Rossmoyne Senior High School

WA Exams Practice Paper A, 2015 Question/Answer Booklet

If required by your examination administrator, please place your student identification label in this box

MATHEMATICS METHODS UNITS 1 AND 2 Section Two:

Calculator-assumed

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Materials required/recommended for this section To be provided by the supervisor

This Question/Answer Booklet Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

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METHODS UNITS 1 AND 2 2

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator- assumed	13	13	100	98	65
			Total	150	100

CALCULATOR-ASSUMED

Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2015. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question that you are continuing to answer at the top of the
 page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

See next page

CALCULATOR-ASSUMED 19 METHODS UNITS 1 AND 2

Additional working space

Question number:

(98 Marks)

Section Two: Calculator-assumed

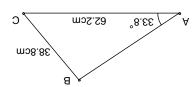
provided. This section has thirteen (13) questions. Answer all questions. Write your answers in the spaces

3

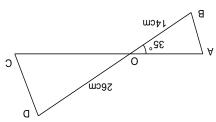
Working time for this section is 100 minutes.

(e marks) Question 9

(The triangle is not drawn to scale). (3 marks) Calculate the smallest possible length of AB in the triangle shown below.



ODC is twice that of triangle OAB, determine the length OA. (3 marks) AOB = 35° , and the lengths OB = 14cm, OD = 26cm and AC = 30cm. If the area of triangle In the diagram below (not to scale), the line AC intersects the line BD at O. The angle



Question number:

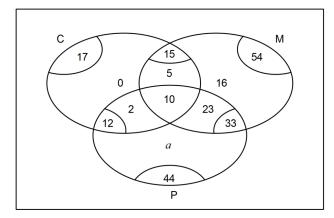
METHODS UNITS 1 AND 2

CALCULATOR-ASSUMED

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Question 10 (5 marks)

The following Venn diagram shows the numbers of students electing to study at least one of Chemistry (C), Math (M) or Physics (P) in upper school.



(a) Determine the value of a.

(1 mark)

(b) Determine $n(C \cup M \cup P)$.

(1 mark)

- (c) If one student is selected at random from the group, determine the probability
 - (i) they elected to study math but not physics.

(1 mark)

- (ii) they elected to study math and physics, given that they did not study chemistry. (1 mark)
- (iii) they elected to study two subjects, given that they did not elect to study all three subjects. (1 mark)

See next page

CALCULATOR-ASSUMED

17

METHODS UNITS 1 AND 2

Additional working space

Question number: _____

Chris have spent a total of at least 30 (2 marks)	(ii) After how many days in his new job will yours answering emails?
ing emails followed an arithmetic job he spent 2 hours 20 minutes answering 36 minutes.	(b) Because of this new job, Chris began to spend answering client emails. His time spent answering progression such that on the 6 th day of his new emails and on the 10 th day he spent just 1 hour emails and on the 10 th day he spent just 1 hour emails and on the 10 th day he spend answering em
w many clients did Chris add on this (2 marks)	(a) During which day did Chris finish the job and ho
Jet aftet 8 days? (1 mark)	(b) How many clients had Chris re-entered altogeth
On the first day he managed to re-enter was given more and more time for this job on the previous day.	After the failure of a computer containing the details of entering all the client information into a new computer. the details of 15 clients. On each subsequent day, he and managed to add two more clients each day than on the managed to add two more clients each day than on the fifth.

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CALCULATOR-ASSUMED

(9 marks)

METHODS UNITS 1 AND 2

METHODS UNITS 1 AND 2 16 CALCULATOR-ASSUMED

Question 21 (6 marks)

The circumference of a circle of radius 25cm passes through the centre of a circle of radius 15cm. Find the area of intersection of the two circles.

Eud of questions See next page

METHODS UNITS 1 AND 2

6

CALCULATOR-ASSUMED

CALCULATOR-ASSUMED

METHODS UNITS 1 AND 2

(6 marks) Question 12

Software has been developed to classify an email message as either good or spam. The software is not perfect: only 88% of spam is classified as such, and 4% of emails that are good are classified as spam.

A large number of emails, 15% of which were spam, were checked by the software.

What is the probability that the software will classify a randomly chosen email as spam?

(3 marks)

Given that the software classifies an email as good, what is the probability that it is actually spam. (3 marks) (b) The displacement, x m, of a particle from a fixed point O is given by $x = 2t^3 - 3t^2 - 12t + 1$, $t \ge 0$, where t is the time, in seconds.

15

Determine the initial velocity of the particle.

(2 marks)

Determine the displacement of the particle at the instant it is stationary. (2 marks)

(b) State the maximum possible value of P(A).

(c) Determine the value of x under each of the following conditions.

(i) A and B are mutually exclusive.

(1 mark)

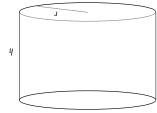
ii) $P(A|B) = \frac{1}{5}$.

(iii) A is independent of B.

14 CALCULATOR-ASSUMED

(10 marks)

A cylinder is such that the sum of the height and three times the radius is $50 \, \mathrm{cm}$.



Question 20

METHODS UNITS 1 AND 2

Write an equation for the height, h, in terms of the radius, v, for this cylinder. (1 mark)

(ii) Show that the total surface area of the cylinder is given by $A=100\pi r-4\pi r^2$. (2 marks

(iii) Using calculus techniques, determine the dimensions of this cylinder to obtain the maximum possible surface area, and state this area. (3 marks)

Question 14 (9 marks)

8

Sequence A is geometric and has n^{th} term ($n \ge 1$) given by $T_n = 5(0.8)^n$.

What is the first term of Sequence A?

(1 mark)

How many terms of Sequence A are greater than 1?

(1 mark)

A student added together the first *m* terms of Sequence A and obtained a total between 21.9 and 22. Explain why the student must have made a mistake, even though the number m is not known. (2 marks)

Sequence B is also geometric with a common ratio of 1.2. The sum of its first two terms is 0.22.

Determine the first term of Sequence B.

(2 marks)

How many terms of Sequence B are less than 1?

(1 mark)

What is the fewest number of terms of Sequence B that must be summed to obtain a total of at least 100? Justify your answer. (2 marks) **Question 19**

(6 marks)

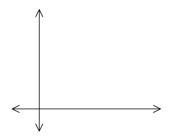
(2 marks)

The quantity P is directly proportional to the quantity T, and it is known that when T = 12,

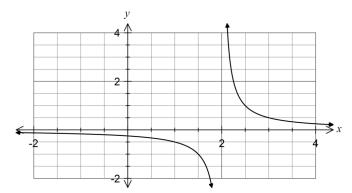
13

Determine an equation for the relationship between P and T. (2 marks)

Sketch a graph of the relationship between P and T.



The graph below shows $y = \frac{a}{x-b}$, where a and b are constants.



Determine the values of a and b.

(2 marks)

(3 marks)

(7 marks) **⊉uestion 15** 6

A function is given by $f(x) = 200 + 32x^2 - x^4$ for $-3 \le x \le 5$.

function for the given domain. Use calculus techniques to determine the coordinates of both stationary points of the

> A government organisation estimated that the world population was 6,783,187.02 on the first of (8 marks) **&l noiteau**

July 2009 and was 6,774,705,647 one month later on the first of August.

15

If the population is assumed to be growing exponentially, determine

the monthly percentage growth rate in the population. (S marks)

an expression for the population 1 months after the first of July 2009. (2 marks)

(S marks) the world population on the first of July 2010, to the nearest million. If this rate of growth continues, determine

(z warks) in which year and month the population of the world was expected to reach 7,000

100

-001

-002

300

007

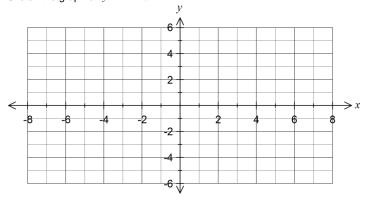
-009

Sketch the graph of y = f(x) for $-3 \le x \le 5$ on the axes below.

Question 16 (8 marks)

(a) Sketch the graph of $y^2 = 4 - 2x$.

(3 marks)



(b) State, with reasons, whether these relationships are also functions:

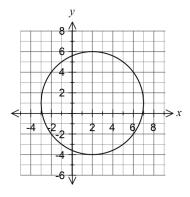
(i)
$$y^2 = 4 - 2x, x \ge 0.$$

(1 mark)

(ii)
$$y^2 = 4 - 2x, y \ge 0$$
.

(1 mark)

(c) The equation of the following graph is $x^2 + y^2 + ax + by = c$. Determine the values of a, b and c. (3 marks)



Question 17

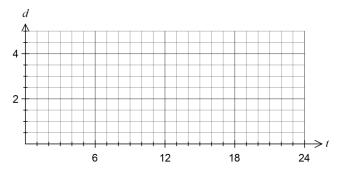
(9 marks)

The depth of water in a harbour, d measured in metres, t hours after midnight, can be modelled by the function $d(t) = a\cos(bt) + c$.

11

The minimum depth of 1.5 meters first occurred at midnight, followed by a maximum of 4.5 metres six hours later.

(a) Sketch how the depth varied over the first 24 hours on the axes below. (3 marks)



b) Explain, with reasoning, why a = -1.5, $b = \frac{\pi}{6}$ and c = 3.

(3 marks)

For what percentage of a day is the depth of water at least 2.5 metres? (3 marks)