



MATHEMATICS METHODS YEAR 11

TEST 3, 2018

Formula Sheet

Write answers in the space provided beneath each question.

Pens, pencils, eraser, ruler

Standard Items:

:smə11 İbiəsq2

IMPORTANT NOTE TO STUDENTS:

Free test. When directed, you will place all other items under your chair.

It is recommended that students do not use pencil, except in diagrams.

marks to be awarded for reasoning. Incorrect answers given without supporting reasoning Show all working clearly, in sufficient detail to allow your answers to be checked and for

Calculator-Free test-paper are the only items permitted on your desk during the Calculator-The standard items listed above, a Formula Sheet provided by the supervisor and this

cannot be allocated any marks.

Marks are shown with the questions.

INSTRUCTIONS TO STUDENTS

You are required to answer ALL questions. Do not open this paper until instructed to do so.

MATERIAL REQUIRED/RECOMMENDED FOR THIS TEST

- Time Allowed: 25 minutes Total Marks: 24 Student's Name: Mark Kinko

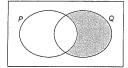
 - SECTION ONE: CALCULATOR-FREE

 - (Trigonometric Functions, Probability)

Question 1[2, 1, 1, 1 = 5 marks]

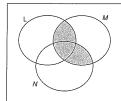
(a) Describe the shaded region in set notation.

(i)



P'nQ ✓

(ii)



 $M \cap (L \cup N) \ \underline{or} \ (L \cap M) \cup (M \cap N)$

b) $U = \{\text{positive integers between 1 and 20, where 1 and 20 are not included}\}$

 $A = \{ \text{prime numbers less than 19} \}$ $A = \{ 2, 3, 5, 7, 11, 13, 17 \}$ $B = \{ \{ 2, 3, 4, 6, 12 \} \}$ $C = \{ \{ 3, 6, 7, 12, 15, 18 \} \}$ State the following:

(i) AnBnC

Question 2 [2, 4 = 6 marks]

(b) Use the sum of two angles to find the exact value of
$$\ \tan\frac{7\pi}{12}$$
 . Rationalise the denominator of your solution.

$$\frac{1}{\left(\frac{\pi}{\varepsilon} + \frac{\pi}{\rho}\right)} \ln st = \left(\frac{\pi \rho}{2\tau} + \frac{\pi \varepsilon}{2\tau}\right) \ln st$$

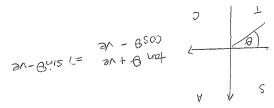
$$\frac{\pi}{\varepsilon} \ln st + \frac{\pi}{\rho} \ln st$$

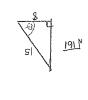
$$\frac{2-\frac{2}{8N2+1}}{\frac{8N2+1}{(8N+1)}}$$

Given that $\cos\theta=-\frac{8}{15}$ and $\tan\theta$ is positive, find the exact value of $\cos 2\theta$.

$$\sqrt{\frac{131}{6}} - \frac{1}{25} \times \frac{1}{21} = \theta \text{ nis}$$

$$\sqrt{\frac{161}{6}} - \frac{1}{25} \times \frac{1}{21} = $





Question 8 [4 marks]

Question 3 [1, 1, 1, 2 = 5 marks]

A doctor wishes to tell her patient's family the probability of his condition improving after a certain treatment. Suppose I is the event that the patient's condition improves, O is the event that his condition remains the same and W is the event that his condition worsens.

If P(W) = 30% and P(O) = 10% find the probability that the patient's condition: P(I) = 60%.

(a) improves.

$$\rho(I) = 100\% - \rho(W) - \rho(0)$$

$$= 100\% - 30\% - 10\%$$

$$= 60\%$$

(b) does not improve.

(b) does not improve.

$$\rho(\bar{I}) = \frac{100\% - \rho(I)}{100\% - 60\%}$$

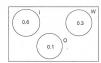
$$= \frac{100\% - 60\%}{100\% - 60\%}$$
(c) increase a taught

improves or stays the same.

70%
$$P(IUO) = P(I) + P(O)$$

= 60% + 10%
= 70% /

(d) Draw a Venn diagram which shows that these three events are mutually exclusive.



/ No intersection
/ Labels, etc.

Accept overlapping
if clear prob. = 0.

Question 7 [3, 1, 1, 1, 1, 2, 1 = 10 marks]

G and H are events such that P(G) = 0.7, $P(G \cap H) = 0.4$ and $P(G \cap H) = 0.2$.

(a) Complete the two-way table below.

	H	· H	
G	0.4	0.3	0.7
G'	0.2	0.1	0.3
	0.6	0.4	1

(b) Find:

0.3 ✓

0.6 ✓

(iii)
$$P(G' \cap H')$$

0.1 ✓

(iv)
$$P(GUH) = P(G) + P(H) - P(G \cap H)$$

0.9 $V = 0.7 + 0.6 - 0.4 /$

(v)
$$P(G|H) = P(G \cap H) = \frac{0.4}{0.6} = \frac{4}{6}$$

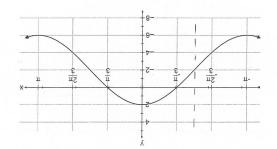
(c) Show that G and H are not mutually exclusive.

Not mutually exclusive: $P(G \cap H) = 0.4$ Should be 0

Question 4 [4, 2, 2 = 8 marks]

The graph below can be written $k(x) = a \cos(x) - b = c \sin(x - d) - b$

(a) Determine the values of a, b, c and d.



$$\Delta - \left(\frac{\pi}{\Delta} - x\right) \text{ nis} A = \Delta - (x) \cos A$$

$$\frac{\pi}{2}$$
 - = b \neq = or $c = \frac{\pi}{2}$ or $c = b$ \neq = c

Almoh hade
$$= 3 - 6 = 4 + 4 = 4 - 6 = 4$$
 with alound $= 3 - 6 = 4$ without (a) State the range of $k(x)$.

(b) State the range of $k(x)$.

 $P_{k(x)} = \{y : -6 \le y \le 2, y \in \mathbb{R}\}$

using the vertical line test on the graph. (c) Explain why the graph represents a function and verify your explanation by

For every x value there is only one y value

Vertical line through graph

(8)

Question 6 [2, 3, 1 = 6 marks]

tha-1 410.6-

 $\frac{\pi}{8}$ To $\frac{\pi}{8}$ = -x

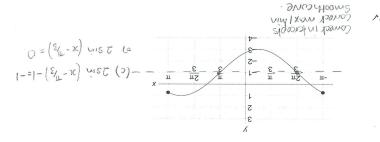
(a) Write the equation of a sine function with the following features: an amplitude of $\Omega = \Omega = 0$ and $\Omega = 0$ an

a vertical translation of I in the negative direction

b+ (2-209) visp = 8

 $f - \left(\frac{\pi}{\varepsilon} - x\right) \text{ nis } S = \chi$

(b) Draw the function from (a) on the axes below for the domain $x \in [-\pi,\pi]$:



(c) Use the graph from (b), or otherwise, to find the solutions to Z sin $\left(x - \frac{\pi}{3}\right) = 0$ in the

1-= h pro



MATHEMATICS METHODS YEAR 11

TEST 3, 2018

(Trigonometric Functions, Probability)

SECTION TWO: CALCULATOR-ASSUMED

Student's Name: Mark Kinké

Total Marks: 💚

Time Allowed: 30 minutes

MATERIAL REQUIRED/RECOMMENDED FOR THIS TEST

Standard Items:

Pens, pencils, eraser, ruler

Special Items:

Up to three approved calculators

One page (unfolded A4 sheet) front and back of Notes

Formula Sheet retained from Section One

INSTRUCTIONS TO STUDENTS

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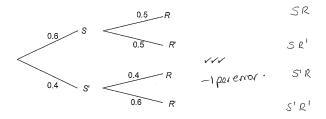
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Question 5 [3, 1, 1, 2, 2 = 9 marks]

Given the following: P(R|S) = 0.5, P(R|S') = 0.4 and P(S) = 0.6

(a) Complete the tree diagram showing all the probabilities.



(b) Determine the following:

(i)
$$P(SnR) = 0.6 \times 0.5$$

(ii)
$$P(S' \cap R') = 0.4 \times 0.6$$

(iii)
$$P(R) = 0.6 \times 0.5 + 0.4 \times 0.4$$

$$= 0.3 + 0.16$$
0.46

(iv)
$$P(S|R) = 0.4 \times 0.4 = 0.16$$

0.348 or $\frac{16}{46}$ \checkmark 0.46