## A COLLEGE OF THE UNITING CHURCH IN AUSTRALIA RESBYTERIAN LADIES' COLLEGE

## MATHEMATICAL METHODS YEAR 12 - TEST 4 **MATHEMATICS DEPARTMENT**

. ВижМ	DATE: 15th August 2016

Reading Time: 3 minutes

SECTION ONE: CALCULATOR FREE

WORKING TIME: Maximum 20 minutes

pens, pencils, pencil sharpener, highlighter, eraser, ruler, SCSA formula sheet :ТИЭМЧІОЎЭ 18 marks :JATOT

SECTION TWO: CALCULATOR ASSUMED

WORKING TIME: Minimum 30 minutes

32 marks :JATOT

pens, pencils, pencil sharpener, highlighter, eraser, ruler, drawing instruments, templates, up to 3 calculators, SCSA formula sheet (provided), :ТИЭМЧІОЎЭ

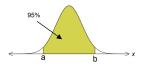
one A4 page of notes (one side only)

	90	JATOT			
	32	Sect 2 Total		8Т	Sect 1 Total
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Marks awarded	Marks available	Question	Marks Awarded	Marks available	Question

The given diagrams show the shaded regions as a percentage of the entire area under the curve. Using the "68, 95, 99.7" rule determine the values of a or a and b in each of the following:

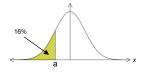
) (2 marks)

$$\mu$$
=5  $\sigma$ =2



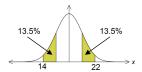
(b) (1 mark)

$$\mu$$
=30  $\sigma$ =8



(c) (2 marks)

$$\mu = a$$
 $\sigma = b$ 



Question 2 (8 marks)

The continuous random variable, X, has the probability density function f, where

$$\begin{array}{ccc}
1 \ge x \ge 0 & x \lambda \\
\xi \ge x > 1 & (x - \xi) \lambda \frac{1}{\zeta}
\end{array}
= (x) \mathcal{I}$$

(a) Show that 
$$k = 2/3$$
 (4 marks)

(b) Find the expected value of X.

Question 3 (5 marks)

Explain why each of the following sampling methods does not represent a random sample.

(a) To predict the outcome of a State Government election, a public opinion poll telephones people randomly selected from a telephone directory to ask which political party they intend voting for on the day of the election. (Give two reasons) (2 marks)

(b) In order to obtain an estimate of the average income of PLC graduates ten years after their graduation all 2006 graduates are to be sent a questionnaire. An estimate of the average income is to be made using the ones that were returned. (1 mark)

(c) At a school assembly the principal of a school with 720 students asks for 20 students to put themselves forward to represent the school at an Anzac Day Dawn Service. (Give two reasons)

(2 marks)

Question 7 (8 marks)

The mean  $\mu$  and standard deviation  $\sigma$  of the uniform distribution on the interval [a, b] are given by

$$\mu = \frac{a+b}{2} \quad \text{and} \quad \sigma = \frac{b-a}{2\sqrt{3}} \ .$$

A calculator can generate random numbers that are uniformly distributed between 0 and 1.

- a) For this distribution of the random numbers generated by the calculator, calculate
  - (i) the mean. (1 mark)
  - i) the standard deviation (to **three (3)** decimal places). (1 mark)
- (b) What is the probability that a randomly generated number lies between  $\frac{1}{4}$  and  $\frac{1}{3}$ ? (1 mark)
- (c) What is the probability that a randomly generated number contains no seven in its first **five (5)** digits? (1 mark)
- (d) What is the probability that a randomly generated number contains at most three odd digits in its first five digits? Give your answer to **four (4)** decimal places. (2 marks)

(e) Another uniform distribution on an interval [a, b] has a standard deviation of  $2\sqrt{3}$ . How wide is the interval? (2 marks)

al, would it matter which one was adopted?	sop tnemeganam et eveithe management so	(p)
	Alternatively, the production sector could achieve the the standard deviation at 2.55 grams and altering the mean weight be set at?	(c)
	The production department decides to maintain the man achieve the management requirement by altering standard deviation be set at?	(q)
	igement is concerned about the high percentage of yog nction department that only half of one percent of yoghu	
(J mark)	What percentage of these yoghurts are underweight?	(a)
	o! Yoghurt Company, a manufacturer of flavoured yogl iners. The weights of the yoghurts are found to be norn ard deviation 2.55 grams.	conta
(7 marks)	4 noit	бnea

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g

Explain your answer.

Section 2: Calculator Assumed

(S marks)

Question 6 (4 marks)

The percentage marks of students sitting for a national mathematics competition were found to be normally distributed. The award of Distinction was presented to 15% of the candidates for achieving a mark in excess of 80% and the top 5% of candidates in addition to the Distinction award also received a prize of a gift-voucher for achieving a mark in excess of 90%. Find the mean and standard deviation of the mathematics scores, giving answers to one decimal place.

8

Question 5 continued ...

(e) Find the 0.7 quantile and explain what it means. (2 marks)

(f) What is the probability that a Briteglobe bulb will last no more than 3500 hours, if it has already lasted 3200 hours? (3 marks)

(g) Find the probability that in a sample of five Briteglobe bulbs, exactly two will last between 3000 and 3200 hours. (3 marks)

(2 marks)

Calculate the inter-quartile range for this distribution.