Mathematics Department Perth Modern Perth Modern Perth Modern Perth Modern Perth Modern



# Course Methods Test 3 Year 12

Formula sheet provided:	tud oN	some formulae given on page 2	
Task weighting:	<sub>bī</sub>	%	
Marks available:	8£	тыгка ——	
Special items:	Drawing A4 pape	g instruments, templates, notes on one unfolded sheet of er	
Standard items:		ılue/black preferred), pencils (including coloured), sharpener, ion fluid/tape, eraser, ruler, highlighters	
Materials required:	No class	speds	
Number of questions:	9	g	
Working time allowed for	orking time allowed for this task: 40 mins		
Reading time for this test	nim 2 : t	sı	
լցջk քλbe։	Kespon	noitsgitzevnl\esr	
Student name:		Тевсрег пате:	

Note: All part questions worth more than 2 marks require working to obtain full marks.

1 | Page

End of test Working out space

8 P A g e

## **Useful formulae**

### Logarithms

$x = \log_a b \iff a^x = b$	$a^{\log_a b} = b$ and $\log_a(a^b) = b$
$\log_a mn = \log_a m + \log_a n$	$\log_a \frac{m}{n} = \log_a m - \log_a n$
$\log_a(m^k) = k \log_a m$	$\log_e x = \ln x$

$\frac{d}{dx} \ln x = \frac{1}{x}$	$\int \frac{1}{x}  dx = \ln x + c,  x > 0$
$\frac{d}{dx}\ln f(x) = \frac{f'(x)}{f(x)}$	$\int \frac{f'(x)}{f(x)} dx = \ln f(x) + c,  f(x) > 0$

$\frac{d}{dx}\ln f(x) = \frac{f(x)}{f(x)}$		$\int \frac{f(x)}{f(x)}  dx = 1$	$\ln f(x) + c,  f(x) > 0$
	If $y = uv$		If $y = f(x) g(x)$
Product rule	then	or	then
	$\frac{d}{dx}(uv) = v\frac{du}{dx} + u\frac{dv}{dx}$		y'=f'(x) g(x) + f(x) g'(x)
	If $y = \frac{u}{v}$		$If y = \frac{f(x)}{g(x)}$
Quotient rule	then	or	then
	$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v\frac{du}{dx} - u\frac{dv}{dx}}{v^2}$		$y' = \frac{f'(x) g(x) - f(x) g'(x)}{(g(x))^2}$
	If $y = f(u)$ and $u = g(x)$	)	If $y = f(g(x))$
Chain rule	then	or	then
	$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$		y' = f'(g(x)) g'(x)
Fundamental theorem	$\left  \frac{d}{dx} \left( \int_{a}^{x} f(t)  dt \right) = f(x)$	and	$\int_{a}^{b} f'(x) dx = f(b) - f(a)$

### Q6 continued

iii) E(X) i.e the mean. (No need to simplify)

b) Derive the cumulative probability function  $P(X \le x)$  for  $0 \le x \le 10$ .

Perth Modern Mathematics Department

Q1 (2 & 2 = 4 marks)

a)  $\log_a b + 3\log_a (ab) - 4\log_a b$ . Express each of the following as a single logarithm.

b) 
$$\delta + 3 \log_5 c - \log_5 \left(c^3\right) + \log_5 b$$
.

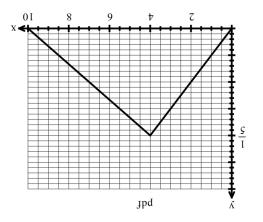
Q2 (2 & 2 = 4 marks) Solve each of the following, giving your answer in exact form.

Solve each of the following, giving your answer in **exact** form. a) 
$$2^{2x}-12(2^x)+32=0$$

 $1\mathcal{E} = \left( {^{2+x}} \nabla \right) \mathcal{E} + {^x} \nabla \right) (d$ 

Perth Modern Mathematics Department

Consider the continuous random variable X and its probability density function which is graphed Q6 (3, 3, 3 & 3 = 12 marks)



a) Determine the following exactly.

below.

(vilidmis of been oN).  $(\xi > X \mid \xi < X)^{q}$  (ii)

6 Page

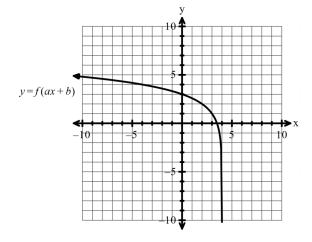
Q3 (1, 3 & 3 = 7 marks)

The Richter scale, R, of an earthquake of intensity I is given by  $R = \log_{10} \left( \frac{I}{I_o} \right)$  where  $I_o$  is a minimum intensity level used for comparison.

- a) Determine R for an earthquake with intensity  $10000I_a$ .
- b) An earthquake measuring 5 on the Richter scale is how many times as intense as that of one measuring 4 on the Richter scale?
- c) If an earthquake registers x on the Richter scale and a second earthquake registers x+4 on the Richter scale, how many more times as intense is the second earthquake?

#### Q4 (3 marks)

Consider the function  $f(x) = \log_2 x$  which undergoes a transformation f(ax+b) where a & b are constants. The graph y = f(ax+b) is plotted below, determine the values of a & b showing reasoning.



4 | Page

Q5 (3 & 5 = 8 marks) Consider the function  $g(x) = (x^2 + 3) \ln(x^3 + 3x)$ .

Mathematics Department

a) Determine g'(x).(Simplify)

b) Use the result from part a to determine  $\int 2x \ln(x^3 + x) dx$ .