

Rossmoyne Senior High School

Semester One Examination, 2021 Question/Answer booklet

SOLUTIONS

MATHEMATICS METHODS UNIT 1

Section One: Calculator-free

Time allowed for this section Reading time:	ork: five	sətunim sətunim	Number of additional answer booklets used (if applicable):	
Your nar	usme			
lu words	ords			
WA student number: In figure	nres			

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: r

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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METHODS UNIT 1 2 CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	54	35
Section Two: Calculator-assumed	13	13	100	95	65
				Total	100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

CALCULATOR-FREE	11	METHODS UNIT 1
CALCULATOR-FREE	11	METHODS ONLY

Supplementary page

Question number: _____

See next page SN085-172-7 SN085-172-7

32% (24 Marks) Section One: Calculator-free

This section has eight questions. Answer all questions. Write your answers in the spaces

Working time: 50 minutes.

(6 marks) L noitesup

Solve the following equations for x.

(2 marks)
$$(2 + x)(2 + x)$$

Specific behaviours 4 = x , 2.5 - x $2.2 - \frac{2}{2} - = x \leftarrow 0 = 2 + x2$ $4 = x \leftarrow 0 = 4 - x$

√ second correct solution √ first correct solution

 $\frac{t}{8-x_6} = \frac{z}{\xi + x_8} \qquad (q)$ (2 marks)

/ indicates correct method Specific behaviours z-=x1 - x = x8 - x6 = 9 + x91(8-x6)2 = $(\xi + x8)$ 4 Solution

√ correct solution

(2 marks) (c) $(x - 8)^2 - 100 = 0$.

See next page

Alternative Solution
$$0 = 001 - (8 - x)(8 - x)$$

$$0 = 00 - (8 - x)(8 - x)$$

$$0 = 0 - (2 + x)(8 - x)$$

$$0 = 0 - (2 + x)(8 - x)$$

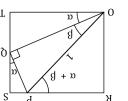
$$0 = 0 - (2 + x)(8 - x)$$
Specific behaviours
bothest sourcest method

✓ both correct solutions ✓ indicates correct method

Z-271-280NS

10

Consider rectangle ORST that (7 marks) **Question 8**



CALCULATOR-FREE

 $.\lambda + \beta = \alpha + \beta.$ $\Delta P = \beta$ and $\omega = 40$ S $\Delta = 10$ Δ Let the length of OP = 1, as shown.

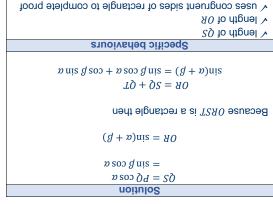
contains the right triangle 0PQ

METHODS UNIT 1

Explain why $QT = \sin \alpha \cos \beta$. (S marks)

Iluser and to obtain result \checkmark $\sqrt{}$ uses ΔOPQ for length of ∂Q Specific behaviours Hence, in triangle 0QT, $QT = 0Q \sin \alpha = \cos \beta \sin \alpha$. In triangle OPQ, $O\overline{Q} = \cos \beta$. Solution

(3 marks) identity $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$. Determine expressions for the lengths of QS and OR and hence prove the angle sum (q)



Use the identity from part (b) to show that $\sin\left(x + \frac{3\pi}{2}\right) = -\cos x$. (z marks)

√ clearly shows both known values and simplifies √ expands using identity Specific behaviours x soo - = $1 - \times x \cos + 0 \times x \text{ nis} =$ noinlos $\frac{\pi \xi}{2} \sin x \cos y + \frac{\pi \xi}{2} \cos x \sin x = \left(\frac{\pi \xi}{2} + x\right) \sin x$

End of questions Z-271-280NS

METHODS UNIT 1

CALCULATOR-FREE

Question 2 (7 marks)

The straight line *L* has equation 4x + 2y = 1.

(a) Write the equation of L in the form y = mx + c to show that its gradient is -2. (1 mark)

Solution
$2y = -4x + 1 \Rightarrow y = -2x + \frac{1}{2} \Rightarrow m = -2$
Specific behaviours
✓ correct values of m and c

Line L_1 is perpendicular to L and passes through the point (2,6).

Line L_2 is parallel to L and passes through the point (1, -7).

(b) Determine the point of intersection of L_1 and L_2 .

(6 marks)

Solution $L_1: (y-6) = \frac{1}{2}(x-2) \Rightarrow y = \frac{1}{2}x+5$ $L_2: (y-1) = -2(x-7) \Rightarrow y = -2x-5$ $\frac{1}{2}x+5 = -2x-5$ $(\frac{1}{2}+2)x = -10$ $\frac{5}{2}x = -10$ x = -4 $y = \frac{1}{2}(-4) + 5 = 3$

Lines intersect at (-4,3).

Specific behaviours

- ✓ gradient of L_1
- ✓ equation of L_1
- ✓ equation of L_2
- ✓ equates lines and groups like terms
- ✓ solves for x
- \checkmark solves for y and states point of intersection

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Question 7 (6 marks)

Two polynomial functions are defined by f(x) = (2x-3)(x+2) and $g(x) = x^3 + 4x^2 - 4x - 12$.

There is a point of intersection of f(x) and g(x) at (2,4). Find the coordinates of the other point(s) of intersection.

Solution

Expand f(x)

$$f(x) = (2x - 3)(x + 2)$$
$$= 2x^2 + x - 6$$

Equate functions:

$$x^3 + 4x^2 - 4x - 12 = 2x^2 + x - 6$$

Equate to zero:

$$x^3 + 2x^2 - 5x - 6 = 0$$

Find root:

From given point of intersection x = 2

Start factorising:

$$x^3 + 2x^2 - 5x - 6 = (x - 2)(x^2 + 4x + 3)$$

Complete factorising:

$$x^3 + 2x^2 - 5x - 6 = (x - 2)(x + 3)(x + 1)$$

Coordinates:

$$f(-1) = (-5)(1) = -5$$

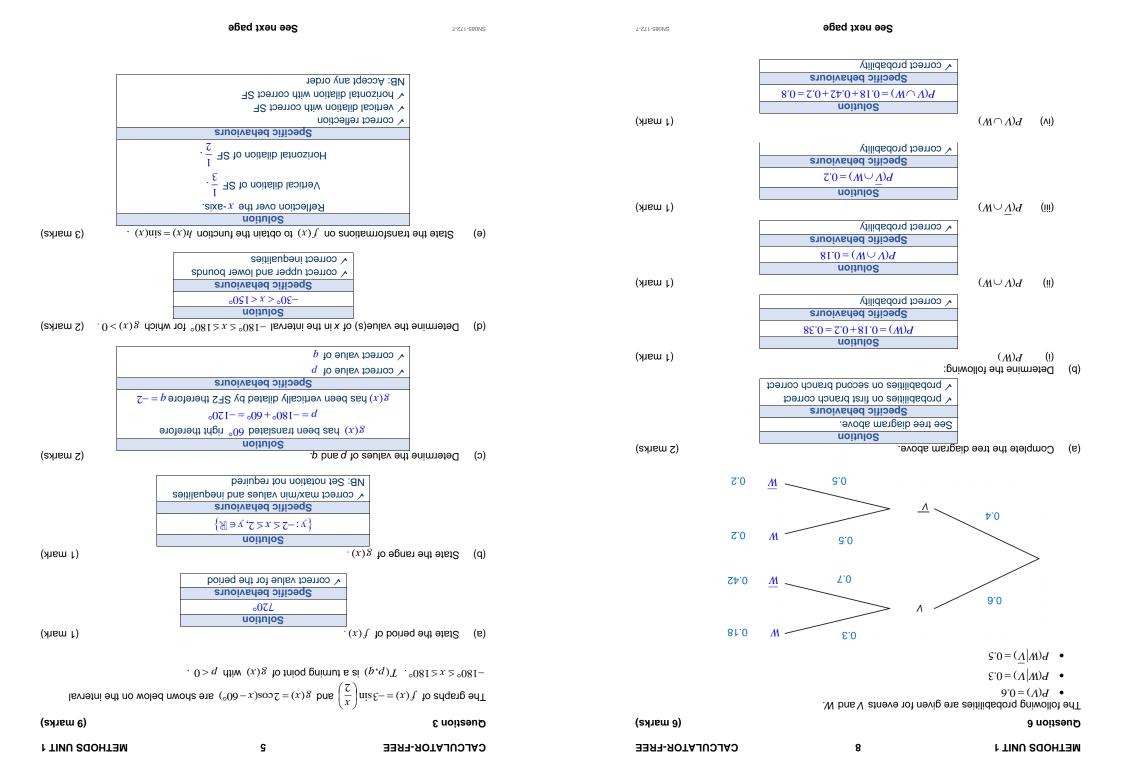
$$f(-3) = (-9)(-1) = 9$$

$$f(2) = (1)(4) = 4$$

Intersect at (-1,-5) and (-3,9).

Specific behaviours

- √ expands quadratic
- √ equate functions and then to zero
- √ recognises first root from given point
- √ factors into linear and quadratic
- √ completes factorisation
- ✓ determines *y*-coordinates and states coordinates of both points



(3 marks)

Question 4 (7 marks)

Consider the function $f(x) = \frac{a}{x+b}$, where a and b are constants. The graph of y = f(x) has an asymptote with equation x = -1 and passes through the point (-4, 1).

(a) Determine the value of a and the value of b.

	Solution
U	sing asymptote, $-1 + b = 0 \Rightarrow b = 1$.
U	sing point:
	$1 = \frac{a}{a}$

$$1 = \frac{a}{-4+1}$$
$$a = -3$$

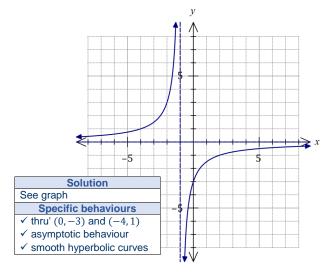
Specific behaviours

- ✓ value of b
- √ forms equation using point
- √ calculates value of a

(b) State the equation of the other asymptote of the graph of y = f(x). (1 mark)

Solution
y = 0
Specific behaviours
✓ correct equation

(c) Sketch the graph of y = f(x) on the axes below. (3 marks)



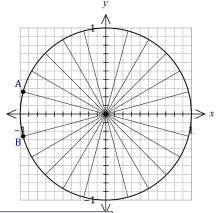
Question 5 (6 marks)

(a) A unit circle is shown.

CALCULATOR-FREE

Mark on the circumference of the circle the points A and B so that rays drawn from the origin to each point make anti-clockwise angles of 165° and $\frac{13\pi}{12}$ from the positive x-axis respectively.

Hence estimate the value of $\cos 165^{\circ}$ and the value of $\sin \left(\frac{13\pi}{12}\right)$.



Solution

See graph for points.

$$\cos 165^{\circ} = x$$
, where $-0.98 \le x \le 0.95$

$$\sin\left(\frac{13\pi}{12}\right) = y, -0.28 \le y \le -0.24$$

Specific behaviours

- √ both points located correctly
- √ value of cosine within range
- √ value of sine within range
- (b) Solve the equation $3 \tan(2x 10^\circ) = \sqrt{3}$ for $0^\circ \le x \le 180^\circ$.

(3 marks)

(3 marks)

Solution $\tan(2x - 10^{\circ}) = \frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}}$ $2x - 10^{\circ} = 30^{\circ}, 210^{\circ}$

Specific behaviours

$$2x = 40^{\circ}, 220^{\circ}$$

 $x = 20^{\circ}, 110^{\circ}$

- ✓ eliminates tan from equation
- ✓ one correct solution
- √ second correct solution