

WA Exams Practice Paper E, 2016

Question/Answer Booklet

If required by your examination administrator, please place your student identification label in this box

Calculator-free
Section One:
E TINU
WETHODS
SULAMAHIAM

Student Number: In figures
In words
Your name

Time allowed for this section

Reading time before commencing work: fifty minutes Working time for section:

Materials required/recommended for this section

To be provided by the supervisor This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: n

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

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METHODS UNIT 3 2 CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	12	12	100	98 65	
			Total	150	100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question that you are continuing to answer at the top of the
 page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

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CALCULATOR-FREE 15 METHODS UNIT 3

Additional working space

METHODS UNIT:		ε	OR-FREE	rA⊐U⊃	СА∟
32% (25 Marks			e: Calculator-free	nO noi	Sect
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		minutes.	e for this section is 50	mit gnix	Worl
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CALCULATOR-FREE ٦t **METHODS UNIT 3**

Additional working space

Question number: ____

Additional working space

Question 2 (9 marks)

4

Differentiate the following with respect to x.

(a)
$$\int_0^x \left(\frac{2}{3\sqrt{t}}\right) dt.$$

(1 mark)

(b)
$$y = e^{\cos(5x-2)}$$
.

(2 marks)

$$(c) y = e^{3x} \sqrt{x} .$$

(3 marks)

(d)
$$y = \frac{\cos(2x)}{\sin(3x)}$$

(3 marks)

δa , where a is a constant.	$3 + x8 - xn2 - 2x\epsilon = (x)$, f si	The first derivative of the function \boldsymbol{J}			
(6 marks)		Question 3			Additional working space
METHODS UNIT 3	S	CALCULATOR-FREE	CALCULATOR-FREE	12	METHODS UNIT 3

Question number:

Determine f(x), given that f has a point of inflection at (3, 5).

Question 4 (10 marks)

(a) Evaluate
$$\int_0^1 \left(\frac{e^{1-2x}}{3} \right) dx$$
.

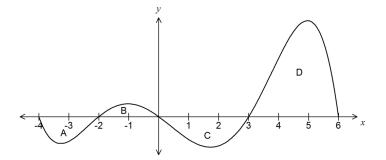
(3 marks)

(b) Determine
$$\int \left(\frac{1}{x^2} - \sin\left(\frac{x}{3}\right)\right) dx$$
.

(3 marks)

Question 7 (7 marks)

The graph of the function y = f(x) is shown below for $-4 \le x \le 6$.



The area of each region enclosed by the curve and the x-axis is shown in the following table.

Region	А	В	С	D
Area of region	5	3	11	25

- (a) Determine the area enclosed between the graph of y = f(x) and the x-axis, from x = -4 to x = 6. (1 mark)
- (b) Determine the value of

(i)
$$\int_{-2}^{6} f(x) dx$$
. (2 marks)

(ii)
$$\int_{-2}^{3} 3f(x) dx$$
. (2 marks)

(iii)
$$\int_{0}^{6} 4 - f(x) dx$$
. (2 marks)

(4 marks)		(a) Evaluate $\int_{0}^{2} \sqrt{1+x\xi} 1+x$
8 METHODS UNIT 3	Z	CALCULATOR-FREE

(2 marks) 2 duestion 6

10

CALCULATOR-FREE

Given that $y=\sqrt{x}$, use x=100 and the increments formula $\delta y=\sqrt{x}\times\delta x$ to determine an

approximate value for $\sqrt{104}$.

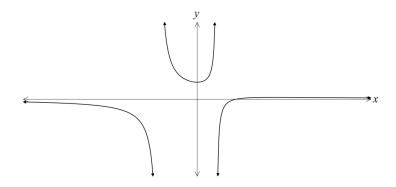
METHODS UNIT 3

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Question 5 (9 marks)

The graph of y = f(x) is shown below, where $f(x) = \frac{x-2}{x^2 + x - 2}$.



(a) Show that
$$f'(x) = \frac{x(4-x)}{(x^2+x-2)^2}$$
. (4 marks)

 The graph has a stationary point at (0, 1). Determine the coordinates of the other stationary point. (3 marks)

CALCULATOR-FREE

(c) Given that $f''(x) = \frac{2(x^3 - 6x^2 - 4)}{(x^2 + x - 2)^3}$, use the second derivative test to determine the nature of stationary point found in (b). (2 marks)