Майнетайсь Дерагитепт Ретіл Модет Ретіл Модет Ретіл Модет

## Working out space

## Exceptional schooling. Exceptional students. Independent Public School Organical Students.

## Course 12 Methods(Test 2 alternative) Year 12

Formula sheet provided: Yes	
Task weighting:12%	
Marks available: ——46 — marks	
	ents, templates, notes on one unfolded sheet of to three calculators approved for use in the WACE
	preferred), pencils (including coloured), sharpener, ape, eraser, ruler, highlighters
Materials required: Calculator with CAS	AS capability (to be provided by the student)
Number of questions:	
Time allowed for this task:45 said:	
Task type: Response	
Student name:	Teacher name:

Note: All part questions worth more than 2 marks require working to obtain full marks.

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Working out space

Q1 (3.2.1-3.2.3)

(3 & 3 =6 marks)

Determine y in terms of x for the following.

(a) 
$$\frac{dy}{dx} = 5x^3 - 4x^2 + 7x + 1$$
 given that  $y = 10, x = 1$ .

(b) 
$$\frac{dy}{dx} = 5x^2 \sqrt{6 + 2x^3}$$
 given that  $y = 1, x = -1$ .

Q2 (3.2.21-3.2.22)

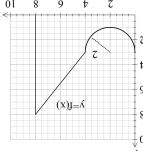
(4 marks)

An object is moving in a straight line such that its velocity m/s as a function time, t seconds, is given by  $v = 5t^2 + pt + 1$  where p is a constant. The acceleration at time t = 3 seconds is  $10m/s^2$  and is initially at the origin. Determine the displacement when t = 6 seconds.

(3 & 4 = 7 marks)

(3.2.10-3.2.11)

Consider the function  $\int (\chi)^{1/2}$  which is graphed for  $0 \le \chi \le 8$  . The arc has a radius of 2 units.



(a) Determine the exact value of  $^{\circ}$ xp(x)  $\iint_{8}$ 

(b) Determine  $\alpha$  to two decimal places such that  $\int_{0}^{\pi} \int_{0}^{\pi} \int_{0$ 

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(4 marks) (3.1.4) 8О

grams. Determine the time taken for half the mass to decay(half-life) and the value of  $^{\!\!\!\!/}$  to three  $NA = \frac{Nb}{1b} \quad \text{of grains and decays according to RZS initially has a mass of 230 grains and decays according to the mass at time $t$ minutes and $t$ in the result of the mass at time $t$ minutes and $t$ in the result of the mass at time $t$ in the result of the$ 

(2 & 4 =6 marks)

(3.2.6)

(b) Using your result from part (a) and **without using your classpad** determine  $\int \frac{x}{\sqrt{5-2x}} dx$ 

(3.2.18 - 3.2.17)

(3 & 2 = 5 marks)

A water tank has a leak and the volume of water contained, V, can be described by the following

$$\frac{dV}{dt} = -\frac{500t^2}{(2x+3)^4}$$

differential equation at time, t minutes,

of Water Co....  $\frac{dV}{dt} = -\frac{500t^2}{\left(2+t^3\right)^4}$ . The tank is initially full but is emptied in 15

- (a) Determine the initial volume of water in the tank.
- (b) Determine the change in volume in the third minute.

(3.2.11 - 3.2.14)

(2, 2 & 2 = 6 marks)

Consider a function f(x) that is defined for  $0 \le x \le 13$  with the following conditions.

$$f(3)=9$$
,  $f(10)=3$ 

$$f(0) = 0 = f(5) = f(8) = f(13)$$

With  $f(x) \ge 0$  for  $0 \le x \le 5$  &  $8 \le x \le 13$  and  $f(x) \le 0$  for  $5 \le x \le 8$ .

$$\int_{0}^{3} f(x) dx = 7$$
,  $\int_{0}^{5} f(x) dx = 12$ 

- (a) Determine  $\int_{a}^{a} f'(x) dx$ .
- (b) Determine  $\int_{a}^{8} f(x) dx$  given that  $\int_{a}^{15} f(x) dx = 6$ .
- (c) Determine  $\frac{d}{dx} \int_{a}^{x} f(t) dt$  when x = 10.

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Determine to two decimal places the area between the curves  $y = x^2 + 6x + 2$  and  $y = -x^2 - 7x + 5$ . (Hint- Sketch the curves first on your classpad)

Q7 (3.2.16) (1 & 3 = 4 marks) Consider 
$$y = \int_{-\infty}^{x} f(t) dt$$

a) In terms of f, express  $\frac{dx^2}{dx^2}$ .

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b) If f''(x) = 3x + 1 and f'(0) = 0 = f(0), determine y in terms of x only.