

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to candidates

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

To be provided by the candidate

Materials required/recommended for this section

Working time for this section: one hundred minutes
Reading time before commencing work: ten minutes
Formula Sheet (retained from Section One)

This Question/Answer Booklet

To be provided by the supervisor

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Your name _____
in words _____
Student Number: _____ in figures _____

SOLUTIONS

MATHEMATICS 3A
Section Two:
Calculator-assumed

Question/Answer Booklet

Semester One Examination, 2015

Rossmanyne Senior High School

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	50	33½%
Section Two: Calculator-assumed	13	13	100	100	66½%
		Total		150	100

Additional working space

Question number: _____

Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2015*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

(2 marks)

- (iv) an introduced species, given that they are not a dove?

$$\begin{array}{r} 137 - 28 = 109 \\ \hline 64 - 15 = 49 \end{array}$$

(1 mark)

- (iii) a native species or a parrot?

$$\begin{array}{r} 137 \\ 73 + 28 = 101 \\ \hline \end{array}$$

(1 mark)

- (ii) an introduced species that is not a seabird?

$$\begin{array}{r} 137 \\ \hline 64 - 9 \end{array}$$

(1 mark)

- (i) a native seabird?

$$\begin{array}{r} 137 \\ \hline 24 \end{array}$$

(2 marks)

- (b) What is the probability that a bird chosen at random from the sightings is

- (a) Complete the missing entries in the table above.

	Dove	Parrot	Seabird	Other	Total	137
Native	13	21	24	15	73	
Introduced	15	28	9	12	64	
Total	28	49	33	27		

The 137 bird sightings by members of a conservation group during a retreat were categorised on the basis of type and species as follows:

Question 8
(7 marks)

Working time: 100 minutes.

Provided.

This section has thirteen (13) questions. Answer all questions. Write your answers in the spaces provided.

Section Two: Calculator-assumed
(100 Marks)

MATHEMATICS 3A

3

CALCULATOR-ASSUMED

MATHEMATICS 3A

18

CALCULATOR-ASSUMED

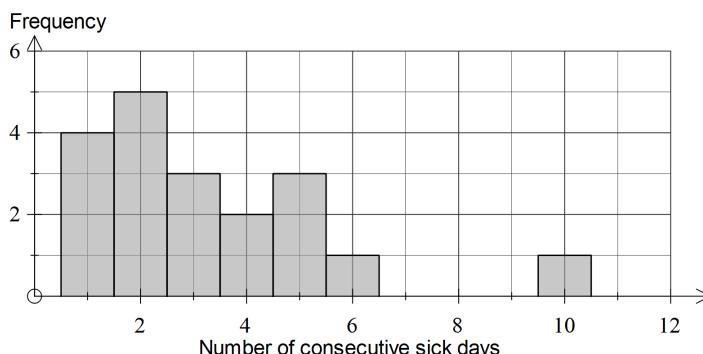
Additional working space

Question number: _____

(8 marks)

Question 9

The histogram below shows the distribution of the number of consecutive sick days (as whole numbers) taken by employees at a workplace.



- (a) Use information from the histogram to complete the table below. (1 mark)

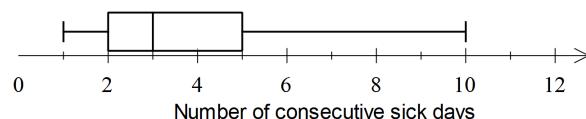
Consecutive sick days	1	2	3	4	4	6	10
Frequency	4	5	3	2	3	1	1

- (b) Determine the mean and standard deviation of the number of sick days. (2 marks)

$$\bar{x} = 3.26$$

$$sd = 2.20$$

- (c) Construct a boxplot for the data shown in the histogram on the scale below. (2 marks)



- (d) Use a calculation to determine whether or not the dataset contains an outlier. (2 marks)

$$UQ + 1.5IQR = 5 + 1.5(3) = 9.5$$

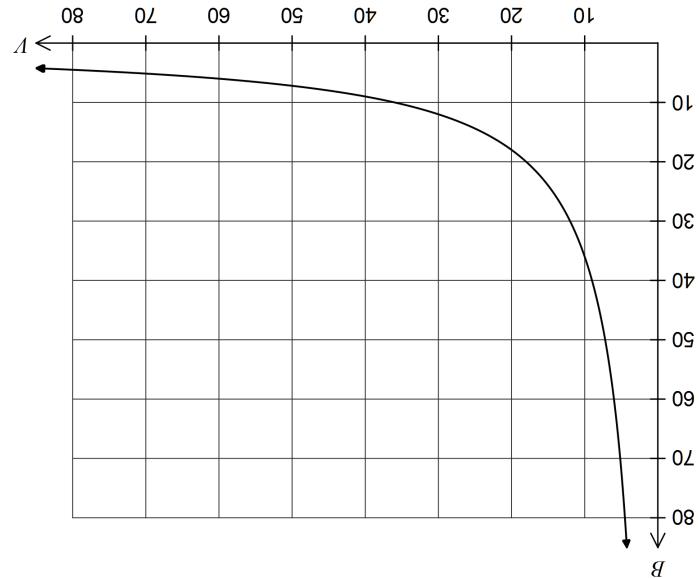
Hence the score of 10 is an outlier as it is more than 1.5 IQR's above the upper quartile.

- (e) Explain one advantage of displaying data as a histogram rather than as a boxplot. (1 mark)

Possible to see the individual frequencies of each class, rather than just summary points in the boxplot.

Additional working space

Question number: _____



- (iii) Sketch the relationship between B and V , adding suitable scales to the axes below.

(1 mark)

- (ii) Describe how B varies as V changes.

(2 marks)

inversely – as one variable increases,
the other decreases.

- (i) Calculate V when $B = 24$.

(2 marks)

$$V = 15$$

- (b) The variable B is related to the variable V by the equation $B = \frac{V}{360}$.

- (a) The variable C is directly proportional to the variable V . Describe the effect on C if V is doubled.

C is also doubled.

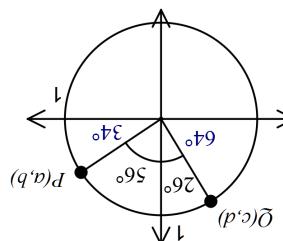
- (a) Two points, $P(a, b)$ and $Q(c, d)$ are shown below on a unit circle. Describe the effect on C if V is doubled.

Determine each of the following in terms of a , b , c , or d .

$$\sin 146^\circ$$

$$-c$$

$$\cos 64^\circ$$



- Question 20
CALCULATOR-ASSUMED
CALCULATOR-ASSUMED

- 6 marks
MATHEMATICS 3A

(7 marks)

- Question 10
CALCULATOR-ASSUMED
CALCULATOR-ASSUMED

(5 marks)

- MATHEMATICS 3A

- 5
MATHEMATICS 3A

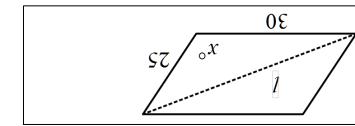
$$350 = \frac{l}{2} (25)(30) \sin(x) \Leftrightarrow x = 68.961^\circ, x = 111.039^\circ$$

$$l^2 = 25^2 + 30^2 - 2(25)(30) \cos(111.039^\circ)$$

$$l = 45.426$$

$$\approx 45.4 \text{ cm (3 sf)}$$

- (iii) Use trigonometry to determine the length of the longest diagonal of the parallelogram, giving your answer to three significant figures.



(8 marks)

Question 11

The weights of tomatoes sold by a market gardener were observed to be normally distributed with a mean of 84 g and a standard deviation of 12 g.

- (a) What proportion of tomatoes will weigh less than 60 g? Give your answer to three significant figures. (2 marks)

$$\begin{aligned} P(w < 60) &= 0.02275 \\ &= 0.0228 \text{ (3 sf)} \end{aligned}$$

- (b) What is the probability that a randomly selected tomato will weigh between 70 and 100 g? (1 mark)

$$P(70 < w < 100) = 0.787$$

- (c) Above what weight will the heaviest 5% of tomatoes fall? (2 marks)

$$\begin{aligned} P(w > x) &= 0.05 \\ x &= 103.7 \text{ g} \end{aligned}$$

- (d) Premium tomatoes, those with a weight between 80 and 90 g, can be sold for more than other tomatoes. Estimate the number of premium tomatoes that would be found in a box of 288 randomly packed tomatoes. (3 marks)

$$\begin{aligned} P(80 < w < 90) &= 0.322 \\ 0.322 \times 288 &= 92.736 \\ 93 \text{ tomatoes} \end{aligned}$$

Question 19

(8 marks)

Water is to be drained from a tank. In the first second after the tap is opened, 10 L drains out. During the next second, 9.5 L drains and so on, so that in each subsequent second 5% less water drains than in the previous second.

- (a) The situation can be represented by a recursive rule of the form $T_{n+1} = rT_n$, $T_1 = k$. State the values of r and k . (2 marks)

$$\begin{aligned} r &= 0.95 \\ k &= 10 \end{aligned}$$

- (b) How many litres of water will drain from the tank during the tenth second? Give your answer to one decimal place. (2 marks)

$$\begin{aligned} T_{10} &= 6.3025 \\ &\approx 6.3 \text{ (1dp)} \end{aligned}$$

- (c) How many litres of water will drain from the tank during the first sixteen seconds? (2 marks)

$$\begin{aligned} S_{16} &= 111.975 \\ &\approx 112 \text{ L} \end{aligned}$$

- (d) If the tank initially held 170 L of water, determine how long it takes to completely empty and state how much water drains in the final second. (2 marks)

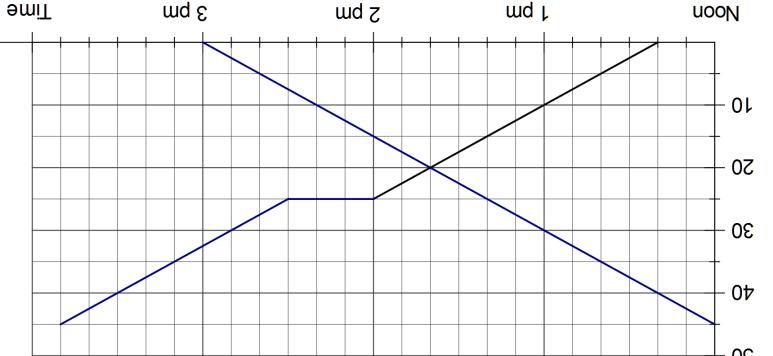
$$\begin{aligned} S_{37} &= 170.022 \Rightarrow \text{After 37 seconds} \\ T_{37} &= 1.578 \\ &\approx 1.6 \text{ L} \end{aligned}$$

Towns P and Q are 45 km apart and connected by a road passing through flat country-side.

At noon, a cyclist A leaves town P and cycles at a constant 15 km per hour towards town Q.

Twenty minutes later, cyclist B leaves town Q and cycles at a constant speed towards town P, stopping at 2 pm for a 30 minute rest before continuing at the same speed. Part of their journey has been shown on the graph below.

Distance from Q (km)



15 km/h

(a) Use the graph above to determine the speed of cyclist B between 12:20 pm and 2 pm.

- (b) Complete the travel graph for cyclist B between 2 pm and 3 pm.
 (c) Draw the travel graph for cyclist A from noon until 3 pm.
 (d) At what time do the cyclists pass each other?

1:40 pm

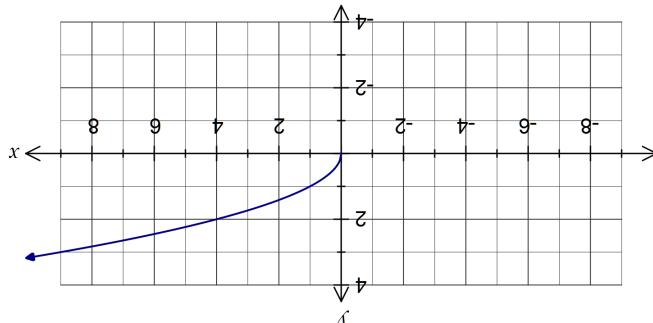
(e) A motorist going to town Q left town P at 1:45 pm and passed cyclist B just as the cyclist began their rest. Determine the average speed that the motorist was travelling at.

vertically by a scale factor of $\frac{1}{2}$. (Order not important)

Reflect the graph of $g(x)$ in the y -axis and dilate

$$\text{Describe how to use the graph in (b) to obtain the graph of } y = \sqrt{-x}.$$

(2 marks)



(b)

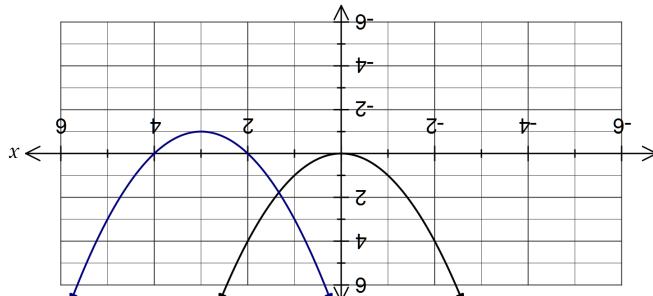
On the axes below, sketch the graph of $y(x) = x^2$.

$$\begin{aligned} b &= -1 \\ d &= 3 \\ f(x) &= (x - 3)^2 - 1 \end{aligned}$$

(2 marks)

(i)

On the axes above, sketch the graph of $f(x) = x^2 - 6x + 8$.



(a)

The graph of $y = x^2$ is shown below.

Question 13

(8 marks)

A young person has just started work and borrowed \$7 500 to purchase a car. They can afford to make monthly repayments of \$660. Interest on the loan is charged monthly.

The spreadsheet below shows the balance and interest of the loan for the first three months.

Month	Balance at start of month (\$)	Interest for month (\$)
1	7 500.00	52.50
2	6 892.50	48.25
3	6 280.75	43.97

- (a) Use information from the table to show that the annual interest rate on the loan is 8.4% per annum. (2 marks)

$$\frac{52.50}{7500} = 0.007$$

$$0.007 \times 12 \times 100 = 8.4\%$$

- (b) Determine the balance at the start of month 4, and the interest for this month. (2 marks)

$$\text{Bal: } 6280.75 + 43.97 - 660.00 = \$5664.72$$

$$\text{Int: } 5664.72 \times 0.007 = \$39.65$$

- (c) Write a recursive rule to determine the balance at the start of each month. (2 marks)

$$T_{n+1} = T_n \times 1.007 - 660, \quad T_1 = 7500$$

- (d) The loan is fully repaid by the end of month 12. Determine, to the nearest dollar,

- (i) the amount of the final repayment. (1 mark)

$$582.68 \approx \$583$$

- (ii) the total amount of interest on the loan. (1 mark)

$$11 \times 660 + 583 - 7500 =$$

Question 17

(7 marks)

Consider a country in which mobile telephone numbers always start with the two digits 06 followed by eight other digits. An example of such a number is 0624 654 321.

- (a) Determine the number of possible mobile telephone numbers if

- (i) there are no other restrictions. (1 mark)

$$10^8 = 100\ 000\ 000 \text{ numbers}$$

- (ii) the first four digits must be 0624 and no digits are repeated in the number. (1 mark)

$$6 \times 5 \times 4 \times 3 \times 2 \times 1 = 720 \text{ numbers}$$

- (iii) only even digits can be used, with no two adjacent digits the same. (1 mark)

$$4^8 = 65\ 536$$

- (b) A caller starts a number with 0624 and then randomly chooses digits for the rest of the number. Determine the probability that the number dialled

- (i) ends in 5. (1 mark)

$$\frac{1}{10}$$

- (ii) contains a 6. (1 mark)

$$\boxed{1}$$

- (iii) does not contain an 8, given that it only contains even digits. (2 marks)

$$\begin{aligned} \frac{4^6}{5^6} &= \frac{4096}{15625} \\ &\approx 0.262 \end{aligned}$$

(a) A student achieved a final semester mark of 70% in his course. This mark was calculated from his weighted marks in the three areas of the course as shown in the table below.

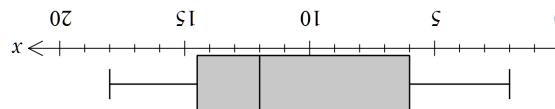
Mean Score (%)	Lab skills	Theory	Practical	Weighting (%)
69	25	75	40	35

$$\frac{69 \times 25 + 75 \times 40 + 35x}{100} = 70$$

$x = 65\%$

Determine the missing mean score in the table for his practical work.

(a) Evaluate a , b , c and d . (3 marks)



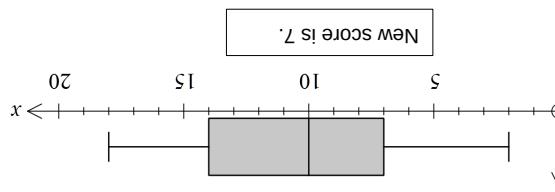
The median boxplot represents the set of scores 2, 4, 8, b, 13, c, 15, d. The scores are all integers and are listed in ascending order.

Question 14 (8 marks)

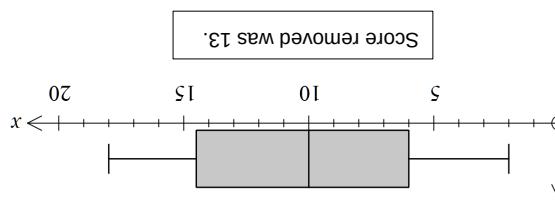
(b) Part of the practical assessment carried out by the student was to estimate the size of a population of wild rabbits in a nature reserve. Together with some fellow students, 35 rabbits were captured, tagged and released in the reserve. A few days later and at the same place, 42 rabbits were caught and it was noted that just three of these were tagged.

When a tenth integer is added to the original nine scores, the boxplot changes as shown below. Determine the value of the new score. (2 marks)

(i) Show how the student could use these figures to estimate the size of a population of wild rabbits in a nature reserve. (2 marks)



When one integer is removed from the original set of nine scores, the boxplot changes as shown below. Determine the value of the score that has been removed. (2 marks)



When one integer is removed from the original set of nine scores, the boxplot changes as shown below. Determine the value of the score that has been removed. (2 marks)

(ii) The students' supervisor was concerned that the tag on one of the rabbits reappeared had not been placed by this group of students, but by another group. The student assumed that removing this rabbit from their calculations would not affect their estimate by much and did not recalculate the population estimate. The change in their estimate by removing this rabbit from their calculations would not increase by 245 to 735 rabbits.

Assumption not good, as it can be seen that if only two rabbits were actually recaptured, then population estimate increases by 245 to 735 rabbits.

$$\frac{35}{p} = \frac{2}{42} \Leftrightarrow p = 735$$

Comment on this assumption. (2 marks)

(11 marks)

- (a) The function f is defined by $f(x) = \frac{1}{x+1} + 2$.

- (i) Determine the range of $f(x)$ over the domain $\{-3, -2, 0, 1\}$. (2 marks)

$$\begin{aligned}f(-3) &= 1.5 \\f(-2) &= 1 \\f(0) &= 3 \\f(1) &= 2.5\end{aligned}$$

Range: {1.5, 1, 3, 2.5}

- (ii) Determine the transformations required to obtain the graph of $y = f(x)$ from the

$$y = \frac{1}{x}$$

Translate 1 unit left.

Translate 2 units upwards.

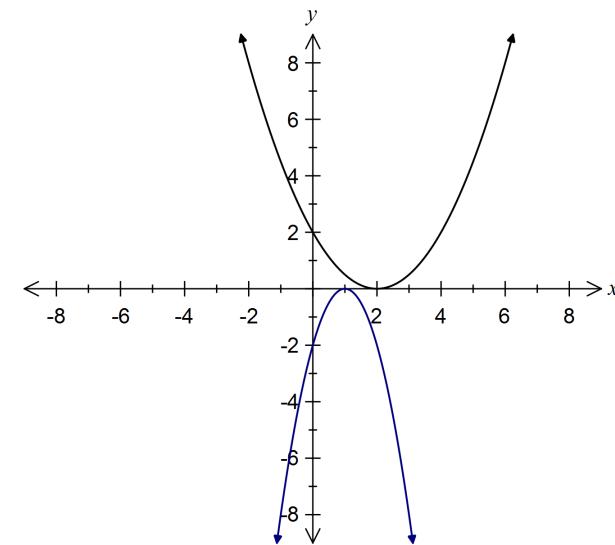
(Either order OK)

- (b) The function g is defined by $g(x) = 2\sqrt{x+4} - 1$. Determine the domain and range of $g(x)$. (2 marks)

Domain: $x \geq -4$.Range: $y \geq -1$.

(2 marks)

- (c) The graph of the function $h(x) = ax^2 + bx + c$ is shown below.



- (i) Determine the values of a , b and c . (3 marks)

$$y = a(x - 2)^2$$

$$x = 0, y = 2$$

$$2 = a(-2)^2 \Rightarrow a = 0.5$$

$$\begin{aligned}h(x) &= 0.5(x - 2)^2 \\&= 0.5x^2 - 2x + 2\end{aligned}$$

$$a = 0.5, b = -2, c = 2$$

- (ii) On the axes above sketch the function $y = -h(2x)$. (2 marks)