Applecross Senior High School

Semester One Examination, 2020

Question/Answer booklet



MATHEMATICS
METHODS
Section One:
Calculator-free

	Number of additional answer booklets used (if applicable):	five minutes		Time allowed for this s Reading time before commen Working time:
		əı	Your nam	
			In words	
			ln figures	WA student number:

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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METHODS UNIT 1 2 CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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Supplementary page

Question number:	

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(3 marks)

32% (25 Warks)

Section One: Calculator-free

This section has **eight** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

(q)

Question 1 (5 marks)

The point M(-2,5) is the midpoint of point A(-6,5) and point B.

(2 marks) Determine the coordinates of point B.

Solution $-6+x = -2 \Rightarrow x = 2$ $\frac{3+y}{2} = 5 \Rightarrow y = 7$ B(2,7) Specific behaviours $\sqrt{\text{correct } x\text{-coordinate}}$

Determine the equation of the straight line that passes through point C(4,-1) and is perpendicular to the line through points A and M. (3 marks)

Solution
$$m_{AM} = \frac{S-3}{-2-(-6)} = \frac{1}{2}$$

$$m_{AM} = \frac{1}{2} = -2$$

$$m_{AM} = -2(x-4)y = -2x+7$$

$$Specific behaviours$$

$$Specific behaviours$$

$$Specific behaviours$$

$$T = -2x + 7$$

$$Specific behaviours$$

$$T = -2x + 7$$

$$T = -2x +$$

(8) Determine an exact value for $\cos 103^{\circ} \cos 58^{\circ} + \sin 103^{\circ} \sin 58^{\circ}$. (2 marks)

Solution

cos 103 ° cos 58 ° + sin 103 ° sin 58 ° = cos (103 ° - 58 °)

¿ cos 45 °. \frac{\sqrt{2}}{2}

Specific behaviours

v uses double angle formula

states exact value

Determine all possible values of tanh when $\sin\theta$

Solution

Solution $a = \sqrt{9 - 4} = \sqrt{5}$ And that θ can be in quadrant 1 or 2.

In Q1: $\tan \theta = \frac{2}{\sqrt{5}}$, in Q2 $\tan \theta = \frac{-2}{\sqrt{5}}$ Specific behaviours

Televant use of right triangle

Televant use of right triangle

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(c) Determine an exact value for $\sin 75^\circ$.

both correct values

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Question 2 (4 marks)

Expand and simplify the following.

(a) $(x-9)^2$. (1 mark)

Solution
$$(x-9)^2 = x^2 - 18x + 81$$

Specific behaviours

✓ correct expansion

(b)
$$(2x+1)(x-3)(x+7)$$
. (3 marks)

Solution
$(2x+1)(x-3)(x+7)=(2x+1)(x^2+4x-21)$
$62x^3+8x^2-42x+x^2+4x-2162x^3+9x^2-38x-21$

Specific behaviours

- ✓ correct binomial expansion
- correct full expansion
- simplifies correctly

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Question 7 (8 marks)

Solve the following equations for x.

(a) $x^2 + 20x - 21 = 0$.

Solution
$$x^2 + 20x - 21 = (x-1)(x+21)$$

Hence x=1, x=-21.

Specific behaviours

- √ factorises
- states both solutions

(b)
$$(x-1)^2-4=2x-3$$
.

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(3 marks)

METHODS UNIT 1

(2 marks)

Solution
$$x^2 - 2x + 1 - 4 = 2x - 3x^2 - 4x = 0$$

$$x(x-4)=0$$

$$x = 0, x = 4$$

- Specific behaviours

 ✓ expands and equates to zero
- factorises
- states both solutions

(c)
$$x^3 - 2x^2 - 11x + 12 = 0$$
. (3 marks)

Solution
$$x^3 - 2x^2 - 11x + 12\dot{c}_{x=1} = 13 - 13 = 0$$

$$x^3-2x^2-11x+12=(x-1)(x^2-x-12)$$

 $\delta(x-1)(x+3)(x-4)$

$$x=-3, x=1, x=4$$

Specific behaviours

See next page

- √ indicates linear factor
- factorises
- states all solutions

METHODS UNIT 1 g CALCULATOR-FREE

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Functions f and g are defined by f(x) = 4x + 5 and g(x) = 2x + 6.

(S marks) Determine the discriminant of f and the discriminant of g.

√ discriminant of g √ discriminant of f Specific behaviours $\Delta_9 = (8)(2) \Delta_9 - 4(8) = 16$ Solution $\Delta_f = (-\Delta_f)^2 - \Delta_f(\Delta_f)(S) = -6\Delta_f$

(3 marks) State, with justification, which function has no zeros and determine all zeros of the other (q)

▼ indicates appropriate method to find zeros ✓ states f has no zeroes Specific behaviours θ has zeros when x=1, x=3. $1 \pm 2 = x \frac{\overline{\partial \Gamma} / \pm (8 -) -}{(2)2} = x$ $1 \pm 3 = x \frac{\overline{\partial \Gamma} / \pm (8 -) -}{(2)2} = x$ f has no zeroes as Δ_f <0.

> (7 marks) 4 and a section 6 8

CALCULATOR-FREE

The variable V is inversely proportional to the variable t, so that when t=3.6, V=10.

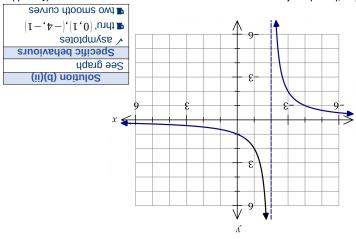
(ii) (2 marks) Determine t when V=3. ✓ correct explanation Specific behaviours As t increases V will decrease. Solution (J mark) Explain how V will change as t increases. (i)

31=36⇒1=12 $V \times t = k = 3.6 \times 10 = 36$ Solution

■ correct value ✓ indicates appropriate method Specific behaviours

(b) Part of the graph of $y = \frac{a}{1 + x}$ is drawn below.

METHODS UNIT 1



(J mark) Determine the value of a.

✓ correct value Specific behaviours $Z = b \leftarrow \frac{b}{Z+I-} = Z \leftarrow (Z,I-)$

(3 marks) Draw the remainder of the graph. (ii)

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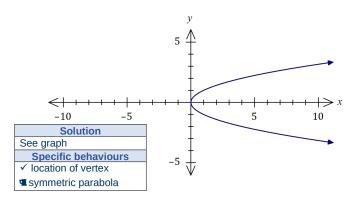
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CALCULATOR-FREE

Question 4 (7 marks)

a) Sketch the graph of $v^2 = x$ on the axes below.

(2 marks)

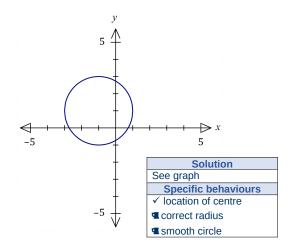


(b) Sketch the graph of $(x+1)^2 + (y-1)^2 = 4$ on the axes below.

(3 marks)

(2 marks)

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(c) Explain whether y is a function of x in the relationship graphed in (a).

Solution
y is NOT a function of x . This is because the
graph of the relationship fails the vertical line test.
Specific behaviours
✓ states not a function
■ explanation (VLT, one-to-many, etc)

See next page

(8 marks)

(1 mark)

(1 mark)

(3 marks)

Question 5

- (a) A periodic function is defined by $f(x) = 2 2\sin(3x)$.
 - (i) State the amplitude of the function.

Solution
Amplitude is 2.

Specific behaviours

✓ correct amplitude

7

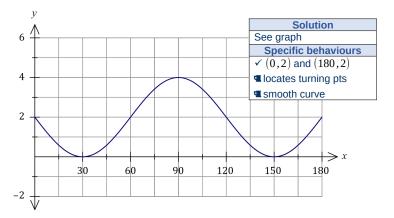
ii) State the period of the function in degrees.

Solution
Period is 360 ÷ 3=120 °.

Specific behaviours

✓ correct period

(iii) Sketch the graph of y=f(x) on the axes below.



b) Solve the equation $2\cos(x-15^\circ) = \sqrt{3}$ where $0 \le x \le 360^\circ$. (3 marks)

Solution
$\cos(x-15^\circ)=\frac{\sqrt{3}}{2}$
x-15°=30°,330°x=45°,345°
Specific behaviours
determines an angle for $\frac{\sqrt{3}}{2}$
determines one solution
both correct solutions

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