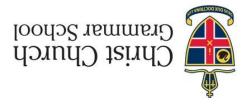
TEST 2 2019



MATHEMATICS METHODS Year 11

MARKING KEY

Time and marks available:

32 marks Marks available: 30 minutes Working time for this section: 3 minutes Reading time Calculator-Free

Calculator-Assumed

10 marks Marks available: 10 minutes Working time for this section:

This Question/Answer Booklet To be provided by the supervisor Materials required/recommended:

Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

and up to three calculators approved for use in the WACE examinations drawing instruments, templates, notes on one unfolded sheet of A4 paper Special items:

Important note to candidates

before reading any further. examination room. If you have any unauthorised material with you, hand it to the supervisor you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be taken into the examination room. It is your responsibility to ensure that MARKING KEY 2 MATHEMATICS METHODS Year 11

Instructions to candidates

- The rules of conduct of the CCGS assessments are detailed in the Reporting and Assessment Policy. Sitting this assessment implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- Answer all questions.
- 4. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 6. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.

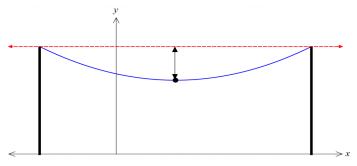
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MARKING KEY 11 MATHEMATICS METHODS Year 11

Question 7 (6 marks)

A high voltage power line is supported by support towers that are each 6.7 m in height. The 'sag' in the power line is defined to be the vertical distance the power line is below 6.7 m

The height of the power line between the towers is modelled by the quadratic function $y = 0.004x^2 - 0.08x + 5$ as shown below.



(a) Determine the distance between the support towers, correct to the nearest 0.01 metres (3 marks)

Solution

Require y = 6.7 i.e. solve $0.004x^2 - 0.08x + 5 = 6.7$

From CAS x = -12.913..., x = 32.913...

Hence the distance between the support towers = 32.913... - (-12.913..)

: Distance between towers is 45.83 metres

Specific behaviours

- \checkmark forms the quadratic equation correctly for y = 6.7
- √ solves the quadratic equation correctly
- √ determines the distance between the towers correctly to 0.01 metres
- 1.1.9 and 1.1.12
- (b) Determine the maximum sag in the power line, correct to the nearest 0.01 metres.

(3 marks)

Solution

The greatest sag will occur at the turning point for the parabolic shaped power line. From CAS this is at the point (10, 4.6)

OR
$$y = 0.004(x-10)^2 + 4.6$$

Hence the greatest sag = 6.7 - 4.6

$$= 2.1$$

i.e. the greatest sag is 2.10 metres.

Specific behaviours

- √ uses the idea of determining the turning point of the height function
- √ determines the minimum function value (minimum height)
- √ determines the maximum sag correctly
- 1.1.12

NATHEMATICS METHODS Year 11

MARKING KEY

Calculator-Free Section

(e marks)

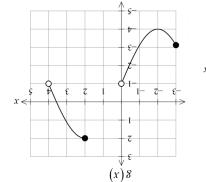
(33 marks)

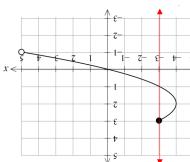
Question 1

ε

The graphs of relations f and g are shown below.

(x) f





(S marks)

Explain. Which of the relations f or g is NOT a function.

Solution

drawn to intersect the graph of f in more than one point. have the same x coordinate e.g. (-3,1) and (-3,5). That is a vertical line can be Relation f is NOT a function, since there are instances where TWO ordered pairs

Specific behaviours

explains why ∮ is not a function 1.1.28 ∨ √ states that f is NOT a function 1.1.28

(2 marks) State the domain of relation f.

42.	λ excludes the value $\lambda = x$ from the domain λ .
77	indicates all real numbers from -4 to δ
nrs	oivad sifiseq8
	Range $D_f = \{x -4 \le x \le \delta \}$
	Solution

(2 marks)

State the range of relation 8.

\checkmark excludes the value $y = -1$ from the range 1.1.24
42.1.1 2 of 4- mort shadmun lise all real indicates all real numbers from -4.1.24
Specific behaviours
Domain $R_s = \{y \mid -4 \le y \le 2, y \ne -1\}$
Solution

See next page

MATHEMATICS METHODS Year 11

MARKING KEY

(10 marks)

Calculator-Assumed Section

(4 marks) Question 6

۱0

inversely proportional to its volume \boldsymbol{V} , measured in Litres . The pressure $\,^{0}$, measured in $\,^{1}\!\!\!/ p_{a}$, exerted by a certain mass of gas at room temperature is

This particular amount of gas exerts a pressure of $2.75 \, \mathrm{kP}a$ when its volume is $4.5 \, \mathrm{litres}$.

(2 marks) Express the relationship between the pressure $\,^{
m V}$ and the volume $\,^{
m V}$.

81.1.		
√ determines the reciprocal rule correctly (in any form)		
 expresses pressure in terms of the reciprocal of volume 		
Specific behaviours		
Hence $P=\frac{12.375}{V}$ OR $PV=12.375$		
$\mathcal{E} \cap \mathcal{E} \cap \mathcal{E} = \mathcal{E} \cap $		
Since $\int d^2 x d^2 x d^2 x d^2 x$ we can write $\int d^2 x d^2 x$		
Solution		

pressure of the gas, correct to 2 decimal places. (z warks) If the volume of this gas is reduced by $0.7\ litres$, determine the increase in the (q)

determines the correct increase in pressure	٨
substitutes the correct volume value	^
Specific behaviours	
902.0 =	
$\Delta P = 3.2652.75$ Hence the pressure will increase by 0.51 kPa.	
hen $P = \frac{12.375}{(3.8)} = 3.2565$ kPa	T
settil $8.\xi = 7.0 - 2.4 = V$ gnis	Λ
Solution	

51.1.1

Question 2 (6 marks)

Solve exactly the following equations:

(a)
$$\frac{5}{x-3} = \frac{3}{x+4}$$
 (3 marks)

Solution

Multiplying each side by (x-3)(x+4) obtains:

$$5(x+4) = 3(x-3)$$
 ... (1)

i.e.
$$5x+20 = 3x-9$$
 ... (2)

i.e.
$$2x = -29$$

$$x = -\frac{29}{2}$$
 or $x = -14.5$

Specific behaviours

- \checkmark multiplies both sides by (x-3)(x+4) to obtain equation (1)
- √ expands correctly to obtain equation (2) or its equivalent
- \checkmark solves correctly to obtain x

1.1.6

(b)
$$x(x-12) = -5$$
 (3 marks)

Solution

$$\therefore x^2 - 12x + 5 = 0$$

i.e.
$$(x-6)^2 - 36 + 5 = 0$$
 \therefore $(x-6)^2 = 31$

$$x-6 = \pm \sqrt{31}$$

i.e.
$$x = 6 + \sqrt{31}$$
 or $x = 6 - \sqrt{31}$

Specific behaviours

- √ obtains the standard quadratic equation correctly
- ✓ performs the completion of square process correctly
- ✓ solves correctly to obtain $x = 6 \pm \sqrt{31}$

Alternative Solution

$$\therefore x^2 - 12x + 5 = 0$$

i.e.
$$x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(1)(5)}}{2(1)}$$
 using the Quadratic Formula

i.e.
$$x = \frac{12 \pm \sqrt{124}}{2} = \frac{12 \pm 2\sqrt{31}}{2} = 6 \pm \sqrt{31}$$

i.e.
$$x = 6 + \sqrt{31}$$
 or $x = 6 - \sqrt{31}$

Specific behaviours

- √ obtains the standard quadratic equation correctly
- √ substitutes correctly into the quadratic formula
- ✓ solves correctly to obtain $x = 6 \pm \sqrt{31}$

1.1.9

See next page

Question 5 (3 marks)

9

The graph of $y = kx^2 + 4x + k$ has no x intercepts. Determine the value(s) of the constant k.

Solution

The intersection with the *x*-axis occurs when $kx^2 + 4x + k = 0$.

Hence this means that $kx^2 + 4x + k = 0$ has NO solutions.

- ∴ ∆<0
- $\therefore (4)^2 4(k)(k) < 0$
- i.e. $16-4k^2 < 0$ i.e. $k^2 > 4$
- \therefore k > 2 or k < -2 for no x intercepts

Specific behaviours

- ✓ states that the discriminant must be negative for no solutions
- √ forms the correct expression for the discriminant
- \checkmark solves correctly for the value for k
- 1.1.11

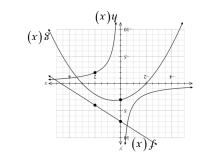
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(S marks)

(s)

(7 marks) Question 4

The diagram below shows the graphs of functions f(x), g(x) and h(x)



Determine the defining rules for function:

Solution Solution Solution
$$(x, y)$$
. Solution $(0, y)$ Gradient $(0, y)$ Gradient Specific behaviours $(0, y)$ Gradient $(0, y)$ Gradient

4.1.1 writes the equation of the line correctly (using correct notation)

Solution · (x)8 (q) (3 marks)

Specific behaviours Using (0,3) 3 = k(0+2)(0-3)intercepts are x = x and Factor Form $(\xi - x)(\Delta + x)\lambda = (x - x)$ and Factor Form

 $\xi = q$ pur $\zeta - = v$ sasn \nearrow $(d-x)(n-x)\lambda = (x)S$ moof factor form S

 \checkmark uses a known ordered pair to correctly deduce the value of k (dilation factor)

01.1.1,8.1.1

(x)y(c) (2 marks)

See next page

Graph suggests the defining rule
$$h(x) = \frac{\lambda}{x}$$
 i.e. $h(x) = -\frac{\lambda}{x}$ i.e. $h(x) = -\frac{\lambda}{x}$ Specific behaviours

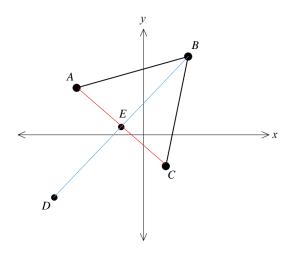
√ writes the reciprocal defining rule correctly $\frac{x}{y} = (x)y$ muot ett sesu >

41.1.1

See next page

Question 3 (10 marks)

The graph indicates points A(-3,3), B(2,5) and C(1,-2). Point D is positioned so that ABCD is a parallelogram. Point E is the midpoint of both AC and \overline{BD} since it is a property of a parallelogram that the diagonals bisect each other. The coordinates of E are (-1,0.5).



Determine the equation for \overrightarrow{BC} in the form y = mx + c.

(3 marks)

	Solution	
$m(\overline{BC}) = \frac{5 - (-2)}{2 - 1} = 7$	Equation for \overrightarrow{BC} :	y-5=7(x-2)
	i.e. $y-5 = 7x-14$	
	$\therefore y = 7x - 9$	

Specific behaviours

- determines the gradient correctly
- \checkmark forms the equation of the line correctly using point B or C
- writes the equation correctly in the form y = mx + c

1.1.5

Using the coordinates of E(-1,0.5), determine the coordinates for point D. (2 marks)

2+a $5+b$
Let point D be (a,b) $\therefore -1 = \frac{2+a}{2}$ and $0.5 = \frac{5+b}{2}$
Solving gives $a=-4$ and $b=-4$ i.e. D is the point $\left(-4,-4\right)$.
Specific behaviours

- \checkmark writes the equations relating the coordinates of E in terms of B and D correctly
- \checkmark solves these equations correctly to determine point D

1.1.2

Using the coordinates of E(-1,0.5), determine the coordinates for point D. (2 marks)

7

Alternative Solution

From $B \rightarrow E$ $\Delta x = -3$ and $\Delta y = -4.5$

So $E \rightarrow D$ will also have $\Delta x = -3$ and $\Delta y = -4.5$

i.e. D is the point (-1-3, 0.5-4.5) = (-4, -4).

Specific behaviours

 \checkmark determines the step sizes/changes in coordinates from $B \to E$ correctly

 \checkmark determines point D correctly

1.1.2

MARKING KEY

Consider a line containing C and perpendicular to \overrightarrow{AB} .

Determine the equation for this perpendicular line.

(3 marks)

$$m(\overline{AB}) = \frac{5-3}{2-(-3)} = \frac{2}{5} \qquad \therefore \quad m(Perp) = -\frac{5}{2} \text{ since } m_1 m_2 = -1$$

Equation for Perpendicular containing $C: y-(-2) = -\frac{5}{2}(x-1)$

i.e.
$$2(y+2) = -5(x-1)$$

$$5x + 2y = 1$$

OR
$$y = 0.5 - 2.5x$$
 OR $y = \frac{1 - 5x}{2}$

Specific behaviours

- \checkmark determines the gradient of \overrightarrow{AB} correctly
- ✓ determines the perpendicular gradient correctly using $m_1 m_2 = -1$
- \checkmark forms the equation correctly containing point C

1.1.5

Show that ABCD is NOT a rectangle.

(2 marks)

Solution

We need to show that $s\angle ABC \neq 90^{\circ}$ i.e. $m(\overrightarrow{AB})m(\overrightarrow{BC}) \neq -1$

$$m(\overline{AB}) = \frac{2}{5} \quad m(\overline{BC}) = 7$$

Since $\frac{2}{5} \times 7 \neq -1$ then *ABCD* is NOT a rectangle.

Specific behaviours

- ✓ states or infers that if *ABCD* is a rectangle then sides are at right angles
- ✓ states or concludes that the product of adjacent gradients $\neq -1$

1.1.5