CALCULATOR ASSUMED

Perth Modern School



METHODS UNIT 3 AND 4

Exceptional schooling. Exceptional students.

Semester Two Examination, 2019
Question/Answer Booklet

TS WETHODS & 4

Calculator-assumed

Working time for section:

Your name

Your Teacher's name

Time allowed for this section

Reading time before commencing work: ten minutes

one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet Formula Sheet (retained from Section One)

Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction

fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor

before reading any further.

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Ì	Max	Marks	Question	Max	Marks	Question

Additional working space

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Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	50	35
Section Two: Calculator-assumed	14	14	100	105	65
			Total	155	100

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question that you are continuing to answer at the top of the
 page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- The Formula Sheet is not to be handed in with your Question/Answer Booklet.

Question number:	
Question number.	

See next page End of Questions

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(TO2 W91KS)		Section Two: Calculator-assumed			
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Working time for this section is 100 minutes.

Question 8 (4 marks)

The area of a triangle can be found by the formula $Area = \frac{1}{2}ab\sin C$. Using the incremental formula, determine the approximate change in area of an equilateral triangle, with each side of 5 cm, when each side increases by 0.2 cm.

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Question 9 (9 marks)

(a) The probability of Australian Year 12 students obtaining their driver's licence is thought to be around 65%. How large a sample of students should be used to establish this within a margin of error of 5% at the 90% confidence level? (3 marks)

- (b) A survey of 1000 Australians renting houses found that 35% of their income was paid in rent.
 - (i) Estimate the standard deviation of the sampling distribution. (2 marks)
 - (ii) What z-score should be used for an 80% confidence interval? (1 marks)
 - (iii) Estimate the 80% confidence interval for the proportion of income used for renting in Australia. (3 marks)

Question 21 (5 marks)

Let
$$g(x) = \int_{-2}^{x} f(t) dt$$
 with $g(2) = 20$ and $\frac{d^2 g}{dx^2} = 6x$. Determine the function $f(x)$.

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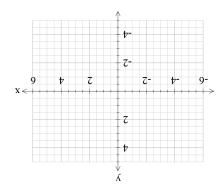
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(3 marks)

$$\frac{x}{(x+x) \text{ II}} = (x) \int_{0}^{1} 197$$

a) Determine $f'(\chi)$ using the quotient rule.

b) Sketch $f(\chi)$ on the axes below showing any intercepts and asymptotes. (3 marks)



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 Question 20
 (10 marks)

The graph of h(x) is shown on the right.

(exhibiting (iii) (iii) $xb(x)^{\dagger}h0t\int\limits_{x}^{\varepsilon}$

(iii) $\int_{-2}^{4} (h.(x)'.5x) dx.$

(b) Find the area bounded by the graph of h(x) and the x axis between x=-2 and x=4. Justify your answer. (4 marks)

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Question 11 (9 marks)

In a general population, 15% of people are left-handed. A class has 32 students and number of who are left-handed is counted. Let X = number of left-handed students in a class of 32 students.

(a) State and describe the type of distribution of

(3 marks)

(b) How many in the class would you expect to be left-handed?

(1 mark)

(c) What is the probability that the number of left-handed students in the class is within one standard deviation of the mean? (3 marks)

(d) Find the probability that at most half of the class are left-handed.

(2 marks)

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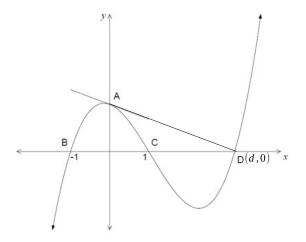
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Question 19

(6 marks)

The diagram below shows the graph of y=(x+1)(x-1)(x-d) with constant d where d>1. The graph intercepts the y-axis at the point A.

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(a) Find the equation of line AD in terms of d.

(2 marks)

(b) Show that a line that passes through A and D is tangent to the graph at A.

		Sample C 50 polluting vehicles out of a sample size of 420		Sanple A 44 polluting vehicles out of a sample size of 340
be origin after $\frac{\pi}{2}$ seconds. (3 marks)	(b) Find its displacement from the		f vehicles, one of them is actua of to be in Perth and give reasor e of 85%)	
		vehicles, the proportion of (2 marks)	hat in a random sample of 350 v 0.02 and 0.12.	c) Determine the probability t polluting vehicles lies betw
			nce interval of the true proportic sces and state the margin of err	
π after π seconds. (3 marks)	(a) Find the velocity of the weig	ly polluting. (1 mark)	ortion of vehicles that are illegal	a). Carculate the sample prop
used to describe the acceleration, $^{\Omega}$ metres per second ght at the end of a spring. Initially the weight is at rest at the		otor vehicles, 35 where found		producing an illegal amount of to produce an illegal amount o
(6 marks)	Question 12	(10 marks)		Question 18
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Question 13 (9 marks)

A chocolate factory makes bars of chocolate such that the mass of these bars forms a normal distribution of mean mass of 35 grams and a standard deviation of 4 grams. Only those bars that have a mass within 1.5 standard deviations are usually sent to stores for sale.

 a) Determine the probability that a bar of chocolate produced, will be usually sent to a store for sale.
 (3 marks)

In December each year, the person who's job is to check the mass of bars is on holiday and no one replaces their role. The bars of chocolate are packed in boxes of 50.

X Let = number of bars suitable for sale in a box of 50 in December.

b) State the distribution for $\frac{\lambda}{\lambda}$ giving the mean and standard deviation. (3 marks)

 Determine the probability that in a given box of 50 that at least 40 are suitable for sale in December.

 d) It is decided to employ a part time worker in December to select boxes of 50 at random to check the number of bars that are suitable for sale. State a method for randomly selecting these boxes for inspection. (1 mark)

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Question 17 (7 marks)

A school has analysed the exam scores for all Year 12 Methods students and found that the mean was 76 with a standard deviation of 21. Let X be the exam scores out of a 100. Determine the following.

(a)
$$E(X-6)$$
 (1 mark)

(b)
$$Var(10-2X)$$
 (2 marks)

The school has decided to scale the results down to mean of 65 and standard deviation of 15, using the transformation Y = aX + b where a and b are constants and Y is the scaled percentage scores.

(c) Determine the value(s) of a and b. (4 marks)

		(5 шяцг)	(d) Total distance travelled in the first 12 seconds.
		.s. (2 marks)	(c) Maximum speed of the particle and the time when this occu
		(2 marks)	(b) Displacement of the particle during the sixth second.
אווט אי, שווט אי שווט אי שווט אין שווט אין א שוט אין אווט אין אווט אין אווט אין אווט אין אווט אין אווט אין או	(a) Determine wo postave muni	(2 marks)	Calculate the: (a) Time(s) that the particle is at rest.
Question 14 (8 marks) For the following questions, show using calculus how to determine an optimal solution. (a) Determine two positive numbers, x and y , whose product is 36 and such that $2x+y$ is a		(8 marks) א straight line is given by d in seconds.	Question 16 The displacement, X , in centimetres of a particle from the point O in 2 The displacement, X in centimetres of a particle from the point O in 2
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radius r .

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(b) Find the area of the largest rectangle of lengths ${}^{\chi} \& y$ that can be enclosed in a circle of

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(4 marks)

Question 15 (8 marks)

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(3

A game consists of a wheel divided into sixteen equal sectors numbered 1 through 16. You may place a \$2 bet on any number. If your number comes up, you get \$20 back. That is, you win \$18 after getting your \$2 back. If you lose then you have lost \$2.

(a) Let X be the amount	of profit won on a	a bet by the player.	Find the amount the pl	aye
	E(X)			

expects to profit on a bet. i.e , explain what this means.

marks)

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X	
P(x)	

(b) Determine the standard deviation of $\,^{\chi}$, amount of profit won on a bet by the player (3 marks)

(c) How much should you **win** for the game to be fair? (E(X)=0) (2 marks)