

## Mathematics Methods Year 12 Test 6 2016

Section 1 Calculator Free Semester 2 Test

[7]	7	$\lambda = (x - 3)_{7} \text{ Ju } x_{5}$	(a)	
	of each of the following. Do not simplify your answers.	ovine the derivative	Deterr	
		.ķa)	1. (5 man	
	nore than 2 marks require working to be shown to receive full marks	rts of questions worth	Questions or par	
	cils, drawing templates, eraser, Formula page		Standard Items:	
<b>MARKS</b> : 21	TIME: 20 minutes	ay 2 September	DATE: Frid	
_	SAL'S NAME			

 $\lambda = \ln \sqrt{\frac{\Sigma^{x_2}}{(x_2 - \Sigma^{x_2})^3}}$ 

(9 marks)

A recent poll by ReachTEL, commissioned by prominent Perth business figures, sampled 10478 voters asking them the following question:

Who of the following do you think would make the better premier?

4574 of the respondents indicated they preferred Colin Barnett over Mark McGowan.

(a) Determine a sample proportion,  $\hat{p}$ , for those who preferred Colin Barnett.

(b) Determine a 99% confidence interval for the sample proportion who preferred Colin Barnett. [2]

(c) Population figures from the Australian Bureau of Statistics currently state that WA has a population of 2.6039 million people. Determine the minimum number of people, that we can be 99% confident, who will vote for Colin Barnett. [2]

Using  $\hat{p}$  as an estimate for the true proportion of WA voters who prefer Colin Barnett, determine how many people need to be sampled to achieve a margin of error of 1% for a 99% confidence interval.

(e) The original 10478 voters were also asked the following question:

Would you be more of less likely to vote for the Liberal party if Colin Barnett

The majority of voters stated their vote would remain unchanged.

Without knowing how many people indicated this, determine the maximum possible margin of error for a 99% confidence interval.

[2]

## 2. (6 marks)

Determine each of the following:

(a) 
$$\int \frac{x^2 + 5x^4}{2x^3} dx$$
 [3]

(b) 
$$\int \frac{5x^5 - 5x^2}{(x^3 - 1)^2} dx$$
 [3]

For oranges classified as **large**, the quantity of juice obtained from each orange is a normally distributed random variable with a mean of 74 mL and a standard deviation of 9 mL.

d) What is the probability that a randomly selected large orange produces less than 85 mL of juice, given that it produces more than 74 mL of juice? [3]

Mani also grows lemons, which are sold to a food factory. When a truckload of lemons arrives at the food factory, the manager randomly selects and weighs four lemons from the load. If one or more of these lemons is underweight, the load is rejected. Otherwise it is accepted.

It is known that 3% of Mani's lemons are underweight.

- (e) (i) Determine the probability that a particular load of lemons will be rejected. [3]
  - ii) Suppose that instead of selecting only four lemons, *n* lemons are selected at random from a particular load.

    Determine the smallest integer value of *n* such that the probability of at least one lemon being underweight exceeds 0.5. [3]

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(2 marks)

.9

A random variable X has the cumulative distribution function with rule:

$$0 > x \qquad 0$$

$$\downarrow \ge x \ge 0 \qquad \frac{^{c}x}{91}$$

$$\downarrow < x \qquad 1$$

Calculate:

(a) 
$$P(X \ge 2)$$

[7]

$$(\xi > X \mid \zeta \le X) q \qquad (d)$$

$$(\xi < X \mid \zeta = X)$$
 (5)

$$(z < X \mid z = X)$$
 (3)

$$(C \times V | T = V) I \qquad (2)$$

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$$(c) \quad L(Y = 7 \mid Y > 2)$$

Determine the probability that exactly one of the oranges has a diameter greater than 7 cm. [2]

Determine the probability that a randomly selected medium orange has a diameter greater than

The distribution of the diameter, in centimetres, of medium oranges is modelled by a continuous random

size. Oranges classifies as medium are sold to fruit shops and the remainder are made into orange juice.

Mani is a fruit grower. After his oranges have been picked, they are sorted by a machine, according to

standard deviation of medium oranges.

mean diameter of medium oranges

Mani randomly selects three medium oranges.

 $8 \ge x \ge 0 \quad (x-8)^2 (0-x) \frac{\varepsilon}{4}$   $= (x) \frac{\varepsilon}{2}$ 

variable, X, with probability density function

Determine, in centimetres, the:

(i)

(q)

[3]

[7]

## 4. (5 marks)

The function f is a probability density function with rule

$$f(x) = \begin{cases} \frac{a}{x} & \frac{1}{2} \le x \le 1\\ a & 1 < x < 2\\ 0 & otherwise \end{cases}$$

Determine the value of a.



## Mathematics Methods Year 12 Test 6 2016

Section 2 Calculator Assumed Semester 2 Test

STU	DENT	'S NAME					
DAT	DATE: Friday 2 September		<b>TIME:</b> 30 minutes		MARK	MARKS: 35	
INSTRUCTIONS: Standard Items: Special Items:		s: Pens, pencils, dra	Pens, pencils, drawing templates, eraser, Formula page (retain from Section 1) Three calculators, notes on one side of a single A4 page (these notes to be handed i assessment)				
Questi	ions or p	arts of questions worth more	than 2 marks require	e working to be shown t	o receive full marks.		
5.	(5 ma	arks)					
	The time (in seconds) that it takes a student to complete a puzzle is a continuous uniform random variable $X$ . It takes students between 2 and 18 seconds to complete the puzzle.						
	(a)	Determine the probabili	ty distribution fun	ction for $X$ .		[2]	
	(b)	Determine the probabili	ty that a student ta	ikes less than 12 seco	nds to complete the puzzle.	[1]	
	(c)	Determine the probabili		akes between 8 and 10	seconds to complete the p	ouzzle [2]	

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