



Course \_\_\_\_\_ Methods Test 2 \_\_\_\_\_ Year \_\_\_\_\_ 12 \_\_\_\_\_

Student name: \_\_\_\_\_ Teacher name: \_\_\_\_\_  
Date: 30 March

Task type: Response

Time allowed for this task: 45 mins

Number of questions: 8

Materials required: Calculator with CAS capability (to be provided by the student)

Standard items: Pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: Drawing instruments, templates, notes on one unfolded sheet of A4 paper, and up to three calculators approved for use in the WACE examinations

Marks available: 46 marks

Task weighting: 10%

Formula sheet provided: Yes

Note: All part questions worth more than 2 marks require working to obtain full marks.

Working out space

Q1 (3.2.1-3.2.3)

(3 &amp; 3 = 6 marks)

Determine  $y$  in terms of  $x$  for the following.

a)  $\frac{dy}{dx} = 5x^3 - \frac{2}{x^2}$  given that  $y = 10$  when  $x = 2$ .

**Working out space**

b)  $\frac{dy}{dx} = \frac{50x^2}{(5 - x^3)^5}$  given that  $y = 100$  when  $x = 2$ .

Q2 (3.2.21-3.2.22)

(4 marks)

A particle travels along a straight line such that its acceleration at time  $t$  seconds is equal to  $(5t - 1)m/s^2$ . When  $t = 1$  the displacement is 22 metres and when  $t = 3$  the displacement is -10 metres. Determine the displacement when  $t = 6$ .

Q8 (3.1.4)

(4 marks)  
The instantaneous rate of decline in the number of kangaroos on a particular park is 30% of the population per year. If there were 12 050 kangaroos on the park 3 years ago, how many will be on the park in four years from now

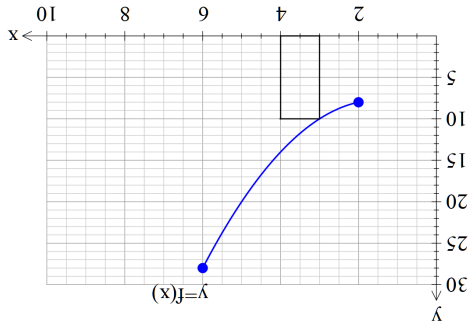
Q9 (3.2.6) (a) Determine  $\frac{d}{dx} \left( x^x (x+1)^x \right)$ .

(2 & 4 = 6 marks)

(b) Using your result from part (a) and **without using your classpad** determine  $\int \frac{x}{x^2} dx$ .

Q3 (3.2.10-3.2.11)

Consider the function  $f(x)$  which is graphed for  $2 \leq x \leq 6$ .



a) By using rectangles of width one unit, as shown above, determine a lower estimate for the area under  $f(x)$  for  $2 \leq x \leq 6$ .

b) By using rectangles of width one unit, as shown above, determine an upper estimate for the area under  $f(x)$  for  $2 \leq x \leq 6$ .

c) Determine a better approximation for the area under  $f(x)$  for  $2 \leq x \leq 6$ .

d) Describe two different methods to improve the approximation for the area under  $f(x)$  for  $2 \leq x \leq 6$ .

Q4 (3.2.18-3.2.17) (3 & 2 = 5 marks)

An oil tank is drained of oil such that if  $V$  kL of oil in the tank  $t$  seconds after draining commences is

$$\frac{dV}{dt} = 230 - \frac{120}{(t+3)^4}$$

described by

The initially full tank is emptied in 2 mins.

a) How much oil was in the full tank? (nearest kL)

b) How much oil was drained from the tank in the fifth second, nearest kL.

Q5 (3.2.11-3.2.14) (2, 2 & 2 = 6 marks)

Consider a function  $f(x)$  which is only defined for  $-5 \leq x \leq 7$  with

$$f(-5) = 0 = f(0) = f(7)$$

$$f(-4) = 8$$

$$f(-1) = 11$$

$$\int_{-5}^0 f(x) dx = 22$$

$$\int_{-5}^7 f(x) dx = -43$$

It is known that  $f(x) \geq 0$  for  $-5 \leq x \leq 0$  and  $f(x) \leq 0$  for  $0 < x \leq 7$ .

Determine.

a)  $\int_{-4}^1 f'(x) dx$

b)  $\int_{-5}^7 f(x) dx$

c) The area between  $y = f(x)$  and the x axes for  $-5 \leq x \leq 7$ .

Q6 (3.2.20) (4 marks)

Determine to two decimal places the area between the curves  $y = x^3 + x + 1$  and  $y = 4x$ .  
(Hint- Sketch the curves first on your classpad)

Q7 (3.2.16) (2 & 2 = 4 marks)

Consider  $y = \int_0^x t^3 + 3(1 + 4e^{2t})^5 dt$

Determine.

a)  $\frac{dy}{dx}$

b)  $\frac{d^2 y}{dx^2}$