General Discrete Random Variables Calculator Assumed

Time: 45 minutes Total Marks: 45 Your Score: / 45



Question One: [2, 2, 3 = 7 marks] ₹

random variable. Determine, with reasoning, whether each of the following represent a discrete

61.0	60.0	4.0	1.0	£.0	(X=X)d
t	3	2	ī	О	X

(q)

6.0	9.0	£.o-	0	2.0	(X=X)d
9	8	ī	I-	2-	X

....
$$f(x = X) = \int_{0}^{x} \int_{0}^{x} f(x = X) dx$$

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Question Six: [3, 2, z = 7 marks] **CA** Mathematics Methods Unit 3

The probability distribution for X is given by:

$$\begin{vmatrix} 2.7.0 = x & \frac{1+x}{\lambda} \\ 4x & \frac{x\lambda - 002}{228} \end{vmatrix} = (x = X)q$$

(a) Determine the value of k.

$$I = \frac{1}{12} + \frac{1}{$$

(b) Calculate E(X)

$$E(X) = 0 \times \frac{1}{10} + 1 \times \frac{2}{10} + 2 \times \frac{3}{10} + 3 \times \frac{170}{825} + 4 \times \frac{160}{825}$$

(c) Calculate $(2 \le X \mid E > X)^{q}$

$$\frac{\frac{2}{01}}{\frac{8}{228} + \frac{2}{01}} = 0.4286$$

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Question Two: [1, 2, 2, 2, 1, 2 = 10 marks] CA

A regular 8-sided dice is rolled.

- (a) Explain why this experiment yields a uniform discrete random variable.
- (b) Define the cumulative probability function of this random variable in a table below.
- (c) In the long run, what is the value we expect to obtain on one roll of the dice?
- (d) What is the standard deviation of these outcomes?
- (e) If instead of an 8-sided dice, we roll a 16-sided dice, by what scale do each of the probability values change?

$$E(aX + b) = aE(X) + b$$

(f) Would the rule hold in this situation. Explain your answer.

Mathematics Methods Unit 3

$$=\frac{0.4}{0.65}=0.6154$$

$$P(Y > 2 | Y \le 4)$$

(e)

$$=\frac{0.4}{0.8}=0.5$$

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Question Three: [1, 2, 3, 2 = 8 marks]

Each of the following represent discrete probability functions. Determine the value of

CA

(a)
$$P(x) = \frac{1}{\lambda} = 1, 2, 3, \dots 12$$

(q)

$$P(x) = \frac{x}{2k - 1}; x = 1, 2, 3, 4, 5, 6$$

(X=X)d

3

Ą

7

УZ

3

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Question Four: [4 marks] Mathematics Methods Unit 3

Consider the discrete probability function represented in the table below.

£.0	81.0	q	2.0	В	(X=X)d
Z	2	t	3	I	X

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Determine the values of a and
$$b$$
 such that

68.0 = q + p

 \checkmark 22.1= d + D

№ 20.0= p

√ E.0= d

A probability distribution for Vis: [1, 2, 2, 2, 2 = 9 marks]Question Five:

69.0 ₽.0 1.0 (∧5_A)d 8.0 G ħ

K⊃

10

Determine:

(a) b(X=3)

22.0=

 $b(2 \le Y < 4)$

(q)

35.0 = 32.0 + 5.0 =

1

 $b(X < Y \cap Y > 4)$

(o)

(p)

E.0 = 2.0 + 1.0 =

 $b(X \le Z \mid X \le 3)$

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Question Four: [4 marks] CA

Consider the discrete probability function represented in the table below.

X	1	3	4	5	7
P(X=x)	a	0.2	b	0.15	0.3

$$E(X) = 4.7$$

Determine the values of a and b such that

Question Five: [1, 2, 2, 2, 2 = 9 marks] CA

A probability distribution for *Y* is:

У	1	2	3	4	5
<i>P</i> (<i>Y</i> ≤ <i>y</i>)	0.1	0.4	0.65	0.8	1

Determine:

$$P(Y = 3)$$
 (a)

 $P(2 \le Y < 4)$

$$P(Y < 2 \cup Y > 4)$$
 (c)

$$P(Y \le 2 \mid Y \le 3)$$

(d)

Mathematics Methods Unit 3

Question Three: [1, 2, 3, 2 = 8 marks] CA

Each of the following represent discrete probability functions. Determine the value of k for each.

(a)
$$P(x) = \frac{1}{k}$$
; $x = 1, 2, 3, ... 12$
 $k = 12$

$$k = 1 - 0.2 - 0.3 - 0.1 - 0.15$$

 $k = 0.25$

$$P(x) = \frac{x}{2k-1}$$
; $x = 1, 2, 3, 4, 5, 6$

$$1 = \frac{1+2+3+4+5+6}{2k-1}$$

$$1 = \frac{21}{2k-1}$$

$$k = 11$$

(d)

 X
 1
 2
 3
 5
 7

 P(X=x)
 2k
 k
 k
 5k
 6k

$$2k+k+k+5k+6k=1$$

$$k = \frac{1}{15}$$

 $b(X > 5 | X \leq t)$ Mathematics Methods Unit 3

[1, 2, 2, 2, 1, 2 = 10 marks]Ouestion Two: **CA** Mathematics Methods Unit 3

A regular 8-sided dice is rolled.

Explain why this experiment yields a uniform discrete random variable.

all add to 1, making it a DRV. The chance of each outcome is the same (1/8) therefore making it uniform, and they

Define the cumulative probability function of this random variable in a table

Ţ	g√8.0	o92·o	0.625	6. 0	975.0	0.250	0.125	(x5X)d
8	<u></u>	9	9	b	8	2	ī	X

(c) In the long run, what is the value we expect to obtain on one roll of the dice?

$$E(X) = 0.125(1+2+3+4+5+6+7+8)$$

 $E(X) = 4.5$
 $\therefore 4015 \checkmark$

What is the standard deviation of these outcomes?

$$\nabla_{s} = \frac{1}{2} (2.5)^{2} + \frac{1}{2} (2.5)^{2$$

the probability values change? (e) If instead of an 8-sided dice, we roll a 16-sided dice, by what scale do each of

Multiplied by a half

(f) hold in this situation. Explain your Would the rule E(aX + b) = aE(X) + b

no change from one unit to another. Instead, the number of outcomes have No. There has been no change of scale or origin in this situation, for example,

doubled.

answer.

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Question Six: [3, 2, 2 = 7 marks] CA

The probability distribution for X is given by:

$$P(X = x) = \begin{cases} \frac{x+1}{k} & x = 0,1,2\\ \frac{200 - kx}{825} & x = 3,4 \end{cases}$$

(a) Determine the value of k.

(b) Calculate E(X)

$$P(X < 3 | X \ge 2)$$

(c) Calculate

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SOLUTIONS Calculator Assumed General Discrete Random Variables

Time: 45 minutes Total Marks: 45 Your Score: / 45

Question One: [2, 2, 3 = 7 marks]

Determine, with reasoning, whether each of the following represent a discrete random variable.

(a)

	X	0	1	2	3	4
Ī	P(X=x)	0.3	0.1	0.4	0.05	0.15

CA

Yes this table does represent a DRV, all probabilities add to 1 and there are no negative values.

(b)

X	-2	-1	1	3	5
P(X=x)	0.2	0	-0.3	0.6	0.5

No, this table does not represent a DRV. Despite all the probability values adding to 1, as one is negative, this cannot represent a DRV. $\checkmark\checkmark$

$$P(X = x) = \left(\frac{1}{2}\right)^{x}$$
; $x = 1, 2, 3, 4...$

(c)

$$\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16} \dots \checkmark$$

$$S_{\infty} = \frac{0.5}{1 - 0.5} = 1 \checkmark$$

The sequence of probabilities is:

Therefore all probabilities will add to 1, and none are negative.

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