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Question/Answer booklet Semester One Examination, 2019

Calculator-free Section One: E TINU **METHODS MATHEMATICS**

NOILHTOS

Your name:_

Friday Smith

Time allowed for this section

Teacher name (circle one):

Working time: Reading time before commencing work:

fifty minutes sətunim əvit

To be provided by the supervisor Materials required/recommended for this section

This Question/Answer booklet

Formula sheet

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

Special items:

Important note to candidates

it to the supervisor before reading any further. you do not have any unauthorised material. If you have any unauthorised material with you, hand No other items may be taken into the examination room. It is your responsibility to ensure that

METHODS UNIT 3

CALCULATOR-FREE

Supplementary page

Question number:

15

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available
Section One: Calculator-free	8	8	50	51
Section Two: Calculator-assumed	13	13	100	96

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams

	Markers use only				
	Question	Maximum	Mark		
	1	6			
	2	8			
	3	8			
	4	5			
Э	5	4			
9	6	8			
	7	5			
	8	7			
	S1 Total	51			

- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

CALCULATOR-FREE	11	METHODS UNIT
Supplementary page		
Question number:		

 $A = \begin{cases} \frac{1}{x} + 10 & dx \end{cases}$ $= \begin{cases} \frac{1}{x} + 10x \end{cases}$ $= \begin{cases} \frac{1}{x} +$ underaune xp al + 2K - 1 = Y (3 marks) Determine the area of the region enclosed by the curve, the x-axis, the line x=1 and the (q) 1 = 1 = 10 States equation when rate of integration λ in the rate of λ in (3 marks) Determine the equation of the curve. The curve shown below passes through the point (1, 2) and is such that $\frac{dy}{dx} = \frac{16}{x^3}$ (e marks) Question 1 Working time: 50 minutes. This section has eight (8) questions. Answer all questions. Write your answers in the spaces (51 Marks) Section One: Calculator-free **METHODS UNIT 3** 3 CALCULATOR-FREE

spuno9 xp x+1/2/1 (x) f from (x) fwork which $\frac{1}{2} = \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} + \frac{1}$ Thinky to day referred from part (a) or otherwise, determine $\int_{a}^{x} \frac{x}{\sqrt{4+x}} dx$. (2 warks) (b) Part of the graph of $y = \frac{x}{x + \hbar V}$ is shown below. $\frac{x+4}{x+4} = \frac{x+4}{x+4} =$ (a) Determine $\frac{d}{dx}(2x\sqrt{4} + x)$. (S marks) (7 marks) Question 8 CALCULATOR-FREE **METHODS UNIT 3** TO

End of Section 1 Questions

BUOHS HOU

V world

CALCULATOR-FREE

4

METHODS UNIT 3

(8 marks) Question 2 A calculator program will generate a single random integer n, where $3 \le n \le 12$. The program is run once, and the discrete random variable X is the number of fours or fives obtained.

Explain why X is a Bernoulli random variable. Marks iwavoled for VERY

Two mutually exclusive and exhaustive (2 mark)

Methors

Outcomes from a single trial

2 possible $\chi = \begin{cases} 1 & \text{if out come } 4 \text{ or } 5 \end{cases}$ Values

(2 mark)

Methors

Anter

Canhaustive

(b) Determine P(X = 1). (1 mark)

$$P(\chi=1) = \frac{2}{10} = \frac{1}{5}$$

Determine the mean and standard deviation of X.

(2 marks)

Standard devighor

2xtensive

answer

The random variable Y is the number of fours or fives obtained in three consecutive runs of the program.

Determine $P(Y \leq 1)$.

(3 marks)

$$P(Y \le 1) = P(Y = 0) + P(Y = 1)$$

$$= (\frac{4}{5})^{3} + (\frac{4}{5})^{2}(\frac{1}{5}) \times 3$$

$$= (\frac{64}{125})^{3} + (\frac{4}{5})^{2}(\frac{1}{5}) \times 3$$

$$= \frac{64}{125} + \frac{48}{125}$$

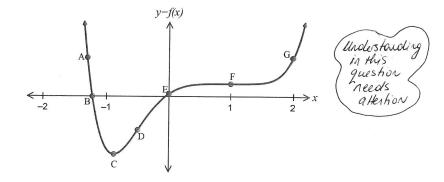
$$= \frac{112}{125}$$

$$Clear reasoning for 3 marks$$

CALCULATOR-FREE

METHODS UNIT 3

Question 7 Consider the function y = f(x) shown below. The points, A, B, C, D, E, F and G each lie on the graph.



(a) Which point/s labelled on the graph above satisfy the following,

(i) a point of inflection occurs?

(ii) f'(x) = 0 and $f''(x) \neq 0$?

(iii) f is increasing and f "(x) < 0?

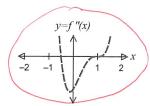
(iv) f(x) > 0 and the function is concave up?

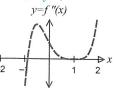
A, 6

(b) Circle the graph below that represents f''(x).

y=f''(x)

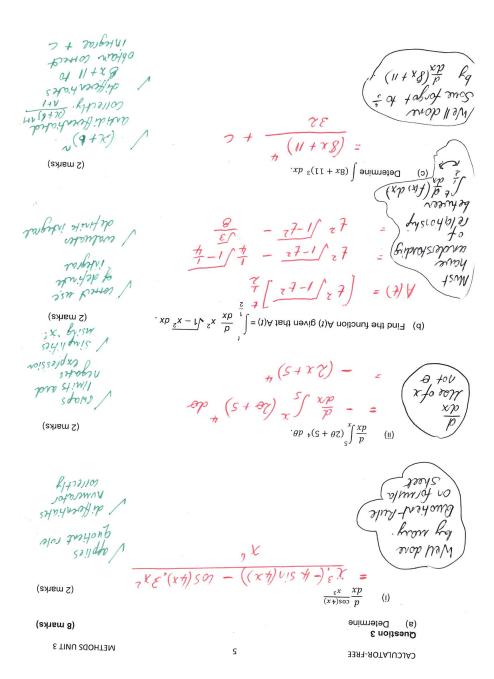
wrect graph





(1 mark)

(1 mark)



Vehill is 275 m from a $\frac{1}{9}$ $\frac{1}$ Tew mueroled o [401 + 2 + E7-] de leguires (4) x of 1 pp of + 18 + 17 - 0 = (7) X reget short Gree Both all $(\tau+2)(s-2) - = 0$ (with sation) 01 + 78 + 27 - = 0 1 jaun 425 (b) Determine how far from Q the vehicle first comes to rest for t > 0. (2 marks) 1-SW 9 = (4) 1 01 +27-78 = (7)1 SWO/ = 12 tof 23V/02 V 2+27-7E = 20 TY-E S= (7) A Determine the velocity of the vehicle when t=4. (3 marks)

acceleration of the vehicle is given by 3-2t ms², where t is the time in seconds since the

8

(8 marks)

METHODS UNIT 3

A vehicle travelling in a straight line has a velocity of $10~\mathrm{ms}^{-1}$ as it leaves point Q. The

vehicle left Q.

Question 6

CALCULATOR-FREE

CALCULATOR-FREE

6

METHODS UNIT 3

Question 4

(5 marks)

Let $f(x) = 5x + \frac{k}{2x}$, x < 0 and k is a constant. The graph of y = f(x) has a stationary point when x = -3.

Determine the value of k.

$$f'(x) = 5 - \frac{K}{2x^2}$$

$$\sqrt{f'(x)}$$

mine the value of k.

Stationary point:
$$f'(-3) = 0$$

$$f'(x) = 5 - \frac{K}{2x^2}$$

$$f'(3) = 5 - \frac{K}{18} = 0$$

$$x = 90$$
(2 marks)

(2 marks)

$$\sqrt{f'(x)}$$

$$\sqrt{f'(x)}$$

Use the second derivative test to determine the nature of the stationary point. (3 marks)

$$f'(x) = 5 - \frac{45}{x^2}$$

Algard

In 3 Mark an

State
clearly
WHY Stationary
Point is a
Max eising

2nd derivative

$$f''(x) = \frac{90}{2(3)}$$

v t (x)

v uses <0

the stationary point is a

Maximum.

$$K = 90$$

CALCULATOR-FREE

7

METHODS UNIT 3

Question 5 (4 marks) A random variable X has a binomial probability distribution with a mean of \mathbb{Z} and variance of \mathbb{Z}

Determine the value of n and the value of p for this distribution.

(2 marks)

$$np = 12$$
 $np(p) = 3$
 $= 12(1p) = 3$
 $1-p = \frac{1}{4}$
 $p = \frac{3}{4}$
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Determine the mean and variance of the distribution Y, where Y = 5X + 3.3.

