42 marks 6 Questions One page of notes Classpads allowed

Monday 1 July 2019

TEST 3 Year 12 Specialist

TIME: 45 minutes working PERTH MODERN SCHOOL

572

Teacher:

Note: All part questions worth more than 2 marks require working to obtain full marks.

s) Solve for the following system of linear equations. Q1(3&3=6 marks)

 $\xi = z - \lambda \zeta + x$

 $I - = zz + y\xi + xz$

 $9 = zz - \lambda L + x\varepsilon$

Shows working (Gentstur, elimination) $\sqrt{\frac{2}{3}}$ working (Gentstur, elimination) $\sqrt{\frac{2}{3}}$ working $\sqrt{\frac{2}{3}}$ $\sqrt{\frac$

 $(z-'1-'\xi)$ ups $\xi=(z-)-(H)z+x$ L=(z-)h-h

Page 2

Yr 12 Maths Specialist

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Q1 - continued

$$x + 2y - z = 3$$

b) Determine the values of m & p such that 2x + 3y + 2z = m such that the system has

$$3x + py - 2z = 6$$

- Infinite solutions
- (ii) No solutions

$$\begin{bmatrix} 1 & 2 & -1 & : & 3 \\ 2 & 3 & 2 & : & m \\ 3 & p & -2 & ! & 6 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & -1 & 3 \\ 0 & 1 & -4 & 6-m \\ 0 & 6-p & -1 & 3 \end{bmatrix} 3R_1 - R_3$$

$$\begin{bmatrix}
1 & 2 & -1 & 3 \\
0 & 1 & -4 & 6-m \\
0 & 1-4(6-p) & 0 & 6-m-12
\end{bmatrix}
R_2'-4R_3'$$
Jobbann, a line with two zeros

-6-m

Infinite

$$-23+4p = 0$$
AND

$$-6-m = 0$$
V states values for no soln

ii) No solus
$$p=2\frac{3}{4}$$
 AND $m \neq -6$

12

Page 7

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Q6 (4 marks)

Given that x & y are functions of t , show that $\frac{d^2y}{dx^2} = \frac{\frac{dx}{dt}\frac{d^2y}{dt^2} - \frac{dy}{dt}\frac{d^2x}{dt^2}}{\left(\frac{dx}{dt}\right)^3}$

$$\frac{dy}{dx} = \frac{dy}{dx} \frac{dt}{dx} = \frac{\dot{y}}{\dot{x}}$$

$$\frac{d^2y}{dx^2} = \frac{d}{dt} \left(\frac{dy}{dx} \right) \frac{dt}{dx}$$

$$= \frac{\dot{x} \ddot{y} - \dot{y} \ddot{x}}{\dot{x}^2}$$

$$= \frac{x \ddot{y} - \dot{y} \dot{x}}{\dot{z}^{3}}$$

f(+)

(Not - the marks for

Q3(2,3&3=8 marks)

speed of $\frac{d\theta}{dt} = 5$ radians/minute moving in a clockwise direction and radius 6 metres and Mia sits on wins decide to each try one of the two rides, Jane sits on the merry go round with a constant angular Consider two rides at a circus, one is a merry go round and the other is a train on a straight line. Two Q5 (2 & 5 = 7 marks)

a train moving at 3 metres/minute away from the merry go round. See the diagram below.

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D=distance between twins 5 -

the centre of the merry go round. a) Determine the distance between Jane and Mia when $\frac{2\pi}{\xi} = 0$ and the train is 30 metres from

nine the distance between Jane and Mia when
$$\theta = \frac{\pi}{3}$$
 and the train is 30 metres from nite of the menty go round.
$$D^2 = \int_0^2 \frac{1}{4} \, 30^2 - 2 \, (6) \, (30) \, \cos \frac{2\pi}{3}$$

$$D = 33. \, \sqrt{100} \, \cos \frac{2\pi}{3}$$

b) Determine the time rate of change of this distance at the point defined in (a) above.

$$\int D_{10}(x)(x)(3)z - z_{X} + z_{0} = z_{0}$$

$$\int D_{10}(x)(x)(3)z - z_{X} + z_{0} = z_{0}$$

$$(5-)\frac{1}{6}v_{15}(02)\xi_{1} + (2)\frac{1}{6}\xi_{5}v_{17}(1-(2)(02)\xi_{2} = \xi_{1}(14.2\xi_{2})\xi_{1}$$

$$= \xi_{1}(14.2\xi_{2})\xi_{1}(02)\xi_{2} = \xi_{1}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{2})\xi_{1}(14.2\xi_{2})\xi_{2}(14.2\xi_{$$

 $\sqrt{(1-1)^{2}+12(1-2+1)^{2}} = \frac{1}{1-2+1} =$

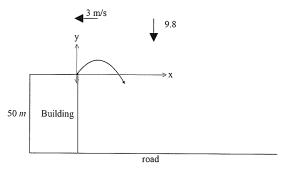
 $a = \left(\frac{3e^t}{2 \sin t}\right) m / s^2 \text{ at time } t \text{ seconds.}$

An object is initially at the origin with initial speed of $\binom{\mathfrak{F}}{T}$ and an acceleration given by

4000 deletator d

Q4(3, 3, 3 & 3 = 12 marks)

Consider a cannon ball that is projected from the top of a building with speed V at an angle θ to the surface of the roof. There is a constant cross wind of 3 metres per second acting against the ball and the acceleration due to gravity is $9.8m/s^2$ down as shown in the diagram below. (Note- let the origin be at the top of the building on the edge)



a) Given that the acceleration is given by $\ddot{r} = \begin{pmatrix} 0 \\ -9.8 \end{pmatrix} m/s^2$ show using vector calculus that the

velocity
$$\dot{r} = \begin{pmatrix} V\cos\theta - 3 \\ V\sin\theta - 9.8t \end{pmatrix} m/s$$
.
$$\dot{r} = \begin{pmatrix} O \\ -9.8t \end{pmatrix} + \begin{pmatrix} O \\$$

$$\dot{f}(0) = \begin{pmatrix} V\cos\theta - 3 \\ V\sin\theta \end{pmatrix} \qquad \begin{pmatrix} V\cos\theta - 3 \\ V\sin\theta - 3 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

b) Determine the cartesian equation of the path of the cannon ball in terms of $V \& \theta$. Show your

$$\int_{C} = \left(\frac{V(\cos 0 - 3) + C}{V + \sin 0 - 4.9 + 2} \right) + C$$

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$$\int_{C} \int_{C} \int_$$

$$y = VtsnO - 4.9t^2$$

$$y = \frac{1}{2} \times \frac{1}{2} \times$$

$$\int (0) = 0 \quad \therefore \quad \zeta = 0$$

$$\int stake \quad \int (0) = 0 \quad \text{on } \zeta = 0$$

$$\int (\cos 0) = 0 \quad \text{obtain exp for time}$$

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Page 5

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Q4 continued

c) Given that a point on the cartesian path has been measured as (7.4,1.1) metres and the initial speed V of the ball from the cannon is 12 m/s, determine the initial angle θ of the ball when

$$| \cdot | = \frac{7.4 (12) \sin 0}{12 \cos 0 - 3} - \frac{4.9 (7.4)^{2}}{(12 \cos 0 - 3)^{2}}$$

$$0 = 30.1^{\circ} \text{ or } 54.7^{\circ}$$

$$(0.524^{\circ}) (0.954^{\circ})$$

$$\sqrt{\text{solves for } 0}$$

$$\sqrt{\text{states}}$$

$$\sqrt{2} \text{ solves for } 0$$

$$\sqrt{3} \text{ solves for } 0$$

$$\sqrt{3} \text{ solves for } 0$$

d) If V = 25 m/s and $\theta = 45$ and a cross wind of 3 m/s as in the diagram on last page, determine how far from the foot of the building that the cannon ball lands on the road.

$$-SO = 2St \sin 45^{\circ} - 4.91^{2}$$

$$+ = -1.86, S.47 \text{ in}$$

$$+ \geq 0 : t = S.47 \text{ son}$$

$$\times = (2S \cos 45^{\circ} - 3) 547$$

$$= 80.286 \text{ m}$$
V sets up eqn for t

V subs + value into x

V states distance

(No need for unit)