

Question	Mark	Max	Question	Mark	Max
4		8			
3		7			
2		6			
1		5			

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised material if you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to candidates

Special items: null

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters
To be provided by the candidate

Formula sheet

This Question/Answer booklet

To be provided by the supervisor

Materials required/recommended for this section

Working time: fifty minutes
 Reading time before commencing work: five minutes
 Working time: fifty minutes

Your Teacher's Name _____

Your Name _____

Calculator-free
 Section Done:

UNIT 3

MATHEMATICS SPECIALIST

Question/Answer booklet

Semester One Examination, 2022

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	14	14	100	97	65
Total					100

Instructions to candidates

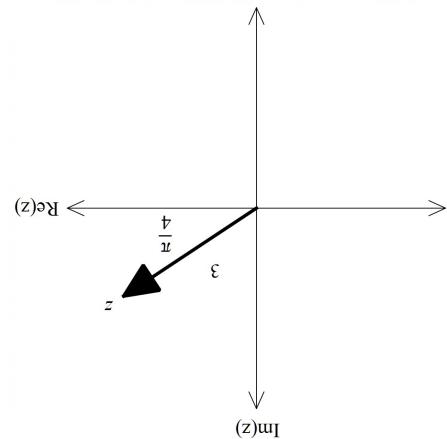
1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2016*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

(2 marks)

- b) Determine the exact value of $|z+i|$.

(2 marks)

- a) Determine the exact value of $Ai(y(i))$ and plot on the axes above.



Consider the complex number z as plotted on the complex plane below.

(4 marks)

Question 1

Working time: 50 minutes.

- Number of the question that you are continuing to answer at the top of the page.
 - Original answer space where the answer is continued, i.e. give the page number. Fill in the original answer space where the answer is continued, i.e. give the page number. Indicate in the original answer space where the answer is continued, i.e. give the page number.
 - Continuing an answer: If you need to use the space to continue an answer, indicate this clearly at the top of the page.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

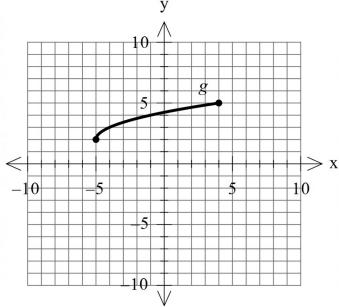
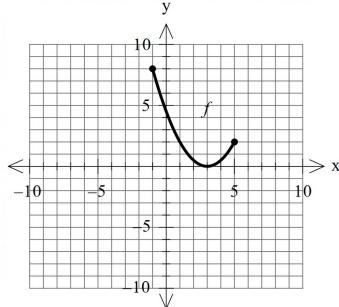
This section has eight (8) questions. Answer all questions. Write your answers in the spaces provided.

Section One: Calculator-free

(52 Marks)

Question 2**(8 marks)**

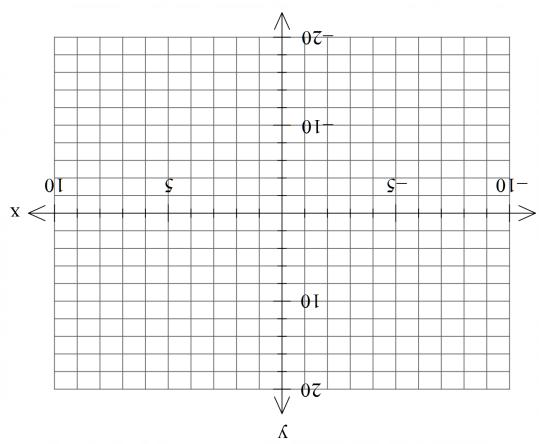
Consider the functions f & g with domains shown in the graphs below.



- a) Sketch the inverse functions above.
If they exist. (2 marks)

- b) Which of the following exist over natural domains, $f \circ g$, $g \circ f$? Explain.
State the natural domain and corresponding ranges for those that exist. (3 marks)

- c) The rule for g is $2 + \sqrt{x+5}$. State the inverse rule g^{-1} and its domain. (3 marks)



Consider the function

$$f(x) = \frac{(x+4)}{(x+3)(x-5)}$$

Plot on the axes below labelling intercepts and asymptotes.

(5 marks)

Question 3

Additional working space
 Question number:
 Additional working space

Question 4

(8 marks)

Consider the polynomial $P(z) = 3z^4 - 18z^3 - 3z^2 + 258z + 510$ for the complex variable z .

- a) Given that $P(5+3i)=0$, determine a quadratic factor of $P(z)$. (3 marks)

Question 8

(4 marks)

$$r_1 \begin{pmatrix} 1 \\ 1 \\ -2 \end{pmatrix} = 4$$

Consider two parallel planes Λ & Ψ . Plane Λ is given by (-2) and plane Ψ contains the point (p, q, r) .

$$\text{by } \left| \frac{p+q-2r-4}{\sqrt{6}} \right|$$

Show that the distance between the two planes is given by

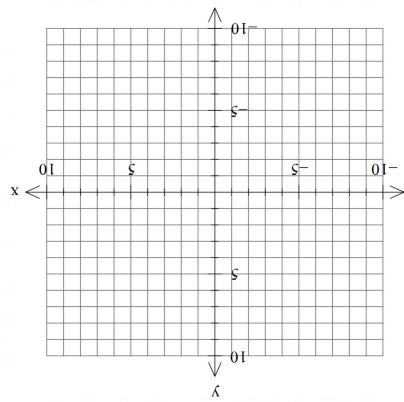
b) If $P(5+3i)=0=P(-2-i)$, determine all solutions to $3z^4 - 18z^3 - 3z^2 + 258z + 510 = 0$.
(2 marks)

c) $P(z)$ can be expressed as $a(z^2 + bz + c)(z^2 + dz + e)$ where a, b, c, d & e are real integers. Determine the values of a, b, c, d & e . (3 marks)

(3 marks)

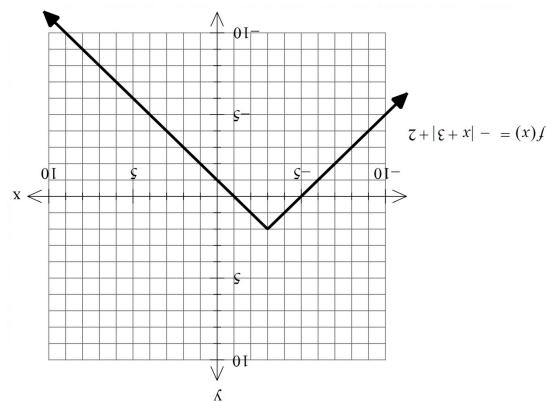
$$\frac{y}{1} = \frac{|x+3| - 6}{1}$$

b) Hence determine the natural domain and range of $y(x)$



(4 marks)

a) Sketch $y = \frac{f(x)}{1}$ on the axes below, labelling important features.



(7 marks)

Consider the function $f(x) = -|x+3| + 2$.

Question 5

(1 mark)

(3 marks)

d) Determine the exact coordinates, if any, where $f(x) = f_{-1}(x)$

c) Determine $f \circ f_{-1}(x)$

Q7 continued.

Question 6

$$3x + 2y + z = 9$$

$$x + 4y + 3z = 5$$

$$2x - 5y + 2z = 15$$

Consider the linear equations

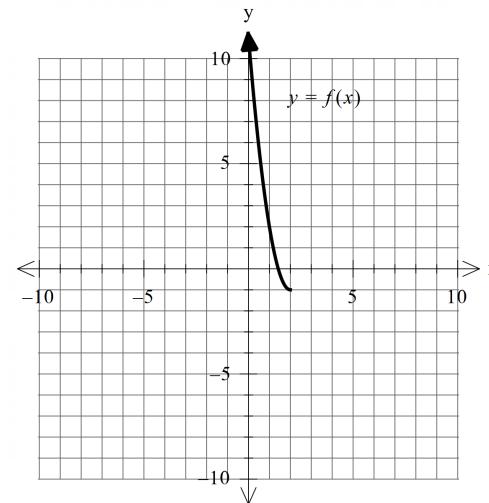
- a) Solve for $x, y \& z$.

(6 marks)

(3 marks)

Question 7**(10 marks)**

Consider the function $f(x) = 3x^2 - 12x + 11$ for $x \leq 2$ which is plotted below.



$$3x + 2y + z = 9$$

$$x + 4y + pz = 5$$

- b) Consider the following system $2x - 5y + 2z = q$ where $p \& q$ are constants. (3 marks)

Solve for all possible values of $p \& q$ for the following scenarios:

- i) Unique solution
- ii) Infinite solutions
- iii) No solutions.

- a) Sketch the inverse function $f^{-1}(x)$ on the axes above. (2 marks)

- b) Determine the rule for $f^{-1}(x)$ and state its domain. (4 marks)