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INDEPENDENT PUBLIC SCHOOL

WAEP Semester Two Examination, 2018

Question/Answer booklet

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If required by your examination administrator, please place your student identification label in this box	

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Calculator-free

five minutes fifty minutes	Time allowed for this section Reading time before commencing work:				
Your name					

Materials required/recommended for this section

To be provided by the supervisor

Student number:

Formula sheet This Question/Answer booklet

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

Special items:

Important note to candidates

it to the supervisor before reading any further. you do not have any unauthorised material. If you have any unauthorised material with you, hand No other items may be taken into the examination room. It is your responsibility to ensure that

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CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65

2

Total 100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet. 2.
- You must be careful to confine your response to the specific question asked and to follow 3. any instructions that are specified to a particular question.
- Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams. 6.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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Supplementary page

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SN078-125-1

Question number:

See next page SN078-125-1

32% (25 Marks)

(3 marks)

CALCULATOR-FREE

Section One: Calculator-free

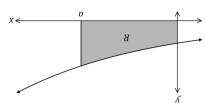
This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

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Working time: 50 minutes.

Question 1 (6 marks)

The shaded region R, shown on the graph below, is bounded by the curve $y=e^{3x}$ and the lines y=0, x=0 and x=0.



Determine the area of R in terms of a.

b) Determine, in simplest form, the value of a for which the area of R is 21 square units. (3 marks)

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1-621-870N2

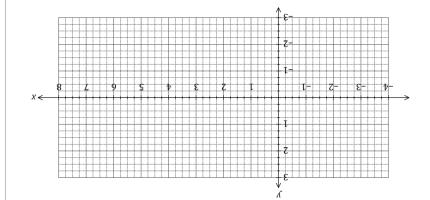
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Question 8 (8 marks)

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(a) Sketch the graph of $y = \log_4(x-2) + 1$ on the axes below, clearly showing the location of all asymptotes and axes intercepts.



Determine the coordinates of the y-intercept of the graph of $y=5-\log_2(x+0.125)$. (2 marks)

(c) The graph of $y=\log_a(x-a)$, where a>1, passes through (8.75,2). Determine the coordinates of the root of the graph. (3 marks)

End of questions SN078-125-1

Question 2

4

CALCULATOR-FREE

(5 marks)

(a) Simplify $\log_2(16) \div \log_5(125^2)$.

(2 marks)

(b) Solve the equation $\ln(4-x) + \ln 2 = 2 \ln x$.

(3 marks)

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CALCULATOR-FREE

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METHODS UNITS 3 AND 4

Question 7

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(6 marks)

The time, t years, to repay a loan of \$57 000 at 8.4% interest with monthly repayments of x dollars can be approximated by

$$t = 12 \ln \left(\frac{x}{x - 400} \right), \quad x > 400$$

(a) Determine the time to repay the loan when the monthly repayment is \$600, simplifying your answer. (1 mark)

(b) Use the increments formula to estimate the time saved in repaying the loan if the monthly repayment of \$600 is increased by 5%. (5 marks

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18m E)			Determine the x -coordinates of	
ls a local (4 mai	mont striod eht to		Use the second derivative test t sacimum and state the coordin	

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1-621-870NS

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(3 marks)

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

METHODS UNITS 3 AND 4 8 (8 marks) (8 marks) Question 6 (8 marks) Question 6 (8 marks) Right-triangle T has vertices (0,0),(p,0) and (0,q) where p>3 and q>5. The straight line from (p,0) to (0,q) passes through the point (3,5). (1 mark) (1,0) (2,0) (3,0) (3,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0) (4,0

(b) Show that the area of the triangle is $\frac{5p^2}{2(p-3)}$.

(c) Determine the value of p that minimises the area of the triangle and state the minimum area.

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CALCULATOR-FREE

Question 4

(6 marks)

The random variable X has probability density function

$$f(x) = \begin{cases} k\left(\frac{x}{4} - 1\right)^3, & 4 \le x \le 12\\ 0, & \text{elsewhere.} \end{cases}$$

(a) Determine the value of the constant k.

(4 marks)

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(b) Write down the cumulative distribution function $F(t) = P(X \le t)$ for $4 \le t \le 12$ and hence determine $P(X \le 8)$. (2 marks)

CALCULATOR-FREE

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METHODS UNITS 3 AND 4

Question 5

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(6 marks)

(a) Determine the anti-derivative of $\frac{\cos(3x)}{5 + \sin(3x)}$

(2 marks)

(b) Determine f'(x) when $f(x) = 2x \ln(5x)$.

(2 marks)

(c) Using your answer from (b) or otherwise, evaluate $\int_{0.2}^{1} (2 \ln(5x) + 2) dx$. (2 marks)

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SN078-125-1

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