Semester 2 (Units 3 and 4) Examination, 2017 **Question/Answer Booklet**

MATHEMATICS METHODS

Section One:	Calculator-free
Student Name/Number:	
Teacher Name:	
Time allowed for th	nis section

Reading time before commencing work: five minutes Working time for this section: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor: This Question/Answer Booklet

Formula Sheet

To be provided by the candidate:

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section Number of questions available		Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam	
Section One: Calculator-free	9	9	50	52	35	
Section Two: Calculator-assumed	1 13 1		100	99	65	
					100	

Instructions to candidates

1.	The rules for the conduct of School exams are detailed in the
	School/College assessment policy
	Sitting this examination implies that you agree to abide by these rules.

- 2. Write your answers in this Question/Answer Booklet.
- 3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
- 5. **Show all working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

Section One: Calculator-free

(53 Marks) Weighting 35%

This section has **9 (nine)** questions. Answer **all** questions. Write your answers in the spaces provided.

Suggested working time: 50 minutes.

Question 1 (6 marks)

(a) A random variable, G, has the following probability distribution.

Find the value of the constant k

(1 mark)

g	1	2	3	4	5
Pr(G = g)	k	2 <i>k</i>	0.5 <i>k</i>	0.5k	k

(b) State, with reason(s), whether distribution. $p(x) = \frac{1}{6}(4-x), x \in [0,1,5]$ is a discrete probability (2 marks)

n and p

(c) For a Binomial distribution with parameters p, the mean is 90 and the standard p deviation is 6. Determine . (3 marks)

Quest	ion 2	(4 marks)
(a)	State what you understand by a census.	(1 mark)
Applia	stove produced by AK Appliances is stamped with a unique serial number. Ances produces stoves in batches of 2000. Before selling them, they test a rele of 5 to see what electric current overload they will take before breaking do	andom wn.
	census.	(1 mark)
(c)	Suggest a suitable method to obtain this sample.	(1 mark)
(d)	Identify the units to be sampled using this method.	(1 mark)

(a) Determine the derivative f'(x) given that

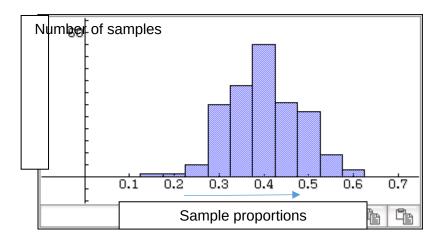
$$f(x) = \frac{x}{2 + \cos x}$$
 (2 marks)

(ii)
$$f(x) = e^{3x + \sin 2x}$$
 (2 marks)

(b) If
$$f'(x) f(x) = 1$$
 show that $f''(x) [f(x)]^3 = -1$. (3 marks)

Question 4 (5 marks)

(a) A number of sample proportions (\hat{p}) each of the same size (50) gave rise to the graph shown below.



(i) Approximately, how many samples were involved

(1 mark)

(ii) Estimate p, the population proportion.

(2 marks)

(b) A local radio station carries out regular polls of its listeners on items of current interest. In one such poll, listeners were asked to telephone the station and just answer yes or no to the following question:

Should the AFL introduce the red card send-off rule into all games?

The poll was carried out between 8:00 am and 9:00 am one morning.

Give two problems associated with this method of sampling and suggest why each problem might cause misleading conclusions to be drawn. (2 marks)

Question 5 (4 marks)

Determine
$$\int \left(\frac{10x}{1-4x^2} \right) dx$$

Question 6 (5 marks)

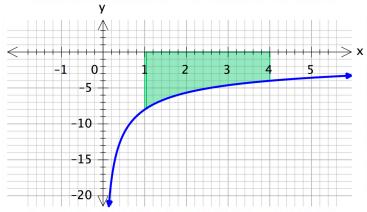
(a) Express y in terms of x given that $\log_s(x + 24y) - 2 = \log_s(x + y)$. (2 marks)

- (b) Suppose that a and b are positive real numbers.
 - (i) What is sign of $\log_a b$ if a > b? (1 mark)

(ii) Deduce that a = b if $\log_a b = \log_b a$ (2 marks)

Question 7

The graph of the function $f(x) = \frac{-8}{\sqrt{x}}$, where x > 0 is shown below. The shaded region is between the graph and the x- axis from units x = 1 to x = 4.



(a) Write down an expression for the area of the shaded region shown on the graph above. (1 mark)

(b) Evaluate the area of the shaded region.

(2 marks)

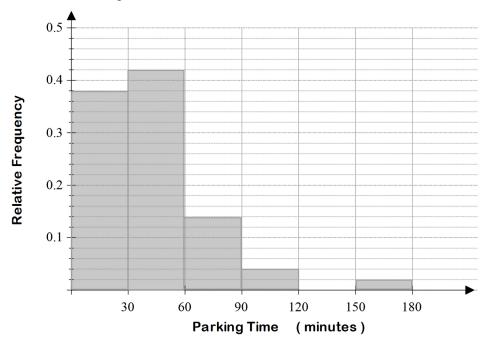
$$\int \left(-\frac{8}{\sqrt{x}}\right) dx = -25$$
 (c) Given , where $a > 1$, determine the exact value of a . (2 marks)

Question 8 (9 marks)

(a) Let X be a continuous random variable whose probability density function is $f(x) = \frac{1}{4}x^3$ for an interval 0 < x < c. What is the value of the constant c that makes f(x) a valid probability density function? Clearly show all working. (3 marks)

(b) Consider the probability density function $w(x) = \frac{1}{20}$ where $12 \le x \le 32$ and w(x) = 0 otherwise. Using integration, determine the expected value of w(x). (2 marks)

(c) 200 vehicles were parked in a parking lot during a 3 hour period. The recorded data is shown on the histogram drawn below.

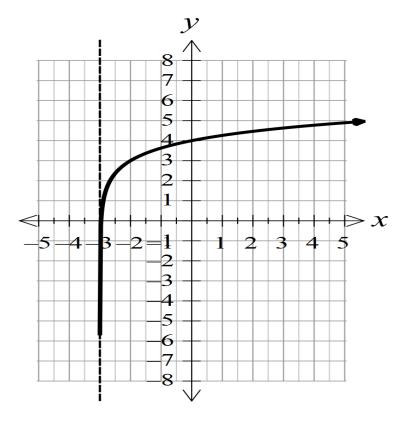


Use this data to answer the following:

- (i) Determine the probability that a randomly selected vehicle was parked for at most 60 minutes. (1 mark)
- (ii) State the number of vehicles that were parked for between 1 and 1.5hrs. (1 mark)
- (iii) Where might you assume that this parking lot was located? Justify your answer. (1 mark)
- (iv) As a statistician, you need to analyse and inquire about data to draw conclusions and make suggestions. Different to (c), what is a question you could ask to help understand if there is a bias in collecting this data? (1 mark)

Question 9 (7 marks)

The graph of $y = \log_a(x+b) + c$, where a, b and c are positive integers, is shown below:



(a) Use the graph to determine the values of a, b and c. (3 marks)

(b) Sketch on the same axes the graph of $y = 3 - \log_2(4 - x)$. Make sure that you show the intercepts on the two axes accurately. (4 marks)

CALCULATOR-FREE SEMESTER 2 (UNITS 3 AND 4) EXAMINATION End of Questions

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Additional working space	
Question number:	

Acknowledgements

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