



Trinity College

Semester One Examination, 2017

Question/Answer booklet

**MATHEMATICS
METHODS
UNIT 3
Section One:
Calculator-free**

If required by your examination administrator, please place your student identification label in this box

Student Number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes
Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	54	35
Section Two: Calculator-assumed	11	11	100	98	65
Total					100

Instructions to candidates

1. The rules for the conduct of Trinity College examinations are detailed in the *Instructions to Candidates* distributed to students prior to the examinations. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

See next page

Additional working space

Question number: _____

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

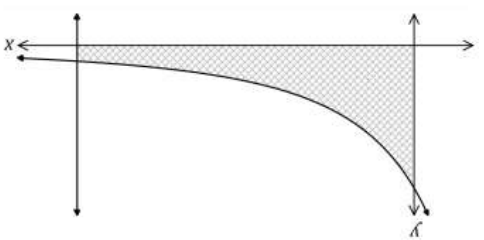
Section One: Calculator-free

(5 marks)

Question 1

The graph below shows the curve $y = \frac{180}{(2x+5)^2}$ and the line $x = 5$.

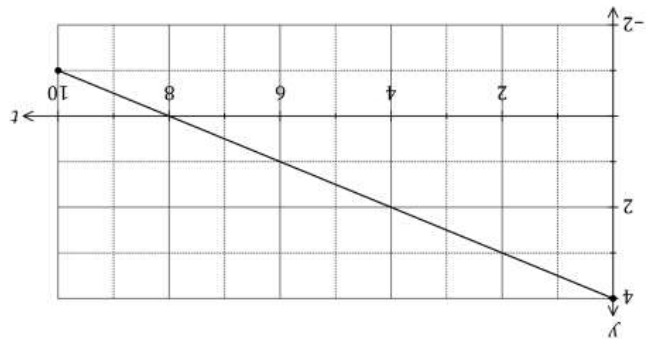
Determine the area of the shaded region, enclosed by the $x -$ axis, the $y -$ axis, the line $x = 5$ and the curve.



(6 marks)

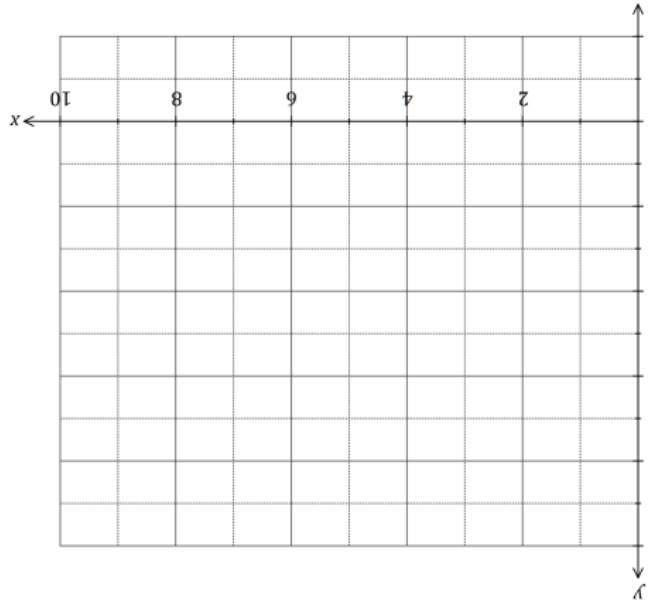
The graph of $y = f(t)$ is shown below over the interval $0 \leq t \leq 10$.

Question 8



(a) Use the graph to determine an estimate for $\int_2^5 f(t) dt$. (2 marks)

(b) On the axes below, sketch the graph of $y = F(x)$ for $0 \leq x \leq 10$, where $F(x) = \int_0^x f(t) dt$. (4 marks)



End of questions

See next page

Question 2

(8 marks)

A small body, initially at the origin, moves in a straight line with acceleration $a(t) = 6t - 10 \text{ ms}^{-2}$, where t is the time in seconds, $t \geq 0$. When $t = 5$, it was observed to have a velocity of 31 ms^{-1} .

(a) Determine an expression for $v(t)$, the velocity of the body. (2 marks)

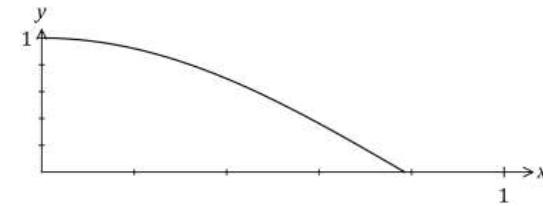
(b) Determine the acceleration of the body when $v = 19$. (3 marks)

(c) Determine the velocity of the body as it passes through the origin for the last time. (3 marks)

Question 7

(6 marks)

A rectangle has its base on the x -axis, its lower left corner at $(0, 0)$ and its upper right corner on the curve shown below, $y = \cos 2x$, $0 \leq x \leq \frac{\pi}{4}$.



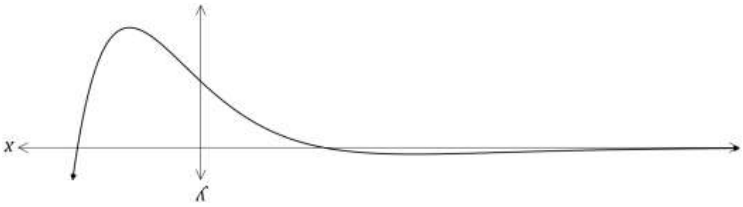
(a) Sketch a possible rectangle on the graph above and explain why the perimeter of the rectangle is given by the function $p(x) = 2x + 2 \cos 2x$. (2 marks)

(b) Determine the largest perimeter of the rectangle. (4 marks)

(7 marks)

Question 3

The graph of $y = f(x)$ is shown below, where $f(x) = e^x(x^2 - 3)$.



(2 mark)

(a) Show that $f'(x) = e^x(x^2 + 2x - 3)$.

(b) Determine the x – coordinates of the stationary points of $f(x)$. (2 marks)

(c) Given that $f''(x) = e^x(x^2 + 4x - 1)$, use the second derivative to justify that one of the stationary points is a local minimum and that the other is a local maximum. (3 marks)

See next page

(7 marks)

Question 6

(a) The function f is such that $f(1) = -2$ and $f'(x) = \sqrt{3 + x^2}$. Use the increments formula to determine an approximate value for $f(1.05)$. (3 marks)

(b) The function C is such that $C(1) = 10$ and $C'(x) = 3\sqrt{x + 3}$.

(i) Explain why the increments formula would not yield an approximate value for $C(6)$. (1 mark)

(ii) Determine $C(6)$. (3 marks)

See next page

Question 4

(8 marks)

(a) Determine $\frac{d}{dx} \left(\frac{1+e^{2x}}{1+\sqrt{x}} \right)$.

(3 marks)

(b) Determine $\frac{d}{dx} (2x \sin(3x))$.

(2 marks)

(c) Use your answer from (b) to determine $\int 6x \cos(3x) dx$.

(3 marks)

Question 5

(7 marks)

The table below shows the probability distribution for a discrete random variable X .

It is known that $E(X) = 1.7$ and $Var(X) = 1.41$.

x	0	1	2	3
$P(X = x)$	a	$a + b$	b	$2a$

(a) Determine the values of the constants a and b .

(4 marks)

(b) Determine

(i) $E(3 - 2X)$.

(2 mark)

(ii) $Var(3 - 2X)$.

(1 mark)