| Mathematics 3C/3D Year 12 | Semester One Examination 2011 |
|---------------------------|-------------------------------|
| Section 2 | Calculator - assumed |

Your Teacher (please circle)

Your Name:

Mrs Macnaughtan Mrs Rippon Mrs Yap

| Question | Marks Available | Your Mark |
|--------------------|-----------------|-----------|
| 9 | 6 | |
| 10 | 6 | |
| 11 | 5 | |
| 12 | 9 | |
| 13 | 9 | |
| 14 | 5 | |
| 15 | 6 | |
| 16 | 10 | |
| 17 | 7 | |
| 18 | 6 | |
| 19 | 6 | |
| 20 | 5 | |
| TOTAL SECTION 2 | 80 | |



PERTH COLLEGE

Year 12

Semester One Examination 2011

Question/Answer booklet

MATHEMATICS 3CMAT/3DMAT

Section Two (Calculator - assumed)

| Student Name: | | | | | |
|---------------|--|--|--|--|--|
| | | | | | |

Time allowed for this section
Reading time before commencing work: 10 minutes
Working time for paper: 100 minutes

Material required/recommended for this section To be provided by the supervisor Question/answer booklet for Section Two Formula sheet

To be provided by the candidate
Standard Items: pens, pencils, pencil sharpener, highlighter, eraser, ruler
Special Items: drawing instruments, templates, notes (two unfolded sheets of A4 paper)
and up to three calculators (CAS, graphic or scientific) which satisfy the
conditions set by the Curriculum Council for this course.

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor

Structure of this paper

| | | | Total marks | 120 |
|-----------------------------------|-------------------------------------|---|--|--------------------|
| Section Two Calculator-assumed | 12 | 12 | 100 minutes | 80 |
| Section One Calculator-free | 8 | 8 | 50 minutes | 40 |
| | Number of questions available | Number of questions to be attempted | Suggested working time (minutes) | Marks available |

Instructions to candidates

- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer a. Planning. If you use the spare pages for planning, indicate this clearly at the top of the page.

 b. Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. If in the number of the question(5) that you are continuing to answer at the top of the page.
- 2. Show all your working clearly. Your working should be in afficient setal to allow your showers by the decision reside, and for marke to be amended for reasoning, incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question on from their how marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancil the armsers you do not wish to have marked.
- 3. It is recommended that you do not use pencil except in diagrams

Mathematics 3C/3D Year 12 Semester One Examination 2011 Section 2 Calculator - assumed

EXTRA PAGE FOR WORKING Clearly number any questions you do here.

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EXTRA PAGE FOR WORKING

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Calculator - assumed

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Section 2

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Mathematics 3C/3D Year 12

[e warks]

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 $\Lambda = 1500_5$

b) If the depth of water in the trough is reduced by 5%, determine the percentage change in the volume of the water using the Incremental Formula.

[5]

10

 $\frac{\Delta G_{-2} + C_{-2}}{\text{Pours.}}$ hours. That is, $\frac{\Delta G}{4}$ = K2. When that the concentration of it, including the value of any constants. Express answers connect to 3dp where necessary,

The rate at which the concentration , C units, of a drug in the blood is reduced by normal metabolism is proportional to the value of this concentration at any time I measured in

If a dosage of 0.5g of dye is administered to a patient, how much dye will be secreted after one hour if the patient's pancreas is functioning normally?

Answer correct to 3 dp.

Mathematics 3C/3D Year 12

Clearly show that the volume of water in the trough at any depth d is given by the equation

Let the depth of the water in the trough be d.

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[1]

 $\int_{A}^{2} |(f(x))| dx$ d) $\int_{2}^{f^{-2}} x - f(x) dx$ [3]

3

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[6 marks] The graph of y = f(x) is shown below.

Section 2

Question 9

a) $\int_{-4}^{2} f(x) dx$

In a pancreas that is functioning normally, 4% of the dye will be excreted each minute. in a certain medical procedure, a tracer dye is injected into the pancreas to ameasure it function real. The amount of dye remaining in the pancreas. Dy genera, at any time it minutes after the injection has been administered is given by the equation $1 = 1_0$, e^2 A water trough 60 cm across, $120\,\mathrm{cm}$ long, and $30\,\mathrm{cm}$ deep has ends in the shape of isosceles triangles. (See the diagram below.) [2 marks] Question 14 Question 15 Calculator - assumed Section 2 Calculator - assumed Section 2

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Mathematics 3C/3D Year 12 Section 2

Semester One Examination 2011 Calculator - assumed

a) The probability of surviving a particular organ transplant operation is 0.8. If a patient survives the operation, the probability that his or her body will reject the transplanted organ within the first month is 0.2. What is the probability that a particular patient survives the operation and their body does not reject the organ?

Given that $P(A \cup B) = 0.8$, $P(A \cap B) = 0.2$ and P(B|A) = 0.5, determine whether or not the events A and B are independent. Justify your answer mathematically. [4]

Given that $\int\limits_{2.5}^{t} e^{2x-5} \ dx = \frac{e-1}{2}, \text{ find the value of k.}$ Clearly show working to support your answer.

END OF SECTION TWO

Mathematics 3C/3D Year 12 Semester One Examination 2011 Section 2 Calculator - assumed

f) both the letters C and E, but with the C and E separated by at least one letter?

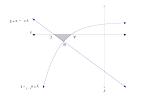
e) both the letters C and E, but with the C and E separated by exactly one letter? One of these five letter words is chosen at random. What is the probability that it contains:

Calculator - assumed 110S noitenimex3 anO 19tsama2 Mathematics 3C/3D Year 12

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Write an expression, involving integrals, to determine the area of the shaded region. Use your expression to determine the area.

a) Determine the co-ordinates of A, B (to 2 dp) and C.



Consider the diagram below, which shows the graphs of ~ $\mathbb{V}=\theta^{x-2}-1$ and " $\mathbb{V}=-x+3$.

| | [10 marks] | Ouestion 16 |
|-------------------------------|---------------------------|-------------|
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Question 19

[6 marks]

Tom is 5 years old and often throws a tantrum to get what he wants. The probability that Tom throws a tantrum over any encounter with his mum is 0.7. Given that he throws a tantrum, the probability he gets his own way is 0.2. Irrespective of whether or not he throws a tantrum, Tom gets his own way 35% of the time.

Let T be the event "throws a tantrum" and W be the event "gets his own way".



- Complete the tree diagram above, showing all branch and end of branch values to represent the above information.
- Determine the probability that Tom throws a tantrum or gets his own way.
- Determine the probability that Tom threw a tantrum, given that he did not get his own

16

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Question 11 [5 marks]

The size of a population of bacteria that is introduced to a nutrient grows according to the $P(t) = 5000 + \frac{3000\,t}{100+t^2}, \text{ where t is the time, measured in hours, after the introduction.}$

- Find the rate at which the population is changing 2 hours into the experiment. Show all working.
- [3]

b) Find the average rate at which the population is changing over the first four hours.
[2]

5

Determine the area enclosed by $\ \, V=6^{X-2}$, V=-X+3 and the line $\ \, X=2$. Clearly show how you used integrals to obtain your answer.

[5]

Calculator - assumed

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d) The function $N = e^{x-x^2} - 1$ undergoes a series of transformations and the resulting curve has the equation $N = 2e^{x-1} - 2$. Clearly describe the transformations that have occurred, in correct order, to obtain this new function.

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 $\label{eq:Long} \text{EVCELIONS}:$ up the work within the snpsets can now be suranged to form different "words." From the letters

d) How many different five letter "words" can be formed?

c) How many **five** letter subsets can be chosen from the word FACETIOUS which are also subsets of the word FACTORISE?

b) How many four letter subsets can be formed which contain at least 1 vowel?

How many four letter subsets can be formed?

Subsets are formed by choosing letters from the word $\ \ FACETIOUS$ (which is a very interesting word because it contains all five vowels in alphabetical order!)

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Question 13 [9 marks] Calculator - assumed Section 2

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Question 12 [9 marks]

Consider the function $h(x) = x^4 - 2x^2 + 1$ defined over the interval $-1.5 \le x \le 2.5$.

a) Use Calculus techniques to determine the co-ordinates and nature of any stationary points. [5]

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Mathematics 3C/3D Year 12 Semester One Examination 2011 Section 2 Calculator - assumed Question 18 [6 marks]

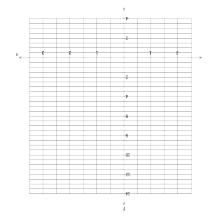
Given that $y = x^2 e^{2x}$,

a) show that the derivative can be expressed in the form $\frac{dy}{dx} = axe^{2x}(1 + cx)$ and determine the values of a and c. [3]

b) Determine the equation of the tangent to the curve $y = x^2 e^{2x}$ at the point $(1, e^2)$. Express all values in exact form.

15

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c) Draw a neat sketch of $\hbar(x)$, clearly indicating all stationary points, points of inflection, intercepts and endpoints. [3]

Mathematics 3C/3D Year 12 Semester One Examination 2011 Semester One Examination 2011 Section 2

b) Find the exact dimensions of the cone which has maximum volume. Justify your answer using Calculus.

 $h = \frac{3}{4} (100 - x_y^2) (100 + x)$ the coue can be Biven by Sprow that the expression too the nollmine of

A cone just first where a sphere of radius 10 cm.
The cone just first where a sphere.
The cone be rom.
O is the centre of the sphere.

Section 2 Calculator - session 27

Question 17

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