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Question/Answer bookle
DS0S noitsnimax3
Semester Two

Insert School Logo

7	ል	ε	METHODS UNITS
			SOITAMENTAM

Section One: Calculator-free

Working time for paper:

səjnuim əvif	ime allowed for this section sading time before commencing work:
	Теасһег's Иате:
	Student Name:

Material required/recommended for this section

To be provided by the supervisor This Question/Answer booklet Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction tape/fluid, erasers, ruler, highlighters

Special Items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before

fifty minutes

before reading any further.

CALCULATOR-FREE 12 METHODS UNITS 3 & 4

Additional working space

Question number(s):

CALCULATOR-FREE 2 METHODS UNITS 3 & 4

Structure of this paper

	Number of questions available	Number of questions to be attempted	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	7	7	50	50	35
Section Two Calculator—assumed	15	15	100	100	65
				Total marks	100

Instructions to candidates

- 1. The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2020. Sitting this examination implies that you agree to abide by these rules.
- 2. Answer the questions according to the following instructions.

Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

It is recommended that you do not use pencil, except in diagrams.

- 3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the
 original answer space where the answer is continued, i.e. give the page number. Fill in the
 number of the question that you are continuing to answer at the top of the page.
- 5. The Formula Sheet is **not** handed in with your Question/Answer Booklet.

CALCULATOR-FREE 11 METHODS UNITS 3 & 4

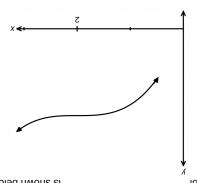
Additional wor	king	space
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Question number(s):

7 noitesuQ

(6 marks)

 $y = x^3 + ax^2 + bx + c$ is shown below. The graph of



0τ

A horizontal point of inflection occurs at (2, 8).

Determine the values of a, b and c.

(e warks)

32% (20 marks) Section One: Calculator-free

provided. This section has seven (7) questions. Attempt all questions. Write your answers in the spaces

and/or as additional space if required to continue an answer. Spare pages are included at the end of this booklet. They can be used for planning your responses

3

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- number of the question(s) that you are continuing to answer at the top of the page. original answer space where the answer is continued, i.e. give the page number. Fill in the Continuing an answer: If you need to use the space to continue an answer, indicate in the

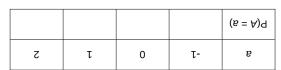
Working time: 50 minutes

Question 1 (7 marks)

Amounts are rounded appropriately, and given in thousands of dollars. A fledgling business recorded its profits, A, for ten consecutive weeks.

 $A = \{-1, 0, 1, -1, 0, 2, 1, 1, 0, 1\}$

(S marks) (a) Complete the probability distribution for A.



(b) Show that the mean amount for the ten week period is \$400. (S marks)

The variance of A is partially calculated below.

(3 marks) (c) Complete the calculation.

$$^{S}[(A)\exists]-(^{S}A)\exists = (A)AAV$$

9

Question 2 (7 marks)

A school has five administrative staff; one male and four females. One of the five is selected at random.

The random variable M represents the number of males selected.

The probability distribution of M is given, in part, below.

m	0	1
P(M = m)		

- (a) Complete the table. (2 marks)
- (b) Explain why M is said to be a Bernoulli variable. (1 mark)
- (c) Determine the mean and standard deviation of *M*. (2 marks)

The selection process is repeated eight times. Each selection is independent of the other selections, and is completely random.

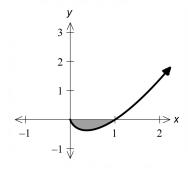
X is the total number of selections resulting in a male staff member. *X* is binomial.

- (d) State the parameters of X. (1 mark)
- (e) State an expression representing the probability of selecting the male staff member on three occasions. Do not attempt to evaluate that expression. (1 mark)

(b) The graph of $y = x \ln x$ is shown below. Determine the shaded area.

CALCULATOR-FREE

(4 marks)



(S marks)

(S marks)

(S marks)

Question 3

(a) Differentiate $(3x^2 + 5)^4$. Do not simplify.

(JJ wyrks)

(4 marks)

- (2 marks)

8

 $0 + \frac{(1 - xn)^2 x}{4} = xb xnl x$ $\int_{0}^{\infty} \frac{(1 - xn)^2 x}{4} + c$ (ii) Use your answer to (i) to show that

(b) A function, g_i is defined as $g(x) = e^{3x}\cos(2x)$. Determine the exact rate of change of g with respect to x at the instant that $x = \pi$. (3 marks)

g

(c) Determine in simplest form:

$$xb$$
 (x E)nis ∂ (i)

- $xb \frac{1+x2}{1+x+^2x}^2$ (ii)
- (d) Given that $\frac{dy}{dx} = 2e^{-5x}$, determine the expression for y if y(0) = -3. (S marks)

CALCULATOR-FREE 6 METHODS UNITS 3 & 4

Question 4 (6 marks)

You should be familiar with the 68 - 95 - 99.7 rule for normally distributed data values. Use those values to answer the following questions about normally distributed variable X, where X is the life span of mobile phone cameras. X has a mean of 7 years and a standard deviation of 1.5 years.

(a) Determine, with working, the expected range of such life spans.

(2 marks)

(b) Approximately what percentage of cameras have a life span less than 5.5 years? (2 marks)

(c) The smallest 2.5% of life spans qualify for replacement with a new phone for the owner.

What is the smallest life span that qualifies for a new phone? (2 marks)

CALCULATOR-FREE 7 METHODS UNITS 3 & 4

Question 5 (3 marks)

A 90% confidence interval has a width of 5, based on a sample size equal to n.

What sample size is required for a 90% confidence interval to have a width of 10?

(3 marks)