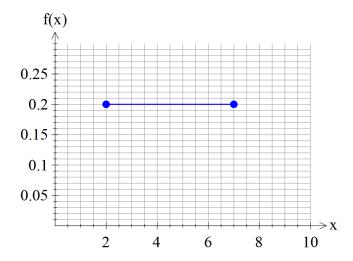


Coursel	Methods_Test 4_ Year12						
Student name: Teacher name:							
Date: Weds 26 Au g	gust						
Task type:	Response						
Time allowed for this	s task:45 mins						
Number of questions	s:6						
Materials required:	Calculator with CAS capability (to be provided by the student)						
Standard items:	Pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters						
Special items:	Drawing instruments, templates, notes on one unfolded sheet of A4 paper, and up to three calculators approved for use in the WACE examinations						
Marks available:	46 marks						
Task weighting:	10%						
Formula sheet provi	ded: Yes						

Note: All part questions worth more than 2 marks require working to obtain full marks.

Q1 (1, 1, 1 & 3 = 6 marks)

Consider a continuous random variable X that is uniformly distributed as follows.



Determine the following:

$$P(X>3)$$

b)
$$P(X \ge 3)$$

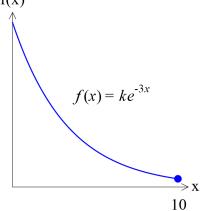
c)
$$P(1 < X \le 7)$$

Q2 (3 marks)

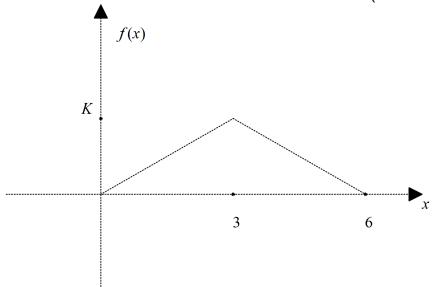
Consider a continuous random variable X shown below.

Solve for the constant k exactly. (Show all working)

$$f(x) = \begin{cases} ke^{-3x} & 0 \le x \le 10\\ 0 & elsewhere \end{cases}$$



Q3 (1 , 4, 1 & 2 = 8 marks) Consider a continuous random variable X shown below. (Not drawn to scale)



a) Determine the value of the constant $\,K\,.$

b) Determine P(1 < x < 4)

c) Determine E(X)

d) Determine Standard deviation of \boldsymbol{X}

Q4 (2, 2, 2 & 1 = 7 marks)

$$f(x) = \begin{cases} \frac{3}{16}(x-3)^2 & 1 \le x \le 5\\ 0 & elsewhere \end{cases}$$

A continuous random variable, $\,^{X}\,$ has a pdf Determine:

a) E(x)

b) Var(X)

- c) Standard deviation
- d) Var(3x 1)

Q5 (2, 2, 2 & 3 = 9 marks)

The results for a class test, X can be modelled by a Normal Distribution given by $X \sim N(60,15^2)$. Determine:

a) The 78th percentile.

b)
$$P(55 \le X \le 72)$$

c) The cut-off for an A grade given that this grade is only given to the top 20%.

d) A second test is a Normal Distribution with a mean of 55. Given that the 58th percentile is 62, determine the standard deviation.

Q6 (3, 3, 3, 2 & 2 = 13 marks)

The time it takes to be served at a supermarket checkout, X seconds, can be modelled by a normal distribution as follows the following scheme. $X \sim N(103, 30^2)$ seconds. The assistant at the check out is paid according to the following scheme.

Time served	$0 \le X < 35$	$35 \le X < 60$	$60 \le X < 150$	$150 \le X < 200$	<i>X</i> ≥200
In seconds					
Payment \$P	\$5	\$7	\$12	\$15	\$18
Probability					
To 4 decimal					
places					

- a) Fill in the probability line of the above table rounded to three decimal places.
- b) Determine the expected payment E(P) showing full working.

c) Determine the variance of the payment Var(P) showing full working.

d) If the payments were all increased by 30% and a bonus of \$2 added to each category, determine the new mean and standard deviation.

e) Explain a limitation of the Normal distribution model and show a calculation to support this.