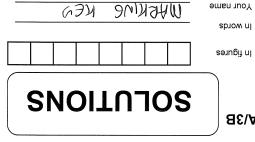
Rossmoyne Senior High School

Year 12 Trial WACE Examination, 2014

Question/Answer Booklet



MATHEMATICS 3A/3B

Student Number:

Calculator-assumed Section Two:

(J) MARKINE

Time allowed for this section

Working time for this section: one hundred minutes Reading time before commencing work: ten minutes

To be provided by the supervisor Materials required/recommended for this section

Formula Sheet (retained from Section One) This Question/Answer Booklet

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters

and up to three calculators satisfying the conditions set by the Curriculum Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

Council for this examination.

Important note to candidates

examination room. If you have any unauthorised material with you, hand it to the supervisor that you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be used in this section of the examination. It is your responsibility to ensure

before reading any further.

MATHEMATICS 3A/3B CALCULATOR-ASSUMED

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MATHEMATICS 3A/3B

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam	
Section One: Calculator-free	6	6	50	50	331⁄3	
Section Two: Calculator-assumed	13	13	100	100	66¾	
			Total	150	100	

Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2013. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages
 are included at the end of this booklet. They can be used for planning your responses
 and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question(s) that you are continuing to answer at the top of the
 page.
- 3. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.

See next page

CALCULATOR-ASSUMED 19 MATHEMATICS 3A/3B

Additional working space

Question	number:	
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Section Two: Calculator-assumed (100 Marks)

This section has thiteen (13) questions. Answer all questions. Write your answers in the spaces provided.

Working time for this section is 100 minutes.

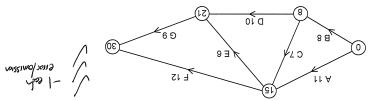
Question 7 (7 marks)

The tasks involved in a project, their immediate predecessors and duration, are shown below.

6	12	9	01	L	8	11	Duration (days)
D, E	D,A	D,A	8	8	-	-	Immediate predecessor
ຄ	4	7	а	2	Я	A	I SSK

(3 marks)

(a) Use the above information to complete the project network below.

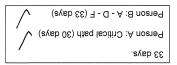


(2 marks)

(b) State the critical path and the minimum completion time for the project.



(c) What is the minimum time that two people would take to complete all tasks if only one person can be allocated to each task at any one time? Justify your answer. (2 marks)

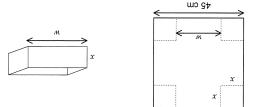


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CALCULATOR-ASSUMED 18 MATHEMATICS 3A/3B

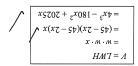
Question 19 (7 marks)

A square sheet of metal has sides of length 45 cm. An open box, with a square base of side w cm, is made by cutting squares with sides of x cm out of the corners of the metal sheet and folding up the sides.

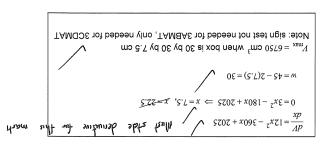


(a) Explain why w = 45 - 2x. (1 mark) Width of box is width of sheet (45 cm) less two corners (2x).

(b) Show that the volume of the open box is given by $V=4x^3-180x^2+2025x$ cm³. (2 marks)



(c) Using calculus techniques, determine the dimensions of the open box that has the maximum possible volume and state what this volume is $(4 \, {\rm marks})$



MATHEMATICS 3A/3B

(6 marks)

Question 8 The net contents of packets of breakfast cereal filled by a machine are normally distributed with a mean of 574.7 g and a standard deviation of 6.3 g.

If a packet is chosen at random from the production line, determine the probability that the contents of the packet

are less than 565 g.

(1 mark)

P(x < 565) = 0.062

lies between 570 g and 580 g.

(1 mark)

P(570 < x < 580) = 0.572

During one shift, the machine filled 2 400 packets with cereal. Estimate how many of these packets have contents of less than 555 g.

$$P(X < 555) = 0.000883$$

 $0.000883 \times 2400 = 2 \ packets$ tion here

Determine, to the nearest gram, the contents exceeded by 5% of all packets of cereal produced.

$$P(x > k) = 0.05$$

 $k = 585 \text{ g}$

See next page

CALCULATOR-ASSUMED 17 **MATHEMATICS 3A/3B**

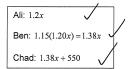
Question 18 (6 marks)

Three nurses were comparing their earnings, during the last tax year, to the national average for their occupation. Ali earned 20% more than the average, Ben earned 15% more than Ali and Chad earned \$550 more than Ben.

Let x be the national average wage for nurses.

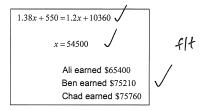
Write a simplified expression, in terms of x, for the earnings of each of the nurses.

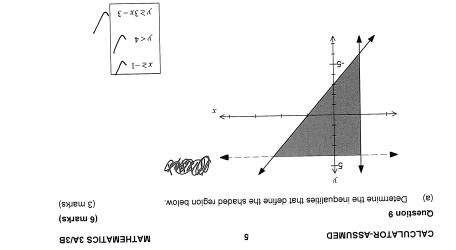
(3 marks)



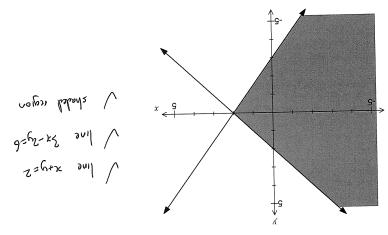
Chad actually earned \$10 360 more than Ali.

Use this information to write an equation, solve it for x and hence determine the earnings of each of the nurses. (3 marks)





Shade the region satisfied by the inequalities $x+y \le 2$ and $3x-2y \le 6$ on the axes below. (3 marks)



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CALCULATOR-ASSUMED 16 MATHEMATICS 3A/3B

Question 17

Question 17

To gain entry to a new apartment building, tenants are given an access code consisting of a non-zero digit, followed by a letter, followed by another non-zero digit (e.g. 3F2, 7Q7, etc).

(a) Show that 2106 access codes are possible. (1 mark)

(b) How many different access codes are possible that contain a vowel and start and end with an even digit? (1 mark)

08 = 4 × 2 × 4

(c) What is the probability that a randomly selected access code

(i) contains a vowel? $\frac{5}{26}$

(ii) starts and ends with an even digit? (i) $\frac{\delta L}{18} = \frac{16}{1000} = \frac{1}{1000} = \frac{1}{1000$

(iii) contains a vowel or starts and ends with an even digit? (2 marks)

6

MATHEMATICS 3A/3B

Question 10

(8 marks)

The ages of the 45 students attending a Statistics evening class are listed below in ascending order. The mean and standard deviation of these ages are 26.6 and 10.8 respectively.

15, 16, 16, 17, 17, 17, 18, 18, 18, 19, 19, 19, 20, 20, 21, 21, 21, 21, 22, 22, 24, 24, 24, 24, 25, 25, 25, 25, 25, 26, 27, 28, 29, 30, 32, 33, 33, 34, 34, 37, 37, 39, 56, 58, 65.

(a) Determine the mode and the median of these ages.

(2 marks)



The ages of students attending a Mathematics evening class are summarised in the frequency table below.

Age	15-19	20-24	25-29	30-34	35-39	40-44
Frequency	5	12	15	9	3	1

(b) Estimate the mean and standard deviation for the ages of the students attending the Mathematics evening class, rounding both figures to three significant figures. (3 marks)

Mean: 26.6 SD: 5.85

J 3.SFs for both

(c) Use the mean and standard deviation to compare the above age datasets for the Statistics and Mathematics classes, explaining any significant differences. (3 marks)

By comparing the means, the average age of students attending both classes can be seen to be the same.

By comparing the standard deviations, it can be seen that the spread of ages of students in the Statistics class was much larger than that of the students in the Math class.

This larger spread in the Statistics class is caused by the three students aged over 50, who are outliers for this dataset.

l mark for each reasonable routed statement

Be leviert.

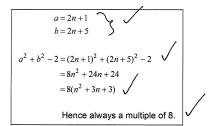
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CALCULATOR-ASSUMED

MATHEMATICS 3A/3B

Prove algebraically that the value of a^2+b^2-2 will always be a multiple of eight if a is an odd integer and b is four more than a.

15

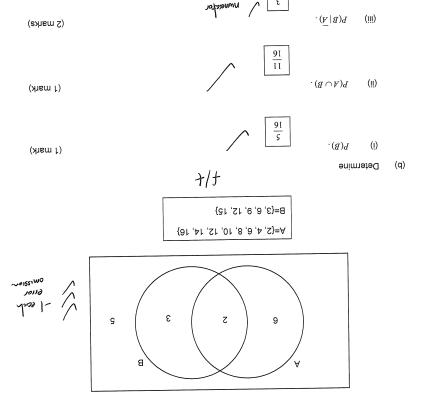


T MATHEMATICS 3A/3B

Question 11
A bag contains 16 balls, numbered from 1 to 16. When one ball is selected at random from the A bag contains 16 balls, numbered from 1 to 16. When one ball is a line 1 that the number of the ball is a line 1 that the number of the ball is a line 1 that the number of the ball is a line 1 that the number of the ball is a line 1 that the number of the ball is a line 1 that the number of the ball is a line 1 that the number of the line 1 that th

bag, event A is that the number on the ball is even and event B is that the number on the ball is a multiple of three.

. (a) Complete the Venn diagram below to show $n(A\cap B)$, $n(A\cap B)$, $n(A\cap B)$ and substance (a) smarks)



See next page

CALCULATOR-ASSUMED 14 MATHEMATICS 3A/3B

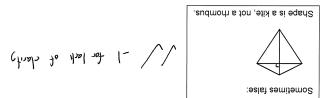
Question 16 (10 marks)

(a) Consider the validity of each of the following geometric arguments and state whether each one is always true or sometimes talse.

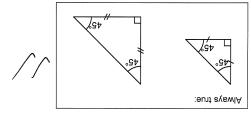
If an argument is always true, sketch one example that demonstrates that it is true. If an argument is sometimes false, sketch one example that shows it is false.

Clearly label key features of your sketch that support your answer.

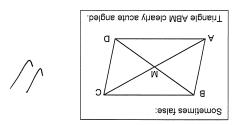
(i) If a quadrilateral has perpendicular diagonals, then it is a rhombus.'



(ii) 'Two right isosceles triangles will always be similar.' (2 marks)



iii) 'If M is the point of intersection of the diagonals AC and BD of parallelogram ABCD, then triangle ABM must be an obtuse triangle. (2 marks)



8

MATHEMATICS 3A/3B

Question 12 (7 marks)

Angela buys a motorbike for \$14 500. She borrows the full amount from a credit company, making monthly repayments of \$1 500. Initially, the interest rate was 13.2% per annum.

The spreadsheet below shows the balance and monthly interest for the life of the loan.

Month (n)	Balance at start of month (T_n)	Interest
1	14 500.00	159.50
2	13 159.50	144.75
3	11 804.25	129.85
4	10 434.10	114.78
5	9 048.88	99.54
6	7 648.42	91.78
7	6 240.20	74.88
8	4 815.08	57.78
9	3 372.86	40.48
10	1 913.34	22.96
11	436.30	5.24

(a) Calculate the eleventh (final) payment made by Angela.

b) Write a recursive rule to determine the balance at the start of each month, when the interest rate was 13.2% per annum. (2 marks)

(c) The interest rate increased at the start of one month and then did not change for the remainder of the loan period.

(i) In which month did the rate increase?

(ii) What was the increase in the annual interest rate?

(2 marks)

(1 mark)

(1 mark)

(1 mark)

$$\frac{91.78}{7648.42} \times 12 \times 100 = 14.4\%$$
Increase is 1.2%

f/t

(d) What was the total amount of interest paid by Angela?

See next page

CALCULATOR-ASSUMED

13

MATHEMATICS 3A/3B

(3 marks)

c) Calculate the value of the missing entries A and B in the table.

$$A = 647.9 - 639.0 \implies A = 8.9$$

$$\frac{664.1}{2} + 649.7 + 647.5 + 642.6 + \frac{B}{2}$$

$$= 652.7 \implies B = 677.9$$

(d) Use your calculator to determine the equation of the linear regression line that could be used to predict the four-point centred moving average (n) from time (t) and state the correlation coefficient for this association. (3 mark

(e) Use appropriate data from the residuals in the table to calculate the seasonal component for February. (1 mark

(f) Predict the number of people employed in the accommodation and food services industry in Australia in February 2006 and comment on the reliability of your prediction. (3 marks)

$$t = 21$$

 $n = 2.225(21) + 618.503 + 3.567$
 $= 668.342$
Or
 $668342 people(approx)$

Despite strong correlation for this relationship, the prediction involves considerable extrapolation and \checkmark so should be treated with caution.

(2 marks) . Determine the largest possible area of triangle ABC. mo £6.4 = 3 (1 mark) (ii) determine the length c. or $0 \cos (6.61) \cos (-2.61) \cos (-2.61)$ $\angle A = 180 - 67.2 = 112.8^{\circ} \implies \angle C = 180 - 112.8 - 50 = 17.2^{\circ}$ write down an equation that could be solved to determine the length c. (2 marks) (b) If ABC is an obtuse-angled triangle, °2.78 = A (1 mark) determine the size of AA. (ii) 0∂ nis A nis 8.21 _ 4.21 write down an equation that could be solved to determine the size of A.A. (1 mark) (a) If ABC is an acute-angled triangle, In triangle ABC, $a=15.4\,\mathrm{cm},\ b=12.8\,\mathrm{cm}$ and $\angle B=50^\circ$. (7 marks) Question 13 MATHEMATICS 3A/3B CALCULATOR-ASSUMED

See next page

²mɔ √.√8 =

Area = 0.5(15.4)(12.8) sin 62.8

 $\angle C = 180 - 67.2 - 50 = 62.8^{\circ}$

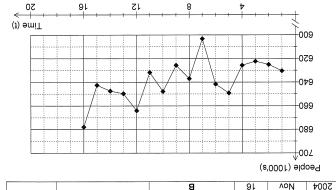
Largest if triangle ABC is acute angled.

CALCULATOR-ASSUMED 12 MATHEMATICS 3A/3B

Question 15 (12 marks)

The table and graph below show the number of people employed in the accommodation and food services industry in Australia from February 2001 to November 2004.

			1 01		1000
		9.248	91	₿n∀	2004
2.2-	7.239	3.74a	ÞΙ	May	2004
1.0	9.649	7.649	13	Feb	2004
8.31	6.848	1.499	15	voM	2003
9.51-	4.348	8.168	11	gu∀	2003
A	0.985	6.74a	01	May	2003
£.8-	0.289	7.329	6	Feb	2003
£.6	7.728	0.758	8	voM	2002
9.92-	8.628	2.809	L	gu∀	2002
5.01	4.188	7.14a	9	May	2002
6.91	6.289	2.648	9	Feb	2002
6.9-	9.289	7.329	7	voM	2001
6.3-	2.829	6.22.3	3	₿n∀	2001
		0.329	7	May	2001
		4.088	l	Feb	2001
	moving average (n)		(1)		
Residual	Four-point centred	People (1000's)	əmiT	Quarter	Year



(a) How do the data points for August support the use of a four-point centred moving average to smooth the entire data set?

The data points for August tend to be the lows for each year, suggesting that there is a cycle of four quarters to the data.

Write down the calculation used to evaluate the four-point centred moving average for (1 mark)

$$\frac{\frac{2.04\lambda}{2} + 7.22\lambda + 6.22\lambda + 0.22\lambda + \frac{4.06\lambda}{2}}{4}$$

10

MATHEMATICS 3A/3B

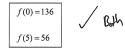
Question 14

(11 marks)

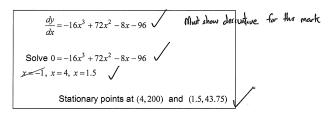
Consider the function $f(x) = 136 - 96x - 4x^2 + 24x^3 - 4x^4$.

(a) Calculate f(0) and f(5).

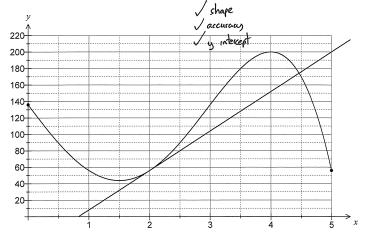
(1 mark)



(b) Using calculus techniques, determine the coordinates of all stationary points of the graph of y = f(x) in the interval $0 \le x \le 5$. (4 marks



(c) Sketch the graph of y = f(x) over the interval $0 \le x \le 5$. (Ignore tangent line drawn)(3 marks)



See next page

CALCULATOR-ASSUMED

11

MATHEMATICS 3A/3B

(1 mark)

(d) Calculate the gradient of the curve y = f(x) at the point (2, 56).

f'(2) = 48

trie point (2, 5

(e) State the equation of the tangent to the curve y = f(x) at the point (2, 56). (2 marks)

$$y = 48x - 40$$