



Course \_\_\_\_\_  
Methods Test 4 Year 12 \_\_\_\_\_

Student name: \_\_\_\_\_  
Teacher name: \_\_\_\_\_  
Date: Weds 26 August

Task type: Response

Time allowed for this task: 45 mins

Number of questions: 6

Materials required: Calculator with CAS capability (to be provided by the student)

Standard items:

Pens (blue/black preferred), pencils (including coloured),  
sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items:

Drawing instruments, templates, notes on one unfolded sheet  
of  
A4 paper, and up to three calculators approved for use in the  
WACE examinations

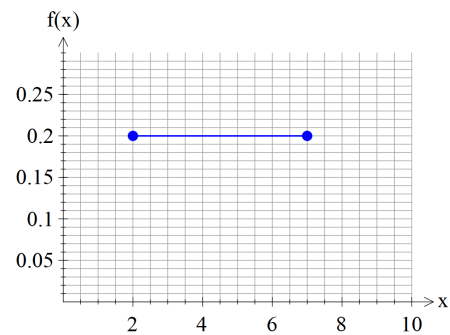
Marks available: 46 marks

Task weighting: 10 %

Formula sheet provided: Yes

Note: All part questions worth more than 2 marks require working to obtain full marks.

Q1 (1, 1, 1 &amp; 3 = 6 marks)

Consider a continuous random variable  $X$  that is uniformly distributed as follows.

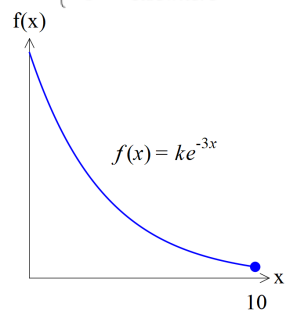
Determine the following:

- a)  $P(X > 3)$
- b)  $P(X \geq 3)$
- c)  $P(1 < X \leq 7)$
- d)  $P(X > 3 | X < 6)$

Q2 (3 marks)

Consider a continuous random variable  $X$  shown below.Solve for the constant  $k$  **exactly**. (Show all working)

$$f(x) = \begin{cases} ke^{-3x} & 0 \leq x \leq 10 \\ 0 & \text{elsewhere} \end{cases}$$



e) Explain a limitation of the Normal distribution model and show a calculation to support this.

d) If the payments were all increased by 30% and a bonus of \$2 added to each category, determine the new mean and standard deviation.

c) Determine the variance of the payment  $Var(P)$  showing full working.

b) Determine the expected payment  $E(P)$  showing full working.

a) Fill in the probability line of the above table rounded to three decimal places.

Time served In seconds	Payment \$P	Probability To 4 decimal places
$0 \leq X < 35$	\$5	
$35 \leq X < 60$	\$7	
$60 \leq X < 150$	\$12	
$150 \leq X < 200$	\$15	
$X \geq 200$	\$18	

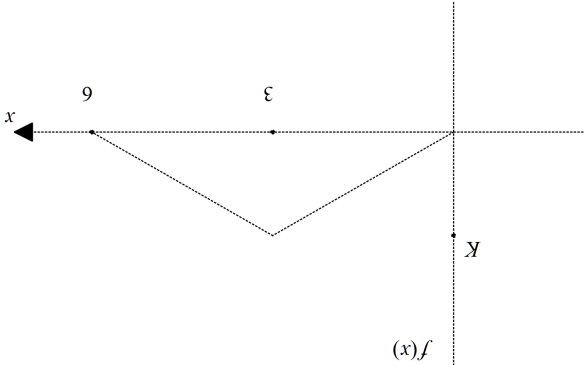
Q6 (3, 3, 2 & 2 =13 marks)  
The time it takes to be served at a supermarket checkout,  $X$  seconds, can be modelled by a normal distribution as follows  
 $X \sim N(103, 30^2)$  seconds. The assistant at the check out is paid according to the following scheme:

c) Determine  $E(X)$

d) Determine Standard deviation of  $X$

b) Determine  $P(1 < x < 4)$

a) Determine the value of the constant  $K$ .



Q3 (1, 4, 1 & 2 = 8 marks)  
Consider a continuous random variable  $X$  shown below. (Not drawn to scale)

Q4 (2, 2, 2 &amp; 1 = 7 marks)

$$f(x) = \begin{cases} \frac{3}{16}(x-3)^2 & 1 \leq x \leq 5 \\ 0 & \text{elsewhere} \end{cases}$$

A continuous random variable,  $X$  has a pdf  
Determine:

a)  $E(X)$

b)  $Var(X)$

c) Standard deviation

d)  $Var(3x - 1)$

Q5 (2, 2, 2 &amp; 3 = 9 marks)

The results for a class test,  $X$  can be modelled by a Normal Distribution given by  $X \sim N(60, 15^2)$ .  
Determine:

a) The 78<sup>th</sup> percentile.

b)  $P(55 \leq X \leq 72)$

c) The cut-off for an A grade given that this grade is only given to the top 20%.

d) A second test is a Normal Distribution with a mean of 55. Given that the 58<sup>th</sup> percentile is 62, determine the standard deviation.