

## WA Exams Practice Paper E, 2016

# Question/Answer Booklet

MATHEMATICS METHODS UNIT 3 Section Two: Calculator-assumed

If required by your examination administrator, please place your student identification label in this box

Student Number: In figures

Time allowed for this section
Reading time before commencing work:
Working time for section:
ten minutes
one hundred minutes

Materials required/recommended for this section To be provided by the supervisor This Question/Answer Booklet Formula Sheet (retained from Section One)

To be provided by the candidate
Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that
you do not have any unauthorised notes or other items of a non-personal nature in the
examination room. If you have any unauthorised material with you, hand it to the supervisor
before reading any further.

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METHODS UNIT 3 2 CALCULATOR-ASSUMED

## Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	12	12	100	98	65
			Total	150	100

### Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
  examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- A. Spars pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

  Planning, If you use the spars pages for planning, indicate this clearly at the top of the page.

  Continuing an answer. If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked seekly and for male be a suited for treasoning, locative answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to neceive full marks. If you repeat any question, ensure that you cancel the snaver you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

See next page

CALCULATOR-ASSUMED	19	METHODS UNIT 3
Additional working space		

Question number: \_\_\_\_\_

CALCULATOR-ASSUMED METHODS UNIT 3 CALCULATOR-ASSUMED METHODS UNIT 3 Additional working space Section Two: Calculator-assumed 65% (98 Marks) This section has **twelve (12)** questions. Answer **all** questions. Write your answers in the spaces provided. Question number: \_\_\_\_\_ Working time for this section is 100 minutes. Question 8 (6 marks) Water flows into a tank, initially holding 125 L, at a rate given by  $V'(t) = \frac{24t - t^2}{3}$  for  $0 \le t \le 24$ , where  $V\left(t\right)$  is measured in litres per hour and t is in hours. (a) Determine how much water is in the tank after 24 hours. (b) Determine the time it takes for the tank to fill to 500 L. (3 marks)

(b) Determine the shaded area in the diagram, enclosed by the curve  $\ y=\sqrt{x}$ , the straight line AB and the y-axis.

The diagram below shows the graph of the function  $y=\sqrt{x}$  and the straight line AB that is perpendicular to the curve at A, where x=4. (c) Determine the stee enclosed by the curve  $\ y=\sqrt{x}$  , the straight line AB and the x-axis. (3 marks) (9 marks) 21 noitseuD METHODS UNIT 3 11

See next page

See next page

CALCULATOR-ASSUMED

(3 marks)

10

METHODS UNIT 3

CALCULATOR-ASSUMED

See next page

(a) Determine the equation of AB.

Question 9  The temperature, $T$ °C, of a bronze casting $t$ seconds after being removed from an	(8 marks)	Additional working space				
modelled for $0 \le t \le 800$ by $T = T_0 e^{-0.0034t}$ .	TOTAL NO.	Question number:				
(a) How long, to the nearest second, did it take for the initial temperature of the halve?	casting to (3 marks)					
(b) Determine the initial temperature of the casting, given that it had cooled to 7 minute.  (c) Can the above rate of change model be used to calculate how long it takes temperature of the casting to fall below 40°C? Explain your answer.	(2 marks)		inth powilitaul, ries of the care, justifying that to achieve this minimum area.  (a) marks)	misim erti enismeteb ot sevitavheb ez() (d) a suber erti eiste bins "mimmin e ai is	act to auter ant animateb , $I=\tau$ (askem $\lambda$ )	(b) Given that the body has a velocity of 3 cm/s when constant $a$ .
			(3 marks)	(a) Show that the total surface area, $\lambda$ cm	(Ansm f)	. $\frac{1}{2} = 1$ nerlw $O$ is at ybod entitle world (6)
				A closed cylindrical can of radius x cm has a		The displacement, in centimetres, of a small body from a $x(t)$ , where $x(t) = (t-a)(2t^2-5t+2)$ , where $a$ is a constant
			(salsem e) cm2 % To 25 to amulou	At noitseuQ	(10 marks) (10 marks)	31 notizeus
See next page			9 METHODS UNIT 3	CALCULATOR-ASSUMED	CALCULATOR-ASSUMED	WETHODS UNIT 3 12

See next page

See next page

METHODS ONLY 3	CALCOLATOR-ASSUMED	CAEGULATOR-AGGUILED 3 METHODS ONT 3		
Question 19	(9 marks)	Question 10 (8 marks)		
The discrete random variable $\boldsymbol{X}$ has the probability distribution show	wn in the table.	A pottery produces souvenir coffee mugs, of which it is known that 5% are defective and the rest are good.		
x 1 2 3 4 5	]			
$P(X = x)$ $b$ $a^2$ $a$ 0.14 0.05		(a) In a box of 12 mugs, what is the probability that there are no defectives? (2 marks)		
(a) Determine the values of a and b, if E(X) = 2.58.	(4 marks)			
				occur in 200 experiments and comment on how well your answer agrees with the experimental result above.
				(b) Use the distribution from (b) to calculate the expected number of times that no sixes would
		(b) In a box of 24 mugs, what is the probability that there are at least 4 defectives?		
		(2 marks)		
				(c) Myst is the probability of obtaining a six when this dice is thrown? (2 marks)
				(c) What is the probability of obtaining a six when this dice is thrown?
(b) Determine $P(X \le 4 \mid X \ge 4)$ .	(1 mark)	(c) What is the probability that in 10 boxes, each containing 12 mugs, that either two or three of the boxes contain no defectives? (2 marks)		
		of the boxes contain no defectives? (2 marks)		
				oue exberument (1 mark)
				(d)
(c) Calculate the values of				
(i) Var(X).	(2 marks)			
		(d) The pottery decides to pack n mugs per box for wholesale clients, so that the chance of		
		there being at least one defective mug in a box is no more than 75%. Find the largest value of n. (2 marks)		
				(s) Strem S) Stremment of sexis to redmun neem eth si terlW
(ii) $Var(10X + 3)$ .	(1 mark)			
				Eredneucy 67 93 33 7
				Mumber of sixes 0 t 0
(iii) $Var(3-2X)$ .	(1 mark)			
			(syletii ç)	A cubical six-sided dice is known to be biased. It is thrown 3 times and the total number of sixes is noted. This experiment is then repeated 200 times, with the results shown in this table.
			(c) Determine the acceleration of the body when $r>0$ and it has a velocity of 27 cm/s.	Question 13 (7 marks)

METHODS UNIT 3

METHODS UNIT 3

CALCULATOR-ASSUMED

End of questions

CALCULATOR-ASSUMED

See next page

See next page

13 WETHODS UNIT 3

CALCULATOR-ASSUMED

See next page

METHODS UNIT 3

CALCULATOR-ASSUMED

METHODS UNIT 3 CALCULATOR-ASSUMED CALCULATOR-ASSUMED 15 METHODS UNIT 3 (7 marks) Question 11 Question 18 (8 marks) A rectangle is inscribed in a semicircle of radius 2 metres, as shown in the diagram. The graph below shows the function  $f(x) = 3 - e^{2x-1}$ . (2 marks) (iii) the smallest value of k, so that  $\,P(X=k) < 0.001\,.$ (a) Show that the perimeter of the rectangle is given by  $4\sin\theta + 8\cos\theta$ . (3 marks) (c) Calculate the change in displacement of the body during the sixth second. 0.5 An estimate is required for the area under the curve between x=0 and x=1, using the average of inscribed rectangles (shown above) and circumscribed rectangles (not shown). Use calculus methods to determine the maximum perimeter of the rectangle, and state the dimensions of the rectangle to achieve this maximum. (5 marks) (5 marks) (a) Complete the table below, rounding values to two decimal places. 0 0.25 0.5 0.75 2.00 (b) Use the right-rectangles shown to calculate an under-estimate for the area. (2 marks) (b) Determine an equation for the displacement of the body at time r. (c) Use four left-rectangles to calculate an over-estimate for the area. (2 marks) (S marks) (d) Determine a rule for P(X = X) for any integer value of x greater than 0. (a) Determine the velocity of the body after one second, rounded to three significant figures. (d) Use your over- and under- estimates to calculate an estimate for the area under the curve between x = 0 and x = 1. (1 mark) The body had an initial displacement of 250 metres relative to a fixed point 0, at which time its velocity was 10 ms  $^{\prime}$  . (a) Complete the table below for the values of x=I, 2, 3 and 4. In the mailroom of a large company it is known that 20% of incoming letters contain a cheque. Let X be the number of randomly chosen letters that are opened until a cheque is discovered. A small body travels in a straight line with acceleration given by  $a=2e^{-\alpha u}$  ms². (8 marks) Question 12 (9 marks)

See next page

See next page

See next page

METHODS UNIT 3

See next page

CALCULATOR-ASSUMED

CALCULATOR-ASSUMED

 $(0 \ge X \ge \varepsilon)^q$  (ii)

 $(01 = X)^{q}$  (i)

 $(x = X)_d$ 

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METHODS UNIT 3

(c) Calculate