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SC\SD

Calculator-assumed

010S noitsnimax3 304W

Final Marking Key

This 'stand alone' version of the WACE Examination 2010 Final Marking Key is provided on an interim basis.

The Standards Guide for this examination will include the examination questions, marking key, question statistics and annotated candidate responses. When the Standards Guide is published, this document will be removed from the website.

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

2 MARKING KEY

Question 8 (3 marks)

Using your calculator, determine the value of $a^2\sqrt{b}$, where $a=1387\times10^4$ and $b=9.203\times10^{-2}$.

(a) Write down the answer given by your calculator.

(1 mark)

Solution
5.836031578 E+13 (Casio); 5.83603157829 E+13(TI); 5.8360315783 E+13 (HP)
Specific Behaviours
✓ states correct answer from calculator

(b) Write the answer in scientific notation, correct to three significant figures. (2 marks)

Solution
5.84×10^{13}
Specific Behaviours
✓ expresses answer in scientific notation
✓ expresses answer correctly to three significant figures

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

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ACKNOWLEDGEMENTS

Section Two

Question 9 Data source: Australian Taxation Office. (2010). *Individual income tax*

rates: 2009-10. Retrieved March 2010, from

www.ato.gov.au/individuals/content.asp?doc=/content/12333.htm.

Queston 11 Data source: Western Australian Office of Road and Safety. (n.d.). *Number*

of road crashes in Western Australia 1995–2004, by days of the week.

Retrieved March 2010, from http://www.ors.wa.gov.au.

Question 15 Data source: Australian Government. Bureau of Meteorology. (n.d.).

Retrieved March, 2010, from http://www.bom.gov.au/.

Question 16 Data source: Government of Western Australia. Department of

Commerce. Fuel Watch. Retrieved March 2010, from

http://www.fuelwatch.wa.gov.au.

CALCULATOR-ASSUMED 3 MARKING KEY MATHEMATICS 2C/2D

Question 9

Of-600S sater xsT

Tax on this income	Taxable income
l!N	0009\$ - 0\$
15c for each \$1 over \$6 000	000 98\$ - 1009\$
\$4350 plus 30c for each \$1 over \$35 000	932 001 - \$80 000
\$17 850 plus 38c for each \$1 over \$80 000	000 081\$ - 100 08\$
\$22 820 plus 45c for each \$1 over \$180 000	\$180 001 and over

(3 marks)

The table above, from the Australian Taxation Office website, shows the tax rates for the 2009-10 financial year.

Luke has a taxable income of \$93 874.

(a) Calculate the amount of tax Luke will be required to pay.

Ans only 2 marks	 calculates correct total amount (includes fixed amount)
	✓ determines variable tax amount (13 874)
	√ identifies correct tax bracket (38 cents)
	Specific Behaviours
	21.221 \$2\$ =
	21.272.8 + 5 272.12
	(478 E1) 8E. + 038 T1
	noituloS

(b) Louise, Luke's partner, has stayed at home throughout the 2009–10 financial year to take care of their young child. For the 2010–11 financial year, they decide to job share, with each earning half of Luke's previous full-time taxable income.

Assuming tax rates stay the same, what effect would this 2010-11 arrangement have on the total amount of tax paid by both Luke and Louise compared with that paid by on the total amount of tax paid by both Luke and Louise compared with that paid by

states that tax decreases
calculates the difference in tax amount or
calculates total tax paid by couple
Specific Behaviours
Which is \$7 259.92 less than then amount of tax paid if only Luke worked full time.
02.238 21\$ = 00.159 $T \times S = 9$ x $T = 9$ x $T = 9$
01.189 7\$ =
(759 it) 05.0 + 035 4 = 00.759 34 and xsT
noituloS

(5)11511 3)

MARKING KEY

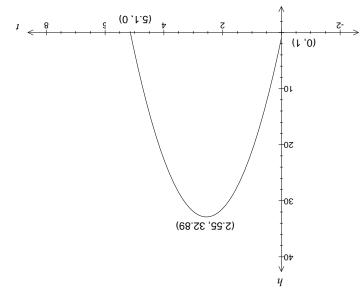
Question 19 (6 marks)

CALCULATOR-ASSUMED

MATHEMATICS 2C/2D

A ball machine sitting on level ground is projecting baseballs into the air so that baseballers can practise their outfield catches. The height (\hbar), in metres, is given by $\hbar = 25t - 4.9t^2 + 1$, where t is the time in seconds after projection.

a) Draw the path of the ball on the axes below, labelling all key features. (4 marks)



identifies maximum at (2.55, 32.89)	^
identifies h -intercept at (0, 1)	^
identifies t -intercept at (5.1, 0)	^
shows shape (graph within bounds, i.e. $t \ge 0$ and $h \ge 0$)	^
Specific Behaviours	
wn above	oys
Solution	

(b) Determine the length of time that the ball is at least 14 metres above the ground.(2 marks)

	√ determines time difference
	$41 = 1 + {}^{2}16.4 - 121$ Sovice >
Specific Behaviours	
	sbroose 29.8 = 1
	12.4 = 1,92.0 = 1
	1.1 = 1 + 1.91 = 1.4
Uomnoe	

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

MARKING KEY

Question 10 (6 marks)

Find the next two terms for each of the sequences defined below.

(i) $T_{n+1} = 0.5T_n$ $T_1 = 40$

$$T_1 = 40$$

(2 marks)

		Solution
	$T_2 = 0.5T_1 = 20$	
	$T_3 = 0.5T_2 = 10$	
	-	Specific Behaviours
✓	calculation of T ₂	
/	calculation of T ₂	

(ii)
$$T_{n+1} = T_{n+2} - T_n$$
 $T_1 = 1, T_2 = 1$

$$T_2 = 1 (2 marks)$$

		Solution
	$T_3 = T_2 + T_1 = 2$	
	$T_4 = T_3 + T_2 = 3$	
		Specific Behaviours
✓	calculation of T ₃	
✓	calculation of T ₄	

Write a recursive rule for the sequence of numbers 8, 12, 18, 27, (2 marks)

		Solution
T _{n+1}	$=\frac{3}{2}$ T _n , T ₁ = 8	
		Specific Behaviours
✓	recognising the rule	
✓	states value of first term.	

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

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MARKING KEY

Question 18 (5 marks)

The table below shows three points of a linear function.

х	1	2	3
y	3 <i>n</i>	4 <i>n</i>	2n + 18

Determine the value of n.

(2 marks)

	Solution
4 <i>n</i>	-3n = 2n + 18 - 4n
n =	= 6
	Specific Behaviours
✓	recognises the common difference
✓	calculates value of n .

Hence determine the equation of the linear rule for this function.

(2 marks)

Solution		
Terms are 18, 24, 30 common difference 6.		
<i>y</i> =	y = 6x + 12	
Specific Behaviours		
✓	determines the gradient	
✓	determines the <i>y</i> -intercept	

Comment on the link between the gradient of your linear rule in (b) and the recursive rule that defines the T_n values in the table below. (1 mark)

n	1	2	3
T_n	3 <i>n</i>	4 <i>n</i>	2n + 18

Solution		
$T_{n+1} = T_n + 6, T_1 = 18$		
The common difference in recursive rule = gradient in linear rule		
Specific Behaviours		
✓ describes the link		

MATHEMATICS 2C/2D 5 MARKING KEY

(10 marks)

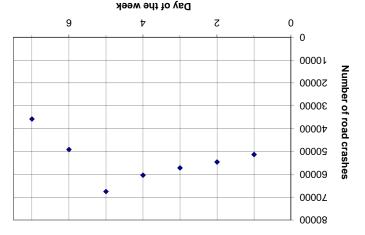
The table and graph show data on the number of road crashes in Western Australia in the 10-year period 1995–2004, by days of the week.

Question 11

Number of road crashes in Western Australia 1995–2004, by days of the week

Number of crashes (nearest thousand)	Day	
91 000	ı	Monday
22 000	2	Tuesday
000 49	ε	Wednesday
000 09	7	Thursday
000 89	G	Friday
000 67	9	Saturday
36 000	L	Sunday

Number of road crashes in Western Australia 1995–2004, by days of the week



(a) Based on the data, which is the safest day of the week on the roads in Western Australia? (1 mark)

	 identifies correct day
Specific Behaviours	
	Sunday
Solution	

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MATHEMATICS 2C/2D CALCULATOR-ASSUMED

A decision has been made to increase all sides of the rhombus by 20%.

(i) Give an expression for the total floor area of the sports centre in the form $ax^2 + bx + c \,. \eqno(2 \text{ marks})$

simplifies expression for area to the form $ax^2 + bx + c$	^
determines an expression for the area of the quadrilateral (using side x 1.2)	^
Specific Behaviours	
$ABCD = 0.72x^2 \text{ m}^2$	391A
$2 \times \left({^{\circ}08 \text{ mis } x2.1 \times x2.1 \times \frac{1}{2}} \right) = \text{QDAA} \text{ and } x = 0$	зэлА
Solution	

How will increasing the sides of the rhombus effect the total floor area of the sports centre? Show your working.

	determines the effect of increasing the side lengths
	Specific Behaviours
	44% increase in the total floor area
	5
	$44. I = {}^{2}x \stackrel{!}{-} \div {}^{2}x \stackrel{?}{\sim} 7.0$
Boildios	

MATHEMATICS 2C/2D
CALCULATOR-ASSUMED

ASSUMED 6 MARKING KEY

(b) Describe any trends in terms of the variables.

(3 marks)

The number of road crashes by days of the week in Western Australia for the period 1995–2004 shows an increasing trend from Monday through to Friday and a decreasing trend from Friday through to Sunday.

Specific Behaviours

- ✓ identifies increasing trend (Monday to Friday)
- ✓ identifies decreasing trend (Friday to Sunday)
- ✓ relates variables to trends
- (c) If a road crash is selected at random from the data for investigation, what is the probability that it occurred on a Saturday or Sunday? (2 marks)

$$\frac{49000 + 36000}{376000} = \frac{85}{376}$$

Or answer approximately 0.2261 (accept: , 0.22 or 0.226)

Specific Behaviours

- ✓ uses correct values from table
- ✓ calculation of probability
- (d) Suppose 1000 of the road crashes are selected at random from the data, and it is found that 223 of them occurred on either a Saturday or a Sunday. Is the result of 223 within the range of values that you would expect? Justify your answer. (4 marks)

Solution

Expected number of crashes (based on the probability $\frac{85}{376}$

$$= \frac{1000 \times 85}{376}$$
$$= 226$$

As 223 is close to 226, the result is likey.

Specific Behaviours

- applies correct probability value to estimate number of crashes
- ✓ calculates expected number of crashes
- ✓ recognises 'close to 226'
- ✓ concludes that the result is likely

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

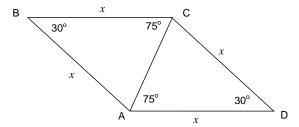
MARKING KEY

(2 marks)

Question 17 (8 marks)

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The diagram below shows a plan for an indoor sports centre ABCD that is to be built in the shape of a rhombus with side length *x* metres. A walkway is planned from A to C.



) Write an expression for the distance between A and C.

	Solution	
Distance = ;xsin30 ⁰ /sin75 ⁰ ;	$\sqrt{x^2 + x^2 - 2 \times x \times x \cos 30^\circ}$ metres. Alternatives:	.5176x;2xsin15 ⁰
Specific Behaviours		
✓ applies correct	ct values to cosine rule	
√ includes squa	are root in expression	

(b) Write a simplified expression for the total floor area of the sports centre. (3 marks)

Solution

Area ABCD =
$$\left(\frac{1}{2} \times x \times x \sin 30^{\circ}\right) \times 2$$

Area ABCD = $\left(\frac{1}{2}x^{2} \times \frac{1}{2}\right) \times 2 = \frac{1}{2}x^{2}$ m²

Specific Behaviours

- √ applies correct rule for area of a triangle
- ✓ multiplies area formula by two for quadrilateral
- ✓ simplifies expression

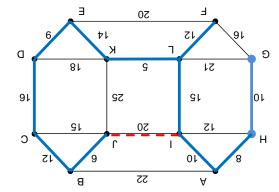
7 MARKING KEY

Question 12 (6 marks)

CALCULATOR-ASSUMED

MATHEMATICS 2C/2D

A communication network linking 12 centres A, B, C, ..., K, L is to be constructed. The possible connections are given in the following network. The number on each arc represents the cost, in thousands of dollars, of establishing the connection.



To minimise the cost, the network management decides to use a minimal spanning tree solution.

ludicate clearly the minimal spanning tree solution on the network above. (3 marks)

noitulo2
evodA nwoda
Specific Behaviours
Sarries through to a degree of accuracy
shows at least 7 correct connections, with no cycle evident
shows at least 9 correct connections, with no cycle evident
shows all connections correctly.

(b) Determine the minimum cost of constructing the communication network. (1 mark)

	expresses total cost in thousands of dollars (based on result in (a))	^
Ī	Specific Behaviours	
	000 ۲۱	l\$
	Solution	

WARKING KEY

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

d) The data for Day 2 includes a price of 161.2 c/L. If this value is removed from the data set, describe the effect on the

(i) mean price value. (1 mark)

m t)	(ii) standard deviation value.
	√ identifies removing the outlier will reduce the mean price
	Specific Behaviours
	Mean will decrease
	Solution

(ii) standard deviation value. (1 mark)

										viation	/əp
standard	ŧре	gnibuloni	sbread,	the	reduce	lliw	outlier	the	removing	səifitnəbi	^
Specific Behaviours											
	Standard deviation will decrease										

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

8 MARKING KEY

(c) The cost of connecting I and J has been overestimated by \$6 000. How does this information change the minimum cost of constructing the network? (2 marks)

JU	utio	Ш

Adding IJ (at a cost of 14 000) and deleting CD (at a saving of 16 000) results in a minimum spanning tree costing \$115 000. Saves \$2 000.

Specific Behaviours

- ✓ identifies connections affected by changed conditions.
- describes effect of changed conditions. Decrease only 0

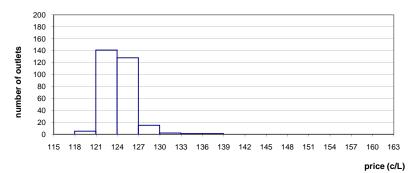
MATHEMATICS 2C/2D CALCULATOR-ASSUMED

MARKING KEY

The frequency histogram for the grouped data for Perth, for Day 1 is shown below.

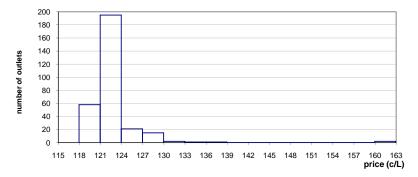
Unleaded petrol prices, Perth, Day 1, grouped data

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Unleaded petrol prices from the same outlets were also recorded for the following day (Day 2). The frequency histogram for Day 2 is given below.

Unleaded petrol prices, Perth, Day 2, grouped data



(c) Did prices for Day 2 tend to be higher or lower than prices for Day 1? Justify your answer. (4 marks)

Solution

The graph suggests that the prices on Day 2 tend to be lower than the prices for Day 1,

because the prices are concentrated (have high frequency/relative frequency) in the intervals 118–120.9 c/L and 121.0 - 123.9 c/L for Day 2 and in the intervals 121.0–123.9 c/L and 124.0–126.9 c/L for Day 1.

Specific Behaviours

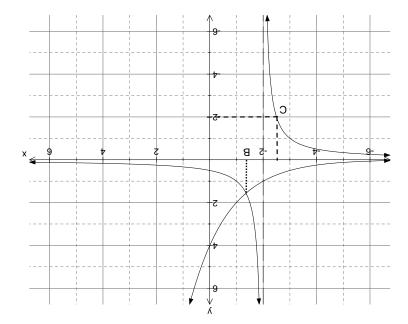
- ✓ identifies correct price behaviour
- ✓ gives reasonable explanation for choice
- √ identifies modal interval
- √ identifies another interval with high frequency

MARKING KEY

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

(7 marks)

The function
$$y = \frac{1}{(x+x)}$$
 is drawn below.



6

On the same axes above, plot the graph of the function $y=2^{(x+2)}$.

identifies exponential growth (behaviour for large x)	^
identifies behaviour for small x	^
identifies y-intercept	^
Specific Behaviours	
уоми ои дгарh	s sA
Solution	

(b) Using your calculator, solve the equation
$$2^{(x+2)} = \frac{1}{(x+2)}$$
.

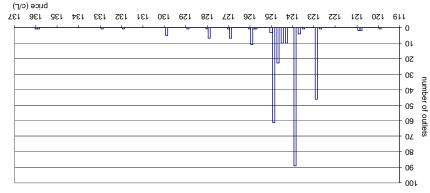
	determines solution	
Specific Behaviours		
	35.1− 10 93£	<u>-1-</u>
Solution		

MARKING KEY

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

The graph displays the price data from the table.

Prices of unleaded petrol, Perth, Day 1



 (a) Describe the centredness and spread of the prices. Use information in the table and graph. Do not calculate any statistics.

Solution

Centredness: Most prices were close to (or slightly more or less equal to) (or within 1 cent) of 123.9C/L; or in the range 122.9 c/L to 124.9 c/L.

Spread: Prices ranged from 119.9 c/L and 136 c/L or two outlets charged more than others (135.9 c/L, 136 c/L) or range in prices was 16.1 c/L or a spread property related to frequency with frequency quantified e.g. the high majority of prices were 124.9 c/L or less (85%); 125.9 c/L or less (91%). Two spread properties.

Specific Behaviours
recognises that most prices were close to "centre"
stating a 'central value' or 'interval'

stating a 'central value' or 'interval'

Y

recognises two spread properties

(b) The table below shows the price data grouped in the equal-sized intervals. Complete
the table.

Unleaded petrol prices, Perth, Day 1

(number of outlets)	
S	118-120.9
141	121-123.9
128	124-126.9
12	127-129.9
7	130-132.9
l	133-135.9
l	136-138.9

	√ determines correct entries.
Specific Behaviours	
	9vods aA
Solution	

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

ED 10 MARKING KEY

(ii) Show on the graph where the answer to (b)(i) can be found. (1 mark)

		Solution	
sho	wn on graph (point B)		
	Specific Behaviours		
✓	identifies correct point		

(c) Indicate on the graph the equation $\frac{1}{(x+2)} = -2$ and state the solution. (2 marks)

	Solution				
Sho	Shown on graph (dashed line)				
x = -	x = -2.5 Point C on the graph				
	Specific Behaviours				
✓	identifies point on graph				
✓	state correct solution				

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

15 MARKING KEY

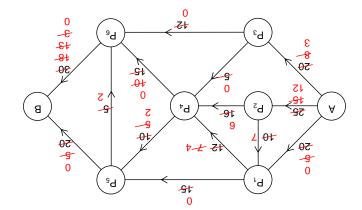
Question 16 (12 marks)

The table shows prices (c/L) of standard unleaded petrol from 293 outlets in Perth on one day in early 2010 (Day 1). All prices published for the day on the Western Australian Government's 'FuelWatch' website are included.

Price (c/L)	Frequency
119.9	
120.8	1 2 2 1
120.9	2
122.7	
122.9	46
123.5	1 4
123.7	4
123.9	89
124.3	10
124.5	10
124.7	23
124.9	61
125.0	3
125.7	3
125.7	1
125.9	11
126.0	1
126.9	7
127.0	7
127.9	
128.0	1
128.9	1
129.9	5
131.9	1
132.9	1
135.9	1
136.0	1

MATHEMATICS 2C/2D 11 MARKING KEY

Question 14In a waste treatment system, liquid waste is moved from treatment plant A to treatment plant B through a pipeline network containing six pumping stations P₁, P₂, P₃, P₄, P₅ and P₆. The network is displayed below. The number on each arc represents the maximum amount of waste, in tonnes per hour, that can be moved along that pipe segment.



(a) What is the maximum hourly amount of liquid waste that can be moved from treatment plant B? Show systematic working to allow your solution to be checked. (3 marks)

calculates total maximum flow.
 shows all flow changes
shows at least 3 flow changes
Carries through to a degree of accuracy
Speci
(Alternatives exist, but max flow = 50 to
Maximum flow = 50 tonnes/hour
09
<u>21:</u> 8 ₈ R A
მ : მ _მ Ч № 4 A
01: 8 a 39 ₄9 ≤9 A
$A_{I} P_{I} P$
3 : 8 ₆ 9 ₄ 9 ₁ 9 A
8 اج اج ا

MARKING KEY	ħί	NED	зеа-яот	.VTD	ZAD
onted by the data for this Western (1 mark)		he box neila nwot nsila	•	(i)	(c)
) the year 2009.	ar 2008 tended to be cooler than	тре уе:			
) the year 2009.	ar 2008 tended to be hotter than	тре уе:			

It is not possible to tell whether the year 2008 tended to be cooler or

	Solution				
(1 mark)	ii) Justify your choice.)			
	identifies correct statement	^			
	Specific Behaviours				
	own above.	as sh			
	noiłuloS				

hotter than the year 2009.

MATHEMATICS 2C/2D

data.	
recognises conclusion about yearly temperature cannot be made from 1 month of	/
Specific Behaviours	
nclusion about temperature for the year can not be drawn from data for 1 month.	0
Solution	

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

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What effect, if any, would there be on the maximum flow of liquid waste from A to B if the capacity of the link between P₆ and B was increased by 5 tonnes per hour. Justify your answer.

Solution	
Flow would increase by 2 tonnes/hour	
Through path: A P ₂ P 1 P ₄ P 5 P 6 B	
(Note that P ₅ P ₆ has only a capacity of 2).	
(Follow through from (a)).	
Specific Behaviours	
√ identifies effect of change on network flow	
✓ describes effect of changed conditions.	

MATHEMATICS 2C/2D CALCULATOR-ASSUMED

MARKING KEY

13 **Question 15** (7 marks)

Table 1 shows some summary statistics for maximum daily temperatures in October 2008 and October 2009 for a Western Australian town. The maximum daily temperatures (°C) in October 2008 for the town are summarised in Table 2.

Table 1: Maximum daily temperatures (°C), October 2008-2009

	October 2008	October 2009
Mean	20.9	21.8
Median	20.0	20.7
Standard deviation	4.4 (4.39)	4.9
Range	17.0	21.8

Table 2: Maximum daily temperatures (°C), October 2008

Temperature T (°C)	Frequency
14 ≤ T < 18	9
18 ≤ T < 22	12
22 ≤ T < 26	5
26 ≤ T < 30	4
30 ≤ T < 34	1

- Use the data in Table 2 to:
 - calculate the mean and standard deviation temperatures for October 2008 and enter the results in Table 1. (2 marks)

	Solution
sho	wn above
	Specific Behaviours
✓	calculates the mean
✓	calculates the standard deviation

determine the modal class.

(1 mark)

	Solution
Moda	I class is 18 ≤ T < 22
Specific Behaviours	
✓	determines the modal class

In which of the two years were the October temperatures in the town less variable? Justify your answer. (2 marks)

Solution
The temperatures in October 2008 were less variable because the standard deviation
of 2008 was lower than the standard deviation for 2009.
(Range may be mentioned, but standard deviation must be mentioned).
Specific Behaviours
✓ recognises sample with higher standard deviation
✓ correct conclusion.