Perth Modern School

Yr 12 Maths Specialist

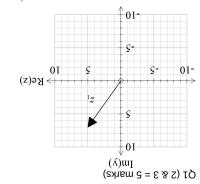
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Year 12 Specialist
TEST 2
Monday 11 March 2019
TIME: 45 minutes working
Classpads allowed
One page of notes
45 marks 7 Questions



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Note: All part questions worth more than 2 marks require working to obtain full marks.



From the diagram, $^{Z_{\perp}}$ is a solution to $^{Z^{+}}=^{k}$ for complex k . i) Determine k .

Determine the other three roots and express in the form $\,^{0\,+\,b}$.

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Q2 (2, 3 & 1 = 6 marks)

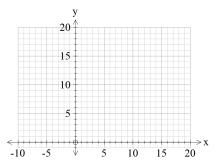
Let
$$f(x) = \sqrt{2x-1}$$
 and $g(x) = \frac{1}{x+5}$.

- a) State the natural domain and range of g(x).
- b) Does $f \circ g(x)$ exist over the natural domain of g? If it does not, determine the largest possible domain for the composite to exist.
- c) Determine $f \circ f^{-1}(x)$

Q3 (2, 3 & 2 = 7 marks)

Given that $f(x) = 2x^2 - 12x + 19$, $x \le 3$, determine the following.

- a) $f^{-1}(x)$ and its domain.
- b) Sketch on the axes below, $f(x) \& f^{-1}(x)$



c) On the sketch above show the precise points where $f(x) = f^{-1}(x)$

Q7 (5 marks)

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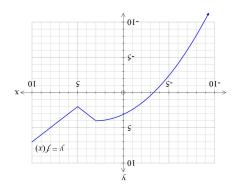
Let w=1+qi where q is a real constant. Let $p(z)=z^3+bz^2+cz+d$, where $b,c\otimes d$ are real constants. If p(z)=0 for z=w and all roots of p(z)=0 satisfy $\left|z^3\right|=8$, determine all possible values of $q,b,c\otimes d$.

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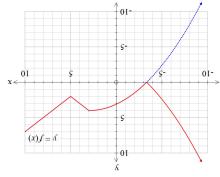
Q6 continued

Q4 (2 & 3 = 5 marks)

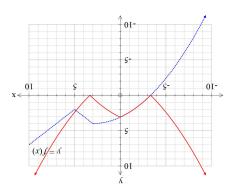
Consider the function y = f(x) for the questions below.



a) Sketch the function y = f(x) on the axes below.



b) Sketch the function $y = |f(x| \cdot |x|)|$ on the axes below.



 $OA = \begin{bmatrix} 3 \\ 2 \\ \sqrt{3} \end{bmatrix} \text{ and } OB = \begin{bmatrix} 0 \\ 0 \\ \sqrt{3} \end{bmatrix}$ and $OB = \begin{bmatrix} 0 \\ \sqrt{3} \\ \sqrt{3} \end{bmatrix} \text{ and } OB = \begin{bmatrix} 0 \\ 0 \\ \sqrt{3} \end{bmatrix}$ where α is a positive consider the particular triangle AB is isosceles, with AB = AB. C) Show that $\alpha = 4$.

d) Use a vector method to show that $^{\rm OQ}$ is perpendicular to $^{\rm AB}$.

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Q5 (3 & 4 = 7 marks)

$$r = \begin{pmatrix} 5 \\ 0 \\ -4 \end{pmatrix} + \mu \begin{pmatrix} 1 \\ -3 \\ 7 \end{pmatrix} + \lambda \begin{pmatrix} 2 \\ 1 \\ -5 \end{pmatrix}$$

Let Π be the plane defined y

a) Show that the cartesian equation of this plane is 8x + 19y + 7z = 12.

b) Let the sphere S have a centre $(1,\beta,-2)$, where β is a constant, and it is known that the plane Π is tangential to this sphere. Determine the value of β and the vector equation of the sphere S.

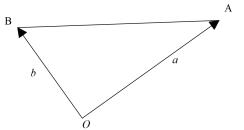
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Q6 (1, 1, 1, 3, 1 & 3 = 10 marks)

The diagram below shows a triangle with vertices with $^{O,\,A\,\&\,B}$. Let O be the origin, with vectors $^{OA}=a$ and $^{OB}=b$.



- a) Determine the following vectors in terms of a & b.
- i) MA, where M is the midpoint of the line segment OA.
- ii) BA
- iii) AQ , where Q is the midpoint of the line segment AB .

Let N be the midpoint of the line segment OB .

b) Use a vector method tom prove that the quadrilateral MNQA is a parallelogram.