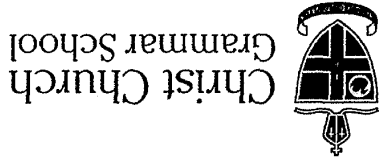


SOLUTIONS



Christ Church
Grammar School

MATHEMATICS METHODS Year 11

Section One:
Calculator-free

2018
UNIT TEST 3
+ for units
on whole
papers

Student name _____

Teacher name _____

Time and marks available for this section
Reading time before commencing work: 2 minutes
Working time for this section: 15 minutes
Marks available: 15 marks

Materials required/recommended for this section
To be provided by the supervisor
This Question/Answer Booklet
Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates
No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Instructions to candidates

1. Write your answers in this Question/Answer Booklet.
2. Answer all questions.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specific to a particular question.
4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that **you do not use pencil**, except in diagrams.

See next page

Additional working space

Question number: _____

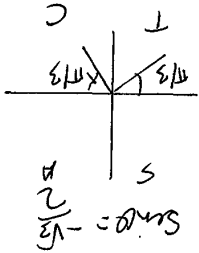
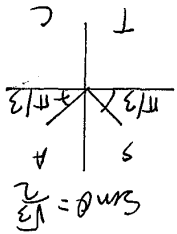
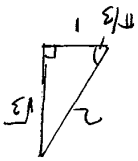
Question 1

Solve the following:

$$4\sin^2(\theta) - 3 = 0 \quad \text{for } 0 \leq \theta \leq 2\pi$$

$$\begin{aligned} 4\sin^2\theta &= 3 \\ \sin^2\theta &= \frac{3}{4} \\ \sin\theta &= \pm\sqrt{\frac{3}{4}} \end{aligned}$$

$$\begin{aligned} \checkmark \text{ (for } \sin\theta = \sqrt{\frac{3}{4}} \text{)} \\ \checkmark \text{ (for } \sin\theta = -\sqrt{\frac{3}{4}} \text{)} \end{aligned}$$



$$\theta = \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$$

$$\checkmark \text{ (for } \frac{\pi}{3}, \frac{5\pi}{3} \text{)} \quad \checkmark \text{ (for } \frac{2\pi}{3}, \frac{4\pi}{3} \text{)}$$

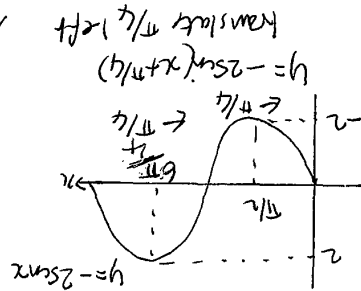
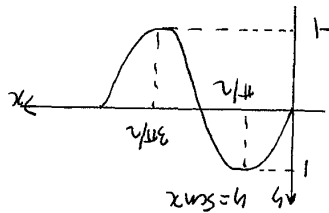
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Question 4

Consider the following function:

$$y = -2\sin\left(x + \frac{\pi}{4}\right)$$

Determine the coordinates (x, y) of the maximum and minimum points of this function for $0 \leq x \leq 2\pi$.



✓ (for appropriate working out)

Maximum point is

$$\left(\frac{5\pi}{4}, 2\right)$$

✓ (for maximum point)

Minimum point is

$$\left(\frac{\pi}{4}, -2\right)$$

✓ (for minimum point)

End of questions

Question 2

(5 marks)

The function $f(x)$ is given by:

$$f(x) = x^3 - 2x^2 - x + 2$$

(a) Show that $x - 1$ is a factor of $f(x)$.

(1 mark)

$$f(1) = 1^3 - 2 \times 1^2 - 1 + 2 = 0$$

$\therefore x-1$ is a factor of $f(x)$,
✓(for showing $f(1) = 0$)

(b) Solve the following equation:

$$x^3 - 2x^2 - x + 2 = 0$$

(4 marks)

$$\begin{array}{r} x^3 - 2x^2 - x + 2 \\ x-1 \overline{) x^3 - 2x^2 - x + 2} \\ \underline{-x^3 + x^2} \\ x^2 - x + 2 \\ \underline{-x^2 + x} \\ -2x + 2 \\ \underline{-2x + 2} \\ 0 \end{array}$$

$$x^3 - 2x^2 - x + 2 = (x-1)(x^2 - x - 2)$$

✓(for initial factorization with correct working out)

$$x^2 - x - 2 = (x-2)(x+1)$$

✓(for factorising quadratic)

$$\therefore x^3 - 2x^2 - x + 2 = (x-1)(x-2)(x+1)$$

✓(for complete factorisation)

So solutions are

$$x = 1, 2, -1$$

✓(1 mark for all 3 solutions)

See next page

Question 3

(3 marks)

Solve the following:

$$1 + \sqrt{2} \cos(2\theta) = 0 \quad \text{for } 0 \leq \theta \leq 2\pi$$

$$\sqrt{2} \cos(2\theta) = -1$$

$$\cos(2\theta) = \frac{-1}{\sqrt{2}} \quad \checkmark \text{ (for simplifying equation)}$$

$$\therefore 2\theta = \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{11\pi}{4}, \frac{13\pi}{4} \quad \checkmark \text{ (for giving all 4 values of } 2\theta, \text{ including adjusting domain to include } 2\theta = \frac{11\pi}{4}, \frac{13\pi}{4})$$

$$\therefore \theta = \frac{3\pi}{8}, \frac{5\pi}{8}, \frac{11\pi}{8}, \frac{13\pi}{8}$$

✓(for converting 2θ values to θ values)

Note: give at most 2 out of 3
if just give $\theta = \frac{3\pi}{8}, \frac{5\pi}{8}$

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