

## Important note to students

<b>To be provided by the student</b>	highlighters fluid/tape, ruler, pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, pens, pencils, pencil sharpener, eraser, correction special items: hightlighters A4 paper,
<b>To be provided by the supervisor</b>	standard items: pencils, pencil sharpener, eraser, correction formula Sheet (retained from Section One) This Question/Answer Booklet
<b>Materials required/recommended for this section</b>	Curriculum and up to three calculators satisfying the conditions set by the Council for this examination
<b>Time allowed for this section</b>	Working time for this section: 10 minutes Reading time before commencing work: 10 minutes Working time for this section: 100 minutes

Name of Student: \_\_\_\_\_ Marking key: \_\_\_\_\_

**Calculator-assumed**  
**Section Two:**

## MATHEMATICS 3CD

### Question/Answer Booklet

### Semester 1 Examination 2012



No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

$$\begin{aligned}
 \text{Total distance} &= \int_0^3 |3t^2 - t - 2| dt \\
 &= 1.5 + 16.5 + 1.5 \\
 &= 19.5 \text{ m}
 \end{aligned}$$
✓

### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator-free	6	6	50	50	
Section Two Calculator-assumed	12	12	100	100	
Total		150		100	

### Instructions to students

- 1 Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer. If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued. i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.
- 2 **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be

- (d) the total distance travelled by the particle in the first three seconds. [2]

$$\therefore v = \frac{6}{t} \text{ m/s}$$

$$\therefore t = \frac{6}{v} \text{ when } v = 0$$

- (c) the minimum velocity of the particle. [2]

$$\begin{aligned} \therefore t &= 1.69 \text{ s} \\ \therefore x &= 0 \text{ when } t^2 - 0.5t - 2 = 0 \\ x(t) &= t^3 - \frac{1}{2}t^2 - 2t \\ x(0) &= 0 \leftarrow k = 0 \end{aligned}$$

$$\therefore x = t^3 - \frac{1}{2}t^2 - 2t + k$$

- (b) when the particle is again at the origin. [2]

$$\begin{aligned} \therefore v(t) &= 3t^2 - t - 2 \\ v(0) &= -2 \leftarrow c = -2 \\ v &= 3t^2 - t + c \end{aligned}$$

- (a) the velocity of the particle at any time  $t$ . [1]

Determine:

Initially the particle is at the origin with a velocity of -2 m/s.

$$a = 6t - 1$$

A particle is moving in rectilinear motion with acceleration  $a$  at any time  $t$ , in  $\text{m s}^{-2}$ , given as  $a = 6t - 1$ .

Question 18

Calculator-assumed marks

marks, valid working or justification is required to receive full marks. If you allocate any marks, for any question or part question worth more than two marks, it is recommended that you **do not use pencil**, except in diagrams.

wish to have marked.

repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

**Section Two: Calculator-assumed  
(100 marks)**

**Question 7  
marks)**

(10

- (a) The radius of a circular oil slick is increasing at a rate of  $0.4 \text{ m s}^{-1}$ . Find the rate at which the area of the oil slick is increasing when the radius is 50 m.

$$\begin{aligned} A &= \pi r^2 \\ \therefore \frac{dA}{dr} &= 2\pi r \quad \checkmark \end{aligned}$$

By the chain rule

$$\begin{aligned} \frac{dA}{dt} &= \frac{dA}{dr} \times \frac{dr}{dt} \quad \checkmark \\ \Rightarrow \frac{dA}{dt} &= 2\pi r \frac{dr}{dt} \end{aligned}$$

When  $r = 50$ ,  $\frac{dr}{dt} = 0.4$ ,  $\frac{dA}{dt} = ?$ 

$$\begin{aligned} \therefore \frac{dA}{dt} &= 2\pi \times 50 \times 0.4 \quad \checkmark \\ &= 40\pi \end{aligned}$$

Thus the rate of increase in the area of the slick is  $40\pi \text{ m}^2/\text{s}$   $\checkmark$   
(4)

- (b) A sink is formed by the rotation of the curve  $y = \frac{x^3}{8}$ , for  $y > 0$ , around the Y axis. If the depth of the sink is 8cm, how many cubic centimetres of water would it hold?

(6)

Specific behaviours
✓ or X

$S = S_0 e^{-0.00001x/20000}$	<b>Solution</b>
$\therefore \sim 82\%$	

(iii) What are the values of  $\frac{dy}{dt}$  at these times?

$$\text{Slowest when } t = 12, \frac{dy}{dt} = 0$$

(ii) When is the fluid in the tank draining fastest and slowest?

$$\frac{dy}{dt}$$

$\frac{dy}{dt} = -\left(1 - \frac{t}{12}\right)$	<b>Specific behaviours</b>
$\frac{dy}{dt}$	<b>Solution</b>

(i) Find the rate  $\frac{dt}{dy}$  m/hour at which the tank is draining at time,  $t$ .

$$\frac{dy}{dt} = 6\left(1 - \frac{t}{12}\right)^2 \text{ metres.}$$

(a) It takes 12 hours to drain a storage tank by opening the valve at the bottom. The depth  $y$  of fluid in the tank,  $t$ , hours after the valve is opened is given by

### Question 8

(7 marks)

$$\therefore \text{A sink can hold } 384\pi \text{ cm}^3 \text{ of water.} \quad \checkmark$$

$$= \frac{5}{3} \pi \int_0^8 (2y)^2 dy \quad \checkmark$$

$$= \pi \int_0^8 x^2 dy \quad \checkmark$$

$$\therefore V = \lim_{y \rightarrow 0} \sum_{y=8}^0 \pi x^2 dy \quad \checkmark$$

If cylinder is rotated around the  $y$  axis, then we have

$$8y = x^3 \quad \checkmark$$

$$\text{When } y = 0, x = 0 \quad \checkmark$$

$$\text{When } y = 8, x = 4 \quad \checkmark$$

$S = S_0 e^{-0.00001x/20000}$	<b>Solution</b>
$S = 0.818750$	$\therefore \sim 82\%$

(as a percentage of our present tooth size)  
 (iii) What will be our descendants tooth size 20 000 years from now? (1)

$t = 10536 \text{ years}$	<b>Specific behaviours</b>
$0.9 = e^{-0.00001t}$	$\checkmark$ solves correctly for $t$

(ii) In how many years will human tooth size be 90% of their present size?

$$0.9 = e^{-0.00001t} \quad \checkmark$$

$S = S_0 e^{-kt}$	<b>Solution</b>
$0.9950 = S_0 e^{-1000k}$	$\checkmark$ solves correctly for $k$

(i) If  $t$  represents time in years and  $S$  represents tooth size, find the value of  $k$ .

In Northern Europeans, for example, tooth size reduction now has a rate of 1% per 1000 years.

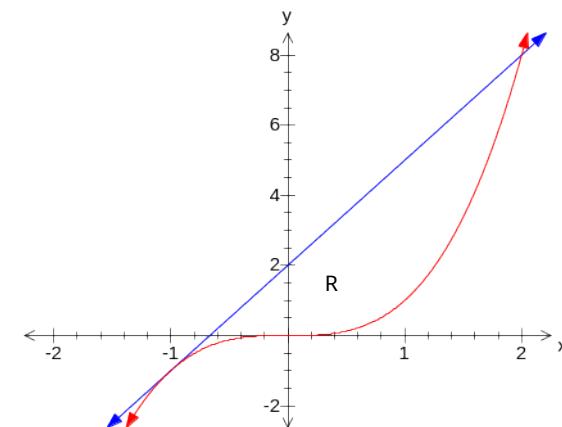
A group of anthropologists found that human tooth size is continuing to decrease, such that

$\frac{dS}{dt} = KS$  of  $K$ .

(b) In Northern Europeans, for example, tooth size reduction now has a rate of 1% per 1000 years.

(b) A group of anthropologists found that human tooth size is continuing to

Fastest when $t = 0$ , $\frac{dy}{dt} = -1$
<b>Specific behaviours</b>
✓ times $\frac{dy}{dt}$
✓ values of $\frac{dy}{dt}$



<b>Solution</b>
Area of region R = $\int_{-1}^0 (3x + 2 - x^3) dx$
$= \left[ \frac{3x^2}{2} + 2x - \frac{x^4}{4} \right]_{-1}^0$
$= \frac{3}{4}$ units <sup>2</sup>
<b>Specific behaviours</b>
✓ correct shading of R
✓ $\int_{-1}^0 (3x + 2 - x^3) dx$
✓ integrates each term correctly
✓ correct answer



**Question 9  
marks)**

(10)

- (a) Give two reasons why the following cannot be a probability distribution.  
(2)

$x$	3	1	2	3	5	0
$P(X=x)$	0.05	0.1	0.4	0.1	0.2	0.3

**Solution**

- Different probabilities for same value of  $x$  i.e.  $P(X=3) = 0.05$  and  $P(X=3) = 0.1$
- Sum of all the probabilities is greater than 1 (1.15)

**Specific behaviours**

✓✓ 1 mark each

- (b) The probability distribution of  $x$  where random variable,  $X$  is the sum of the uppermost numbers when two fair die are rolled is tabulated below.

$x$	2	3	4	5	6	7	8	9	10	11	12
$P(X=x)$	$\frac{1}{36}$	$\frac{2}{36}$	$\frac{3}{36}$	$\frac{4}{36}$	$\frac{5}{36}$	$\frac{6}{36}$	$\frac{5}{36}$	$\frac{4}{36}$	$\frac{3}{36}$	$\frac{2}{36}$	$\frac{1}{36}$

Find

(i)  $P(X > 3)$  (2)

**Solution**

$$\frac{33}{36} = \frac{11}{12}$$

**Specific behaviours**

✓✓

(ii)  $P(X < 10 | X > 3)$  (2)

**Solution**

Range of size of bolts is the same at 118.6 mm to 121.4 mm  
 $\therefore$  in terms of consistency the bolts have the same range.

**Specific behaviours**

✓ valid reason

- (iii) Is the manufacturer better off? Justify. (2)

**Solution**

Yes, as wastage is reduced from 16.15% to 10%. i.e. 6150 more bolts will be accepted

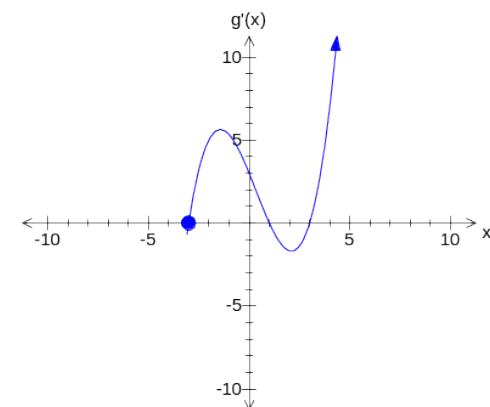
**Specific behaviours**

✓ yes  
 ✓ justification

**Question 16**

(7 marks)

The graph of  $g'(x)$  is given below.



- (a) What can be said about the gradient of the function  $g(x)$  between  $x = -3$  to  $x = 1$ ? (1)

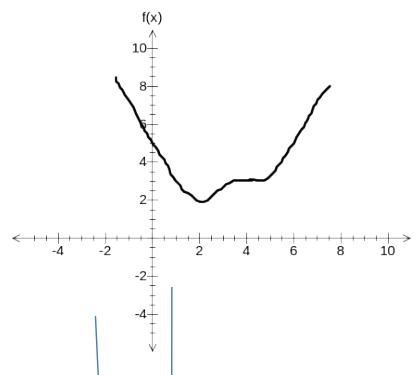
**Solution**

Gradient is positive

**Specific behaviours**

✓ or X

Question 10		Solution	
(a)	The function $f(x)$ is differentiable for all $x \in \mathbb{R}$ and satisfies the conditions $f(x) < 0$ where $x < 2$ $f(x) = 0$ where $x = 2$ $f(x) > 0$ where $x > 2$ $f'(x) > 0$ where $x < 4$ $f'(x) = 0$ where $x = 4$ $f'(x) < 0$ where $x > 4$	(i)	Draw a sketch of this function $f(x)$ .
(b)	$P(a < X < b) = 0.9$ $\bar{x} = 120$ , $\sigma = 0.85$	(ii)	Do the packages now contain bolts that are more consistent in length?
(c)	A new quality controller suggests adjusting the settings on the machines so that standard deviation becomes 0.85mm and that only the shortest 5% and the longest 5% of the bolts are rejected.	(iii)	Find the new minimum and maximum acceptable lengths correct to the nearest 0.1 mm.
(d)	A new quality controller suggests adjusting the settings on the machines so that standard deviation becomes 0.85mm and that only the shortest 5% and the longest 5% of the bolts are rejected.	(iv)	Find the new minimum and maximum acceptable lengths correct to the nearest 0.1 mm.
Question 11		Solution	
(1)	Find the expected number of acceptable bolts in a batch of 100 000	(2)	Is this a reasonable outcome for the company? Justify your answer.
(2)	$0.83847 \times 100000 = 83849$	(3)	Is this a reasonable outcome for the company? Justify your answer.
(3)	$\checkmark$ or $X$	(4)	Independent? Justify your answer.
(4)	$P(3 < X < 10) = \frac{2}{36} = \frac{9}{11} = \frac{1}{12}$		If event A is $X > 3$ and event B is $X < 10$ , are these two events independent? Justify your answer.
Question 12		Solution	
(1)	$0.83847 \times 100000 = 83849$	(2)	$\checkmark$ or $X$
(2)	$\checkmark$ or $X$	(3)	Outcomes not reasonable
(3)	$\checkmark$ or $X$	(4)	% of unacceptable bolts is 16.15% which is too high - too much waste
(4)	$\checkmark$ or $X$	(5)	A new quality controller suggests adjusting the settings on the machines so that standard deviation becomes 0.85mm and that only the shortest 5% and the longest 5% of the bolts are rejected.
Question 13		Solution	
(1)	$\checkmark$ or $X$	(2)	$\checkmark$ or $X$
(2)	$\checkmark$ or $X$	(3)	% of acceptable bolts = 83.85%
(3)	$\checkmark$ or $X$	(4)	% of unacceptable bolts = 16.15% which is too high - too much waste
(4)	$\checkmark$ or $X$	(5)	Outcomes not reasonable
Question 14		Solution	
(1)	$\checkmark$ or $X$	(2)	$\checkmark$ or $X$
(2)	$\checkmark$ or $X$	(3)	Uses inverse NormCDF
(3)	$\checkmark$ or $X$	(4)	Specific behaviours
(4)	$\checkmark$ or $X$	(5)	INV NormCDF( $c, 0.9, 0.85, 120$ ) results in $a = 118.6$ and $b = 121.4$
Question 15		Solution	
(1)	$\checkmark$ or $X$	(2)	$\checkmark$ or $X$
(2)	$\checkmark$ or $X$	(3)	$\checkmark$ or $X$
(3)	$\checkmark$ or $X$	(4)	$\checkmark$ or $X$
(4)	$\checkmark$ or $X$	(5)	$\checkmark$ or $X$



Solution
✓ shape ✓ turns at $x = 2$ ✓ point of inflection at $x = 4$
Specific behaviours
As above

- (ii) State whether the following statement is true or false.  
"The graph  $f(x)$  has a stationary point of inflection where  $x=4$ ". (1)

Solution
True
Specific behaviours
✓ or X

(b) If  $\int_0^a f(x) dx = a$ , find  $2 \int_0^{5a} f\left(\frac{x}{5}\right) + 3 dx$  (3)

Solution
Now if $u = \frac{x}{5}$ , $5u = x$ $\int_0^{5a} f\left(\frac{x}{5}\right) dx = \int_0^a f(u) du = 5a$ $2 \int_0^{5a} f\left(\frac{x}{5}\right) + 3 dx$

- (ii) Using Calculus find the length of each part of the wire when the sum of the areas is a minimum. (5)

Solution
$A = 7x^2 - 8x + 4$ $\frac{dA}{dx} = 14x - 8$ $\frac{d^2 A}{dx^2} = 14 \Rightarrow \text{Min}$ $14x - 8 = 0$ $x = \frac{4}{7}$ $x = 4 \frac{4}{7} \left( \frac{32}{7} \right) \text{ and } 3 \frac{3}{7} \left( \frac{24}{7} \right)$ Lengths of each part of wire are
Specific behaviours
✓ first derivative ✓ second derivative to confirm $x$ value gives a minimum area ✓ $x$ value ✓✓ the two lengths of $\left( \frac{32}{7} \right)$ and $\left( \frac{24}{7} \right)$

### Question 15 (11 marks)

Nuts and Bolts Company manufactures 120mm bolts which are normally distributed with a mean length of 120mm and a standard deviation of 1mm. Only bolts which are between 118.6mm and 121.4mm pass inspection and are packaged as 120mm bolts.

- (a) Find the probability of a randomly selected bolt being an acceptable length. (2)

Solution
$P(118.6 \leq X \leq 121.4) = NCDF(118.6, 121.4, 1, 120) = 0.838487$
Specific behaviours
✓✓

Question 13 (continued)	<p>(d) Adams' little brother, Brodie joins in this business venture. The probability that Brodie's painted gnomes is Regular is 0.8. He wants to ensure that the probability that he paints at least two Superior is at least 0.9. Calculate the minimum number of gnomes that Brodie would need to paint to achieve this aim.</p> <p><math>P(R) = 0.8, PS = 0.2</math></p>
<p><b>Specific behaviours</b></p> $\begin{aligned} &= 2 \int_a^0 f(x) dx + 2 \int_a^0 3 dx \\ &= 2 \int_a^0 f\left(\frac{5}{x}\right) dx + 2 \int_a^0 3 dx \\ &\quad \checkmark \text{integrates correctly} \end{aligned}$	<p><b>Solution</b></p> $\begin{aligned} & \text{Brodie's painted gnomes is Regular is } 0.8. \text{ He wants to ensure that the probability that he paints at least two Superior is at least } 0.9. \text{ Calculate the minimum number of gnomes that Brodie would need to paint to achieve this aim.} \\ & P(X \geq 2) \geq 0.9 \\ & 1 - P(X \leq 1) \geq 0.9 \\ & P(X \leq 1) \leq 0.1 \\ & \text{Using CAS to solve, } n = 17.95 \\ & \therefore \text{minimum number is 18} \end{aligned}$

(4)

- (i) A piece of wire 8cm long is cut into two unequal parts. One part is used to form a rectangle that has a length three times its width. The other part of the wire is used to form a square. If the width of the rectangle is  $x$  units, determine an equation that will give the sum of the areas of the rectangle and the square in terms of  $x$ .

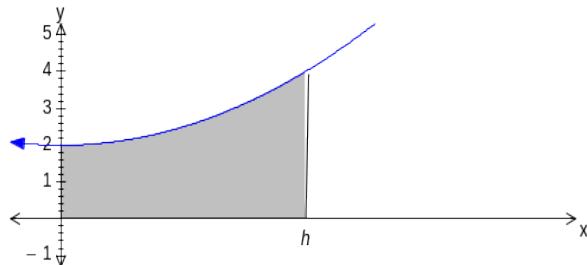
(9 marks)

<b>Specific behaviours</b>
<p><b>Solution</b></p> $\begin{aligned} \text{Area, } A &= 3x^2 + (2 - 2x)^2 \\ &= 7x^2 - 8x + 4 \end{aligned}$

<b>Specific behaviours</b>
<p>(3)</p> <p>gnomes that Brodie would need to paint to achieve this aim.</p> <p>any one of</p> <p>(d) Adams' little brother, Brodie joins in this business venture. The probability that Brodie's painted gnomes is Regular is 0.8. He wants to ensure that the probability that he paints at least two Superior is at least 0.9. Calculate the minimum number of gnomes that Brodie would need to paint to achieve this aim.</p> <p><math>P(R) = 0.8, PS = 0.2</math></p> <p><b>Specific behaviours</b></p> $\begin{aligned} & \text{Brodie's painted gnomes is Regular is } 0.8. \text{ He wants to ensure that the probability that he paints at least two Superior is at least } 0.9. \text{ Calculate the minimum number of gnomes that Brodie would need to paint to achieve this aim.} \\ & P(X \geq 2) \geq 0.9 \\ & 1 - P(X \leq 1) \geq 0.9 \\ & P(X \leq 1) \leq 0.1 \\ & \text{Using CAS to solve, } n = 17.95 \\ & \therefore \text{minimum number is 18} \end{aligned}$

**Question 11****(7 marks)**

A section of the function  $y = 0.5x^2 + 2$  is graphed below, along with a shaded region enclosed by the function, the axes and the line  $x = h$ .



- (a) Show that the volume of the solid generated when the shaded region

$$\text{is rotated about the } x\text{-axis is given by } V = \pi \left[ 0.05h^5 + \frac{2}{3}h^3 + 4h \right].$$

(2)

$$\begin{aligned} V &= \pi \int_0^h (0.5x^2 + 2)^2 dx \\ &= \pi \int_0^h \frac{\pi}{4}x^4 + 2x^2 + 4 dx \\ &= \pi \left[ \frac{x^5}{20} + \frac{2x^3}{3} + 4x \right]_0^h \\ &= \pi \left[ 0.05h^5 + \frac{2}{3}h^3 + 4h \right] \end{aligned}$$

- (b) If  $h$  increases at the rate of 0.5 units per second, find an expression, in terms of  $h$ , for the *rate of change* of the volume of the solid generated when the shaded region is rotated about the  $x$ -axis.

(2)

Find the expected number of these gnomes that will be Superior. (2)

<b>Solution</b>
Expected number = $0 \times 0.09 + 1 \times 0.28 + 2 \times 0.63 = 1.54$
<b>Specific behaviours</b>
✓ calculation
✓ correct answer of 1.54

- (iii) A random sample of ten fruit balls is taken from the box.

<b>Solution</b>	
<b>Specific behaviors</b>	
0.08808	✓ or X
0.9X0.9X0.9 = 0.729	0.9X0.9X0.9 = 0.729

$$(i) \text{ Calculate } C_{10}^4 (0.2)^4 (0.8)^6$$

cent of the fruit balls in the box are coated with dark chocolate. A large number of these fruit balls are placed in a box. Twenty per cent of the fruit balls in the box are coated with dark chocolate.

- (a) A company produces fruit balls coated in either dark chocolate or milk chocolate. A large number of these fruit balls are coated in a box. Twenty per

(9 marks)

### Question 12

$$\text{When } h = 3, dh = 0.01; \Rightarrow dh = 1.327$$

$$= \pi(0.25h^4 + 2h^2 + 4) \Rightarrow dh$$

$$dh = \frac{dV}{dh}$$

(3)

to estimate the change in volume when  $h$  increases from 3 to 3.01.

$$(c) \text{ Use the incremental formula, } \frac{dV}{dh} \approx \frac{dh}{dh}$$

is Regular.

(a) If the first garden gnome inspected is Superior, find the probability that the

third garden gnome is Superior.

If the garden gnome is Superior, the probability that the next garden gnome is

Superior is 0.9. If the garden gnome is Regular, then the probability that the next

garden gnome is Superior is 0.7.

If the garden gnome is Superior, then the probability that the next garden gnome is

Superior, depending on the quality of their finish.

Adam paints garden gnomes to sell. He sends the garden gnomes to his father (a

quality controller) in the order of completion, who classifies them as either

Superior or Regular, depending on the quality of their finish.

Calculusator-Assumed

MATHEMATICS 3CD

CALCULATOR-ASSUMED

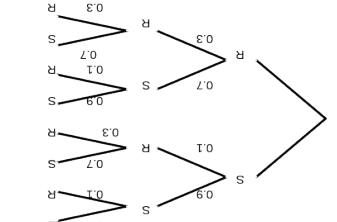
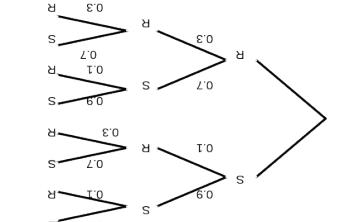
$$\begin{aligned} P(\text{no Superior}) &= 0.09 \\ P(1 \text{ Superior}) &= 0.28 \\ P(2 \text{ Superior}) &= 0.28 \\ P(3 \text{ Superior}) &= 0.63 \end{aligned}$$

found that these three gnomes,

- (c) A group of 3 consecutive garden gnomes is inspected and the first is a Regular. It is also

<b>Solution</b>	
<b>Specific behaviors</b>	
0.9X0.9X0.9 = 0.729	✓ or X
0.9X0.9X0.9 = 0.729	0.9X0.9X0.9 = 0.729

- (b) If the first garden gnome inspected is Superior, find the probability that the next three gnomes are Superior.

<b>Solution</b>	
<b>Specific behaviors</b>	
$P(\text{SSR}) + P(\text{SRR}) = (0.9)(0.1) + (0.1)(0.3) = 0.12$	$P(\text{SSR}) + P(\text{SRR}) = (0.9)(0.1) + (0.1)(0.3) = 0.12$
	

- (a) If the first garden gnome inspected is Superior, find the probability that the

second garden gnome is Superior.

If the garden gnome is Superior, the probability that the next garden gnome is

Superior is 0.9. If the garden gnome is Regular, then the probability that the next

garden gnome is Superior is 0.7.

If the garden gnome is Superior, the probability that the next garden gnome is

Superior, depending on the quality of their finish.

Adam paints garden gnomes to sell. He sends the garden gnomes to his father (a

quality controller) in the order of completion, who classifies them as either

Superior or Regular, depending on the quality of their finish.

Calculusator-Assumed

MATHEMATICS 3CD

CALCULATOR-ASSUMED

Explain the meaning of  $C_4^{10}(0.2)^4(0.8)^6$  with respect to this sample.

(2)

<b>Solution</b>	
In a sample of 10 fruit balls, the probability of picking exactly 4 coated in dark chocolate is approximately 0.0881	
<b>Specific behaviours</b>	
✓✓	

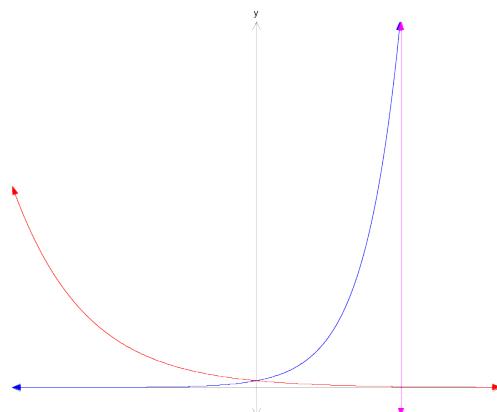
- (b) (i) Find  $n$  given that  $C_0^n(0.2)^0(0.8)^n = 0.167\ 772\ 16$  (1)

<b>Solution</b>	
Using CAS, $n = 8$	
<b>Specific behaviours</b>	
✓	

- (ii) Explain the meaning of your answer to part (b)(i) with respect to the fruit balls. (2)

<b>Solution</b>	
The probability of picking no dark chocolate fruit ball from 8 is 0.16777216	
<b>Specific behaviours</b>	
✓ picking none	
✓ from 8	

- (c) The curve  $y = e^{2x}$  and  $y = e^{-x}$  intersect at the point  $(0, 1)$  as shown in the diagram.



Find the area enclosed by the curves and the line  $x=2$ . Leave your answer in terms of ' $e$ '. (3)

<b>Solution</b>	
$\text{Required area} = \int_0^2 e^{2x} dx - \int_0^2 e^{-x} dx$ $= \left[ \frac{e^{2x}}{2} - (-e^{-x}) \right]_0^2$ $= \frac{e^4}{2} + e^{-2} - \frac{3}{2}$	
<b>Specific behaviours</b>	
$\checkmark \int_0^2 e^{2x} dx - \int_0^2 e^{-x} dx$ $\checkmark$ integrates each term correctly $\checkmark$ substitutes limits of integration to get exact value of $\frac{e^4}{2} + e^{-2} - \frac{3}{2}$	