

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to candidates

Special items: drawing instruments, templates, notes on two unruled sheets of A4 paper, and up to three calculators approved for use in this examination.

Standard items: correction fluid/tape, eraser, ruler, highlighters, pens (blue/black preferred), pencils (including coloured), sharpener, To be provided by the candidate

Formula sheet (retained from Section One)

Materials required/recommended for this section

Working time: one hundred minutes
Reading time before commencing work: ten minutes

Your name _____

Calculator-assumed
Section Two:
UNITS 1 AND 2
METHODS
MATHEMATICS
Question/Answer booklet

Semester Two Examination, 2019



Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total					100

Markers use only		
Question	Maximum	Mark
9	6	
10	8	
11	7	
12	10	
13	7	
14	5	
15	12	
16	7	
17	7	
18	8	
19	7	
20	8	
21	6	
S2 Total	98	
S2 Wt ($\times 0.6633$)	65%	

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.

See next page

2. Write your answers in this Question/Answer booklet preferably using a blue/black pen.

3. You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.

4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be awarded any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

5. It is recommended that you do not use pencil, except in diagrams.

6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet if you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.

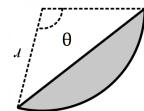
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed
65% (98 Marks)

This section has thirteen (13) questions. Answer all questions. Write your answers in the spaces provided.

(a) Convert 126° to an exact radian measure.
(1 mark)

(b) A segment of a circle of radius 22 cm is shown below, where $\theta = 126^\circ$.
(2 marks)



(i)

Determine the area of the segment.

(2 marks)

(6 marks)

Question 9

Working time: 100 minutes.

(a) Convert 126° to an exact radian measure.

(1 mark)

(i) Determine the area of the segment.

(2 marks)

(b) A segment of a circle of radius 22 cm is shown below, where $\theta = 126^\circ$.

(2 marks)

Question 9

(1 mark)

(6 marks)

(i)

Determine the area of the segment.

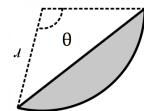
(2 marks)

(i) Determine the area of the segment.

(2 marks)

(b) A segment of a circle of radius 22 cm is shown below, where $\theta = 126^\circ$.

(2 marks)



(i)

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(2 marks)

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(2 marks)

(b) A segment of a circle of radius 22 cm is shown below, where $\theta = 126^\circ$.

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(2 marks)

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(2 marks)

(i) Determine the area of the segment.

(2 marks)

(b) A segment of a circle of radius 22 cm is shown below, where $\theta = 126^\circ$.

(2 marks)

(i)

Determine the area of the segment.

(2 marks)

(ii) Determine the perimeter of the segment.

(3 marks)

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Question 10**(8 marks)**

From a random survey of telephone usage in 261 households it was found that 155 households had access to both mobiles and landlines. 54 households had no access to a mobile and 145 more households had landlines than did not.

(a) Complete the missing entries in the table below. (3 marks)

	Mobile	No mobile	Total
Total			261
No landline			
Landline	155		

(b)

(i) If one household is randomly selected from those surveyed, determine the probability that

(c)

(ii) it had no access to a landline given that it had access to a mobile.

(d)

(iii) it had access to a mobile given that it had no access to a landline. (1 mark)

(e)

(f) Use your answers above to comment on the possible independence of households having access to a landline and households having access to a mobile phone. (2 marks)

Question 11

(7 marks)

A drone is flying in a straight line and at a constant height h m above a level pitch towards a thin goal post. It maintains a constant speed of 4.5 ms^{-1} .

Initially, the angle of depression from the drone to the base of the post is 8° . Exactly 3 seconds later this angle has increased to 10° .

- (a) Sketch a diagram to show the two angles of depression from the drone to the base of the post. (1 mark)

- (b) Determine, showing all working, the value of h and calculate the time after leaving its initial position that the drone will collide with the post. (6 marks)

Supplementary page

Question number: _____

Question 12
METHODS UNITS 1 AND 2
CALCULATOR-ASSUMED

When a manufacturer makes x litres of a chemical using process X , the cost in dollars per litre $C(x)$ varies according to the rule

$$C(x) = \frac{240}{x+15}, 5 \leq x \leq 45.$$

(1 mark)

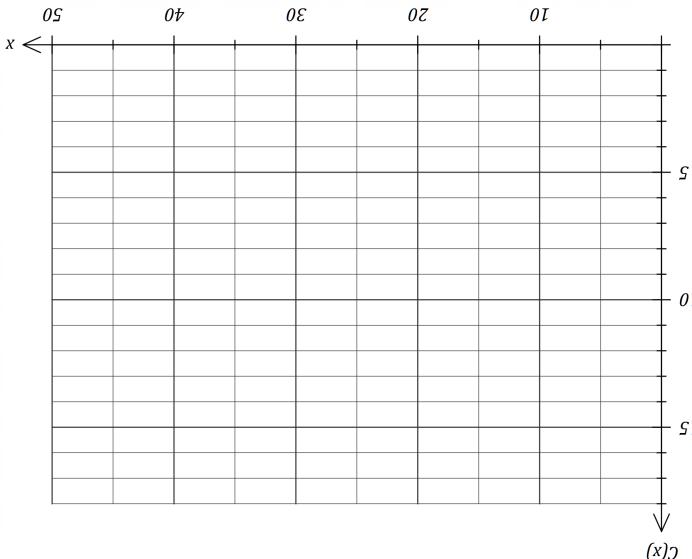
- (i) the cost per litre when 35 L is made.

(2 marks)

- (ii) the total cost of making 17 L of the chemical.

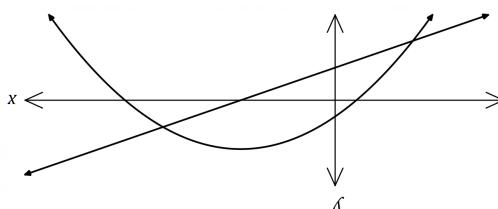
(3 marks)

- (b) Graph the cost per litre over the given domain on the axes below.



(5 marks)

Determine the value(s) of the constant k so that the equation $f(x) = g(x)$ has



$g(x) = 2x + k$.

The graphs of $y = f(x)$ and $y = g(x)$ are shown below where $f(x) = 1 + 4x - 2x^2$ and

$g(x) = 2x + k$.

(6 marks)

$y = f(x)$ and $y = g(x)$ are shown below where $f(x) = 1 + 4x - 2x^2$ and

$g(x) = 2x + k$.

(6 marks)

(1 mark)

(1 mark)

(b) no solutions.

- (c) State the range of $C(x)$.

(1 mark)

When the manufacturer uses process Z , the cost in dollars per litre $K(x)$ is modelled by

$$K(x) = 10.5 - \frac{x}{6}, 5 \leq x \leq 45.$$

- (d) Add this function to the graph and hence, or otherwise, determine the production quantities for which process X is cheaper than process Z . (3 marks)

Question 20

A fair six-sided dice numbered 1, 2, 3, 4, 5 and 6 is thrown n times until it lands on a 6.

- (a) Show that the probability that $n=3$ is $\frac{25}{216}$. (1 mark)

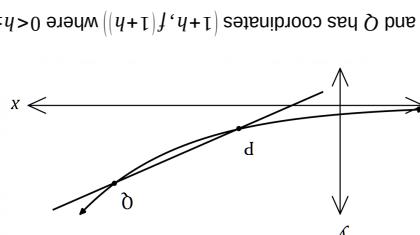
- (b) Determine the probability that $n=5$. (1 mark)

- (c) Write an expression in terms of n for the probability that the first 6 is thrown on the n^{th} throw and explain why the probabilities form a geometric sequence. (2 marks)

- (d) Determine the probability that the first 6 is thrown in 12 or less attempts. (2 marks)

- (e) The probability that the first 6 is thrown in k or less attempts must be at least 99%. Determine the least value of integer k . (2 marks)

Question 13
(7 marks)

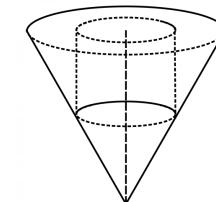


The graph of $y = f(x)$ is shown below, where $f(x) = x^3$, together with the secant to the curve through the points P and Q .

A right circular cone of base radius 10 cm and volume V cm^3 stands on a horizontal surface. A cylinder of radius x cm and height 25 cm stands inside the cone with its axis coincident with that of the cone and such that the cylinder touches the curved surface of the cone as shown.

Question 14
(7 marks)

Show that $V = 25\pi x^2 - 2.5\pi x^3$.



A right circular cone of base radius 10 cm and volume V cm^3 stands on a horizontal surface. A cylinder of radius x cm and height 25 cm stands inside the cone with its axis coincident with that of the cone and such that the cylinder touches the curved surface of the cone as shown.

(c) Determine an estimate, correct to 3 decimal places, for the value that $f(1+h) - f(1)$ approaches as h becomes closer and closer to 0 and state what this value represents. (2 marks)

(b) Name the feature of the graph above that the values you calculated in part (a) represent. (1 mark)

	h	$\frac{f(1+h) - f(1)}{h}$
	1	1
	0.1	0.1
	0.01	0.01
	0.001	0.001

(a) Complete the second column in the table below, rounding values to 4 decimal places where necessary. (4 marks)

(b) Given that x can vary, use a calculus method to determine the maximum value of V . (4 marks)

Question 14

A geometric sequence has a second term of -2.5 and a sum to infinity of 8 .

Determine the sum of the first 3 terms of the sequence.

Question 18

Two events A and B are such that $P(A \cap B) = 0.2$, $P(B) = 0.5$ and $P(A \cap B) = x$.

(a) Determine $P(A \cap B)$ when $x = 0.15$. (2 marks)

(b) Determine an expression for $P(A \cap B)$ in terms of x . (1 mark)

(c) Determine the value of x when

(i) A and B are independent. (2 marks)

(ii) A and B are mutually exclusive. (1 mark)

(iii) $P(A) = 0.6$. (2 marks)

The graph of $y = f(x)$ has the following features:

- passes through $(0, 8)$ and $(-2, 0)$
 - has a local minimum at $(2, 0)$

a) Sketch the graph of $y = f(x)$ on the axes below.

(a) The amount of water in a tank, W litres, varies with time, t , in minutes, and can be modelled by the equation $W = 200 - 185|1.2|^t$, $t \geq 0$.
 Determine the amount of water in the tank after 12 minutes.

Question 17 (4 marks)

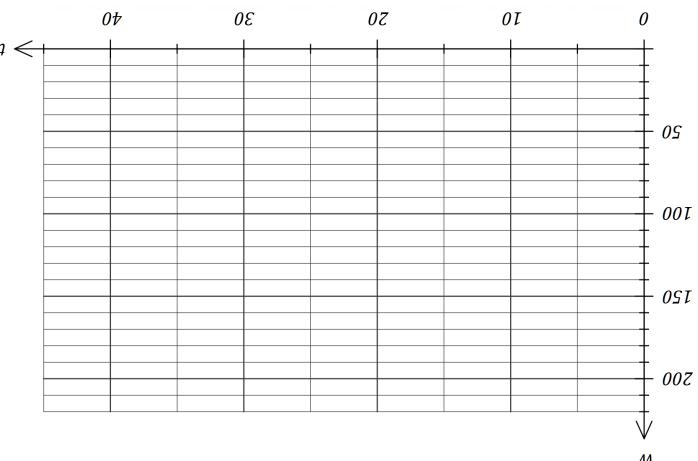
Tillmark

Summary

(marks)

(marks)

(c) Over time, the amount of water in the tank approaches litres. State the value of v and determine the time at which the amount of water in the tank reaches 99 % of this value.

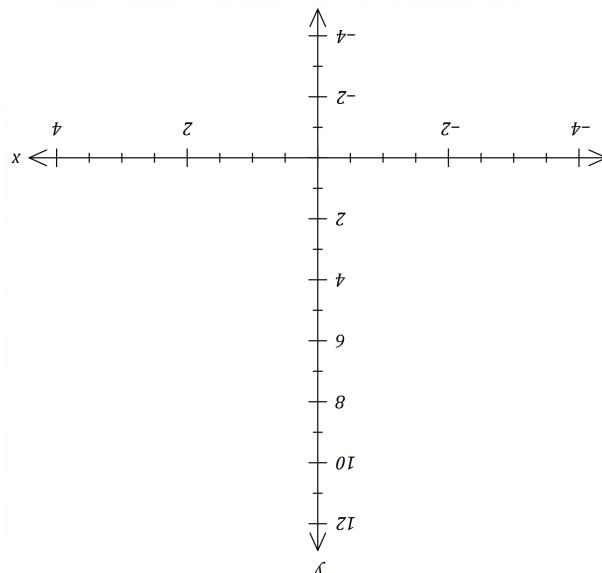


(b) Graph W against t for $U \leq t \leq 45$ on the axes below.

A blank graph with a horizontal axis labeled t and a vertical axis ranging from 0 to 200. The horizontal axis has tick marks at 0, 10, 20, 30, and 40. The vertical axis has tick marks at 0, 50, 100, 150, and 200.

(3 marks)

(b) Determine the value of a , the value of b and the value of c .



a) Sketch the graph of $y = f(x)$ on the axes below.

- passes through $(0, 8)$ and $(-2, 0)$
 - has a local minimum at $(2, 0)$

(a) sketch the graph of $y = f(x)$ on the axes below.

- (c) Use a calculus method to determine the exact coordinates of the local maximum of the graph of $y=f(x)$. (3 marks)
- (d) Determine the coordinates of the point where the tangent to $y=f(x)$ at $(0, 8)$ intersects the curve $y=f(x)$, other than at the point of tangency. (3 marks)

Question 16 (7 marks)

When a patient takes a painkilling drug A , the probability that they experience some side effects is known to be 0.1.

- (a) A doctor prescribes drug A to two unrelated patients. Determine the probability that
(i) neither patient experiences some side effects. (1 mark)

- (ii) one patient experiences some side effects and the other does not. (2 marks)

Other painkilling drugs are available. Of those who take drug A , 88% of patients who suffer some side effects will switch to another drug whereas no patient who has no side effects will switch.

- (b) The doctor prescribes drug A to a patient. Determine the probability that the patient does not switch to another drug. (2 marks)

- (c) The doctor prescribes drug A to three unrelated patients. Determine the probability that at least one of these patients switch to another drug. (2 marks)