

# Semester Two Examination, 2019

# Question/Answer booklet

place your student identification label in this box If required by your examination administrator, please

| Section One:       |
|--------------------|
| 4 GNA & STINU      |
| WETHODS            |
| <b>SOITAMEHTAM</b> |

Calculator-free

| <br>Your name |                 |
|---------------|-----------------|
| <br>ln words  |                 |
| ln figures    | Student number: |

# Time allowed for this section

fifty minutes Working time: Reading time before commencing work: sətunim əvif

## To be provided by the supervisor Materials required/recommended for this section

This Question/Answer booklet

Formula sheet

# To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

Special items:

#### you do not have any unauthorised material. If you have any unauthorised material with you, hand No other items may be taken into the examination room. It is your responsibility to ensure that Important note to candidates

it to the supervisor before reading any further.

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## Structure of this paper

| Section                            | Number of questions available | Number of questions to be answered | Working<br>time<br>(minutes) | Marks<br>available | Percentage<br>of<br>examinatio<br>n |
|------------------------------------|-------------------------------|------------------------------------|------------------------------|--------------------|-------------------------------------|
| Section One:<br>Calculator-free    | 8                             | 8                                  | 50                           | 52                 | 35                                  |
| Section Two:<br>Calculator-assumed | 13                            | 13                                 | 100                          | 98                 | 65                                  |

Total 100

### Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
   Do not use erasable or gel pens.
- You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

| Markers use only   |         |      |
|--------------------|---------|------|
| Question           | Maximum | Mark |
| 1                  | 4       |      |
| 2                  | 7       |      |
| 3                  | 7       |      |
| 4                  | 6       |      |
| 5                  | 7       |      |
| 6                  | 8       |      |
| 7                  | 7       |      |
| 8                  | 6       |      |
| S1 Total           | 52      |      |
| S1 Wt<br>(×0.6731) | 35%     |      |
| S2 Wt              | 65%     |      |
| Total              | 100%    |      |

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|---------------|-------------|----|

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| CALCULATOR-FREE    | 11 | METHODS UNITS 3 AND 4 |
|--------------------|----|-----------------------|
| Supplementary page |    |                       |

Question number: \_\_\_\_\_

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| 35% (52 Marks) Write your answers in the spaces | Answer <b>all</b> questions. <sup>,</sup> | ıjded.                    | siqT |
|---|---|---------------------------|------|
|   |   |                           | b.o/ |
|   |   | king time: 50 minutes.    | юW   |
| (4 marks)                                       |   | £ noite                   | enδ  |
|   |   | ermine the following:     | Dete |
| (S marks)                                       |   | $\int 12(2x+1)^2 dx.$     | (9)  |
|   |   |                           |      |
| (Ynem 1)  |   | $\frac{d}{dx}\cos(2x+1).$ | (q)  |
|   |   |                           |      |

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(7 mark)

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(c)  $\frac{d}{dx} \int_{\varepsilon}^{x} (2t+1) dt.$ 

METHODS UNITS 3 AND 4 10 CALCULATOR-FREE Left  $f(x) = \frac{x}{x+1}$ .

(a) Determine f(x) and  $f(x+\delta x)$  when x=70 and  $\delta x=5$ .

(b) Use f(x) and the increments formula to estimate the difference between  $\frac{99}{90}$  and  $\frac{92}{93}$ . (5 marks)

End of questions snz/s-145-1

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(4 marks)

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Question 2 (7 marks)

$$v = \frac{8}{1+t} \,\mathrm{m/s}\,, t \ge 0.$$

(a) Determine the velocity of the body when its acceleration is  $-2 \text{ m/s}^2$ .

The velocity of a small body moving in a straight line at time t seconds is given by

(b) Calculate the distance travelled by the body in the first 3 seconds. (3 marks)

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CALCULATOR-FREE

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METHODS UNITS 3 AND 4

**Question 7** 

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(7 marks)

In a class of 25 students, 20 are right-handed.

(a) One student is selected at random from the class and the random variable X is the number of right-handed students in the selection. Determine the mean and standard deviation of X. (3 marks)

b) Two students are selected at random from the class without replacement and the random variable Y is the number of right-handed students in the selection.

(i) Complete the probability distribution table below.

(3 marks)

| у      | 0 | 1 | 2 |
|--------|---|---|---|
| P(Y=y) |   |   |   |

Determine E(Y). (1 mark)

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| (3 marks)             | $_5$ 7 in the form $\log_5 k$ . | gol S – E <sub>2</sub> gol + 1 ətirW | (૧) |
|-----------------------|---------------------------------|--------------------------------------|-----|
| (7 marks)             |                                 | £ noits                              | eυδ |
| METHODS UNITS 3 AND 4 | g                               | CULATOR-FREE                         | САГ |

(b) Determine the coordinates of the point of inflection of the graph of y = f(x). (2 marks)

(8 marks)

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**METHODS UNITS 3 AND 4** 

Question 6

Let  $f(x) = (1-x)e^{-2x}$ .

second derivative test to determine its nature. (a) Determine the coordinates of the stationary point of the graph of y = f(x) and use the

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(S marks)

(S marks)

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(c) Determine  $\frac{d}{dx} \left[ \log_e \left( \frac{1}{5x^2 + 1} \right) \right]$ .

(b) Solve for *x* the equation  $e^{x-2} = \sqrt{3}$ .

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**METHODS UNITS 3 AND 4** 

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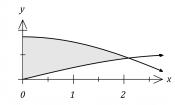
CALCULATOR-FREE

Question 4

(6 marks)

Let 
$$f(x) = \sqrt{3} \cos\left(\frac{x}{2}\right)$$
 and  $g(x) = \sin\left(\frac{x}{2}\right)$ .

The shaded region on the graph below is enclosed by x=0, y=f(x) and y=g(x).



(a) Show that  $f\left(\frac{2\pi}{3}\right) = g\left(\frac{2\pi}{3}\right)$ .

(2 marks)

(b) Determine the area of the shaded region.

(4 marks)

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CALCULATOR-FREE

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**METHODS UNITS 3 AND 4** 

Question 5

(7 marks)

The random variable X has probability density function f(x) shown below, where k is a positive constant.

$$f(x) = \begin{cases} kx + \frac{1}{20} & \text{if } 0 \le x \le 4 \\ 0 & \text{if elsewhere} \end{cases}$$

(a) Deduce that  $k = \frac{1}{10}$ .

(3 marks)

b) Determine the value of a if  $P(1 < X < a) = \frac{1}{5}$ .

(4 marks)

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