

**ROSSMOYNE SHS   SEMESTER 1, 2009**  
**UNIT 3A MATHEMATICS EXAMINATION**  
**SECTION A NON-CALCULATOR SECTION**

TIME                  40 minutes  
 AVAILABLE MARKS    40 marks

Some formulae you might find useful:  
 $\text{Area of triangle} = \frac{1}{2}ab \sin C$   
 $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$   
 $a^2 = b^2 + c^2 - 2bc \cos A$

0	cos	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$
sin	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$
	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$		

(a) Find the area of the triangle below.

Give answers in **exact values** with a rational denominator. All measurements are in cm.

Question 3      (2, 2 marks)

Simplify, expressing your answer in positive indices.  

$$\frac{28a^3b^2}{36(a^2)^3b^9}$$

Question 2      (2 marks)

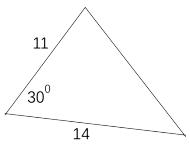
(b) Simplify  $\frac{12x^{3n-1}}{3^{n-1} + 3^n}$  giving the answer in positive indices.

Question 1      (2, 3 marks)

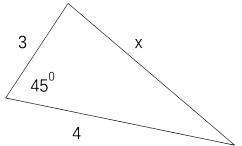
(a) Solve  $(x+1)^{\frac{7}{3}} = 125$

Question 3      (2, 2 marks)

(a) Find the area of the triangle below.



- (b) Find the value of  $x$



Question 4 (2 marks)

A small high school runs two 3A Mathematics classes. Following a test, the mean mark of the first class of 18 students is 82 and the mean mark of the other class of 25 students is 74.  
**Explain** how the combined mean mark of these two classes would be calculated. (You are not required to calculate it.)

Question 5 (1, 2 marks)

If digits can only be used **once**.

- (a) How many 4 digit odd numbers can made using the digits 2, 3, 4, 5, 6?  
(b) How many of the above numbers are greater than 5000?

Question 6 (7 marks)

Find a and b and draw a box and whisker diagram for the above ten scores on the axes below.

$$\text{range} = 7 \quad \text{median} = 5.5$$

a    3    4    5    5    b    7    8    8    9

The following scores are arranged in ascending order

Question 11. (4 marks)

Su-lin's standardised score in a Mathematics test was 1.4. The mean and standard deviation for the class were 66% and 5.5% respectively. What was Su-lin's raw percentage mark?

Question 10 (2 marks)

$$27, -18, 12, -8, \frac{5}{1}, \frac{3}{1}, \dots$$

Write the recursive rule for the sequence below

Question 9 (2 marks)

sequence.

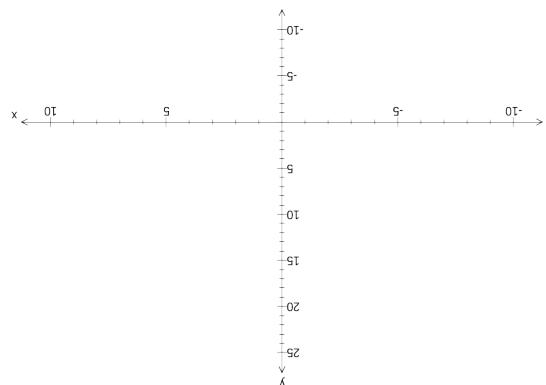
A sequence has the recursive formula  $T_{n+1} = (2)^n T_n$ , with  $T_2 = 4$ . Find  $T_1$ ,  $T_3$  and  $T_4$  of the

Question 8 (3 marks)

What is the tenth number in terms of  $m$ ?

Nine numbers have a mean of  $m$ . When a tenth number is added, the mean of all ten is  $(m - 0.4)$ .

Question 7 (3 marks)



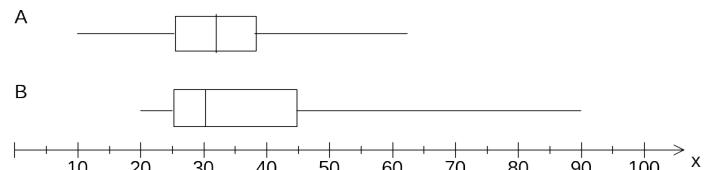
Sketches of each curve on the same set of axes to support

Describe how the graph of  $y = 2(x + 2)^2$  compares to that of  $y = (x - 5)^2$ . 4. Draw well-labelled

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Question 12 (3 marks)

Given that  $a$ ,  $b$  and  $c$  are all positive integers, draw a graph that best represents  $y = a(x - b)^2(c - x)$ . Label all the intercepts.



Write four statements comparing the distributions shown in the box plots above.

Question 14. (5 marks)

Tyson, a young man about town, is in the market for a new car and has narrowed his choice to four cars. The different aspects of the cars and the respective weightings placed by him are as follows.

	Macho rating	Acceleration	Price	All terrain capability	Fuel economy
Weighting	6	5	4	3	2
Car A	7	6	6	4	7
Car B	8	5	7	5	2
Car C	8	7	6	5	5
Car D	6	8	6	6	5

Calculate the weighted scores of the four cars.

Tyson will buy the car with the highest weighted score. Which one will he buy?

Question 15 (2 , 2 marks)

Skye has inherited \$540 000 from her grandmother and will invest \$500 000 in an account paying 3.5% per annum compounded half yearly. She plans to make only one withdrawal each year.

- For how many years will she be able to withdraw \$40 000 a year from this account?
- If she would like the money to last for 20 years, how much will she be able to withdraw from the account each year?

**End of Part A**

**End of Part B**

**ROSSMOYNE SHS**  
**UNIT 3 MATHEMATICS EXAMINATION**  
**SEMESTER 1, 2009**

Of the 130 people at a conference, 52 were male and 97 were 40 years or older. The number of females delegates younger than 40 years was half that of males less than 40 years old.

Question 1. (3, 2, 3 marks)

**SECTION B APPROVED CALCULATORS PERMITTED**

TIME: 80 minutes  
 MARKS ALLOCATED 80 marks

(a) Show the above information in a Venn diagram.  
 (b) How many delegates were male aged 40 years or more?  
 (c) What is the probability that a person chosen at random will be  
 (i) a male aged less than 40 years?  
 (ii) a female aged under 40 years?  
 (iii) a female given she is at least 40 years old?

Question 11. (2, 3 marks)

- Part-time jobs.
- |         |    |                    |                      |
|---------|----|--------------------|----------------------|
| 0 - 9   | 10 | Number of students | Weekly earnings (\$) |
| 30 - 39 | 3  |                    |                      |
| 40 - 49 | 5  |                    |                      |
| 50 - 59 | 4  |                    |                      |
| 60 - 69 | 11 |                    |                      |
| 70 - 79 | 7  |                    |                      |
| 80 - 89 | x  |                    |                      |
- The frequency table below shows the weekly wages earned by some students who have

standard deviation for the students' weekly earnings.

Find the mean and	x	x	x
80 - 89			
70 - 79			
60 - 69			
50 - 59			
40 - 49			
30 - 39			
0 - 9			

Question 2. (2, 1, 2, 2 marks)

A doctor notes that in the last two years, 24 of his patients were diagnosed with some form of cancer. 18 of these patients had been exposed to harmful chemicals in their workplace. 5 had not been exposed to chemicals but were smokers. A total of 20 patients were smokers. Represent this information in a two way table and use it to answer the following.

What is the probability that a cancer patient of this doctor

- (a) is neither a smoker nor has been exposed to chemicals?  
 (b) is a smoker but has not been exposed to chemicals?  
 (c) is a smoker given he/she has not been exposed to chemicals?  
 (d) is not a smoker given he/she has been exposed to chemicals?

Question 3. (1, 1, 2 marks)

- (a) Write the recursive rule used to calculate the amount Kumar will owe at the end of each year.  
 (b) In which year will he owe less than \$10 000?  
 (c) After how many years will he finally pay off his loan? What will Kumar's final payment be?

Kumar borrows \$25 000 at interest rate of 5.5% p.a.. He agrees to pay \$5 000 at the end of each year.

Find the value of x if the mean is 54.5. Show clearly how you obtained your answer.

Question 12. (2, 1, 2 marks)

- (a) Find the standard deviation for the students' weekly earnings.

(b) Find the value of x if the mean is 54.5. Show clearly how you obtained your answer.

(a) If  $x = 2$ ,

Weekly earnings (\$)	Number of students	Find the mean and	x	x	x
0 - 9	10				
30 - 39	3				
40 - 49	5				
50 - 59	4				
60 - 69	11				
70 - 79	7				
80 - 89	x				

The frequency table below shows the weekly wages earned by some students who have

part-time jobs.

- (a) How many of these arrangements have the three vowels next to each other?  
 (b) How many of these arrangements have the vowels and the consonants occupying different positions?  
 (c) What is the probability that the word 'comes' commences with an M and the vowels are together?

All the letters of the word FORMULA are to be arranged at random in a row.

Question 10. (2, 2, 2 marks)

- (a) Solve the following. All working must be shown.

$$(a) 3^{2a} - 12(3^a) = -27$$

$$(a) 7^{3a+2} \times 7^{-1-a} = \frac{1}{16807}$$

(b) What is the maximum monthly production of the gold mine?

(c) What is the total amount of gold in troy ounces was produced in the first twelve years of its

operation?

(d) Figures formed a geometric sequence until full production is reached in the fifth month. Therefore, this

amount is maintained.

Produced. In the third month it produced 392 troy ounces of gold. Successive monthly production

Aziz is driving across the Nullabor to Melbourne and taken a collection of these CDs –  
2 Country and Western, 3 Jazz, 2 modern music and 4 classical music.

In how many ways can he listen to all of them if

- (a) he does not mind the order?
- (b) the Country and Western CDs are the first and the last CDs?
- (c) he listens to the Country and Western ones first, then the Jazz, then the modern music ones and finally the classical CDs?

Question 4. (1, 1, 1, 1, 1 marks)

Match the correct equations with the graphs below. Use the **letter** (eg A, B etc) and not the equation.

**A**  $y = \frac{2}{x}$

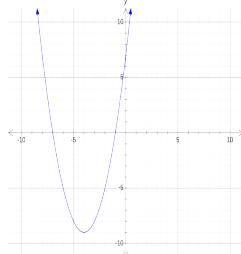
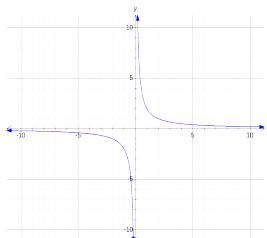
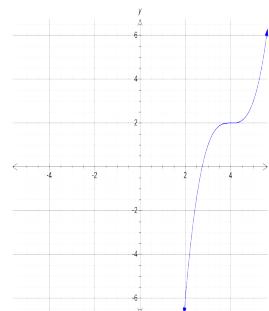
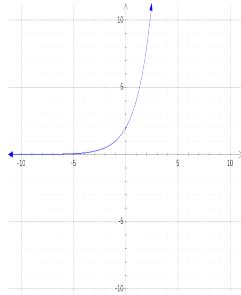
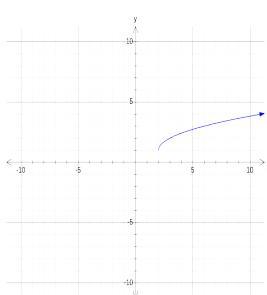
**B**  $y = \frac{1}{x+2}$

**C**  $y = 2\sqrt{x}$

**G**  $y = (x-4)^3 + 2$

**H**  $y = \sqrt{x-2} + 1$

**I**  $y = \frac{1}{(x-4)^2} + 3$



Question 5. (2 marks)

The Health Department needs an estimate of patients infected with Porcine Flu. The names on List A are patients who exhibit symptoms of the disease, List B has some names of people from the Procine Flu Association.. List A had 263 names. List B had 127 names of whom 81 were also on List A.

- (a) How many sufferers of Porcine Flu do these figures suggest exist in the population as a whole?

- (b) How many of these do not feature on either list?

Question 6. (2, 1, 2, 1 marks)

In 1990 it was noticed that the population of rock wallabies in Wayugal Reserve was increasing according to the equation  $y_w = 40 + 0.1(x^2 + 20x)$  whilst the population of feral goats in the same area was increasing according to the equation  $y_g = 20(1.09)^x$  where  $x$  is the number of years after 1990. Use your CAS calculator to answer the following questions.

- (a) How many

(i) rock wallabies were there in 1990? \_\_\_\_\_

(ii) feral goats were there in 1990? \_\_\_\_\_

- (b) In which year and month will the two populations equal each other if these rates of increase are maintained?

- (c) In 2005, the shire council removed forty goats from the population in an eradication programme. If, after the eradication, the two populations will still continue to increase at the same rates, write the equations of the growths of the rock wallabies and feral goats from 2005 onwards.

- (d) In which year will the two populations equal each other? \_\_\_\_\_

Question 7. (2, 3 marks)

L varies directly proportional to  $x$  and inversely proportional to  $\sqrt{y}$ . If  $L = 24$  when  $x = 2$  and  $y = 9$

- (a) Find  $L$  in terms of  $x$  and  $y$ .

- (b) Find the exact value of  $x$  when  $L = 8$  and  $y = 72$ .

Question 8. (3, 3 marks)

In the first month of operation a small gold mine produced 200 troy ounces of gold. (The mass of gold is defined in troy ounces where 1 troy ounce = 31.103 g.) In the second month 280 troy ounces were