

# Trinity College

## Semester Two Examination, 2017

Question/Answer booklet

ed by your examination administrator, please your student identification label in this box	

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Calculator-free Section One:

Materials required/recommended for this section To be provided by the supervisor			
	sətunim əvit fifty minutes	cing work:	Time allowed for this s Reading time before commen Working time:
		Your name	
		ln words	
		ln figures	Student Number:

To be provided by the superv This Question/Answer booklet

Formula sheet

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction To be provided by the candidate

fluid/tape, eraser, ruler, highlighters

Special items:

### Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand

it to the supervisor before reading any further.

TRINITY COLLEGE 2 SEMESTER 2 2017
METHODS UNITS 3 AND 4 CALCULATOR-FREE

#### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	97	65
				Total	100

#### Instructions to candidates

- The rules for the conduct of Trinity College examinations are detailed in the *Instructions to Candidates* distributed to students prior to the examinations. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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#### CALCULATOR-FREE 11 METHODS UNITS 3 AND 4

Additional working space	
Question number:	

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(2 marks)

TRINITY COLLEGE CALCULATOR-FREE

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Section One: Calculator-free 35% (52 Marks)

3

This section has  ${\bf eight}\, {\bf (8)}$  questions. Answer  ${\bf all}$  questions. Write your answers in the spaces provided.

Working time: 50 minutes.

(q)

Question 1 (6 marks)

The discrete random variable X is defined by

$$\Gamma(X = x) = \begin{cases} \frac{\lambda}{1+x} \\ 0 \end{cases} = (x = x)q$$

(a) Determine the value of the constant k.

Determine

(i) E(5-3X).

(ii) Var(1+6X).

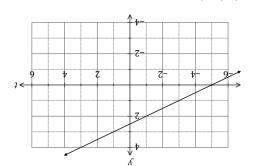
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METHODS UNITS 3 AND 4

Question 8 (5 marks)

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Part of the graph of the linear function y=f(t) is shown below.



 $\mbox{ Another function } \mathbb{A}(x) = \mathbb{A}(x)$  where tunction  $\mathbb{A}(x) = \mathbb{A}(x)$ 

Use the increments formula to estimate the change in A as x increases from 7 to 7.1.

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Question 2

(6 marks)

(a) Determine k, if  $2 \log_4 6 - \log_4 3 + 1 = \log_4 k$ .

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(3 marks)

(b) Determine the exact solution to  $3(4)^{x-1} = 18$ .

(3 marks)

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Question 7 (7 marks)

A function is defined by  $f(x) = \frac{1 + \ln x}{-2x}$ .

(a) State the natural domain of f. (1 mark)

Show that f'(1) = 0. (3 marks)

(c) Use the second derivative test to determine the nature of the stationary point of the function at x = 1. (3 marks)

(3 шэцкэ)	the particle from A after 20 s.	(b) Determine the distance of
(1 mark)	y of the particle.	(a) Calculate the initial velocity
	e at A, a fixed point on the line.	Initially, when $t=0$ , the particle is
	$s/m = 3 + 2e^{0.1t} cm/s.$	
ght line at any time t seconds is	et s particle moving in a strai	The rate of change of displaceme given by
(7 marks)		Question 3
SEMESTER 2 2017 METHODS UNITS 3 AND 4	g	TRINITY COLLEGE CALCULATOR-FREE

(c) Determine when the acceleration of the particle is  $7 \text{ cm/s}^2$ . (3 marks)

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(e marks) Question 6

The first derivatives of the functions are  $f'(x) = 30(5x + 7)^2$  and  $g'(x) = 10\pi \sin(\pi(1 - 2x))$ .

The functions f and g intersect at the point (-1,7).

Determine an expression for each function.

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Question 4 (7 marks)

The graph of y = f(x),  $x \ge 0$ , is shown below, where  $f(x) = \frac{4x}{x^2 + 3}$ .



(a) Determine the gradient of the curve when x = 2.

(3 marks)

(b) Determine the exact area bounded by the curve y=f(x) and the lines y=0 and x=2, simplifying your answer. (4 marks

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Question 5 (8 marks)

A curve has first derivative  $\frac{dy}{dx} = 6x(x-2)$  and passes through the point P(-1, -8).

(a) Determine the value(s) of x for which  $\frac{d^2y}{dx^2} = 0$ . (2 marks)

(b) Sketch the curve on the axes below, clearly indicating the location of all axes intercepts, stationary points and points of inflection. (6 marks

