#### MATHEMATICS 3C/3D 20 CALCULATOR ALLOWED

Space for extra working

Question .....



## Semester One Examination 2012 Question/Answer Booklet

MATHEMATICS 3CD

Section One (Calculator Free)

,

SOLUTIONS

## Time allowed for this section

Reading time before commencing work: 5 minutes
Working time for paper: 50 minutes

## Material required/recommended for this section

To be provided by the supervisor Question/answer booklet for Section One. Formula sheet.

## To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler.

## Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

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(a) Show that the revenue can be expressed as  $20000 + 750x - 12 \cdot 5x^2$ 

Organizars of the "Plotins to Peolas" cycling race are assuming that they will get 2000 entrants if the entry fee is \$10. If the entry fee is increased by 50 cents, they predict they will lose 55 competitors. Before they take any entrants they must raise \$24 000 to cover costs for running the event.

2

(6 marks)

CALCULATOR ALLOWED

Let x represent each 50 cent increase.

Question 12.

MATHEMATICS 3C/3D

There were 10 final-year students

Solving using ClassPad:

(b) How many final-year students are involved in the project?

[8]

[1]

 $000 = z72 + \sqrt[3]{2} + x71 \qquad \text{ oo} \qquad 02 = \frac{z72 + \sqrt[3]{2} + x71}{05}$ 

0E = z + k + xz + k = x

(a) Write down three equations that can be used to solve for x, y and z.

The mean age of all the students is 20 years.

x first-year students, aged  $17~\rm years$  y final-year students, aged  $21~\rm years$  z mature-age students, aged  $27~\rm years$ 

Дреке зке

(Ammeria) (Question II). Question III.
As part of a university teaching project, a group of first-year students is brought
As part of a university teaching the project, a group of the proper final-year and antienrage student. No student remains
each inser-year student is parted with no televation of the project.
without a partner There are a total of 30 students in the project.

MATHEMATICS 3C/3D 4 CALCULATOR ALLOWED

## Structure of this examination

	Number of questions	Working time (minutes)	Marks available
This Section Section One Calculator Free	9	50	50
Section Two Calculator Assumed	13	100	100
		Total marks	150

# Instructions:

- 1. Answer the questions in the spaces provided.
- Spare answer pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.
- Show all working clearly. Any question, or part question, worth more than 2
  marks requires valid working or justification to receive full marks. If you
  repeat an answer to any question, ensure that you cancel the answer you do
  not wish to have marked.

MATHEMATICS 3C/3D 19 CALCULATOR ALLOWED

Space for extra working

[8]

and a multiple of 6 Then  $sum = 6n + 6 = 6(n+1) = 6 \times int eger$  $8-=d\Omega+\omega\hbar$  no Let the consecutive even integers be 2n, 2n+2, 2n+4a = 61 + 62 + 64 = 56. Don't just give examples; your answer must be supported by reasoning. (b) Explain why the sum of 3 consecutive even integers is always a multiple of  $\frac{1}{81 + d2 + nb} = \frac{1}{6} \quad \Leftrightarrow \quad \text{so on so in } \left(\frac{1}{6}, 2\right)$ [2] TRURT  $e.g.~a=15,b=121=104=13\times 8$  then  $252-121=104=13\times 8$  i.e. a multiple of 88 to slqitlum (iii) If a and b are odd counting numbers with a > b, then  $a^2 - b^2$  is a 0 = d + D  $\Leftarrow$  $0 = \frac{(d + nh)^{1-}}{\varepsilon(\epsilon_1 + d\underline{c} + nh)} \quad \Leftarrow \quad 0 = \frac{\sqrt{c}h}{\varepsilon - \pi} xb$ 6.g. 4, 7, 10, ... is in A.P. 8.8 a multiple of 3  $^{\circ}$  4  $^{\circ}$  7 +7 +10 = 21  $^{\circ}$  which is a multiple of 3 (b) Form two equations and hence find the values of a and b. 8 to elqitlum as in noise region of three counting numbers in an arithmetic progression is  $\alpha$ [1] [2] FALSE: e.g. 6 is even, but has a factor of 3 (odd) d and a for the solution of an expression of  $\frac{dy}{dx}$  in terms of a and b(i) Every factor of an even number is even example of when it is true. false or true. If it is false, give a counter-example, otherwise give one The gradient of the curve with equation  $y=\frac{1}{\alpha x^2+bx+13}$  at the point  $\left(\frac{2}{5}\right)$  is (a) A conjecture is true only if it is always true. State whether the following is (s marks) Question 10. (6 marks) Question 13. CALCULATOR ALLOWED CALCULATOR ALLOWED 3 MATHEMATICS 3C/3D MATHEMATICS 3C/3D

[2]

MATHEMATICS 3C/3D CALCULATOR ALLOWED

Space for extra working

Question .....

MATHEMATICS 3C/3D CALCULATOR FREE Question 1. (9 marks)

Differentiate the following functions.

(You do not need to perform more than the most obvious algebraic

(a) 
$$y = \frac{2}{3}x^3 - 3x + \frac{1}{x}$$

$$\frac{dy}{dx} = 2x^2 - 3 - \frac{1}{x^2}$$

[2]

[2]

[2]

[3]

(b) 
$$y = e^{2x^2-x}$$

$$\frac{dy}{dx} = \left(6x^2 - 1\right)e^{2x^3 - 1}$$

$$\frac{dy}{dx} = x^3 \left( -3e^{-3x} \right) + e^{-3x} \cdot 3x^2$$

$$= x^{3} \left( -3e^{-3x} \right) + e^{-3x} \cdot 3x^{2}$$

(d) 
$$y = \frac{(1+x^4)^3}{e^x}$$

(c)  $y = x^3 e^{-3x}$ 

$$\frac{dy}{dx} = \frac{e^{x} \cdot 3(1 + x^{4})^{2} \cdot 4x^{3} - e^{x}(1 + x^{4})^{3}}{e^{2x}}$$

CALCULATOR ALLOWED L MATHEMATICS 3C/3D

 $R_y: 0 < y \le 1$ 

[1/]

[1/]

(8 marks) Question 14.

Answers must be supported with appropriate working.  $\frac{x}{1} = (x)f$ 

 $D_x: x \in \mathbb{R}$ Since  $1+x^2 \ge 0$  for all values of x,

 $\frac{x}{1-x} = -1 + ((x)S)E$ 

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 $\begin{array}{c} (0=x \text{ in}) \text{ I to outer } \underbrace{\min x \text{ m. in}}_{X=1} \frac{1}{x} \cdot .\\ \\ \infty \leftarrow \overset{\times}{x} + 1 \\ 0 \leftarrow \frac{1}{z_{X+1} I} \quad \text{os} \end{array}$ 

(0=x ts) I to oulay muminim a sad  $^{2}x+1$ 

Answers must be supported with appropriate working.

(b) Given that  $f \circ g(x) = \frac{x}{1-x}$  and f(x) = 3x + 1, find the rule for g.

(a) Use an  $\frac{\text{algebraic}}{r}$  method to find the natural domain and range for

Marks available

120

100

20

## Structure of this examination

1. Answer the questions in the spaces provided.

instructions:

This Section Section Two Calculator Assumed

Section One Calculator Free

3. Show all working clearly. Any question, or part question, worth more than 2 marks arequires and working or justification to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

 $\Sigma$  -Spare answer pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.

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Total marks

100

20

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Working time

Question 2. (5 marks) Given  $h(x) = e^x$  and  $l(x) = \frac{1}{1-x}$ (a) State the natural domain for l(x)  $D_x: x \neq 1$ [1] (b) State the natural range for h(x)  $R_y: y > 0$ [1] (c) Find the natural domain for the function  $l \circ h(x)$  $l \circ h(x) = \frac{1}{1 - e^x}$  $1-e^x\neq 0$  $e^x \neq 1$  $D_x: x \neq 0$ [3]

CALCULATOR FREE

(3 marks)

Question 3. Given ABCD is a parallelogram, prove  $\triangle ABE$  is isosceles



MATHEMATICS 3C/3D

In the major segment ADEC  $\angle ADC = \angle AEC \ \ (angles \ standing \ on \ the \ same \ arc)$ In parallelogram ABCD  $\angle ADC = \angle ABC$ (Property of par'm)

Since  $\angle ABE = \angle AEB$  then  $\triangle ABE$  is isosceles (Property of isosceles triangle)

MATHEMATICS 3C/3D CALCULATOR ALLOWED

Space for extra working

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## Important note to candidates

To be provided by the candidate
Sandard tiems: prea, pencil abrapener, highlighter, eraser, ruler.
Special items: advantg instruments, remplates, notes on up to two unfolded candidates, and the control and the control of the contro

To be provided by the supervisor Question/snawer booklet for Section Two. Formula sheet.

Material required/recommended for this section

Reading time before commencing work: 10 minutes

Working time for paper:

Time allowed for this section

SOLUTIONS

Section Two (Calculator Assumed)

MATHEMATICS 3CD

Question/Answer Booklet

Semester One Examination 2012

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(a) the initial speed of projection

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6 = (0)x 6 + 321 - 35 = x

02 + b + b = isid

 $a = (\epsilon)x$ 

v = (1)x

 $0 \le = (5)x : 0 = (8)x : 4 = (1)x : 0 = (0)x$ 

(d) the total distance travelled in the first 5 seconds

(c) when the particle is moving in a positive direction

E = 1 no I = 1 ←

0 = 6 + 12t - 2x = 0

The particle is at rest after t . I metres from the origin and a sin at t = t

(b) when the particle is at rest and how far it is from the origin at these times

(II marks) Question 15.

CALCULATOR ALLOWED MATHEMATICS 3C/3D

[3]

[3]

[v]

[3]

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(f) Prove your conjecture. Mark allocation:  $T_* = 1 + 2 + \ldots + n + (n + 1) = \frac{(n + 1)}{2}(n + 2)$  Replace  $T_*$  with correct expression  $8T_* + 1 = 8 \times \frac{(n + 1)}{2}(n + 2) + 1$  Expand and then simplify  $= 4(n^2 + 3n + 2) + 1$   $= 4n^2 + 12n + 9$  = (2n + 3)(2n + 3) Factorise as a perfect square

 $=(2n+3)^{2}$ 

a perfect square  ${\bf Question~5.}$   ${\bf Question~5.}$  When resistors are position is given by

MATHEMATICS 3C/3D

Question 4.

Determine the gradient of  $y = 2\sqrt{x} + \frac{6}{x^2}$  at the point (1, 8)  $y = 2x^{\frac{1}{2}} + 6x^3$   $\frac{dy}{dx} = \frac{2}{3}x^{\frac{3}{2}} - 18x^{-4} \quad \left( \text{or } \frac{2}{3x^{\frac{3}{2}}} \cdot \frac{18}{x^4} \right)$   $\frac{dy}{dx_{|_{DR}}} = \frac{2}{3} - 18$   $= -17\frac{1}{3}$  [4]  $Question 5. \qquad (5 \text{ marks})$  When resistors are positioned in series, the total resistance, R, is given by  $R = R_c + R_c$  Given  $R = \frac{35}{(x+1)(x+2)}, \quad R = \frac{x}{x+1} \text{ and } R_x = \frac{x}{x+2}, \text{ and } x > 0$  find the value of x.  $i.e. \quad \frac{x}{x+1} + \frac{x}{x+2} = \frac{35}{(x+1)(x+2)} \Rightarrow \frac{x(x+2) + x(x+1)}{(x+1)(x+2)} = \frac{35}{(x+1)(x+2)}$   $\frac{x^2 + 2x + x^2 + x + x^2 + 35}{2x^4 + 3x - 36 = 0}$ 

(2x-7)(x+5)=0

 $x = \frac{7}{2}$  or x = -5 (reject this as x > 0)

CALCULATOR FREE

(4 marks)

[5]

[8] m000 21 to tdgis<br/>H  $\,$  $6761.0 = ^{44-01502.1-9}$  ${}_{0}^{\bullet}46761.0 = 9$  . 12.08 = 9809795b % (c) When a commercial jet is at a maximum cruising speed the percentage decrease in air presenter from sea level is 80.21%
Determine the height of the jet to the nearest metre. [2] ∵ 56% деслеаве  $_{0}^{4}\Phi T.0 =$  $when \ h=2230 \qquad P=P_0e^{-1.25610^{-1}\times 2220}$ Determine the percentage **decrease** in air pressure from a point at sea level to a point on top of the mountain. (b) Mt. Kosciusko is 2230 metres above sea level. [1] The air pressure at sea level (a) What does  $P_0$  represent?  $\mathbf{b} = \mathbf{b}^{0} \, \epsilon_{-1.32 \times 10.4 \, \mathrm{y}}$ Air pressure decreases exponentially (approximately) with the height in metres above sea level  $\hbar$  by the rule

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Space for extra working

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Question 16.

MATHEMATICS 3C/3D  $\,$  6 CALCULATOR FREE

Question 6. (6 marks

(a) If  $y=kx^3$  for some constant k, use the incremental formula to estimate the percentage change in x required to yield a 15% increase in y.

$$\begin{split} \frac{dy}{dx} &= 3kx^2 \\ \Delta x &= \frac{dy}{dx} \quad \Rightarrow \quad 0.15y = 3kx^2 \cdot \Delta x \\ & \therefore \Delta x = \frac{0.15kx^2}{3kx^2} = \frac{0.15x}{3} = 0.05x \end{split}$$

A percentage <u>increase</u> of 5% in x is required.

[3]

(b) A company sells goods such that its revenue, in dollars, from selling  $\boldsymbol{x}$  items is given by the equation

$$R(x) = 5x(20x - x^2)$$

(i) Determine the <u>marginal revenue</u>, when x = 10

$$R(x) = 100x^{2} - 5x^{3}$$
$$R'(x) = 200x - 15x^{2}$$

R'(10) = 2000-1500= \$500

[2]

[1]

(ii) What does this represent?

R'(10) represents the revenue from selling the  $11^{\rm th}$  item

MATHEMATICS 3C/3D

5 CALCULATOR ALLOWED

[6]

[1]

[1]

Question 22. (9 marks The sequence of numbers 3, 6, 10, 15, 21, ... are known as triangular numbers.

(a) Show that the first three triangular numbers can each be written as the sum of the first n consecutive positive integers.

$$T_1 = 3 = 1 + 2$$
  
 $T_2 = 6 = 1 + 2 + 3$   
 $T_3 = 10 = 1 + 2 + 3 + 4$ 

(b) Hence determine the  $8^{th}$  triangular number

$$T_{\rm s} = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 = 45$$

The formula  $\frac{n}{2}(n+1)$  can be used to determine the sum of the first n positive integers

(c) Use this formula to determine the  $79^{\rm th}$  triangular number

$$T_{79} = \frac{80}{2} (80 + 1) = 40 \times 81$$
  
= 3240

[2]

(d) For each of the first three triangular numbers, multiply the number by 8 and then add 1  $\,$ 

$$3 \times 8 + 1 = 25$$
  
 $6 \times 8 + 1 = 49$   
 $10 \times 8 + 1 = 81$ 

[1]

(e) Based on your results from (d), write a conjecture relating to multiplying any triangular number by 8 and then adding 1

Multiplying  ${\it any}$  triangular number by 8 and then adding 1 produces a  ${\it square}$   ${\it number}$ 

[1] PLEASE TURN OVER $\rightarrow$ 

[5]

Space for extra working

MATHEMATICS 3C/3D 11 CALCULATOR FREE

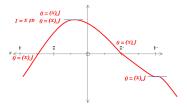
(2)  $(xam : 0>(2-)^n) \qquad 2-=x \qquad \text{murnixam fasof } a \quad \text{(ii)}$  [1]  $L-=x \quad \text{no non } li \text{ Aguenth wolloy } v^{q} \quad l=x \quad \text{no irselini to 1 non } a \quad \text{(iii)}$ 

[2]

(nim :  $0 < (E)^{n}$ ) E = x muminim lesol B (i)

sвц **(х)** *f* 

[4]
(b) Use your answer to (a), or otherwise, to determine the value(s) of x at which



(a) Sketch the graph of y = f'(x)

- $\Omega-=x$  ts tradiberg svitegen s  $\quad \bullet$
- S=x ts the distinct gradient s  $\bullet$
- $\label{eq:controller} \begin{aligned} & & & & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ &$

Question 17. (8 marks) The graph of  $\gamma = f'(x)$  has the following properties:

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MATHEMATICS 3C/3D

CALCULATOR ALLOWED

Question 21. (10 marks) Question 21. (10 mark
A radio-active substance has a half-life of 16 months. After a year, only 700 g
were left.
Assume the radioactive substance decays exponentially.

(a) Find the initial amount of the substance  $A = A_{\scriptscriptstyle 0} e^{-kt}$ 

when 
$$t=16\,{\rm months}\,A=\frac{1}{2}A_{\rm o}$$
 
$$\frac{1}{2}A_{\rm o}=A_{\rm o}e^{-{\rm i}\pi k} \qquad \Rightarrow k=0.0433$$

when t = 12 months A = 700

$$700 = A_0 e^{-0.043342} \qquad \Rightarrow A_0 = 1177.25\,g$$

[5]

(b) Find the instantaneous rate of decay when 75% of the original amount has

$$A = 1177.25\,e^{-0.04332}$$
 Rate of decay 
$$\frac{dA}{dt} = kA$$
 
$$= -0.0433A$$

For  $A = 0.25A_n = 0.25 \times 1177.25 = 294.31$ 

$$\frac{dA}{dt}$$
 = -0.0433×294.31

 $= -12.75\,grams\,/\,month$ 

MATHEMATICS 3C/3D

CALCULATOR FREE

[7]

(7 marks) Question 7. The points P(-4,3), Q(6,3) and R(-2,-1) all lie on the graph  $f(x) = ax^2 + bx + c$ .

Calculate the values of a, b and c.

Substituting:

$$(-4,3)$$
:  $16a-4b+c=3$   $(1)$ 

$$\left( 6,3\right) \ : \qquad 36a+6b+c=3 \qquad \left( 2\right)$$

$$(-2,-1)$$
:  $4a-2b+c=-1$  (3)

 $(5)-2\times(4): 8a+2b=1$ 

(2)-(1): 
$$20a+10b=0$$
 or  $2a+b=0$  (4)

$$\left(2\right)-\left(3\right): \qquad 32a+8b=4 \qquad \qquad or \qquad 8a+2b=1 \qquad \left(5\right)$$

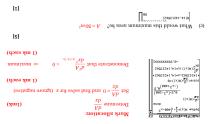
$$4a + 2b = 0$$

$$4a = 1$$

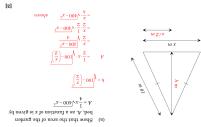
$$\Rightarrow a = \frac{1}{4}$$

$$in(4)$$
:  $\frac{1}{2} + b = 0$   $\Rightarrow b = -\frac{1}{2}$ 

$$in \big(3\big) \colon \hspace{1cm} 1+1+c=-1 \hspace{1cm} \Rightarrow c=-3$$



(b) Use calculus methods, showing full reasoning, to find the value of x that will maximise the area of the garden bed.



As part of their community service, the Wesley College senior prefects designed and built a new garden bed for the local hospice according to the following clocks. (9 marks) Question 18.

CALCULATOR FREE MATHEMATICS 3C/3D CALCULATOR ALLOWED 11 MATHEMATICS 3C/3D

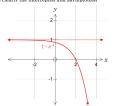
Question .....

Space for extra working

MATHEMATICS 3C/3D 8 CALCULATOR FREE Question 8. (5 marks)

(a) Sketch the graph of  $y = 1 - e^{x-2}$  on the axes provided.

Indicate clearly the intercept(s) and asymptote(s)



(b) Find g(x) if the curve  $y = e^x$  is mapped to y = g(x) by the following sequence of transformations

A reflection about the x-axis followed by a dilation in the direction of the positive x-axis by a factor of 4 followed by a reflection about the y-axis

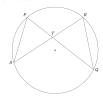
 $y = e^{x}$   $\Rightarrow y = -e^{x}$   $\Rightarrow y = -e^{\frac{x}{2}}$ 

 $\Rightarrow$   $y = -e^{\frac{-a}{2}}$ 

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MATHEMATICS 3C/3D 13 CALCULATOR ALLOWED

Question 20. (8 marks) In the diagram below the chords PQ and RS intersect at the point T. The area of  $\Delta TPS$  is  $17.5cm^2$ 



(a) Explain why ∠TPS = ∠TRQ Angles in the same major segment are equal – they are subtended by the same arc
[1]

(b) Prove that  $\Delta TPS$  is similar to  $\Delta TRQ$ 

 $\Delta TPS = \Delta TRQ$  Stand on are QS  $\Delta TSP = \Delta TQR$  Stand on are PR  $\Delta PTS = \Delta RTQ$  Vertically opposite  $\Delta TPS = \Delta TRQ$  (AAA)

[2]

(c) Use your result from (b) to show that  $PT \times QT = ST \times RT$   $\Delta TPS \approx \Delta TRQ \qquad \frac{PT}{ST} = \frac{RT}{QT}$ 

 $PS \approx \Delta TRQ$   $\overline{ST} = \overline{QT}$   $\Rightarrow PT \times QT = ST \times RT$ 

(d) Find the area of  $\Delta TRQ$  if RT =  $1\cdot 4\times PT$  If RT =  $1.4\times PT$  then ST =  $1.4\times QT$  Area of  $\Delta TRQ$  =  $1.4\times 1.4\times 1.7\cdot 5$  =  $34\cdot 3cm^2$ 

(a) Exalunte  $g(T) = g(S) = -\frac{x}{2}$  (b)  $g(T) = \frac{x}{2}$  (c)  $g(T) = \frac{x}{2}$  (d) In this that the dominity of  $g(T) = \frac{x}{2}$  (e)  $g(T) = \frac{x}{2}$  (f)  $g(T) = \frac{x}{2}$  (f)

0 > x > L-

[1/]

MATHEMATICS 2C/3D 9 CALCULATOR PREE  $\begin{cases} \text{G marks} \\ \text{g} \end{cases}$  (a) Evaluate  $g(x) = g(x) = \frac{-3}{2}$ 

(exirum a)

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[9]