

Semester One Examination, 2019

Question/Answer booklet

E TINU MATHEMATICS METHODS

Calculator-free Section One:

laterials required/recomn o be provided by the supervisor
 ime allowed for this secti eading time before commencing w orking time:
Your Teacher's Name:
Допк Изте:

This Question/Answer booklet

Formula sheet

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

Special items:

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that

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Max	Mark	Question	Max	Marks	Question

CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	34
Section Two: Calculator- assumed	13	13	100	104	66
				Total	100

Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR
 course examinations are detailed in the Year 12 Information Handbook 2019. Sitting this
 examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- 3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- 5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

Working time: 50 minutes. number of the question that you are continuing to answer at the top of the page. original answer space where the answer is continued, i.e. give the page number. Fill in the Continuing an answer: If you need to use the space to continue an answer, indicate in the Planning: If you use the spare pages for planning, indicate this clearly at the top of the page. responses and/or as additional space if required to continue an answer. Spare pages are included at the end of this booklet. They can be used for planning your This section has seven questions. Answer all questions. Write your answers in the spaces (25 Marks) Section One: Calculator-free MATHEMATICS METHODS 3 CALCULATOR-FREE

(b) $\frac{\cos x}{\xi^{+} \frac{\zeta}{X}}$ (do not simplify) (S marks)

See next page

 p_{ϵ^1}

(a) $e^x \sin(x^2 + 2)$

Question 1

Differentiate the following with respect to X:

(S marks)

(S warks)

(6 marks)

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Question number:

Explain why the incremental formula does not give a good estimate for the change in V

in part (a).

CALCULATOR-FREE 13 MATHEMATICS METHODS

End of questions

See next page See next page

(1 mark)

75

Question 3 (8 marks)

Determine the following:

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(a)
$$\frac{d}{dx}(e^{2x}\sin 3x)$$

(b)
$$\frac{d}{dx}(e^{2x}\cos 3x)$$

Hence, determine the following integral by considering $\mbox{\bf both}$ $\mbox{\bf expressions}$ above.

(c)
$$\int_{\frac{\pi}{2}}^{0} 13 e^{2x} \cos 3x dx$$
 (4 marks)

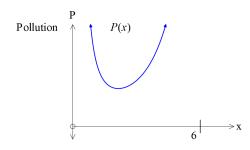
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Question 4 (6 marks)

The amount of pollution, P, in tonnes, to build x thousands number of transistors by an electronic manufacturer, is given by the following formula:

$$P(x) = \frac{e^x}{x^3}$$

where $0 < x \le 5.5$ thousands.



number of transistors in thousands

(a) Describe how the pollution changes as the number of transistors made, varies from $0 < x \le 5.5$ thousands. (2 marks)

Question 7 (10 marks)

Consider a smooth and continuous function f(x) where f(-5)=0=f(0)=f(7)=f(10), f(-3)=22 and f(4)=-13. It is known that $f(x)\ge 0$ for $-5\le x\le 0$ and $7\le x\le 10$ with f(x)<0 for all other values. It is also given that $\int\limits_{-5}^{10}f(x)dx=19$ and $\int\limits_{0}^{7}f(x)dx=-6$ and $\int\limits_{7}^{10}f(x)dx=15$.

Determine the following:

(a)
$$\int_{-3}^{4} f'(x) dx$$
 (2 marks)

(b)
$$\int_{-5}^{7} f(x) dx$$
 (2 marks)

(c) the stationary points of
$$g(x)$$
 given that $g(x) = \int_{-5}^{x} f(t) dt$ with $-5 \le x \le 10$ (3 marks)

It is known that
$$f'(x) \le 0$$
 for $-3 \le x \le 4$ and $f'(x) \ge 0$ for $-5 \le x \le -3$.
(d) Determine the area under the curve $y = f'(x)$ from $-5 \le x \le 4$. (3 marks)

(b) Using calculus, determine the number of transistors that will minimize the pollution produced. (4 marks)

See next page

Question 5 (6 marks)

Twenty teachers have been marking the same set of exam papers and after double checking it was found that the teachers made the following number of errors, 1, 1, 3, 1, 4, 4, 1, 3, 5, 1, 2, 2, 4, 4, 5, 0, 6, 5, 5, 5.

Let X = i the number of errors of a teacher.

(a) Construct a table that defines the **probability distribution** of X. (3 marks)

(b) Use the probability distribution above to show how to evaluate the expected value of X. State this value. (3 marks)

Question 6 (10 marks)

In a shop an average of 1 out of 5 pay with cash, 3 out of every 5 customers use a credit card, and the rest use a debit card to pay. A single customer is selected from the shop. The random variable X is defined as the number of customers who pay with cash.

(a) Complete the probability distribution for *X* shown below.

(2 marks)

х	0	1
P(X=x)		

b) State the distribution of X.

(1 mark)

(c) Determine the mean and standard deviation of the distribution.

(2 marks)

Four customers are waiting in a queue to pay. The random variable Y is defined as number of customers from this queue who pay with **credit card**.

(d) State the distribution of Y, including its parameters. marks)

(2

(3 marks)

Evaluate the probability of at most one customer paying with credit card.
 (No need to simplify)