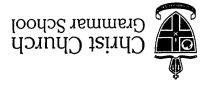
2017 C TS3T TINU



MATHEMATICS METHODS Year 12 Section One:

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Time and marks available for this section
Reading time before commencing work: 2 minutes
Working time for this section: 15 minutes

Marks available: 15 marks

Materials required/recommended for this section To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate Standard (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Calculator-free

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to nature that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 12

Guestion 8

The rate of change of temperature with respect to time of a liquid which has been boiled and then allowed to cool is given by $\frac{dT}{dt}=-0.5(T-30)$, where T is the temperature (°C) at time t (minutes).

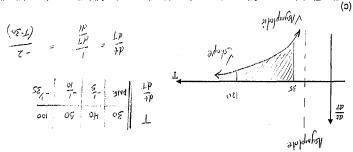
(S warks)

(e wsrks)

(a) Sketch the graph of $\frac{dT}{dt}$ against T for T>30 below.

(z warks)

(b) Sketch the graph of $\frac{dt}{dT}$ against T for T > 30 below.



Find the srea of the region enclosed by the graph of (b), the x-axis and the lines T=35 and T=120. Give your answer to two decimal places. (1 mark)

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(II) What does this area represent?

End of auestions

MATHEMATICS METHODS Year 12

2

CALCULATOR-FREE

Instructions to candidates

- 1. Write your answers in this Question/Answer Booklet.
- 2. Answer all questions.
- 3. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 4. It is recommended that you do not use pencil, except in diagrams.

See next page

MATHEMATICS METHODS Year 12

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CALCULATOR-ASSUMED

Question 6

(4 marks)

(a) Evaluate the integral $\int_0^2 (\frac{1}{1+9x^2} - \frac{1}{10}) dx$ to 4 decimal places.

(2 marks)

(b) Hence, or otherwise, find the area under the curve of the function $f(x) = \frac{1}{1+9x^2} - \frac{1}{10}$, from x = 0 to x = 2.

(2 marks)

$$\int_0^1 \left| f(x) \right| dx = \frac{0.3641}{\sqrt{}} \text{ units}^2$$

Question 7

(3 marks)

A function f(x) passes through the point $\left(\frac{\pi}{6}, -2\right)$. If $f'(x) = \sin(2x)$ find f(x).

$$S(x) = -\cos(2x)$$
Sub in $(76, -2)$

$$-2 = -\cos \frac{\pi}{3} + c$$

$$-2 = -\frac{\pi}{2} + c$$
See next page

MATHEMATICS METHODS Year 12

CALCULATOR-FREE

(7 marks)

gnestion 1

Evaluate each of the following integrals (Leave answers with positive indices):

 $xp \underline{x} \wedge -\frac{z^x}{\tau} + v^x \int$ (e) (z warks)

x10 xx -2-x + xs

1 - 7 + \frac{7}{2} - \frac{1-\frac{7}{2}}{5} + \frac{5}{2} =

f: 110,000 1-

(2 marks)

 $xp\left(\frac{v}{xu}\right)\cos\frac{z}{t}\int$ (q)

 $xb + \frac{x}{4} xo \int \frac{1}{5} =$

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CALCULATOR-ASSUMED

MATHEMATICS METHODS Year 12

(6 marks)

(3 marks)

Guestion 5

the time, in seconds, since the body first passed through the origin, O. A small body is moving in a straight line with velocity $v = 2t^2 - 19t + 30$ m/s, where t is

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(a) Determine an expression for x(t), the displacement of the body at time t.

$$\chi(f) = \frac{3}{5}f_{3} - \frac{1}{10}f_{1}f_{3} + \frac{30}{5}f_{4}f_{5} = \frac{3}{5}f_{5} - \frac{3}{10}f_{5}f_{5} = \frac{3}{5}f_{5} - \frac{3}{10}f_{5}f_{5} = \frac{3}{5}f_{5}f_{5} - \frac{3}{10}f_{5}f_{5} + \frac{3}{5}f_{5}f_{5} = \frac{3}{5}f_{5}f_{5} + \frac{3}{5}f_{5}f_{5} + \frac{3}{5}f_{5}f_{5} = \frac{3}{5}f_{5}f_{5}f_{5} + \frac{3}{5}f_{5}f_{5} + \frac{3}{5}f_{5}f_{5}$$

body between these two instants. (b) Show that the body is stationary twice and find the change in displacement of the

$$\int \frac{1}{|x|^{2}} = \frac{1}{|x|^{$$

(c) Determine the position of the body when it's velocity is a minimum.

$$\frac{8h}{6l} = (SL \cdot h) \times ...$$

$$\int \frac{SL \cdot h}{0} = \frac{7}{h}$$

$$\int \frac{SL \cdot h}{0} = \frac{7}{h}$$

$$\int \frac{SL \cdot h}{0} = \frac{7}{h}$$

See next page

(3 marks)

(c) If
$$\int_0^k \frac{1}{\sqrt{4x+1}} dx = 4$$
, find the value of k.

$$\int_{0}^{K} (4x+1)^{-1/2} dx = 4$$

$$\left[\frac{(4x+1)^{1/2}}{\frac{1}{2} \times 4}\right]_{0}^{K} = 4$$

$$\left[\frac{1}{2} \sqrt{4x+1}\right]_{0}^{K} = 4$$

$$4k = 80$$

<u>/3</u>

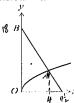
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Question 4

(8 marks)

The diagram below shows the graph of the function $y=\sqrt{x}$ and the straight line AB that is perpendicular to the curve at A, where x=4.

3



(a) Determine the equation of AB.

(3 marks)

Hence
$$\frac{dy}{dx} = \frac{1}{2}x^{-1/2}\Big|_{x=4}$$
 : Equ $y = -4x + c$ pt $(4,2)^{-1/2}$
Hence $\frac{1}{2}$ $\frac{1}{$

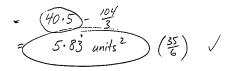
(b) Determine the shaded area in the diagram, enclosed by the curve $y = \sqrt{x}$, the straight line AB and the y-axis. (2 mark

$$\int_{0}^{4} (-4x+18) - 5x dx = \frac{104}{3}$$
= 34.6 unit²

(c) Determine the area enclosed by the curve $y=\sqrt{x}$, the straight line AB and the x-axis. (3 marks)

AB circle x-axis at 4.5 (0 = -4x+18)

$$\therefore \Delta = \frac{1}{2} (4.5) \times 18 - \frac{104}{3}$$
 from (b)

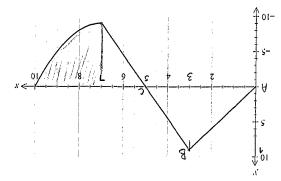


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CALCULATOR-FREE

Question 2

The graph of y=f(x) is shown below. It consists of two straight lines followed by a curve. The area between the function and the x-axis is equal to 50 square units.



(a) $\int_0^z f(x)dx = Area of \triangle ABC$ $\sqrt{(9)} \times (2) = \frac{1}{2} = \frac{1}$

(2 marks) $(2 \log x + \sqrt{x} (x)) = - (2 \log x + \sqrt{x} (x))$ $(2 \log x + \sqrt{x} (x)) = - (2 \log x + \sqrt{x} (x))$

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Answer all questions.

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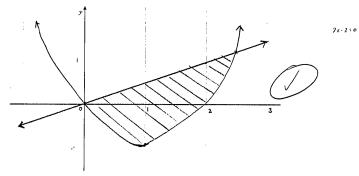
MATHEMATICS METHODS Year 12

CALCULATOR-FREE

Question 3

(4 marks)

(a) Sketch the curves $f(x) = \frac{x}{2}$ and $g(x) = x^2 - 2x$ on the axes below and shade the areabetween the curves. (2 marks)



$$\chi^{2}-2x = \frac{x}{2}$$

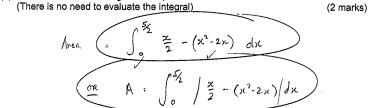
$$2x^{2}-4x - x = 0$$

$$2x^{2}-5x = 0$$

$$x(2x-5) = 0$$

$$x = 0, \frac{5}{2}$$

(b) Determine a definite integral that represents the area between the curves.



End of Questions





2017 **UNIT TEST 2**

MATHEMATICS METHODS Year 12

Section Two: Calculator-assumed

Student name	- Jolutions -
Teacher name	

c . .

Time and marks available for this section

Reading time before commencing work: 3 minutes Working time for this section: 30 minutes Marks available:

30 marks

Materials required/recommended for this section

To be provided by the supervisor This Question/Answer Booklet Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, and up to three calculators approved

for use in the WACE examinations

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