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WAEP Semester One Examination, 2020

Question/Answer booklet



Section Two:
METHODS
MIT 3

Calculator-assumed

WA student number: In figures

Number of additional answer booklets used (if applicable):	ten minutes one hundred minutes	Time allowed for this section Reading time before commencing work: Working time:
		Your nan
		ln words

# Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

This Question/Answer booklet Formula sheet (retained from Section One)

# To be provided by the candidate

Standard items: pens (blue/black prefetred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators, which can include scientific, graphic and

Computer Algebra System (CAS) calculators, are permitted in this ATAR

conrse examination

# Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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METHODS UNIT 3 2 CALCULATOR-ASSUMED

# Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

# Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
  examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
   Do not use erasable or gel pens.
- 3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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CALCULATOR-ASSUMED	19	METHODS UNIT 3
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Supplementary page

Question number:

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METHODS UNIT 3

CALCULATOR-ASSUMED

65% (98 Marks)

Section Two: Calculator-assumed

This section has **thirteen** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 Question 9

A seatood processor buys batches of n prawns from their supplier, where n is a constant. In any given batch, the probability that a prawn is export quality is p, where p is a constant and the quality of an individual prawn is independent of other prawns.

The discrete random variable X is the number of export quality prawns in a batch and the mean of X is 79.2 and standard deviation of X is 6.6.

State the name given to the distribution of X and determine its parameters n and p.

(4 marks)

Y follows a binomial distribution.

2.97 = n a p = 79.2 a p = 7.95 a p = 7.95 a p = 6.45 b = 1.75 b = 1.75Specific behaviours

✓ names binomial distribution
✓ equation for mean and variance (or sd)

v value of n

(b) Determine the probability that more than 50% of prawns in a randomly selected batch are export quality. (2 marks)

Solution  $50\% \times 176 = 88$   $50\% \times 176 = 88$   $P(X \ge 89) = 0.0797$ Specific behaviours
V lower bound
V probability

See next page

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METHODS UNIT 3 18 CALCULATOR-ASSUMED

Question 21 (8 marks)

When a byte of data is sent through a network in binary form (a sequence of bits - 0's and 1's), there is a chance of bit errors that corrupt the byte, i.e. a 0 becomes a 1 and vice versa.

Suppose a byte consists of a sequence of 8 bits and for a particular network, the chance of a bit error is 0.300%.

a) Determine the probability that a byte is transmitted without corruption, rounding your answer to 5 decimal places. (3 marks)

Solution  $X \sim B(8,0.003)$  P(X = 0) = 0.97625 Verific behaviours
<math display="block">Verific per verific p

Determine the probability that during the transmission of 32 bytes, at least one of the bytes becomes corrupted. (2 marks)

Solution  $Y \sim B(32, 0.02375)$   $P(Y \geq 1) = 0.5366$  Vorrect method Vorrect probability

A Hamming code converts a byte of 8 bits into a byte of 12 bits for transmission, with the advantage that if just one bit error occurs during transmission, it can be detected and corrected.

Determine the probability that during the transmission of 32 bytes using Hamming codes, at least one of the bytes becomes permanently corrupted.

(3 marks)

Solution  $H \sim B(12,0.003)$   $P(H \geq 2) = 0.00058$   $M \sim B(32,0.00058) \Rightarrow P(M \geq 1) = 0.0185$   $\Rightarrow P(32,0.00058) \Rightarrow P(M \geq 1) = 0.0185$   $\Rightarrow P(M \geq 1) = 0.0185$ 

End of questions anoisten to bn3

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Question 10 (8 marks)

The voltage,  $\ensuremath{\mathit{V}}$  volts, supplied by a battery t hours after timing began is given by

$$V = 8.95e^{-0.265t}$$

(a) Determine

(i)	the initial voltage.	Solution
(1)	the initial voltage.	V(0) = 8.95  V
		Specific behaviours
		✓ correct value

(ii) the voltage after 3 hours.

Solution
V(3) = 4.04  V
Specific behaviours
✓ correct value

(iii) the time taken for the voltage to reach 0.03 volts.

(1 mark)

(1 mark)

(1 mark)

Solution
t = 21.5  h
Specific behaviours
✓ correct value

(b) Show that  $\frac{dV}{dt} = aV$  and state the value of the constant a.

(2 marks)

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Solution
$$\frac{dV}{dt} = -0.265(8.95e^{-0.265})$$

$$= aV$$

$$a = -0.265$$
Specific behaviours
$$\checkmark \text{ correct derivative}$$

$$\checkmark \text{ value of } a$$

(c) Determine the rate of change of voltage 3 hours after timing began.

(1 mark)

(2 marks)

5 5
Solution
$\dot{V} = -0.265 \times 4.04 = -1.07 \text{ V/h}$
Specific behaviours
✓ correct rate

(d) Determine the time at which the voltage is decreasing at 5% of its initial rate of decrease.

Solution
$\dot{V} \propto V \Rightarrow e^{-0.265t} = 0.05$
t = 11.3  h
, , , , , , , , , , , , , , , , , , , ,
Specific behaviours
Specific beliaviours
√ indicatos suitable method

See next page

✓ correct time

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Question 20 (6 marks)

Given that f(2) = -3, f'(2) = 4, g(2) = 2 and g'(2) = 5, evaluate h'(2) in each of the following cases:

(a) 
$$h(x) = f(x) \cdot g(x)$$
.

(2 marks)

0.1.4
Solution
$h'(2) = f'(2) \times g(2) + f(2) \times g'(2)$
$= 4 \times 2 + (-3) \times 5$
= -7
Specific behaviours

✓ uses product rule✓ correct value

(b) 
$$h(x) = (g(x))^4$$
. (2 marks)

Solution
$h'(2) = 4 \times (g(2))^3 \times g'(2)$
$=4\times2^3\times5$
= 160
Specific behaviours
✓ uses chain rule
√ correct value

(c) 
$$h(x) = f(g(x))$$
. (2 marks)

Solution
$h'(2) = f'(g(2)) \times g'(2)$
$= f'(2) \times g'(2)$
$=4\times5$
= 20
Specific behaviours
✓ uses chain rule
✓ correct value

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See next page

(8 marks)

A small body moving in a straight line has displacement x cm from the origin at time t seconds Question 11

$$5.5 \le 5 \le 0$$
  $5.0 \le 1 \le 0$   $5.5 \le 1 \le 0$ 

Use derivatives to justify that the maximum displacement of the body occurs when t = 0.5.

$$(1 - 32) \operatorname{nis} 01 - \frac{xb}{3b} = \frac{xb}{3b}$$

$$(1-42)80302-=\frac{x^{2}}{2}$$

$$0S - = (0) \cos 0S - = \frac{x^2 b}{z_1 b} \approx 0.0 = 1$$

and so the body has a maximum displacement when t = 0.5.

# Specific behaviours

watement that justifies maximum value of second derivative at required time

(2 marks)

Determine the time(s) when the velocity of the body is not changing.

noibulos
$$(1 - 32)\cos 02 - \frac{x^2b}{53b} = n$$

$$0 = (1 - 32)\cos 0 = 0$$

sbroose 328.2, 285.1 
$$\approx \frac{1}{c} + \frac{\pi \epsilon}{\lambda}, \frac{1}{c} + \frac{\pi}{\lambda} = \frac{\pi}{c}$$

✓ states exact (or approximate) times in interval v indicates acceleration/second derivative must be zero ∨

(S marks) Express the acceleration of the body in terms of its displacement x.

√ correct expression

See next page

 $(1 - 32) \operatorname{mis} 01 - \frac{xb}{3b}$   $0 = (0) \operatorname{mis} 01 - \frac{xb}{3b} \Leftarrow 2.0 = 3$ 

Hence when t = 0.5, x has a stationary point.

 $(1 - 32)\cos 02 - = \frac{x^2 b}{24b}$ 

◆ first derivative

✓ indicates stationary point at required time

sbnoose 858.2, 285.1  $\approx \frac{1}{5} + \frac{\pi \epsilon}{4}, \frac{1}{5} + \frac{\pi}{4} = 3$ 

Specific behaviours

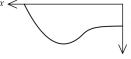
Specific behaviours

↓ factors out -4

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The edges of a swimming pool design, when viewed (7 marks) Question 19



 $^{2-x}9 + 27.2 = y$  bns  $22.9 - x\xi + ^2x2.0 - = y$ from above, are the x-axis, the y-axis and the curves

where x and y are measured in metres.

(S marks) Determine the gradient of the curve at the point where the two curves meet.

 $Y = {}^{8-8}9 = \xi + (\xi)4.0 - = Y$ Z = x nədw təəstəfini səvru

✓ x-coordinate of intersection Specific behaviours

√ common gradient

(4 marks)

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Determine the surface area of the swimming pool.

$$\mathcal{E}h \mathcal{T}.h \mathbf{I} \approx \frac{1}{29} - \frac{62}{4} = xb^{2-x}9 + 27.2 \int_{0}^{2} = {}_{\mathbf{I}}A$$

$$221.82 \approx \frac{222}{8} = xb 22.3 - x\mathcal{E} + {}^{2}x2.0 - \int_{2}^{2.51} = {}_{\mathbf{I}}A$$

$$\frac{3}{5} = \frac{8}{8} = x \times 2.5 = x \times 2.12$$

$$^{2}$$
 M  $^{2}$   $^{2}$   $^{2}$   $^{3}$   $^{2}$   $^{3}$   $^{2}$ 

Specific behaviours

√ area A<sub>1</sub> ✓ upper bound for parabola

✓ total area, with units

the pool in kilolitres (1 kilolitre of water occupies a volume of 1 m<sup>3</sup>). Given that the water in the pool has a uniform depth of 135 cm, determine the capacity of

√ correct capacity Specific behaviours  $C = 42.868 \times 1.35 \approx 57.87 \text{ kL}$ Solution

See next page 7-991-840NS

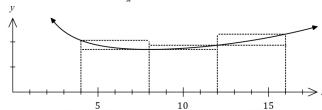
**METHODS UNIT 3** 

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CALCULATOR-ASSUMED

Question 12 (7 marks)

The function f is defined as  $f(x) = \frac{5e^{0.125x}}{x}$ , x > 0, and the graph of y = f(x) is shown below.



(a) Complete the missing values in the table below, rounding to 2 decimal places. (1 mark)

х	4	8	12	16
f(x)	2.06	1.70	1.87	2.31

Solution
See table
Specific behaviours
✓ both correct

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(b) Use the areas of the rectangles shown on the graph to determine an under- and overestimate for  $\int_{0}^{16} f(x) dx$ . (3 marks)

Solution
$U = 4(1.70 + 1.70 + 1.87) = 4 \times 5.27 = 21.08$
$0 = 4(2.06 + 1.87 + 2.31) = 4 \times 6.24 = 24.96$
Specific behaviours

- ✓ indicates  $\delta x = 4$
- ✓ under-estimate
- ✓ over-estimate

(c) Use your answers to part (b) to obtain an estimate for  $\int_{0}^{16} f(x) dx$ . (1 mark)

. , ,	$J_4$	, , ,
Solution		
$E = (21.08 + 24.96) \div 2 \approx$	23.	0
Specific behaviours		
✓ correct mean		

(d) State whether your estimate in part (c) is too large or too small and suggest a modification to the numerical method employed to obtain a more accurate estimate. (2 marks)

Solution
Estimate is too large $(f(x))$ is concave upwards).
Better estimate can be found using a larger number of thinner rectangles.
g . a g
Specific behaviours
✓ states too big
√ indicates modification to improve estimate

See next page SN078-155-4

(4 marks)

b) Use calculus to determine the coordinates of *P* that minimise *A*.

Solution
$$\frac{dA}{da} = \frac{3a^4 + 16a^2 - 64}{4a^2}$$

$$\frac{dA}{da} = 0 \Rightarrow a = \frac{2\sqrt{6}}{3} \approx 1.633$$

$$\frac{d^2A}{da^2} = \frac{3a^4 + 64}{2a^3} \bigg|_{a = \frac{2\sqrt{6}}{3}} = 4\sqrt{6} \Rightarrow \text{Minimum}$$
$$b = 8 - a^2 = \frac{16}{3}$$

Hence 
$$P\left(\frac{2\sqrt{6}}{3}, \frac{16}{3}\right) \approx P(1.633, 5.333)$$

#### Specific behaviours

- √ first derivative
- √ solves for a
- √ indicates check for minimum (graph, sign or second derivative test)
- ✓ correct coordinates, exact or at least 2 dp

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See next page

 $(x = X)_d$ х

drawn. The random variable X is the number of red balls selected in one game. selecting two balls at random, one after the other and with the first replaced before the second is A bag contains four similar balls, one coloured red and three coloured green. A game consists of

(3 marks)

(8 marks)

Complete the probability distribution for X below.

1 fo mus exam of 1
✓ one correct probability
Specific behaviours
(5290.0, 275.0, 0.3625)
$\frac{1}{9} = \frac{1}{9} = \frac{1}$
noituloS

√ all correct probabilities

(2 marks) Determine E(X) and Var(X). (q)

Solution 
$$E(X) = 0 + \frac{6}{16} + \frac{2}{16} + \frac{1}{2}; \quad Var(X) = \frac{3}{8} = 0.375$$

$$VB \ Using \ CAS, \ sd = \frac{\sqrt{6}}{4} \approx 0.6124.$$

$$Specific behaviours$$

$$Verpected value$$

$$Verpected value$$

probability that a player wins no more than three times when they play five games. A player wins a game if the two balls selected have the same colour. Determine the

(3 marks)

Solution
$$V \sim B\left(5, \frac{10}{16}\right)$$

$$V \sim B\left(5, \frac{10}{16}\right)$$

$$P(Y \leq 3) \approx 0.6185$$

$$V = Specific behaviours$$

$$V = States probability required$$

$$V = States probability required$$

$$V = States probability required$$

See next page

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CALCULATOR-ASSUMED

(8 marks)

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**METHODS UNIT 3** 

**Question 18** ゎ

curve at P and the coordinate axes. of the triangle formed by the tangent to the lies on the curve  $y = 8 - x^2$  and A be the area Let P(a,b) be a point in the first quadrant that

 $\frac{^2(8+^2n)}{n!} = 1.8 \text{ so work}$ (4 marks)

Equation of tangent:  $pz - = {}^d w \Leftarrow xz - = \frac{xp}{\kappa p}$ Gradient at P:

$$y - b = -2a(x - a)$$
  
 $y - b = -2ax + 2a^{2}$   
 $y - 6 = -2ax + 2a^{2}$ 

 $8 + {}^2 n = y \Leftrightarrow 0 = x \qquad \frac{8 + {}^2 n}{5} = x \Leftrightarrow 0 = y$ Axes intercepts:

 $\frac{(8+^{2}n)}{n^{4}} = (8+^{2}n)\left(\frac{8+^{2}n}{n^{2}}\right)\frac{1}{n^{2}} = \mathbb{A}$ 

Specific behaviours

- $_qm$  bns  $_b$  in terms of  $_a$  and  $_p$
- (mnof vns) V, x, x for small in terms of x, x, y (any form)
- √ axes intercepts
- √ indicates area of right triangle

See next page 7-991-840NS

A curve has equation  $y = (x - 3)e^{2x}$ .

(a) Show that the curve has only one stationary point and use an algebraic method to determine its nature. (3 marks)

Solution  

$$y' = 2xe^{2x} - 5e^{2x}$$

$$= e^{2x}(2x - 5)$$

For stationary point, require y' = 0 and since  $e^{2x} \neq 0$  then x = 2.5 - there is only one stationary point.

$$y'' = 4xe^{2x} - 8e^{2x}$$
  
 $x = 2.5 \Rightarrow y'' = 2e^5$ 

Hence stationary point is a local minimum.

# Specific behaviours

- √ first derivative
- ✓ uses factored form to justify one stationary point
- √ indicates minimum using derivatives (sign or 2nd)

(b) Justify that the curve has a point of inflection when x = 2.

(3 marks)

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# Solution

$$y'' = 4e^{2x}(x-2)$$

$$y''(1.9) = 4e^{2(1.9)}(1.9-2) \approx -18$$

$$y''(2) = 4e^{2(2)}(2-2) = 0$$

$$y''(2.1) = 4e^{2(2.1)}(2.1-2) \approx 27$$

Hence point of inflection as concavity changes from -ve to +ve as x increases through x = 2.

#### Specific behaviours

- √ shows second derivative is zero
- √ calculates second derivative either side
- ✓ explains justification

#### **Alternative Solution**

$$y'' = 4e^{2x}(x-2)$$
$$y''(2) = 4e^{2(2)}(2-2) = 0$$

$$y''' = 4e^{2x}(2x - 3)$$
$$y'''(2) = 4e^4$$

Hence point of inflection as f''(2) = 0 and  $f'''(2) \neq 0$ .

#### Specific behaviours

- ✓ shows second derivative is zero
- √ calculates third derivative
- √ explains justification

zero

#### See next page SN078-155-4

# Question 17

.....

(6 marks)

Some values of the polynomial function f are shown in the table below:

x	-2	-1	0	1	2	3	4
f(x)	-8	0	5	6	4	1	-3

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(a) Evaluate  $\int_{1}^{4} f'(x) dx$ .

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(2 marks)

Solution			
$\int_{1}^{4} f'(x)  dx = f(4) - f(1)$			
= -3 - 6			
= -9			

#### Specific behaviours

√ uses fundamental theorem

✓ correct value

The following is also known about f'(x):

Interval	$-2 \le x \le 1$	x = 1	$1 \le x \le 4$
f'(x)	f'(x) > 0	f'(x)=0	f'(x) < 0

(b) Determine the area between the curve y = f'(x) and the *x*-axis, bounded by x = -2 and x = 3. (4 marks)

# Solution

Area to left of x = 1 is above axis but to left is below so will need to negate/drop negative sign for that integral:

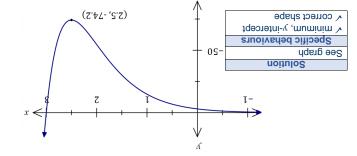
Area = 
$$\int_{-2}^{1} f'(x) dx - \int_{1}^{3} f'(x) dx$$
= 
$$f(1) - f(-2) - [f(3) - f(1)]$$
= 
$$2f(1) - f(-2) - f(3)$$
= 
$$2(6) - (-8) - 1$$
= 
$$19 \text{ sq units}$$

#### Specific behaviours

- ✓ integral for f'(x) > 0
- ✓ negated integral for f'(x) < 0
- √ uses fundamental theorem
- ✓ correct area

CALCULATOR-ASSUMED 9 METHODS UNIT 3 (C) Sketch the curve on the axes below. (2 marks)

See next page



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(2 marks)

80.0

0.12

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METHODS UNIT 3 12 CALCULATOR-ASSUMED

Question 16 (9 marks)

When a machine is serviced, between 1 and 5 of its parts are replaced. Records indicate that 7% of machines need 1 part replaced, 8% need 5 parts replaced, 12% need 4 parts replaced, and the mean number of parts replaced per service is 2.82.

Let the random variable X be the number of parts that need replacing when a randomly selected machine is serviced.

(a) Complete the probability distribution table for X below. (4 marks)

0.32

$ \Gamma = d + n + 72.0 $ $ 28.2 = 4.0 + 84.0 + d\xi + n\Delta + 70.0 $	
Solution Solution Let $P(x = 2) = a, P(x = 3) = b$ then	

14.0 = d

14.0

Specific behaviours  $\nabla$  values for x = 1, 4, 5

a = 0.32

Hence

0.07

 $(x = X)_d$ 

 $\checkmark$  equation using sum of probabilities  $\checkmark$  equation using expected value  $\checkmark$  values for x=2,3

(b) Determine Var (X). Using CAS,  $\sigma=1.00379281$  Hence  $Var(X)=\sigma^2=1.0076$ 

Specific behaviours

vindicates ad using CAS

v correct variance

The cost of servicing a machine is \$56 plus \$12.50 per part replaced and the random variable Y is the cost of servicing a randomly selected machine.

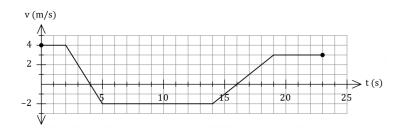
Determine the mean and standard deviation of Y. (3 marks)

Solution Y = 56 + 12.5X  $E(Y) = 56 + 12.5 \times 2.82 = \$91.25$   $\sigma_{Y} = 12.5 \times 1.00379 \approx \$12.55$   $\sigma_{Q} = 12.5 \times 1.00379 \approx \$12.55$ 

See next page 5-7-87-078

Question 15 (9 marks)

A small body leaves point A and travels in a straight line for 23 seconds until it reaches point B. The velocity v m/s of the body is shown in the graph below for  $0 \le t \le 23$  seconds.



(a) Use the graph to evaluate  $\int_0^4 v \, dt$  and interpret your answer with reference to the motion of the small body. (3 marks)

Solution
$$\int_{0}^{4} v \, dt = 2 \times 4 + \frac{1}{2} \times 2 \times 4 = 12 \text{ m}$$

The change in displacement of the body during the first 4 seconds is 12 m.  $\overline{\text{OR}}$ 

The body has moved 12 m to the right of P during first 4 seconds.

# Specific behaviours

- √ value of integral
- √ interprets as change in displacement
- ✓ includes specific time and distance with units in interpretation
- (b) Determine an expression, in terms of t, for the displacement of the body relative to A during the interval  $2 \le t \le 5$ . (3 marks)

Solution				
$v = 8 - 2t \Rightarrow x = \int 8 - 2t  dt = 8t - t^2 + c$				
$t = 2, x = 8 \Rightarrow 8 = 8(2) - 2^2 + c \Rightarrow c = -4$				
$x = 8t - t^2 - 4$ , $2 \le t \le 5$				

#### Specific behaviours

- ✓ expression for v
- $\checkmark$  expression for x with constant c
- $\checkmark$  correct expression for x

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CALCULATOR-ASSUMED

Determine the time(s) at which the body was at point A for  $0 < t \le 23$ .

# It point A for $0 < t \le 23$ . (3 marks)

Solution  

$$x(5) = 12 + \frac{1}{2} \times 1 \times (-2) = 11$$

$$11 - 2(t - 5) = 0 \Rightarrow t = 10.5$$

$$x(19) = -4.5$$
$$-4.5 + 3(t - 19) = 0 \Rightarrow t = 20.5$$

Body at point A when t = 10.5 s and t = 20.5 s.

#### Specific behaviours

- √ indicates appropriate method using areas
- ✓ one correct time
- √ two correct times

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