

Name: \_\_\_\_\_

Teacher: \_\_\_\_\_

TIME ALLOWED FOR THIS SECTION

Reading time before commencing work:  
Working time for section:  
10 minutes  
100 minutes

MATERIAL REQUIRED / RECOMMENDED FOR THIS SECTION

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler.

Special items: drawing instruments, templates, notes on up to two unfolded sheet of A4 paper, and up to three calculators approved for use in the WACE examinations.

IMPORTANT NOTE TO CANDIDATES

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non–personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

To be provided by the supervisor

Question/answer booklet for Section Two.  
Formula sheet retained from Section One.

**Structure of this examination**

	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	8	8	50	52	35
<b>Section Two Calculator—assumed</b>	<b>12</b>	<b>12</b>	<b>100</b>	<b>98</b>	<b>65</b>
Total marks				150	100

**Instructions to candidates**

1. The rules for the conduct of this examination are detailed in the Information Handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in the Question/Answer booklet.
3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Spare pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer booklet.

Extra page for working if necessary

9. (6 marks)

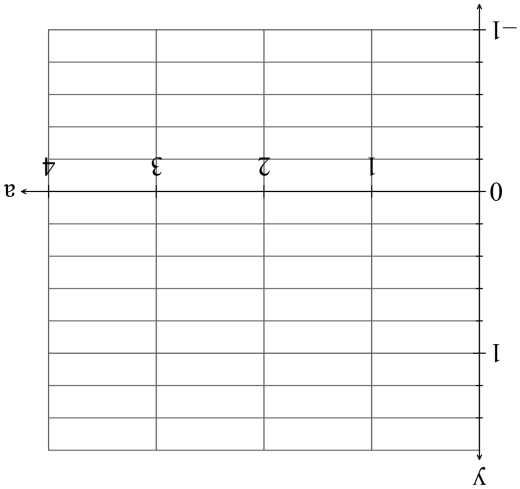
(a) Use your calculator to complete the table below

(2)

$a$	$\frac{1}{2}$	1	2	3	4
$y = \lim_{h \rightarrow 0} \frac{a^h - 1}{h}$					

(b) Plot the data in the table above on the set of axes below.

(2)



(c) Write down the equation of the function graphed in (b).

(1)

(d) Determine  $a$  such that  $\lim_{h \rightarrow 0} \frac{a^h - 1}{h} = 1$ .

(1)

10. (7 marks)

The number of people who have the flu in the first three weeks of an epidemic can be modelled by the equation  $P = 120e^{kt}$  where  $t$  is measured in days and  $k > 0$ . Initially, the number of people who had the flu was 120.

After 10 days, 250 people had the flu.

(a) Determine the value of  $k$ . (1)

(b) After how many days would you expect 300 people to be infected? (1)

(c) Determine how fast the flu is spreading after one week. (2)

(b) In WA the probability of those in favour of raising the age to 18 when a person can obtain a driving license is unknown.

What sample size should be used to estimate the probability of those in favour of raising the age to 18 to get a driver's license with an error margin of 10% and a confidence level of 95%? (5)

(c) If the confidence level in (b) is 90% instead of 95% would the sample size be smaller or larger? Explain. (2)

END OF SECTION TWO

(d) How fast is the rate of infection increasing after one week? (2)

(e) Briefly explain why the model cannot be used indefinitely. (1)



20. (12 marks)  
(a) One hundred and forty out of a sample of 200 Shenton Park ratepayers do not want Shenton College moved to the Perth CBD.  
Within what range of percentages of ratepayers can we be 95% confident that the ratepayers of Shenton Park do not want Shenton College moved to Perth CBD? (5)  
HINT: Use  $p = 0.5$  to ensure valid confidence limits.

11. (5 marks)

Given  $h = 4 + 2 \sin\left(\frac{t}{2}\right)$ .

find

(a)  $h$  at  $t = \frac{\pi}{2}$  minutes. (1)

(b)  $t$  such that  $h \geq 5$  for  $0 \leq t \leq 2\pi$ . (1)

(c)  $\frac{dh}{dt}$  at  $t = \pi$ . (1)

(d)  $\frac{d^2h}{dt^2}$  at  $t = \frac{\pi}{2}$ . (2)

(e) Find a simplified expression for the cumulative probability density function. (3)

(f) Using the simplified expression for the cumulative probability density function determine  $P(x \geq 2)$ . (2)

19. (14 marks)

The continuous random variable  $X$  has the probability density function

$$f(x) = \begin{cases} 3-x & \text{for } 1.5 \leq x \leq 2.5 \\ 0 & \text{otherwise} \end{cases}$$

- (a) Prove that  $f$  represents a probability density function. Show all steps. (3)

- (b) Determine  $P(x > 2)$ . (2)

- (c) Determine  $P(x > 2 | x > 1.8)$ . (2)

- (d) Write down the expressions that if evaluated gives the expected value. (2)

12. (4 marks)

A pizza is 30 cm in diameter. Josh asks for a piece in the shape of a sector that makes an angle of  $30^\circ$  at the centre of the pizza. His piece is 0.5 cm high.



Josh is given a piece of pizza that makes an angle of  $33^\circ$  at the centre of the pizza.

- (a) Write down the formula for the volume of a piece of pizza in the shape on a sector in  $\text{cm}^3$ . (1)

- (b) Use a calculus method to determine the extra volume of pizza Josh is given. (3)

13. (14 marks)

(a) The number of amoeba in a petri dish is given by  $N = 2(3)^t$  where  $t$  is given in hours.

(a) (i) Complete the following table. (2)

$t$	$N$
1	6
2	
3	
4	
5	

(ii) Complete the table below that uses  $\ln(N)$  instead of  $N$ . (2)

$t$	$\ln(N)$
1	
2	
3	
4	
5	

18. (8 marks)

Only 30% of cars have the petrol cap on the driver's side of the car. Eight cars drove into a petrol station to top up their petrol.

(a) What is the probability that three of the cars had the petrol cap on the driver's side of the car? (2)

(b) What is the probability that no more than three of the cars had the petrol cap the driver's side of the car? (2)

(c) What is the probability that none of the cars had the petrol cap on the driver's side of the car? (2)

(d) Given the first three cars had petrol caps on the driver's side of the car, what is the probability that the last five cars had their petrol cap on the other side of the car? (2)



(b) Three hundred 4 child families were surveyed to estimate the number of families

expected to have 0, 1, 2, 3 or 4 girls in the family.

The results are in the table below

Number of girls in the family	Frequency
0	20
1	80
2	110
3	74
4	16

(i) Complete the chart below using the data in the table.

$X$  is the set of numbers that represents the number of girls in a 4 child family.

$x$	0	1	2	3	4
$P(X = x)$					

(2)

(ii) Calculate the theoretical probabilities to complete the table below.

$x$	0	1	2	3	4
$P(X = x)$					

(2)

Determine the theoretical probabilities below.

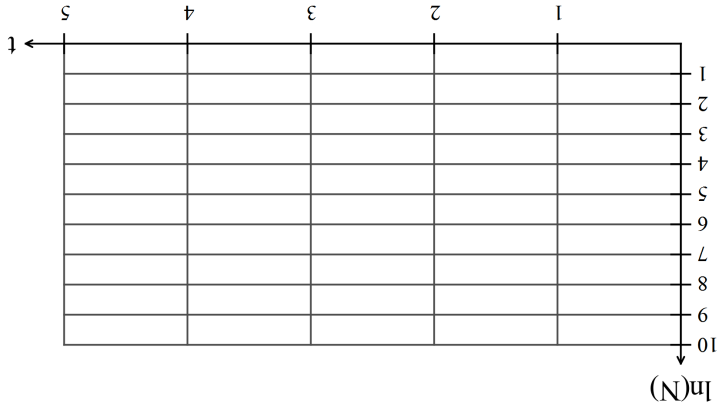
(iii)  $P(X \geq 2)$

(1)

(iv)  $P(X = 4 | x \geq 2)$

(2)

(iii) Plot the data in (b) on the set of axes below.

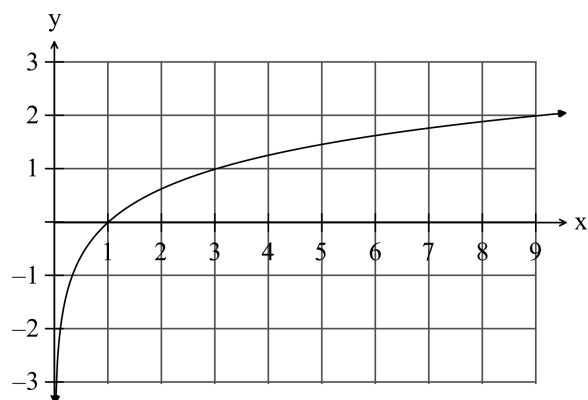


(iv) Explain the advantage of plotting  $\ln(N)$  against  $t$  instead of  $N$  against  $t$ .

(2)

- (b) Given the graph of  $y = \log_3(x)$  sketch  $y = \log_3(x-3)$  on the same set of axes.

(2)



- (c) Solve for  $x$  :

(i)  $\log_3(x+3) = 2$

(2)

(ii)  $\log_x(4) = 2$

(2)

17. (12 marks)

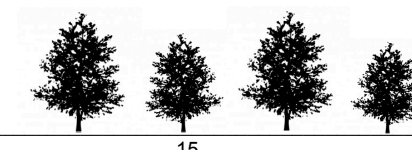
- (a) The heights attained by a variety of a small flowering tree are normally distributed with an average height of 3.5 m and a standard deviation of 0.5 m. Joan planted one of the trees under a second storey window the base of which is 4 m above the ground.

- (i) What are the chances the tree will reach more than 4 m? (1)

- (ii) What are the chances the tree will grow no more than 0.5 m above the base of the window if it has already reached 4 m in height? (2)

Joan planted four of the trees one metre from the house.

- (iii) What is the probability that at least three of them grow to more than 4 m? (2)



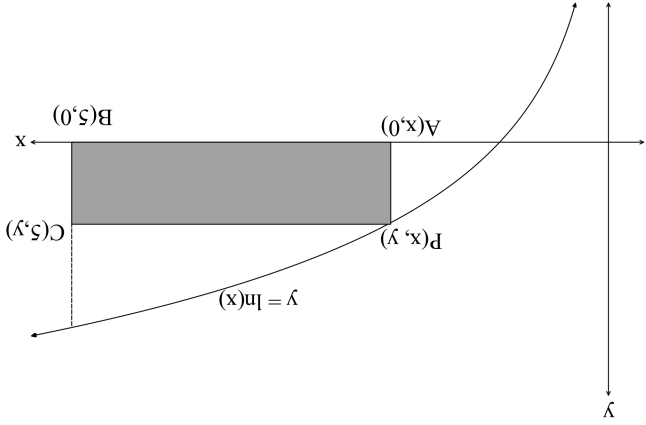
14. (6 marks)

The displacement  $s$  of a particle is given by  $s = 2t^4 - 4t^2$  m, for  $t \geq 0$  where  $t$  is in seconds.

Determine

(a) the velocity when the displacement is zero for  $t > 0$ .

(3)



Consider the rectangle ABCP in the diagram below.

16. (5 marks)

The rectangle is bounded by the  $x$  axis  $x = 5$  and one vertex  $P(x, y)$  lies on the function  $y = \ln(x)$ .

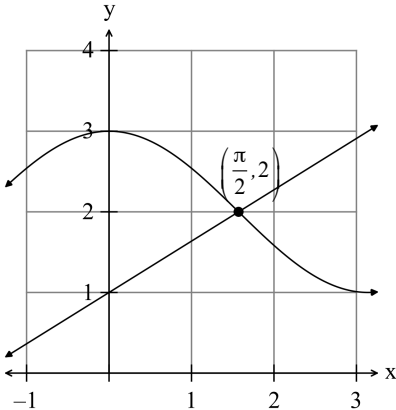
Find the coordinates of point  $P$  such that the area of the rectangle is maximised. (5)

(b) The velocity of a particle is given by  $\frac{ds}{dt} = -4 + 2t$  for  $t \geq 0$ .  
If the initial displacement is 1 m. find the displacement and acceleration when  $t = 3$  s.

(3)

15. (5 marks)

- (a) Determine the area bounded by the functions  $y = 2 + \cos(x)$  and  $y = \frac{2x}{\pi} + 1$  and the  $y$  axis in the diagram below.



(2)

- (b) Determine the shaded area in the diagram below for  $0.5 \leq x \leq 2$  .  
The integral of some bounded regions for each function are given. (3)

