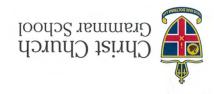
2019 TEST 4



Section One:

Calculator-free

			Teacher's name
KEY	& WARKING	240171102	Your name

Time and marks available for this section

Reading time for this section: 3 minutes 15 minutes 15 minutes 15 minutes 15 minutes 17 minutes 18 minutes 19 minutes 19

Marks available:

Materials required/recommended for this section To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items:

Important note to candidates

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MATHEMATICS METHODS Year 11

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MATHEMATICS METHODS Year 11

CALCULATOR-FREE

(z marks)

↑ noitesuD

In Australia, the probability of having blue eyes is approximately 35% and the probability of having fair hair is approximately 24%. The probability of having both blue eyes and fair hair is approximately 17%.

Determine the probability that someone with blue eyes will have fair hair.

$$\frac{f!}{2\varepsilon} = (29\mu \text{ sud} | \text{his hair})$$

Lovrest humevator

See next page

CALCULATOR-ASSUMED 8 MATHEMATICS METHODS Year 11

Question 7

The diagram below shows 13 points where no three points are selliness.

The diagram below shows 12 points where no three points are collinear. Points A,B,C and D define a quadrilateral.

Quadrilateral $\ensuremath{\mathit{ABCD}}$ is one of the many quadrilaterals that can be formed. Determine the number of quadrilaterals that can be formed.

Number of specialisticities = 295

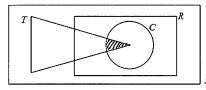
V states that a combination of the points is sequired from 12 to combination coefficient.

End of Questions

Sets T,R and C are defined in a sample space S . No region within the sample space S is empty.

(a) Shade the appropriate region to represent the set $T \cap R \cap C$.

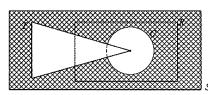
(1 mark)



Vorrect region shaded

(b) Use set notation to represent the shaded region in the following diagrams:

(i)



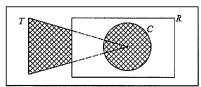
(2 marks)

TUC or TIC

Junites union of Tand C

Juntes the complement of this union

(ii)



(2 marks)

CU (TOR)

Vwrites the union with C

I writes the intersection

of T with the complement of R

See next page

CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 11

Question 6 continued

(c) A student is selected at random from the group of.56 students. Write an expression for the **probability** that this student plays hockey given that they play football.

7

$$P(H|F) = \frac{x}{x+15}$$

(2 marks)

Vapplies the probability of the conditional event H given F. Varites correct expression in terms of x.

(d) If playing hockey and playing football are independent events, determine the possible value(s) of x.
(3 marks)

If H and F are independent events, then P(H|F) = P(H)

$$\therefore \frac{\varkappa}{\varkappa+15} = \frac{\varkappa+12}{56}$$

CAS SOLVE: x=9 or x=20

(R) If H and F are independent events , then $P(H \cap F) = P(H) \times P(F)$

$$\frac{x}{56} = \frac{x+12}{56} \times \frac{x+15}{56}$$

CAS SOLVE:
$$x=9$$
 or $x=20$

V states the condition for independent events correctly in terms of H and F

V forms correct expressions in terms of x

V solves correctly to give both values of x.

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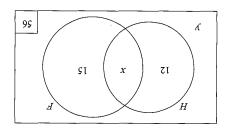
MATHEMATICS METHODS Year 11

CALCULATOR-ASSUMED

Question 2 continued

(8 marks) g uonseno

number of students who play either hockey, football or both. For a particular group of 56 Year 11 students, the Venn diagram shown below indicates the



Describe in words what this means in this specific context. $(a) The diagram indicates that <math> (A \cup F) = y$. (a)

Mere are y students who do not play either hockey or football.

broughots trongo sofoten

(j wsik)

(2 marks) Write an expression for the probability that this student plays hockey or football. A student is selected at random from the group of 56 students.

See next page

$$\frac{1}{\sqrt{1+x+1}} = (3)$$

$$\frac{1}{8} - \frac{1}{1} = (4)$$
 (3)

Vapplies the probability of the union consectute a correct expression in terms

(z warks)

V justifies their answer

Suft 21 franchets out 1stats/

(i) R and R are mutually exclusive.

State whether the following statements are true or false. Justify your answer.

True.

Since RNR = \$

ton oh A had a sett to the A do not the sett of the setting the New devilopment.

(z marks)

(ii) R and C are independent events.

A to tood as is a since () A) A

Also , P(R) < 1 (from Venn diogram)

: P(R/c) + P(R)

Hence R and C are NOT independent events.

Vintifica their ensurer solid is thomstate out estate **CALCULATOR-FREE**

MATHEMATICS METHODS Year 11

Question 3

(6 marks)

The 6th, 7th and 8th rows of Pascal's triangle are shown below. This information may be used to answer the questions that follow.

(a) Evaluate
$$\binom{8}{2}$$
. = 28 (1 mark)

Vstates arrest value

(b) Evaluate
$$\binom{9}{4}$$
 = 56 + 70 (2 marks)
$$= \frac{126}{4}$$
Vuses value in 8th row to correctly determine the value in the 9th row
$$V \text{ states correct Value}$$

(c) If
$$(1-2x)^6 = a+bx+cx^2 + ...$$
 determine the value for a,b and c . (3 marks)
$$(1-2x)^6 = 1^6 + 6(1)^5(-2x) + 15(-2x)^2 + ...$$

$$= 1 - 12x + 60x^2 + ...$$

Vomett value for a Vannect value for b V correct value for C

End of Questions

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MATHEMATICS METHODS Year 11

Question 5 continued

Determine the following probabilities:

$$(i) \qquad P(W_2 \mid R_1) \quad = \quad \frac{4}{7}$$

5

Verrest numerator Lamest denominator

(2 marks)

(2 marks)

$$P(R_1 \cap W_2)$$
 (2 marks)
$$= P(R_1) \times P(W_2 \mid R_1)$$

$$= \frac{3}{5} \times \frac{4}{7} = \frac{12}{35} \quad \text{or} \quad 0.34 \text{ (2dp)}$$
 from (b) and (c)(i).

Variety probability

(iii)
$$P(W_2)$$
 (2 marks)
$$= \frac{3}{5} \times \frac{4}{7} + \frac{2}{5} \times \frac{5}{7}$$

$$= \frac{22}{35} \quad \text{or} \quad 0.6285$$

$$= \frac{22}{35} \quad \text{or} \quad 0.6285$$

$$\text{Correct probability}$$

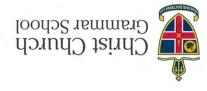
Determine the probability that a white ball was selected from Bag 1, given that a white ball is selected from Bag 2. (2 marks)

$$P(W_1 | W_2) = \frac{\frac{2}{5} \times \frac{5}{7}}{\frac{2^2}{35}}$$

$$= \frac{5}{11} \quad \text{or} \quad 0.4545$$

Forms correct conditional probability Varrect probability

TEST 4 2019



MATHEMATICS METHODS Year 11

Calculator-assumed Section Two:

Your name

Teacher's name

Time and marks available for this section

26 marks 25 minutes 4 minutes

SOLUTIONS & MARKING KEY

Working time for this section: Reading time for this section:

Marks available:

To be provided by the supervisor Materials required/recommended for this section

This Question/Answer Booklet

Formula Sheet (retained from Section One)

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

in the ATA examinations drawing instruments, templates and up to three calculators approved for use Special items:

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> (11 marks) MATHEMATICS METHODS Year 11

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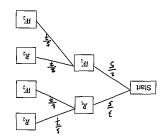
Guestion 5

An experiment is conducted using two separate bags, Bag 1 and Bag 2.

Bag 2 has 2 red and 4 white balls. Bag 1 has 3 red and 2 white balls.

Then a ball is randomly selected from Bag 2. A ball is randomly selected from Bag 1 and is then placed into Bag 2.

A tree diagram can be drawn showing the possibilities:



Note: R_1 is the event a red ball was selected from Bag 1.

R₂ is the event a red ball was selected from Bag 2.

complementary events. Explain why events R_1 and W_1 are considered to be both mutually exclusive and

They are mutually exclusive since $P(R, N, N_i) = 0$ is, both connot occur simultaneously.

They are complementary since $P(R,UW_1) = 1$ or $P(R_1) = 1 - P(W_1)$

VStates why Al and WI are complementary Vistates why R, and W, one mutually exclusive

philidadorg tremos

(1 mark)

(b) Determine $P(R_1)$

b(k1)= 3 or 0.6

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See next page

CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 11

Question 4

(5 marks)

Two events M and N are such that:

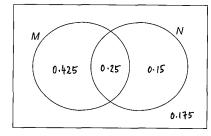
P(M) = 0.675

 $P(M \cap N) = 0.25$

 $P(\overline{M} \cap N) = 0.15$

(a) Complete the Venn diagram below.

(2 marks)



Lurites 0.425 and 0.25 in the correct spaces

/ Writes 0.15 and 0.175 in the correct spaces

(b) Determine $P(M \cup N)$

(1 mark)

$$P(MUN) = 0.675 + 0.15$$

= 0.825

Varrect answer

(c) Determine P(N|M)

(2 marks)

$$P(N|M) = \frac{0.25}{0.675}$$
= $\frac{10}{27}$ or 0.37 (2d.p.)

Vorrect numerator (10)

V correct denominator (27)