



Course Specialist Year 12 Test Three 2022

Student name: _____ Teacher name: _____

Task type: Response

Time allowed for this task: 40 mins

Number of questions: 6

Materials required: NO classpads nor calculators

Standard items:

Pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items:

Drawing instruments, templates, notes on one unfolded sheet of A4 paper, and up to three calculators approved for use in the WACE examinations

Marks available: 40 marks

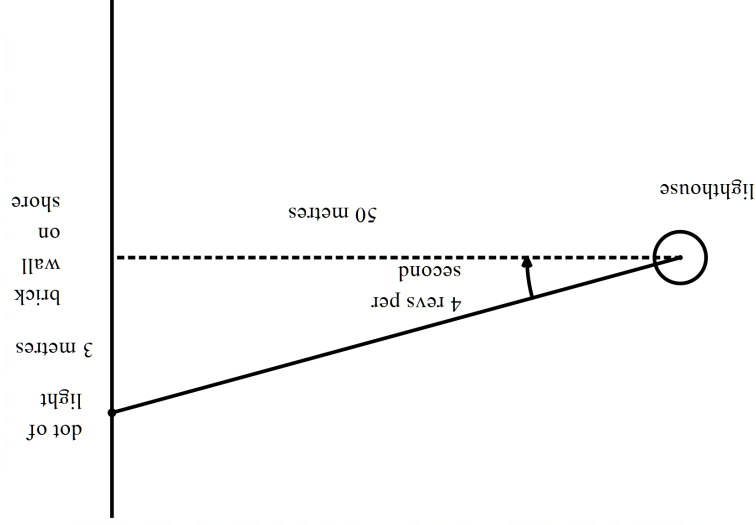
Task weighting: 10 %

Formula sheet provided: Yes

NO classpads nor calculators!

Note: All part questions worth more than 2 marks require working to obtain full marks.

Q6 (5 marks) (4.1.1, 4.2.2)
Consider a lighthouse that is 50 metres away from the shore. On the shore is a long brick wall. The light on the lighthouse is rotating at 4 revolutions per second. Determine the exact speed of the dot of light on the wall at a point 3 metres from the point directly opposite the lighthouse as shown below.



Q1 (3 & 3= 6 marks) (3.3.9-3.3.10)

a) Solve the following set of linear equations.

$$3x - 2y + z = -8$$

$$x + 2y - 3z = -14$$

$$2x + y - z = -9$$

b) Consider the system below,

$$3x - 2y + z = p$$

$$x + 2y - 3z = -14$$

$$2x + y + qz = -9$$

Determine the values of p & q such that there are:

- i) Unique solution
- ii) Infinite solutions
- iii) No solutions.

b)
$$\int \frac{8x^2 - 6x + 5}{(x - 2)(x^2 + 1)} dx$$

Q4 (4 marks) (4.2.1)

If $y^2 - \sin x = 1 - 5y$, determine $\frac{dy}{dx}$ & $\frac{d^2y}{dx^2}$ in terms of x & y only.

Q5 (3 & 4 = 7 marks) (4.2.1)
Determine the following integrals:
a) $\int \frac{\sqrt{x+1}}{5x} dx$ $u = x+1$

Q2 (2, 2, 2 & 3 = 9 marks) (3.3.11, 3.3.13)

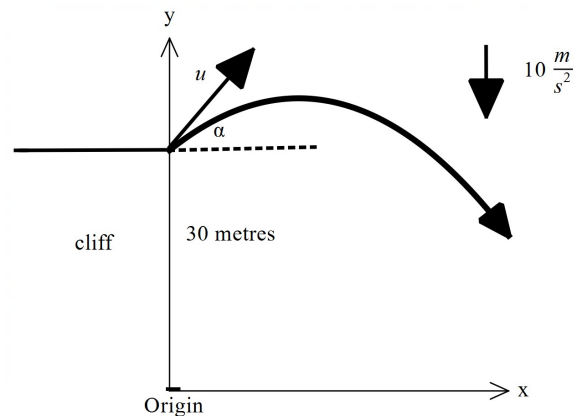
A particle moves such that at time t seconds the velocity is
the origin.
Determine:
a) The position vector at time $t = 1$ second.
b) The acceleration of the particle at $t = 1$ second.
c) The speed of the particle at $t = 2$ seconds.
d) The time(s) when the velocity is perpendicular to the acceleration.

$$v = \begin{pmatrix} t \\ -t^2 \\ -3 \end{pmatrix} m/s$$

. The particle is initially at

Q3 (4, 3 & 2 = 9 marks) (3.3.12, 3.3.13, 3.3.15)

Consider a particle that is projected from the top of a cliff of height 30 metres with a speed of u metres per second at an angle of α to the horizontal. Assume that the acceleration is constant at 10 m/s^2 towards the centre of the Earth. Let the origin of cartesian axes be at the base of the cliff as shown below with the appropriate unit vectors i & j .



Let $\ddot{r} = \begin{pmatrix} 0 \\ -10 \end{pmatrix} \text{ m/s}^2$.

- a) Using vector integration, show how to derive the position vector r at time t seconds in terms of u & α . Show all steps.

- b) Show how to derive the cartesian equation for the path of the particle in terms of u & α .

- c) Set up an equation in terms of u & $\tan \alpha$ ONLY, but do not solve, that would allow the range (x) to be determined where the particle hits the floor from the base of the cliff.