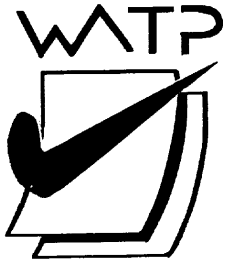
Additional working space

Question number(s): ……



Semester Two
Examination 2017
Question/Answer booklet

MATHEMATICS METHODS UNIT 1 and 2

Section One: Calculator-free

Student Name: _____

Teacher's Name: _____

Time allowed for this section

Reading time before commencing work: five minutes
Working time for paper: fifty minutes

Material required/recommended for this section

To be provided by the supervisor
This Question/Answer booklet
Formula Sheet

To be provided by the candidate
Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction tape/fluid, erasers, ruler, highlighters

Special Items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

	Number of questions available	Number of questions to be attempted	Working time (minutes)	Marks available	Percentage of exam
Section One Calculator—free	**9**	**9**	**50**	**50**	**35**
Section Two Calculator—assumed	14	14	100	100	65
					100

Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2017.* Sitting this examination implies that you agree to abide by these rules.

2. Answer the questions according to the following instructions.

   Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

   It is recommended that you **do not use pencil**, except in diagrams.

3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.

4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
   - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
   - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

5. The Formula Sheet is **not** handed in with your Question/Answer Booklet.

Additional working space

Question number(s): ……

Question 9 (3 marks)

(a) State the first three terms of the recursive sequence defined as $a_n = a_{n-1} + n + 1$, $a_1 = 3$.
(2 marks)

(b) State the recursive rule for the following sequence.
1, 1, 2, 3, 5, 8, 13, 21… (1 mark)

End of Questions

Section One: Calculator–free 35% (50 marks)

This section has **nine (9)** questions. Attempt **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

Working time: 50 minutes

Question 1 (2 marks)

Find the equation of the circle which has a diameter with endpoints at $(-2,8)$ and $(6, 8)$.
(2 marks)

Question 2 (4 marks)

(a) Solve $2\sin 2x = \sqrt{3}$ for x where $x \in [-\pi, \pi]$. (3 marks)

(b) Explain why $\cos x = 1.2$ has no real solution. (1 mark)

Question 3 (7 marks)

Determine $\frac{dy}{dx}$ for each of the following.

(a) $y = \frac{3}{5}kx^3 + k^2$ where k is a constant (2 marks)

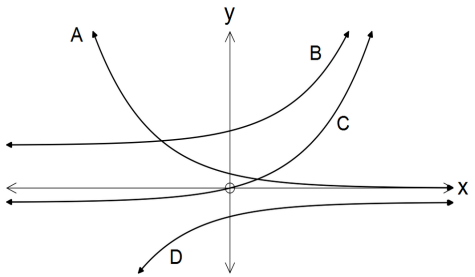
(b) $y = \frac{6x - 3x^3 + \sqrt{x}}{2x}$ (3 marks)

(c) $y = x(2x - 3)(2x + 3)$ (2 marks)

Question 4 (4 marks)

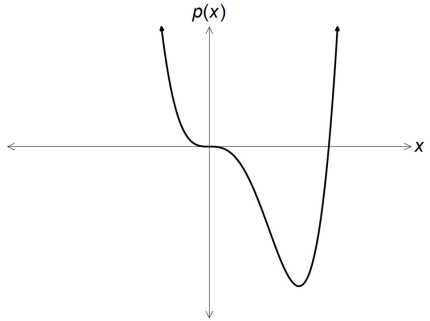
Match each function to its graph below:

$y = -2^{-x} - 1$	$y = \left(\frac{1}{2}\right)^x$	$y = 2^x + 3$	$y = 2^x - 1$



Question 8 (6 marks)

The function $p(x) = \frac{x^3}{2}(x - b)$ is shown below.



(a) Given $p(4) = 0$, show that $b = 4$. (1 mark)

(b) Find the co-ordinates of the local minimum. (3 marks)

(c) Show that there is a horizontal point of inflection at $x = 0$. (2 marks)

Question 7 (8 marks)

(a) Determine the antiderivative of the following. Leave your answers with positive indices where necessary.

(i) $x\left(x + \frac{1}{x}\right)$ where $x \neq 0$ (2 marks)

(ii) $\frac{t - 2t^4 + \pi}{t^3}$ (3 marks)

(b) Find y in terms of x for $\frac{dy}{dx} = 3 + x - 2x^4$, and $y = 2$ when $x = 1$. (3 marks)

CALCULATOR – FREE 5 MATHEMATICS METHODS UNIT 1 and 2

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Question 5 (11 marks)

(a) Simplify the following.

(i) $(2^4 \times 3^4)^{\frac{1}{4}}$ (1 mark)

(ii) $\dfrac{(ab^2c^{-3})^2\sqrt{a^4b^{-2}c^6}}{a^3b^2c}$ (2 marks)

(iii) $\dfrac{24^{\frac{2}{3}}.\sqrt{18} \times 3^{\frac{1}{3}}}{\sqrt[6]{8}.(27)^{\frac{1}{3}}}$ (3 marks)

(b) Solve for x. (3 marks)

(i) $\dfrac{16^{x-1}}{0.25^2} = \dfrac{1}{8}$

(ii) $(2^x - 8)(2^x - 1) = 0$ (2 marks)

Question 6 (5 marks)

(a) G and H are independent events. Given that $P(G) = 0.4$ and $P(H) = 0.5$, find;

(i) $P(G \cap H)$ (1 mark)

(ii) $P(G \mid H)$ (1 mark)

(iii) $P(G \cup H)$ (1 mark)

(b) In the expansion of $(2x + 3)^5$, state the coefficient of x^3. (2 marks)