

Semester Two Examination, 2022

Question/Answer booklet

MATHEMATICS SPECIALIST UNITs 3 & 4

Section Two: Calculator-assumed

Your Name

Your Teacher's Name

Time allowed for this section

Reading time before commencing work: ten minutes

Working time:

Materials required/recommended for this section

To be provided by the supervisor This Question/Answer booklet

Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material. If you have any unauthorised material.

hand it to the supervisor before reading any further.

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Max	Marks	Question	Max	Marks	Question

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Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	49	34
Section Two: Calculator-assumed	11	11	100	97	66
<u> </u>				Total	100

Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR
 course examinations are detailed in the Year 12 Information Handbook 2016. Sitting this
 examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

(97 Marks) Section Two: Calculator-assumed

and/or as additional space if required to continue an answer. Spare pages are included at the end of this booklet. They can be used for planning your responses This section has 11 questions. Answer all questions. Write your answers in the spaces provided.

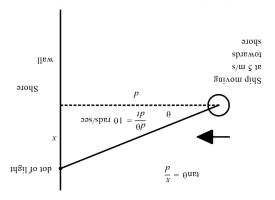
- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- snawer space where the answer is continued, i.e. give the page number. Fill in the number of the • Continuing an answer: If you need to use the space to continue an answer, indicate in the original

question that you are continuing to answer at the top of the page.

Working time: 100 minutes.

(e marks) Question 9

metres from point directly opposite ship on shore, x = 3 m. Answer to 2 decimal places in the speed of the dot when the ship is 50 m from shore, b = 50 m and the dot of light 3 at10 rads/sec. This light causes a dot of light to move along the wall on the shore. Determine Consider a ship moving towards the shore at 5m/s with a revolving light on the roof rotating



Solution

$$\theta \operatorname{min} b = x$$

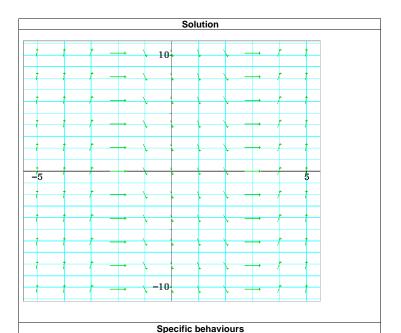
$$2 - 01\left(\frac{9}{0022} + 1\right) = 5 - 01\left(\frac{9}{0002} + 1\right) = 5 - 01 \left(\frac{9}{0002} + 1\right) = 5 - 01 \left(\frac{9}$$

Specific behaviours

- √ nses broduct rule
- √ uses value of secant \checkmark uses negative rate for distance of boat from shore
- √ uses rate of angle (+/- both accepted)
- √ obtains an expression for speed
- $\sqrt{\text{old} \hat{\theta} \text{ besu } \text{li } 01.20\text{d}}$ db Δ of beeds setsite.

Question 10 (8 marks)

a) On the axes below, sketch the slope field for $\frac{dy}{dx} = (x+2)(x-3)$ (3 marks)



- ✓ shows horizontal lines at x=-2&3
- √ shows negative lines on y axis
- ✓ shows steep positive lines at x=-10&10

Specific behaviours

- ✓ separates dv and dx and writes integral
- √ solves for constant
- ✓ solves for x when v=0 and simplifies
- c) Show that the train stops when $t = \frac{1}{\sqrt{ab}} \tan^{-1} \left(\frac{\sqrt{b}}{\sqrt{a}} u \right)$ (3 marks)

(Hint- use the substitution $v = \sqrt{\frac{a}{b}} \tan \theta$)

Solution $\frac{dv}{dt} = -(a+bv^2)$ $\int \frac{dv}{(a+bv^2)} = \int -dt$ $\int \frac{1}{(a+bv^2)} \frac{dv}{d\theta} d\theta = \int \frac{1}{(a+a\tan^2\theta)} \sqrt{\frac{a}{b}} \sec^2\theta d\theta = \int \frac{1}{\sqrt{ab}} d\theta = -t + c$ $\frac{\theta}{\sqrt{ab}} = -t + c$ $\frac{1}{\sqrt{ab}} \tan^{-1} \left(\sqrt{\frac{b}{a}}v\right) = -t + c$ v = u, t = 0 $c = \frac{1}{\sqrt{ab}} \tan^{-1} \left(\sqrt{\frac{b}{a}}u\right)$ $t = \frac{1}{\sqrt{ab}} \tan^{-1} \left(\sqrt{\frac{b}{a}}u\right)$ v = 0

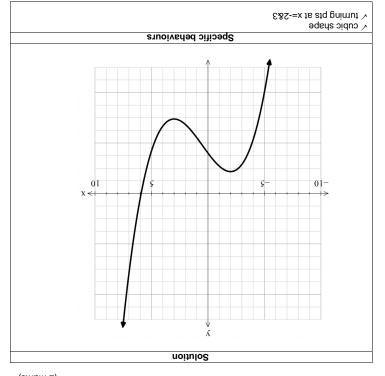
Specific behaviours

- ✓ changes variable to angle OR determines $\frac{dv}{d\theta}$
- √ simplifies integral

 $t = \frac{1}{\sqrt{ab}} \tan^{-1} \left(\sqrt{\frac{b}{a}} u \right)$

✓ solves for t when v=0

b) On the axes above, sketch the solution curve that passes through the point (6.2) (2 marks)



c) Determine the Cartesian equation of the curve for part (b) above.

Solution

Solution $y' = x^2 - x - 6$ $y = x^3 - \frac{x^2}{2} - 6x + 6$ (6,2) c = -16 $y = \frac{x^3}{3} - \frac{x^2}{2} - 6x - 16$ Specific behaviours

A adds a constant wing (6,2)

Solutes for constant using (6,2)

9

Question 19

(9 marks)

Consider a train that suddenly brakes causing a deceleration of $(a+bv^2)$ metres per second squared, where v equals its velocity. (Note: a,b>0)

a) Show that $\frac{dv}{dx}=-\frac{(a+bv^2)}{v}$, where x is the distance travelled from when the brakes are first applied. (3 marks)

Solution
$$\frac{dv}{dt} = -\left(a + bv^2\right)$$

$$\frac{dv}{dx} = -\left(a + bv^2\right)$$

$$\frac{dv}{dx} = -\frac{av}{v} + \frac{dv}{dx}$$
 for acceleration
$$\frac{dv}{dx} = \frac{dv}{dx}$$

b) If u is the velocity of the train when the brakes are first applied, show that the train comes to rest when $x = \frac{1}{2b} \ln \left(1 + \frac{bu^2}{a} \right)$. (3 marks)

noinios $\frac{d}{dt} = x$ $\frac{d}{dt} =$

Question 11 (8 marks)

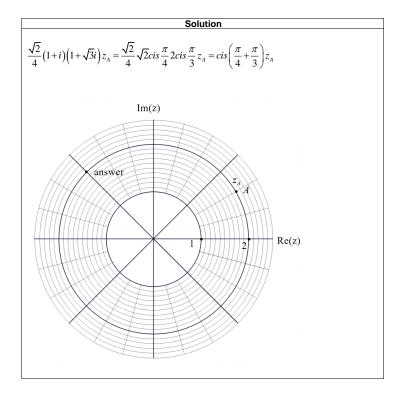
Consider the point A , z_4 plotted on the Argand plane below.

a) Determine the polar form of point A, z_A

	Solution	
$z = 2cis\frac{\pi}{6}$		
6		
	0	
	Specific behaviours	
✓ modulus		
✓ argument		
_		

(2 marks)

b) Plot the following value on the diagram above $\frac{\sqrt{2}}{4}(1+i)(1+\sqrt{3}i)z_A$ (3 marks)

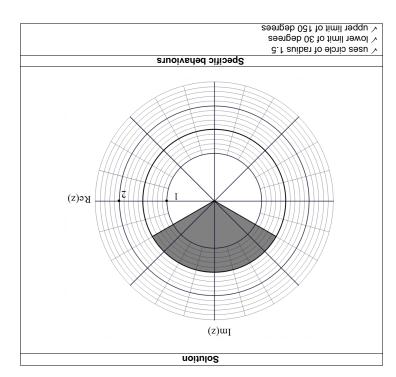


Specific behaviours

- √ differentiates in terms of angle
- √ equates to zero
- √ gives one possible value for angle
- √ gives positive area

$$\left\{\frac{\pi\lambda}{\delta} \ge \left(z\right)g^{-1}A \ge \frac{\pi}{\delta} : z\right\} \cap \left\{\lambda \cdot 1 \ge \left|z\right| : z\right\} : \text{sovods saxs ant no noigh equation}$$
 (a)

(3 marks)



Z

 $1 = \frac{x}{4} + \frac{x}{2n}$ $0 = \frac{x}{4} + \frac{x}{2n}$ $0 = \frac{x}{4} + \frac{x}{2n}$ $\frac{x}{4} + \frac{x}{2n}$ $\frac{x}{4n} + \frac{x}{2n}$

b) Determine the values of ϑ for which the area of triangle OMN is a minimum and state this minimum area in terms of a & b.

$$\frac{dn}{\theta \sin x} = A$$

$$\theta \cos x \cos x^{2} - (\theta \sin x) dx - \frac{h}{\theta x}$$

$$0 = \theta \cos x$$

$$\pi n \cos x + \frac{\pi}{x} = \theta \cos x$$

$$\frac{\pi}{x} > \theta > 0 \sec \frac{\pi}{x} = \theta$$

$$dn = A$$

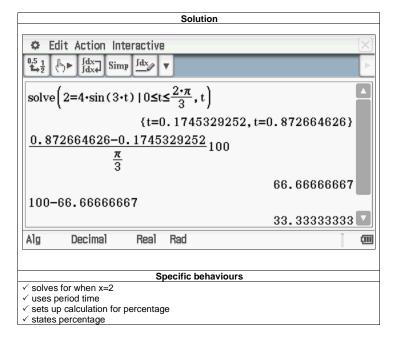
Question 12 (10 marks)

An object is moving along a straight line such that $\ddot{x} = -9x$ where x, metres is the displacement from the origin. The maximum speed and the initial speed are both 12 m/s.

a) Determine an expression for x at time t seconds. (2 marks)

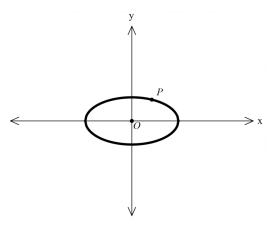
ſ	Solution
	$\ddot{x} = -9x$
	n = 3
	12 = nA = 3A
	A = 4
	$x = 4\sin 3t$
Į	
l	Specific behaviours
	√ value of n
	✓ Amplitude
ı	

 b) Determine the percentage of time in the long run that the object is no more than 2 metres from the origin. (4 marks)



Question 18 (8 marks)

An ellipse has equation $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.(Note: a, b > 0) The tangent at a point $P(a\cos\theta, b\sin\theta)$ with $0 < \theta < \frac{\pi}{2}$, intersects the x and y axes at Points M & N respectively. The origin is at O.



21

a) Determine the area of triangle OMN in terms of $a,b \& \theta$. (4 marks) Note: Diagram is not drawn to scale.

ı	Solution
l	Solution
ı	

c) Determine the speed and acceleration when the object is 1.5 metres from the origin.

Solution

$$(^{2}S.I - \partial I)\theta = (^{2}X - ^{2}A)^{2}n = ^{2}V$$
$$s \setminus m\Omega I.II = \overline{ST.S\Omega I}V = V$$

$$(c.61+)$$
 $roc.61-=(c.1)$ $e-=\ddot{x}$

$$(c;c) \rightarrow (c;c) = (c;i) \leftarrow -\infty$$

✓ uses correct formula for speed and shows calculation Specific behaviours

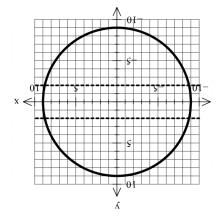
 $\boldsymbol{\vee}$ uses correct formula for acceleration and shows calculation √ states approx. speed

√ states acceleration

(4 marks)

(2 marks) Question 13

Consider a solid sphere of radius 9 metres with a cross-section as shown below.



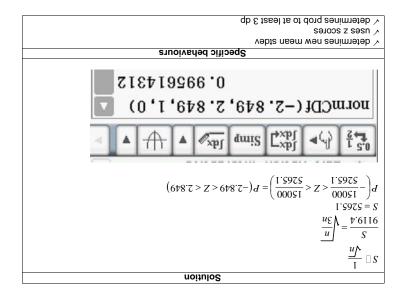
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sphere, determine the volume of the sphere remaining. If a hollow cylinder of radius 2 metres, is drilled completely through the middle of the solid

mean that differs from $\it u$ by no more than \$15 000?

d) What is the probability to 3 dp that another sample size of 3n would give a sample

(3 marks)



(3 marks) increase or decrease. e) In each of the scenarios below, state whether the confidence interval width would

Sample size trebled.

(ii Confidence changed to 95%.

(iii Sample standard deviation decreased.

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Specific behaviours	
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ocrease	ıl (ii
ecrease	J (i
Solution	

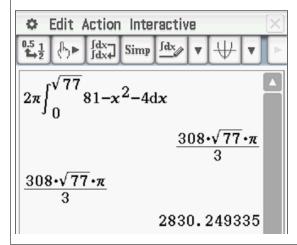
$$y = 2$$

$$x^2 = 77$$

$$x = \pm \sqrt{77}$$

 $x^2 + y^2 = 81$

$$V = 2\pi \int_{0}^{\sqrt{77}} 81 - x^2 - 4 dx$$



Specific behaviours

- √ determines where y=2 intersects with circle
- √ uses a revolution around an axis
- ✓ sets up rule for integral
- √ uses appropriate limits on integral
- ✓ states volume (no need for units)

Full marks awarded if used the following method correctly

$$V = 2\pi \int_{2}^{9} y \sqrt{9^2 - y^2} dy$$

Question 17 (12 marks)

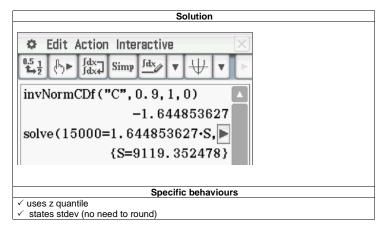
In order to estimate the mean amount of superannuation for workers in Perth, u, a sample of n workers were chosen with a sample mean of \$90 000 and a sample standard deviation of s and a 90% confidence interval width of \$30 000.

a) State the 90% confidence interval.

(1 mark)

(2 marks)

b) Determine the sample mean standard deviation.



c) In terms of n , what sample size would give a 90% confidence interval of width of \$10 000? (3 marks)

	Solution
$W \square \frac{1}{\sqrt{n}}$	
$\frac{10000}{30000} = \sqrt{\frac{n}{n_{new}}}$	
$n_{new} = 9n$	
	Specific behaviours
√ uses inverse ratio	
✓ uses square of width ratio	
✓ states new size in terms of n	

Question 14 (9 marks)

a) Solve the following system of equations showing full working.

$$Z = 2S + \sqrt{S} - xS$$

$$Z = 2S + \sqrt{S} - xS$$

$$S = 2S + \sqrt{S} - xS$$

(3 marks)

$$\begin{bmatrix} 1 & 2 & 3 & 2 \\ 2 & -3 & 5 & -7 \\ 3 & -5 & 5 \\ \end{bmatrix}$$

$$\begin{bmatrix} 2 & -3 & 5 & -7 \\ 3 & -5 & 5 \\ \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 & 2 \\ 0 & 11 & 1 & 7 \\ 0 & 11 & 7 & 1 \\ 0 & 11 & 7 & 1 \\ \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 & 2 \\ 0 & 11 & 7 & 1 \\ 0 & 38 & 0 & 76 \\ \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 & 2 \\ 0 & 38 & 0 & 76 \\ \end{bmatrix}$$

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$$\begin{bmatrix} 2 & 2 & 2 & 2 \\ 0 & 38 & 0 & 76 \\ \end{bmatrix}$$

$$\begin{bmatrix} 2 & 2 & 2 & 2 \\ 0 & 38 & 2 \\ \end{bmatrix}$$

$$\begin{bmatrix} 2 & 2 & 2$$

b) Determine all possible values of $\,p\,\&\,q\,$ such the below system has:

$$c = 2b + \sqrt{c} - xc$$

$$c = 2b + \sqrt{c} - xc$$

$$d = 2c + \sqrt{c} - xc$$

Unique solution anoitulos etiniful

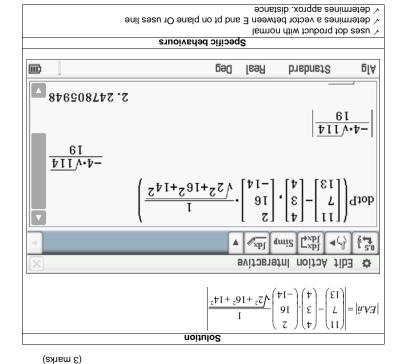
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(i

Solution

11

d) Given E(11,7,13) , determine the distance of pt $\,E\,$ to the plane containing B



$$\begin{bmatrix} 1 & 2 & q & 2 \\ 2 & -3 & 5 & p \\ 3 & -5 & 2 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & q & 2 \\ 0 & 7 & 2q - 5 & 4 - p \\ 0 & 11 & 3q - 2 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & q & 2 \\ 0 & 7 & 2q - 5 & 4 - p \\ 0 & 0 & q - 41 & 37 - 11p \end{bmatrix}$$

$$unique: q \neq 41$$

$$inf inite: q = 41 \& p = \frac{37}{11}$$

$$no so ln: q = 41 \& p \neq \frac{37}{11}$$
Specific behaviours
$$\checkmark \text{ sets up equation with two coefficients in terms of p&q}$$

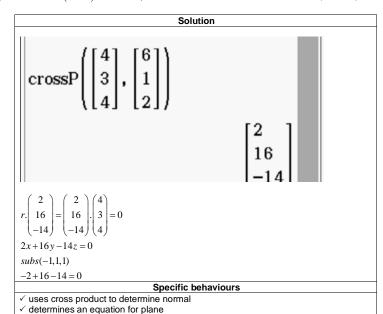
solves for infinite & no solutions
 For the values of p & q that give infinite solutions in (bii) above, determine the vector equation of the line of possible solutions. (3 marks)

✓ solves for unique values

0.1.0
Solution

b) Show that D(-1,1,1) lies in the plane OAB.

(3 marks)



c) Given that C(0,9,-6) show that the line CD is perpendicular to the plane OAB. (2 marks)

 $CD = \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix} - \begin{pmatrix} 0 \\ 9 \\ -6 \end{pmatrix} = \begin{pmatrix} -1 \\ -8 \\ 7 \end{pmatrix} = -\frac{1}{2} \begin{pmatrix} 2 \\ 16 \\ -14 \end{pmatrix}$

Specific behaviours

✓ subs point to show is on plane

√ determines CD

✓ shows that is a scalar multiple of normal hence perpendicular to plane

$$\begin{pmatrix}
I \\
II - \\
6I -
\end{pmatrix} I + \begin{pmatrix}
0 \\
II \\
II \\
III \\
III - II \\
III - II \\
III - III = X$$

$$S = IZ + (III - III / II)S - XE$$

$$S = IZ + (III - III / II)S - XE$$

$$S = IZ + (III - III / II)S - XE$$

$$III - III = X$$

Specific behaviours

- \checkmark expresses two variables in terms of common parameter for p&q values infinite
- √ expresses all 3 variables in terms of common parameter
- √ sets up a vector equation for line

13

✓ states that population mean does not fit in either interval √ shows working for at least one confidence interval √ determines at least one confidence intervals (SCSA would prefer two) Specific behaviours .os

X states that does not supports Aust but cannot assume UK

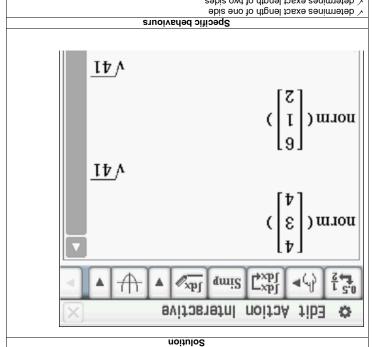
√

OR no inference can be made as not all intervals contain true value of pop mean

Question 16 (11 marks)

Consider the triangle OAB as with A(4,3,4) & B(6,1,2) and O as the origin.

(3 marks) a) Show that OAB is an isosceles triangle.

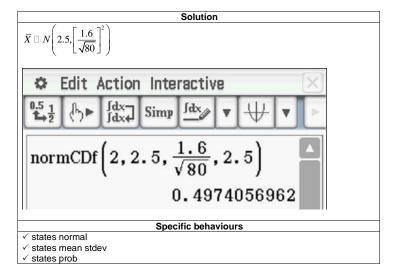


- √ determines exact length of two sides
- √ states that both are equal hence isosceles

Question 15 (11 marks)

It is found that for the entire population of Yr 12 students in Australia that the mean number for daily homework is 2.5 hours with a standard deviation of 1.6 hours. Samples of 80 students are taken and the students sampled are surveyed as to their daily homework hours.

 a) Determine the probability that the mean number of homework hours in a sample is between 2 and 2.5 hours.
 (3 marks)



Let T = sample mean of HW hours from samples of size 80 students.

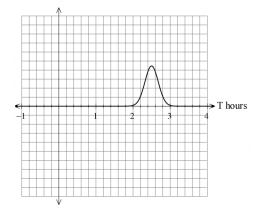
b) Define the probability distribution of T.

(2 marks)

$$\overline{X} \,\square\, \, N \Bigg(2.5, \left[\frac{1.6}{\sqrt{80}} \right]^2 \Bigg)$$
 Specific behaviours
$$\checkmark \, \, \text{states Normal with mean} \\ \checkmark \, \, \text{mean stdev}$$

c) Sketch the probability density function for *T* on the axes below.

(2 marks)



Solution

Specific behaviours

- ✓ Bell shape curve centred on T=2.5
- √ outer limits around 2 & 3 (3 stdevs)

Q15 continued

A sample of 100 Yr 12 students found that the mean number of HW hours is 2.0 hours with a sample standard deviation of 1.1 hours. It is suggested that this sample is from the United Kingdom.

d) Present an argument and necessary calculations to determine whether this suggestion is correct or not.

(4 marks)

Solution

99% confidence interval

$$2.0 \pm 2.576 \frac{1.1}{10}$$

1.71664-2.28336

95% confidence interval

1.7844-2.2156

The Aust population mean does not lie in either interval which would support the idea that this sample is not from Aust but we cannot suggest UK or any other named country.

OR

The two above intervals may not contain the true population p as not all intervals do