BSHS SCHOOL

Sems 2 Examination, 2012

Question/Answer Booklet

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	V10-21	J. 17. 10 V V	In words
_	671	MACHINO	Your name

MATHEMATICS 2C/2D

Student Number:

Section Two:

Calculator-assumed

Time allowed for this section

setunim benbrud eno Working time for this section: Reading time before commencing work: ten minutes

To be provided by the supervisor Materials required/recommended for this section

Formula Sheet (retained from Section One) This Question/Answer Booklet

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters

Council for this examination. and up to three calculators satisfying the conditions set by the Curriculum Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

Important note to candidates

examination room. If you have any unauthorised material with you, hand it to the supervisor that you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be used in this section of the examination. It is your responsibility to ensure

before reading any further.

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CALCULATOR-ASSUMED

Structure of this paper

Section	Number of questions available	Number of questions to be answered Working time (minutes)		Marks available	Percentage of exam	
Section One: Calculator-free	7	7	50	50	33	
Section Two: Calculator-assumed	12	12	100	100	67	
			Total	150	100	

Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2012. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages
 are included at the end of this booklet. They can be used for planning your responses
 and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question(s) that you are continuing to answer at the top of the page.
- 3. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 4. It is recommended that you do not use pencil, except in diagrams.

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CALCULATOR-ASSUMED

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MATHEMATICS 2C/2D

Additional working space

CALCULATOR-ASSUMED

(100 Wsrks)

Section Two: Calculator-assumed

This section has twelve (12) questions. Answer all questions. Write your answers in the spaces

3

Working time for this section is 100 minutes.

(2 marks) (7 marks)

Question 8

(a) Write down a recursive rule for the arithmetic sequence 35, 29, 23, 17, ...

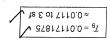
- (b) A different sequence is defined by $T_{n+1} = 0.25 \times T_n$, $T_1 = 768$.
- Write down the first three terms of this sequence.

(1 mark)

(S marks)

3781.0 . ∏ nwob ejhW (ii)

(5 marks) (iii) Calculate T_9 , rounded to 3 significant figures.



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CALCULATOR-ASSUMED

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MATHEMATICS 2C/2D

Additional working space

Question number:

CALCULATOR-ASSUMED

Question 9

(7 marks)

The cost per unit of gas used by residential customers in a city depends upon their average daily consumption, as shown in the table below.

Residential Customers	Prices including GST			
Supply charge	18.54 cents per day			
The first 12 units used on average per day	12.79 cents per unit			
Over 12 units used on average per day	11.54 cents per unit			

- (a) A consumer used an average of 9 units of gas per day over a period of 91 days.
 - (i) Calculate the supply charge for a period of 91 days.

91×0.1854 = \$16.87

(1 mark)

(ii) Calculate the cost of using 9 units per day for 91 days.

91×9×0.1279 = \$104.75

(1 mark)

(iii) Calculate the total of the supply charge and gas cost for this consumer. (1 mark)

16.87 + 104.75 = \$121.62

- (b) Another consumer used a total of 900 units of gas over a period of 60 days.
 - (i) How many units did they use on average per day?

(1 mark)

900 ÷ 60 = 15

(ii) Calculate the total of the supply charge and gas cost for this consumer. (3 marks)

 $60 \times 0.1854 = \$11.12$

 $60 \times 12 \times .1279 = \92.09

60×3×.1154=\$20.77

Total = \$123.98

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CALCULATOR-ASSUMED

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MATHEMATICS 2C/2D

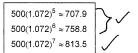
Question 19

(10 marks)

- (a) A and t are related by the formula $A = 500(1.072)^t$
 - (i) Evaluate A when t = 5, 6, and 7.

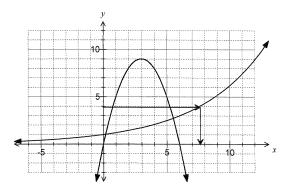
(2 marks)

(2 marks)



(ii) Estimate the solution to $500(1.072)^t = 800$ if t must be a whole number. (1 mark)

(b) The graph of $y = 1.2^x$ is drawn below.



(i) Show use of the graph to solve the equation $1.2^x = 4$.

0 ne for answer (2 marks)

One for line
drawn on graph about

(ii) Add the graph of y = x(6-x) to the axes above. $\sqrt{\frac{1}{3}}$ both x integer (3 marks $\sqrt{\frac{1}{3}}$ Symmetry area x = 3

ii) Explain how to use the two graphs above to solve the equation $x(6-x) = 1.2^x$, and state how many solutions there are. There are no marks for solving the equation.

Read from the x-axis the x-coordinates of the points of intersection of the two curves. There are 2 solutions for x.

End of questions

(ii) the probability that they own a dog given that they own a cat. (z marks) %Z9 (1 mark) b(D∩C) If a household is chosen at random, determine Households owning dogs but not cats. (1 mark) Describe the pet ownership of members of the set $\overline{C} \cap D$. %91 (J wsuk) (b) What percentage of households owned both dogs and cata? 52 91 (04) a 001=(U)n (a) Express this information using a Venn diagram, completing any missing entries. (3 marks) dogs (set D), 27% own cats (set C) and 48% own neither. In a recent survey of Australian households (the universal set U), it was noted that 40% own

Question 10

CALCULATOR-ASSUMED

(8 marks)

MATHEMATICS 2C/2D

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MATHEMATICS 2C/2D 16 CALCULATOR-ASSUMED

Guestion 18 (6 marks)

A motoring club is planning an event and wants to know what its members would like. They plan to ask 80 members, chosen at random, from the total membership of 885 people.

(a) An extract from a table of three-digit random numbers is shown below:

601 187 280 860 486 467 601 672 713 046

Choose one of the numbers from the list and explain how the club could use it to

517 - Number the members from 1 to 685 and then pick member 517.

ii) How many numbers in the above list could be used to select a sample? Explain your answer. (2 marks)

5 Add: :

Six of the numbers are no more than 685, but one

(109) is repeated, which leaves five to use.

One of the questions that the club plans to sak is the age of the member. They know that the youngest is 17 and that the oldest member is 63. Two possible data summary tables are shown below:

A npised

	69 - 09
	50 - 28
	61 - 01
Frequency	əgA
g u	gisəQ

	99 - 99
	99 - 97
	36 - 46
	25 - 35
	12 - 22
Frequency	əgA
Αu	gisəQ

(i) State one disadvantage of using Design A.

Not clear into which age group a member aged 25, 35, etc would go.

(ii) State one disadvantage of using Design B. (1 mark)

Too few groups - likely that most members would go into the middle group.

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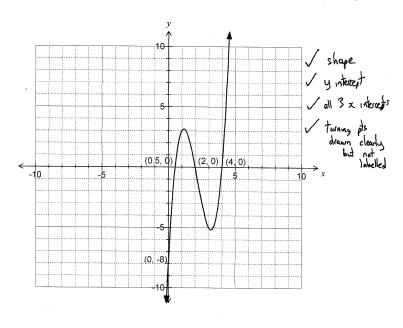
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CALCULATOR-ASSUMED

Question 11

(4 marks)

On the axes below, draw the graph of $y = 2x^3 - 13x^2 + 22x - 8$, labelling all axes intercepts. (4 marks)



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CALCULATOR-ASSUMED

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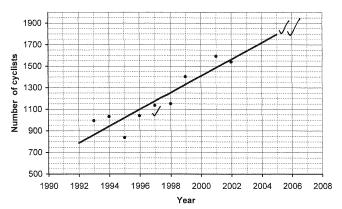
MATHEMATICS 2C/2D

Question 17

(8 marks)

The graph below shows the average weekday cyclist traffic flow on Bridge Road from 1993 to 2002. Data was not available for 1997 and 2000.

Average weekday cyclist traffic flow on Bridge Road, 1993 - 2002



(a) What was the average weekday cyclist traffic flow in 1994?

(1 mark)

(b) The average weekday cyclist traffic flow in 1997 was 1135. Add this point to the graph.

See graph above (1 mark)

(c) Draw a trend line on the graph.

(2 marks)

(2 marks)

(d) Use your trend line to estimate the average weekday cyclist traffic flow in:

(i) 2000 (1 mark)
(ii) 2004 (1 mark)

(e) Comment, with reasons, on the reliability of each of your predictions in (d).

Prediction for 2000 is reliable as is interpolated and relationship is strong. Prediction for 2004 is not reliable as is extrapolated.

CALCULATOR-ASSUMED

(8 msrks) Question 12 L

- that it reaches 2.8 m up the wall. A straight ladder, 3.5 m long, stands on level ground and leans against a vertical wall so
- (J mark) Sketch a diagram of the ground, wall and ladder, showing all given measurements.

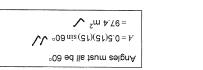


(S marks)

(3 marks)

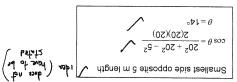
Calculate the angle that the ladder makes with the ground.

- is then stretched out tightly on level ground to form a triangle. The two ends of a length of rope are fied together to make a loop of length 45 m. The loop
- (i) Calculate the area of this triangle, if it has three equal sides.





(3 marks) 20 m long. Calculate the size of the smallest angle in the triangle, if two of the sides are both





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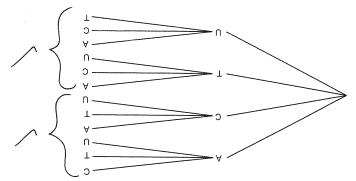
CALCULATOR-ASSUMED かし MATHEMATICS 2C/2D

A student wants to watch two different movies over the weekend, one on Saturday and one on (7 marks) Question 16

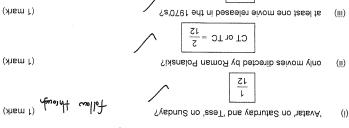
Sunday. They have four movies to choose from, listed in the table below:

	Rating	Year Released	Director	9ivoM
	ÐЫ	5005	James Cameron	TefevA
	M	⊅ 761	Roman Polanski	Chinatown
200	94	6761	Roman Polanski	Tess
	БЯ	6761	Pete Docter	qU

(5 msrks) Draw a tree diagram to show all the different orders they could watch two of these movies



Given that all orders are equally likely, what is the probability that the student watches



(5 marks) (iv) the movie 'Up', given that both movies they watched were rated PG?



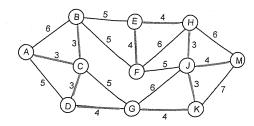
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CALCULATOR-ASSUMED

Question 13

(11 marks)

Each number on the network below represents the distance, in kilometres, between adjacent vertices



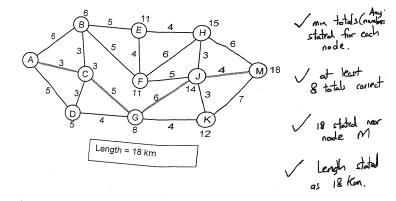
Find the length of the minimum spanning tree of the network above, clearly indicating the tree on the diagram.

(3 marks

V at least 8 segments labelled concepts

at least 9 segments concept Length = 35 km I all segments correct with 25 km.

The network below is a copy of the one above. Determine the length of the shortest path added to the diagram to show that a contact and has been used. (4 marks added to the diagram to show that a systematic method has been used. (4 marks)



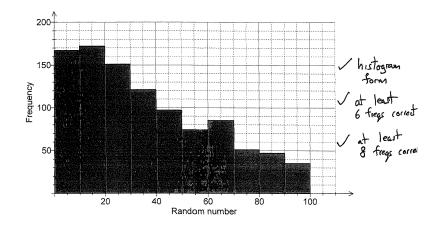
CALCULATOR-ASSUMED

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MATHEMATICS 2C/2D

Construct a frequency histogram for the 1000 numbers on the axes below.

(3 marks)

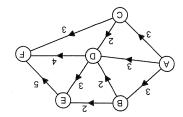


Use the above information to state whether the circuit designer's claim, that all numbers have an equal chance of being chosen, is justified. Explain your answer. (2 marks)

> No. If all numbers had an equal chance of being chosen then one would expect roughly equal numbers in each group for such a large number of trials, but it can be seen that this is not the case.

CALCULATOR-ASSUMED

(c) The following network shows the maximum number of daily flights between sirports A to F in an easterly direction.



If each flight can carry 300 passengers, what is the maximum number of passengers that can be carried from A to F in a day? Systematic working must be shown to be awarded full marks)



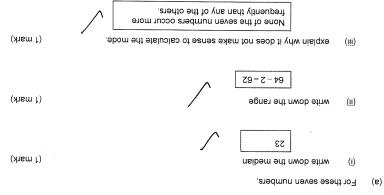
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MATHEMATICS 2C/2D 12 CALCULATOR-ASSUMED

(12 marks)
An electronics student built a circuit and display to generate random numbers from 0 to 99. The

circuit designer claimed that all numbers had an equal chance of being chosen.

The first seven numbers generated by the circuit were 12, 5, 41, 64, 37, 2 and 23.

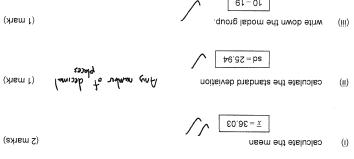


To thoroughly test the circuit, 1000 numbers were generated and summarised in the table below.

35	74	19	98	₽Z	Z 6	121	191	172	491	Frequency
66-06	68-08	67-07	69-09	69-09	6t-0t	30-38	50-29	61-01	6-0	Number

(b) For these 1000 numbers,

(i) calculate the mean (2 marks)



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CALCULATOR-ASSUMED

Question 14

(11 marks)

A newspaper contained an advertisement for a laptop computer with a cash price of \$999.

- (a) The computer could also be bought on credit over three years by weekly payments of \$11.92, subject to approval.
 - (i) Assuming there are 52 weeks per year, how much would the computer cost if bought on credit? (1 mark)

(ii) How much interest is paid using the credit terms? (Assume that the interest is the extra amount paid when buying the computer on credit instead of cash). (1 mark)

(iii) Calculate the simple interest rate that would generate the interest calculated in (ii) on the cash price over the credit period. (3 marks)



The same newspaper carried another advertisement from a lender offering unsecured loans for amounts up to \$3000 at a rate of 15.9% pa with interest compounded monthly.

(b) How much interest would accumulate on a loan of \$999 over three years, if no repayments were made? (3 marks)

$$F = 999 \times \left(1 + \frac{15.9}{100 \times 12}\right)^{12 \times 3}$$

$$= 1604.59$$

$$I = 1604.59 - 999$$

$$= $605.59$$

follow through

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CALCULATOR-ASSUMED

MATHEMATICS 2C/2D

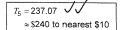
(c) The recursive formula $T_{n+1}=0.75T_n$, $T_0=999$ can be used to calculate the value of the laptop computer after n years.

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(i) What annual rate of depreciation does this formula use?

 $100 \times (1-0.75) = 25\%$

ii) Calculate the value of the computer after five years, rounded to the nearest \$10.



No need to round.

(Roundown has been assessed elsewhere)