



WA Exams Practice Paper D, 2016

Question/Answer Booklet

**MATHEMATICS
METHODS
UNIT 3**

**Section One:
Calculator-free**

If required by your examination administrator, please
place your student identification label in this box

Student Number: In figures

| | | | | | | | |
|--|--|--|--|--|--|--|--|
| | | | | | | | |
|--|--|--|--|--|--|--|--|

In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes
Working time for section: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet
Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction
fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that
you do not have any unauthorised notes or other items of a non-personal nature in the
examination room. If you have any unauthorised material with you, hand it to the supervisor
before reading any further.

Structure of this paper

| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of exam |
|---------------------------------|-------------------------------|------------------------------------|------------------------|-----------------|--------------------|
| Section One: Calculator-free | 8 | 8 | 50 | 53 | 35 |
| Section Two: Calculator-assumed | 12 | 12 | 100 | 98 | 65 |
| Total | | | | 151 | 100 |

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

• Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.

• Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

See next page

Additional working space

Question number: _____

The graph of $y = f(x)$ is shown below, where $f(x) = xe^x$.



- (a) Determine the exact location of the stationary point on the graph of $y = f(x)$. (3 marks)

- (b) Apply the second derivative test to show that the stationary point in (a) is a minimum. (3 marks)

- (c) The graph of $y = f(x)$ has just one point of inflection. Determine the exact coordinates of this point. (3 marks)

This section has **eight (8)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

Question 1

(5 marks)

The gradient function of a curve is given by $\frac{dQ}{dt} = at - 2t^2$, where a is a constant. Determine the equation of the curve if it has a maximum when $t = 3$ and a zero when $t = 1$.

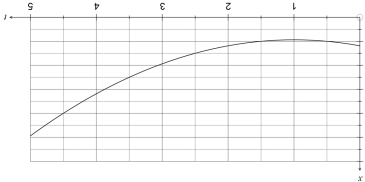
- (d) Suggest a way to improve the accuracy of this estimation method. (1 mark)

- (c) State, with reasons, whether your estimate in (b) is larger or smaller than the actual distance travelled by the car. (2 marks)

- (b) Estimate the area under the graph for the interval $0 \leq t \leq 5$ seconds using five centred rectangles of equal widths, and hence state the distance travelled by the toy car in this time. (2 marks)
- The area under the graph can be interpreted as the total distance travelled by the car during the first five seconds.

| Displacement, x (m) | 2 |
|-----------------------|-----|
| t | 0.5 |
| | 1.5 |
| | 2.5 |
| | 3.5 |
| | 4.5 |

- (a) Use the graph to complete the table below. (2 marks)



Question 5

CALCULATOR-FREE

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METHODS UNIT 3

A toy car travels along a straight path on level ground so that its displacement, x metres, relative to a fixed point O , is shown on the graph below for the interval $0 \leq t \leq 5$ seconds.

(7 marks)

- (c) Write, if possible, the three integrals below as a single integral. If not possible, explain why. (2 marks)
- $$\int_2^5 f(x) dx + \int_1^2 f(x) dx + \int_1^2 f(x) dx$$

- (b) Evaluate $\int_1^2 2 \cos \left(x - \frac{4}{x^2} \right) dx$. (3 marks)

- Question 4
- METHODS UNIT 3
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- (8 marks)
- (3 marks)
- Determine $\int \left(\cos x + e^{2x} \right) dx$, simplifying your answer.

