

# Perth College

### Semester Two Examination, 2016

# Question/Answer Booklet

				1
			ednirec olace y	

:0/		uo	-	_
S QNA	ļ	SJ	LIN	N
SC	<b>3</b> C	)H.	LЭ	Λ
CULIAN	N =	ш	ΙH	IΛ

Section 1 wo.

Time allowed for this section seading time before commencing work:		sətunim				
Тоиг пат	Your name					
ln words	lu words		 	 	 	
Student Number: In figures	sənugif nl					

### Morking time for section: one hundred minutes

Materials required/recommended for this section To be provided by the supervisor

This Question/Answer Booklet Formula Sheet (retained from Section One)

## To be provided by the candidate Standard items: pens (blue/black pre

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations

### Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

	92	Weighted score
	86	JATOT
	6	20
	L	61
	8	81
	8	<b>لا</b>
	8	91
	01	SI
	01	ħ١
	9	13
	01	12
	8	11
	8	01
	9	6
Your Mark	Available Marks	Question

001/	Final mark
<b>99/</b>	Section Two
98/	Section One

METHODS UNITS 1 AND 2

#### **CALCULATOR-ASSUMED**

### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	12	12	100	98	65
			Total	150	100

#### Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer Booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the
  - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams. 6.
- The Formula Sheet is not to be handed in with your Question/Booklet. 7.

See next page

#### **CALCULATOR-ASSUMED**

19

**METHODS UNITS 1 AND 2** 

Additional	working	enace
Additional	working	Space

Question number:	
------------------	--

<b>m                                    </b>	straight line that pass	Question 9 (a) Determine the equation of the s	
)		Guestion 9	
	inutes.	Working time for this section is 100 mi	
		brovided.	
ns. Write your answers in t	s. Answer <b>all</b> questio	This section has <b>twelve (12)</b> question:	
86) %99		Section Two: Calculator-assumed	
METHODS UNITS 1	3	CALCULATOR-ASSUMED	CALCULATOR-ASSUMED

Question number: \_

METHODS UNITS 1 AND 2
Additional working space

Calculate and use the discriminant to determine the number of solutions to the equation  $9x^2 - 24x + 16 = 0. \tag{3 marks}$ 

perpendicular to the line with equation 2x + 5y = 1.

(3 marks)

#### Question 10 (8 marks)

A walking club is planning a charity walk from Perth to Esperance. Food and camping supplies are to be set up at each overnight campsite in advance, using a vehicle based in Perth that is just large enough to carry enough for one campsite.

To leave the supplies at the first campsite, the vehicle must travel 40 km. For the second and third campsites, the vehicle must travel 100 km and 160 km respectively, and this pattern continues.

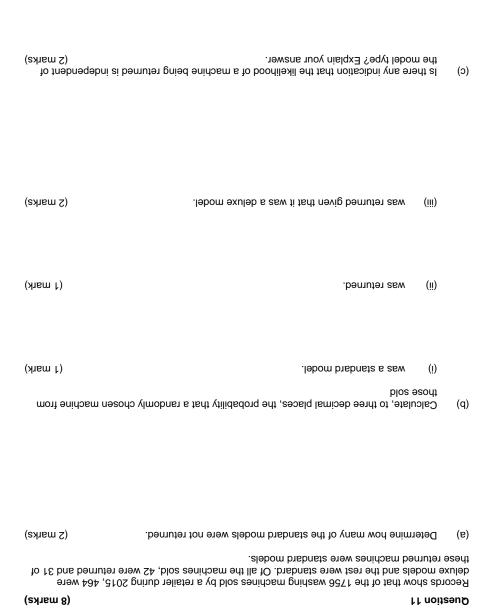
Determine the distances the vehicle will travel to set up campsites four and five. (1 mark)

Determine, in simplified form, a rule for the distance, d km, that the vehicle will have to travel to set up campsite n. (2 marks)

The vehicle can travel a maximum of 700 km on one tank of fuel. Determine the number of the furthest campsite the vehicle can leave supplies at, using no more than one tank of (2 marks) fuel.

If fuel costs 128 cents per litre and the fuel consumption of the vehicle is 9.5 litres per 100 km, determine the total fuel cost to set up the first 20 campsites. (3 marks) **CALCULATOR-ASSUMED** Additional working space

Question number: \_\_\_\_



g

CALCULATOR-ASSUMED

METHODS UNITS 1 AND 2

CALCULATOR-ASSUMED 9١ METHODS UNITS 1 AND 2

(9 marks)

(a) Show that the equation of the tangent to the curve  $y = \frac{x + x^3}{2}$  at the point where x = 2 is

Question 20

 $.01 = \chi \Omega - \chi E I$ (4 marks)

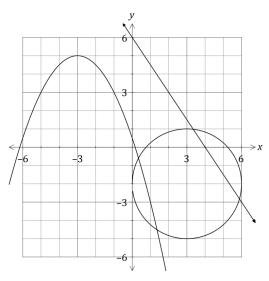
The line with equation  $y = 5x + \epsilon$  is a tangent to the curve  $y = x^3 + 3x^2 - 4x - 12$ .

(5 marks) Determine the value(s) of c.

Question 19

Question 12 (10 marks)

The graph of two functions and a circle of radius 3 units are shown.



(a) One function is f(x) = ax + b. Determine the values of the constants a and b. (2 marks)

(b) The relation can be written in the form  $x^2 + px + y^2 + qy + r = 0$ .

Determine the values of the constants p, q and r.

(3 marks)

(a) A sequence is defined by  $T_{n+1} = T_n - 7$ ,  $T_1 = 111$ .

(i) Determine  $T_{20}$ .

(1 mark)

(7 marks)

The sum of the first 40 terms,  $S_{40}$ .

(1 mark)

(iii) The value of n that maximises  $S_n$ .

(2 marks)

(b) A geometric sequence with  $T_2=87.5$  has a sum to infinity of 800. Determine all possible values of  $T_1$  for this sequence. (3 marks)

(S marks)

The other function is  $g(x) = cx^2 + dx + e$ .

Determine the values of the constants c, d and e, given that g(x) has a maximum

State coordinates of the turning point of the graph of y = g(x - 7). (1 mark)

(1 mark) State the range of the function y = -g(x).

> (8 marks) **&t noitseu**

Two students are to be chosen from a class of 18.

(1 mark) Determine how many different pairs of students may be chosen.

that this student is included in the pair chosen? One of the students in the class is the oldest in the school. What is the probability

remainder that do not. Four cans are to be selected at random from the box. A box contains 13 cans of soup, four of which have tomato as an ingredient and the

(1 mark) Calculate how many different selections of four cans can be made from the box.

ingredient. Determine the probability that none of the four cans will have tomato as an

number of cans with and without tomato as an ingredient. (S marks) Determine the probability that in the selection of four cans, there will be an equal Question 13 (6 marks)

In triangle PQR, PR = 50 cm, QR = 30 cm and  $\angle QPR = 25^{\circ}$ .

(a) Sketch two possible triangles that *PQR* could represent. (Your diagrams do not need to be to scale). (2 marks)

- (b) Given that  $\angle PQR$  is greater than  $75^{\circ}$  determine
  - (i) the size of  $\angle PQR$ .

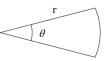
(2 marks)

(ii) the area of triangle PQR.

(2 marks)

Question 17 (8 marks)

The perimeter of a sector of a circle, of radius r cm and central angle  $\theta$  radians, is 60 cm.



(a) Show that  $\theta = \frac{60}{r} - 2$ .

(2 marks)

(b) Show that the area of the sector is given by  $30r - r^2$ .

(2 marks)

(c) Use calculus to determine the maximum area of the sector and state the values of r and  $\theta$  that achieve this maximum. (4 marks)

(10 marks)

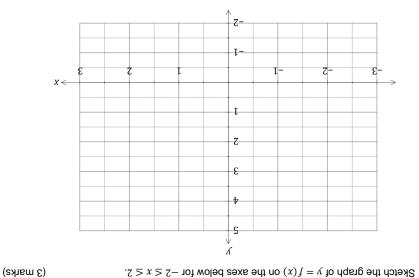
41 noitesup

The function f is given by  $f(x) = x^3 - 3x + 2$ .

Show that the graph of y = f(x) has two roots and state their coordinates. (2 marks)

6

of y = f(x) and use the sign test to determine the nature of these points. (5 marks) Use calculus techniques to determine the coordinates of all stationary points of the graph



(8 marks) 2 duestion 16 15

The imprisonment rate R, in number of prisoners per 100 000 people, in the US between the

 $^{0001-n}(850.1)$ 28 =  $^{9}$ years 1960 and 2000, can be modelled by the following equation, where  $\boldsymbol{n}$  is the year.

(1 mark) Calculate the imprisonment rate in the year 2000.

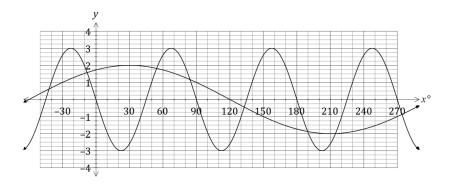
(3 marks) Draw the graph of the imprisonment rate for 1960  $\leq n \leq 2000$  on the axes below.



(3 marks) the US at this time, to the nearest 1 000. The population of the US was 266 million in 1995. Determine the number of prisoners in

prison population and the model no longer applied. In what year did this occur? (1 mark) When R first exceeded 500, steps were taken to address the exponential growth in the Question 15 (10 marks)

(a) The graphs of  $f(x) = a \sin(bx)$  and  $g(x) = c \cos(x + d)$ , where x is in degrees, are shown below



- (i) Determine the values of the constants a, b, c and d.
- (4 marks)

(ii) Use the graph to solve, to the nearest degree,  $f(x) = g(x), \ 0^{\circ} \le x \le 180^{\circ}$ . (2 marks)

(b) P and Q are acute angles with  $\sin P = \frac{12}{13}$  and  $\cos Q = \frac{15}{17}$ . Determine the **exact** value of  $\cos(P-Q)$ . (4 marks)

11