Perth Modern School

Year 12 Mathematics Methods

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Year 12 Methods
TEST 1
Friday 22 February 2019
One-page notes allowed
Calculator Assumed
39 marks 7 Questions

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Note: All part questions worth more than 2 marks require working to obtain full marks.

Question 1 (6 marks)

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s value for h'(z). (3 marks)

(a) Define $h(x) = \frac{f(x)}{g(x)}$, use the table to find the value for h'(2).

(3 marks) Define $I(x) = [g(x)]^{\mathbb{I}}$, use the table to find the value for I'(1).

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Question 2 (3 marks)

Find the equation of the line tangent to the function $y = (3x^2 - 2)^3$ at the point (2,1000). Give your answer in the gradient-intercept form.

Question 3 (3 marks)

If $\frac{dy}{dx} = (5x+3)^3$, and y = 50 when x = 1, determine the expression of y in terms of x.

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Supplementary Page

Question Number:

Question 4 (7 marks)

A company is purchasing a type of thin sheet metal required to make a closed cylindrical container with a capacity of 4000 π cm³. Let the radius of the cylindrical base be $\,^{\rm r}$ and the height $\,^{\rm h}$.

(a) Show that the surface area of the cylinder can be expressed as
$$\frac{2\pi r^2}{r} + \frac{8000\pi}{r}$$

(3 marks)

(b) Using calculus, determine the least area of metal required to make a closed cylindrical container from thin sheet metal in order that it will have a capacity of 4000π cm³. (4 marks)

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Question 7 (6 marks)

The position of a train on a straight mono rail, X metres at time I seconds, is modelled by the following formula for the velocity, V in metres/second, $^V = pt^2 - 12t + q$ where $^P \otimes q$ are constants.

The deceleration of the train is $8ms^{-2}$ when t=1, has a position t=1 when t=1 and is initially at the origin (t=0).

a) Determine the values of the constants $p^{\mathcal{B},q}$.

b) Determine the position of the train when the acceleration is $12ms^{-2}$.

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Question 5 (6 marks)

A share portfolio, initially worth \$26000, has a value of f dollars after f months, and begins with a negative rate of growth. The rate of growth remains negative until after 20 months (t = 20) when the value of the portfolio is momentarily stationary and then continues with negative growth for the life of the investment. The value of the portfolio, f(t) after t months can be modelled by the following, $f(t) = -2t^3 + bt^2 + ct + d$, $0 \le t \le 37$ months where b, c & d are constants.

Determine the values of the constants.

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Question 6 (8 marks)

The volume, V in cubic metres and radius R metres, of a spherical balloon are changing with time, $V=\frac{4\tau R^3}{3}$. The radius of the balloon at any time is given by $R=2t(t+3)^3$.

Determine the following:

a) The value of
$$\frac{dR}{dt}$$
 when $t=1$. (3 marks)

b) The value of
$$\frac{dV}{dt}$$
 when $t=1$. (3 marks)

Consider the volume of the balloon at t=1.

c) Use the increments formula to estimate the change in volume 0.1 seconds later (i.e t =1.1) (2 marks)