

# Semester One Examination, 2018

						Que	stic	n/Ar	swe	r bo	ok
MATHEMA METHODS UNIT 3,4 Section One: Calculator-fro	3			equired lace yo							
Studer	nt number:	In figures									
		In words	_								
		Your name	е _								
Fime allowed Reading time before Working time:			five m								
Materials req To be provided to This Question/And Formula sheet	by the super		ed for	this	secti	on					
To be provided to Standard items:	by the candi pens (blue/ correction f	black prefer					oured	l), sha	rpene	r,	
Special items:	nil										

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that
you do not have any unauthorised material. If you have any unauthorised material with you, hand
it to the supervisor before reading any further.

TRINITY COLLEGE 2 METHODS UNIT 3,4

# Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

SEMESTER 1 2018 CALCULATOR FREE

# Instructions to candidates

- The rules for the conduct of Trinity College examinations are detailed in the Instructions to Candidates distributed to students prior to the examinations. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Supplementary pages for the use of planning/continuing your answer to a question
  have been provided at the end of this Question/Answer booklet. If you use these pages
  to continue an answer, indicate at the original answer where the answer is continued,
  i.e. give the page number.
- 5. Shor all your working clearly. Your working should be in afficient cleast to allow your answers to be decided ready and for marks to be warded for readying incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question work more than two marks, valid working or sufficient on required to neceive full marks. If you repeat any question, ensure that you cancel the answery out of not with to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

See next page

RINITY COLLEGE	11	SEMESTER 1 20
IETHODS UNIT 3.4		CALCULATOR FR

Supplementary page

Question number: \_\_\_\_\_

TRINITY COLLEGE METHODS UNIT 3,4

SEMESTER 1 2018 CALCULATOR FREE

(8 mark:
Two houses, P and Q, are 900 m apart on either side of a straight railway line A.C. A.C is the
perpendicular bisector of PQ and the midpoint of PQ is B. A small train, R, leaves station C and
travels towards B, 1200 m from C.



Let  $\angle PRB = \angle QRB = \theta$ , where  $0 < \theta < 90^{\circ}$ , and X = PR + QR + CR, the sum of the distances of the train from the houses and station.

the train from the houses and station. (a) By forming expressions for PR, BR and CR, show that  $X=1200+\frac{450(2-\cos\theta)}{\sin\theta}$ . (3 marks)

(b) Use a calculus method to determine the minimum value of X.

End of questions See next page

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

A particle travels in a straight line so that its distance x cm from a fixed point  $\theta$  on the line after t seconds is given by  $x = \frac{t^2}{2t+1}, t \ge 0.$ 

Working time: 50 minutes.

Calculate the acceleration of the particle when t=1.

TRINITY COLLEGE METHODS UNIT 3,4 SEMESTER 1 2018 CALCULATOR FREE See next page See next page 35% (52 Marks) Section One: Calculator-free

(a) Determine 
$$\frac{\sqrt{h}}{h}$$
 (by wen  $y = \frac{1}{h}$  of  $y = h$  (b)  $y = h$  (c)  $y = h$  (c)  $y = h$  (c)  $y = h$  (d)  $y = h$  (d)  $y = h$  (e)  $y = h$  (f)  $y = h$  (f)  $y = h$  (e)  $y = h$  (f)  $y$ 

(d) Determine 
$$\frac{d}{d\tau} \epsilon^{1-\lambda} - 2\epsilon$$
 .

(a) Determine the area of the region enclosed by the curve and the coordinates axes.

(a) Determine  $\int 5(2x-1)^3 dx$ . The graph of  $y = (3 - 4x)^3$  is shown below. (e marks) Question 5 Question 4 SEMESTER 1 2018 CALCULATOR FREE TRINITY COLLEGE METHODS UNIT 3,4 SEMESTER 1 2018 CALCULATOR FREE TRINITY COLLEGE METHODS UNIT 3,4

(S marks)

TRINGY COLLEGE
THOSE UNITS 4.

4. SALCULATOR FREE

Question 2.

(S marks)
A function defined by  $f(z) = 13 + 18x - 6x^2 - 2x^3$  has stationary points at (1,23) and (-3, -41).

(a) Use the second derivative to show that one of the stationary points in a local maximum.

(b) Use the second derivative to show that one of the stationary points in a local maximum.

(c) a units (a) Use the second derivative to show that one of the stationary points in a local maximum.

(b) Determine the coordinates of the point of inflection of the graph of y = f(x). (2 marks)

(c) Determine the coordinates of the point of inflection of the graph of y = f(x). (2 marks)

See next page

See next page

 $-xp 91 + (x)^{2}\theta^{4}$  (ii)  $xp(x), \delta \int_{x}^{t}$  (i) (S marks) (2 marks) (c) Calculate E(X). (2 marks) (b) Construct a table to show the probability distribution of X. (a) By listing all possible combinations (135, 137, etc.), determine  $P(X \le 7)$ . .(5) $\theta$  enimeted (6) (2 warks) xod and month which the relations of the relation of the relations of the same time and the random variables of the random variables of the largest of the three and the random variables of the rand The function g is such that  $g'(x)=ax^2+18x+b$ , it has a point of inflection at (-1,29) and a stationary point at (1,-19). (e marks) (9 marks) Question 6 SEMESTER 1 2018 CALCULATOR FREE TRINITY COLLEGE METHODS UNIT 3,4

See next page

See next page