

Semester Two Examination, 2018

Question/Answer booklet

	ln words
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If required by your examination administrator, please place your student identification label in this box	1

4 GNA & STINU WETHODS MATHEMATICS

Calculator-free Section One:

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	Your nam
	sbrow nl

Resqing time before commencing work: miT

Student number:

Working time: sətunim yttif səmulu əm

To be provided by the supervisor Materials required/recommended for this section

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items:

Important note to candidates

it to the supervisor before reading any further. you do not have any unauthorised material. If you have any unauthorised material with you, hand No other items may be taken into the examination room. It is your responsibility to ensure that Trinity College 2 Semester 2 2018
Methods Year 12 Section 1 Calculator-Free

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	51	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

Instructions to candidates

- The rules for the conduct of Trinity College examinations are detailed in the *Instructions to Candidates* distributed to students prior to the examinations. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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Supplementary page

Question number: _____

Section 1 Calculator-Free Semester 2 2018

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32% (21 Marks)

Section One: Calculator-free

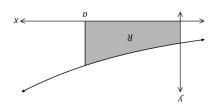
provided. This section has eight (8) questions. Answer all questions. Write your answers in the spaces

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Working time: 50 minutes.

(6 marks) Question 1

y = x pue 0 = x '0 = xThe shaded region R, shown on the graph below, is bounded by the curve $y=e^{4x}$ and the lines



(3 marks)

(3 marks)

Calculate the area of R in terms of a. (ဗ)

Determine the value of a for which the area of R is 20 square units.

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(s)

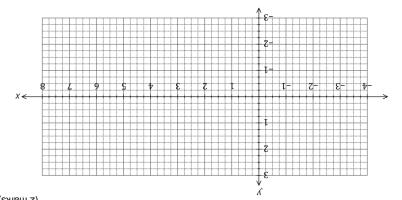
(8 marks) Question 8

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 $y = \log_5(x+1) - 1.$ Determine the coordinates of the x-intercept and y-intercept of the graph of

(2 marks)

(2 marks) all asymptotes and axes intercepts. Sketch the graph of $y = \log_5(x+1) - 1$ on the axes below, clearly showing the location of



(4 marks) coordinates of the root of the graph. The graph of $y = \log_a(x + a)$, where a > 1, passes through (15.75,2). Determine the

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Question 2

(5 marks)

(a) Simplify $\log_2(16) \div \log_5(125^2)$.

(2 marks)

(b) Solve the equation $\ln(4-x) + \ln 2 = 2 \ln x$.

(3 marks)

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Question 7 (6 marks)

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The time, t years, to repay a loan of \$180 000 at 4% interest with monthly repayments of x dollars can be approximated by

$$t = 25 \ln \left(\frac{x}{x - 600} \right), \quad x > 600$$

 (a) Determine the expression for the time to repay the loan when the monthly repayment is \$750.
 (1 mark)

(b) Use the increments formula to estimate the time saved in repaying the loan if the monthly repayment of \$750 is increased by 2%. (5 marks

maximum or a local minimum and state the coordinates of this point. (b) Use the second derivative test to determine whether the stationary point from (a) is a local (3 marks) (a) Determine the x-coordinate of the stationary point of the graph. The graph of $y=3xe^{2x}$ has one stationary point. (7 marks) Question 3 Section 1 Calculator-Free Methods Year 12

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(7 marks) Question 6 Section 1 Calculator-Free Methods Year 12 Semester 2 2018 Trinity College

A closed cylindrical can of radius $\, r \,$ cm has a volume of 250 $\pi \,$ cm $^3.$

(a) Show that the total surface area, A cm², of this can is given by $A = \frac{500\pi}{r} + 2\pi r^2$.

required to achieve this optimum area. Determine the minimum possible surface area of the can and the radius and height

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Question 4 (6 marks)

The random variable X has probability density function

$$f(x) = \begin{cases} k(2x-1)^3, & 0.5 \le x \le 2\\ 0, & \text{elsewhere.} \end{cases}$$

(a) Determine the value of the constant k.

(4 marks)

(b) Write down the cumulative distribution function $F(t) = P(X \le t)$ for $0.5 \le t \le 2$ and hence determine $P(X \le 1)$. (2 marks)

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Question 5

(6 marks)

(a) Determine the anti-derivative of
$$\frac{\cos(4x)}{7 + \sin(4x)}$$
.

(2 marks)

(b) (i) Determine
$$f'(x)$$
 when $f(x) = 4x \ln(3x)$.

(2 marks)

(ii) Hence, or otherwise, evaluate
$$\int_{\frac{1}{3}}^{2} (4 \ln(3x) + 4) dx$$
. (2 marks)