

# Semester One Examination, 2023

Question/Answer booklet

# E TINU MATHEMATICS METHODS

Section One:

ılculator-free

	Time allowed for Reading time before Working time:
е дяше:	Your Teacher's
	Your Name:

## Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

#### To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items:

### Important note to candidates

you do not have any unauthorised material. If you have any unauthorised material with you, No other items may be taken into the examination room. It is your responsibility to ensure that

hand it to the supervisor before reading any further.

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Max	Marks	Question	Max	Marks	Question

2

#### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	6	6	50	51	36
Section Two: Calculator- assumed	10	10	100	90	64
				Total	100

#### Instructions to candidates

- 1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

CALCULATOR-FREE 3 MATHEMATICS METHODS
Section One: Calculator-free (51 marks)
This section has six questions. Answer all questions. Write your answers in the spaces provided.
Spare pages are included at the end of this booklet. They can be used for planning your

Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

responses and/or as additional space if required to continue an answer.

Working time: 50 minutes.

(S marks)

Question 2 (6 marks)

- (a) Determine:
  - (i)  $\int 3 + \cos(3 2x) dx$

(1 mark)

(ii)  $\int_{3}^{4} \left( (2x-5)^{-2} \right) dx$ 

(3 marks)

(b) (i) Determine the derivative of  $y=e^{3x}(3x+5)$ . Simplify your answer.

(2 marks)

(S marks)	Complete the table showing the possible outcomes and the probability.	(a)

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(3 warks)

A student pays \$5 to play the game

(b) Find the value of x if the expected return on the game is \$0.

(c) Is the selection of a counter a Bernoulli trail? Justify your answer.

#### Question 3 (continued)

The random variable W is a Bernoulli distribution that models the situation from (a).

(d) Given that Var(W) = 0.16, determine the probability of success and use the information in part (a) to what outcome is therefore considered to be a success. (2 marks)

The counter selected is returned to the bag, then the bag is shaken before the next student selects a counter. A student is interested in whether they win \$15 or not. They pay to play 10 rames

Let *Y* be the number of times the student wins \$15.

(e) State the distribution that would be used to determine the probability of Y.

(2 marks)

(f) The student performs the calculations given. Determine the number of times the student wins \$15 in each of the following:

(i) 
$$\binom{10}{2} \left(\frac{1}{10}\right)^2 \left(\frac{9}{10}\right)^8$$
 (1 mark)

(ii) 
$$\left(\frac{9}{10}\right)^{10}$$
 (1 mark)

(iii) 
$$\binom{10}{4} \left(\frac{1}{10}\right)^4 \left(\frac{9}{10}\right)^6 + \binom{10}{5} \left(\frac{1}{10}\right)^5 \left(\frac{9}{10}\right)^5$$
 (1 mark)

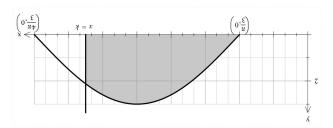
(iv) 
$$1 - \left(\frac{9}{10}\right)^{10}$$
 (1 mark)

#### Additional working space

Question number: \_\_\_\_\_

Question 6 marks)

The region bounded by the x-axis and the graph of  $y=\sin\left(x-\frac{\pi}{3}\right)$ ,  $0\le x\le \pi$  shown below is divided into two regions by the line x=k.



If the area of the region for  $\frac{\pi}{3} \le x \le k$  is 3 times the size of the area of the region for  $k \le x \le \frac{4\pi}{3}$  , determine k.

(e warks)

See next page

CALCULATOR-FREE

Question 4

(9 marks)

The function f(x) is defined for x>1.5, has derivative  $f'(x)=\frac{8}{(2x-3)^2}$ , and passes through the point (4,1).

(a) Determine the rate of change of f'(x) when x=3.

(3 marks)

(b) Determine f(x).

(4 marks)

(c) Determine  $\frac{d}{dt} \int_{t}^{3} (f'(x) - 4x) dx$ .

(2 marks)

- The probability function for the random variable X is  $P(X=x) = \begin{bmatrix} k^2 k + x \,, & x = 0 \\ 5 \, k^2 \, x \,, & x = 1 \\ 0 \,, & \text{otherwise.} \end{bmatrix}$
- (a) Determine the value of the constant k.

(4 marks)

(8 marks)

(b) Determine the mean and variance of X. (2 marks)

(c) The random variable Y = 3X + 1. Determine the mean and variance of Y. (2 marks)