

Markers use only		
Question	Maximum	Mark
1	6	
2	5	
3	5	
4	8	
5	7	
6	5	
7	9	
8	7	
S1 Total	52	
S1 Wt	35%	
S2 Wt	65%	
Total	100%	

MATHEMATICS

METHODS

UNIT 3

Section One:

Calculator-free

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total					100

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Supplementary page

Question number: _____

Section One: Calculator-free

35% (52 Marks)

This section has eight (8) questions. Answer all questions. Write your answers in the spaces provided.

Working time: 50 minutes.

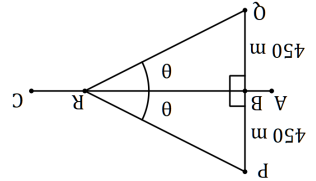
Question 1

A box contains five balls numbered 2, 3, 4, 5 and 6. Three balls are randomly drawn from the box at the same time and the random variable X is the largest of the three numbers drawn.

(a) By listing all possible outcomes (234, 235, etc.), determine $P(X \leq 5)$.

(a) By forming expressions for PR , BR and CR , show that $X = 1200 + 450(2 - \cos \theta) \frac{\sin \theta}{\sin \theta}$.

Let $\angle PRB = \angle QRB = \theta$, where $0 < \theta < 90^\circ$, and $X = PR + QR + CR$, the sum of the distances of the train from the houses and station.



Two houses, P and Q , are 900 m apart on either side of a straight railway line AC . AC is the perpendicular bisector of PQ and the midpoint of PQ is B . A small train, R , leaves station C and travels towards B , 1200 m from C .

Question 8 (7 marks)

(b) Construct a table to show the probability distribution of X .

(c) Calculate $E(X)$.

(b) Use a calculus method to determine the minimum value of X .

(4 marks)

Question 2

(5 marks)

Question 7

(9 marks)

A function defined by $f(x)=13+18x-6x^2-2x^3$ has stationary points at $(1,23)$ and $(-3,-41)$.

The function g is such that $g'(x)=ax^2+18x+b$, it has a point of inflection at $(-1,29)$ and a stationary point at $(1,-19)$.

(a) Use the second derivative to show that one of the stationary points is a local maximum and the other a local minimum. (3 marks)

(a) Determine $g(2)$. (5 marks)

(b) Determine the coordinates of the point of inflection of the graph of $y=f(x)$. (2 marks)

(b) Determine

(i) $\int_1^2 g'(x) dx$. (2 marks)

(ii) $\int_1^2 4g'(x)+16 dx$. (2 marks)

(5 marks)

A particle travels in a straight line so that its distance x cm from a fixed point O on the line after t seconds is given by

$$x = -\frac{3t^3}{2t+1}, t \geq 0.$$

Calculate the acceleration of the particle when $t = 1$.

(5 marks)

The height, in metres, of a lift above the ground t seconds after it starts moving is given by

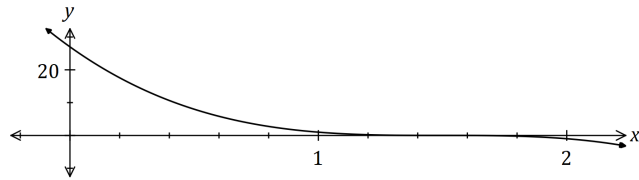
$$h = 2 \cos^2 \left(\frac{\pi}{5} t \right).$$

Use the increments formula to estimate the change in height of the lift from $t = \frac{5\pi}{6}$ to $t = \frac{17\pi}{20}$.

Question 4

(8 marks)

The graph of $y = (3 - 2x)^3$ is shown below.



- (a) Determine the area of the region enclosed by the curve and the coordinates axes. (4 marks)

- (b) Given that the area of the region bounded by the curve, the x -axis and the line $x = k$ is 8 square units, determine the value of k , where $0 < k < 1.5$. (4 marks)

Question 5

(7 marks)

Determine $\frac{dy}{dx}$ for the following, simplifying each answer.

- (a) $y = \sqrt{5 - 6x}$. (2 marks)

- (b) $y = 3x^4 \sin(4x)$. (3 marks)

- (c) $y = \int_x^2 \frac{1}{\sqrt{1+t}} dt$. (2 marks)