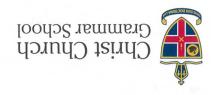
TEST 3 2019



Section One: MATHEMATICS METHODS Year 12

Teacher's name
Your name

Working time for this section: 15 minutes Reading time before commencing work: 2 minutes Time and marks available for this section

15 marks Marks available:

Formula Sheet This Question/Answer Booklet To be provided by the supervisor Materials required/recommended for this section

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

Special items: nil

Calculator-free

Important note to candidates

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> MATHEMATICS METHODS Year 12 CALCULATOR-ASSUMED

Additional working space

Question number:

2

CALCULATOR-FREE

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MATHEMATICS METHODS Year 12

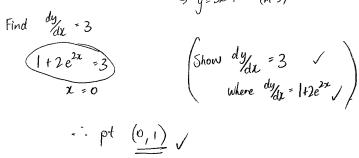
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CALCULATOR-ASSUMED

Question 9

(3 marks)

Find the coordinates of the point(s) on the curve $y = x + e^{2x}$ where the tangent to the curve at these point(s) are parallel to 3x - y = 1.



Question 10

(3 marks)

A bush fire near Walpole at time t hours is spreading at a rate of $2.1e^{2t-6} m^2/hour$.

(a) What area is burnt out in the first 9 hours?

(1 mark)

$$\int_{0}^{9} 2 \cdot 1 e^{2t-6} dt = 170 \ 8.92.53 \ m^{2} \ /$$

(b) What area is burnt out during the 11th hour?

(1 mark)

$$\int_{10}^{11} 2.1e^{2t-6} dt = 8.067.681.55 m^2 /$$

(c) Explain why this function is an unrealistic model for t > 11.

(1 mark)

End of questions



(1 mark)		$xp_{\varepsilon+x_L} \partial \int$ (e)
		Determine the following.
(7 marks)		Question 1
MATHEMATICS METHODS Year 12	3	CALCULATOR-FREE

(S marks)
$$\frac{a}{\sqrt{x}} \left(x^2 e^{x^2}\right)$$

(4 marks) CALCULATOR-ASSUMED MATHEMATICS METHODS Year 12

is $\frac{2}{\pi}$ and is independent of each other. Let x represent the number of times the car must are two school crosswalks. The probability that they will have to stop at each crosswalk The Kappa family live one kilometre from their school. On the route they drive to school

Question 8

(S marks) (a) Complete the following probability distribution table for this random variable.

91.0 = 5/2 × 5/2 : NN

most once on their way to school on exactly three of the five days. (b) After five weekdays, what is the probability that the Kappa family have to stop at

$$\sqrt{Lbss.0} = \sqrt{9s.0} = (1=x)d$$

zee next page

4

CALCULATOR-FREE

Question 1 continued

Evaluate the following.

(c)
$$\int_0^2 3(x + e^{3x}) dx$$

(2 marks)

(d) $\int_0^{\frac{\pi}{2}} \frac{d}{du} \sin(u) du$

(2 marks)

See next page

MATHEMATICS METHODS Year 12

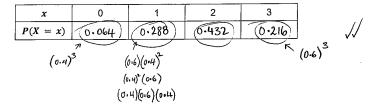
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CALCULATOR-ASSUMED

Question 7

(5 marks)

(a) A coin is biased in favour of heads such that the probability of obtaining a head on any single toss is 0.6. The coin is tossed three times and the result noted. If X is the number of heads obtained on the three tosses, find E(X), the expected value of X by first completing the table below: (3 marks)



$$E(x) = 0.288 + 2(0.432) + 3(0.216)$$

$$E(x) = 1.8$$

b) For the random variable X defined above, find:

$$E(3X+1)$$

$$E(3X+1) = 3(1.8) + 1$$

$$= (6.4) \qquad (Value)$$

CALCULATOR-FREE

Question 2 (3 marks)

S

For a \$5 monthly fee, a TV repair company guarantees customers a complete service. The company estimates the probability that a customer will require one service call in a month is 0.05, the probability of 2 calls is 0.01 and the probability of 3 or more calls is 0.00. Each call costs the repair company \$40.

(J wark)

(a) Complete the table below.

00.0		90.0		P(G = 9)
	9 Z -			(g) nisə
5≤	. 2	ı	0	Calls

(b) What is the TV repair company's expected monthly gain from such a contract?

See next page

MATHEMATICS METHODS Year 12 5 CALCULATOR-ASSUMED

Question 6 marks)

The population in a certain country is growing continuously at 3% per annum. Its population P is such that $P=P_0 e^{kt}$ where P is the population in millions, t years from now. The population is currently 35 million.

(a) When will the population of the country reach 50 million if it continues to grow at the same rate? (2 marks)

Data suggests that the capital city's population is growing at a faster rate than that of the country. Currently 22% of the people in the country live in the capital city, and if its population continues to grow at its present rate, 40% of the entire population will live in the capital city 15 years from now. What is the continuous growth rate of the population of the capital city?

| 15 years time => 35 e 15x0.03 | Where c is growth |
| 15 years time => 0.04 x 35 e 15x0.03 | Where c is growth rate |
| 15 years time => 0.04 x 35 e 15x0.03 |
| 15 years time => 0.04 x 35 e 15x0.03 |
| 16 years time => 0.04 x 35 e 15x0.03 |
| 17 years time => 0.05085

6

CALCULATOR-FREE

Question 3

(5 marks)

(a) Determine $\frac{dy}{dx}$ where $y = xe^{2x-1}$

(2 marks)

(b) Hence, determine $\int xe^{2x-1} dx$

(3 marks)

End of questions

MATHEMATICS METHODS Year 12

4

CALCULATOR-ASSUMED

Question 5

(6 marks)

The table shows the pdf of a discrete random variable; where $\mathcal{E}(X)$ is the expected value of X.

x	1	2	3	4	5
P(X = x)	0.2	р	0.3	q	0.1

(a) If $E(X^2) = 8.2$, determine p and q.

(3 marks)

, \

(2)
$$1^{2}(0.2) + 2^{2}(p) + 3^{2}(6.3) + 4^{2}(q) + 5^{2}(0.1) = 8.2$$

on $0.2 + 4p + 2.7 + 16q + 2.5 = 8.2$

q=0.1

(b) Calculate E(X).

(1 mark)

$$E(x) = 0.2 + 0.6 + 0.9 + 0.4 + 0.5$$

$$E(x) = 2.6$$

(c) If
$$Y = 1 - 2X$$
, calculate $E(Y)$.

(1 mark)

$$E(y) = 1 - 2(2.6)$$



Additional working space CALCULATOR-FREE

Question number:

CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 12

Question 4

(4 marks)

(5 marks)

random variable associated with this trial. randomly selected and it was noted whether he/she was a plumber. Define X as the Assume one in 300 Australian adults were plumbers. One Australian adult was

(a) Describe the distribution of X. Include its parameter.

X is Bernoulli, paranuler p = 300

(2 marks)

State the mean and variance of this distribution.

See next page

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Additional	working	space

Question number: _____

MATHEMATICS METHODS Year 12

2

CALCULATOR-ASSUMED

Instructions to candidates

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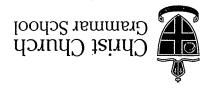
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CALCULATOR-FREE

Additional working space

Question number:

2019



TEST 3

Section Two: MATHEMATICS METHODS Year 12

Calculator-assumed

	u	rke available for this section
		Теасћег's пате
e	SOUTTIONS.	Your name

30 marks Marks available: 30 minutes Working time for this section: Reading time before commencing work: 3 minutes Time and marks available for this section

Formula Sheet (retained from Section One) This Question/Answer Booklet To be provided by the supervisor Materials required/recommended for this section

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, To be provided by the candidate

Special items: drawing instruments, templates, and up to three calculators approved

for use in the WACE examinations

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MATHEMATICS METHODS Year 12 Additional working space	10	CALCULATOR-FREE
Question number:		

CALCULATOR-FREE	7	MATHEMATICS METHODS Year 12
Additional working space		
Question number:		

TEST 3 2019



Section Two: MATHEMATICS METHODS Year 12

Your name

30 minutes Working time for this section: Reading time before commencing work: 3 minutes Time and marks available for this section

30 marks Marks available:

Formula Sheet (retained from Section One) This Question/Answer Booklet To be provided by the supervisor Materials required/recommended for this section

To be provided by the candidate

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MATHEMATICS METHODS Year 12

(2 marks)

Determine $\frac{dy}{dx}$ where y = x

Question 3

(s)

(5 marks).

$$\int_{-\infty}^{\infty} \frac{1-x \cdot \delta}{(x)} + \frac{1-x \cdot \delta}{(x)} = \frac{1-x \cdot \delta}{(x)} = \frac{1-x \cdot \delta}{(x)}$$

(3 marks)

Hence, determine $\int xe^{-xz} dx$

$$\frac{d}{dx} \frac{x}{x} \frac{2x-1}{6x} = \frac{2x-1}{2} + \frac{2x}{2} \frac{2x-1}{6x}$$

$$\frac{d}{dx} \frac{x}{x} \cdot \frac{2x-1}{6x} = \int_{0}^{2x-1} \frac{2x-1}{6x} + \int_{0}^{2x-1} \frac{2x-1}{6x} \cdot \frac{2x-1}{6x}$$

$$\frac{d}{dx} \frac{x}{x} \cdot \frac{2x-1}{6x} = \int_{0}^{2x-1} \frac{2x-1}{2} \cdot \frac{2x-1}{6x} \cdot \frac{2x-1}{6x}$$

 $\int \chi \cdot \int \chi \cdot e^{2x-1} d\chi = \frac{1}{2} \left(\chi \cdot e^{2x-1} - \frac{1}{2} e^{2x-1} - \frac{1}{2} e^{2x-1} \right) + C$ $\int \chi \cdot \int \chi \cdot e^{2x-1} d\chi = \frac{1}{2} e^{2x-1} - \frac{1}{4} e^{2x-1} + C$ $\int \chi \cdot \int \chi \cdot e^{2x-1} d\chi = \frac{1}{2} e^{2x-1} - \frac{1}{4} e^{2x-1} + C$ $\int \chi \cdot \int \chi \cdot e^{2x-1} d\chi = \frac{1}{2} e^{2x-1} - \frac{1}{4} e^{2x-1} + C$

End of questions

2

CALCULATOR-ASSUMED

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CALCULATOR-FREE

MATHEMATICS METHODS Year 12

Question 2

(3 marks)

For a \$5 monthly fee, a TV repair company guarantees customers a complete service. The company estimates the probability that a customer will require one service call in a month is 0.05, the probability of 2 calls is 0.01 and the probability of 3 or more calls is 0.00. Each call costs the repair company \$40. What is the TV repair company's expected monthly gain from such a contract?

Begin by filling out the table below.

Calls	0	1	2	≥3
Gain (g)	15	-35	-75	
P(G = g)	0.94	0.05	0.01	0.00

$$E(G) = 5(0.94) - 35(0.05) - 75(0.01)$$
= 4.70 - 1.75 - 0.75 (working)

(4 marks)		₽ noitsenD
CALCULATOR-ASSUMED	ε	MATHEMATICS METHODS Year 12

Assume one in 300 Australian adults were plumbers. One Australian adult was randomly selected and it was noted whether he/she was a plumber. Define X as the random variable associated with this trial.

See next page

WATHEMATICS METHODS Year 12 4 CALCULATOR-FREE

Question 1 continued

Evaluate the following.

(c)
$$\int_0^2 3(x+e^{3x}) dx$$

$$\int_{\zeta} \frac{1}{2} \frac{1}{2$$

$$0 \text{ wis} - \frac{1}{2} \text{ wis} = \frac{1}{2} \text{ and } \frac{1}{2} \text{ and } \frac{1}{2} \text{ wis} = \frac{1}{2} \text{ and } \frac{$$

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CALCULATOR-ASSUMED

Question 5

(6 marks)

The table shows the pdf of a discrete random variable, where E(X) is the expected value of X.

x	1	2	3	4	5	
P(X = x)	0.2	р	0.3	q	0.1	

(a) If $E(X^2) = 8.2$, determine p and q.

(3 marks)

(b) Calculate E(X).

(1 mark)

(c) If Y = 1 - 2X, calculate E(Y).

(2 marks)

CALCULATOR-FREE

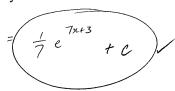
MATHEMATICS METHODS Year 12

Question 1

(7 marks)

Determine the following.

(a) $\int e^{7x+3} dx$



(1 mark)

(b) $\frac{d}{dx}(x^2 | e^{x^2})$ (2 marks)

3

$$= \frac{2 \pi e^{x^2} + \kappa^2 (2 \pi e^{x^2})}{\sqrt{}}$$

$$\frac{\partial R}{\partial x} \left(2x e^{x^2} (1+x^2) \right)$$

/3

CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 12

(2 marks)

2 duestion 6

The population of a certain country is growing continuously at 3% per annum. Its population P is such that $P=P_0 e^{kt}$ where P is the population in millions, t years from now. The population is currently 36 million.

(a) In how many years will the population of the country reach 50 million if it continues to grow at the same rate? (2 marks)

Data suggests that the capital city's population is growing at a faster rate than that of the country. Currently 22% of the people in the country live in the capital city, and if its population continues to grow at its present rate, 40% of the entire population will live in the capital city 15 years from now. What is the continuous growth rate of the population of the capital city?

(3 marks)

See next page

MATHEMATICS METHODS Year 12 Z CALCULATOR-FREE

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6

CALCULATOR-ASSUMED

Question 7

(5 marks)

(a) A coin is biased in favour of heads such that the probability of obtaining a head on any single toss is 0.6. The coin is tossed three times and the result noted. If X is the number of heads obtained on the three tosses, find E(X), the expected value of X by first completing the table below: (3 marks)

х	0	1	2	3
P(X = x)				

- (b) For the random variable *X* defined above, find:
 - (i) E(3X + 1)

(1 mark)

(ii) SD(3X + 1)

(1 mark)

See next page



2019 TEST 3

MATHEMATICS METHODS Year 12

Section One: Calculator-free

Your name	0	SOLUTIONS	6	
Teacher's name				

Time and marks available for this section

Reading time before commencing work: 2 minutes
Working time for this section: 15 minutes
Marks available: 15 marks

Materials required/recommended for this section

To be provided by the supervisor This Question/Answer Booklet Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

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CALCULATOR-ASSUMED

(4 marks)

MATHEMATICS METHODS Year 12

Question 8

The Kappa family live one kilometre from their school. On the route they drive to school are two school crosswalks. The probability that they will have to stop at each crosswalk is $\frac{1}{5}$ and is independent of each other. Let x represent the number of times the car must stop at a crosswalk.

(a) Complete the following probability distribution table for this random variable. (2 marks)

			(x = X)d
2	ı	0	x

(b) After five weekdays, what is the probability that the Kappa family have to stop at most once on their way to school on exactly three of the five days? (2 marks)

See next page

CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 12

Additional working space

Question number:

MATI	HEMATICS METHODS Year 12	8	CALCULATOR	-ASSUMED
Ques	stion 9			(3 marks)
Find 1 curve	the coordinates of the point(s) on the α at these point(s) are parallel to $3x-y$	Surve $y = x + e^{2x}$ where $y = 1$.	re the tangent	to the
	tion 10		24-21-6211-	(3 marks)
A bus	h fire near Walpole at time t hours is $\mathfrak s$		$2.1e^{2t-0} m^2/h$	
(a)	What area is burnt out in the first 9 h	ours?		(1 mark)
(b)	What area is burnt out during the 11	¹ hour?		(1 mark)
(c)	Explain why this function is an unrea	listic model for $t>11$		(1 mark)

End of questions

MATHEMATICS METHODS Year 12	9	CALCULATOR-ASSUMED
Additional working space		
Question number:		