

MATHEMATICS

Semester One Examination, 2018

Question/Answer booklet

Important note to candidates	
Special items: nil	
To be provided by the candidate Standard items: pens (blue/black prefer correction fluid/tape, er	ed), pencils (including coloured), sharpener, ззег, ruler, highlighters
Materials required/recommend To be provided by the supervisor This Question/Answer booklet Formuls sheet	ed for this section
Time allowed for this section Reading time before commencing work:	sətunim evit fifty minutes
msn 1voY	
ln words	
Student number: In figures	
Calculator-free	
Section One:	
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WETHODS	

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material with you, hand it to the supervisor **before** reading any further.

TRINITY COLLEGE 2 SEMESTER 1 2018
METHODS UNIT 3.4 CALCULATOR FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

Instructions to candidates

- The rules for the conduct of Trinity College examinations are detailed in the *Instructions to Candidates* distributed to students prior to the examinations. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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Supplementary page

Question number: _____

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provided.

P,E TINU SOUHT

Section One: Calculator-free
This section has eight (8) questions. Answer all questions. Write your answers in the spaces

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Working time: 50 minutes.

Question 1 (5 marks)

A particle travels in a straight line so that its distance x cm from a fixed point 0 on the line after t seconds is given by

$$0 \le 3, \frac{2}{1+3} = x$$

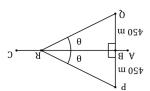
Calculate the acceleration of the particle when t=1.

SEMESTER 1 2018 CALCULATOR FREE TRINITY COLLEGE METHODS UNIT 3,4

Question 8 (8 marks)

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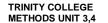
Two houses, P and Q, are 900 m apart on either side of a straight railway line AC. AC is the perpendicular bisector of PQ and the midpoint of PQ is B. A small train, R, leaves station C and travels towards B, 1200 m from C.



Let $\angle PRB = \angle QRB = \theta$, where $0 < \theta < 90^{\circ}$, and X = PR + QR + CR, the sum of the distances of the train from the houses and station.

(a) By forming expressions for
$$PR$$
, BR and CR , show that $X=1200+\frac{450(2-\cos\theta)}{\sin\theta}$. (3 marks)

(b) Use a calculus method to determine the minimum value of X.



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Question 2 (5 marks)

A function defined by $f(x) = 13 + 18x - 6x^2 - 2x^3$ has stationary points at (1, 23) and (-3, -41).

 (a) Use the second derivative to show that one of the stationary points is a local maximum and the other a local minimum.
 (3 marks)

(b) Determine the coordinates of the point of inflection of the graph of y = f(x). (2 marks)

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Question 7 (5 marks)

The height, in metres, of a lift above the ground t seconds after it starts moving is given by

$$h = 8\cos\left(\frac{t}{7}\right)$$

Use the increments formula to estimate the change in height of the lift from $t=\frac{7\pi}{4}$ to $t=\frac{176\pi}{100}$.

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						ənimətə0	(d)
(2 marks)	Calculate $\mathrm{E}(X)$.	(c)					
(2 marks)	Construct a table to show the probability distribution of X .	(q)					
(2 marks)	By listing all possible combinations (135, 137, etc.), determine $P(X \le 7)$.	(9)	(5	(2 marks)	•(:	oetermine g(Z	(s) [
·um	contains five balls numbered $1,3,5,7$ and 9 . Three balls are randomly drawn same time and the random variable X is the largest of the three numbers dra	at the	,	it has a point of inflection at $(-1,29)$ and a	.(91–	ry point at (1,	stationa
(е шяцка)	£ nois:		(9	(9 marks)			Questio
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(a) Determine $\int 5(2x-1)^3 dx$.

(2 marks)

(b) Determine $\frac{d}{dx} e^{1-3x} - 2e$.

(2 marks)

(c) Determine $\frac{dy}{dx}$ given $y = \int_{x}^{1} t\sqrt{t} dt$.

(2 marks)

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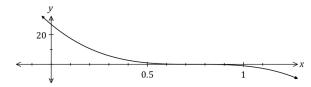
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(8 marks)

Question 5

The graph of $y = (3 - 4x)^3$ is shown below.



(a) Determine the area of the region enclosed by the curve and the coordinates axes.

(4 marks)

Given that the area of the region bounded by the line x=k, the curve and the x-axis is 4 square units, determine the value of k, where 0 < k < 0.75. (4 marks