

Perth College

Semester Two Examination, 2018

Answer booklet	Guestion
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required by your examination administrator, please place your student identification label in this box	il .

Solutions

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Calculator-free

five minutes	Time allowed for this section Reading time before commencing work: Working time:
<u> </u>	Your nam

Student number: In figures

Materials required/recommended for this section

In words

To be provided by the supervisor

Formula sheet This Question/Answer booklet

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, To be provided by the candidate

Special items:

it to the supervisor before reading any further. you do not have any unauthorised material. If you have any unauthorised material with you, hand No other items may be taken into the examination room. It is your responsibility to ensure that Important note to candidates

correction fluid/tape, eraser, ruler, highlighters

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METHODS UNITS 1 AND 2

CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	questions questions to		Marks available	Percentage of examination	
Section One: Calculator-free	8	8	50	54	35	
Section Two: Calculator-assumed	13	13	100	96	65	
1				Total	100	

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Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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CALCULATOR-FREE

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METHODS UNITS 1 AND 2

Supplementary page

Question	number:	

CALCULATOR-FREE 3 METHODS UNITS 1 AND 2 Section One: Calculator-free 35% (54 Marks)

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1

The first four terms of a sequence are -1, 3, -9 and 27.

Write a recursive rule for the sequence above. (1 mark)

Write a rule for the n^{th} term. (1 mark) $= \frac{1}{n^{2}} \sum_{i=1}^{n} \frac{1}$

1-n(8-) 1- = n]

iii) Determine the value of $T_{\mathbb{S}}$.

1 18-

The first three terms, in order, of an arithmetic sequence are 4x + 3, 2x - 1 and x - 8. Determine the fourth term of the sequence. (4 marks)

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METHODS UNITS 1 AND 2 10 CALCULATOR-FREE Question 8 (8 marks) Let $\int (x) = x^2 + x$.

(a) Determine the average rate of change when x=3 and x=5.

(b) Use first principles to determine the rate of change function f'(x)

 $\frac{1}{(X+_7X)-(Y+X)+_7(Y+X)} = (X)_{10}^{10}$

1 X-x-y+x+zy+yx7+zx [m]

 $\frac{4}{4^{+2}4^{+}4x^{2}}$ mil =

·2 gravity \ (1+4+ x5) \ (1+4+

Shots Withsman V $(X)^{1}f$ $(X)^{2}f$ $(X)^{2}f$ (

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(2 marks)

End of questions

METHODS UNITS 1 AND 2

CALCULATOR-FREE

Question 2

(6 marks)

(a) State the 4th term of $(1-2x)^{10}$.

(3 marks)

$$\begin{pmatrix} 10\\3 \end{pmatrix} \begin{pmatrix} 1 \end{pmatrix}^{7} \begin{pmatrix} -2\chi \end{pmatrix}^{3}$$

$$= -960 x^3$$

(b) Sketch the graph of a function that satisfies all conditions below:

(3 marks)

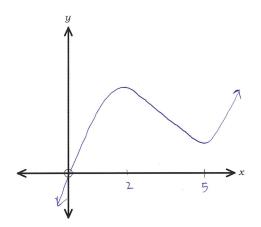
- has one root, which is the origin,
- $\frac{dy}{dx} = 0$ when x = 2 and x = 5,

•
$$\frac{dy}{dx} < 0$$
 when $2 < x < 5$

-1 / wondition not

• $\frac{dy}{dx} > 0$ otherwise

met.



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METHODS UNITS 1 AND 2

Question 7

(6 marks)

(a) Evaluate $\frac{m^{0.5}}{n^2}$ when $m=4\times10^6$ and $n=5\times10^2$, writing your answer in simplest form without the use of scientific notation. (3 marks)

$$\frac{(4 \times 10^{6})^{0.5}}{(5 \times 10^{2})^{2}} = \frac{2 \times 40^{3}}{25 \times 10^{4}}$$

$$= \frac{2}{250}$$

$$= \frac{1}{125}$$
Correctly expand:

correctly simplifies

power of 10.

(b) Determine the value of x when $4^x = 32\sqrt{2}$.

(3 marks)

$$(2^{2})^{k} = 2^{5} \cdot 2^{\frac{1}{2}}$$

$$2x = 5\frac{1}{2}$$

$$2x = \frac{11}{2}$$

$$x = \frac{11}{4}$$

$$\sqrt{\text{solver equation}}$$

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CALCULATOR-FREE

Question 3

Solve each equation below for x.

(5 marks)

$$x\varepsilon = (\varepsilon - x)(\varepsilon + x)$$

$$0 = \chi \xi - \chi = (x - x)(x + x)$$

$$0 = \chi \xi - \chi = \chi$$

$$0 = (1 + \chi)(y - \chi)$$

$$\int C = (1+x)(\mu-x)$$

(3 marks)

(8 marks)



(c) $\Delta \cos x + \sqrt{3} = 0$, $0 \le x \le 2\pi$.

$$\int \frac{1}{2} = 0 + 70$$

$$\int \frac{7}{2} = 1 + 2 = 1 + 2 = 1$$

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CALCULATOR-FREE

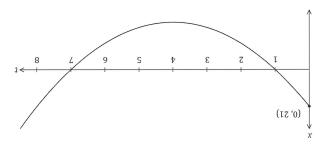
(e marks)

METHODS UNITS 1 AND 2

Question 6

seconds is given by $x = at^2 + bt + c$ metres. A small body moves in a straight line so that its displacement x from a fixed point 0 after t

The position-time graph of the body is shown below.



(3 marks)

(a) Determine the values of the constants a,b and c.

1 hr-=9 / 8=9 / 1c=3

$$|7+7+7-78=$$

 $(L+78-7)8=$
 $(L-7)(1-1)8=$

(3 marks)

(b) Determine the displacement of the body when its velocity is 24 ms⁻¹.

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METHODS UNITS 1 AND 2

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CALCULATOR-FREE

Question 4

(7 marks)

(a) Simplify

(i)
$$\frac{d}{dx}(2x^5 + 6x - 7)$$
.

(1 mark)

10x + +b

(ii)
$$\lim_{h \to 0} \frac{(x+h)^4 - x^4}{h}$$
.

(1 mark)

(b) Determine the gradient of the tangent to the curve $y = x^3 - 4x + 3$ when x = -2. (2 marks)

$$\frac{dy}{dx} = 3x^{2} - 4$$

$$= 3(-2)^{2} - 4$$

$$= 8$$

(c) Determine f(x) given f'(x) = 4x - 5 and f(2) = -3.

(3 marks)

$$f(x) = 2x^2 - 5x + c$$

$$-3 = 2(2)^2 - 5(2) + c$$

$$f(x) = 2x^2 - 5x - 1$$

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CALCULATOR-FREE

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METHODS UNITS 1 AND 2

Question 5

(6 marks)

The derivative of a cubic polynomial is given by $\frac{dy}{dx} = 3x^2 - 2x - 24$.

The cubic passes through the point (-1, -14).

(a) Determine the equation of the cubic.

(2 marks)

$$\int = \chi^{3} - \chi^{2} - 24\chi + c$$

$$-14 = -1 - 1 + 24 + c$$

$$\boxed{c = -36}$$

(b) Show that the cubic has a root when x = -2.

$$y = (-2)^{3} - (-2)^{2} - 24(-2) - 36$$
= 0

(c) Determine the other two roots of the cubic.

(3 marks)

(1 mark)

$$(x+2) \frac{x^{2}-3x-18}{x^{3}-x^{2}-24x-36}$$

$$\frac{-(x^{3}+2x^{2})}{-3x^{2}-24x} = (x-6)(x+3)$$

$$\frac{-(-3x^{2}-6x)}{-19x-36}$$

$$\therefore \text{ other roots are }$$

$$x=6, x=-3$$

$$y=2$$

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