

Time:	20 minutes
Total Marks:	19 marks



**Year 12 Methods**  
**Review Response 2**  
Wednesday Sept 8th 2021

**Resource Free**  
**ClassPad calculators are Not permitted.**  
**Formulae Sheet is Permitted.**

Name:
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1. (2, 2 = 4 marks)  
Find  $\frac{dy}{dx}$  for each of the following. Do not simplify.

a)  $y = \log_e (x + x^2 + x^3)$

b)  $y = x^2 \ln(2x)$

14. (2, 1 = 3 marks)  
232 fish from a local lake were captured, tagged and released back into the lake. 150 fish were captured in a second sample and 35 were found to have a tag.  
a) Find an approximation for the total number of fish in the lake.

b) Give an assumption that needed to be made for the above capture-recapture process to produce a valid estimation for the population of fish in the lake.

2. (1 marks)

Solve  $3^x = 5$  giving the exact answer using base ten logarithms.

3. (3 marks)

Find an expression (which does not contain log functions) for  $p$  in the following.

$$3 - 2 \log_3 y = \log_3 p$$

4. (2 marks)

A continuous random variable  $X$  is uniformly distributed on the interval  $-2 \leq X \leq 4$ .

Determine  $P(X \leq 2 \mid X \geq 1)$ .

12. (2, 3 = 5 marks)

A particle moves in a straight line such that its displacement from a fixed point O, at time  $t$  seconds ( $t \geq 0$ ), is  $x$  metres where  $x = 8 \ln(1 + t) - 3t$ .

a) Find  $t$  when the velocity is zero.

b) Find  $t$  when the velocity (m/s) is numerically equal to the acceleration (in  $\text{m/s}^2$ ).

13. (2, 1 = 3 marks)

The discrete random variable  $X$  is binomially distributed with  $X \sim \text{Bin}(n, p)$ . If  $E(X) = 50$  and  $\text{SD}(X) = 5$  find  $n, p$  and  $P(X \leq 50)$  giving the last of these correct to 4 decimal places.

10. (2, 1, 1 = 4 marks)

A random variable  $X$  has probability density function:

$$f(x) = \begin{cases} ae^{-3x} & \text{for } x > 0 \\ 0 & \text{elsewhere} \end{cases}$$

a) Solve for  $a$

b) Find the mean of  $X$

c) Find the variance of  $X$

Let us suppose that the monthly rainfall in a region is normally distributed with a mean of 120.2 mm and a standard deviation of 13.1 mm. In a year, how many months would you expect this region to have a rainfall that is a between 130 mm and 150 mm?

11. (3 marks)

$$\log_3 \left( \frac{a^2 b^3}{9} \right)$$

If  $\log_3 a = p$  and  $\log_3 b = q$ , express the following in terms of  $p$  and/or  $q$ .  
7. (2 marks)

6. (2 marks)  
Evaluate  $\log(100) - \ln(e^{-3})$ .

$$y = \ln \left( \frac{\cos(x)}{e^{2x}} \right)$$

5. (3 marks)  
Differentiate the following. Simplify your answers.

8. (2 marks)

If  $P = 5e^{(t-1)}$  find an exact expression for  $t$  in terms of  $P$ .



<b>Time:</b>	25 minutes
<b>Marks:</b>	21 marks

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#### **Resource Assumed**

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9. (3 marks)

Through geological surveys and test drilling, a company discovers a new oil field off the coast Cottesloe. The experts predict that profitable extraction of the oil can be carried out and that in any one year this extraction will reduce the quantity of oil remaining in the field by 10% of what it was at the beginning of that year. Extraction will become unprofitable when just 45% of the original quantity remains. For how many years can the company expect the field to remain profitable?