SHENTON COLLEGE

ATMAM Mathematics Methods

Test 2 (2019) Calculator Assumed

Name: .....

Teacher: Friday Smith Ai

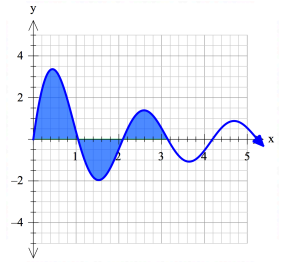
Time Allowed : 25 minutes

Marks /22

Materials allowed: Classpad, Formula Sheet.

Attempt all questions. Questions 5 to 9 are in this section.
All necessary working and reasoning must be shown for full marks.
Where appropriate, answers should be given to two decimal places.
Marks may not be awarded for untidy or poorly arranged work.

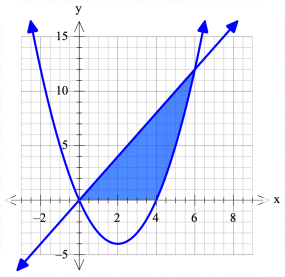
5 a) Below is a graph of the function $y = \frac{5\sin(3x)}{x+1}$, $x \geq 0$. Without using absolute values, write an expression to calculate the area shown below. (2)



b) Calculate $\int_0^{\pi} \frac{5\sin(3x)}{x+1}\,dx$ on your Classpad and explain why it gives a different result to your expression in part a). (2)

6 For each of the following diagrams, circle the integral that would give the indicated area. If neither integral would give the correct area, cross out all integrals and write "neither". (4)

a)

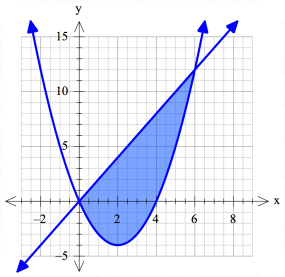


$\int_0^6 2x\,dx - \int_0^6 x(x-4)\,dx$

$\int_0^6 2x\,dx - \int_4^6 x(x-4)\,dx$

$\int_0^6 2x\,dx - \int_0^4 x(x-4)\,dx$

b)

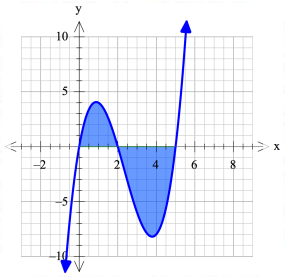


$\int_0^6 2x\,dx + \int_6^0 x(x-4)\,dx$

$\int_0^6 2x\,dx - \int_4^6 x(x-4)\,dx$

$\int_0^6 2x\,dx + \int_0^4 x(x-4)\,dx$

c)

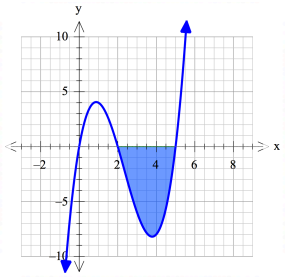


$\int_0^5 x^3 - 7x^2 + 10x\,dx$

$\int_0^2 x^3 - 7x^2 + 10x\,dx + \int_2^5 x^3 - 7x^2 + 10x\,dx$

$\int_0^2 x^3 - 7x^2 + 10x\,dx + \int_5^2 x^3 - 7x^2 + 10x\,dx$

d)



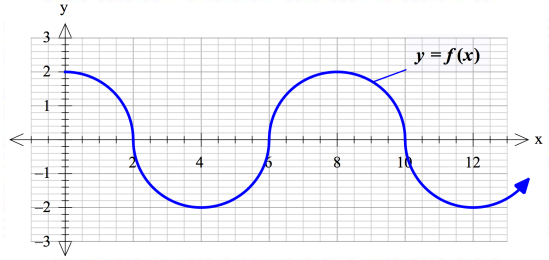
$\int_2^5 x^3 - 7x^2 + 10x\,dx$

$\int_2^5 -x^3 + 7x^2 - 10x\,dx$

$-\int_0^5 x^3 - 7x^2 + 10x\,dx$

7 Using appropriate algebra and calculus techniques, show how you would calculate the area trapped between the curves given by $f(x) = x(x-5)^2$ and $g(x) = 8x - 12$. (4)

8 The graph below is made from sections of a circle with radius 2 units.



a) Determine $\int_0^4 f(x)dx$ (1)

b) The function A(p) is defined as $A(p) = \int_0^p f(x)dx$.
For the questions below, we will only consider the values $0 \leq p \leq 12$.

(i) Determine the value(s) for p such that A(p) < 0. (1)

(ii) Determine the value(s) for p such that A(p) is at its maximum. (1)

(iii) Determine the value(s) of p, $p > 0$, where the value of A(p) is increasing at its fastest rate. (1)

c) Evaluate $\int_2^{10} |f(x)|dx$ (1)

9 The curve $y = 9 - x^2$ is shown on the diagram below. A line is drawn from the origin to a point on the curve such that the area trapped between the line, the curve and the y-axis is the same as the area trapped between the curve, the line and the positive x-axis. Determine the equation of the line needed to achieve the equal areas. (5)

[HINT: Divide the half on the right into a triangle and a curved section]