8 P a g e

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b) Determine how far the bullet penetrates the wall before coming to rest to the nearest mm.

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Course Specialist Year 12 Test Four 2022

Formula sheet provided:	Yes	
Task weighting:	% 0τ-	
Marks available:	nsm04	
Special items:	_	ents, templates, No notes allowed for use in the WACE
Standard items:		preferred), pencils (including coloured), sharpener, sape, eraser, ruler, highlighters
Materials required:	Upto 3 Calcula	rs with CAS capability (to be provided by the student
Number of questions:	9	
Time allowed for this tas	;	suim _
_sak type:	Кеsbonse	
Student name:		

No notes allowed

1 Page

Note: All part questions worth more than 2 marks require working to obtain full marks.

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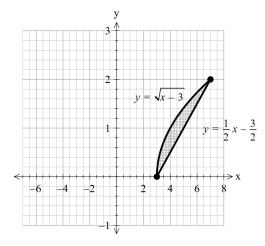
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No notes allowed

Q1 (5 marks) (4.1.6)

Determine the volume of the solid formed by rotating the area enclosed between

$$y = \sqrt{x-3} \& y = \frac{1}{2}x - \frac{3}{2}$$
 about the y axis, as shown below.



Consider a particle that is moving with SHM such that $\ddot{x} = -9x$ with a maximum speed of 12 m/s. a) Determine the exact speed when the particle is half of an amplitude from the origin.

b) Determine the percentage of the time that the particle is more than half an amplitude from the centre.

The motion of a bullet through a wall is modelled by the equation $a = -25(v + 75)^2$, v > 0 where $a m / s^2$ is its acceleration and v m / s its velocity t seconds after impact. Initially at impact the speed is 300 m/s and is at the origin (x = 0 metres)

a) Determine X in terms of Y only.

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Q2 (5, 3 & 2= 10 marks) (4.1.4)

differential equation $\frac{dN}{dt} = aN - bN^2$ and C is a constant. a) By using integration and partial fractions, show how to derive

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Q4 (5 marks) (4.2.1)

Determine expressions in terms of ${}^{X \otimes Y}$ only for $\frac{dy}{dx} \otimes \frac{d^2y}{dx^2}$ in terms of ${}^{X, Y \otimes Y}$ only, using the following equation ${}^{X^2} \cdot \mathbb{P}^2 = \mathbb{P} \cdot \chi$

3 | P a g e 9 g e 4 | 9 Q2 continued

b) Let $\frac{N}{dt}$ equal the number of kangaroos living in a habitat after t years and $\frac{dN}{dt} = \frac{1}{5}N - \frac{1}{12500}N^2$

If initially there are 50 kangaroos, determine the number in 10 years time.

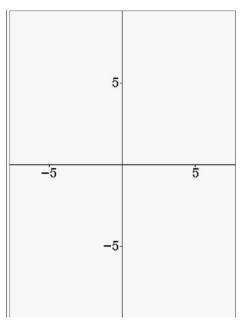
c) Determine the size of the population at the maximum growth rate.

4 | P a g e

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$$\frac{dy}{dy} = 3$$

a) Sketch the slope field on the axes below for dx



- b) Show the solution curve on the axes above that passes through point (2,2).
- c) Determine in cartesian form the solution curve for b above without using a classpad. Hint – use logarithmic differentiation. Show all working.