Perth Modern School

Yr 12 Maths Specialist

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50 Marks 7 Questions NO Classpads NOR calculators allowed! TIME: 50 minutes working 27 July 2018 ↑ TEST Year 12 Specialist

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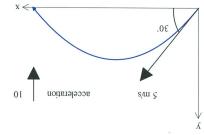
SOCUTIONS

Teacher:

Name:

Note: All part questions worth more than 2 marks require working to obtain full marks.

Q1 (2, 43, 3 & 2 = 10 marks)



A particle is projected with an initial speed of 5m $^\circ$ to the horizontal. The particle

experiences a constant downward acceleration of $10m / s^2$.

Determine in the initial velocity of the particle in i-j form. $\begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas peace} \end{cases}$ ii) the position velocity of the particle in i-j form. $\begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas peace} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas peace} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas peace} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{ cas 20} \\ 5 \text{ cas 20} \end{cases} = \begin{cases} 5 \text{$

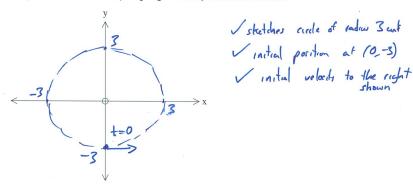
Q2 (2, 3, 3 & 3 = 11 marks)

An object moves such that its position vector, \mathcal{F} metres, at time t seconds is given by

$$r = \begin{pmatrix} 3\sin(4\pi t) \\ -3\cos(4\pi t) \end{pmatrix}$$

i) Determine the cartesian equation of the path of the object and the period of the motion.

ii) Sketch the cartesian path giving the initial position and direction.



iv) Show that the acceleration is directly proportional to the position vector, stating the constant of proportionality (i.e $\ddot{r} = -k r$ where k is a constant)

$$\hat{\Gamma} = \begin{pmatrix} -46\eta^2 \sin 4\pi t \\ 46\eta^2 \cos 4\pi t \end{pmatrix} = -16\eta^2 / 3 \sinh t \\ -3 \cos 4\pi t \end{pmatrix} = -16\eta^2 \Gamma$$

$$K = 16\eta^2 / (accept - 16\eta^2)$$

V 152 - = 14 / 12 PAIS - = x5

Consider the curve $\chi^2 = \cos(y)$. In terms of χ & y determine an expression for

Q7 (4 marks)

By using an appropriate substitution and integration, show that

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$$0 + \left(\frac{1 - x \cos x}{1 - x \cos x}\right) \ln \left(\frac{1}{x}\right) = xp \frac{x \cos x - 1}{x \sin x} \int \frac{1}{x \cos x} dx$$

uses natural logs to use to Lists partial fractions 1-30 Valdens

x160=11 1821 V

$$hb \left\{ \frac{1}{2} + \frac{1}{4} \right\} = \frac{1-3}{2}$$

$$hb \left\{ \frac{1}{2} + \frac{4}{4} \right\} = \frac{1-3}{2}$$

$$k = \frac{1}{2}$$

$$k$$

$$\frac{1+n}{1-n} = \frac{1-n}{1-n} =$$

1-2500 4 3

() SA (05 4 2) (-25m2) + 7 (3605 2), (-25m2), 2+25201+ x520061- = 2 + 2(520) € = √ Kb x5 200 165 x12 - K54200 165 x12
 No neal to factorise. $\int \int d^{2}x \, d^{2}x$ >+ 8 151 + 19 => + [8 151 + 15] b = np 21+ n5 = np 2 (Σ1+ m5) = np 2 n (Σ+ (2+m)5) $\sum_{k=1}^{N} \frac{2x^k}{2x^k} = \frac{2x^k}{2x^k} =$ 1 - 2 (4) 420) - = 44 5 - (16) REOS = 1/4 PAIS > ('p 200 -) 'b + "PRONIE = 5

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Q5 (4 & 3 = 7 marks)

Consider the curve described parametrically by

$$x = 5\cos t$$

$$y = -3\sin t$$
 from $t = 0$ to $t = \frac{\pi}{2}$

If this curve is revolved around the x axis a three dimensional shape is formed.

Show that the volume of this three dimensional shape is $45\pi \sin^3 t \, dt$ (Hint- consider direction of integration) = (71 (-3 sint) dx dt / (mydu = \(\frac{2}{2} 9 \pi \sin^2 + (5 \sin +) d+ V (my du dt V correct limits in correct order & = (ysnsint dt ii) Evaluate this integral to determine the exact volume $\left(\begin{array}{c} 2\\ 4S\pi \left(1-\cos^2t\right) \sin t \ dt = \int 4S\pi \sin t - 4\Gamma\pi \cos^2t \sin t \ dt \end{array}\right)$

$$= 4Sn \left[A\cos t + B\cos^3 t\right]^{\frac{7}{2}}$$

$$= 4Sn \left[A\cos t + B\cos^3 t\right]^{\frac{7}{2}}$$

$$= 4Sn \left[-3B\cos t + \cos t\right]$$

$$= 4Sn \left[-\cos t + \frac{1}{3}(\cos^3 t)\right]^{\frac{7}{2}}$$

$$= 4Sn \left[-\cos t + \frac{1}{3}(\cos^3 t)\right]^{\frac{7}{2}}$$

$$= 4Sn \left[0 - (-1 + \frac{1}{3})\right] = 30n$$

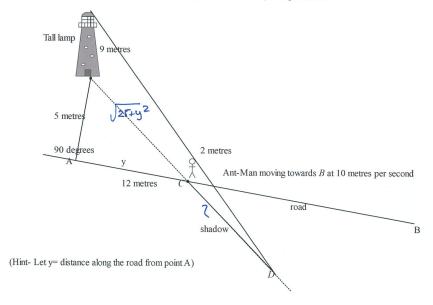
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Q6 (6 marks)

Consider the Ant-Man walking along a road AB towards point B at an incredible constant speed of $10m\ /\ s$. The height of the Ant-Man is 2 metres. Let point A be the closest point of the base of the Tall lamp from the road, i.e 5 metres and the height of the Tall lamp being 9 metres.



Determine at the point where the Ant-Man is 12 metres along the road from point A, the time rate of change of the length of the shadow CD.

$$\frac{7}{13(7)} = \frac{2}{9}$$

$$\frac{7}{13(7)} = \frac{2}{9}$$

$$\frac{7}{13} = \frac{2}{13}$$

$$\frac{7}{13} = \frac{2}{$$

Juces similar triangles V uses J2T+y2 determines expression linking Pength to y $72 = 2\sqrt{27+y^2}$ $72 = (27+y^2) 2y \dot{y}$ $71 = \frac{1}{13} 2(12)(10)$ $\sqrt{\frac{1}{13}} \frac{1}{2} 2(12)(10)$ $\sqrt{\frac{1}{13}} \frac{1}{2} 2(12)(10)$ $\sqrt{\frac{1}{13}} \frac{1}{2} 2(12)(10)$