Mathematics Department Perth Modern



## Course Specialist Test 2 Year 12

| ormula sheet provided:    | уе́з   |     |
|---------------------------|--|-----|
| Task weighting:           | %0τ_   |     |
| Marks available:          | naarks   |     |
| sməti litems:             | Drawing instruments, templates, notes on one o<br>A4 paper, and up to three calculators approved<br>examinations | 3:  |
| standard items:           | Pens (blue/black preferred), pencils (including c<br>correction fluid/tape, eraser, ruler, highlighters          | ;ړ' |
| Naterials required:       | Calculator with CAS capability (to be provided b   |     |
| Number of questions:      |  |     |
| rime allowed for this tas | snim04 :>  |     |
| լցsk type։                | <b>gesbouse</b>  |     |
| :əmen tnəbut              | Teacher name:  |     |

Note: All part questions worth more than 2 marks require working to obtain full marks.

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Q7 (4 marks) (3.1.4)

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Determine all possible values of  $\boldsymbol{n}$  .

a complex constant). Exactly four of the solutions are plotted in the second quadrant,  $\frac{\pi}{2} < Arg(z) < \pi$  , and no more. Of these four solutions The solutions to the complex equation  ${}^{\Gamma^n}={}^k$  are plotted in the complex plane. ( ${}^n$  is an integer &  ${}^k$  is

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and  $\mbox{no more}$  . Of these four solutions, the smallest argument is

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Q1 (2, 2 & 3 = 7 marks) (3.2.1-3.2.3)

Consider the functions  $f(x) = \frac{1}{x-2}$  and  $g(x) = \sqrt{x}$ 

- a) State the natural domain and range of f(x).
- b) Does  $g \circ f(x)$  exist over the natural domain of f(x)? Explain.
- c) State the rule and natural domain and range of  $f \circ g(x)$

Q2 (3, 3, 1 &2 = 9 marks) (3.2.4)

Consider the function  $f(x) = 3x^2 - 12x + 8$  with domain  $x \le 2$ .

a) Sketch the inverse function on the axes below.

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Q6 (6 marks) (3.3.4, 3.3.6)

$$r = \begin{pmatrix} 3 \\ 0 \\ 1 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ 7 \\ -2 \end{pmatrix} \qquad \qquad \begin{vmatrix} r - \begin{pmatrix} 6 \\ \beta \\ -7 \end{vmatrix} = 5$$

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Determine the value(s) of  $^{\beta}$  , to one decimal place, such that: a) The line is a tangent to sphere.

- b) The line meets the sphere in two places.
- c) The line misses the sphere completely.

Q6 (3 & 3 = 6 marks) (3.3.3-3.3.6) Consider two rockets A & B, moving with constant velocities such that at time  $^{\rm t}=^{\rm 0}$  hours their positions and velocities are as follows:

$$m\lambda \begin{pmatrix} 2 \\ 2 \\ 1 \end{pmatrix} = n \quad m\lambda \begin{pmatrix} 2 \\ \zeta \\ \zeta \end{pmatrix} = n$$

$$A \setminus MA \begin{pmatrix} S \\ S \\ S \end{pmatrix} = {}_{B}V + A \setminus MA \begin{pmatrix} I \\ S \\ I \end{pmatrix} = {}_{A}V$$

a) Determine the time and distance of their closest approach.

b) Determine the inverse function  $f^{-1}(\chi)$  stating its domain. (Show all working)

c) Determine  $\int \cdot \int \cdot \cdot \int X$ 

d) Determine when  $f(x) = f^{-1}(x)$  exactly.

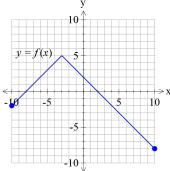
b) Civen that the rockets leave smoke trails that stay in the air for a long period of time, determine
if the smoke trails cross at all and if they do, the point in space. Justify.

Q3 (3 marks) (3.2.6)

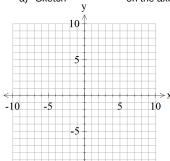
Consider the inequality 
$$\left|\frac{3}{2}x+b\right| \le 4.5$$
 is **only true** for  $4 \le x \le 10$  with  $b$  a constant. Determine the value of  $b$ .

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Q4 (3 & 3 = 6 marks) (3.2.7)

Consider the following function f(x).



a) Sketch y = f(-|x|) on the axes below.



b) Sketch  $y = \frac{1}{f(x)}$  on the axes below.

