### Christ Church Grammar School

2015	'8	Paper	Practice	Exams	A٧
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Question/Answer Booklet

S GNA 1 STINU If required by your examination administrator, please place your student identification label in this box **MATHEMATICS** 

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								<b>ime allowed for this se</b> seding time before commencir vorking time for this section:	Ħ
		 				-	Your name		
-		 				-	ln words		
							In figures	Student Number:	

To be provided by the candidate Standard lieuristical, pencils (including coloured), sharpener, contection fluid/spe, eraser, ruler, highlighters

Special items: nil

Section One: Calculator-free

**WETHODS** 

Important note to candidates

No other lenns may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised materials with you, hand it to the supervisor beatons reading any further.

### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator- assumed	13	13	100	98	65
			Total	150	100

CALCULATOR-FREE

### Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2015. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - responses and/or as additional space if required to continue an answer.

    Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - page.

    Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the name.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

(2 marks)	(iii) the coordinates of all axes intercepts.	
(1 mark)	(ii) the equation of the line of symmetry.	
(Ynsm †)	(i) the coordinates of the furning point.	
	For the graph of $y = f(x)$ , state:	(c)
(2 таңка)	0 = (x)f notine equal only only only only only only only onl	(q)
(2 marks)	o pue	
bx + c. Determine the values of b	The function can also be written in the form $f(x) = x^2 + x$	(8)
	usdratic function is given by $J(x) = (x - 2)^2 - 9$ .	pΑ
(8 marks)	t noitee	gne
	vided. rking time for this section is 50 minutes.	b.o.
(52 Marks) (fite your answers in the spaces	tion One: Calculator-free section has seven (7) questions. Answer all questions. W	
METHODS UNITS 1 AND 2	E 33RF-FOELAUDL	CAI

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### METHODS UNITS 1 AND 2 CALCULATOR-FREE

Question 2 (7 marks)

- (a) Determine the coordinates of the midpoint of A(-12, 3) and B(8, -9). (1 mark)
- (b) Are the straight lines given by 3x + 4y = 12 and y = 0.75x + 1.25 parallel, perpendicular or neither? Justify your answer.

(c) Determine the equation of the straight line perpendicular to the line  $y = 8 - \frac{1}{3}x$  and passing through the point (2, 1). (2 marks)

(d) Solve  $2(3x-2) = \frac{2x+11}{2}$ . (2 marks)

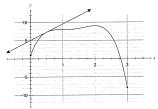
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CALCULATOR-ASSUMED METHODS UNITS 1 AND 2 (10 marks) A function is given by  $f(x) = 1 + 24x - 30x^2 + 16x^3 - 3x^4$ .

(a) Use calculus techniques to determine the coordinates of all stationary points of the function. (3 marks)



(b) Sketch the graph of y = f(x) for  $0 \le x \le 3$  on the axes below.



(c) Determine the equation of the tangent to the curve y = f(x) when x = 0.5 and draw the tangent on the graph in part (c). (3 marks)

$$y = \frac{9x}{2} + \frac{81}{16}$$
$$= 4.5x + 5.0625$$

End of questions

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230(1.0232)' = 1000 = 1 = 64.2 days

(c) If no measures were laken to control the spread of cowpea aphilds, after how many days will more than 1000m² of the crop be infeated? (1 mark)

. We will be graph of the graph of the graph of the graph of the season in the season (d) and (e) we will be season to the season of the seas

V=230(1,0232)<sup>4</sup>

(ii) a formula for A in terms of 1, the number of days since observations be (iii) (

Growth rate is 2.32% per day.

r³ = 270 ÷ 230 ⇒ r = 1 0232

(i) the daily percentage growth rate, rounded to two decimal places.

(a) Assuming that the area infested is increasing exponentially, determine

The initial area of a fupin crop, A, in aquare metres, infeated by cowpee aphids was 230 m $^2$ . One week later the area infeated had increased to 270 m $^2$ .

8t noiteauD METHODS UNITS 1 AND 2 CALCULATOR-ASSUMED

V<sub>ess</sub> = 6750 cm<sup>3</sup> when box is 30 by 30 by 7.5 cm

Using calculus techniques, determine the dimensions of the open box that has the marks) maximum possible volume and state what this volume is. (4 marks)

(b) Show that the volume of the open box is given by  $V = 4x^2 - 180x^2 + 3025x$  cm<sup>3</sup>. (2 marks) Width of box is width of sheet (45 cm) less two corners (2x).

w = 45 - 2(7.5) = 30 $\overline{S}2542$ ,  $Z_1 = X = X = 2025 + 2081 - <math>Z_2 = 0$  $|\xi | = |x | = |x | = |x |$ 

> $=4x^{3} - 180x^{2} + 5025x$  $x(x_2 - \xi k)(x_2 - \xi k) =$ HA(7 = A

> > .x2-24=w y/hw nielqx3 (e)

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See next page

 $0 = S + (I - x + ) \xi$  (ii)

 $.\overline{S}VA = xS8$  (i)

(b) Determine the value of n if  $\frac{1}{\sqrt[4]{\chi}} = x^n$ .

evios (a)

(5 шацка)

(5 marks)

(2 marks)

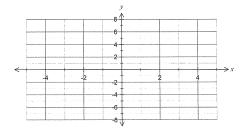
Question 4

6

CALCULATOR-FREE

(a) Sketch the graph of  $y = 0.5(x-2)^3 - 1$ .

(8 marks) (3 marks)



(b) Expand (3x-1)(3x+1)(x+3). (2 marks)

(c) Solve  $x^3 + 6x^2 + 5x - 12 = 0$ . (3 marks)

See next page

CALCULATOR-ASSUMED 11 METHODS UNITS 1 AND 2 Question 16 (8 marks) The events A and B have the properties  $P(A) = \frac{1}{6}$  and  $P(A \cup B) = \frac{1}{4}$ .

(a) Determine P(B) in each of these cases:

(i) If A and B are mutually exclusive. (1 mark)

 $P(B) = \frac{1}{2} - \frac{3}{8}$   $= \frac{1}{8}$ 

(ii) If  $P(A \cap B) = \frac{3}{40}$ . (2 marks)

$$\begin{split} P(A \cup B) &= P(A) + P(B) - P(A \cap B) \\ \frac{1}{2} &= \frac{3}{8} + P(B) - \frac{3}{40} \\ P(B) &= \frac{32 \cdot 14 \cdot 2}{40} \\ &= \frac{3}{60} \\ &= \frac{1}{2} \end{split}$$

(iii) If  $P(B|A) = \frac{1}{6}$ . (3 marks)

 $P(B \cap \overline{A}) = \frac{1}{8}$  x = P(B)  $P(A \cap B) = x - \frac{1}{6}$   $P(B \mid A) = \left(x - \frac{1}{8}\right) + \frac{3}{8}$   $\frac{1}{6} \times \frac{3}{6} = x - \frac{1}{6}$   $x = P(B) = \frac{3}{16}$ 

(b) For the case where P(A ∩ B) = <sup>3</sup>/<sub>66</sub>, are A and B independent? Justify your answer.

Yes, as  $P(A) \times P(B) = P(A \cap B)$  $\frac{3}{6} \times \frac{1}{5} = \frac{3}{40}$  METHODS UNITS 1 AND 2

Cascillot 17

(In marks)

(a) The value of an investment, 5 y , after n whole years in an account paying 2 % simple interest each year, is given by V = 2520 + 250(n - 1).

(i) What was the initial value of the investment? (1 mark) \$5000

(ii) After how many years did the value of the investment reach \$6500? (1 mark)

6 years

(iii) Determine the simple interest rate. (1 mark)



(b) An arithmetic sequence has an 9th term of 267 and a 14th term of 237.

The sequence is defined by the rule T<sub>n</sub> = a + (n − 1)d. Determine the values of a and d.
 (2 marks)

 $d = \frac{237 - 267}{14 - 9} = -6$  a = 267 - 8(-6) = 315

(ii) Write a recursive rule for this sequence. (2 mark  $T_{n+1} = T_n - 6, \quad T_1 = 315$ 

(iii) Calculate  $T_{20}$ . (1 mark  $T_{30}=23$ 

(iv) If  $T_1 + T_2 + ... + T_n = 0$ , determine the value of n. (2 marks)

 $\frac{n}{2}(2a - 6(n - 1)) = 0 \implies n = 0, n = 106$ Solution: n = 106

## CALCULATOR-FREE (7 marks) Question 5 (7 marks) Question 5 (7 marks) The graph of y = f(x) and a chord of the graph from (2.5, 7.5) to (5.5, 19.5) is shown below. The graph of y = f(x) and so the callo f(x+h) - f(x) to determine the gradient of the chord. Clearly state the values of x and h that you use. (2 marks)

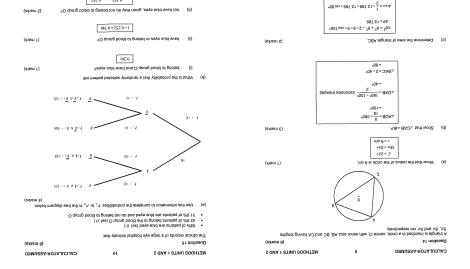
(c) Obsary describe what feature of the graph of  $\gamma=f(x)$  will be found by evaluating  $\lim_{h\to 0}\left(\frac{1}{h}\frac{1}{x}-\frac{1}{h}\frac{1}{h}\right) \inf_{x\to 0}\left(\frac{1}{h}\frac{1}{h}\frac{1}{h}\frac{1}{h}\frac{1}{h}\right)$ 

(b) As the value of h used in (a) decreases towards zero and the value of x remains on the same? Explain your contents of the same? Explain your

(S marks)

.(3.7, -8.5) finite axes above, draw the tangent to the graph of  $\chi$  to  $\chi$  at the point object them  $\chi$ ).

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 $\frac{0.319+0.252}{0.252} = \frac{0.571}{0.252}$ 

8

CALCULATOR-FREE

Question 6

(9 marks)

(a) Differentiate the following with respect to t:

(i)  $x = 1 + t - t^2$ .

(1 mark)

- (ii)  $v = \frac{t^2}{6} + \frac{4t^3}{9}$ . (1 mark)
- (b) State whether the graph of  $y=x^3-2x^2-3x-2$  is increasing, decreasing or stationary at the point (-1, 1). Justify your answer. (2 marks
- (c) The tangent to the curve y=f(x) at the point A is 13x+3y+14=0. If  $f'(x)=\frac{x^3}{2}-\frac{1}{3}$  find
  - (i) the coordinates of point A.

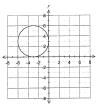
(3 marks)

See next page

 CALCULATOR-ASSUMED
 7
 METHODS UNITS 1 AND 2

 Question 12
 (7 marks)

 (a) Sketch the graph of  $(x + 3)^2 + (y - 3)^2 = 3^2$ .
 (3 marks)



(b) State two functions that combine to form the graph of  $(y-2)^2 = x+3$ . (2 marks)

 $y = 2 + \sqrt{x+3}$   $y = 2 - \sqrt{x+3}$ 

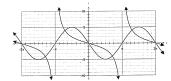
(c) Determine the coordinates of the points of intersection of the line y+16=7x and the circle given by x<sup>2</sup> + y<sup>2</sup> + 4x + 10y + 4 = 0. (2 marks)

Graph or solve simultaneously to get (1, -9) and (2, -2).

 METHODS UNITS 1 AND 2
 8
 CALCULATOR-ASSUMED

 Question 13
 (9 marks)

 The function f(x)=afan(fx) has been graphed below.



(a) Determine the values of the constants a and b. (3 marks)



(b) On the same axes, sketch the graph of  $y = Scos\left(x + \frac{\pi}{2}\right)$ . (3 marks)

(c) State the number of solutions to the equation  $Scos\left(x+\frac{x}{2}\right)=f(x)$  over the domain  $-x\leq x\leq x$ .

(d) Solve Scos $\left(x+\frac{x}{2}\right)=f(x)$ ,  $\pi < x < 2\pi$ , giving your answer(s) correct to three decimal places.

x=4.069 (2 marks)

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See next page

(S marks)

METHODS UNITS 1 AND 2

.(x)\( (ii)

CALCULATOR-FREE

 $\frac{2.2 \times 2 + 4}{8.0 - 1} \times 2 + 4 = 82 + 4$   $8.0 - 1 \times 2 + 4 = 82 \times 4$   $8.0 - 1 \times 2 + 4 = 82 \times 4$   $8.0 - 1 \times 2 + 4 = 82 \times 4$ (c) A sampte of six students who attended a science revision seminar is to be selected for a follow up survey. Determine how many different samptes can be selected. (1 mark) (e) Determine the total distance travelled by the ball until it ceases to bounce. (2 marks) 091 = 611+1<del>p</del> 808.7 × 2 + 4 = <sub>6</sub>2 × 2 + 4 m 818.91 = (E|N)9 (ii) (1 mark) (d) Determine the lotal distance travelled by the ball at the instant it hils the ground for the courth time. (Suem 1) So bounce 20 is the first less than 5cm.  $8720.0 = e_1 T$  $1810.0 = e_2 T$  (c) Determine which bounce is the first to have a height of less than 5 cm. Justify your snawer.  $\begin{array}{c} \mathcal{L}.\mathcal{E}=n \\ 8.0=\tau \end{array}$ (b) The height, in metres, reached by the bell effer the  $u^n$  bounce is given by the formula  $T_n=u^{n-1}$ . State the values of u and v. m 2 €=8.0×4 (a) Use this information to complete all regions of the Venn diagram below. .18 =  $(2 \cup M)n$  bins 0 + = (2)n , 8 = (M)n lief if inword is if (a) Determine the height reached by the ball after the first bounce. (sniem 8)

It notiseuce of the property of the Oue moltes of the most of most of the most of the most of the most of the pround below. The ball seconds vertically from a height of 4 meters onto the ground below of the height of the previous council. (5 marks) CALCULATOR-ASSUMED METHODS UNITS 1 AND 2 S GNA 1 STINU SGOHTEM 9 CALCULATOR-ASSUMED

(a) Determine the coefficient of the  $x^3$  term in the expansion of  $(3-2x)^5$ . (2 marks) (b) Solve  $\sin 2x = \frac{1}{2} \text{ for } 0 \le x \le 90$ . (2 marks) (c) Simplify  $\cos\left(\frac{\pi}{7}\right)\cos\left(\frac{\pi}{5}\right) + \sin\left(\frac{\pi}{7}\right)\sin\left(\frac{\pi}{5}\right)$ . (2 marks)

METHODS UNITS 1 AND 2

Question 7

CALCULATOR-FREE

(6 marks)

End of questions



### METHODS UNITS 1 AND 2

Section Two: Calculator-assumed (98 Marks) This section has thirteen (13) questions. Answer all questions. Write your answers in the spaces provided.

Working time for this section is 100 minutes.

(5 marks)

(s marks
The diagram below shows the path of a student who was walking on a level playing floth. The
student left O and walked for 40m to A, where they turned 40° to their right and then walked on
for another 35m to 5. Al 5, they turned another 40° to their right and walked 50m to C, where
they stopped.



Use trigonometry to show that when the student reached C, the straight line distance back to O was close to 90m.

$$OB = \sqrt{40^2 + 35^2 - 2(40)(35)\cos 140^9} = 70.498m$$

$$A\hat{B}O = \sin^{-1}\left(40 \times \frac{\sin 140^6}{70.498}\right) = 21.39^{\circ}$$

$$O\hat{B}C = 180 - 40 - 21.39 = 118.61^{\circ}$$

 $OC = \sqrt{70.498^2 + 30^2 - 2(70.498)(30)\cos 118.61^4} = 88.856 m$ 

CALCULATOR-ASSUMED METHODS UNITS 1 AND 2 Question 9 The pressure,  $\,P_{\,\circ}$  in an air bubble varies inversely with the volume,  $\,V_{\,\circ}$  of the bubble. It is known that P = 2.4 kPa when  $V = 5 \text{ cm}^3$ .

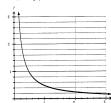
(a) Find the value of the constant k in the equation  $P = \frac{k}{k^2}$ . (1 mark)

 $2.4 = \frac{k}{5}$  $2.4 \times 5 = k$ k = 12

(b) Determine

(i) the value of 
$$P$$
 when  $V=2.5$  cm $^3$ . (1 mark) 
$$P=\frac{12}{2.5}$$
 
$$=4.6$$
 k/Pa

(c) On the axes below, draw a graph to show how P varies with V . (3 marks)



### Christ Church Grammar School

**NATHEMATICS** 

### WA Exams Practice Paper B, 2015

Question/Answer Booklet

	Your name		-
	ln words		-
Student Number:	sənugii ul		
Section Two: Calculator-assumed			_
METHODS NUITS 1 AND 2		If required by your examination administrator, place your student Identification label in this b	

				\$ minutes			Time allowed for this s Reading time before commend Working time for this section:
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-			 	 	 vords	w uj	
	T	l	Γ		figures	uj	Student Number:

### Materials required/recommended for this section To be worked by the supervisor This Cuestion/harwer Booklet Formula Sheet (retained from Section One)

To be provided by the candidate Standard items: pens (blueblack preferred), pensils (including coloured), sharpener, correction fluid/spe, eraser, ruler, highlighters

Special items: a drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations and up to three calculators approved for use in the WACE examinations.

### Important note to candidates

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End of questions

(S marks)

METHODS UNITS 1 AND 2

 $c = 4 - 2 - \frac{3}{2}$ 

CALCULATOR-FREE

 $4 = \frac{C-1}{8} - \frac{1}{3} + c$ 

 $\left(\frac{x}{\xi} - \frac{x}{\xi}\right) \cos \left(\frac{x}{\xi}\right) \sin \left(\frac{x}{\xi}\right) \sin \left(\frac{x}{\xi}\right) \cos \left(\frac{x}{\xi}\right) \cos \left(\frac{x}{\xi}\right) \cos \left(\frac{x}{\xi}\right) \cos \left(\frac{x}{\xi}\right) \sin \left(\frac{$ 

(c) Simplify  $\cos(\frac{\pi}{2})\cos(\frac{\pi}{2}) + \sin(\frac{\pi}{2})\sin(\frac{\pi}{2})$ .

.09  $\ge x \ge 0$  10f  $\frac{1}{5} = x^{\frac{\alpha}{2}}$  nis evio? (d)

METHODS UNITS 1 AND 2

021 ,05 = x5 °27 ,°21 = x

+ 10×9×(-8)x<sup>2</sup> + ...

 $x + \frac{1}{4}(x\Delta - 1)^{\frac{\alpha}{4}}(\xi)\begin{pmatrix} \xi \\ \xi \end{pmatrix} + \frac{1}{4}$ (a) Determine the coefficient of the  $x^3$  term in the expansion of  $(3-2x)^3$ .

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CALCULATOR-FREE

### CALCULATOR-ASSUMED

### Structure of this paper

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    Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- The Formula Sheet is not to be handed in with your Question/Answer Booklet.

See next page

### CALCULATOR-FREE METHODS UNITS 1 AND 2

The graph of y = f(x) and a chord of the graph from (2.5, 7.5) to (5.5, 19.5) is shown below.



(a) Use the ratio  $\frac{f(x+h)-f(x)}{h}$  to determine the gradient of the chord. Clearly state the values of x and h that you use. (2 marks)

$$x=2.5$$

$$h=3$$

$$\frac{f(2.5+3)-f(2.5)}{3} = \frac{19.5-7.5}{3} = 4$$

(b) As the value of h used in (a) decreases towards zero and the value of x remains unchanged, will  $\frac{f(x+h)-f(x)}{h}$  increase, decrease or stay the same? Explain your

(c) Clearly describe what feature of the graph of y = f(x) will be found by evaluating  $\lim_{k \to 0} \left( \frac{f(x+h) - f(x)}{h} \right) \text{ when } x = 4.$ 

The gradient (or derivative) of 
$$y = f(x)$$
 at the point where  $x = 4$ .

(d) On the axes above, draw the tangent to the graph of y = f(x) at the point (2.5, 7.5).

METHODS UNITS 1 AND 2 8 CALCULATOR-FREE
Question 6 (9 marks)
(a) Differentiate the following with respect to 
$$r$$
:

(b)  $x = 1 + r - r^2$ , (1 mark)
$$\frac{dr}{dr} = 1 - 2r$$
(i)  $v = \frac{r^2}{6} + \frac{4r^2}{9}$ . (1 mark)

(b) State whether the graph of  $y = x^3 - 2x^2 - 3x - 2$  is increasing, decreasing or stationary at the point (-1, 1). Justify your answer.

$$\begin{aligned} \frac{dy}{dx} &= 3x^2 - 4x - 3\Big|_{x=-1} \\ &= 3 + 4 - 3 \\ &= 4 \end{aligned}$$
 Graph is increasing as has a +ve gradient.

(c) The tangent to the curve y = f(x) at the point A is 13x + 3y + 14 = 0

If 
$$f'(x) = \frac{x^3}{2} - \frac{1}{3}$$
 find

(i) the coordinates of point A. (3 marks)

Gradient of tangent is 
$$-\frac{13}{3}$$
.

$$\frac{x^3}{2} - \frac{1}{3} = -\frac{13}{3}$$

$$\frac{x^3}{3} - \frac{2}{3} = -26$$

$$x^3 = -8 \Rightarrow x = -2$$

$$13(-2) + 3y + 14 = 0$$

$$3y = 12 \Rightarrow y = 4$$

$$A(\cdot 2, 4)$$

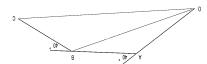
### CELCULATOR-ASSUMED 3 METHODS UNITS 1 AND 2 Section Two: Calculator-assumed (98 Marks)

This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 100 minutes.

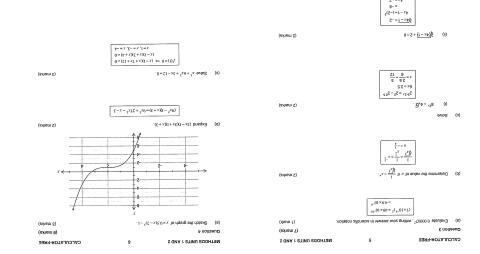
Question 8

The diagram below shows the path of a student who was walking on a level playing field. The student while Bf O and walked for 40m to A, where they turned 40° to their right and then walked on to another 55m to E.At B, they turned another 40° to their right and walked 50° to they turned snother 40° to their right and walked 30m to C, where



Use trigonometry to show that when the student reached C, the straight line distance back to O was close to 90m.

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4

CALCULATOR-ASSUMED

Question 9

(6 marks)

The pressure,  $\it{P}$  , in an air bubble varies inversely with the volume,  $\it{V}$  , of the bubble.

It is known that P = 2.4 kPa when  $V = 5 \text{ cm}^3$ .

(a) Find the value of the constant k in the equation  $P = \frac{k}{V}$ .

(1 mark)

(b) Determine

(i) the value of P when V = 2.5 cm<sup>3</sup>.

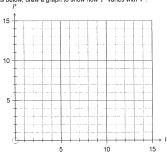
(1 mark)

(ii) the value of V when P = 10 kPa.

(1 mark)

(3 marks)

(c) On the axes below, draw a graph to show how P varies with V .



See next page

### SOLUTIONS

x = 2

(0, -5), (-1, 0) and (5, 0)

CALCULATOR-FREE	3	METHODS UNITS 1 AND 2	METHO	OS UNITS 1 AND 2	4	CALCULATOR-FREE
Section One: Calculator-free		(52 Marks)	Question			(7 marks
This section has seven (7) questions, provided.  Working time for this section is 50 minutes.		your answers in the spaces	(a) Do	etermine the coordinates of	the midpoint of A(-12, 3)	and B(8, -9). (1 mark
Question 1 A quadratic function is given by f(x)=		(8 marks)		e the straight lines given be		75x+1.25 parallel, perpendicular or (2 marks
(a) The function can also be written and $c$ . $f(x) = (x-2)(x-2)$ $= x^2 - 4x - 5$ $b = -4, c = -5$ (b) Solve the equation $f(x) = 0$ . $x-2 = 3x$ $x = -1 \text{ or } x = 5$	_	c . Determine the values of b (2 marks) (2 marks)		Neither $3x + 4y = 12$ $4y = -3x + 12$ $y = -0.75x + 3$ Gradients are not the s	ame (-0.75 and 0.75) so i a product of -1 (~0.75×0	
(c) For the graph of $y = f(x)$ , state				etermine the equation of the		for to the line $y = 8 - \frac{1}{3}x$ and (2 marks)
(i) the coordinates of the tu		(1 mark)		Required gradient $-\frac{1}{3}$ : 1=3(2)+c	× m = -1 ::> m = 3.	
(ii) the equation of the line of	of symmetry.	(1 mark)		c = -5 $y = 3x - 5$		

See next page See next page

(2 marks)

(d) Solve  $2(3x-2)=\frac{2x+11}{2}$ ,  $\begin{cases} 4(3x-2)=2x+11\\ 12x-8+2x+11\\ 10x=9\\ x=1.9 \end{cases}$ 

(2 marks)

bounce. (2 marks)	ball until it ceases to	stance travelled by the	Determine the total dis	(ə)
effine ground for the (2)	ind il at the instant if hi	atance travelled by the	Determine the total dis	(p)
cm. Justify your (2 marks)	ð neight of less than 8	everl of first to have	Determine which boun	(c)
iven by the formula	g si eonnod <sup>n</sup> n bounce is g		The height, in metres, $T_n = \omega_n^{n-1}. \mbox{ State the value}$	(q)
	gied ent fo %08 si eon	the height of each bou	offon 10 mail ball is dropped vertics bunds upwards such that i nce. Determine the height n	is A der
S GNA 1 STINU SGOH	Tam	9	CULATOR-ASSUMED	CAI

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6

CALCULATOR-ASSUMED

Question 11

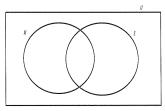
Two subsets, M and S, belong to a universal set of 200 students. Students belonging to subset M have attended a math revision seminar and students belonging to subset S have attended a science revision seminar.

It is known that n(M) = 58, n(S) = 40 and  $n(M \cup S) = 81$ .

(a) Use this information to complete all regions of the Venn diagram below.



(5 marks)



(b) If a student is selected at random from the group, determine

(i) 
$$P(\overline{M} \cup S)$$

(1 mark)

(ii) 
$$P(\overline{M} \mid \overline{S})$$

(1 mark)

(c) A sample of six students who attended a science revision seminar is to be selected for a follow up survey. Determine how many different samples can be selected. (1 mark

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CALCULATOR-ASSUMED

15

METHODS UNITS 1 AND 2

Question 20

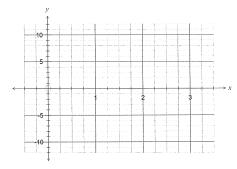
(10 marks)

A function is given by  $f(x) = 1 + 24x - 30x^2 + 16x^3 - 3x^4$ .

(a) Use calculus techniques to determine the coordinates of all stationary points of the function. (3 marks)

(b) Sketch the graph of y = f(x) for  $0 \le x \le 3$  on the axes below.

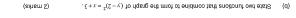
(4 marks)



(c) Determine the equation of the tangent to the curve y = f(x) when x = 0.5 and draw the tangent on the graph in part (c). (3 marks)

End of questions

### CALCULATOR-ASSUMED 7 METHODS UNITS 1 AND 2 (3 marks) (3 marks) (3 marks) (4) $\frac{1}{2}$ (5 marks) (5) $\frac{1}{2}$ (7 marks) (6) Sketch the graph of $(x+3)^2+(y-3)^2=3^2$ .

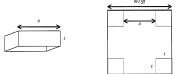


(c) Determine the coordinates of the points of intersection of the line  $\ y+16=7x \$ and the circle given by  $\ x^2+y^2+4x+10y+4=0.$ 

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WETHODS UNITS 1 AND 2 14 CALCULATOR-ASSUMED

Question 19 A square sheet of metal has sides of length 45 cm. An open box, with a square base of side  $\rm w$  cm, sh made by cutting squares with sides of  $\rm x$  cm out of the comers of the metal sheet and folding up the sides.



(a) Explain why  $\mathbb{A} = \mathcal{L} X - \mathcal{L} X$  (b) Explain why  $\mathbb{A} = \mathbb{A} X - \mathbb{A} X$ 

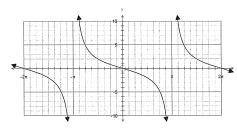
(b) Show that the volume of the open box is given by  $V=4x^3-180x^2+2025x$  cm³. (2 marks)

(c) Using calculus fechiniques, determine the dimensions of the open box that has the maximum possible volume and state what this volume is. (4 marks)

METHODS UNITS 1 AND 2 8 CALCULATOR-ASSUMED

Question 13 (9 marks)

The function  $f(x) = a \tan(bx)$  has been graphed below.



(3 marks)

(a) Determine the values of the constants a and b.

(b) On the same axes, sketch the graph of  $y = 5\cos\left(x + \frac{\pi}{2}\right)$ . (3 marks)

(c) State the number of solutions to the equation  $5\cos\left(x+\frac{\pi}{2}\right)=f(x)$  over the domain  $-\pi \le x \le \pi$ . (1 mark)

(d) Solve  $S\cos\left(x+\frac{\epsilon}{2}\right)=f(x)$ ,  $\pi< x<2\pi$ , giving your answer(s) correct to three decimal places. (2 marks)

See next page

CALCULATOR-ASSUMED 13 METHODS UNITS 1 AND 2

Question 18 (8 marks)

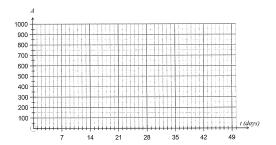
The initial area of a lupin crop, A, in square metres, infested by cowpea aphids was 230 m $^2$ . One week later the area infested had increased to 270 m $^2$ .

(a) Assuming that the area infested is increasing exponentially, determine

(i) the daily percentage growth rate, rounded to two decimal places. (2 marks)

(ii) a formula for A in terms of I, the number of days since observations began.

(b) Sketch the graph of the area infected against time for the first 7 weeks on the axes below.



(c) If no measures were taken to control the spread of cowpea aphids, after how many days will more than 1000m² of the crop be infested? (1 mark)

# CALCULATOR-ASSUMED 6 METHODS UNITS 1 AND 2 Question 14 (6 marks) A triangle is inscribed in a circle, centre O, with minor arcs AB, BC and CA having lengths $5\pi$ , $5\pi$ and $5\pi$ cm respectively. (a) Show that the radius of the circle is 9 cm. (1 mark) (b) Show that $\angle CAB = 80^\circ$ . (3 marks)

See next page

(2 marks)

(c) Determine the area of triangle ABC.

(ii) Determine the simple inferest rate. (1)

An arithmetic sequence has an 9th tem of 267 and a 14th tem of 237.

(iii) Determine the simple inferest rate. (1)

The sequence has an 9th tem of 267 and a 14th tem of 237.

(i) The sequence is defined by the rule  $T_n = a + (n - 1) d$ . Determine the values of a and d.

(ii) White a recursive rule for this sequence. (2 marks)

(iii) Calculate  $T_{50}$ . (1 marks)

(iii) Calculate  $T_{50}$ .

(i) What was the initial value of the investment?

METHODS UNITS 1 AND 2

(a) The value of an investment, \$V , after n whole years in an account paying R% simple interest each year, is given by V=5250+250(n-1).

15

(10 marks)

CALCULATOR-ASSUMED

CALCULATOR-ASSUMED

Question 15

(8 marks)

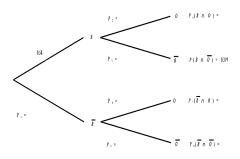
The clinical records of a large eye hospital indicate that

58% of patients are blue eyed (set B)
42.9% of patients belong to the blood group O (set O)

31.9% of patients are blue eyed and do not belong to blood group O

(a) Use this information to complete the probabilities  $P_1$  to  $P_8$  in the tree diagram below.

(4 marks)



(b) What is the probability that a randomly selected patient will

(i) belong to blood group O and have blue eyes?

(1 mark)

(ii) have blue eyes or belong to blood group O?

(1 mark)

(2 marks)

(iii) not have blue eyes, given they do not belong to blood group O?

See next page

METHODS UNITS 1 AND 2 CALCULATOR-ASSUMED 11 (8 marks) Question 16 The events A and B have the properties  $P(A) = \frac{3}{8}$  and  $P(A \cup B) = \frac{1}{2}$ .

(a) Determine P(B) in each of these cases:

(i) If A and B are mutually exclusive. (1 mark)

(2 marks) (ii) If  $P(A \cap B) = \frac{3}{40}$ .

(3 marks) (iii) If  $P(B | A) = \frac{1}{6}$ .

(b) For the case where  $P(A \cap B) = \frac{3}{40}$ , are A and B independent? Justify your answer. (2 marks)