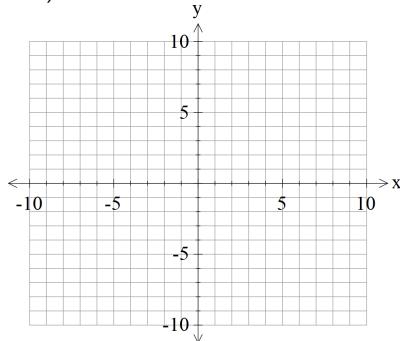
Question 6

Consider the function below.



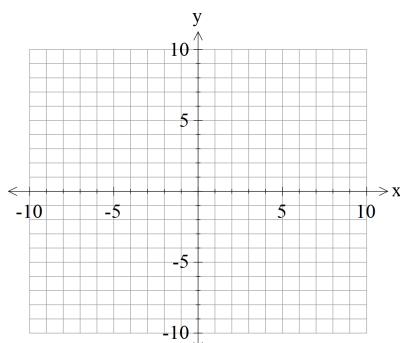
Sketch the following functions showing all major features.

a) $y = |f(x)|$



(2 marks)

b) $y = f(-|x|)$

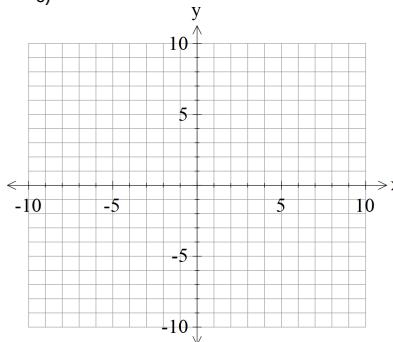


(3 marks)

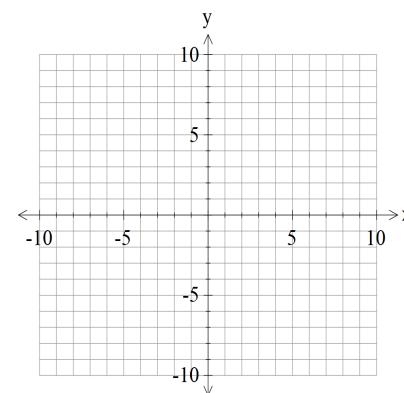
(11 marks)

(3 marks)

c) $y = |f(|x|)|$



d) $y = \frac{1}{|f(x)|}$



See next page

See next page