



Semester One Examination, 2023
Question/Answer booklet

MATHEMATICS METHODS
UNIT 3
Section One:
Calculator-free

Your Name: _____
Your Teacher's Name: _____

Time allowed for this section
Reading time before commencing work: five minutes
Working time: fifty minutes

Materials required/recommended for this section
To be provided by the supervisor
This Question/Answer booklet
Formula sheet

To be provided by the candidate
Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates
No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Marks	Max	Question	Marks	Max
1		7	4		9
2		6	5		8
3		15	6		9

(c) The random variable $Y = 3X + 1$. Determine the mean and variance of Y . (2 marks)

(b) Determine the mean and variance of X . (2 marks)

(b) Determine $f'(x)$. (4 marks)

(a) Determine the rate of change of $f'(x)$ when $x = 3$. (3 marks)

The function $f(x)$ is defined for $x > 1.5$, has derivative $f'(x) = \frac{2x-3}{8}$, and passes through the point $(4, 1)$.

Question 5
MATHEMATICS METHODS
CALCULATOR-FREE
9
(8 marks)

The probability function for the random variable X is $P(X = x) = \begin{cases} 5k^2x, & x = 0 \\ 0, & \text{otherwise.} \end{cases}$

See next page

See next page

Structure of this paper

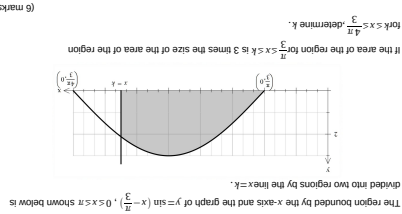
Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	6	6	50	51	36
Section Two: Calculator-assumed	10	10	100	90	64
Total					100

Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you **do not use pencil**, except in diagrams.
- The Formula sheet is **not** to be handed in with your Question/Answer booklet.

See next page

See next page



Question 6
MATHEMATICS METHODS 10
(6 marks)

MATHEMATICS METHODS

7

CALCULATOR-FREE

See next page

Question 3 (continued)
The random variable W is a Bernoulli distribution that models the situation from (a).
(d) Given that $\text{Var}(W) = 0.16$, determine the probability of success and use the information in part (a) to what outcome is therefore considered to be a success.
(2 marks)

(e) State the distribution that would be used to determine the probability of Y .
(2 marks)
Let Y be the number of times the student wins \$ 15.
The counter selected is returned to the bag, then the bag is shaken before the next student selects a counter. A student is reselected in whether they win \$ 15 or not. They pay to play 10 games.
wins \$15 in each of the following.

- (i) $\left(\frac{10}{9}\right)^4 \left(\frac{1}{9}\right)$ (1 mark)
- (ii) $\left(\frac{10}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4$ (1 mark)
- (iii) $\left(\frac{10}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4 \left(\frac{1}{9}\right)^4$ (1 mark)

See next page

See next page

Additional working space

Question number: _____

See next page

Section One: Calculator-free (51 marks)

This section has six questions. Answer all questions. Write your answers in the spaces provided.

- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 50 minutes.

Question 1 (7 marks)

A function $f(x)$ has the derivative $f'(x) = 3x^2 + 12x$. (3 marks)

The graph has an x -intercept at $x = -1$.

(a) Find $f'(x)$.

(b) The graph has a point of inflection at $x = p$. Find p . (2 marks)

(c) Find the value(s) of x for which the graph $y = f(x)$ is concave down. (2 marks)

12

MATHEMATICS METHODS

CALCULATOR-FREE

5

MATHEMATICS METHODS

(15 marks)

Question 3

At a mathematics camp, a student selects a counter from a bag containing 10 counters. The counters are numbered from 1 to 10 inclusive. Depending on the outcome, the student wins Maths Dollars that can be spent on prizes.

(a) Complete the table showing the possible outcomes and the probability. (2 marks)

Outcomes	Probability	Maths Dollars Won
A multiple of 3		\$3
A multiple of 4		\$9
A multiple of 10		\$15
All other numbers		\$x

A student pays \$5 to play the game

(b) Find the value of x if the expected return on the game is \$0. (3 marks)

(c) Is the selection of a counter a Bernoulli trial? Justify your answer. (2 marks)

See next page

MATHEMATICS METHODS

13

CALCULATOR-FREE

MATHEMATICS METHODS

4

CALCULATOR-FREE

Question 2 (6 marks)

(a) Determine:

(i) $\int 3 + \cos(3 - 2x) dx$

(1 mark)

(ii) $\int_5^6 |(2x - 5)^{-2}| dx$

(3 marks)

(b) (i) Determine the derivative of $y = e^{1/2}(3x + 5)$. Simplify your answer.

(2 marks)

See next page