Applecross Senior High School

Semester One Examination, 2019

Question/Answer booklet



MATHEMATICS
METHODS
Section One:

Calculator-free

| Your name | |
|---------------|-----------------|
| ln words | |
| ln figures | Student number: |

Time allowed for this section

Reading time before commencing work: firth minutes Working time:

Materials required/recommended for this section To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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Structure of this paper

| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of examinatio n |
|------------------------------------|-------------------------------|------------------------------------|------------------------------|--------------------|-------------------------------------|
| Section One: Calculator-free | 8 | 8 | 50 | 52 | 35 |
| Section Two: Calculator-assumed | 13 | 13 | 100 | 98 | 65 |
| | | | | Total | 100 |

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

See next page SN002-132-6

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Supplementary page

Question number: _____

t=x'0=xT correct value of ✓ obtains cos² B 0 = (1 - x)x +A 'mis nibtdo of work setsibni \ Solution Specific behaviours (S marks) ■ correct solution $\cos B = \frac{3}{3}$ Specific behaviours $\cos_5 B = I - \left(\frac{2}{3}\right)^2 = \frac{9}{5}$ $\frac{\varepsilon}{\hbar} = x \in \varepsilon = x \, \hbar$ $\frac{\overline{\zeta} \vee \zeta}{\overline{\varepsilon}} = \frac{\overline{8} \vee}{\overline{\varepsilon}} = A \text{ mis} \Leftarrow \frac{8}{6} = {}^{2} \left(\frac{1}{\varepsilon}\right) - 1 = A^{2} \text{ mis}$ 5-x9=x2Solution Show that $\sin A = \frac{\sum \sqrt{2}}{5}$ and determine the value of $\cos B$. (2 marks) (3 marks) ■ both correct solutions (b) A is an acute angle and B is an obtuse angle such that $\cos A = \frac{1}{3}$ and $\sin B = \frac{2}{3}$. Specific behaviours 7-=x, 2.4=x■ exact value Solution √ reduces angle (i) (J mark) .0 = (7 + x)(8 - x 2)Specific behaviours Solve the following equations for x. $\frac{\overline{\zeta}\sqrt{-}}{\zeta} = \frac{1}{\overline{\zeta}\sqrt{-}} = \frac{\pi}{4} \text{ mis } - = \frac{\pi}{4} \text{ mis}$ (7 marks) Question 1 $\frac{\pi \, 7}{4} \operatorname{nis} = \frac{\pi (2\xi - 2\xi)}{4} \operatorname{nis} = \frac{\pi \, 2\xi}{4} \operatorname{nis}$ Working time: 50 minutes. $\cdot \left(\frac{30}{4}\right)^{0.0}$ Single Single Figure 6.1 (S marks) This section has eight (8) questions. Answer all questions. Write your answers in the spaces 32% (22 Marks) Section One: Calculator-free (2 warks) 8 noitesup **METHODS UNIT 1** 3 CALCULATOR-FREE CALCULATOR-FREE OΤ METHODS UNIT 1

■ correct solutions

Specific behaviours

v one correct solution

public both correct solutions

(i)

(q)

Solution x = 0, y = -6(0, -6) Specific behaviours

What are the coordinates of the y-intercept of the graph of y = (x-2)(x+3)?

(**1** mark)

| METHODS UNIT 1 | 4 | CALCULATOR-FREE |
|----------------|---|-----------------|
| | | |

| (ii) number | Solution | State the of x-intercepts |
|----------------|---------------------|---------------------------|
| the | i | graph of |
| | Specific behaviours | $y = 2x^2 + 1$ |
| mark) | ■ correct solutions | . (1 |

Question 2 (6 marks)

(a) A circle of radius 4 has its centre at the point (-2,3). Determine the equation of the circle in the form $x^2 + y^2 = ax + by + c$. (3 marks)

| Solution |
|------------------------------------|
| $(x+2)^2+(y-3)^2=4^2$ |
| $x^2 + 4x + 4 + y^2 - 6y + 9 = 16$ |
| $x^2 + y^2 = -4x + 6y + 3$ |
| Specific behaviours |
| ✓ writes equation of circle |
| ■ correctly expands |
| ■writes in required form |

(b) The graph of $x = y^2$ passes through the point (4,q). Determine the value(s) of q and hence explain why y is a relation but not a function of x. (3 marks)

| | Solution |
|--------------|---|
| | $4 = q^2 \Rightarrow q = \pm 2$ |
| A rela | ation exists as we are told that $x = y^2$. |
| | elation is not a function because it is not one-to-one |
| (101 11 | nost values of x there is more than one value of y). |
| | Specific behaviours |
| ✓ bot | h possible values |
| ≖ ехр | lains relation between variables |
| ■ eyn | lains why relation not a function |

Question 7 (7 marks)

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(1 mark)

Line *L* has equation $\frac{x}{4} + \frac{y}{5} = 1$.

State the coordinates of the point where L intersects the x-axis.

| | Solution |
|---|-----------------------|
| | $y=0 \Rightarrow x=4$ |
| | At(4,0) |
| | , , |
| | Specific behaviours |
| √ | correct coordinates |

(b) State, with justification, if L is parallel to the line with equation y = 0.8x + 1. (2 marks)

| Solution | |
|--|--------------------------|
| $y=5-\frac{5}{4}x$ | |
| L is not parallel to this line as the gradients are different: $\frac{1}{L}$ | $\frac{5}{4} \neq 0.8$. |
| Specific behaviours | |
| \checkmark indicates gradient of L | |
| ■ states not parallel, comparing gradients | |

(c) Determine the equation of line P that is perpendicular to L and passes through the point with coordinates (50,4). (2 marks)

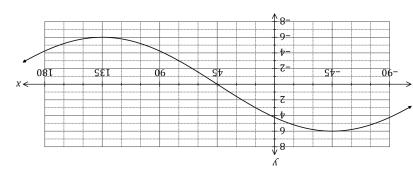
| | Solution | |
|------------------------------------|-------------------------|--|
| | $y = \frac{4}{5}x + c$ | |
| (50, 4)⇒ | $y = \frac{4}{5}x - 36$ | |
| Sp | ecific behaviours | |
| ✓ indicates perpendicular gradient | | |
| ⊈ correct ed | quation | |

(d) Determine the coordinates of the point of intersection of L and P. (2 marks)

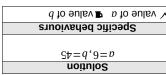
| ordinates of the point of intersection of L and P . | |
|---|--|
| Solution | |
| $P: y = \frac{4}{5}x - 36$ | |
| $\frac{4}{5}x - 36 = 5 - \frac{5}{4}x \Rightarrow \frac{41}{20}x = 41 \Rightarrow x = 20$ | |
| $y = \frac{4}{5}(20) - 36 = -20$ | |
| Intersect at $(20, -20)$ | |
| Specific behaviours | |
| \checkmark equates equations and solves for x | |
| ■ correct coordinates | |

Question 3 (6 marks)

(a) The graph of $y = a\cos(x+b)$ is shown below, where a and b are constants.



Determine the value of a and the value of b, where $-90 \circ \le b \le 180 \circ$.



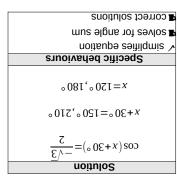
(b) Given that $0^{\circ} \le x \le 360^{\circ}$, solve

(A mark)
$$\frac{1}{\sqrt{2}} = (x) \cos x \qquad (1)$$

■ correct solutions

Specific behaviours

(ii)
$$8\cos(x+30^{\circ})+4\sqrt{3}=0$$
.

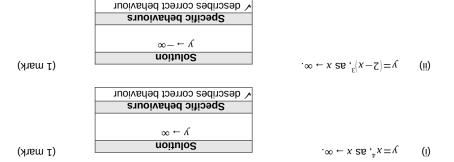


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Question 6 (7 marks)

(a) Briefly describe the behaviour of the y values for each of the following graphs, given the behaviour of the x values:



Solution $y \to 0$ Specific behaviours $\sqrt{\text{describes correct behaviour}}$

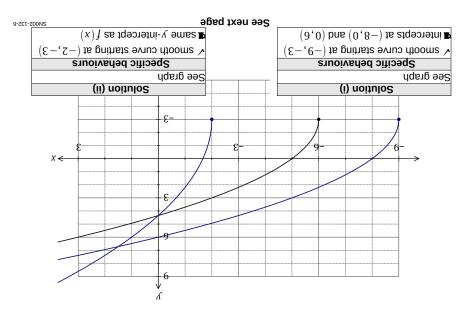
(T mark)

(b) The graph of y=f(x) is shown below. On the same axes sketch the graph of

 $.\infty - \leftarrow x \text{ ss.} \frac{1}{x} = y$ (iii)

(i)
$$y = f(x+3)$$
.

(ii)
$$y = f(3x)$$
.



CALCULATOR-FREE

CALCULATOR-FREE

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METHODS UNIT 1

Question 4

Determine the coordinates of the y-intercept of the graph of $y=4(x-3)^2-26$.

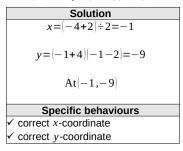
(1 mark)

(7 marks)

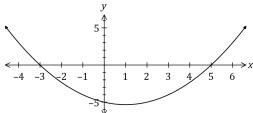
| Solution |
|------------------------------|
| $x=0, y=4(-3)^2-26=36-26=10$ |
| At(0,10) |
| Specific behaviours |
| ✓ correct coordinates |
| |

turning point of the graph of y=(x+4)(x-2).

(2 marks)



The graph of $y=ax^2+bx+c$ is shown below. Determine the value of the coefficients a,b(4 marks) and c.



Solution y = a(x+3)(x-5) $-5 = a(3)(-5) \Rightarrow a = \frac{1}{3}$ $y = \frac{1}{3}(x^2 - 2x - 15)$ $a = \frac{1}{3}, b = \frac{-2}{3}, c = -5$ Specific behaviours ✓ uses roots to write in factored form

 \blacksquare uses y-intercept to determine a

Question 5

(7 marks) (a) Expand $x(x+4)^2$. (2 marks)

| Solution |
|-------------------------------|
| $x(x^2+8x+16)=x^3+8x^2+16x$ |
| |
| Specific behaviours |
| ■ expands quadratic correctly |
| ✓ correct expansion |

Let $f(x) = x^3 + 2x^2 - 5x - 6$.

Determine f(2).

| Solution | (1 mark) |
|--------------------------|----------|
| $f(2)=2^3+2(2)^2-5(2)-6$ | |
| ¿8+8−10−6¿0 | |
| | |
| Specific behaviours | |
| correct value | |

Solve f(x) = 0. (4 marks)

| Solution | | |
|----------|---|--|
| Ī | $x^3+2x^2-5x-6=(x-2)(x^2+bx+3)$ | |
| | $-5x = -2bx + 3x \Rightarrow b = 4$ | |
| | $x^2+4x+3=(x+3)(x+1)$ | |
| | $(x-2)(x+3)(x+1)=0 \Rightarrow x=-3,-1,2$ | |
| | Specific behaviours | |

✓ uses (a) to write cubic as linear and quadratic factor

determines entire quadratic factor

■ factorises quadratic

■ all correct solutions