Eastern Hills Senior High School

WA Exams Practice Paper C, 2015

Question/Answer Booklet

If required by your examination administrator, please place your student identification label in this box

S QNA	l	ST	.INC
SC	10	LHC	L∃Ν
SOITAN	NΞ	LHE	TAN

Calculator-assumed Section Two:

allowed for this section time before commencing work: time for section: one hundred minutes	gaibs
Your name	
n words	
Student Number: In figures	

Rea Wor

Materials required/recommended for this section

To be provided by the supervisor

Formula Sheet (retained from Section One) This Question/Answer Booklet

To be provided by the candidate

fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction

and up to three calculators approved for use in the WACE examinations drawing instruments, templates, notes on two unfolded sheets of A4 paper, Special items:

Important note to candidates

before reading any further. examination room. If you have any unauthorised material with you, hand it to the supervisor you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be taken into the examination room. It is your responsibility to ensure that

permission of WA Exam Papers. school. No other copying, communication or use is permitted without the express written to copy and communicate this paper for non-commercial, educational use within the © 2015 WA Exam Papers. Eastern Hills Senior High School has a non-exclusive licence METHODS UNITS 1 AND 2 2 CALCULATOR-ASSUMED

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
			Total	150	100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question that you are continuing to answer at the top of the
 page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

See next page

CALCULATOR-ASSUMED	19	METHODS UNITS 1 AND 2
--------------------	----	-----------------------

Additional	working	space

Question number: _____

		ere any indication that swimmir he gender of the swimmer? Ju:			(၁)
lark)	m t)	y were female.	wam regularly, given that the	s (ii)	
ark)	vtilidsdorq e m t)	those surveyed, determine the	er is selected at random from wam regularly.		(q)
	162		601	lstoT	
				Male	
				Female	
	Total	Did not swim regularly	Swam regularly		
stion 8 (5 marks) random survey of 162 swimmers at a council owned pool, 109 said they swam regularly. 39 as said they swam regularly and 16 fewer males than females were surveyed. Complete this two-way table using the above information. (2 marks)					ln a ra
			section is 50 minutes.	og time for this	Worki

This section has thirteen (13) questions. Answer all questions. Write your answers in the spaces

3

Section Two: Calculator-assumed

CALCULATOR-ASSUMED

CALCULATOR-ASSUMED

81

(98 Marks)

METHODS UNITS 1 AND 2

Question number: _

Additional working space

METHODS UNITS 1 AND 2

maximum number of pages the draft contained. (1 mark)

Determine T_{10} of the arithmetic sequence where $T_1 = x - 3$, $T_2 = 2x + 1$ and $T_3 = 4x - 1$. (3 marks) **CALCULATOR-ASSUMED**

17

METHODS UNITS 1 AND 2

Additional working space

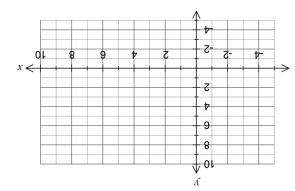
Question number: _____

(8 marks) Question 10 G

$$\frac{\zeta}{x-1} = (x) \int dx \, dx$$
 (a)

State the equations of the asymptotes of the graph of
$$y = f(x)$$
. (2 marks)

(2 marks) Sketch the graph of y = f(x).



- The two variables h and w are inversely proportional to one another.
- (2 marks) Circle all of the equations below that reflect this relationship, where $\,k\,$ is a

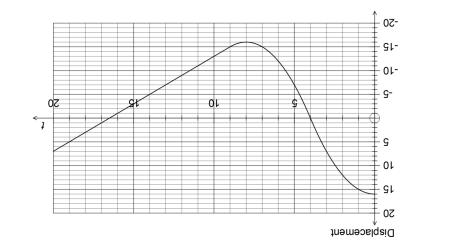
$$\gamma = \frac{M}{\eta}$$
 $\gamma = \frac{M}{\eta}$ $\gamma = \frac{M}{\eta}$ $\gamma = \gamma$

When
$$h=12.5$$
, $w=38.8$. If h decreases by 2.8, by how much will w change? (2 marks)

(2 marks) Question 20

9١

for the interval $0 \le t \le 20$ seconds. ground. The displacement in metres, of the train relative to point A, is shown on the graph below A small toy train is able to travel backwards and forwards along a straight track built on level



- (1 mark) State an interval of time during which the train is moving towards point A.
- (1 mark) What total distance did the train travel during the 20 second interval?
- (3 marks) velocity of the train when t = 6. By drawing adding a suitable tangent to the graph above, determine an estimate for the

6 **Question 11** (10 marks)

Determine x if the terms 12, x, 27 form part of a geometric sequence. (2 marks)

- A team of workers is using a pile driver to drive wooden poles 4 metres long into the ground. The first hit of the pile driver drives a pole 50 cm into the ground. The second hit drives the pole another 40 cm into the ground. The third hit drives the pole another 32 cm into the ground and successive distances driven by the pile driver form a geometric sequence.
 - How much further will the fourth hit drive the pole into the ground? (1 mark)
 - Determine the total distance the wooden pole has been driven into the ground after 12 hits of the pile driver. (2 marks)

If the workers continued in this way for some time, what length of the wooden pole will always be left above the ground? Justify your answer. (2 marks)

A geometric series has a first term of 80 and a sum to infinity of 800. Determine the minimum number of terms of this sequence required so that their sum exceeds 700. (3 marks)

Question 19

CALCULATOR-ASSUMED

(6 marks)

A cone has a radius r and perpendicular height h and is such that the sum of the radius and twice the height is 45



Show that the volume, V, of the cone is given by $V = \frac{\pi}{3} \left(4h^3 - 180h^2 + 2025h \right)$ cm³. (3 marks)

Using calculus techniques, find the height that will maximise the volume of the cone, and state this maximum volume, rounded to one decimal place. (3 marks)

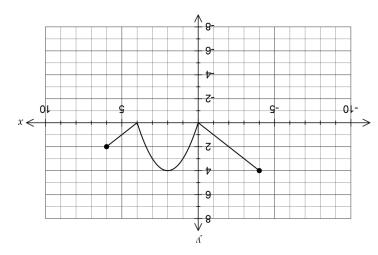
Question 12

(2 marks)

(2 marks) State the domain and range of $f(x) = x^4 - 4$.

L

The graph of y = g(x) is shown below.



On the same axes, sketch the graph of

$$y = g(x) - 4.$$

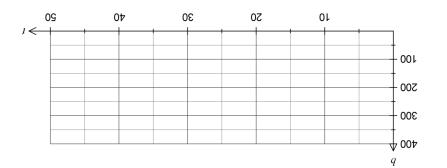
$$\gamma = g(2x). \tag{2 marks}$$

(9 marks) **&t noitsau** れ

measurements began can be modelled by the function $b(t) = r + p \sin(qt)$. The brightness of a small incandescent light globe, b lumens, t milliseconds after

lumens and then dropping to a minimum brightness of 50 lumens after a further 10 milliseconds. Initially the brightness was 200 lumens, increasing after 5 milliseconds to a maximum of 350

(3 marks) Sketch how the brightness varied over the first 50 milliseconds on the axes below.



(d) Explain why p = 150, $q = \frac{\pi}{10}$ and r = 200. (3 marks)

(3 marks) For what percentage of each cycle is the brightness of the globe less than 90 lumens?

8 **Question 13** (12 marks)

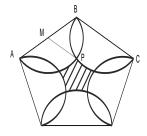
A thin piece of glass has been cut into the shape of an obtuse-angled triangle with an area of 135.5 cm² and two sides of 21.8 cm and 25.4 cm.

Calculate the length of the third side, correct to 3 significant figures.

(4 marks)

The diagram shows five congruent semicircles standing on the inside of a regular pentagon with sides of length 20 cm.

M is the midpoint of the side AB and P is the point of intersection of two semi-circles.



Show that the size of angle $\angle BMP = 72^{\circ}$.

(2 marks)

Question 17 (7 marks)

When a capacitor discharges through a resistor, the voltage, V in volts, across the capacitor decays according to the rule $V = 20(0.38)^t$, where t is the time, in seconds, after the discharge began.

What was the initial voltage across the capacitor?

CALCULATOR-ASSUMED

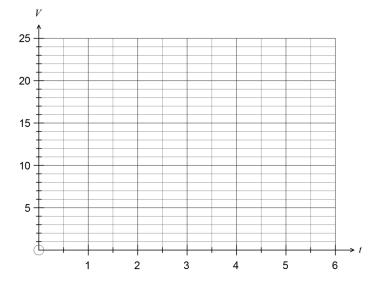
(1 mark)

What was the voltage across the capacitor after four seconds?

Draw the graph of the voltage against time for $0 \le t \le 5$.

(3 marks)

(1 mark)



How long, to the nearest millisecond, does it take for the voltage across the capacitor to halve? (2 marks)

		(2 тагкs)	y with event A. الدe of P(C ∪ B) ؟	(b) A third event, C, is complementar What is the maximum possible va
		(2 тагкs)		((ā∪Ā) ā)Я (iii)
		(1 mark)		(B∪A)¶ (ii)
		(2 тағк <i>s</i>)	. $3.0 = (\overline{a})$ 9 bns $2.0 = (8 \cap A)$ 9 isati to	Two independent events A and B are su (a) Calculate (A) P(A)
METHODS UNITS 1 AND 2	(ii) Determine the area of the central shaded region.		12 CALCULATOR-A	METHODS UNITS 1 AND 2

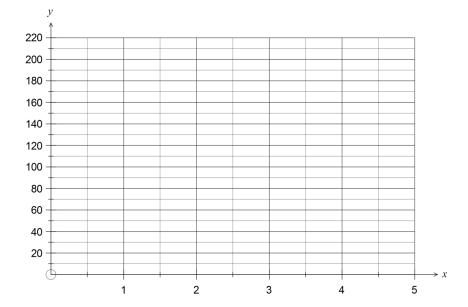
See next page

Question 14 (7 marks)

Consider the function $f(x) = 136 - 96x - 4x^2 + 24x^3 - 4x^4$.

Using calculus techniques, determine the coordinates of all stationary points of the graph of y = f(x) in the interval $0 \le x \le 5$. (4 marks)

Sketch the graph of y = f(x) over the interval $0 \le x \le 5$. (3 marks)



11 **Question 15** (8 marks)

A store accepts credit card payments from customers using American Express, Mastercard or VISA cards. Records indicate that 65% of customers use a credit card, and of these customers, 20% use American Express, 35% Mastercard and the rest VISA. Further analysis shows that the male to female ratio for users of each type of card is 5:3 for American Express, 2:3 for Mastercard and 3:2 for VISA.

Calculate the probability that a randomly selected customer from the records will be a female who uses an American Express credit card. (2 marks)

Given that a randomly selected customer used a credit card, what is the probability that they are male? (3 marks)

What is the probability that a randomly selected female customer who used a credit card used a VISA card? (3 marks)