

WA Exams Practice Paper A, 2016 Question/Answer Booklet

place your student identification label in this box
If required by your examination administrator, please

MATHEMATICS UNITS 3 AND 4 Section One:

before reading any further.

Important note to candidates

Section One: Calculator-free

Special items:	lin							
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Materials required/recommended for this section To be provided by the supervisor This Question/Answer Booklet Formula Sheet								
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No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor examination room. If you have any unauthorised material with you, hand it to the supervisor

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METHODS UNITS 3 AND 4 2 CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	99	65
			Total	151	100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question that you are continuing to answer at the top of the
 page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

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Additional working space

Question number:	
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METHODS UNITS 3 AND 4 3

Section One: Calculator-free

CALCULATOR-FREE

This section has eight (8) questions. Answer all questions. Write your answers in the spaces 32% (25 Marks)

Working time for this section is 50 minutes.

(4 marks) ↑ noitesup

A function has a stationary point at (-2, 3) and is such that $\int (x) = 16 + kx^3$.

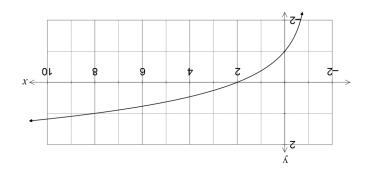
Determine the constant k and hence an equation for f(x).

(e marks) 2 duestion 8 10

CALCULATOR-FREE

The graph of y=f(x), where $f(x)=\log_a(x+1)+d$, is shown below.

METHODS UNITS 3 AND 4



(2 marks) Determine the values of a and b.

p bnns q for smint in the property p=xb (x) $\int\limits_{z}^{b}$ bnns q=xb (x) $\int\limits_{0}^{2}$ d (d)

 $xp(x)f\int_{0}^{t}$ (i) (1 mark)

(2 marks)

(1 mark) the area between the x-axis and the curve y = f(x) between x = 0 and x = 0. Question 2 (4 marks)

Let $G(x) = \int_{0}^{x} \cos\left(2t + \frac{\pi}{6}\right) dt$.

(a) Determine G'(x).

(1 mark)

(b) Determine $G\left(\frac{\pi}{6}\right)$.

(3 marks)

Question 7 (8 marks)

A small storage tank, initially holding 20 L of water, is being filled so that the rate of change of volume of water in the tank t minutes after filling began is given by $\frac{dV}{dt} = \frac{10t}{t^2+1}$ for $t \ge 0$, where V is the volume of water in the tank, in litres.

(a) Use calculus to show that the tank is filling at the fastest rate after exactly 1 minute.
(3 marks)

Determine an expression for V in terms of t. (3 marks)

The tank has a maximum capacity of 80 litres. Determine an exact expression for the time it will take to reach this capacity. (2 marks)

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(e marks) Question 3

9.0

(a) Indicate, with reasons, which of the following could **not** represent a discrete probability

1.0

(x = X)d1.0

(i)

2.0

(x = X)d2.0 1.0-3.0 4.0 3

(x = X)d4.0 6.0 2.0 6.0 8 9 (iii)

supermarket is shown below. The probability distribution for the number of broken eggs, X, in a carton of six sold at a

00.0	00.0	10.0	20.0	₽ 0.0	70.0	98.0	(x = X)d
9	9	7	3	7	l	0	x

(1 mark) nuproken eggs. Determine the probability that a randomly chosen egg carton contains at least four

(2 marks) Calculate E(X).

> (7 marks) Question 6

> > 8

CALCULATOR-FREE

 $\text{Let } f(x) = x^2 e^{2x-1}.$

METHODS UNITS 3 AND 4

(3 marks) Determine the exact value of f'(1).

(4 marks)

See next page See next page

Question 5

The continuous random variable *X* has probability density function $f(x) = \begin{cases} \frac{2x}{9} \end{cases}$

(9 marks)

(2 marks)

(1 mark)

(1 mark)

(3 marks)

 $0 \le x \le 3$ elsewhere

Question 4

(8 marks)

Simplify $\log_2 32$. (2 marks)

Solve $2^{x-1} = 5$.

- If $x = \log_n 3$ and $y = \log_n 4$
 - express $\log_n\left(\frac{4}{9}\right)$ in terms of x and/or y.

- evaluate n^{2x} .

(2 marks)

(2 marks)

(2 marks)

Determine E(X).

- The variance of X, Var(X), is $\frac{1}{2}$.
 - (i) Determine E(4X + 3).
 - Determine Var(4X + 3).
- (c) Determine the cumulative distribution function F(x).

Calculate P(1 < X < 2).

(2 marks)

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