

Stage 3 Physics STAWA Set 11: Photons

$$\begin{aligned}
 1 \quad E &= 2.0 \times 10^{-24} \text{ J} \\
 c &= 3.0 \times 10^8 \text{ ms}^{-1} \\
 h &= 6.63 \times 10^{-34} \text{ Js}
 \end{aligned}$$

$$\begin{aligned}
 a \quad E &= h.f \\
 f &= \frac{E}{h} \\
 &= \frac{2.0 \times 10^{-24}}{6.63 \times 10^{-34}} \\
 f &= 3.0 \times 10^9 \text{ Hz}
 \end{aligned}$$

$$\begin{aligned}
 b \quad c &= \lambda.f \\
 \lambda &= \frac{c}{f} \\
 &= \frac{3.0 \times 10^8}{3.0 \times 10^9} \\
 \lambda &= 1.0 \times 10^{-1} \text{ m } (=10 \text{ cm})
 \end{aligned}$$

c Compared with visible light, microwaves have lower energies, lower frequencies and longer (greater) wavelengths.

$$\begin{aligned}
 2 \quad c &= 3.0 \times 10^8 \text{ ms}^{-1} \\
 h &= 6.63 \times 10^{-34} \text{ Js} \\
 \text{red } \lambda &= 680 \text{ nm} = 680 \times 10^{-9} \text{ m} \\
 \text{orange (amber) } \lambda &= 580 \text{ nm} = 580 \times 10^{-9} \text{ m} \\
 \text{green } \lambda &= 500 \text{ nm} = 500 \times 10^{-9} \text{ m}
 \end{aligned}$$

$$\begin{aligned}
 c &= \lambda.f \\
 f &= \frac{c}{\lambda} \\
 \text{red } f &= \frac{3.0 \times 10^8}{680 \times 10^{-9}} \\
 &= 4.4 \times 10^{14} \text{ Hz} \\
 \text{orange } f &= \frac{3.0 \times 10^8}{580 \times 10^{-9}} \\
 &= 5.2 \times 10^{14} \text{ Hz} \\
 \text{green } f &= \frac{3.0 \times 10^8}{500 \times 10^{-9}} \\
 &= 6.0 \times 10^{14} \text{ Hz}
 \end{aligned}$$

$$\begin{aligned}
 E &= h.f \\
 \text{red } E &= 6.63 \times 10^{-34} \times 4.4 \times 10^{14} \\
 &= 2.9 \times 10^{-19} \text{ J} \\
 \text{orange } E &= 6.63 \times 10^{-34} \times 5.2 \times 10^{14} \\
 &= 3.4 \times 10^{-19} \text{ J} \\
 \text{green } E &= 6.63 \times 10^{-34} \times 6.0 \times 10^{14} \\
 &= 4.0 \times 10^{-19} \text{ J}
 \end{aligned}$$

3

$$E_{av}(X\text{-rays}) = 1 \times 10^4 \text{ eV}$$

$$E_{av}(\gamma\text{-rays}) = 1 \times 10^7 \text{ eV}$$

$$\frac{E(X\text{-ray})}{E(\gamma\text{-ray})} = \frac{h \cdot f(X\text{-ray})}{h \cdot f(\gamma\text{-ray})}$$

$$\frac{1 \times 10^4}{1 \times 10^7} = \frac{f(X\text{-ray})}{f(\gamma\text{-ray})}$$

$$\text{ratio of frequencies} = 1 \times 10^{-3}:1$$

$$\frac{c(X\text{-ray})}{c(\gamma\text{-ray})} = \frac{\lambda(X\text{-ray}) \cdot f(X\text{-ray})}{\lambda(\gamma\text{-ray}) \cdot f(\gamma\text{-ray})}$$

$$1 = \frac{\lambda(X\text{-ray})}{\lambda(\gamma\text{-ray})} \times 1 \times 10^{-3}$$

$$\frac{\lambda(X\text{-ray})}{\lambda(\gamma\text{-ray})} = 1 \times 10^3$$

$$\text{ratio of wavelengths} = 1 \times 10^3:1$$

4

$$P = 1.0 \text{ W}$$

$$c = 3.0 \times 10^8 \text{ ms}^{-1}$$

$$h = 6.63 \times 10^{-34} \text{ Js}$$

$$\lambda = 694 \text{ nm} = 694 \times 10^{-9} \text{ m}$$

a 694nm is a 'red' wavelength

b

$$E = h \cdot f$$

$$\text{and } c = \lambda \cdot f$$

$$E = \frac{h \cdot c}{\lambda}$$

$$= \frac{6.63 \times 10^{-34} \times 3.00 \times 10^8}{694 \times 10^{-9}}$$

$$E = 2.87 \times 10^{-19} \text{ J / photon}$$

c

$$A = 10 \text{ mm}^2 = 10 \times 10^{-6} \text{ m}^2$$

$$I = \frac{P}{A}$$

$$= \frac{1.0}{10 \times 10^{-6}}$$

$$I = 1 \times 10^5 \text{ Wm}^{-2}$$

$$\text{d } I(\text{sunlight}) = 1000 \text{ Wm}^{-2}$$

$$\frac{I(\text{laser})}{I(\text{sunlight})} = \frac{1 \times 10^5}{1000}$$

$$= 100$$

The laser beam is 100 times more intense than sunlight.

$$\begin{aligned}
 5 \quad P &= 750\text{W (output power)} \\
 &= 750\text{Js}^{-1} \\
 E (\text{photon}) &= 1.0 \times 10^{-23}\text{J} \\
 t &= 1.0\text{s}
 \end{aligned}$$

$$\begin{aligned}
 P &= \frac{E}{t} \\
 E &= P.t \\
 &= 750 \times 1 \\
 &= 750\text{J}
 \end{aligned}$$

$$\begin{aligned}
 \text{Number of photons} &= \frac{750\text{J}}{1.0 \times 10^{-23}\text{J/photon}} \\
 &= 7.5 \times 10^{25} \text{ photons}
 \end{aligned}$$

$$\begin{aligned}
 6 \quad \lambda &= 6.0 \times 10^{-7}\text{m} \\
 P &= 1.7 \times 10^{-8}\text{W} = 1.7 \times 10^{-8}\text{Js}^{-1} \\
 c &= 3.0 \times 10^8\text{ms}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 P &= \frac{E}{t} \\
 E &= P.t \\
 &= 1.7 \times 10^{-8} \times 1 \\
 &= 1.7 \times 10^{-8}\text{J (per second)}
 \end{aligned}$$

$$\begin{aligned}
 E &= h.f \\
 \text{and } c &= \lambda.f \\
 \therefore E &= \frac{h.c}{\lambda} \\
 &= \frac{6.63 \times 10^{-34} \times 3.00 \times 10^8}{6.0 \times 10^{-7}}
 \end{aligned}$$

$$\text{photon energy} = 3.3 \times 10^{-19}\text{J}$$

$$\begin{aligned}
 \text{photons / second} &= \frac{\text{energy / second}}{\text{energy / photon}} \\
 &= \frac{1.7 \times 10^{-8}}{3.3 \times 10^{-19}}
 \end{aligned}$$

$$\text{photons / second} = 5.1 \times 10^{10}$$

$$\begin{aligned}
 7 \quad P &= 50\text{kW} = 50 \times 10^3\text{W} \\
 f &= 720\text{kHz} = 720 \times 10^3\text{Hz} \\
 c &= 3.0 \times 10^8\text{ms}^{-1}
 \end{aligned}$$

$$\begin{aligned}
 a \quad c &= \lambda.f \\
 \lambda &= \frac{c}{f} \\
 &= \frac{3.0 \times 10^8}{720 \times 10^3} \\
 \lambda &= 4.2 \times 10^2\text{m}
 \end{aligned}$$

$$\begin{aligned}
 \mathbf{b} \quad t &= 1 \text{ day} \\
 &= 8.64 \times 10^4 \text{ s} \\
 P &= \frac{E}{t} \\
 E &= P \cdot t \\
 &= 50 \times 10^3 \times 8.64 \times 10^4 \\
 E &= 4.3 \times 10^9 \text{ J}
 \end{aligned}$$

- 8 Graph (a) - shows absorption of the short wavelengths, blue and violet, but transmission of the long wavelengths, i.e. red. Therefore, this is red filter.
- Graph (b) - shows transmission of both blue and red, but absorption of the middle frequencies. This is a purple filter.
- Graph (c) - shows maximum transmission at 500nm, and as this is the frequency of green light, this is the green filter.

9. Some of the following is from http://en.wikipedia.org/wiki/Blue_shift

Blue shift is the shortening of a transmitted signal's wavelength, and/or an increase in its frequency, due to the Doppler Effect, which indicates that the object is moving toward the observer. The name comes from the fact that the shorter-wavelength end of the optical spectrum is the blue (or violet) end, hence, when visible light is compacted in wavelength, it is shifted towards the "blue" end of the spectrum. Since the longer-wavelength end of the visible electromagnetic spectrum is *red*, the opposite effect, of a lengthening of a signal's wavelength, is referred to as redshifting.

While the terms "redshifting" and "blueshifting" imply significantly redder or bluer light, only the most distant galaxies and those moving at speeds far above average emit light that arrives with perceptible red or blue tinges. For the most part, shifting is not a visible phenomenon.

These terms and conventions ("blue" = compaction, "red"= diffusing) are used even when referring to signals outside the optical range (for instance, radio waves, x-rays and gamma rays).

If the universe is expanding then the stars, etc are moving further away so they would have longer wavelengths and have a red shift. As this is the case with most of the celestial objects we look at, it is suggested that our universe is expanding so blue shift will not occur in an expanding universe.

10. While not in the course, Hubble's constant is $v = H_0 D$ or $H_0 = \frac{v}{D}$ where v = is the velocity of the celestial object and D is the distance to the celestial object. The most recent value is suggested to be $H_0 = 70.6 \pm 3.1$ (km/sec)/Mpc although it has been as high as $500 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

Now to the question.

From the line of best fit on the graph (very rough) for $v = 10\,000 \text{ km s}^{-1}$, $D = \text{about } 17 \text{ Mpc}$

$$H_0 = \frac{v}{D} = \frac{10000}{17} = 588 \text{ km s}^{-1} \text{ Mpc}^{-1}.$$

No answer is given in Exploring Physics at the moment so I don't know if this is what they are looking for but the value seems to be too high.