



PERTH MODERN SCHOOL

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INDEPENDENT PUBLIC SCHOOL

Semester One Examination, 2021

Question/Answer booklet

MATHEMATICS SPECIALIST UNIT 3

Section One:
Calculator-free

Your Name _____

Your Teacher's Name _____

Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Mark	Max	Question	Mark	Max
1			5		
2			6		
3			7		
4			8		

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	50	36
Section Two: Calculator-assumed	14	14	100	96	64
Total					100

Instructions to candidates

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2016*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

Section One: Calculator-free**(50 Marks)**

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 50 minutes.

Question 1**(6 marks)**

Consider the plane $3x - 2y + 5z = 10$ which contains point A $(1, -1, 1)$

- (a) Write a vector equation for this plane.

(3 marks)

$$r = \begin{pmatrix} 2 \\ -3 \\ 1 \end{pmatrix} + \lambda \begin{pmatrix} 5 \\ 1 \\ -2 \end{pmatrix}$$

Consider the line

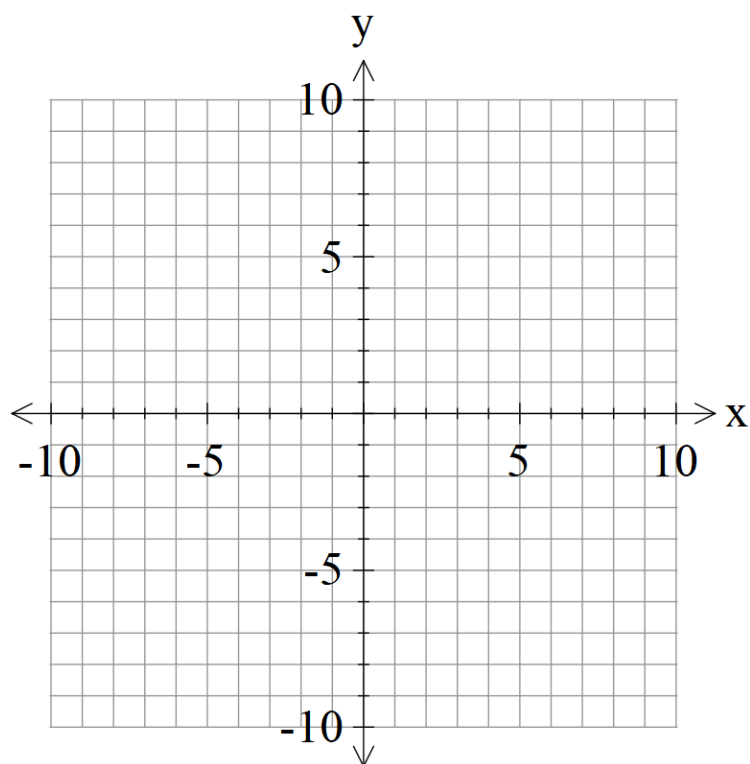
- (b) Determine the coordinates of where the line above meets the plane.

(3 marks)

Question 2

(6 marks)

Sketch the graph $y = f(x)$ where $f(x) = \frac{(x+2)(x-5)}{(x+1)(x-3)}$. Clearly show the major features of the graph.



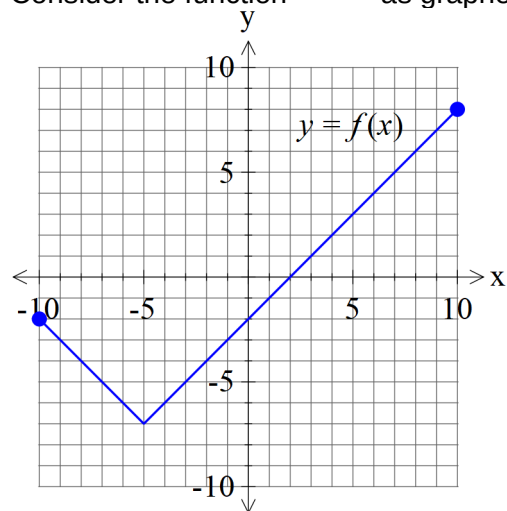
Question 3**(6 marks)**

Consider the plane Ψ that contains the following three points $A(1, 4, -1)$, $B(1, 1, 2)$ & $C(3, -1, 2)$. Using vector methods, determine the distance of point $D(6, -7, 1)$ from the plane Ψ . Show all working and reasoning.

Question 4

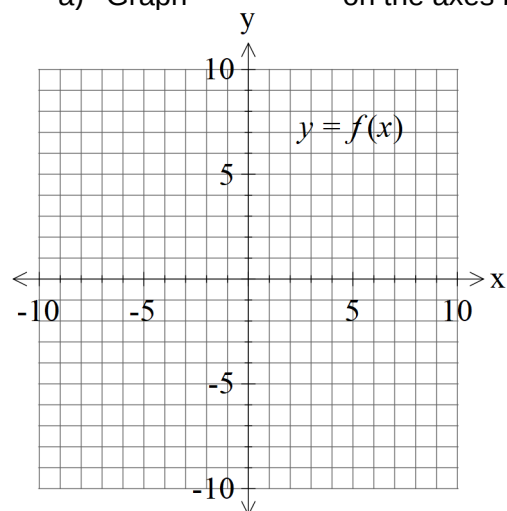
(5 marks)

Consider the function $f(x)$ as graphed below.



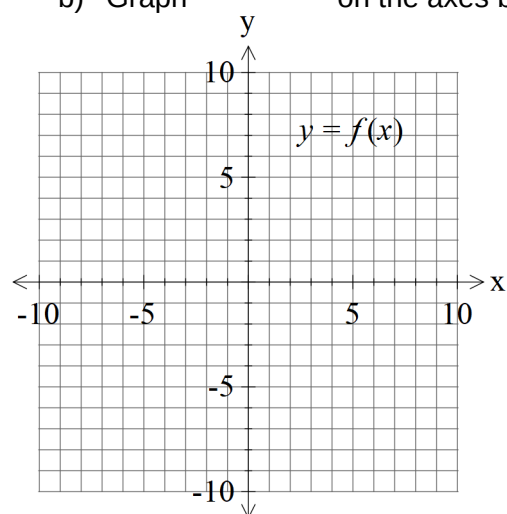
a) Graph $y = f(|x|)$ on the axes below.

(2 marks)



b) Graph $y = \frac{-1}{f(x)}$ on the axes below.

(3 marks)



Question 5

(7 marks)

Consider the function $f(x) = 4x^2 - 8x + 2$ with domain $x \leq 1$

- (a) Determine $f^{-1}(x)$ and its domain. (4 marks)

- (b) Consider $g(x) = x^2 + bx + c$ with $x \leq \frac{-b}{2}$ and b & c real constants. Given that $g(x)$ has an inverse which intersects graphically with $g^{-1}(x)$ at one point only, determine a possible exact value for x in terms of b & c and an equation that b & c must satisfy. (3 marks)

Question 6**(7 marks)**

Consider the following system of linear equations.

$$5x + y + 2z = 19$$

$$x - y + z = 8$$

$$2x - 3y + 4z = 27$$

a) Solve for x, y & z .

(3 marks)

Q6 cont-

b) If we modify the equations to the following with p & q being constants, solve for the following values of p & q such that there are:

- i) no solutions
- ii) infinite solutions (Give a geometrical interpretation of this situation) (4 marks)

$$5x + y + pz = 19$$

$$x - y + z = 8$$

$$2x - 3y + 4z = q$$

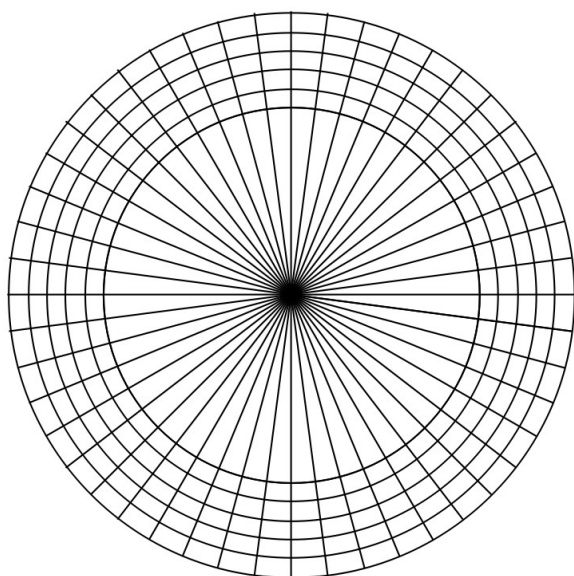
Question 7

(10 marks)

- a) Solve for all solutions to the following $z^6 = -5(2 + 2i)$ in the form $rcis\theta$ with $-\pi < \theta \leq \pi$.
(4 marks)

- b) Plot the above roots on the diagram below, indicating scale.

(3 marks)



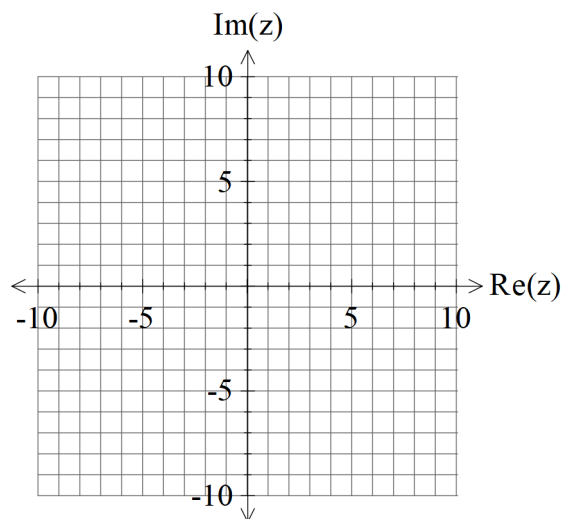
- c) If these points are joined, forming a polygon, determine the exact area of this polygon.
(3 marks)

End of questions

Question 8

(3 marks)

Sketch the locus of points that satisfy $\text{Arg}(z - 5 - 7i) + \pi = \text{Arg}(z)$ on the complex plane below and explain your reasoning.



Additional working space

Question number: _____

Additional working space

Question number: _____

Additional working space

Question number: _____

Acknowledgements