

SOITAMEHTAM

BS/AS

Calculator-assumed

WACE Examination 2010

Final Marking Key

This 'stand alone' version of the WACE Examination 2010 Final Marking Key is provided on an interim basis.

The Standards Guide for this examination will include the examination questions, marking key, question statistics and annotated candidate responses. When the Standards Guide is published, this document will be removed from the website.

| MATHEMATICS 2A/2B | 2 | MARKING KEY |
|--------------------|---|-------------|
| CALCULATOR-ASSUMED | | |

Question 7 (8 marks)

Brian designs a three-character password made from the characters A, B, # and 1, without using a character more than once in the password. There are 24 different possible passwords which are listed below.

| A B # | B A # | # A B | 1 A B |
|-------|-------|-------|-------|
| A B 1 | B A 1 | # A 1 | 1 A # |
| A # B | B#A | # B A | 1 B A |
| A#1 | B#1 | # B 1 | 1B# |
| A 1 B | B 1 A | # 1 A | 1#A |
| A 1# | B1# | #1B | 1#B |

(a) Brian states that the probability that his password will end in the # character is 0.4. Is Brian correct? Justify your answer. (2 marks)

| Solution |
|---|
| $P(\text{ends \#}) = \frac{6}{24} = 0.25$ |
| $0.25 \neq 0.4$ |
| Therefore Brian is incorrect |
| Specific Behaviours |
| ✓ correctly calculates P(ends #) |
| ✓ makes conclusion based on values |

- (b) Using the list above, determine the probability that Brian's password
 - (i) contains the # character. (1 mark)

| Solution | |
|--------------------------------------|--|
| $\frac{18}{24}$ | |
| $\overline{24}$ | |
| Specific Behaviours | |
| ✓ correctly calculates P(contains #) | |

(ii) ends in the letter A. (1 mark)

| | Solution |
|----------------------------------|---------------------|
| 6 | |
| $\overline{24}$ | |
| | Specific Behaviours |
| √ correctly calculates P(ends A) | |

(iii) starts with the number 1 **or** ends with the # character. (1 mark)

| Solution |
|--|
| 10 |
| $\frac{10}{24}$ |
| Specific Behaviours |
| ✓ correctly calculates P(start 1 or end #) |

MATHEMATICS 2A/2B 23 MARKING KEY CALCULATOR-ASSUMED

(2 marks)

Question 19 (5 marks)

Consider the first four rows given below.

) Extend the pattern below for rows 5 and 6.

| | | | Solution | | |
|---|-------------------|----|--------------|-------|--|
| | Question | | Result | | |
| | $1 \times 2 + 11$ | = | 13 | row 1 | |
| | $2 \times 3 + 11$ | = | 17 | row 2 | |
| | $3 \times 4 + 11$ | = | 23 | row 3 | |
| | $4 \times 5 + 11$ | = | 31 | row 4 | |
| | $5\times6+11$ | = | 41 | row 5 | |
| | 6×7+11 | = | 53 | row 6 | |
| | | | | | |
| | | Sp | ecific Behav | iours | |
| ✓ correctly comp✓ correctly comp | | | | | |

(b) Determine the result for row 25. (1 mark)

| Solution |
|--|
| $25 \times 26 + 11 = 661$ |
| Specific Behaviours |
| ✓ correctly calculates the result for row 25 |

(c) Con looked at the above results and conjectured that every result is a prime number (a number with only two factors, 1 and itself). Test three further cases and comment on whether they support or refute his conjecture. (2 marks)

| Solution |
|---|
| 10×11+11=121 (one possible answer) |
| 121=11×11 |
| therefore 121 is not prime |
| Specific Behaviours |
| ✓uses patterns correctly to test further cases |
| √comments on conjecture – conjecture is refuted because counter example is found or |
| conjecture is supported by the three test cases |

MATHEMATICS 2A/2B CALCULATOR-ASSUMED

(c) Ava decides to make her own three-character password from the characters %, V and 5, without using a character more than once in the password.

3

) List all of the possible passwords Ava could make. (2 marks)

| | | | | | √ lists at least 4 po √ lists every possib |
|--------|---------|-----------|-------------|---------|---|
| | | ehaviours | Specific Bo | | |
| ۷ '% ۲ | % 'A 'S | % '9 'Λ | ς '% 'Λ | Λ '9 '% | '9 'Λ '% |
| | | noii | njog | | |

(ii) Brian tries to guess Ava's password. What is the probability that Brian guesses Ava's password correctly with only one guess? (1 mark

| | correctly calculates probability |
|---------------------|--|
| Specific Behaviours | |
| | 9 |
| | Ī |
| Solution | |

WARKING KEY

MATHEMATICS 2A/2B CALCULATOR-ASSUMED

It has already been determined that a bridge from A to D would be 1250 metres long, while a bridge from B to E would be 1120 metres long. Given that 1 unit is 100 metres, decide which bridge should be built and how long (to the nearest 10 metres) it would be Justify your answer.

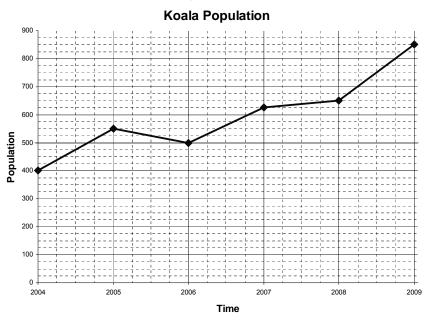
22

| rounds BD correctly to the nearest 10 metres |
|--|
| ✓ states BD is the shortest bridge |
| ✓ correctly determines other lengths |
| ✓ correctly determines one length |
| Specific Behaviours |
| _ |
| BD is shortest with a length of 630 m |
| |
| $BD = \sqrt{6^2 + 2^2} = 6.32$ |
| · · · · · · · · · · · · · · · · · · · |
| $BC = \sqrt{4^2 + 7^2} = 8.06$ |
| $VC = \sqrt{9^2 + 1^2} = 9.06$ |
| $AE = \sqrt{7^2 + 3^2} = 7.62$ |
| |
| UOINIOC |

MATHEMATICS 2A/2B 4 MARKING KEY CALCULATOR-ASSUMED

Question 8 (7 marks)

(a) The population of koalas in a national park is recorded at the start of every year. The data collected from 2004–2009 are plotted below.



(i) Describe the trend in the population of koalas against time. (1 mark)

| Solution | | |
|------------------------------|---------------------|---|
| increasing | | |
| | Specific Behaviours | - |
| √ correctly identifies trend | | - |

(ii) What assumption has been made by the joining of the points in the graph above? (1 mark)

| Solution | |
|---|--|
| The population steadily increases or decreases (at the same rate during each year) | |
| Specific Behaviours | |
| √ identifies a constant rate of change, or increasing (at the same rate) uniformly. | |

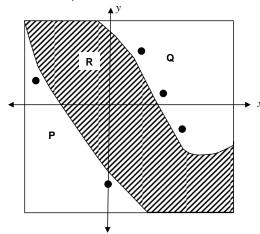
(iii) Estimate the population half-way through the year 2005. (1 mark)

| Solution | |
|---|--|
| 525 | |
| Specific Behaviours | |
| ✓ correctly reads value from graph between calibrations | |

MATHEMATICS 2A/2B 21 MARKING KEY CALCULATOR-ASSUMED

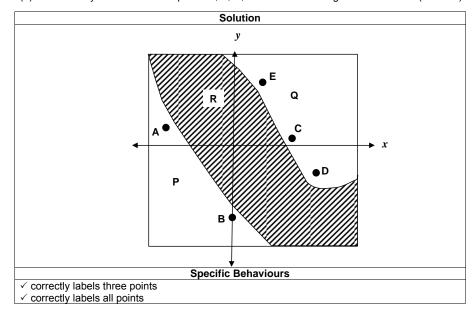
Question 18 (6 marks)

A bridge is to be built to connect land P and land Q, which are separated by river R as shown in the diagram below (not drawn to scale).



The government wants to minimise the cost of building the bridge, so it is in favour of building the shortest bridge possible. Five points have been chosen: A(-5, 2), B(0, -6), C(4, 1), D(6, -4) and E(2, 5).

(a) Correctly label each of the points A, B, C, D and E on the diagram above. (2 marks)



MATHEMATICS 2A/2B

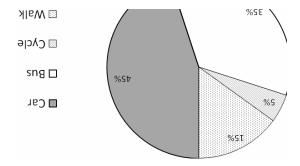
CALCULATOR-ASSUMED

month and year, e.g. October 2005. Approximately when did the population first exceed 700? Give your answer as a

| | √ correctly gives month and year |
|---------------------|----------------------------------|
| Specific Behaviours | |
| | April 2008 (accept March 2008) |
| Solution | |

9

part-time jobs one Saturday. They drew a pie chart to show the results. Annie and Jimmy surveyed a group of teenagers to find out how they travelled to their



Syevrus ymmiL bns einnA bib (2 marks) If 14 teenagers caught buses to their jobs on the Saturday, how many teenagers

| ✓ correctly determines the number of teenagers |
|--|
| $^{\prime}$ writes an equation to solve that will give the correct value of N $_{ m Or}$ |
| Specific Behaviours |
| 0 t = V |
| $t I = N \times \frac{00I}{CC}$ |
| $V_1 = V \times \frac{1}{\delta \varepsilon}$ |
| uoinios |

(1 mark) probability that they walked or cycled to their job on the Saturday? (ii) A teenager is selected at random from the group surveyed. What is the

| | correctly calculates probability |
|---------------------|--|
| Specific Behaviours | |
| | 20% or 0.0 ac |
| Pointion | |

MARKING KEY 50 CALCULATOR-ASSUMED MATHEMATICS 2A/2B

(e marks) Auestion 17

buys four non-fiction and ten fiction books and receives \$4 change. price. Breanna buys eight non-fiction and five fiction books and is given \$1 change. Stephanie non-fiction books are sold at one fixed price and all fiction books are sold at a different fixed Sisters Breanna and Stephanie are each given \$40 to spend at the second-hand book fair. All

(S marks) linear equations from the above information. Let n be the price of a non-fiction book and f the price of a fiction book. Write two

| correctly expresses items bought by Breanna and Stephanie | | |
|---|--|--|
| correctly determines total amounts, i.e. \$39 and \$36 | | |
| Specific Behaviours | | |
| $\partial \mathcal{E} = \mathcal{V} 0 1 + n 4$:einshqəft | | |
| $6\mathcal{E}=\mathcal{F}\mathcal{E}+n$ 8 :sanna: | | |
| uonnios | | |

(2 marks) dollars and cents. Determine algebraically the cost of buying a non-fiction book. Give your answer in

| | \checkmark gives correct price in dollars and cents (not $n=3.5$) |
|--|--|
| v simplifies equations to one variable | |
| Specific Behaviours | |
| | non-fiction books cost \$3.50 |
| | $\varsigma \cdot \varepsilon = u$ |
| | $\Delta L = n\Delta I.9.i$ |
| | $9\xi + \int 0 \mathbf{I} + n \mathbf{L}$ |
| | $87 = \int 01 + n\delta 1$ |
| noiżuloS | |

non-fiction books. Does she have enough money? Justify your answer. Their little sister Alicia is only given \$20 to spend. She wants to buy five fiction and two

| ✓ states Alicia has enough money | |
|---|--|
| correctly calculates money Alicia needs | |
| Specific Behaviours | |
| Alicia has enough money by \$2 | |
| 81\$= | |
| Alicia spenda sioil A | |
| | |
| $Z.Z = \mathcal{F}$ | |
| $\varsigma \cdot \varepsilon = u$ | |
| noituloS | |

MATHEMATICS 2A/2B CALCULATOR-ASSUMED 6 **MARKING KEY**

Question 9 (5 marks)

Consider the sequence of numbers below.

24. 60. 150. 375. ...

State a recursive rule in words for this sequence.

(1 mark)

Solution

The next term is two and half (2.5) times the previous term

Specific Behaviours

✓ states the link between consecutive terms

Write a recursive rule for this sequence using algebraic notation. (2 marks)

Solution

$$\frac{60}{24} = \frac{150}{60} = 2.5$$

$$\frac{}{24} = \frac{}{60} = 2$$

$$T_{n+1} = 2.5 \times T_n$$

$$T_1 = 24$$

Specific Behaviours

√ correctly writes the recursive equation

√ states the value of the first term

The sequence of numbers: 12, 67, 342, 1717 ... can be defined recursively as:

$$T_{n+1} = 5T_n + k$$
, $T_1 = 12$

Determine the value of k.

(1 mark)

Solution

$$T_2 = 5 \times T_1 + k$$

$$67 = 5(12) + k$$

$$k = 7$$

Specific Behaviours

√ correctly calculates value of k

Determine the value of n when this sequence first exceeds one million.

(1 mark)

Solution

n = 8

Specific Behaviours

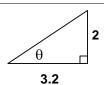
 \checkmark correctly determines the value of n based on (i)

MATHEMATICS 2A/2B CALCULATOR-ASSUMED **MARKING KEY**

Use trigonometry to determine the angle a short wire makes with the ground, to the nearest degree. (2 marks)

19





$$\tan(\theta) = \frac{2}{3.2}$$

$$\theta$$
 = 32.01°

$$\theta = 32^{\circ}$$

Specific Behaviours

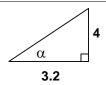
√ uses tangent ratio correctly

√ correctly calculates angle size

Determine the angle between a short wire and a long wire, to the nearest degree.

(2 marks)





$$\tan(\alpha) = \frac{4}{3.2}$$

$$\alpha = 51.3^{\circ}$$

$$\alpha = 51^{\circ}$$

Angle between long and short wires = 51-32

Specific Behaviours

√ calculates size of angle alpha

√ correctly calculates angle size to nearest degree

CALCULATOR-ASSUMED MATHEMATICS 2A/2B

Ot noitsau

nappies costs \$52.49.

(e marks)

When Granny cooks some rice, she adds 4 cups of water to 3 cups of rice.

mixed numeral, e.g. $6\frac{1}{2}$ cups. How many cups of water does she need for 5 cups of rice? Give your answer as a

| expressing the answer as a mixed numeral | √ solves for the unknown to the contract of the contract |
|--|--|
| | √ writes the correct ratios |
| Specific Behaviours | |
| | $\frac{\varepsilon}{\overline{c}}9 = x$ |
| | $\frac{\mathcal{E}}{\mathcal{G}} = \frac{\mathcal{V}}{\mathcal{X}}$ |
| | ç∶x |
| | €:† |
| Solution | |

A pack of 64 Ymiracle nappies costs \$21.95. A bulk package of Peonies containing 144

(2 marks) Which brand is the better buy? Justify your answer.

| correctly states the cheaper brand based on comparison | |
|--|--|
| √ calculates unit prices for both brands | |
| Specific Behaviours | |
| Ymiracle is cheaper | |
| Peonies $52.49 \div 144 = 0.36$ (2 decimal places) | |
| Ymiracle 21.95 \div 64 = 0.34 (2 decimal places) | |
| Homnice | |

price of all clothes sold. Margaret runs a boutique. She makes a profit of between 10% and 40% on the cost

lowest and highest price Margaret could have paid for the dress. Margaret sells a dress for \$280 with the profit in her desired range. Determine the

| | r price | V calculates the uppe |
|---------------|------------------------------|--|
| | √ calculates the lower price | |
| ic Behaviours | Specif | |
| | 32.432\$ bns 002\$ r | Dress bought between |
| | 002 = v | $\mathcal{SS}.4\mathcal{SL} = \mathcal{X}$ |
| | $082 = 4.1 \times \chi$ | $085 = 1.1 \times x$ |
| oojnjos | | |

MARKING KEY

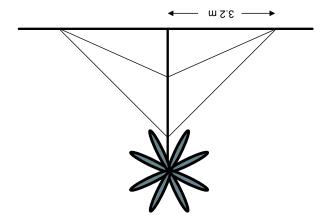
(S marks)

CALCULATOR-ASSUMED MATHEMATICS 2A/2B

(e marks) Question 16

18

the trunk of the tree. tree. The other ends are attached to points that are either one-third or two-thirds of the way up wires. All of these wires have one end attached to the ground 3.2 metres from the base of the Australia. The tree must stand vertically on horizontal ground, so it is supported by a number of A salm tree has been moved from a plant nursery to a private garden in the north of Western



After planting, the trunk height of the palm is 6 metres.

Determine the length of one of the short wires, to the nearest 10 cm.



√ correctly rounds to the nearest 10 cm √ calculates length MATHEMATICS 2A/2B CALCULATOR-ASSUMED

MARKING KEY

Question 11 (6 marks)

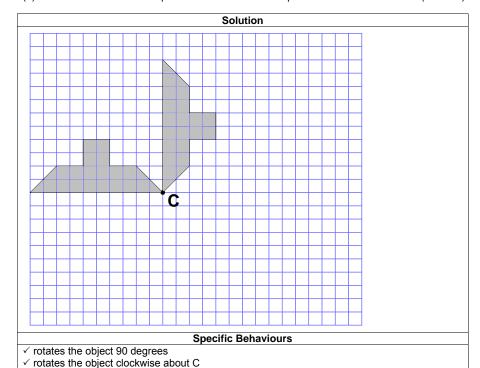
8

Consider the shaded shape drawn below.



(a) Rotate the shaded shape 90° clockwise about the point C.

(2 marks)

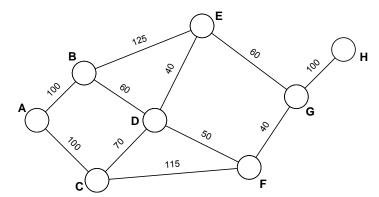


MATHEMATICS 2A/2B 17
CALCULATOR-ASSUMED

Question 15 (5 marks)

MARKING KEY

The network below shows the distances (metres) and connections between a series of classroom blocks, A to H, at a local high school.



(a) Is the network of classroom blocks traversable? Explain why/why not. (1 mark)

| Solution | | |
|--|--|--|
| No because it has 6 odd vertices. To be traversable it needs 0 or 2 odd vertices | | |
| Specific Behaviours | | |
| ✓ refers to the number of odd vertices as a reason why it is not traversable | | |

(b) Determine the shortest way to travel from Block A to Block H and state this shortest distance. (2 marks)

| Solution |
|---------------------------|
| ABDFGH, 350 metres |
| Specific Behaviours |
| ✓ states correct path |
| ✓ states correct distance |

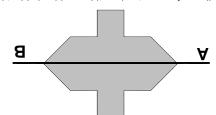
(c) Explain how, if at all, the shortest path from Block A to Block H is affected if you must travel via Block C. (2 marks)

| | Solution | | |
|-----|--|--|--|
| The | e shortest distance is now 355 metres, path is ACFGH | | |
| Inc | Increased distances by 5 metres | | |
| | Specific Behaviours | | |
| √ ι | uses change to determine the shortest path | | |
| √ C | describes effect of change | | |

CALCULATOR-ASSUMED MATHEMATICS 2A/2B

original shape and image as one combined object. The diagram below shows the original shape reflected about the line AB. Consider the

6



How many lines of symmetry does this combined object have? (1 mark)

| (1 mark) | (ii) What is the order of rotational symmetry for this combined object? |
|----------|---|
| | √ correctly states the number of lines of symmetry |
| | Specific Behaviours |
| | 7 |
| | Solution |

Solution

Specific Behaviours

correctly states the order of rotational symmetry 7

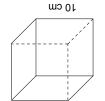
MARKING KEY

CALCULATOR-ASSUMED MATHEMATICS 2A/2B

(4 marks) 41 noitesup

9١

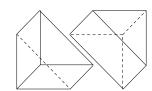
Consider the solid cube shown below.



(1 mark) Determine the total surface area of this cube.

| correctly calculates the surface area | | | |
|---------------------------------------|--|--|--|
| Specific Behaviours | | | |
| $= 600 \mathrm{cm}^2$ | | | |
| $^{\circ}01\times 0=A$ | | | |
| Solution | | | |

This solid cube is to be cut into two equal pieces, as shown in the diagram below.



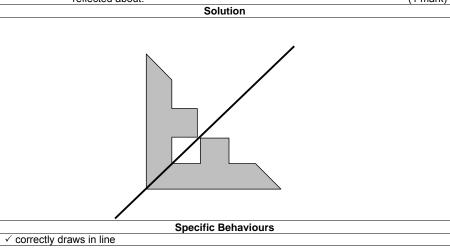
(3 marks) surface area of the cube obtained in (a)? Show working to justify your answer. What difference in total surface area does this cut make when compared to the total (q)

| | determines length of cut side | | |
|--|--|--|--|
| scific Behaviours | edS | | |
| | AR increases by 282.8 cm | | |
| 2 m = 282.8 cm ² | $= 882.8 \mathrm{cm}^2$ | | |
| $01 \times 14 \cdot 14 \times 10$ | · · | | |
| $Diff = 2 \times 10 \times \sqrt{10^2 + 10^2}$ | $SA = 6 \times 10^2 + 2 \times 10 \times \sqrt{10^2 + 10^2}$ | | |
| Solution | | | |

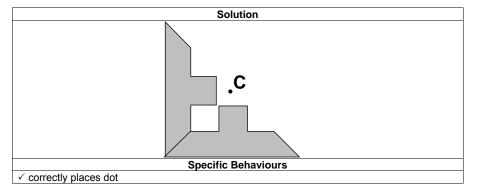
√ correctly determines the difference the cut makes to the SA. ✓ correctly determines the area of the new rectangular face

MATHEMATICS 2A/2B 10 MARKING KEY CALCULATOR-ASSUMED

- (c) A new combined object (shown below) could be produced either by a reflection or a rotation of the original shape.
 - If the transformation was a reflection, draw in the line that the original shape was reflected about. (1 mark)



(ii) If the transformation was a rotation, mark the point C where the original object was rotated about. (1 mark)



MATHEMATICS 2A/2B 15 MARKING KEY CALCULATOR-ASSUMED

√ expresses this number as a percentage

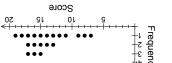
CALCULATOR-ASSUMED MATHEMATICS 2A/2B

(10 marks) Question 12

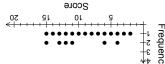
11

each test is displayed in the dot frequency graphs below. beginning of the topic and a post-test (out of 20) at the end. The score for each student on improved their understanding of chance. She gave the students a pre-test (out of 20) at the Moya the mathematics teacher wanted to check whether the students in her class had

| ncy | |
|-----|--|
| | |



Post-test



Jeet-est

improved from the pre-test'. Why is this statement false? The teacher commented: 'Looking at the dot frequency graphs, it is clear that everyone

Specific Behaviours may have scored 10 in the pre-test but 8 in the post-test. From the dot plots we do not know which student scored what result. For example, a student

 \checkmark identifies that we do not have individuals scores for both tests

remaining summary statistics. (3 marks) Some summary statistics have been provided. Complete the table by calculating the

Solution

| 3.6 | 6 | Pre-test |
|--------|------|-----------|
| Median | Mean | Statistic |

| Specific Behaviours | | | | | |
|---------------------|-------|--------|-------------------|-----------|--|
| | 12 | 91 | l ⁻ †l | Post-test | |
| | 13 | 3.6 | 6 | Pre-test | |
| | Range | Median | Mean | Statistic | |

✓ correctly states mean for the pre-test

√ correctly states range for the post-test √ correctly states median for the pre-test

the class as a whole improved from the pre-test to the post-test? (2 marks) Compare the two data sets, commenting on the distribution of the graphed data. Has

Solution

Pre-test data set was more uniformly distributed whereas post-test is more symmetrical (though

As a class the results have improved as the mean and median have both increased by about 5.

Specific Behaviours

√ justifies an improvement by looking at mean and/or median (not just range) compares the shape of the dot plots

> CALCULATOR-ASSUMED **MARKING KEY** MATHEMATICS 2A/2B カレ

> (6 marks) Question 13

three weeks measured their height. The results are displayed in the frequency table below. At the start of spring, Jennifer planted 120 tulip bulbs. She watered them regularly and after

| Frequency | Height of tulip, h (cm) |
|-----------|-------------------------|
| 2 | 9 > 4 ≥ 0 |
| 0 | 01 > 4 5 g |
| 0 | 9l>4≥0l |
| 0 | 12 ≤ h < 20 |
| 12 | SO ≤ P < 25 |
| 72 | S5 ≤ h < 30 |
| 34 | 30 ≥ 4 ≥ 35 |
| 12 | 32 < P < 40 |
| 12 | St>4≥0t |
| 9 | 09 > Y ≥ 97 |
| L | 99 > 4 ≥ 09 |

(2 marks) Determine the mean height of the tulips, correct to one decimal place.

| ctly rounds to one decimal place | √ corre |
|----------------------------------|---------|
| lates mean | ✓ calcu |
| Specific Behaviours | - |
| = 33.5 cm | ะ นธอเม |
| Solution | |

(1 mark) Determine the class interval which contains the median.

| | √ determines correct interval |
|---------------------|---|
| Specific Behaviours | |
| | $\varsigma \varepsilon > \eta > 0\varepsilon$ |
| Solution | |

(1 mark) Determine the proportion of tulips that were less than 30 cm high.

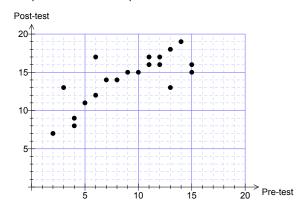
| | √ determines correct proportion. |
|---------------------|----------------------------------|
| Specific Behaviours | |
| | $(q.b2) 42.0 = \frac{14}{021}$ |
| uomios | |

(2 marks) that could be displayed at the fair? tulips must be at least 30 cm high. What is the highest percentage of Jennifer's tulips Jennifer wants to display some of her tulips at the annual spring fair. To be eligible,

| √ determines number of tulips that could be displayed |
|---|
| Specific Behaviours |
| $%8.68 = 0.01 \times \frac{97}{0.01}$ |
| Solution |

MATHEMATICS 2A/2B 12 MARKING KEY CALCULATOR-ASSUMED

The test results were plotted on the scatterplot as shown below.



Use the scatterplot and any previous information to answer the following:

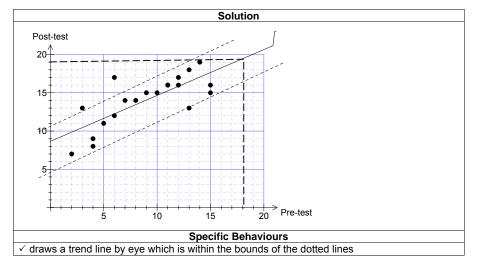
(d) What result did the student who scored 12 in the post-test achieve in the pre-test?

(1 mark)

| Solution | | |
|--|--|--|
| 6 | | |
| Specific Behaviours | | |
| ✓ identifies pre-test score from scatterplot | | |

(e) Draw in a trend line on the scatterplot above.

(1 mark)



MATHEMATICS 2A/2B 13 MARKING KEY CALCULATOR-ASSUMED

(f) Show how to use your trend line to predict a post-test score for a student who scored 18 in the pre-test but was absent for the post-test. Comment on the reliability of your prediction. (2 marks)

| Solution | | |
|---------------------------------|--|--|
| See diagram (e) | | |
| Post-test approx 19/20 | | |
| Unreliable due to extrapolation | | |
| Specific Behaviours | | |
| | | |

√ check student answer from diagram

[✓] comment on unreliability of prediction because of extrapolation