



Semester One Examination, 2019

Question/Answer booklet

**MATHEMATICS
METHODS
UNIT 3**
Section Two:
Calculator-assumed

If required by your examination administrator, please place your student identification label in this box

Student number: In figures

<input type="text"/>	<input type="text"/>	<input type="text"/>	<input type="text"/>
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In words

Your name _____

Time allowed for this section

Reading time before commencing work: ten minutes
Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor
This Question/Answer booklet
Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters
Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,
and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total					100

Supplementary page

Question number: _____

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
- You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allowed any marks. For any question or part question with more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for continuing/continuing your answer(s) are provided at the end of the Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only		
Question	Maximum	Mark
9	5	
10	8	
11	7	
12	5	
13	8	
14	12	
15	7	
16	7	
17	9	
18	9	
19	7	
20	7	
21	7	
S2 Total	98	
S2 Wt (=0.6633)	65%	

An aquarium, with a volume of $50\ 000\ \text{cm}^3$, takes the shape of a rectangular prism with square ends of side $x\ \text{cm}$ and no top. The glass for the four vertical sides costs $0.05\ \text{cents per square cm}$ and for the base costs $0.08\ \text{cents per square cm}$. The cost of glue to join the edges of two adjacent pieces of glass is $0.6\ \text{cents per cm}$. Assume the glass has negligible thickness and ignore any other costs.

- (a) Show that $C = \frac{x^2}{1000} + \frac{9x}{250} + \frac{90}{x^2} + \frac{600}{x}$, where C is the cost, in dollars, to make the aquarium. (4 marks)

CALCULATOR-ASSUMED

METHODS UNIT 3

Question 11

- X is a uniform discrete random variable where $x=1,2,4,8,12$.

(ii) $P[X > 7 | X \geq 2]$.

(b) Calculate the exact value of

(i) $E(X)$

- (b) Show use of a calculus method to determine the minimum cost of making the aquarium.
(3 marks)

(ii) $\text{Var}(X)$. (2 marks)

These features are summarized in Fig. 11(a) for the three cases (a), (b) and (c) corresponding to the following two situations: (i) the case where the features are extracted from the original image, and (ii) the case where the features are extracted from the denoised image.

Key features: *...the first three main characteristics of the system are the same as in the original version, but the fourth one is different.*

(a) Determine the probability that the team scores at least one goal in a match. (2 marks)

$p(X=x) = \frac{e^{-x}}{x!} x^x$ for $x=0, 1, 2, 3, \dots$ to infinity

The random variable X is the number of goals scored by a team in a soccer match, where

(d) Complete the probability distribution table for X .	<table border="1"> <thead> <tr> <th>Goals scored</th><th>$x=0$</th><th>$x=1$</th><th>$2 \leq x \leq 3$</th><th>$x \geq 4$</th><th>$P(X=x)$</th><th>μ</th></tr> </thead> <tbody> <tr> <td>$y(\\$)$</td><td>0</td><td></td><td></td><td></td><td>0.1806</td><td></td></tr> <tr> <td>Goals scored</td><td></td><td></td><td></td><td></td><td>500</td><td></td></tr> </tbody> </table> <p>(3 marks)</p>	Goals scored	$x=0$	$x=1$	$2 \leq x \leq 3$	$x \geq 4$	$P(X=x)$	μ	$y(\$)$	0				0.1806		Goals scored					500	
Goals scored	$x=0$	$x=1$	$2 \leq x \leq 3$	$x \geq 4$	$P(X=x)$	μ																
$y(\$)$	0				0.1806																	
Goals scored					500																	

