PENRHOS COLLEGE

STRIVE FOR THE HIGHEST

Semester One Examination 2011

Question/answer booklet

YEAR 12 MATHEMATICS 3C/DMAT

Section One (Calculator-Free)

Student Name: _____

Circle your teacher's name

S. ROWDEN N. EDMUNDS

Time allowed for this section

Reading time before commencing work: 5 minutes
Working time for section: 50 minutes

Material required/recommended for this section

To be provided by the supervisor
Question/answer booklet for Section One
Formula sheet

To be provided by the candidate
Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this examination

	Number of questions available	Number of questions to be attempted	Suggested working time (minutes)	Marks available
Section One: Calculator-free	**10**	**10**	**50 minutes**	**40**
Section Two: Calculator-assumed	15	15	100 minutes	80
			Total marks	120

Instructions to candidates

1. Answer the questions in the spaces provided.

2. Spare answer pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.

3. **Show all your working clearly.**
   Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks.
   For any question or part question worth more than two marks, valid working or justification is required to receive full marks.
   If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

4. It is recommended that you **do not use pencil** except in diagrams.

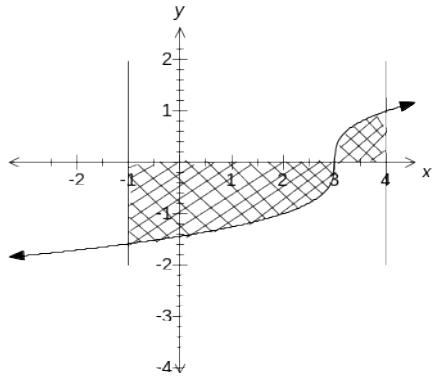
SEE NEXT PAGE

Section One: Calculator-Free 40 Marks

This section has **Ten (10)** questions. Attempt **all** questions.

Question 1 (3 marks)

Explain how you would find the area of the region bounded by the x-axis and the equations $y = (x - 2)^{\frac{1}{3}}$, $x = -1$ and $x = 4$. You are not required to find the area.



Question 2 (5 marks)

Differentiate the following: (do not simplify your answers)

(a) $y = 8x^4 + \frac{2}{x} - \frac{3}{7}$

(b) $y = \sqrt{x^2 - \frac{1}{x^2}}$

[2]

(c) $y = \frac{2x+1}{(3x+2)^2}$

[2]

SEE NEXT PAGE

Additional working space

Question number: _____

Additional working space

Question number: _____

Question 3 (4 marks)

In a probability experiment, events M and N are such that

$P(M)=\frac{1}{4}$, $P(N|M)=\frac{1}{3}$ and $P(\overline{M}\cap\overline{N})=\frac{1}{4}$

Find

(a) $P(M\cup N)$

[2]

(b) $P(N)$

SEE NEXT PAGE

Question 4 (7 marks)

Determine the following integrals:

(a) $\int (3x + x^{\frac{-2}{3}})\,dx$

(b) $\int \frac{x - 2x^3}{3x^5}\,dx$

SEE NEXT PAGE

Additional working space

Question number: _____

Question 10 (5 marks)

Simplify the following:

$$\frac{x^3 - 5x^2 - 14x}{x^2 - 2x - 3} \div \frac{x^2 - 4}{2x - 6}$$

END OF QUESTIONS

Question 4 Continued

(c) $\int \frac{1}{(3x - 2)^4} dx$

[2]

(d) $\int \frac{2}{\sqrt{x}}(3 - \sqrt{x})^2 dx$

Question 5 (3 marks)

Find the equation of the tangent to the curve $y = \frac{1}{3x + 2}$ at (-1, -1).

SEE NEXT PAGE

Question 6 (5 marks)

Solve the system of equations

$$x + y + z = 9$$
$$3x + y - 2z = 1$$
$$x + z = 2y$$

Question 7 (3 marks)

Determine the value of b for the following, given b is a positive integer.

$$10 = \int_4^b \frac{1}{\sqrt{x}}\, dx$$

Question 8 (3 marks)

Solve for y the inequality $\frac{1}{y - 1} < \frac{1}{y + 1}$

Question 9 (2 marks)

Find $\frac{d}{dx}\left(\int_3^{2x^2} t(6 - t)\, dt\right)$