



St Mary's Anglican Girls' School

Semester Two, 2010

Question/Answer Booklet

MATHEMATICS

Year 12 3C/3D

Section One:

Calculator-free

Time allowed for this section

Reading time before commencing work: 5 minutes

Working time for this section:

50 minutes

Material required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be used in this section of the examination. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available
Section One: Calculator-free	8	8	50	40
Section Two: Calculator-assumed	13	13	100	80
				120

Instructions to candidates

- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.
- Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

1. [4 marks]

Find the absolute maximum and absolute minimum of the function $f(x) = \frac{x^3}{3} - x^2 + 4$ on the interval $-3 \leq x \leq 3$.

Additional working space

2. [2 marks]

Find $\int (6x^2 - 2)(x^3 - x + 1)^4 dx$

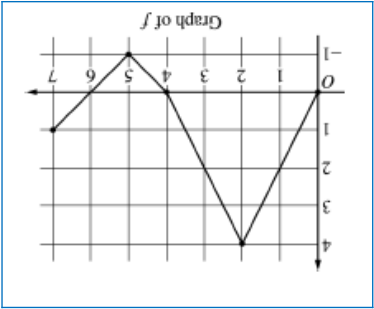
3. [4 marks]

Find a and b if:

$$\frac{d}{dx} \left(3x\sqrt{2x-1} \right) = \frac{dx+b}{\sqrt{2x-1}}$$

8. [4 marks]

Let f be a function defined on the interval $[0, 7]$. The graph of f , consisting of 4 line segments, is shown below.



Let g be the function given by
$$g(x) = \int_x^2 f(t) \, dt.$$

(a) Find $g(3)$ and $g(6)$.

(2)

(b) Find $g'(3)$.

(2)

4. [5 marks]

The points $P(-4, 3)$, $Q(6, 3)$ and $R(-2, -1)$ all lie on the graph of $f(x) = ax^2 + bx + c$.
Find a , b and c .

7. [5 marks]

Consider the function f with second derivative $f''(x) = 3x - 1$. The graph of f has a minimum point at $A(2, 4)$ and a maximum point at $B\left(-\frac{4}{3}, \frac{358}{27}\right)$.

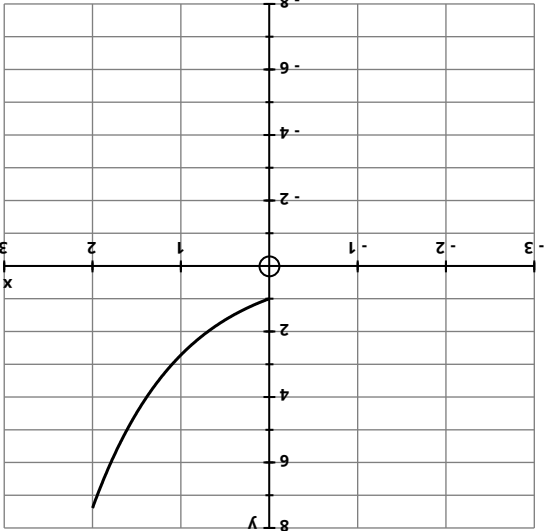
(a) Justify that B is a maximum. [2]

(b) Given that $f'(x) = \frac{3}{2}x^2 - x + p$, show that $p = -4$. [1]

(c) Find $f(x)$. [2]

5. [6 marks]

This is the graph of $f(x) = e^x$, for $0 \leq x \leq 2$.

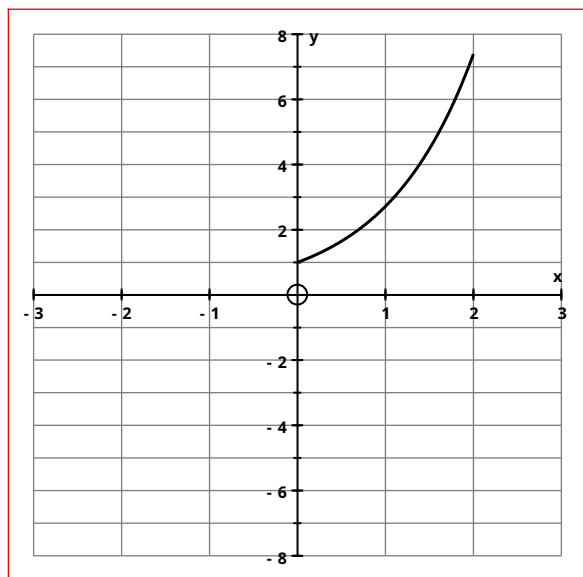


- (a) The area between the graph of $y = e^x$ and the x-axis from $x = 0$ to $x = 2$ is rotated through 360° about the x-axis. Find, in terms of e , the volume of this solid.
- (3)

- (d) Find the domain of $(f \circ g)(x)$.

(4)

- (b) On the axes below sketch the graph of $g(x) = -f(2x+2)$.
Label 3 points accurately. (3)



6. [10 marks]

The functions $f(x)$ and $g(x)$ are defined as $f(x) = \sqrt{x-1}$ and $g(x) = \frac{x^2-2}{x+4}$.

- (a) Evaluate $g(f(5))$. (1)

- (b) Show that there are no points on the graph of $g(x)$ where the gradient is 1. (4)

- (c) To find the domain of $(f \circ g)(x)$, it is necessary to solve the inequality $\frac{x^2-2}{x+4} \geq 1$.
Explain why. (1)