

Semester Two Examination, 2020

Question/Answer booklet

If required by your examination administrator, please place your student identification label in this box

2211-1018182182
Calculator-free
Section One:
₽&E STINU
WETHODS
NATHEMATICS

:YA student number:

Number of additional answer booklets used (if applicable):	eətunim əvit sətunim yiti	Time allowed for this section seading time before commencing work: Vorking time:
		Your nam

Materials required/recommended for this section

In words

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: r

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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METHODS UNITS 3&4 2 CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65

Total 100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only			
Question	Maximum	Mark	
1	7		
2	5		
3	6		
4	7		
5	7		
6	7		
7	7		
8	6		
S1 Total	52		
S1 Wt (×0.6731)	35%		
S2 Wt	65%		
Total	100%		

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CALCULATOR-FREE	11	METHODS UNITS 3&4
Supplementary page		

Question	numher:	
Question	number.	

METHODS UNITS 3&4 3 CALCULATOR-FREE

This section has eight questions. Answer all questions. Write your answers in the spaces 32% (25 Warks) Section One: Calculator-free

Working time: 50 minutes.

(7 marks) ⊈ noitesuQ

See next page

The function f is defined by $f(x) = \frac{x^2 - 5}{x - 5}$, $x \ne 3$.

Determine the coordinates and nature of all stationary points of the graph of y = f(x). The second derivative of f is $f''(x)=8(3-x)^{-3}$. DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

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ZNS42-T02-T

(6 marks) 8 noitsau9 CALCULATOR-FREE OΤ METHODS UNITS 3&4

The acceleration at time t seconds of a small body travelling in a straight line is given by

$$a(t) = \frac{-3}{\sqrt{2t+3}} cm/s^2, t \ge 0.$$

When $t\!=\!3$ the body was at the origin and 8 seconds later its displacement was 30~cm.

Determine the velocity of the body when t=6.5.

End of questions ZN542-T62-T

METHODS UNITS 3&4 CALCULATOR-FREE Question 2 (5 marks) The rate of change of pressure in an air tank is given by $P'(t) = -3e^{-0.05t}$, where t is the time in minutes since it began emptying from an initial pressure of 70 psi. Determine an expression for the pressure *P* in the tank at any time t, $t \ge 0$. (2 marks) Determine (i) the time taken for the pressure in the tank to fall to 40 psi. (2 marks) the minimum pressure in the tank for $t \ge 0$. (1 mark)

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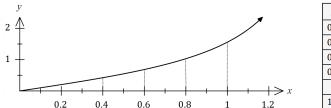
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Question 7 (7 marks)

The graph and a table of values for y=f(x) is shown below, where $f(x)=\tan x$.



 x
 y

 0.2
 0.2

 0.4
 0.42

 0.6
 0.68

 0.8
 1.03

 1
 1.56

 1.2
 2.57

Let $I = \int_{0}^{1} \tan x \, dx$.

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(a) By using the information shown and considering sums of the form $\sum_i f(x_i) \delta x_i$, explain why I > 0.426. (3 marks)

(b) In a similar manner to (a), determine the best estimate for the value of the constant U, where I < U. (2 marks)

(c) Use your previous answers to determine a numerical estimate for I and explain whether your estimate is smaller or larger than the exact value of I. (2 marks)

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See next page

distribution function F(x) where The continuous random variable X takes values in the interval 1 to 5 and has cumulative (e marks) & noitesup METHODS UNITS 3&4 g CALCULATOR-FREE

$$\begin{vmatrix}
1 > x & 0 \\
5 \ge x \ge 1 & \frac{1-x}{5} \\
1 & 1
\end{vmatrix} = (x \ge X) d = (x) d$$

Determine

.(≳.£≥X)¶

(ii) the value of k, if P(X>k)=0.85. (S marks)

(† wark)

(3 marks) (b) Determine f(x), the probability density function of X, and sketch the graph of y = f(x).

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ZNS42-T02-T

The discrete random variable X is defined by (7 marks) Question 6 CALCULATOR-FREE 8 METHODS UNITS 3&4

$$P(X=x) = \begin{cases} \frac{x+k}{3x+2} & x=0,1\\ 0 & x \end{cases}$$
 elsewhere. (a) Determine the value of the constant k .

(b) Determine
$$(1) \qquad \qquad (1) \qquad \qquad (2) \label{eq:potential}$$

(ii)
$$E(3X-1)$$
.

(iii)
$$Var(3X = 1)$$
.

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METHODS UNITS 3&4

6

CALCULATOR-FREE

Question 4

(7 marks)

(a) Determine an expression for f'(x) when

(i) $f(x) = \ln(1 - \cos 3x)$.

(2 marks)

(ii) $f(x) = e^{5x} (5-2x)^3$.

(3 marks)

(b) For the positive number x, let $A(x) = \int_0^x (8-2^{t^2}) dt$.

Determine the value(s) of x for which $\frac{dA}{dx} = 0$.

(2 marks)

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CALCULATOR-FREE 7

Question 5

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(7 marks)

METHODS UNITS 3&4

(a) Simplify $\log 8 + 2 \log 5 - \log 2$.

(2 marks)

(2 marks)

(b) Given that $\log_a x = 1.4$, determine the value of $\log_a x \sqrt{x}$.

(c) Determine the solution to the equation $5^{2x} = 2^{3-x}$ in the form $x = \frac{\log a}{\log b}$. (3 marks)

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