



# MATHEMATICS

3C/3D

Section One:

Calculator-free

Student Name: \_\_\_\_\_

**Time allowed for this section**

Reading time before commencing work: Five (5) minutes  
Working time for this section: Fifty (50) minutes

**Material required/recommended for this section*****To be provided by the supervisor***

This Question/Answer Booklet

Formula Sheet

***To be provided by the candidate***

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid, ruler, highlighters

Special items: nil

**Important note to candidates**

No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Additional working space

Question number(s): \_\_\_\_\_

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Section	Section One:	Section Two:	Calculator-assumed
Number of questions to be answered	8	13	13
Working time (minutes)	50	100	100
Marks available	40	80	120
Percentage of exam	33 1/3	66 2/3	100

Structure of this paper

Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2011*. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

3. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

4. It is recommended that you **do not use pencil** except in diagrams.

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## Section One: Calculator-free

(40 Marks)

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the space provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

The working time for this section is 50 minutes.

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## Question 1

(2 marks)

Show, by counter-example, that the conjecture

$$a > b \Rightarrow (a+1)^2 > (b+1)^2$$

is not true for all integers  $a$  and  $b$ .

[2]

See next page

## Additional working space

Question number(s): \_\_\_\_\_

The velocity  $v(t)$  in metres per second at time  $t$  seconds of an object moving in a straight line is given by:  $v(t) = 3t^2 - 10t$  where  $0 \leq t \leq 5$

(a) Find  $x(t)$ , the displacement at time  $t$  given  $x(0) = 0$

[2]

(b) At what time, in the given interval, does the object return to its starting point?

[1]

(c) At what time, in the given interval, is the object furthest from its starting point?

[2]

See next page

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Additional working space

Question number(s): \_\_\_\_\_

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SEMESTER TWO EXAMINATION  
SECTION ONE

6

MATHEMATICS 3C/3D  
CALCULATOR FREE

## Question 3

(4 marks)

Find the equation of the tangent to the curve  $y = (x+3)^2 e^{-x}$  at the point with coordinates  $(0,9)$ .

[4]

## Question 4

(8 marks)

(a) Find  $\frac{dy}{dx}$ ;

(You do not need to perform more than the most obvious algebraic simplifications)

(i)  $y = \frac{e^{\frac{1}{x}}}{(1-3x)^4}$

[3]

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SEMESTER TWO EXAMINATION  
SECTION ONE

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MATHEMATICS 3C/3D  
CALCULATOR FREE

## Question 8

(4 marks)

Find the value(s) of  $x$  for which

$$\frac{1}{x+1} \leq \frac{1}{x^2-1}$$

[4]

See next page

Question 7 (6 marks)

A bag contains 40 beads of the same shape and size.  
The ratio of red to green to blue beads is 1 : 3 : 4 and there are no beads of any other colour.  
A bead is picked at random, its colour noted and the bead replaced in the bag. This is done ten times

- (a) Find an expression for the probability that
- (i) five are blue

- (ii) at least one is red

[2]

[2]

The experiment is repeated, but this time a bead is picked out and replaced  $n$  times

- (b) Find in the form  $a^n > b$ , where  $a$  and  $b$  are exact fractions, the condition which  $n$  must satisfy in order to have at least a 99% chance of picking out at least one red bead.  
(You do not need to solve the inequality)

[2]

See next page

(ii) 
$$y = \int_{5x}^0 \frac{3\sqrt{1-t^2}}{t} dt$$

- (b) Evaluate 
$$\int_1^{e\sqrt{e}} \frac{\sqrt{x}}{x} dx$$

[2]

[3]

See next page

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Question 5 (7 marks)

Given  $f(x) = x^2 - 2$ ,  $x \in \mathbb{R}$ , and  $g(x) = \sqrt{2-x}$ ,  $x \leq 2$

(a) Find and simplify an expression for  $f \circ g(x)$

[2]

(b) State the range of  $f \circ g(x)$

[1]

(c) State the domain and range of  $g \circ f(x)$

[3]

(d) Find an unsimplified expression for  $f \circ f(x)$

[1]

See next page

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Question 6 (4 marks)

(a) Differentiate  $\left(1 - \frac{1}{x}\right)^3$

[1]

(b) The gradient function of a curve is given by  $\frac{dy}{dx} = \frac{3}{x^2} \left(1 - \frac{1}{x}\right)^2$   
Find the equation of this curve given it passes through the point  $(1, 0)$

[3]

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