Test date: Friday 24th March TERM 1, 2017 TEST 2

Kesult

YEAR 12 MATHEMATICS

METHODS UNIT 3



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rugynjos STUDENT NAME:

Working time: 25 minutes Section 1: Resource - Free

Onestion 1 [2 marks]

 $(1-\kappa)_{\tau}(1+\kappa) = 0 = \frac{\pi p}{(1-\kappa)_{\tau}(1+\kappa)} = 0 = \frac{\pi p}{(1-\kappa)_{\tau}(1+\kappa)}$

Find the x coordinate(s) of the stationary point(s) of the curve given by $y = \int_1^{x+x} t^2(t-z) dt$

Onestion 9 [4 marks]

Question 8 [4 marks]

$\frac{\frac{c}{b} + x + \frac{c}{k} + \frac{c}{k}$ Find y if $\frac{dy}{dx} = 3x^2 + x + 3$ and y = 0 when x = 1.

Total

Section 2

Section 1

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8745

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Total

Ouestion 2 [2 marks]

Determine
$$\int_{3}^{4} \frac{(x+x)}{(x+x)} = \frac{1}{2} \left(\frac{(x+x)}{(x+x)} + \frac{1}{2}\right)$$
 $\int_{3}^{4} \frac{(x+x)}{(x+x)} = \frac{1}{2} \left(\frac{(x+x)}{(x+x)} + \frac{1}{2}\right)$

efermine
$$\int \frac{dy}{dx} dx = \int \frac{dx}{dx} \int$$

$$\frac{2^{k}}{\sqrt{4x+3}} \frac{dx}{dx} = x \ln \frac{2^{k}}{\sqrt{4x+4}} + \frac{2^{k}}{\sqrt$$

$$xb^{+}(s_{x}+s) \cdot s_{x} \cdot s_{x} = \frac{xb^{+}(s_{x}+s) \cdot s_{x} \cdot s_{x}}{a} = \frac{xb^{+}(s_{x}+s) \cdot s_{x}}$$

QUESTION 4 [\angle , \angle , \angle = 0 marks]

Find
a)
$$\int_{\frac{\pi}{2}}^{5} (\sqrt{x} - 1)^{2} dx = \int_{\frac{\pi}{2}}^{5} (x - 2\sqrt{x} + 1) dx$$

$$= \int_{\frac{\pi}{2}}^{5} (x^{2} -$$

Find the derivative of
$$F(x)$$
 given that $F(x) = \int_{1}^{x^{2}+3} (2t-1)dt$

For $f(x) = \int_{g(x)}^{g(x)} f(x) dx$

$$= \left(2(x^{2}+3) - 1 \right) \times 2x$$

$$= 4x \left(x^{2}+3 \right) - 2x$$

$$= 4x^{3} + 10x$$

For $f(x) = \int_{g(x)}^{x^{2}+3} f(x) dx$

or yet could by integrably $f(x) = \int_{g(x)}^{g(x)} f(x) dx$

Question 6 [2, 3, 3 = 8 marks]

etermine these definite integrals:

$$\int_{-1}^{1} (x+1)(x-2) dx = \int_{1}^{\infty} (x^{2}-x-2) dx$$

$$= \left[\frac{x^{3}}{3} - \frac{x^{2}}{2} - 2x \right]_{-1}^{1}$$

$$= \left(\frac{1}{3} - \frac{1}{2} - 2 \right) - \left(-\frac{1}{3} - \frac{1}{2} + 2 \right)$$

$$= -\frac{13}{2} - \frac{7}{2}$$

$$= -\frac{13}{2} - \frac{7}{2}$$

c)
$$\int_{-1}^{0} \sqrt{1+x} \, dx$$

= $\int_{-1}^{0} (1+x)^{3/2} \, dx$
= $\int_{-1}^{0} (1+x)^{3/2} \, dx$
= $\int_{-1}^{0} (1+x)^{3/2} \, dx$

$$= \int_{1}^{2} (\frac{1}{x^{3}} + \frac{1}{x^{3}}) dn$$

$$= \int_{1}^{2} (x^{-2} + x^{-3}) dn$$

$$= \left[-\frac{x^{-1}}{x^{-1}} + \frac{x^{-2}}{x^{-2}} \right]_{1}^{2}$$

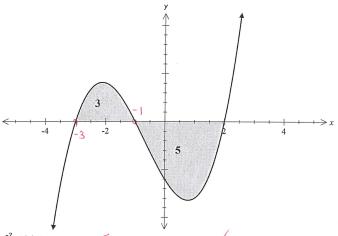
$$= \left[-\frac{1}{x^{-1}} - \frac{1}{x^{-2}} \right]_{1}^{2}$$

$$= \left(-\frac{1}{x^{-1}} - \frac{1}{x^{-2}} \right) - \left(-1 - \frac{1}{x^{-2}} \right)$$

$$= \int_{1}^{2} \frac{1}{x^{-1}} dx$$

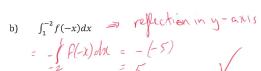
Question 7 [1, 1, 1, 1, = 4 marks]

Use the graph below to determine the following definite integrals. The area of the curve containing A is 3 square units and the area of the curve containing B is 5 square units.



a)
$$\int_{-3}^{2} f(x)dx = 3 + -1$$

= -2





d)
$$\int_{-3}^{-1} [f(x) + 3] dx = \int_{-3}^{3} [f(x)] + \int_{-3}^{3} 3 dx$$

= $3 + \left(-3 - \left(-9\right)\right)$
= $3 + 6$ Page 7

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Test date: Thursday 23rd March **METHODS UNIT 3** YEAR 12 MATHEMATICS



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more than 1 mark, valid working or justification is required to receive full marks. without supporting reasoning cannot be allocated any marks. For any question or part question worth answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given All working must be shown in the space provided. Your working should be in sufficient detail to allow your

1 sheet of A4-sized paper of notes, double-sided ClassPad and/or Scientific Calculators To be provided by the student:

Working time: 38 minutes Section 2: Resource - Rich

 $\underline{\textbf{Ouestion 1}} \quad [2, 2, 2, 2 = 8 \text{ marks}]$

The velocity v(t) in m/s of a particle travelling in a straight line is given by

Determine the distance travelled in the 4th second. $\xi = 3$ k $\ell = 4$ S + 19 - 71 = (1)

WEX ? 10 (+) 11 = 4:h

Determine the distance travelled in the interval $1 \le t \le 5$.

the true = time

If initially the particle has a displacement of -10m , what is the displacement when t=3 .

01-=7:01-=x'0=7 +0 7+25+28-53=16

d) Calculate the acceleration when = 2.

1 25/WE- = 2700 (Z=7 for 1 9-10 = (7),1 = DO

Page 3

9 aged

1 5001- = Tr $+09.7 = \left(\frac{7}{78} - \frac{\epsilon}{8}\right) - m^{\circ}$ $\int_{0.5}^{1} h = \int_{0.5}^{1} \left[\frac{h}{2x^{2}} - \frac{\varepsilon}{\varepsilon x} \right]$ 409-5= xb(xe-x) }

Find the value of k for which the area of region A equals the area of region B. $y = \int_{0}^{\infty} (x^{2} - x^{2}) dx$ A 216 (x2-2x-2x) = A

State an integral which represents the area of region A.

V xb((662-x)-2) } = A = 25 0 0 = 25 2000 = 25

 $y = x^2 - 2x$, $y = \frac{1}{2}x$, y = k where k is a constant

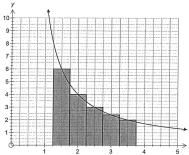
The graph below consists of the following functions:

Question 6 [3, 2, 3 = 8 marks]

State an integral which represents the area of region B and calculate the area.

Question 2 [3 marks]

The graph below shows the curve y = f(x), where f(3) = 2.4.



Use three of the five centred rectangles shown to estimate the shaded area under the curve from

There is no the live centred rectangles shown to estimate the shaded area under the curve from
$$= 1.75 \text{ to } x = 3.25.$$

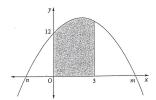
Here = $0.5 \times 4 + 0.5 \times 3 + 0.5 \times 2.4$

$$= 4.7 \text{ unds}^2$$

$$= 4.7 \text{ unds}^2$$

Ouestion 3 [5 marks]

Part of the graph of $f(x) = -x^2 + ax + 12$ is shown below:



If the area of the shaded section is 45 square units, determine the values of a, m and n, where *m* and *n* are the *x* intercepts of the graph of y = f(x).

Question 4 [2, 3= 5 marks]

The instantaneous rate with which the concentration C, in mg/KL, of a chemical compound in a river system changes with respect to time, t weeks, is modelled by the equation

$$\frac{dC}{dt} = \frac{1}{(t+0.5)^2} - 2t, \quad for \ t \ge 0$$

The initial concentration was 9.3 mg/KL.

Determine the net change in concentration in the first week. DC= S dC dt VOR DC= [-10.5-t2] For Justpool = 3 mg/KL = 4 mg/KL V

Find the maximum concentration and when this occurred

Man/Min when
$$d\xi = 0$$
 $d\xi = 0$
 d

Given that f(x) is continuous everywhere and that $\int_{-4}^{6} f(x) dx = 10$, find

a)
$$\int_{-4}^{6} (2x - 2f(x))dx = \int_{-4}^{6} 2x \, dx - 2 \int_{-4}^{6} f(x) \, dx$$

$$= \left[x \right]_{-4}^{6} - 2 \times 10$$

$$= 36 - 16 - 20$$

$$= 20 - 20$$
b)
$$\int_{-2}^{8} 3f(x - 2) \, dx = 0$$

b)
$$\int_{-2}^{8} 3f(x-2) dx = 0$$

$$= 3 \int_{-2}^{9} f(x-2) dx + \text{translate } F(x) = 2 \text{ units right}$$

$$= 3 \int_{-4}^{9} f(x) dx$$

$$= 3 \times 10$$

$$= 30$$
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