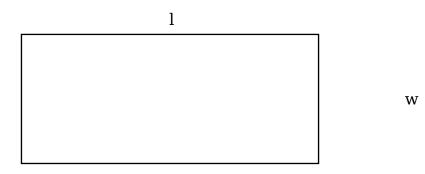
Rectangle of perimeter L m. Find in terms of L:

[a] The maximum area.



$$2w + 2l = L \rightarrow l = \frac{L - 2w}{2}$$

$$A = lw = (\frac{L - 2w}{2})w$$

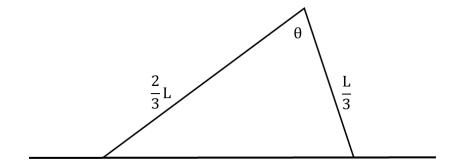
[b] The dimensions.

$$\mathbf{A}' = \frac{-4x + y}{2} \rightarrow \mathbf{A}' = 0 \rightarrow \mathbf{w} = \frac{L}{4}$$

$$1 = \frac{L - 2(\frac{L}{4})}{2} = \frac{L}{2} \times \frac{1}{2} = \frac{L}{4}$$

A triangle has one side twice as long as the other, the third being replaced with a sufficiently long straight wall.

[a] Determine the maximum area, in terms of L. You don't necessarily have to use calculus techniques but be sure to state your reasoning.



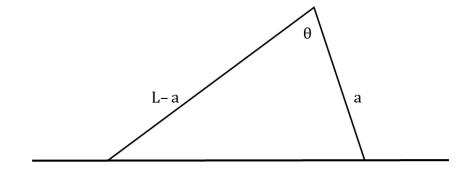
Let 'A' represent area.

$$A = \frac{1}{2} \left(\frac{2}{3}L\right) \left(\frac{L}{3}\right) \sin\theta = \frac{2L^2}{18} \sin\theta = \frac{L^2}{9} \sin\theta$$

$$\frac{dA}{d\theta} = \frac{L^2}{9} \cos\theta \rightarrow A' = 0 \rightarrow \theta = \frac{\pi}{2} (0 < \theta < \pi)$$

$$A = \frac{L^2}{9} \sin(\frac{\pi}{2}) = \frac{L^2}{9}$$

[b] Determine what would happen if the sides had no restrictions. Use calculus.



Let 'A' represent area.

$$A = \frac{1}{2}(L-a)(a)\sin\theta = \frac{La-a^2}{2}\sin\theta$$

$$\frac{dA}{d\theta} = \frac{La - a^2}{2} \cos\theta \rightarrow A' = 0 \rightarrow \theta = \frac{\pi}{2} (0 < \theta < \pi)$$

$$A = \frac{La - a^2}{2} \sin(\frac{\pi}{2}) = \frac{La - a^2}{2}$$

$$\frac{dA}{da} = \frac{-2a + L}{2} \rightarrow A' = 0 \rightarrow a = \frac{L}{2}$$

$$A = \frac{1}{2}(L-a)(a) = \frac{1}{2}(L - \frac{L}{2})(\frac{L}{2}) = \frac{1}{2}(\frac{L}{2})^2 = \frac{1}{2} \times \frac{L^2}{4} = \frac{L^2}{8}$$