

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

#### Important note to candidates

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler.

#### To be provided by the candidate

Formula sheet.

Question/answer booklet for Section One.

#### To be provided by the supervisor

#### Material required/recommended for this section

Working time for paper: 50 minutes

Reading time before commencing work: 5 minutes

#### Time allowed for this section

Teacher

Name

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Student Number

(Calculator Free)

Section One

## MATHEMATICS 3C/3D

Question/Answer Booklet

Semester 1 Examination 2011

PERTH MODERN SCHOOL  
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further.

**Structure of this examination**

	Number of questions	Working time (minutes)	Marks available
This Section (Section 1) <b>Calculator Free</b>	<b>6</b>	<b>50</b>	<b>40</b>
Section Two Calculator Assumed	12	100	80
Total marks			120

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**Instructions to candidates**

1. The rules for the conduct of WACE external examinations are detailed in the booklet *WACE Examinations Handbook*. Sitting this examination implies that you agree to abide by these rules.
2. Answer the questions in the spaces provided.
3. Spare answer pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.
4. Show all working clearly. Any question, or part question, worth more than 2 marks requires valid working or justification to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

No, since  $-1 < x \leq 0$ 

[I]

(I, I') lies on the curve defined by  $f(g(x))$ .

(b)

Without substituting any values in  $f(g(x))$ , determine whether or not the point

$$\begin{aligned} f(g(x)) &= \sqrt{\frac{x+1}{2}} - 2 \\ (\text{III}) \quad f(g(x)) & \\ [2] \end{aligned}$$

$$\begin{aligned} \{y \in R : y \geq 0\} \\ \{x \in R : x \geq 2\} \\ (\text{II}) \quad f(x) \\ [2] \end{aligned}$$

[I]

$$\begin{aligned} \{y \in R : y \neq 0\} \\ \{x \in R : x \neq -1\} \\ (\text{I}) \quad g(x) \\ [2] \end{aligned}$$

(a) Determine the domain and range of:

A function is defined by the rule  $y = f(g(x))$ , where  $f(x) = \sqrt{x-2}$  and  $g(x) = \frac{x+1}{2}$ .**Question 1****[5 marks]**

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- Suggested working time for this section is 50 minutes.
- Counting: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Share pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

This section has **five (5)** questions. Answer all questions. Write your answers in the space provided.

**Section One (calculator-free) 40 Marks**

**Question 2**

(a) Solve the equation below:

$$\frac{10}{x+1} + \frac{2}{x-3} = 4$$

[3]

$$\frac{10(x+1)(x-3)}{x+1} + \frac{2(x+1)(x-3)}{x-3} = 4(x+1)(x-3)$$

$$10(x-3) + 2(x+1) = 4(x^2 - 2x - 3)$$

$$10x - 30 + 2x + 2 = 4x^2 - 8x - 12$$

$$0 = 4x^2 - 20x + 16$$

$$0 = x^2 - 5x + 4$$

$$0 = (x-4)(x-1)$$

$$\therefore x = 1 \text{ or } 4$$

$$(b) \text{ Simplify: } \frac{x^2 - 1}{x} \div \frac{x^2 + 2x + 1}{3x^2 - 6x}$$

[3]

✓✓

$$\begin{aligned} & \frac{(x-1)(x+1)}{x} \times \frac{3x(x-2)}{(x+1)(x+1)} \\ &= \frac{3(x-1)(x-2)}{x+1} \end{aligned}$$

**Question 3**  
**marks**Find the maximum and minimum values over the interval  $1 \leq x \leq 5$  of the function

$$f(x) = 3x + \frac{16}{x^3}$$

$$f(x) = 3x + 16x^{-3}$$

$$f'(x) = 3 - 48x^{-4} = 3 - \frac{48}{x^4}$$

$$\text{Put } f'(x) = 0 \Rightarrow 3 = \frac{48}{x^4}$$

$$3x^4 = 48$$

$$x = \pm 2 \quad \text{reject } x = -2$$

$$f(1) = 19$$

$$f(2) = 8$$

$$f(5) = 15\frac{16}{125}$$

$\therefore$  Maximum Value is 19 when  $x$  is 1 and

Minimum Value is 8 when  $x$  is 2

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$$\begin{aligned}
 &= \left[ \frac{e^{-2x}}{-2} + c \right]_0^5 \\
 &= -\frac{e^{-10}}{2} - \frac{e^0}{-2} \\
 &= \frac{1}{2} + \frac{e^{-10}}{2} \\
 &= \frac{1}{2} + \frac{1}{2e^{10}}
 \end{aligned}$$

**Question 6**  
**marks)**

- (a) The probabilities of two events A and B are given by:

Calculate  $P(A \cup B)$ , given that are independent. [3]

$$P(A \cap B) = P(A) \times P(B) = 0.18$$

$$\begin{aligned}
 P(A \cup B) &= P(A) + P(B) - P(A \cap B) \\
 &= 0.6 + 0.3 - 0.18 \\
 &= 0.72
 \end{aligned}$$

- (b) R and S are events where
- $P(R) = \frac{1}{3}$
- ,
- $P(S) = \frac{1}{4}$
- , and
- $P(R \cup S) = \frac{1}{2}$
- .

- (i) Find
- $P(R|S)$
- and
- $P(S|R)$
- . [2]

$$P(R \cup S) = P(R) + P(S) - P(R \cap S)$$

$$\frac{1}{2} = \frac{1}{3} + \frac{1}{4} - P(R \cap S)$$

$$\therefore P(R \cap S) = \frac{1}{12}$$

$$P(R|S) = \frac{P(R \cap S)}{P(S)}$$

$$= \frac{1}{12} \div \frac{1}{4}$$

$$= \frac{1}{3}$$

$$P(S|R) = \frac{P(R \cap S)}{P(R)}$$

$$= \frac{1}{12} \div \frac{1}{3}$$

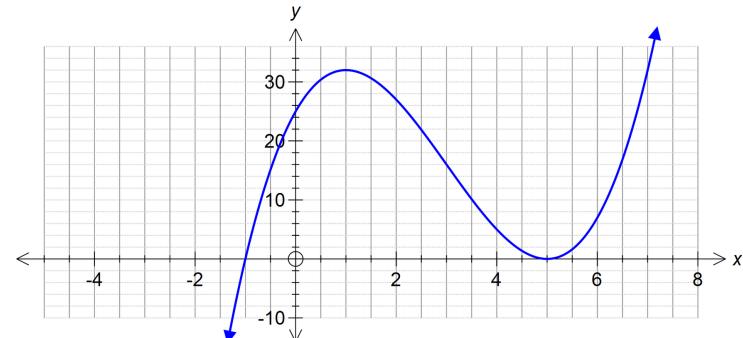
$$= \frac{1}{4}$$

**(6)**

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- (ii) Are R and S independent? Give a reason. [1]

Yes they are independent.  $P(R|S) = P(R)$ **Question 7****(7 marks)**On the axes below, sketch the function  $f(x) = x^3 - 9x^2 + 15x + 25$  showing any turning points, points of inflection and intercepts on axes.

$$f(x) = x^3 - 9x^2 + 15x + 25$$

$$f'(x) = 3x^2 - 18x + 15$$

$$3x^2 - 18x + 15 = 0$$

$$x^2 - 6x + 5 = 0$$

$$(x - 5)(x - 1) = 0$$

$$x = 1, 5 \Rightarrow \text{so turning points are } (1, 32) \text{ and } (5, 0)$$

$$f''(x) = 6x - 18$$

$$f''(3) = 0 \therefore (3, 16) \text{ is a point of inflection}$$

$$f''(1) = -12 \text{ Maximum}$$

$$f''(5) = 12 \text{ Minimum}$$

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