



## SOITAMEHTAM

**5C/5D** 

**Calculator-free** 

**010S** noitsnimax3 304W

Final Marking Key

This 'stand alone' version of the WACE Examination 2010 Final Marking Key is provided on an interim basis.

The Standards Guide for this examination will include the examination questions, marking key, question statistics and annotated candidate responses. When the Standards Guide is published, this document will be removed from the website.

| <b>MATHEMATICS 2C/2D</b> |
|--------------------------|
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MARKING KEY

Question 1 (6 marks)

Solve each of the following equations.

a) 
$$3x^2 - 15x = 0$$

(3 marks)

|                                | Solution |  |
|--------------------------------|----------|--|
| $3x^2 - 15x = 0$               |          |  |
| 3x(x-5)=0                      |          |  |
| x = 0 or $x = 5$               |          |  |
| Specific Behaviours            |          |  |
| √ factorises expression        |          |  |
| √√ solves for both values of x |          |  |

(b) (x + 1)(x - 2) = 4

(3 marks)

| Solution            |  |  |
|---------------------|--|--|
| $x^2 - x - 6 = 0$   |  |  |
| (x + 2)(x - 3) = 0  |  |  |
| x = -2 or $x = 3$   |  |  |
| Specific Behaviours |  |  |

✓ follows conventions when rearranging algebraic terms

√ ✓ solves for both values of x

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Question 2

(a) Simplify

(b) Simplify

(c) Marks)

 $\frac{\Im_{\pi}}{\Im_{2} \times \Im_{3}}$  (1 mark)

|          | ✓ simplifies by adding and subtracting powers |
|----------|---|
|          | Specific Behaviours                           |
|          | 91= +2=                                       |
|          | $= 2^{4} = 16$                                |
|          | $\Sigma_{t}$                                  |
|          | $\overline{\Sigma_2 \times \Sigma_3}$         |
| Solution |   |

(b) Estimate the solution to the equation  $\frac{14}{2^x} = 1$  to the nearest whole number. Justify your answer. (2 marks)

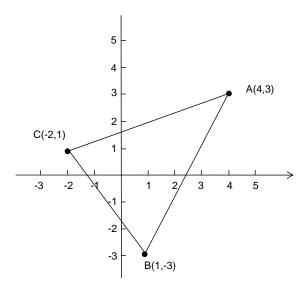
| value; 1 for justification) | ✓ tests values to decide nearest estimate (1 for correct   |
|-----------------------------|--|
|                             | ✓ simplifies equation  |
|                             | Specific Behaviours  |
|                             | <b>⊅</b> = <b>X</b> ∴  |
|                             | $\frac{7}{8} = \frac{1}{8}$  |
|                             | $\delta \nabla \cdot \Gamma = \frac{\Gamma}{\mu} = \frac{\mu \Gamma}{8}$ $\delta = {}^{6}\Sigma$ |
|                             | Testing:   |
|                             | $I t = \Sigma_x$   |
|                             | $I = \frac{x \zeta}{t}$  |
|                             | noituloS   |

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Question 3 (7 Marks)

The diagram below shows the position of three mine shafts A(4, 3), B(1, -3) and C(-2, 1), relative to the processing plant that is located at the origin (0, 0). All units are in kilometres.



(a) Determine the gradient of the line passing through AB.

(1 mark)

|                     | Solution  |
|---------------------|---|
| 2                   |   |
| Specific Behaviours |   |
| ✓                   | uses co-ordinates of A and B to determine gradient. |

(b) What is the gradient of the line perpendicular to the side AB?

(1 mark)

|                     | Solution  |  |
|---------------------|---|--|
|                     |   |  |
| 1                   |   |  |
|                     |   |  |
| 2                   |   |  |
|                     |   |  |
| Specific Behaviours |   |  |
|                     | opcomo Bonavicare   |  |
| ✓                   | recognises the relationship between gradients of perpendicular lines. |  |
|                     |   |  |

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## **ACKNOWLEDGEMENT**

**Section One** 

Question 6 Data source: Australian Bureau of Statistics. (n.d.). Retrieved March, 2010,

from www.abs.gov.au.

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**MARKING KEY** 

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(3 marks) Question 7

**MARKING KEY** 

The following is a list of all prime numbers less than 20.

2, 3, 5, 7, 11, 13, 17, 19

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Kate looked at this list and came up with the following conjecture:

Ένeιγ integer greater than three can be written as the sum of two prime numbers.'

(S marks) Show calculations for four different integers to test whether this conjecture might be (a)

tests conjecture with two examples tests conjecture with two examples Specific Behaviours \* 9 + 5 = 11 9+9=01 7 + 2 = 03 + 5 = 83 + 2 = 7  $\mathcal{E} + \mathcal{E} = 0$ E + S = B2 + 2 = 4 Solution

Give your conclusion to the conjecture, based on your results in (a). (1 mark)

| (1  | pased on (s | makes valid statement | ^ |
|---|-------------|-----------------------|---|
| Sehaviours                                  | Specific E  |                       |   |
| cannot conclusively say it is true.         |             |                       |   |
| have not tested all possible values and     |             |                       |   |
| the sum of two prime numbers, however, we   |             |                       |   |
| because all values in (a) can be written as |             | Not true for 11       |   |
| It appears to be true                       | 10          | False.                |   |
| Politich                                    |             |                       |   |

through the point C. (c) Determine the equation of the line that is perpendicular to the side AB and passes

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| Specific Behaviours  nd co-ordinates of C into equation.  | substitutes gradient a | •  |
|---|------------------------|--|
| 7   |                        |  |
| 7   |                        |  |
| noibulos $3 + xxn = \zeta$ $3 + (2 -)\frac{1}{2} = I$ $3 + I = I$ $0 = 3$ $x \frac{1}{\zeta} = \zeta$ | -                      | $x\frac{\zeta}{\zeta} - = \zeta$ $-x\frac{\zeta}{\zeta} - = \zeta$ |

(1 mark) (d) Determine the distance between the mine shaft at A and the processing plant.

|           | determines correct distance                 |
|-----------|---|
| ehaviours | Specific B                                  |
|           | $\sqrt{(4-0)^2+(3-0)^2} = \sqrt{25} = 5$ km |
| noitulos  |   |

(2 marks) determine who will be the first to arrive at their destination. Justify your answer. from A. Assuming that they both start to travel at the same time and at the same speed, Mary needs to drive from B to C, while John needs to return to the processing plant

| makes correct conclusion based on distances                               | ^          |
|---|------------|
| determine correct distance for John                                       | ^          |
| Specific Behaviours   |            |
| Mary and John will take exactly the same time to reach their destination. | Therefore, |
| $\sqrt{(1+2)^2+(-3-1)^2}=\sqrt{25}=5km$                                   |            |
| Solution  |            |

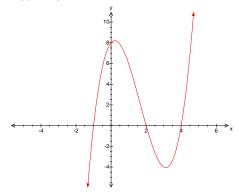
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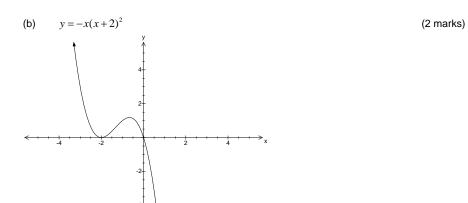
Question 4 (5 marks)

Draw a neat sketch of each function.

(a) 
$$y = (x+1)(x-2)(x-4)$$
 (3 marks)



|          | Solution                         |
|----------|----------------------------------|
| Graph as | s above                          |
|          | Specific Behaviours              |
| ✓        | displays the correct orientation |
| ✓        | identifies correct y-intercept   |
| ✓        | identifies correct x-intercepts  |



| Solution                |                                 |  |
|-------------------------|---------------------------------|--|
| as above                |                                 |  |
| Specific Behaviours     |                                 |  |
| ✓                       | ✓ recognises minimum at (-2, 0) |  |
| ✓ passes through (0, 0) |                                 |  |

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(d) (i) Express the following question using probability notation:

'Given that the value of a crop for the year ending June 2009 was greater than the value for the year ending June 2008, what is the probability that the harvest (tonnes) increased?'

(1 mark

(1 mark)

| Solution            |                                     |  |
|---------------------|-------------------------------------|--|
|                     | P(H <sup>+</sup>   V <sup>+</sup> ) |  |
| Specific Behaviours |                                     |  |
| ✓                   | correct notation                    |  |

Determine the answer to the question in (i).

|                     | Solution                         |  |
|---------------------|----------------------------------|--|
|                     | 4                                |  |
|                     | <del>-</del> 5                   |  |
| Specific Behaviours |                                  |  |
| ✓                   | correctly determines probability |  |

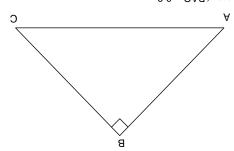
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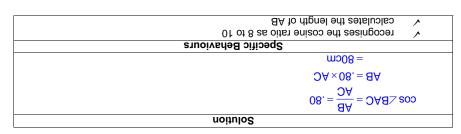
Question 5 (4 marks)

Consider the following triangle.



In the triangle above,  $\cos \angle BAC = 0.8$ .

(a) If the length of AC is 100 cm, calculate the length of AB.



(2 marks)

(2 marks) (2 marks)

| A⊃A ≤ Actermines tan ∠ACB  |
|--|
| v recognises the tangent ratio as 80 to 60   |
| Specific Behaviours  |
| $\left(\hat{\varepsilon}\hat{\varepsilon}.\hat{\Gamma}\text{10}\right)$ $\frac{1}{\hat{\varepsilon}}=$ |
| 09   |
| $\frac{08}{}$  |
| BC BC  |
| $\frac{08}{a} = \frac{AA}{a} = AA \triangle nst$   |
| Solution   |

WARKING KEY

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(b) Explain the real-life meaning of  $n(H^+ \cap V^+)$  and find its value.

Solution

The number of crops for which the harvest and value increased in the year ending 2009 compared to the year 2008.  $n(H^+ \cap V^+) = 4$  Specific Behaviours

Specific Behaviours

identifies intersection of sets correct value.

(c) Evaluate

(i)  $P(H^+ \cup V^+)$ 

(ii)  $P(H^+ \cup V^+)$ 

 $= \frac{2}{9}$  Specific Behaviours  $\sqrt{\text{calculates probability based on (a)}}$ 

(iii)  $P(\overline{H}^{\uparrow} \cup \overline{V}^{\uparrow})$  (2 marks)

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Question 6 (12 marks)

Australian agriculture is important for food production and export earnings. The table compares the harvest (000 t) and value (\$million) of some crops in Australia for the years ending June 2008 and June 2009.

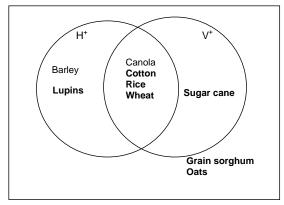
## Australian agriculture, years ending June 2008 and June 2009

|                            |               | Harvest (000t) |        | Value (\$million) |       |
|----------------------------|---------------|----------------|--------|-------------------|-------|
|                            | Crop          | 2008           | 2009   | 2008              | 2009  |
| Harvest up in 2009         | Barley        | 7 160          | 7 669  | 2 244             | 1 767 |
|                            | Canola        | 1 214          | 1 861  | 659               | 1 026 |
|                            | Cotton        | 119            | 303    | 227               | 623   |
|                            | Lupins        | 662            | 716    | 222               | 202   |
|                            | Rice          | 18             | 63     | 7.3               | 35.5  |
|                            | Wheat         | 13 569         | 20 939 | 5 292             | 5 894 |
| Harvest<br>down in<br>2009 | Grain sorghum | 3790           | 2671   | 977               | 550   |
|                            | Oats          | 1502           | 1205   | 423               | 255   |
|                            | Sugar cane    | 32 621         | 30284  | 861               | 983   |

Let  $H^+$  denote the set of crops for which the harvest was greater in the year ending June 2009 than in the year ending June 2008 and  $V^+$  denote the set of crops whose value was greater in the year ending June 2009 than in the year ending June 2008.

(a) Complete the Venn diagram for sets H<sup>+</sup> and V<sup>+</sup>.

(4 marks)



| Solution            |                                     |  |
|---------------------|-------------------------------------|--|
| as above            |                                     |  |
| Specific Behaviours |                                     |  |
| ✓                   | correct entries in the intersection |  |
| ✓                   | ✓ correct entry – lupins            |  |
| ✓                   | correct entry – sugar cane          |  |

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correct entries – grain sorghum, oats.

**MARKING KEY**