Test One 2016

Teacher:

Year 12 Mathematics Methods

Test One

Calculator Free Year 12 Mathematics Methods Semester One 2016

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• Complete all questions

- Sunyaom Linecessary working
- səmuim 22 o o Total Marks = 25
- [saram 21] .1

Find $\frac{dy}{dx}$ in each of the following, by using the appropriate rule.

(a) $y = (3x^2 - x)(x^3 - 4x^2 - 5x + 3)$ (Do not aimplify) $(2x^2 - 5x + 3)(3x^2 - 5x + 3)$ (B) $(2x^2 - 5x + 3)(3x^2 - 5x + 3)(3x^2 - 5x + 3)$

(b) $y = 2x - \sqrt{x} + 3\pi^3 + \frac{4}{x^2}$ (Leave with positive indices.) $y = 2x - \sqrt{x} + 3\pi^3 + \frac{4}{x^2} = 1$ $y = 2x - 3\pi + 3\pi^3 + 3\pi$

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 $\sqrt{\frac{2}{\sqrt{2}}} = \sqrt{\frac{5}{\sqrt{2}}} = \sqrt{\frac{5}{\sqrt{2}}$

 $\sqrt{(x^{2} + 3x^{2} + 2x^{2})^{2}} = \sqrt{(x^{2} + 3x^{2} + 3x^{2})^{2}} = \sqrt{(x^{2} + 3x^{2} + 3x^{2})^{2}}$ (a) $\sqrt{(x^{2} + 3x^{2} + 3x^{2})^{2}} = \sqrt{(x^{2} + 3x^{2} + 3x^{2})^{2}}$ (b) [٤]

(e) $y = y u^2 - 3$ using the chain rule $\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$, where $u = 2x^3 + 3$ $W_{A} = W_{A} \times W_{A}$ $= \frac{2}{2} \left((U^2 - 3)^{-2} \cdot U_{A} \times U_{A} \right) \times \frac{2}{2} \times U_{A} \times U_{A} \times U_{A}$ Perth Modern School $= \frac{2}{2} \left((2x^3 + 3) \cdot U_{A} \times U_{A} \right) \times U_{A} \times U_{A}$ [7]

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[7]

[7]

Ms Cheng

Mr Roohi

Mr Bertram

Mrs. Carter

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[S marks]

Sketch the graph of y = f(x) given the data below:

(i) f(2) = -9, f(-4) = 27, f(-1) = 9

 $\Delta = X$ ΔA ΔA with $0 < (2)^n \text{if bins } 0 = (2)^n \text{i}$ (ii)

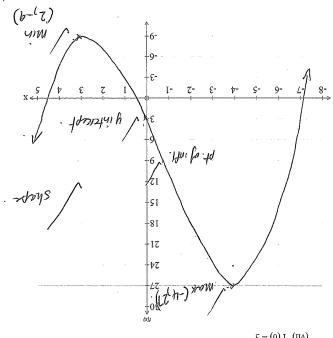
 $-\mu - = \mathcal{K}$ for χ_{DM} $0 > (\hbar -)^{n} \text{I} \text{ bns } 0 = (\hbar -)^{n} \text{I}$ (iii)

Infleder when x=-1. $0 = (1-)^n 1$ (vi)

(v) for x > 2, x < -4

 $\Delta > X > 4 - 101 \ 0 > (X)$, (iv)

 $\varepsilon = (0) 1$ (iiv)



[2]

2. [3 marks]

Consider the function $f(x) = x^3 - 5x^2 - 8x + p$ where p is a constant.

(a) Determine where the local (relative) extrema points occur.

$$f(x) = 3x^2 - 10x - 8$$
.
 $3x^2 - 10x - 8 = 0$

$$(3n+2)(2x-4) = 0$$

 $x=-\frac{2}{3}, 4$

(b) What can we say about value of p given that two of the three roots are negative [1]

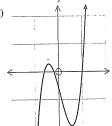
3. [4 marks]

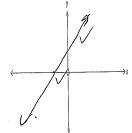
Draw a sketch below of each of the gradient functions formed by each of the following functions

(a)



(b)





3. [7 marks]

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(a) If the volume of a cylinder is given by $V = 2\pi r^3$, find the appropriate percentage change in V when r changes by $\frac{1}{2}$ % [3]

$$V = 2\pi r^{3^{2}}$$

$$dy_{dv} = 6\pi r^{2} \quad \begin{cases} \$r - 9.005 \\ \$ = 6\pi r^{2} \end{cases} \quad \begin{cases} \$r - 9.005 \\ \$ = 6$$

(b) If the volume of the solid generated by rotating a shaded region is given by $V = \pi [0.05h^5 + \frac{2}{3}h^3 + 4h]$, use the incremental formula, $\delta V \approx \frac{dV}{dh} \delta h$, to estimate the change in volume when h increases from 3 to 3.01.

$$\frac{dV}{dh} = \frac{TT(h^4 + 8h^2 + 16)}{4} \quad \text{off classpad}.$$

For small change on h $\frac{8V}{8h} \approx \frac{\pi (n^4 + 8h^2 + 16)}{4}$ $\begin{cases} V = \frac{\pi (3^4 + 8.3^2 + 16)}{4} \times (0.01) \end{cases} \times (0.01)$ $= \frac{169 \pi}{400}$ $\approx 1.33 \text{ units.}$

The increase would be 1.33 units as h Increase 3 to 3.01.

2

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4. [6 marks]

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 $y = x^2 - 3x^2 - 9x + 1$. Then graph a sketch of the function on the axes provided below,

clearly showing these key points. Find the turning points, points of inflection and intercepts for the function

 $\int_{-\infty}^{\infty} d^{2} x dx = \int_{-\infty}^{\infty} (2\pi)^{2} = \int_{-\infty}^{\infty} (2$ 0=6-29-22 V. P-18-5x2-bb (10) = til . y 41161 $X \leftarrow$

dig = 6x-6. .. pt of interdier x=(,-10).V

Perth Modern School Man x=-1 dig \$0. max.

Perth Modern School Man x=-3. dig =0 min

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2. [8 marks]

The volume of a certain rectangular box is given by the equation $\int f(x) = x^2 - 8x + 48$.

the base of the box. If the height of the box is (4-x) units, determine an algebraic expression for the area of

Are of the box.

$$\frac{\lambda^3 - 5 \chi^2 - 5 \chi + 448}{\mu - \chi} = -\chi^2 + \chi + 12$$

[5]

Calculate the value of x for which the volume is a maximum.

$$N_{x} = x \quad V_{x} V_{y} \quad x_{y} V_{y}$$

$$V_{y} = x \quad V_{y} V_{y} \quad x_{y} V_{y}$$

$$V_{y} = V_{y} \quad V_{y$$

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Calculator Assume

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[3]

Name:

- · Complete all questions
- · Show all necessary working
- Total Marks = 25
- o 25 minutes

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,E. •		BEEFFE LEG

A particle's position along the x-axis	s, in meters	, is given by	y the function	$s = 3t^3 - 5t + $	F9

Find the Velocity and Acceleration of this particle when t = 2 seconds $V = 9^{2^2} - 5$

a= 18t		,
At $t=2$	V= 31 m/s	$, a = 36 m/s^2 /$

When does the particle stop moving, and how far from the origin is it at this time? [2]

$$9t^2-5=0$$

 $t=\sqrt{5}_3$ ignore—ve value.
 $S(\sqrt{5}_3)=6.51m$.
Stops after $\sqrt{5}_3$ s at $6.51m$.