

Semester Two Examination, 2021 Question/Answer booklet

MATHEMATICS SPECIALIST UNITS 1&2

Sec Calc

Section Two:		30	LUTIO	<u> </u>
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	In words			
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Time allowed for this seeding time before commen Working time: minutes		ten minutes one hundred	Number of additio answer booklets u (if applicable):	

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet (retained from Section One)

To be provided by the candidate

pens (blue/black preferred), pencils (including coloured), sharpener, Standard items:

correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

> and up to three calculators, which can include scientific, graphic and Computer Algebra System (CAS) calculators, are permitted in this ATAR

course examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	50	35
Section Two: Calculator-assumed	13	13	100	92	65
				Total	100

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- 3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed

65% (92 Marks)

This section has **thirteen** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (6 marks)

(a) Determine the vector projection of $\begin{pmatrix} 5 \\ -5 \end{pmatrix}$ on $\begin{pmatrix} -1 \\ 2 \end{pmatrix}$.

(2 marks)

Solution
$$\frac{\binom{5}{-5} \cdot \binom{-1}{2}}{\binom{-1}{2} \cdot \binom{-1}{2}} \binom{-1}{2} = \frac{-15}{5} \binom{-1}{2} \cdot 3 \binom{-1}{2}$$

$$\vdots \binom{3}{-6}$$

Specific behaviours

 \checkmark indicates appropriate method

ü correct vector

- (b) Determine the value(s) of t so that the vectors $\begin{pmatrix} t \\ -3 \end{pmatrix}$ and $\begin{pmatrix} 3t+8 \\ 1 \end{pmatrix}$ are
 - (i) parallel. (2 marks)

Solution
$$\frac{t}{-3} = \frac{3t+8}{1} \Rightarrow t = \frac{-12}{5} = -2.4$$

Specific behaviours

√ indicates equation using of ratio of coefficients
ü correct value

(ii) perpendicular.

(2 marks)

$$\frac{t}{\binom{t}{-3} \cdot \binom{3t+8}{1}} = 03t^2 + 8t - 3 = 0t = -3, t = \frac{1}{3}$$

Specific behaviours

✓ indicates equation using scalar product

ü correct values

Question 10 (7 marks)

(a) Five-digit odd numbers are to be made using the digits 1,2,3,4,5,6 and 7. Determine how many such numbers exist if the number must exceed 50 000 and no digit may be used more than once in a number. (3 marks)

Solution

End with 1 or 3: $2 \times 3 \times 5 \times 4 \times 3 = 360$

End with 5 or 7: $2 \times 2 \times 5 \times 4 \times 3 = 240$

Total possible numbers: 360+240=600

Specific behaviours

✓ splits into mutually exclusive cases

ü correctly counts at least one case

ü calculates total

- (b) The library in a small guesthouse has 32 different books, of which 21 are non-fiction and the remainder fiction. Determine the number of different ways that a guest can select four books if they want
 - (i) the same number of fiction and non-fiction books.

(2 marks)

Solution

$$n = {21 \choose 2} {11 \choose 2} \stackrel{?}{6} 210 \times 55 \stackrel{?}{6} 11550 \text{ ways}$$

Specific behaviours

√ indicates correct method

ü correct number of ways

(ii) more fiction than non-fiction books.

(2 marks)

Solution

$$n = {21 \choose 1} {11 \choose 3} + {21 \choose 0} {11 \choose 4}$$

$$21 \times 165 + 1 \times 330 & 3465 + 330$$

₹3795 ways

- ✓ indicates correct method
- ü correct number of ways

Question 11 (7 marks)

Two transformation matrices are $M = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ and $N = \begin{bmatrix} 2 & 2 \\ -4 & 4 \end{bmatrix}$.

Triangle PQR has an area of 39 cm², with vertices at P(5,3), Q(-2,8) and R(-5,-1).

(a) Determine the coordinates of PQR after the triangle has been transformed by matrix M.

(3 marks)

Solution $\begin{bmatrix}
0 & 1 \\
1 & 0
\end{bmatrix}
\begin{bmatrix}
5 & -2 & -5 \\
3 & 8 & -1
\end{bmatrix}
=
\begin{bmatrix}
3 & 8 & -1 \\
5 & -2 & -5
\end{bmatrix}$

P'(3,5), Q'(8,-2), R'(-1,-5).

Specific behaviours

- \checkmark indicates pre-multiplication by M
- ü correct matrix product
- ü correctly lists set of coordinates

(b) Use the geometric transformation to explain why the determinant of M is 1. (1 mark)

Solution

 ${\it M}$ represents a reflection, the area of triangle does not change and so determinant is 1.

Specific behaviours

✓ reflection will not change area

(c) Use the geometric transformation to explain why $M^2 = I$, where I is the 2×2 identity matrix. (1 mark)

Solution

 M^2 represents two reflections in the same line, and so the triangle will be back where it started, with the same coordinates.

Specific behaviours

√ two reflections in same line

(d) Determine the area of PQR after the triangle has been transformed by matrix N. (2 marks)

$$det(N) = 8 + 8 = 16$$

New area = $16 \times 39 = 624 \text{ cm}^2$

Specific behaviours

✓ calculates determinant

ü calculates new area

Question 12 (8 marks)

(a) Write the converse of the true statement 'if a figure is a square then it has four congruent sides' and use an example or counter-example to briefly discuss the truth of the converse.

(2 marks)

Solution

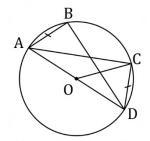
Converse: If a figure has four congruent sides, then it is a square. The converse is false, as the figure could be a rhombus.

Specific behaviours

√ correct converse

ü states false with counter-example

(b) Points A, B, C and D lie as shown on a circle with centre O so that AD is a diameter, AB=CD and $\angle COD=42^{\circ}$.



Determine the size of

(i) $\angle CAD$.

Solution
$\angle CAD = 42^{\circ} \div 2 = 21^{\circ}$

$$\angle BAD = \angle CDA = 90^{\circ} - 21^{\circ} = 69^{\circ}$$

$$\angle CAB = 69^{\circ} - 21^{\circ} = 48^{\circ}$$

(ii) $\angle BAD$.

 \checkmark \angle CAD

 $\checkmark \angle BAD$

 \checkmark \angle CAB

(1 mark)

(1 mark)

(iii) ∠ CAB.

(1 mark)

(c) Two chords of a circle, LM and PQ, intersect at N so that LM = 41 cm, NM = 20 cm and PQ = 44 cm. Determine all possible lengths of QN. (3 marks)

Solution

Using intersecting chord theorem, $\ln \times NM = PN \times NQ$.

$$\ln = LM - NM = 41 - 20 = 21$$

Let
$$NQ = x$$
, so that $PN = 44 - x$

$$21 \times 20 = x(44 - x)x = 14,30$$

Hence
$$QN = 14$$
 cm or $QN = 30$ cm.

- √ identifies required lengths
- ü forms quadratic equation
- ü states both values

Question 13 (8 marks)

In triangle OAB, P is the midpoint of OA and M is the midpoint of PB. Let $\overrightarrow{OA} = a$ and $\overrightarrow{OB} = b$.

(a) Show that
$$\overline{OM} = \frac{1}{4}a + \frac{1}{2}b$$
. (2 marks)

Solution
$$\overrightarrow{OM} = \overrightarrow{OP} + \overrightarrow{PM}, \overrightarrow{OP} = \frac{1}{2} \overrightarrow{OA}, \overrightarrow{PM} = \frac{1}{2} \overrightarrow{PB} = \frac{1}{2} (\overrightarrow{OB} - \overrightarrow{OP})$$

$$\frac{1}{2} a + \frac{1}{2} \left(b - \frac{1}{2} a \right) \frac{1}{4} a + \frac{1}{2} b$$

Specific behaviours

√ indicates logical steps

ü uses correct vector notation throughout

The position vector of A is $\begin{pmatrix} 6 \\ 4 \end{pmatrix}$, position vector of B is $\begin{pmatrix} 7 \\ -4 \end{pmatrix}$ and O is the origin.

Determine a unit vector \hat{u} in the same direction as \overrightarrow{OM} . (b)

(2 marks)

$$\overrightarrow{OM} = \frac{1}{4} \begin{pmatrix} 6 \\ 4 \end{pmatrix} + \frac{1}{2} \begin{pmatrix} 7 \\ -4 \end{pmatrix} = \begin{pmatrix} 5 \\ -1 \end{pmatrix} \hat{u} = \frac{\sqrt{26}}{26} \begin{pmatrix} 5 \\ -1 \end{pmatrix}$$

*NB might use CAS for last step

Specific behaviours

- ✓ calculates OM
- ü states unit vector

(c) Show that OA is perpendicular to PM.

(2 marks)

Solution
$$\overrightarrow{OA} = \begin{pmatrix} 6 \\ 4 \end{pmatrix}, \overrightarrow{PM} = \frac{1}{2} \begin{pmatrix} 7 \\ -4 \end{pmatrix} - \frac{1}{4} \begin{pmatrix} 6 \\ 4 \end{pmatrix} = \begin{pmatrix} 2 \\ -3 \end{pmatrix}$$

$$\overrightarrow{OA} \cdot \overrightarrow{PM} = \begin{pmatrix} 6 \\ 4 \end{pmatrix} \cdot \begin{pmatrix} 2 \\ -3 \end{pmatrix} = 12 - 12 = 0$$

Hence vectors are perpendicular.

- \checkmark calculates \overline{PM}
- ü shows scalar product is zero

(d) Determine the size of $\angle AOB$.

(2 marks)

Solution

$$\angle AOB = \cos^{-1} \left(\frac{a \cdot b}{|a||b|} \right) \dot{c} \cos^{-1} \left(\frac{\sqrt{5}}{5} \right)$$
$$\dot{c} 63.4^{\circ}$$

*NB might use CAS

Specific behaviours

✓ indicates suitable method

ü correct angle

Question 14 (7 marks)

(a) In trapezium ABCD, AC and BD are diagonals, and AB is parallel to CD. Use a vector method to prove that $\overrightarrow{AC} + \overrightarrow{DB} = \overrightarrow{AB} + \overrightarrow{DC}$. (3 marks)

Note that
$$\overrightarrow{AC} = \overrightarrow{AB} + \overrightarrow{BC}$$
 and $\overrightarrow{DB} = \overrightarrow{DC} - \overrightarrow{BC}$.

$$LHS = \overrightarrow{AC} + \overrightarrow{DB} \overrightarrow{\iota} \overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{DC} - \overrightarrow{BC} \overrightarrow{\iota} \overrightarrow{AB} + \overrightarrow{DC}$$

$$\overrightarrow{\iota} RHS$$

Specific behaviours

- \checkmark expression for \overrightarrow{AC}
- \ddot{u} expression for \overrightarrow{DB}
- ü adds expressions and simplifies

(b) In rectangle \overrightarrow{OPQR} , let $\overrightarrow{OP} = p$ and $\overrightarrow{l} = r$. Use a vector method to prove that if the diagonals OQ and PR are perpendicular, then OPQR is a square. (4 marks)

Solution

The diagonals are the vectors $\overrightarrow{OQ} = p + r$ and $\overrightarrow{PR} = r - p$.

If diagonals are perpendicular, then $\overrightarrow{OQ} \cdot \overrightarrow{PR} = 0$ and so:

$$(p+r)\cdot(r-p)=0$$
 $p\cdot r-p\cdot p+r\cdot r-r\cdot p=0$ $|r|^2-|p|^2=0$ $|r|^2=|p|^2\Rightarrow |r|=i$ $p\vee i$

Hence *OPQR* must be a square since it is a rectangle with equal length sides.

- √ determines vectors for diagonals
- √ uses scalar product
- ✓ expands and simplifies scalar product
- ✓ explains that sides are equal length

Question 15 (6 marks)

Consider the following statement:

For two integers a, b if $3a^2 - 2b^2$ is a multiple of 4 then at least one of a, b is even.

(a) Write the contrapositive of the statement.

(1 mark)

Solution

For two integers a, b if both are odd then $3a^2 - 2b^2$ is not a multiple of 4.

Specific behaviours

✓ correct contrapositive

(b) Prove that the statement is true.

(5 marks)

Solution

Proof of contrapositive:

If a, b both odd, then a=2m+1 and b=2n+1, where n, m both integers.

Hence

$$3a^2-2b^2=3(2m+1)^2-2(2n+1)^2$$
; $12m^2+12m-8n^2-8n+1$
; $4(3m^2+3m-2n^2-2n)+1$

Hence $3a^2-2b^2$ will never be a multiple of 4 as it is always one more than a multiple of 4.

Since the contrapositive statement has been proved to be true then it follows that the original statement must also be true.

Specific behaviours

 \checkmark attempts to prove contrapositive and states truth of contrapositive implies truth of original statement

 \ddot{u} uses form 2k+1 form for odd numbers a,b

 \ddot{u} substitutes for a, b and expands

ü factors out 4

ü explains why contrapositive true

Question 16 (8 marks)

The height of the tide, h cm, of the sea above the mean level at time t hours after midnight one day is given by

$$h(t) = 28 \cos\left(\frac{\pi t}{6}\right) + 45 \sin\left(\frac{\pi t}{6}\right)$$
.

(a) Express h in the form $a \cos(bt-\theta)$, where a,b>0 and $0 \le \theta \le 2\pi$.

Solution $a = \sqrt{28^2 + 45^2} = 53$ $h = 53 \cos\left(\frac{\pi t}{6} - \theta\right)$ $653 \left(\cos\left(\frac{\pi t}{6}\right)\cos\theta + \sin\left(\frac{\pi t}{6}\right)\sin\theta\right)$ $\cos\theta = \frac{28}{53}, \sin\theta = \frac{45}{53} \Rightarrow \theta = 1.0142$ $h = 53 \cos\left(\frac{\pi t}{6} - 1.0142\right)$ Specific behaviours $\checkmark \text{ value of } a$

(b) Determine, to the nearest minute, the time of the first high tide.

(2 marks)

(3 marks)

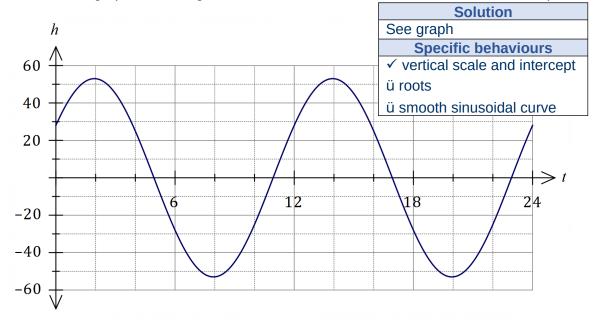
Require $\frac{\pi t}{6} - 1.0142 = 0 \Rightarrow t = 1.937 \,\text{h}$. Hence at 0156 or 1:56 am.

Specific behaviours

✓ time in hours

Littime of day, to nearest minute

(c) Sketch the graph of the height of the tide on the axes below. (3 marks)



Question 17 (7 marks)

Three forces F_1 , F_2 and F_3 act on a small body, where F_1 =4i-10j N, F_2 =-8i+16j N and F_3 =9i-15j N.

(a) Determine the magnitude of the resultant force and the angle between the resultant force and the vector *i*. (3 marks)

Solution
$$R = F_1 + F_2 + F_3 \stackrel{?}{\circ} \left(\begin{array}{c} 4 \\ -10 \end{array} \right) + \left(\begin{array}{c} -8 \\ 16 \end{array} \right) + \left(\begin{array}{c} 9 \\ -15 \end{array} \right) = \left(\begin{array}{c} 5 \\ -9 \end{array} \right)$$

$$|R| = \sqrt{5^2 + 9^2} = \sqrt{106} \approx 10.3 \,\text{N}$$

$$\angle = \tan^{-1} \left(\frac{-9}{5} \right) \approx -60.9$$
°

Hence resultant has a magnitude of $10.3~\mathrm{N}$ and makes an angle of $60.9~\mathrm{°}$ with i.

Specific behaviours

- ✓ correct sum in component form
- ü calculates magnitude
- ü calculates angle
- (b) Two of the forces, F_2 and F_3 , can be multiplied by scalars λ and μ respectively so that the three forces are in equilibrium. Determine the value of λ and the value of μ . (4 marks)

Solution
$$F_1 + \lambda F_2 + \mu F_3 = 0 \begin{pmatrix} 4 \\ -10 \end{pmatrix} + \lambda \begin{pmatrix} -8 \\ 16 \end{pmatrix} + \mu \begin{pmatrix} 9 \\ -15 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

Resolving in i and j directions:

$$4-8\lambda+9\mu=0-10+16\lambda-15\mu=0$$

Solving simultaneously gives

$$\lambda = \frac{5}{4} = 1.25, \mu = \frac{2}{3}$$

- ✓ writes vector equation equal to 0
- ü forms two equations
- \ddot{u} value of λ
- \ddot{u} value of μ

Question 18 (7 marks)

90 people are asked to choose two different letters from those in the word GAMBLER and (a) write them down in order. Use the pigeonhole principle to prove that at least three people will write the same pair of letters in the same order. (3 marks)

Solution

There are $\frac{1}{6}$ 7 $P_2 = 42$ different ordered pairs of letters, each of which is a pigeonhole.

Using the pigeonhole principle, if 90 pigeons (the number of pairs of letters written by people) are placed into 42 pigeonholes, then at least one pigeonhole will contain $\int 90 \div 42 = 3$ or more pigeons.

Hence at least 3 people will write the same pair of letters in the same order.

Specific behaviours

- ✓ obtains number of permutations
- ü indicates pigeons and pigeonholes
- ü uses pigeonhole principle to complete proof
- Three character codes, such as TCU, are made using three different letters chosen from (b) the word DISCOUNT. Determine the proportion of all possible codes that start with a D or end with a T. (4 marks)

Start with D: $n(D)=1 \times P_2=42$ codes.

End with T: $n(T)=1 \times P_2=42$ codes.

Start with D and end with T: $n(D \cap T) = 1 \times 1 \times P_1 = 6$ codes.

Start with D or end with T: $n(D \cup T) = 42 + 42 - 6 = 78$ codes.

There are $\stackrel{\cdot}{\iota} 8 P_3 = 336$ different codes.

Hence required proportion is $\frac{78}{336} = \frac{13}{56} \approx 0.232$.

Specific behaviours

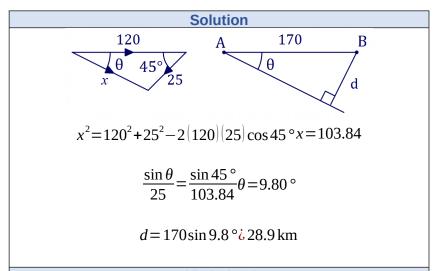
 $\ddot{\mathbf{u}} n(\mathbf{D})$ and n(T)

Question 19 (7 marks)

Airport B lies 170 km due east of airport A, and in the region of the airports a wind of 25 km/h is blowing from the northeast.

A small plane, with a cruising speed of 120 km/h, leaves airport A. The pilot, not aware of the wind and intending to fly to airport B, steered the plane on a bearing of 090° .

Assuming that the pilot does not realise their mistake, determine how close the plane will come to airport B if it continues to fly for several hours on the same bearing.



- ✓ appropriate sketch/explanation for x and θ
- \ddot{u} equation for x
- ü solves for x
- $\ddot{\mathrm{u}}$ equation for θ
- $\ddot{\mathrm{u}}$ solves for θ
- ✓ appropriate sketch/explanation for closest distance
- ü calculates closest distance

Question 20 (7 marks)

Triangle *ABC* has vertices A(2,2), B(-4,6) and C(4,8).

ABC is rotated clockwise 60° about the origin to form triangle A'B'C'.

(a) Determine the coordinates of C'.

(2 marks)

Solution $\frac{1}{2} \begin{bmatrix} 1 & \sqrt{3} \\ -\sqrt{3} & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 8 \end{bmatrix} = \begin{bmatrix} 2+4\sqrt{3} \\ 4-2\sqrt{3} \end{bmatrix} \approx \begin{bmatrix} 8.928 \\ 0.536 \end{bmatrix}$ $C' \begin{bmatrix} 2+4\sqrt{3}, 4-2\sqrt{3} \end{bmatrix}$

$$C(2+4\sqrt{3},4-2\sqrt{3})$$

Specific behaviours

√ rotation matrix

ü correct coordinates

ABC is reflected in the line y = 2x to form triangle A''B''C''.

(b) Determine the coordinates of B'.

(2 marks)

Solution
$$\frac{1}{5} \begin{bmatrix} -3 & 4 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} -4 \\ 6 \end{bmatrix} = \begin{bmatrix} \frac{36}{5} \\ \frac{2}{5} \end{bmatrix} = \begin{bmatrix} 7.2 \\ 0.4 \end{bmatrix}$$

$$B''(7.2,0.4)$$
Specific behaviours

(c) Determine matrix T that will realisation B'C' to A''B''C''.

(3 marks)

Solution

Matrix *P* for $A'B'C' \rightarrow ABC$ is inverse of that used in (a).

Matrix Q for $ABC \rightarrow A''B''C''$ is same as used in (b).

Hence

$$T = Q P^{-1} \stackrel{?}{\circ} \frac{1}{5} \begin{bmatrix} -3 & 4 \\ 4 & 3 \end{bmatrix} \times \frac{1}{2} \begin{bmatrix} 1 & \sqrt{3} \\ -\sqrt{3} & 1 \end{bmatrix}^{-1}$$

$$\stackrel{?}{\circ} \frac{1}{10} \begin{bmatrix} 4\sqrt{3} - 3 & 3\sqrt{3} + 4 \\ 3\sqrt{3} + 4 & -4\sqrt{3} + 3 \end{bmatrix} \approx \begin{bmatrix} 0.393 & 0.920 \\ 0.920 & -0.393 \end{bmatrix}$$

Specific behaviours

✓ matrix for $A'B'C' \rightarrow ABC$

ü indicates correct order of multiplication

 $\ddot{\text{u}}$ correct matrix T

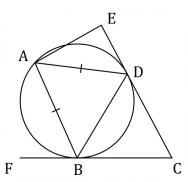
Question 21 (7 marks)

The diagram, not drawn to scale, shows vertices A, B and D of an isosceles triangle lying on a circle so that AD = AB.

Lines CE and CF are tangential to the circle at D and B respectively.

ABCE is a cyclic quadrilateral.

Let $\angle FCE = x$.



(a) Determine, with reasons, the size of $\angle AEC$ in terms of x.

(5 marks)

Solution

$$\angle DBC = \frac{1}{2}(180^{\circ} - x) = 90^{\circ} - \frac{1}{2}x \text{ (tangents from } C \Rightarrow CD = CB \&$$

$$\angle BAD = \angle DBC = 90^{\circ} - \frac{1}{2}x \text{ (alternate segment)}$$

$$\angle ABD = \frac{1}{2}\left(180^{\circ} - \left(90^{\circ} - \frac{1}{2}x\right)\right) = 45^{\circ} + \frac{1}{4}x \text{ (isosceles triangle)}$$

$$\angle ABC = \angle ABD + \angle DBC \text{ (adjacent angles)}$$

$$\& 45^{\circ} + \frac{1}{4}x + 90^{\circ} - \frac{1}{2}x = 135^{\circ} - \frac{1}{4}x$$

$$\angle AEC = 180^{\circ} - \angle ABC \text{ (cyclic quadrilateral)}$$

$$\& 180^{\circ} - \left(135^{\circ} - \frac{1}{4}x\right) = 45^{\circ} + \frac{1}{4}x$$

Specific behaviours

- \checkmark expression for $\angle DBC$ with reason
- ✓ expression for $\angle BAD$ with reason
- ✓ expression for \angle *ABD* with reason
- √ expression for ADC with reason

(b) Hence determine the range of values for the size of \angle *AEC* in degrees.

(2 marks)

Solution

For figure to exist, $0^{\circ} < x < 180^{\circ}$.

Hence
$$\angle$$
 AEC>45°+ $\frac{1}{4}$ (0°) and \angle AEC<45°+ $\frac{1}{4}$ (180°)

Range is
$$45^{\circ} < \angle AEC < 90^{\circ}$$
.

Specific behaviours

 \checkmark indicates correct domain for x

ü correct range, i **Endoorguestiehts**es

Supplementary page

Question number: _____

Supplementary page

Question number: _____