Calculator Free Test 1 2018 ATMAM Mathematics Methods

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3	
2	

Name: Solutions

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Smith

I was of chaus role

I was of product rule

(1-)(x-3) x ris + x sou x-3 = 1/2 / (1-1)

x 415- = x500 xpp

V quotient rule demonstated

131

 $x \operatorname{uis}_{x-\theta} = \chi(b)$

 $\frac{x_{++}x}{x = 0} = \mathcal{K} (q)$

Marks

Friday

Teacher:

Time Allowed: 30 minutes

Materials allowed: Formula Sheet.

Where appropriate, answers should be given as exact values. All necessary working and reasoning must be shown for full marks. snoiteapt all questions.

Marks may not be awarded for untidy or poorly arranged work.

Differentiate each of the following with respect to x, clearly showing appropriate rules $\, \, {
m Do} \, {
m not} \, {
m simplify} \,$ [2,2,2,2] .I

I recipiosal term

I Polynowied ton

 $S + \frac{z^x}{z} - \varepsilon x \frac{z}{z} = \chi (b)$

1 + 2 x = 2 = 2 p

4+XE B

(x3)= (4+x8) = 2/p

 $(c) y = \sqrt{3x^2 + 4}$

(f) Determine the growth rate when the Population is 3 million.

000 012 2

000 000 E X £000

retained to store = 16

I growth rate

(e) Express the rate of growth as a function of P

= 16 916 persons/ year V contact rate.

(d) Determine the rate of growth after 10 years.

(c) Express the rate of growth as a function of t. $\frac{dd}{ddt} = 8 + 000 = 0.07 + 2.$

(b) Find how long it takes for the population to double in size.

(4) [1,1,1,1,1] .6

The population of a city over t years is given by $P=120\ 000e^{0.07t}$

voital boy to be

059 148

(a) Determine the population after 10 years.

End of Questions

Evaluate each of the following limits.

(a)
$$\lim_{h\to 0} \frac{e^{h}-1}{h}$$

I emplyates limit

(b)
$$\lim_{h\to 0} \left(\frac{\cos(x+h)-\cos x}{h}\right)$$

Vevaluates limit.

Determine the value of f''(-1) if $f(x) = (2x + 1)^5$.

Describe the concavity of the curve at this point.

$$f(x) = (2x+1)^{5}$$

$$f'(x) = 10(2x+1)^4$$

$$f''(x) = BO(2x+1)^3$$

Concave down as gradient function is decreasing of

f"(x) < 0 Would apply to a Maximum T.P.

Wich is concave down

Concavity With reason

8. [1,1,1,2,4]

On the Indonesian coast, the depth of water t hours after midnight s given by $D(t) = 9.3 + 6.8\cos(0.507t)$ metres $0 \le t \le 24$

(a) Find the depth of the water at 8 am.

Viorrect depth

(b) Determine the maximum height of the water during this time.

I max depth

(c) At what rate is the water changing at 8 am?

I correct rate g change

(d) At what time of day is water rising at its fastest rate?

one each
only Dif hours
only

(e) Show how to use calculus to determine the time(s) of day the height increasing at 1.5 metres per hour. Use your calculator to help you determine the time(s).

Peralise ONCE -1 no 2dp not 16.10 m -1 sounding accuracy -1 rate limit -1 units

/ differentiate 1 = 1.5 I solve fort V correct HMES

[t] t

Find the equation of the tangent to $y = 3 - \sin(1 - 2x)$ at the point where $x = \frac{1}{x}$.

wo wo how
$$\sqrt{\frac{4b}{x^2}}$$
 $\sqrt{\frac{4b}{x^2}}$ $\sqrt{$

Calculator Assumed ATMAM Mathematics Methods

Smith

Test 1 2018

1911103 SHENLON

Name: Soly 7101/5-

Friday Teacher:

6T/ Marks Time Allowed: 20 minutes

Materials allowed: Classpad, calculator, formula sheet.

Marks may not be awarded for untidy or poorly arranged work. Where appropriate, answers should be given to two decimal places. All necessary working and reasoning must be shown for full marks. Attempt all questions.

7. [1,1,1,1] (4)

The number of bees in a hive after t months is modelled by $B(t) = \frac{3000}{1+0.5e^{-1.73t}}$.

(0)9/

2000 62005 (a) Determine the initial bee population.

(b) Determine the percentage increase in its population after one month.

37 799°

19 GARASO

(c) Explain why the population is increasing over time.

8 (4) > 0 for all values of to surplace to should be take at which the population is increasing after 3 months.

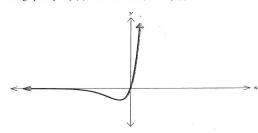
(d) Determine the rate at which the population is increasing after 3 months.

B.(3) = 14.38 bus/month.

WITH Take

5. [3,2,3]

The graph of y = f(x) is shown below, where $f(x) = 2xe^x$



(a) Determine the exact location of the stationary point on the graph of y = f(x).

$$f(x) = 2xe^{x}$$

$$f'(x) = 2x \cdot e^{x} + e^{x}(2)$$

$$= 2e^{x}(x+1)$$

$$f'(x) = 0 \quad \text{when } x = -1 \quad e^{x} > 0 \quad \text{for all } x$$

$$f(-1) = 2f(1)e^{-1}$$

$$\therefore \quad \text{Stationary point at } (-1, -\frac{2}{e})$$

(b) Apply the second derivative test to show that the stationary point in (a) is a minimum.

$$f''(x) = 2e^{x}(1) + (x+1) 2e^{x}$$

$$= 2e^{x}(2+x) 4e^{x} + 2xe^{x}$$

$$f''(-1) > 0 ... minimum stationary$$

$$point \sqrt{f''(x)}$$

$$\sqrt{apply test}$$

$$totrectly.$$

(c) The graph of y = f(x) has just one point of inflection. Determine the exact coordinates of this point.

this point.

$$f''(x) = 0 \text{ for point of inflection} \qquad \begin{array}{c} /f''(x) = 0 \\ \text{V check} \\ \text{Concavity} \\ \text{Check concavity} \\ \text{Check change of concavity} \\ \text{Check change of Inflection at } (-2, \frac{-4}{e^2}) \end{array}$$

6 [5] Given the graph of y = f'(x) provide possible graphs of y = f(x) and y = f''(x) [Care should be taken with the x values of critical points, but the 'heights' of the derivatives are not unique, use whatever makes your sketch easier to draw.]

