ebortleM eatternertlaM AATA 11 189Y Semester 2, 2022 Department of Mathematics and Science egelleð lanettametni negjað

Section One (Calculator Free) (Sequences and sequences)

Total availate mark: 33

.... Jack. J. J. M. . . iemsk etnebuts eetunim 06 ibewollA emiT

(6 marks) (9 marks)

f notteeuD

(i) the general equation for ";,

2. 1. July

(3 marks)

(8 marks)

Question 12

50 V

annually. Let B_{n} be the account balance at the end of n years/.

 Find the general rule for the account balance at the end of n years. (S wsuks)

(1) 20.05 × 0.00 000 h = 18

percentage growth rate in the first 10 years. (S warks) b. Find the growth in the account balance in the first 10 years. Hence, find the average

122.8281221

X m/17, 5-9 WA

c. Calculate the average percentage growth rate in the first 20 years. (S marks)

X 2024) 2 89. F

dive an explanation for the different answers in the parts((b) and (c).

to a de greater that the interest sales of bomos Companded armaily so at later times, The interest

Scanned with CamScanner

Question 2

(8 marks)

(a) The tenth term of an arithmetic sequence is 98 and the sixteenth term is 80. Determine the sum of the first 20 terms of the sequence.

93 =
$$\alpha + (9 = -5)$$

93 = $\alpha + 27$
93 - $\alpha + 27$
93 - $\alpha + 27$
 $\alpha = -4$
 $\alpha = -3$
 $\alpha = -4$
 $\alpha = -4$

(b) The first two terms of a geometric sequence are 3×10^{-4} and 6×10^{-6} . Calculate the fifth term of the sequence, giving your answer in scientific notation. (4 marks)

2

(5 marks)

Ques

Jenny has 6 weeks to train from the City to Surf Marathon.

a. Jenny's training schedule demands that she runs a total of 8000 km. Each week she plans to run a constant number of kilometers further then the week before. If she starts by running 100 km in the first week, how much further she run each week in irder to complete 800km planned in the schedule? (3 marks)

493. > kar more early week

- b. Jenny decides she can also increase her fitness level by skipping. She starts with 60 skips a minute and wants to increase the rate by 5% each week.
 - i. How many skips per minutes is she skipping during the last week before the Marathon? (i.e Week 6) (1 mark)

ii. How many weeks would it take Jenny to be able to skip at over double her initial rate? (1 mark)

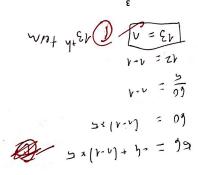
Ouestion 3 Grate whether the following sequences are Arithmetic or Geometric and state the 6^{th} term of the sequence. (2 marks) term of the sequence. (2 marks) $\frac{1}{8} \cdot \frac{1}{8} \cdot \frac{1}{8} \cdot \frac{1}{1} \cdot \frac{1}{8} \cdot \frac{1}{1} \cdot$

Dy-= LT sully

withouting

(1 marks)

ii. Which term is equal to 56?



Scanned with CamScanner

100

Guestion 10 (10 marks)

a. Determine the sum of the following series.

b. Determine the sum of the following series.

C. The sum of the sum of the following series.

C. The sum of the

b. How many terms of the series -3 +5 +13 + ... + $\xi + \xi + 3$ + ... + $\xi + \xi + 3$ + ... $\xi + \xi + 3$

c. Three numbers form a geometric sequence. Their sum is 21 and their product is 64.

(3 marks)

2 78 9 : touboad

5 12 28 8, 4, 8

d. In a converging geometric series $S_{\infty}=\frac{3}{2}$ and the sum of the first 3 terms is $\frac{14}{9}$. Determine the value of r, the constant ratio. (3 marks)

O

The sum of the first n terms of an arithmetic progression are given by

 $S_n = 3n(n-1) - 18n$

Determine:

a. T1.

$$S_{n} = 3 \times 4 \times (\Lambda - \Lambda) - \Lambda \delta \times \Lambda$$

$$S_{\Lambda} = 3 \times 0 - \Lambda \delta$$

$$S_{\Lambda} = -\Lambda \delta$$

$$T_{\Lambda} = -\Lambda \delta$$

$$T_{\Lambda} = -\Lambda \delta$$

$$(1 \text{ mark})$$

b. The common difference.

(2 marks)

$$5_2 = 3 \times 2 \times 1 - 18 \times 2$$

 $5_2 = 6 - 36$
 $5_2 = -30$ $-30 + 18 = 12$ x .

c. Determine n if $S_n = 0$.

(2 marks)

(Dren

$$0 = 3n(n-1) - 18n$$

$$0 = 3n^2 - 3n - 18n$$

$$0 = 3n^2 - 24n$$

$$0 = 3(n-1)$$

Question 9

-

(7 marks)

(a) Determine the first negative term of the sequence 99, 95, 91.

(3 marks). 99 A-100 first negative term: n-1: 95

(b) A couple gave gifts to various charities over a number of years. Over the last twelve year period they gave gifts annually, increasing in the form of an arithmetic sequence, starting with \$200 twelve years ago, increasing to \$1201 in the twelfth year.

Determine how much they donated over the twelve years.

(4 marks)

$$0 = 200$$

$$1201 = 200 + 1001$$

$$-1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

$$1001 = 100$$

Question 5

A geometric sequence is described by the rule $Tn=5x3^n$, where $n=1,2,3,4,\ldots$. Find the first three terms of the sequence.

941/59/51

End of Section One

Scanned with CamScanner

Question 8 Question 8

a. A sequence is defined by $A_{n+1} = 3^n - 2$ where $A_1 = -1$. Determine A_2 and A_3 . (2 marks) $S_1 = S_2 - S_3 = S_3 - S_3 = S_3$

$$2 = {}_{\xi} + \chi \times = {}_{\xi} + \chi \times = {}_{\xi} \times {}_$$

b. $T_{n+3}=T_{n+2}+T_{n+1}-T_n+2$ produces a sequence where $T_2=1,\ T_3=2,\ T_4=3$. (2 marks)

c. The 10th term of an arithmetic progression is 28 and the 7^{th} term is 19. i. Calculate the first three terms of the progression.

i. Calculate the first three ferms of the progression. (3 marks)

$$\lambda q = \alpha + \lambda 3$$

$$\lambda q = \alpha + \lambda 4$$

$$\lambda q = \alpha + \lambda 3$$

$$\lambda q = \alpha + \lambda 4$$

Scanned with CamScanner



Saigon International College Department of Mathematics and Science Semester 2, 2022

Year 11 ATAR Mathematics Methods

Test 5

(Sequence and series)

(6% weighting for the Unit 1 and Unit 2)

Section Two (Calculator Assumed)

Time Allowed: 55 minutes

Total available mark: 52

Question 6

(6 marks)

(a) In a given arithmetic sequence $T_1 = 7$ and $T_{20} = 45$. Evaluate S_{20}

(3 marks)

$$5_{30} = 10 \times (2 \times 7 + 19 \times 2)$$
 $1 = 7$
 $5_{30} = 10 \times (14 + 38)$
 $1 = 7 + 19 \times 0$
 $1 = 7$

(b) In a given geometric sequence $T_1 = 256$ and $T_9 = 1$. Evaluate S_{10}

(3 marks)

Question 7

(6 marks)

The table shows the compound growth of an initial investment of \$5000 at the end of each successive year.

- +	, 2013	2000	Ö
Eń	d of year	Principal (\$)	Annual Interest (\$)
	2018	5300.00	300.00
	2019	5618.00	318.00
9	2020	5955.08	337.08
	2021	6312.38	357.30
	2022	6691.13	378.74

Given T_1 is the start of 2018, state the recursive formula for

(4 marks)

(i) $^{\text{LG}}$ the value of the principal at the end of successive years

29

30 13

Tota = 9.06 x To

(ii) the annual interest earned at the end of successive years

calculate the value of the principal at the end of 2030

(2 marks)