



Course Specialist Test 3 Year 12

Student name: _____ Teacher name: _____

Task type: Response

Time allowed for this task: 40 mins

Number of questions: 7

Materials required: Calculator with CAS capability (to be provided by the student)

Standard items: Pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: Drawing instruments, templates, notes on one unfolded sheet of A4 paper, and up to three calculators approved for use in the WACE examinations

Marks available: 44 marks

Task weighting: 10%

Formula sheet provided: Yes

Note: All part questions worth more than 2 marks require working to obtain full marks.

Q1 (6 marks) (3.3.9-3.3.10)

a) Solve the following system of linear equations.

$$\begin{aligned}x + 2y - 3z &= -28 \\2x - 7y + 5z &= 76 \\3x - 4y + 6z &= 71\end{aligned}$$

(3 marks)

b) Determine all possible values of p & q for the three scenarios below.

$$\begin{aligned}x + 2y - 3z &= q \\2x - 7y + 5z &= 76 \\3x - 4y + pz &= 71\end{aligned}$$

- i) No solutions
- ii) One solution
- iii) Infinite solutions

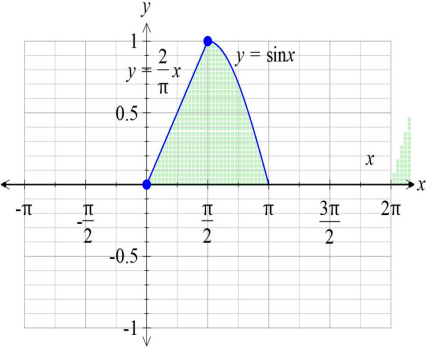
(3 marks)

b) Given that $V = 50\text{ m/s}$, $g = 10\text{ m/s}^2$ and that $y = 44\text{ m}$ when $x = 38\text{ m}$, determine possible value(s) for α .

(3 marks)

Q7 (4 marks) (4.1.6)

Consider the area between $y = \sin x$, $y = \frac{2}{\pi}x$ and the x axis with $0 \leq x \leq \pi$, as shown below.



If the shaded area above is revolved **around the y axis**, determine the volume of the 3D object created to two decimal places.

Mathematics Department

Q2 (9 marks) (3.3.15)

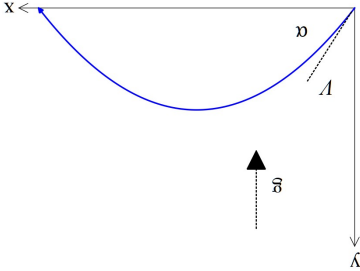
A particle moves with acceleration $\begin{pmatrix} 4 \\ -1 \end{pmatrix} m/s^2$ and initial position $\begin{pmatrix} 3 \\ -2 \end{pmatrix} m/s$ at time t seconds. The initial velocity is $\begin{pmatrix} 3 \\ -2 \end{pmatrix} m/s$

a) Determine the velocity at time t seconds. (2 marks)

Mathematics Department

Q6 (7 marks) (3.3.15)

Consider a projectile that leaves with speed $V m/s$ at an angle α to the horizontal, see diagram. Assume that the constant acceleration is $-g m/s^2$.



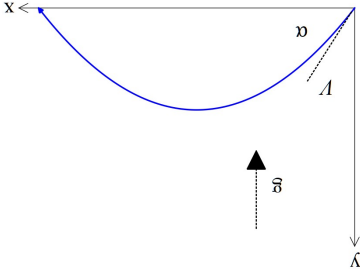
a) Using vector calculus and starting with the acceleration, show how to derive the cartesian equation of the path in terms of V, g & α . (4 marks)

b) Determine the position vector at time $t = 5$ seconds to two decimal places. (2 marks)

Mathematics Department

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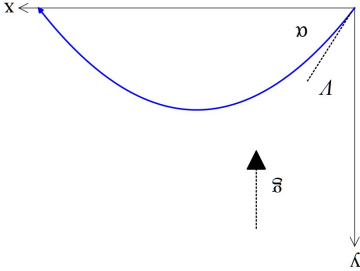
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Mathematics Department

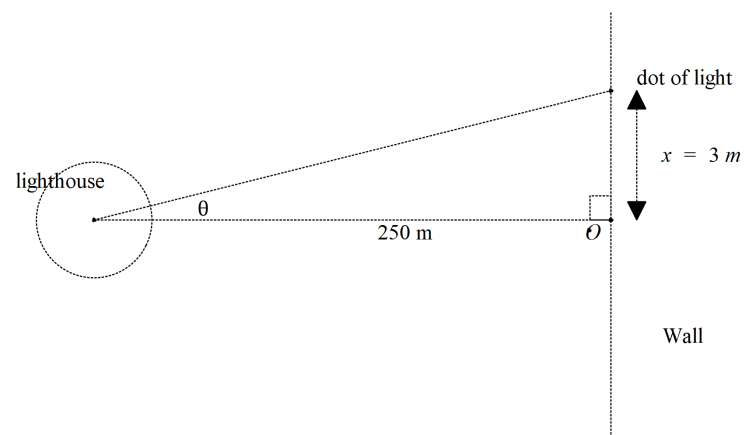
Q5 cont-

b) $\int \frac{(x-3)(x+5)}{2x+1} dx$

Q3 (7 marks) (4.2.1)

Consider an artificial island that contains a revolving light that is 250 metres from shore. There is a long wall on the shore and the light from the lighthouse can be seen as a moving dot of light on the

wall. The angular speed of the light is 24 radians/second, ($\frac{d\theta}{dt} = 24$).



- a) Determine the speed of the dot of light on the wall when the dot is 3 metres away from the closest point to the lighthouse, pt O, see diagram above. (4 marks)

- b) If the artificial island containing the lighthouse is moving towards the shore, pt O, at a speed of 5 metres per second, determine the speed of the dot when 3 metres away from pt O and the lighthouse being 170 metres from the shore, pt O. (3 marks)

Q4 (3 marks) (4.1.3)

Show using logarithmic differentiation how to differentiate $y = x^{\sin(2x)}$.

Q5 (8 marks) (4.1.1, 4.1.4)

Show how to evaluate the following **without any use of the classpad**. Show all working.

a) $\int_0^{\pi} \sin^3 x \, dx$

(4 marks)