

Question	Marks	Max	Quesiton	Mark	Max
8	6	15		8	
9	8	16		8	
10	6	17		10	
11	4	18		8	
12	10	19		8	
13	9	20		8	
14		8			

Important note to candidates

Also other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Special terms: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

What are the standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Materials required/recommended for this section
To be provided by the supervisor
This question/Answer booklet
formula sheet (retained from Section One)

Time allowed for this section
Reading time before commencing work:
one hundred minutes

Your Teacher's Name:

Your Name:

UNIT 3 MATHEMATICS METHODS Section Two: Calculator-assumed

Question/Answer booklet

Semester One Examination, 2019



Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	34
Section Two: Calculator-assumed	13	13	100	103	66
Total					100

Instructions to candidates

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

$$P(X=4) + P(X=5) = 0.3$$

Solution

(1 mark)

b) Find $P(X \geq 4)$

		\checkmark determines probs for all x values \checkmark determines probs for $x=2 \& 3$ specific behaviours																	
		<table border="1"> <tr> <td>$P(X=x)$</td><td>0.1</td><td>0.3</td><td>0.3</td><td>0.2</td><td>0.1</td></tr> <tr> <td>x</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr> </table>						$P(X=x)$	0.1	0.3	0.3	0.2	0.1	x	1	2	3	4	5
$P(X=x)$	0.1	0.3	0.3	0.2	0.1														
x	1	2	3	4	5														
		Solution																	

(2 marks)

a) Complete the probabilities in the table below

$P(X \leq x)$	0.1	0.4	0.7	0.9	1
x	1	2	3	4	5

$$P(X=0)=0$$

Consider the following table with

(6 marks)

Question 8

Working time: 100 minutes.

- Responses and/or as additional space if required to continue an answer.
- Continuum: If you need to use the spare pages for planning, indicate this clearly at the top of the page.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
- This section has **thirteen** questions. Answer all questions. Write your answers in the spaces provided.

(103 Marks)

Section One: Calculator-assumed

Specific behaviours	
✓ determines prob by adding for $x=4$ & 5	

Question number: _____

- c) Find $P(x>2 \vee x<4)$ (simplify) (3 marks)

Solution	
$P(x>2 x<4) = \frac{P(x=3)}{P(x<4)} = \frac{0.3}{0.7} = \frac{3}{7}$	
Specific behaviours	
✓ uses conditional prob formula ✓ determines correct quotient of probs ✓ expresses as simple fraction of integers	

Question 9 (8 marks)

A liquid is spilled onto a floor forming a circle of radius r metres. The surface area, A , square metres, of the spilt liquid is given by $A = \int_0^r 15e^{\frac{x^2}{20}} dx$.

- (a) Determine $\frac{dA}{dr}$ when $r=5$ metres. (2 marks)

Solution	
$\frac{d}{dr} \int_0^r 15e^{\frac{x^2}{20}} dx = 15e^{\frac{r^2}{20}}$	
$= 15e^{\frac{25}{20}} = 15e^{\frac{5}{4}}$	
Approx. 7770.2	
Specific behaviours	
✓ uses fundamental theorem ✓ states an approx value for rate	

$\frac{dA}{dt} = \frac{dr}{dt} \cdot \frac{dA}{dr} = 15e^{2t} \cdot 8640 = 15e^{2t} \cdot 8640$ $= 6e^t = 1296$ $= 40(6) = 240$ $A = \int_{-1}^t (5e^z + 1)^2 dz = 4(5e^z + 1) \Big _{-1}^t = 4(5e^t + 1 - 5e^{-1} - 1) = 4(5e^t - 5e^{-1}) = 20(e^t - e^{-1})$	Solution	states derivative of radius wrt time and radius at t=1 Specific behaviours uses chain rule with $\frac{dA}{dr}$ uses fundamental theorem of calculus gives an exact expression (no need to simplify)
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(4 marks)

c) Determine $\frac{dA}{dt}$ when $t = 1$ second as an exact value.

The radius, r , varies with time, t seconds, by the model $r = \sqrt{5t^2 + 1}$.

Solution	Rate of change of area with respect to radius.
Specific behaviours	Stales a rate with respect to radius

(2 marks)

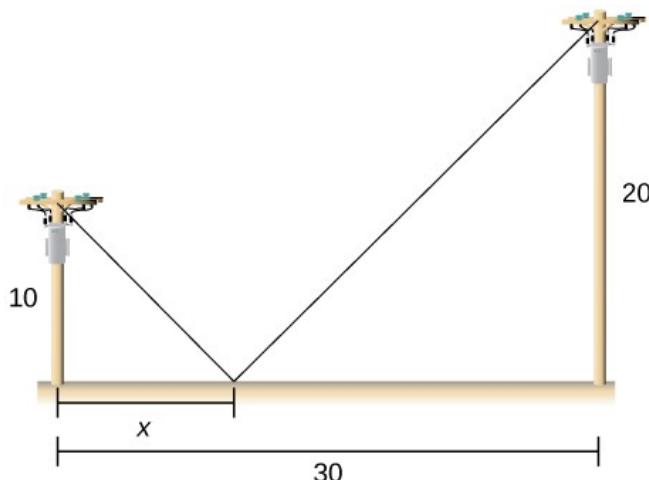
b) What is the meaning of your answer in (a) above?

Question number:

Additional working space

Question 10**(6 marks)**

Two power poles need to be joined using a wire that is also connected to the ground, as shown below. The two poles are 10 and 20 metres high, and are separated by 30 metres.



- (a) Determine an expression for the length of wire needed in terms of x metres. (2 marks)

Solution
$\sqrt{10^2 + x^2} + \sqrt{20^2 + (30 - x)^2}$
Specific behaviours
✓ uses Pythagoras with x ✓ states total length in terms of x

Specific behaviours

Using **calculus**, show how to determine the value of x to minimize the length of wire required. Determine this length to the nearest centimetre. (4 marks)

(Use of a classpad is required)

Solution

$$\frac{dl}{dx} = \frac{\sqrt{100+x^2} + \sqrt{20+(30-x)^2}}{2x}$$

$$l = \sqrt{100+x^2} + \sqrt{20+(30-x)^2}$$

$$\frac{dx}{dx} \left(\sqrt{100+x^2} + \sqrt{400+(30-x)^2} \right) =$$

$$\text{solve} \left(\sqrt{x\sqrt{x^2-60x+1300+x\sqrt{x^2+100-30\sqrt{x^2+100}}} = 0 \right)$$

Second derivative at $x=10$ is positive as shown below.

$$\frac{d^2l}{dx^2} = \frac{\sqrt{x^2-60x+1300+x\sqrt{x^2+100-30\sqrt{x^2+100}}}}{x^2-60x+1300+x\sqrt{x^2+100}}$$

Alg Standard Cplx Deg

30·V2

Length = 42.43 metres(4243cm)

42.42640687

Specific behaviours

- ✓ states total length of wire to nearest cm
- ✓ equates derivative to zero and solves for x
- ✓ states derivative of length in terms of x
- ✓ equates derivative to zero and solves for x
- ✓ states total length of wire to nearest cm

Specific behaviours

Determine the acceleration of the spot of light when $\theta = \frac{\pi}{6}$ radians. (4 marks)

Solution

$$v = 200 \frac{\cos^2 \theta}{4\tau} = 800\tau \cos^2 \theta$$

$$a = \frac{dv}{dt} = \frac{d\theta}{dt} \frac{dv}{d\theta} = \frac{\cos^2 \theta}{4\tau} (-\sin \theta) 4\tau$$

$$= -6400\tau^2 (-1) = \frac{3\sqrt{3}}{25600\tau^2} = 48624.8 \text{ m/s}^2$$

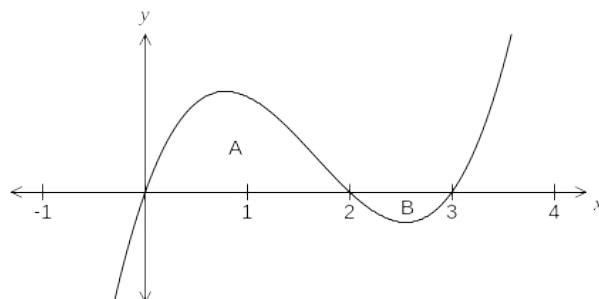
$$= \frac{\sqrt{3}}{2} \left(\frac{2}{2} \right) = \frac{3\sqrt{3}}{2} \approx 48624.8 \text{ m/s}^2$$

obtains an approx value for acceleration (no need of units) or exact un-simplified
 ✓ uses chain rule
 ✓ differentiates velocity wrt time
 ✓ subs required angle and rate
 ✓ obtains acceleration for acceleration (no need of units) or exact un-simplified

✓ uses second derivative sign test or first derivative to show a minimum

Question 11**(4 marks)**

Part of the graph of $y=f(x)$ is shown below. The areas of regions A and B, bounded by the curve and the x -axis, are 16 and 2 square units respectively.



Evaluate:

a) $\int_{-2}^3 f(x) dx$ (1 mark)

Solution

-2

Specific behaviours

✓ states integral value

b) $\int_0^3 f(x) dx$ (1 mark)

Solution

16-2=14

Specific behaviours

✓ states total value

$$\begin{aligned}\frac{d \tan \theta}{d \theta} &= \frac{d \left(\frac{\sin \theta}{\cos \theta} \right)}{d \theta} = \frac{\cos \theta \cos \theta - \sin \theta (-\sin \theta)}{\cos^2 \theta} \\ &= \frac{\sin^2 \theta + \cos^2 \theta}{\cos^2 \theta} \\ &= \frac{1}{\cos^2 \theta}\end{aligned}$$

Specific behaviours

- ✓ subs u and v into quotient rule with derivatives
- ✓ uses trig identity
- ✓ simplifies to required result

c) Determine the velocity of the spot of light, $\frac{dx}{dt}$ in metres/second, when $\theta = \frac{\pi}{6}$ radians.
 $\frac{dx}{dt} = \frac{dx}{d\theta} \frac{d\theta}{dt}$ with $\frac{d\theta}{dt} = 4\pi$
(Hint- use $\frac{dx}{dt} = \frac{dx}{d\theta} \frac{d\theta}{dt}$ with $\frac{d\theta}{dt} = 4\pi$) (3 marks)

Solution

$$\begin{aligned}\frac{dx}{dt} &= \frac{dx}{d\theta} \frac{d\theta}{dt} = 200 \frac{1}{\cos^2 \theta} 4\pi \text{ OR } 200(1 + \tan^2 \theta) 4\pi \\ &= 800\pi \frac{1}{\left(\frac{\sqrt{3}}{2}\right)^2} = \frac{3200\pi}{3} \text{ m/s} \approx 3351 \text{ m/s}\end{aligned}$$

Specific behaviours

- ✓ differentiates x wrt θ
- ✓ uses chain rule with correct angle
- ✓ obtains approx value of velocity

(3 marks)

(b) The first time that the train begins to decelerate.

Specific behaviours	
✓ states max speed(must be positive)	
✓ integrates to determine velocity(no constant required)	
max speed = $\frac{3}{5} \text{ m/s}$	
$v = -\frac{3}{5} \cos\left(\frac{3t}{5}\right) + c$ OR $\frac{3}{5} \sin(3t) + c$	
$c = 0$	
$v = -\frac{3}{5} \cos\left(\frac{3t}{5}\right) + c$ OR $\frac{3}{5} \sin(3t) + c$	
$\frac{dv}{dt} = 5 \sin\left(\frac{3t}{5}\right) + \frac{2}{5}$ OR $5 \cos(3t)$	
Solution	

(2 marks)

(a) The greatest speed of the train.

Determine:

The train begins at the origin and at rest.

$$a = 5 \sin\left(3t + \frac{\pi}{2}\right)$$

(10 marks)

A train on a monorail moves with velocity, v metres per second, at time t seconds, in a straight line, with acceleration, a metres per second squared, given by:

(10 marks)

Question 12

Specific behaviours	
✓ uses linearity and breaks into two integrals	
✓ states value	
$\int_2^0 (x) - 3 dx = \int_2^0 (x) dx - \int_2^0 3 dx = [4 - 3x]_2^0 = 16 - 6 = 10$	
Solution	

(2 marks)

$$(c) \quad \int_2^0 f(x) - 3 dx$$

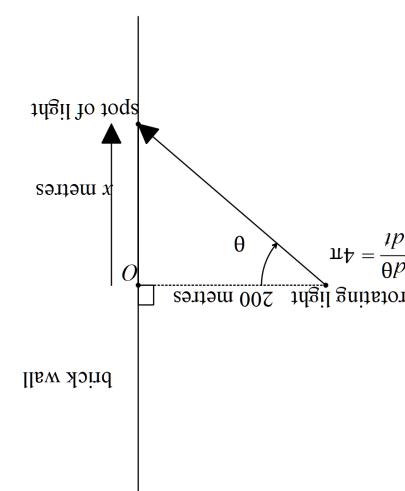
b) By using $\tan \theta = \frac{\sin \theta}{\cos \theta}$ and the quotient rule, show that $\frac{d\theta}{d(tan \theta)} = \frac{\cos^2 \theta}{1}$ (3 marks)

Specific behaviours

$$\tan \theta = \frac{x}{200}$$

a) Show that $x = 200 \tan \theta$.

(1 mark)



Solution
$\frac{dv}{dt} = 5 \sin\left(3t + \frac{\pi}{2}\right)$ $3t = \frac{\pi}{2}$ $t = \frac{\pi}{6}$
Specific behaviours
<ul style="list-style-type: none"> ✓ equates acceleration to zero ✓ solves for first positive value of time ✓ states first time

- (c) An expression for the displacement of the train from the origin. (3 marks)

Solution
$\frac{dv}{dt} = 5 \sin\left(3t + \frac{\pi}{2}\right)$ $v = -\frac{5}{3} \cos\left(3t + \frac{\pi}{2}\right) + c$ $c = 0$ $v = -\frac{5}{3} \cos\left(3t + \frac{\pi}{2}\right)$ $x = -\frac{5}{9} \sin\left(3t + \frac{\pi}{2}\right) + c$ $t = 0, x = 0$ $0 = -\frac{5}{9} + c$ $c = \frac{5}{9}$ $x = -\frac{5}{9} \sin\left(3t + \frac{\pi}{2}\right) + \frac{5}{9}$
Specific behaviours
<ul style="list-style-type: none"> ✓ integrates velocity ✓ solves for constant ✓ states displacement function

See next page

- c) The area trapped between the graphs of $y=f(x)$ and $y=h(x)$ is 36 square units. Determine the value of m . (4 marks)

Solution
$\int_0^{3+m} mx + 4 - x^2 + 3x - 4 dx = 36$ $\int_0^{3+m} -x^2 + (3+m)x dx = 36$ $\left[-\frac{x^3}{3} + (3+m)\frac{x^2}{2} \right]_0^{3+m} = 36$ $-\frac{(3+m)^3}{3} + (3+m)\frac{(3+m)^2}{2} = \frac{(3+m)^3}{6} = 36$ $3+m = 6$ $m = 3$
Specific behaviours
<ul style="list-style-type: none"> ✓ shows integral in terms of m ✓ sets up equation with integral for m ✓ shows integration equation for m ✓ solves for m

Question 20

(8 marks)

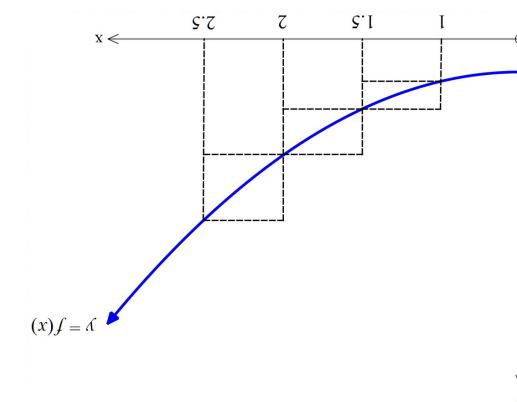
On a tarmac of a wide airfield is a rotating light that has two complete revolutions per second. (4π radians/second) The light is placed 200 metres in front of a long brick wall as shown in the diagram below. As the light is shone against the wall, the spot of light can be seen racing across the wall. Let x = the displacement of the spot of light from the point closest to the light, point O, on the wall.

See next page

(3 marks)

a) By considering the areas of the rectangles shown, demonstrate and explain why $4.1 < \int_{2.5}^1 f(x) dx < 5.9$.

$f(x)$	1	1.8	2	2.6	3.8	5.4
x	2	1.5	1	1.2	0.8	0.5



Consider the function $f(x)$ shown graphed below. The table gives the value of the function at the given x values.

(9 marks)

Question 13

- ✓ recognizes that sin function equals -1
- ✓ states max distance (no need for units)

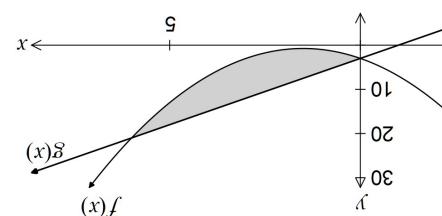
Solution

$$x = \frac{5}{9} + \frac{9}{10} = \frac{9}{10}m$$

(2 marks)

- (d) The maximum distance that the train is from the origin.

The graphs of $y=f(x)$ and $y=g(x)$ are shown on the axes below.



Solution

(2 marks)

- Show that the graphs of $y=f(x)$ and $y=h(x)$ intersect when $x=0$ and $x=m+3$.

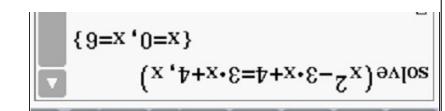
- ✓ states limits
- ✓ shows integral of difference for positive area

Solution

$$\int_0^6 [3x + 4 - (x^2 - 3x + 4)] dx$$

OR

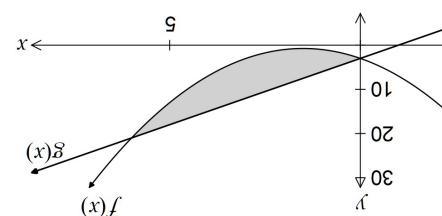
$$\int_0^6 [3x + 4 - (x^2 - 3x + 4)] dx$$



Solution

(2 marks)

- State the integral required to calculate the shaded area.



Solution
Upper value = $0.5 \times 2.6 + 0.5 \times 3.8 + 0.5 \times 5.4 = 5.9$
Lower value = $0.5 \times 1.8 + 0.5 \times 2.6 + 0.5 \times 3.8 = 4.1$
Definite integral represents area under curve from $x=1$ to $x=2.5$ in this context

Specific behaviours
✓ states that integral represents area
✓ shows area of larger rectangles
✓ shows area of smaller rectangles

Consider the table of further values of $f(x)$ given below.

x	0	1	1.5	2	2.5	3	3.5
$f(x)$	1	1.8	2.6	3.8	5.4	7.3	9.6

- b) Use the table values to determine the best estimate possible for $\int_1^3 2f(x)dx$ (4 marks)

Solution
$0.5 \times 1.8 + 0.5 \times 2.6 + 0.5 \times 3.8 + 0.5 \times 5.4$
$< \int_1^3 f(x)dx < 0.5 \times 2.6 + 0.5 \times 3.8 + 0.5 \times 5.4 + 0.5 \times 7.3$
$6.8 < \int_1^3 f(x)dx < 9.55$
$\int_1^3 f(x)dx \approx \frac{6.8 + 9.55}{2} = 8.175$
$\int_1^3 2f(x)dx \approx 16.35$
Specific behaviours
✓ shows sum of lower rectangles
✓ shows sum of upper rectangles
✓ uses average

See next page

- b) Determine the selling price per unit to establish the maximum profit in (a) above. (2 marks)

Solution
$x(3x^2+19x+4)$ $x \cdot (3 \cdot x^2 + 19 \cdot x + 4)$ $(3 \cdot x^2 + 19 \cdot x + 4) x=50$ 8454
Selling price per unit = \$8454
Specific behaviours
✓ factorises revenue ✓ determines selling price for $x=50$

- c) What is the average cost of producing 100 items? (2 marks)

Solution
$\int_0^{100} 3x^3 + 20x^2 - 96x - 80000 x=100$ 3110400 3110400/100 31104
Average cost is \$31104
Specific behaviours
✓ subs $x=100$ into cost function ✓ divides total cost by 100 items

Question 19

(8 marks)

Consider the following 3 equations, where m is a positive real constant:

$$\begin{aligned}f(x) &= x^2 - 3x + 4 \\g(x) &= 3x + 4 \\h(x) &= mx + 4\end{aligned}$$

See next page

Solution						
X \$	Number of houses sold in a month	0	1	2	3	4
Probability		0.15	0.4	0.3	0.1	0.05
$E(X)$		1000	2500	4000	5500	7300
		=3265				

- (a) The expected monthly earning of the realtor, $E(X)$. (4 marks)

Determine:

Let $X = ?$ the monthly earning of the realtor.

The realtor is paid \$1000 every month with a bonus of \$1500 for every house sold up to three houses and a special bonus of \$1800 if four or more houses are sold in a month.

Distribution						
Number of houses sold in a month	0	1	2	3	0.1	0.05
Probability		0.15	0.4	0.3	0.1	0.05
$E(X)$		1000	2500	4000	5500	7300
		=3265				

- A realtor's sales history over any month can be represented by the following probability distribution:

Using calculus methods, determine the number of units, x , to maximise the profit.

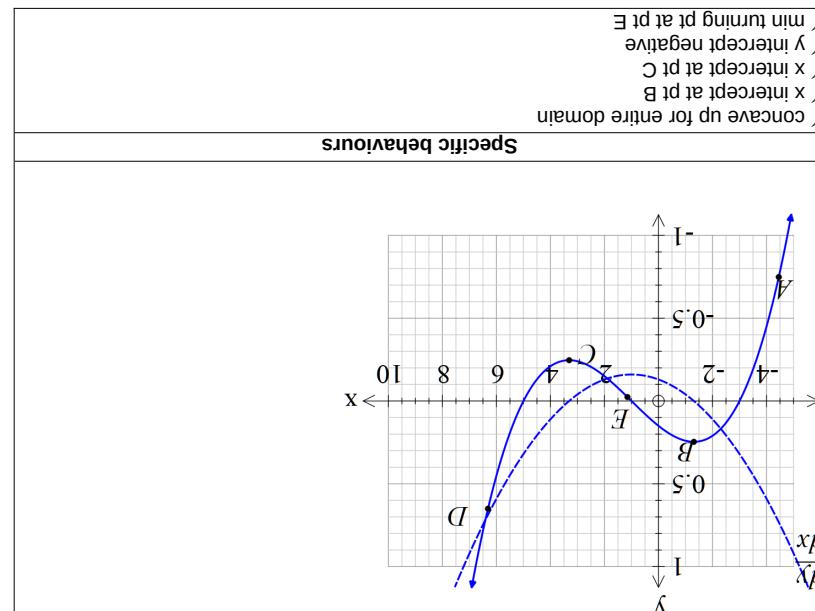
(8 marks)

Question 14

Solution						
*model a rule for function and integrate						
*use smaller widths of rectangles						
States one reasonable method						
States two reasonable methods						

- (c) State two ways in which you could determine a more accurate value for $\int_3^1 2f(x) dx$ (2 marks)

Solution						
Specific behaviours						
$P(x) = R - C = -x^2 + 100x + 80000$						
$\frac{dp}{dx} = -2x + 100$						
$x = 50$						
$-2x + 100 = 0$						
$\frac{dp}{dx} = -2x + 100$						
$d^2p \quad = -2 \therefore \text{local max}$						
\checkmark uses second derivative sign test (or first) to verify a maximum						
\checkmark determines derivative and equations to zero						
\checkmark states profit function						
\checkmark solves for x						
\checkmark uses second derivative sign test (or first) to verify a maximum						



Specific behaviours		
✓ states two values of earnings, X		
✓ states all earning values for X		
✓ shows calculation for expected value of X		
✓ states expected value		

- (b) The standard deviation of X . (2 marks)

Solution		
Specific behaviours		
✓ calculates variance		
✓ states standard deviation(answer only required for full marks)		

- (c) Variance ($5X - 3$). (2 marks)

Solution		
$Variance = 5^2 \times V_{\text{obj}} = 25 \times 1574.57^2 = 61981767.12$		
Specific behaviours		
✓ multiplies by 25 and does NOT subtract 3		
✓ states variance(accept standard notation)		

Question 15 (8 marks)

Consider a fair die with the numbers $\{1, 2, 3, 4, 5, 6\}$. The random variable X is defined as the number of trials of the thrown die showing an even number on top.

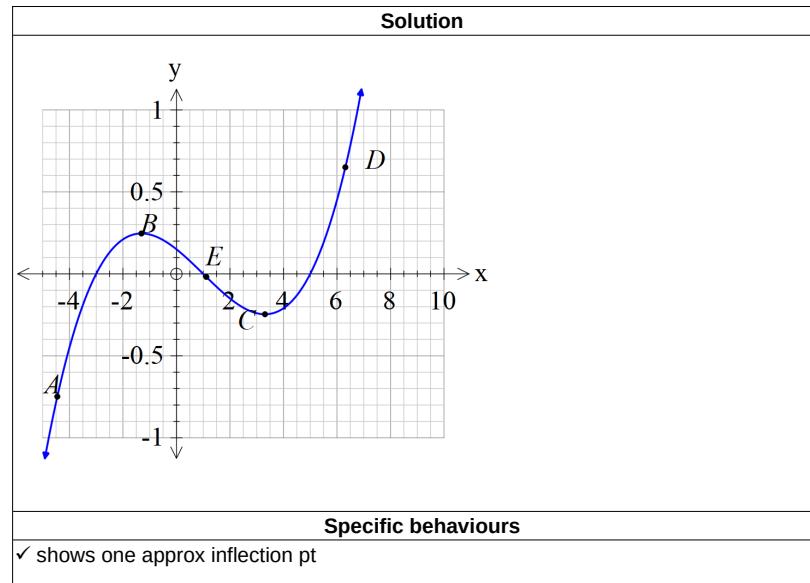
- (a) If you throw the die 11 times,
- (i) Determine the probability that you will end up with more even numbers than odd numbers. (2 marks)

See next page

B	zero	-ve
C	Zero	+ve
D	+ve	+ve

Specific behaviours		
✓ two correct first derivatives		
✓ all first derivatives correct		
✓ two correct second derivatives		
✓ all second derivatives correct		

- b) Indicate on the graph of f above the inflection point and label as E . (1 mark)



- c) Sketch the graph of f' on the same axes as the graph of f above. (5 marks)

Solution		

See next page

<p>Solution</p> <p>$X \sim \text{Bin}(10, 0.5)$</p> <p>$p(X=2) + p(X=4) + p(X=6) + p(X=8) + p(X=10)$</p> <p>OR</p> <p>$=0.49951$</p> <p>$=0.4995$</p> <p>$=0.5000$</p> <p>$=$ 0.5000</p> <p>specific behaviours</p> <ul style="list-style-type: none"> ✓ states binomial dist ✓ states all even values of X ✓ states prob to 4 decimal places
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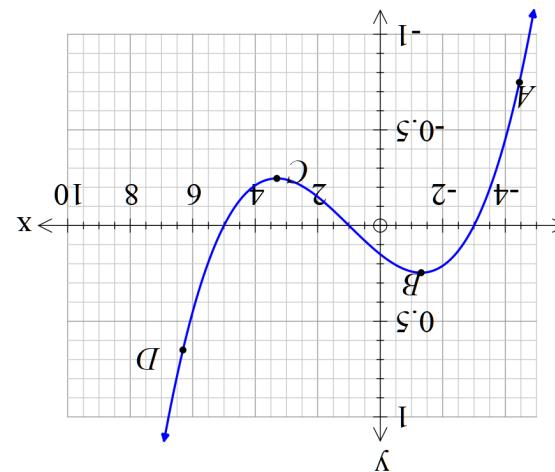
(3 marks)

- (ii) Determine the probability, to 4 decimal places, that there are in total, even number of times that the die shows an even number.

<p>Solution</p> <p></p> <p>specific behaviours</p> <ul style="list-style-type: none"> ✓ uses binomial cdf with correct parameters ✓ states probability
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See next page				
<p>Solution</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>Point</td> <td>f'</td> <td>f''</td> <td>-ve</td> </tr> </table>	Point	f'	f''	-ve
Point	f'	f''	-ve	

- a) A, B, C, D are points on the graph of f . Determine whether the first and second derivatives are positive, negative or equal to zero at these points. Record your findings in the table below.
- (4 marks)

The graph of a function f is given below.

(10 marks)

Question 17

<p>Solution</p> <p></p> <p>specific behaviours</p> <ul style="list-style-type: none"> ✓ uses correct limits ✓ uses integration (or antiderivative) ✓ states net change

- (b) If you would like to get at least three times an even number. Find the minimum times that you need to throw the die for which the probability of three or more even numbers is at least 85%. (3 marks)

Solution

The calculator screen shows the following sequence of commands and results:

```

binomialCDF(3, 5, 5, 0.5)
0.5
binomialCDF(3, 6, 6, 0.5)
0.65625
binomialCDF(3, 7, 7, 0.5)
0.7734375
binomialCDF(3, 8, 8, 0.5)
0.85546875

```

8 throws

Specific behaviours

- ✓ shows at least two attempts with differing n values
- ✓ states value of n=7
- ✓ states n=8

Question 16 (8 marks)

The marginal profit from the sale of x^{th} item is given by $P'(x)=0.0015x^2+1.6x-4.8$, where $P(x)$ is the profit from selling x items.

- a) Given that the company incurs a loss of \$70 if no items are sold, find an expression for P in terms of x . (3 marks)

Solution

$$\begin{aligned} \frac{dP}{dx} &= 0.0015x^2 + 1.6x - 4.8 \\ P(x) &= 0.0005x^3 + 0.8x^2 - 4.8x + c \\ -70 &= c \\ P(x) &= 0.0005x^3 + 0.8x^2 - 4.8x - 70 \end{aligned}$$

Specific behaviours

- ✓ integrates
- ✓ uses a constant
- ✓ solves for constant

- b) Hence determine the profit from selling 80 items. (2 marks)

Solution

The calculator screen shows the following command and result:

```

0.0005x^3+0.8x^2-4.8x-70 | x=80
4922

```

Profit of \$4922

Specific behaviours

- ✓ subs x=80
- ✓ states profit

- c) Find the net change in profit if the number of items sold changes from 80 to 160 items. (3 marks)

Solution