

No other items may be taken into the examination room. It is **Your responsibility** to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to candidates

Special items: nil

Standard items: pens(blue/black preferred), pencils(including coloured), sharpener, correction tape/fluid, erasers, ruler, highlighters

To be provided by the candidate

Formula Sheet
This Question/Answer booklet
This Question/Answer booklet

Material required/recommended for this section

Reading time before commencing work: five minutes
Working time for paper: fifty minutes

Time allowed for this section

Teacher's Name:

Student Name:

Calculator-free
Section One:

MATHEMATICS METHODS UNIT 3

Question/Answer Booklet
Semester One Examination 2018



Structure of this paper

	Number of questions available	Number of questions to be attempted	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	9	9	50	52	35
Section Two Calculator—assumed	13	13	100	96	65
					100

Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2018*. Sitting this examination implies that you agree to abide by these rules.
2. Answer the questions according to the following instructions.

Section One: Write answers in this Question/Answer Booklet. Answer **all** questions.

Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

It is recommended that you **do not use pencil**, except in diagrams.

3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. The Formula Sheet is **not** handed in with your Question/Answer Booklet.

WATP acknowledges the permission of the School Curriculum and Assessment Authority in providing instructions to students.

- Question 1 (4 marks)**
- A function has $f(x) = e^x$ and $f'(1) = 0$. Determine the nature of those turning points. (4 marks)
- Determine the x -value of any turning points on the graph of f , and use the second derivative test to determine the nature of those turning points.

- Working time: 50 minutes
- number of the question(s) that you are continuing to answer at the top of the page.
- Continuing an answer: if you need to use the space to continue an answer, indicate this clearly at the top of the page.
 - Planning: if you use the spare pages for planning, indicate this clearly at the top of the page.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

This section has nine (9) questions. Attempt all questions. Write your answers in the spaces provided.

52 marks

CALCULATOR - FREE

Section One: Calculator-free

MATHEMATICS METHODS UNIT 3

3

CALCULATOR - FREE

End of Section One

Additional working space

Question number(s):

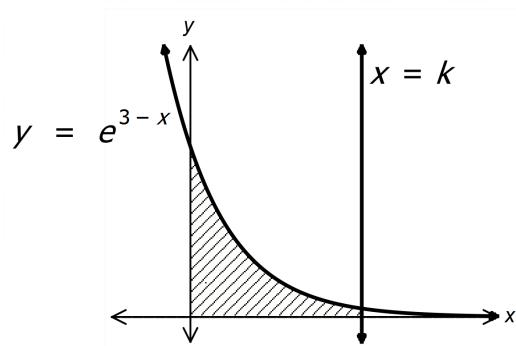
MATHEMATICS METHODS UNIT 3

14

CALCULATOR - FREE

Question 2 (6 marks)

Consider the following graph and the associated shaded region.



It is known that the shaded area has size either e^3 or $(e^3 - 1)$.

One of these values is incorrect.

Determine the value of k and state which solution is correct.

(6 marks)

Question 9 (5 marks)

- (a) Use the product rule to differentiate $y = ex(e^x)$.
Give your answer in factored form.

(2 marks)

$$(b) \text{ Use the quotient rule and } \tan(x) = \frac{\sin(x)}{\cos(x)} \text{ to show that the derivative of } y = \pi \tan x$$

$$\text{is } y' = \frac{\pi}{\cos^2 x}.$$

(3 marks)

(2 marks)

- (iii) the area enclosed by the graph of f and the x -axis between 1 and 4.

(2 marks)

$$\int_4^0 f(x) \, dx \text{ given that Area A} = 3 \text{ units}^2$$

(2 marks)

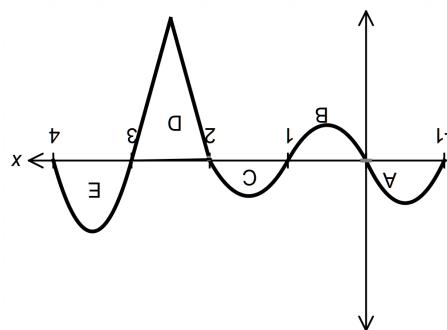
$$(i) \int_{-1}^4 f(x) \, dx$$

(a) Determine :

- Areas C, D and E are 1, 5 and 4 units² respectively.

$$\int_{-1}^1 f(x) = 0$$

It is known that:



Consider the graph of $y = f(x)$ for $-1 \leq x \leq 4$.

(3 marks)

$$(b) \text{ determine } \int \frac{5 \cos x}{1 - \cos^2 x} \, dx$$

Hence,

(2 marks)

$$(a) \text{ determine } \frac{dy}{dx} \text{ where } y = \frac{\sin x}{1}$$

Question 3 (10 marks)

Question 7 (5 marks)

Determine the following.

$$(a) \frac{d}{dx} \int_{\pi}^{e^x} \sin t \, dt$$

(2 marks)

$$(b) \frac{d^2}{dx^2} \int_{\pi}^{e^x} \sin t \, dt$$

(3 marks)

(2 marks)

$$\int_4^3 2f(x) \, dx \quad (\text{iii})$$

(b) Determine the values of:
 $\int_4^2 [f(x) + 7] \, dx \quad (\text{i})$

(2 marks)

(3 marks)

A discrete random variable X has a mean m and variance v .
 A discrete random variable Y is related to X by the rule $Y = 2X + 3$.
 The mean of Y is 8 and the variance is 20.
 Determine the values of m and v .

Question 6 (3 marks)

Question 4 (6 marks)

State, with reasons in each case, whether the functions are probability distribution functions for discrete random variables.

(a) $f(x) = \frac{1}{3}$, $x = 0, 1, 2$

(2 marks)

(b)

x	-2	-1	0	1	2
$f(x)$	0.5	0.1	0.1	0.1	0.2

(2 marks)

(c) $f(x) = \frac{x-2}{6}$, $x = 0, 2, 4, 8$

(2 marks)

Question 5 (8 marks)

The table below shows the probability function for a discrete random variable, X.

x	0	1	2	3	4
$P(X = x)$	0.5	0.1	0.1	0.1	a

(a) Show why $a = 0.2$

(1 mark)

(b) Determine $P(X < 2 | X \leq 2)$.

(2 marks)

(c) Calculate $E(X)$, which is the mean of X.

(2 marks)

A formula for the variance of X is $\sigma^2 = E(X^2) - [E(X)]^2$, where E is the expected value.

Hence, or otherwise,

(d) determine the variance of X.

(3 marks)