

# Examination, 2014 Western Australian Certificate of Education

## Question/Answer Booklet

(	1	)
	Ensure the label is straight and within the lines of this box.	
l	Place one of your candidate identification labels in this box.	

Calculator-assumed
Section Two:
3A/3B
<b>SOLIAMAHTAM</b>

Time allowed for this section Reading time before commencing work: Working time for section:		ninutes hundred minutes	Number of a answer book (if applicable	klets used	
in words	_				
Student Number: In figures					

## Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet (retained from Section One)

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

drawing instruments, templates, notes on two unfolded sheets of A4 paper, Special items:

and up to three calculators approved for use in the WACE examinations

## Important note to candidates

before reading any further. examination room. If you have any unauthorised material with you, hand it to the supervisor that you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be taken into the examination room. It is your responsibility to ensure

Copyright © School Curriculum and Standards Authority 2014



CANNINGTON WA 6107 303 Sevenoaks Street Published by the School Curriculum and Standards Authority of Western Australia

Any content in this document that has been derived from the Australian Curriculum may be used under the terms of the Creative

permission of the School Curroulum and Standards Authority. Copying or communication of any third party copyright material can be done only within the terms of the Copyright Act 1968 or with permission of the copyright owners.

This document – apart from any third party copyright material contained in it – may be freely copied, or communicated on an intrance, for non-commercial purposes in educational institutions, provided that it is not changed and that the School Cumculum and

Copying or communication for any other purpose can be done only within the terms of the Copyright Act 1968 or with prior written

Commons Attribution-NonCommercial 3.0 Australia licence.

Standards Authority is acknowledged as the copyright owner, and that the Authority's moral rights are not infringed.

2

#### CALCULATOR-ASSUMED

### Structure of this paper

0 "	Number of	Number of	Working	Marks	Percentage
Section	questions available	questions to be answered	time (minutes)	available	of exam
Section One: Calculator-free	7	7	50	50	331/3
Section Two: Calculator-assumed	12	12	100	100	662/3
				Total	100

#### Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2014. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in
    the original answer space where the answer is continued, i.e. give the page number.
     Fill in the number of the question that you are continuing to answer at the top of the
    page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

See next page

OFF
CUT
Ж
L WILL
ASI
AREA
THIS
Z
NRITE
NOT \
00

#### CALCULATOR-ASSUMED

23

MATHEMATICS 3A/3B

	working	

Question number: \_\_\_\_\_

(3 marks) (b) Prove that  $(3n+1)^2 - (3n-1)^2$  is a multiple of six for all positive integer values of n. (2 marks) Was Adam's conjecture true? If not, state a value of  $\boldsymbol{x}$  for which the conjecture is false. for  $1 \le x \le 9$ , where x is an integer. Adam made the conjecture that the function  $f(x) = x^2 - 3x + 7$  generated prime numbers (2 marks) 8 noiteauD Working time: 100 minutes. number of the question that you are continuing to answer at the top of the page. original answer space where the answer is continued, i.e. give the page number. Fill in the • Continuing an answer: If you need to use the space to continue an answer, indicate in the Planning: If you use the spare pages for planning, indicate this clearly at the top of the page. responses and/or as additional space if required to continue an answer. Spare pages are included at the end of this booklet. They can be used for planning your This section has 12 questions. Answer all questions. Write your answers in the spaces provided. (100 Marks) Section Two: Calculator-assumed MATHEMATICS 3A/3B 3 CALCULATOR-ASSUMED

See next page

$\simeq$	
0	
$\overline{}$	
VTOV	
$\circ$	
$\sim$	
$\neg$	
_	
5	
<	
77	
~	
=	
_	
m.	
=	
H E	
_	
_	
-	
S	
THIS AREA AS	
➣	
$\leq$	
$\pi$	
$\mathbb{Q}$	
$\triangleright$	
♪	
70	
S	
=	
7	
_	
>	
WILL BE (	
_	
_	
_	
W	
ш	
$\overline{}$	
CUTO	
$\overline{}$	
_	
_	
$\cap$	

CALCULATOR-ASSUMED

22 **MATHEMATICS 3A/3B** 

Additional working space

Question number:

.

#### CALCULATOR-ASSUMED

Question 9 (16 marks)

A biologist was conducting trials of a new fertiliser. She obtained ten almost identical plants and applied different amounts of fertiliser to test its effectiveness. The heights of the plants were measured after two months. The results are shown in the table below.

Plant	1	2	3	4	5	6	7	8	9	10
Fertiliser (f) (grams)	8	9	11	12	13	15	17	20	21	23
Height (h) (centimetres)	24	26	29	28	32	33	35	35	34	33

(a) Determine the correlation coefficient  $r_{fh}$ .

(1 mark)

(b) Describe, in words, the relationship between f and h.

(2 marks)

(c) Determine the regression line of h on f.

(1 mark)

DO NOT WRITE IN

- (d) The difference between the actual plant height and the predicted plant height using the regression line for each different amount of fertiliser is calculated. This difference is called the residual.
  - Calculate the residuals for plants 9 and 10 and complete the table below. The first eight residuals are recorded in the table correct to two decimal places. (2 marks)

Plant	1	2	3	4	5	6	7	8	9	10
Residual	-2.47	-1.11	0.60	-1.04	2.32	2.04	2.75	0.83		

See next page

## CALCULATOR-ASSUMED

21

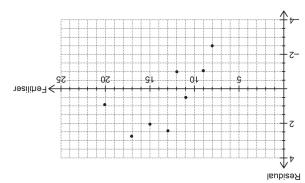
MATHEMATICS 3A/3B

A al al : 4: a a a		
Addillona	al workina	SDac

Question number: \_\_\_\_\_

**MATHEMATICS 3A/3B** CALCULATOR-ASSUMED

(2 marks) .01 bns 9 shalf for plants 9 and 10. The residuals for the first eight plants have been plotted below. Complete the



Comment on the information the residual plot revealed to the biologist. (2 marks)

(3 marks) and plot it on the residual plot in part (ii). State the coordinates  $(\overline{f},\overline{h})$ , determine the corresponding residual for this point

22 grams of fertiliser are applied. (1 mark) Use the regression line to predict the height of a plant after two months when

Comment on the reliability of the prediction in part (e) (i). (S marks)

See next page

Additional working space CALCULATOR-ASSUMED 20 MATHEMATICS 3A/3B

Question number:

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

MATHEMATICS 3A/3B CALCULATOR-ASSUMED Question 10 (8 marks) On 2 March, Michael is assigned to read a particular novel for his Literature class in preparation for a test on 22 March. On the first night, he reads 80 pages before falling asleep. On the next night, he reads 60 pages and on the third night, 45 pages. He continues to read 25% fewer pages each consecutive night. The situation can be represented by a recursive rule in the form  $a_{n+1} = pa_n$ , where  $a_1 = q$ . Determine the values of p and q. (2 marks) How many pages, to the nearest whole number, will Michael read on the fifth night? (2 marks) How long will it take Michael to read at least 300 pages? (1 mark) If the book has 320 pages, will Michael complete the book by the test date? Justify your answer.

See next page

ļĻ
JT OFF
BE CUT
MILLI
ASIT
<b>AREA A</b>
THIS
Z
WRITI
5

CALCULATOR-ASSUMED	19	MATHEMATICS 3A/3B

Additional working space

Question number: \_\_\_\_\_

# (1 mark) produce the boxplots shown below. Determine an eighth data point which, when included with the original data would (1 mark) the median. (1 mark) the mean. (1 mark) the standard deviation. scores are both reduced by one, state the effect on If the smallest two scores from the data are both increased by one and the largest two 3, 4, \_\_\_\_, \_\_\_, 17, 26 .ff si nsibem with the middle three values missing. The mean is 11.14 (correct to two decimal places) and the Consider the following data written in ascending order and consisting of seven integer values (e marks) It noitsauD MATHEMATICS 3A/3B CALCULATOR-ASSUMED

See next page

56

56

(z marks)



DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

ε

7

(ii)

3.01

MATHEMATICS 3A/3B (8 marks)

Question 19
A jeweller purchased cultured pearls for the production of necklaces. The diameters of the pearls were found to be normally distributed, with a mean of 1 cm and a standard deviation of pearls were found to be normally distributed, with a mean of 1 cm and a standard deviation of pearls were found to be normally distributed, with a mean of 1 cm and a standard deviation of 0.025 cm.

(a) What proportion of the pearls will have a diameter exceeding 1.07 cm? Give your answer correct to three significant figures.

What is the probability that a pearl will have a diameter between 0.975 cm and 1.025 cm?

(c) Below what size will the diameter of 10% of the peaks fall? (2 marks)

Industry standards dictate that for the consistency of the necklace, pearls with a diameter of less than  $0.93\,\mathrm{cm}$  or greater than  $1.07\,\mathrm{cm}$  cannot be used.

(d) For every 1000 pearls, determine the number of pearls that will **not** be suitable for use in the necklaces. (3 marks)

End of questions

Q

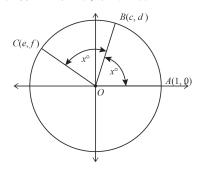
CALCULATOR-ASSUMED

CUT

DO NOT WRITE IN THIS AREA AS IT WILL

Question 12 (7 marks)

The unit circle below, with centre O at the origin, has the points A(1,0), B(c,d) and C(e,f) on the circumference and  $\angle COB = \angle BOA = x^{\circ}$ ,  $45^{\circ} < x^{\circ} < 90^{\circ}$ .



Given Pythagoras's Theorem: 'In a right triangle PQR where p, q are the short sides and r is the hypotenuse,  $r^2 = p^2 + q^2$ ,' use the pronumerals c, d, e and f to:

- (a) state a relationship between c and d not involving x. (2 marks)
- (b) determine an equation for  $\sin x^{\circ}$ . (1 mark)
- (c) evaluate  $\cos 2x^{\circ}$ . (2 marks)
- (d) determine the area of triangle *OBC*. (2 marks)

See next page

CALCULATOR-ASSUMED

17

MATHEMATICS 3A/3B

Question 18

(3 marks)

The heights of a small population of people living on a Pacific island were all measured for a regional census. It was found that 99.7% of the population were between 124 cm and 190 cm tall and 68% of the population were between 146 cm and 168 cm tall. If the heights are normally distributed, use this information to estimate the mean and standard deviation of the population heights.

DO NOT WRITE IN THIS AREAAS IT WILL BE CUT OFF

	See next page	
	See next page	
(2 marks)	ле раддоск.	(b) Calculate the perimeter of the
ds to calculate the perimeter of and on a bearing of 055° and (2 marks)	is $k$ finioq morît m 8.34 si $k$ finiog $^\circ$ 816 îo gninsəd is no t	A farmer wishes to fence a triangula the paddock. He determines that po point C is 68.44 m from point A and (a) Draw a diagram to represen
(4 marks)		£t noiteauQ
BE/AE SOITAMENTAM	6	CALCULATOR-ASSUMED

DO NOT WRITE IN THIS AREAAS IT WILL BE CUT OFF

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

(10 marks)		Question 17
CALCULATOR-ASSUMED	91	<b>BE/AE SOITAMEHTAM</b>

A retailer determines that he can sell 60 headbands per week if he charges \$10 per headbands. The retailer estimates that for each 50 cent reduction in price he can sell 15 extra headbands per week.

(a) Complete the table below. (2 marks)

Number of headbands sold	Price(\$)	Number of 50 cent reductions
09	10	0
	09.6	ļ
06		2
		3
	x = 0.0 - 01	x

(b) Given that Revenue (R) = Sale Price (P) × Number Sold (N), and ignoring any other overhead costs, show that  $R=600+120x-7.5x^2$ . (2 mar

(c) Using calculus techniques, calculate the amount that should be charged per headband to maximise the revenue.

(d) If the retailer initially purchased 200 headbands at \$4 each, calculate his expected profit given that the price is set to maximise the revenue.

10

CALCULATOR-ASSUMED

Question 14

(12 marks)

The table below shows the cost of gas for a Perth household. Accounts are sent at the end of each time period. Accounts for 2010 are unavailable, but some statistics are provided.

Time (t)	Months/Year	Cost (\$)	Four-point centred moving averages (m)	Residual
1	November 2009–January 2010	D	-	-
2	February 2010–April 2010	-	-	-
3	May 2010-July 2010	-	-	-
4	August 2010–October 2010	A	-	-
5	November 2010–January 2011	121.52	138.84	-17.32
6	February 2011–April 2011	140.14	139.07	1.08
7	May 2011-July 2011	153.26	140.13	С
8	August 2011–October 2011	143.11	141.73	1.38
9	November 2011–January 2012	126.47	144.68	-18.21
10	February 2012–April 2012	148.02	148.07	-0.05
11	May 2012-July 2012	169.00	151.15	17.85
12	August 2012–October 2012	154.45	152.33	2.12
13	November 2012–January 2013	139.78	152.58	-12.80
14	February 2013–April 2013	144.17	154.30	-10.13
15	May 2013-July 2013	174.80	155.32	19.48
16	August 2013–October 2013	162.43	155.80	6.63
17	November 2013–January 2014	139.96	156.73	-16.77
18	February 2014–April 2014	147.88	157.77	-9.89
19	May 2014-July 2014	178.50	-	-
20	August 2014–October 2014	167.05	-	-

(a) What is the time period of the household gas accounts?

(1 mark)

BE CUT

DO NOT WRITE IN THIS AREA AS IT WILL

b) Calculate the missing entries marked by *A* and *C*.

(2 marks)

See next page

CALCULATOR-ASSUMED 15 MATHEMATICS 3A/3B

Determine the equation of the tangent to the curve at the point (-1, 13). (2 marks)

d) Verify that this tangent passes through the minimum turning point. (1 mark)

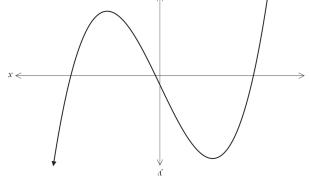
DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

33.79. Determine (2 marks)	r\$ ei 010S YnsunsL—600S 1		The seasonally adjuste the value of the missin	(f)
(2 marks)	from part (d).	ոն your prediction	Comment on the reliab	(ə)
	nst the four-point centred r ar the November 2014–Jan			(p)
(2 marks)	ovember-January period.	component for the No	Calculate the seasonal	(c)
HEMATICS 3A/3B	TAM	11	CULATOR-ASSUMED	CAI

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

See next page





(a) By differentiating the function, determine the coordinates of the turning points. (4 marks)

(b) For what values of x is the function decreasing?

(2 marks)

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

Question 15

(a) Given f(x) = 7 - 3x with domain  $\left\{-2, 1, \frac{1}{3}, 4\right\}$ , determine the range of f(x). (2 marks)

(b) (i) The function  $g(x) = \sqrt{2(x+1)}$  can be formed by transforming  $k(x) = \sqrt{x}$ . Determine the transformations required to obtain g(x) from k(x) and state the transformations in the correct order. (2 marks

(ii) Determine the domain of g(x).

(2 marks)

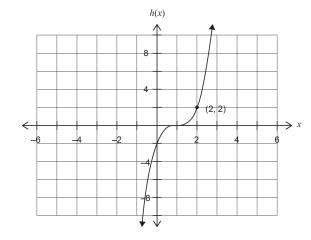
DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

See next page

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

(3 marks)

(c) (i) Determine the equation of the function h(x) shown on the axes below. (3 marks)



(ii) Use the axes above to sketch the function y = h(-x) + 2.