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Question/Answer Bookle
Semester One Examination 2018

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METHODS UNIT 3 MATHEMATICS

Calculator-free Section One:

sətunim əvit sətunim Viti	Time allowed for this section Reading time before commencing work: Working time for paper:
	Теасһег's Иате:
	Student Name:

Material required/recommended for this section

Formula Sheet This Question/Answer booklet To be provided by the supervisor

To be provided by the candidate

Standard items: pens(blue/black preferred), pencils(including coloured), sharpener,

correction tape/fluid, erasers, ruler, highlighters

Special Items:

Important note to candidates

before reading any further. examination room. If you have any unauthorised material with you, hand it to the supervisor you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be taken into the examination room. It is your responsibility to ensure that

MATHEMATICS METHODS UNIT 3

Structure of this paper

	Number of questions available	Number of questions to be attempted	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	10	10	50	52	35
Section Two Calculator—assumed	12	12	100	96	65
					100

Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2018. Sitting this examination implies that you agree to abide by these rules.
- 2. Answer the questions according to the following instructions.

Section One: Write answers in this Question/Answer Booklet. Answer all questions.

Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

It is recommended that you do not use pencil, except in diagrams.

- You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question that you are continuing to answer at the top of the page.
- 5. The Formula Sheet is **not** handed in with your Question/Answer Booklet.

Section One: Calculator-free

25 marks

This section has ten (10) questions. Attempt all questions. Write your answers in the spaces

and/or as additional space if required to continue an answer. Spare pages are included at the end of this booklet. They can be used for planning your responses

- Continuing an answer: If you need to use the space to continue an answer, indicate in the Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- number of the question(s) that you are continuing to answer at the top of the page. original answer space where the answer is continued, i.e. give the page number. Fill in the

Working time: 50 minutes

provided.

(4 marks) Question 1

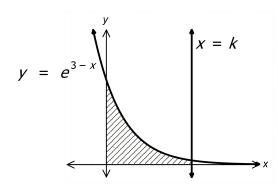
to determine the nature of those turning points. Determine the x-values of any turning points on the graph of f, and use the second derivative test $\frac{x-1}{x_{\Theta}} = (x)' t$ A function has 4

MATHEMATICS METHODS UNIT 3

13 End of Section One CALCULATOR - FREE

Question 2 (6 marks)

Consider the following graph and the associated shaded region.



It is known that the shaded area has size either e^3 or $(e^3 - 1)$. One of these values is incorrect. Determine the value of k.

(6 marks)

Additional working space

Question number(s):

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(4 marks)	(b) Determine the value of the vertical intercept on the graph of M.	х net п	= V to eviteviteb	Use the quotient rule to show that the $\frac{\pi}{x^2 \cos^2 x} = \frac{\pi}{\sin^2 x}$
(2 marks)	Question 3 (6 marks) A function M (x) has $M^{-1}(x) = 3x^2 - kx$, where k is a constant. A stationary point occurs at (6, 1). (a) Calculate the value of k.	(2 marks)	$\lambda = \Theta X(\Theta_X)$	Question 10 (5 marks) (a) Use the product rule to differentiate Give your answer in factored form.
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SEE NEXT PAGE

Question 4 (4 marks)

The exponential series can be expressed as:

$$e^{x} = 1 + \frac{x}{1!} + \frac{x^{2}}{2!} + \frac{x^{3}}{3!} + \frac{x^{4}}{4!} + \dots$$

- (a) Use the first five terms of the series to evaluate e as a fraction. (Hint: $e = e^1$)
- (2 marks)

(b) Use the series to show that the derivative of *ex* is *ex*.

(2 marks)

Question 9 (5 marks)

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(a) Determine
$$\frac{dy}{dx}$$
 where $y = \frac{1}{\sin x}$

(2 marks)

Hence,

(b) determine
$$\int \frac{5\cos x}{1-\cos^2 x} dx$$
 (3 marks)

(6 marks)

∂ noitesu⊘

8 noiteau9 (2 marks)

Determine the following.

(5 marks)

στ

discrete random variables. State, with reasons in each case, whether the functions are probability distribution functions for

 $S, l, 0 = x, \frac{l}{\varepsilon} = (x) l$ (a) (2 marks)

1.0 2-2.0 2.0 1.0 1.0 0 (S marks)

(3 marks)

 $\text{tb } 1 \text{ nis } \int_{\pi}^{\infty} \frac{z_{b}}{z_{xb}}$

(S marks)

8, 4, 2, 0 = x, $\frac{2-x}{6} = (x)$

8

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CALCULATOR - FREE

Question 6 (8 marks)

The table below shows the probability function for a discrete random variable, X.

Х	0	1	2	3	4
P(X = x)	0.5	0.1	0.1	0.1	а

(a) Show why a = 0.2

(1 mark)

(b) Determine $P(X < 2 \mid X \le 2)$.

(2 marks)

(c) Calculate E(X), which is the mean of X.

(2 marks)

A formula for the variance of X is $\sigma^2 = E(X^2) - [E(X)]^2$, where E is the expected value.

Hence, or otherwise,

(d) determine the variance of X.

(3 marks)

Question 7 (3 marks)

A discrete random variable X has a mean m and variance v. A discrete random variable Y is related to X by the rule Y = 2X + 3. The mean of Y is 8 and the variance is 20. Determine the values of m and v.

(3 marks)