# SEMESTER ONE YEAR 12

# Papers written by Australian Maths Software

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METHODS	SOITAMEHTAM

Unit 3 2016

Section Two

(Calculator-assumed)

Working time for section:	sətunim 001	
Reading time before commencing work:	sətunim 01	
TIME ALLOWED FOR THIS SECTION		
Теасhег:		
Лате:		

MATERIAL REQUIRED / RECOMMENDED FOR THIS SECTION

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler.

Special items: drawing instruments, templates, notes on up to two unfolded sheet of A4 paper, and up to three calculators approved for use in the WACE

examinations.

#### IMPORTANT NOTE TO CANDIDATES

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non–personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

To be provided by the supervisor

Question/answer booklet for Section Two. Formula sheet retained from Section One.

### Structure of this examination

	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	7	7	50	50	35
Section Two Calculator—assumed	13	13	100	100	65
			Total marks	150	100

#### Instructions to candidates

- The rules for the conduct of this examination are detailed in the Information Handbook.
   Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in the Question/Answer booklet.
- You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Spare pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer booklet.

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(5)

(١)

20. (5 marks)

least a 90% chance of having two winning tickets.

The probability of a scratchy winning a prize is about 15%.

A fundraising committee wants to raise as much money as possible on a film evening. If they charge \$25 per person they expect 100 people will attend. From experience they know that for every \$1 they increase the price, 3 people less will attend and for every \$1 they drop the price, they expect 3 more people to attend.

(S) Complete the following table.

		\$54
\$5 200	100	\$7\$
		97\$
Revenue	Number of people attending	Price per entry

(b) Let x be the increase in price in dollars. Find an expected revenue.

maximise the revenue. Show all working.

(c) $p(x) = x$ (c) $p(x) = x$			(c)
		(x + 57)\$	

ε

8. (8 marks)

Write down an equation that needs to be solved to give Paul his answer. (5) (You do not have to solve the equation.)

Paul wants to know how many scratchies he should buy for his wife so that she has at

END OF SECTION TWO

The probability that a new Hardwear tyre will last 18 months is 0.7.

Gerry bought 4 new Hardwear tyres for his car.

(a) What is the probability that over the next 18 months

(i) all four tyres will still be OK?

(2)

(ii) at least one tyre will need replacing?

(2)

(iii) exactly one tyre will need replacing?

(2)

b) (i) Find the expected number of tyres that need replacing over 18 months. (2)

(ii) Find the variance of the distribution.

(2)

(c) A new discrete probability distribution is formed using the transformation y = 3x - 2 on the data in the table in (b).

Write down the expected value and standard deviation of Y.

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(2)

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The value of a spherical pearl, assuming the quality is good, ls proportional to the volume of the pearl. Eddie estimated the diameter to be 12 mm. The diameter was actually 11 mm.

Use a calculus method to estimate the error in the estimated volume of the pearl. (4)

10. (4 marks)

(a) Determine if the data in the following table represents a discrete random variable. Give your reasons.

2.0	4.0	ε.0	1.0	(x = X)d
9 <	ς	<i>t</i>	3	х

(i) Complete the following table for a discrete random variable X.

Determine

(1) 
$$(2 = x \text{ so } I = x) \mathbf{q} (ii)$$

 $(1) (2 \le x)^{q} (iii)$ 

(iv) the expected value and the standard deviation of X.

(3)

11. (6 marks)

The acceleration of a particle is given by a = 2 - t

(a) Determine an expression for the velocity and displacement given that at

$$t = 1, v = 1.5 \, ms^{-1} \text{ and } x = \frac{5}{6} \, m.$$
 (3)

(b) Determine the displacement x when the particle first changes direction for t > 0.

(3)

6

## 18. (8 marks)

A spinner is labelled 1,2,3,4 and a die is rolled. The number on the spinner and the upper face of the die are added.

The possible outcomes are shown in the table below.

		Die							
	Scores	1	2	3	4	5	6		
	1	2	3	4	5	6	7		
Spinner	2	3	4	5	6	7	8		
	3	4	5	6	7	8	9		
	4	5	6	7	8	9	10		

(a) Complete the probability density table below for the scores.

х	2	3	4	5	6	7	8	9	10
P(X = x)									

(b) Find the probability that the score is even. (2)

(c) Find the probability of a score less than 6. (2)

(d) Find a, for  $a \neq 4$ , such that P(X = 4) = P(X = a). (1)

(2)

(2)

12. (7 marks)

The definition of a derivative of a function y = f(x) is defined as

$$\frac{y}{(x)f-(y+x)f} \min_{0 \leftarrow y} = (x), f$$

(a) Consider 
$$f(x) = 2^x$$
.

Fill in the gaps indicated below as Fill in the gaps indicated below as

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$$\frac{\eta}{\left(\begin{array}{c} \eta \\ \end{array}\right)_{x}} \underbrace{\begin{array}{c} 0 \leftarrow \eta \\ u i j \\ \end{array}}_{I \times x Z - \eta Z \times x Z} \underbrace{\begin{array}{c} 0 \leftarrow \eta \\ u i j \\ \end{array}}_{i = 1} = \underbrace{\begin{array}{c} \eta \\ u i j \\ \end{array}}_{x Z - (\eta + x)} \underbrace{\begin{array}{c} 0 \leftarrow \eta \\ u i j \\ \end{array}}_{i = 1} = (x), f$$

Therefore if 
$$f(x) = 2^x$$
 then  $f(x) = x^*$ 

(2) Given 
$$f(x) = 2^x$$
, find  $f'(3)$ .

17. (5 marks)

Consider the following table.

I	6.0	7.0	4.0	1.0	$(x \ge X)d$
ς	7	ε	7	I	х

(2) (a) Complete the probabilities in the table below

				1.0	(x = X)d
ς	7	3	7	I	х

$$(t) \qquad \qquad (t \le x)^q \quad \text{brid} \quad (d)$$

(c) Find 
$$P(x>2)$$

13. (11 marks)

(a) A body moves according to the law  $x = 3 \sin(2t)$ .

(i) Find x when 
$$t = \frac{\pi}{4}$$
. (1)

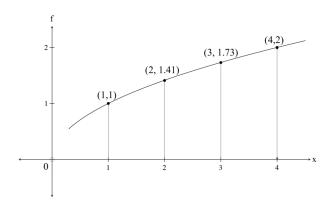
(ii) Find the expressions for velocity (v) and acceleration (a). (2)

(iii) Show that a = kx where k is a constant. (1)

(b) Given the functions f(x) = sin(2x) and g(x) = cos(x), find the smallest positive x where f'(x) = g'(x). (3)

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(b) The function  $f(x) = \sqrt{x}$  is graphed below.



(i) Using rectangles from above and from below, find an estimate for the area between the function  $y = \sqrt{x}$ , x = 1, x = 4 and the x axis.

Use 
$$\Box x = 1$$
 as the width of the interval. (5)

(ii) Use integration to evaluate the exact area estimated in (i). (2)

Choose pairs of functions that have the same derivatives and explain why this is

(c) Some of the following functions have the same derivative.

(<del>1</del>)

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 $(x)^{2} nis - 1 = (x) f \quad (iv)$ 

 $^{2}x - 4.\mathcal{E} = (x) t \qquad (v)$  $\underline{t-x} = (x) f \quad \text{(vi)}$  $\underline{x} = (x) f$  (iii)  $u + z x - = (x) f \qquad \text{(ii)}$  $(i) \quad f(x) = \cos x$ 

(a) Consider the graph below

16. (11 marks)

 $6.\varepsilon = xb(x) \int_0^d \int_0^d bms \ 4.\varepsilon = xb(x) \int_0^d \int_0^d mevið$ 

(2)

 $xp(x) \int_{a}^{d}$  bnif (i)

(ii) find the area bounded by the function and the x axis on the interval [0,b].

14. (5 marks)

- (a) Given  $y = e^{\sin(x)}$ 
  - (ii) find an expression  $\frac{dy}{dx}$  (1)

(ii) hence evaluate  $\int_0^{\frac{\pi}{2}} (\cos(x) \times e^{\sin(x)}) dx$ . (2)

(b) Use your calculator to evaluate  $\int_{2}^{3} \frac{1-x^{2}}{\sqrt{1+x^{2}}} dx$  correct to two decimal places. (2)

10

15. (8 marks)

The population in China in 1965 was estimated to be 715.2 million people. In 1979 this had increased to 969 million people.

(a) Had this rate of growth continued, what is the expected population in 2016? (3)

With the introduction of the one child policy in 1979, the population was thought to be increasing at a slower rate.

In 2015 China's population was 1 401.6 million people.

(b) What was the annual rate of growth since 1979? (3)

c) What reduction in population did the one child policy result in by 2016? (2)