

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

### Important note to candidates

Special items: nil

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

To be provided by the candidate

Formula sheet

This Question/Answer booklet

To be provided by the supervisor

### Materials required/recommended for this section

Working time: fifty minutes  
Reading time before commencing work: five minutes

Time allowed for this section

Your name \_\_\_\_\_  
\_\_\_\_\_

In words \_\_\_\_\_

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Student Number: in figures \_\_\_\_\_

Calculator-free  
Section One:

## MATHEMATICS METHODS UNIT 3

If required by your examination administrator, please place your student identification label in this box

Question/Answer booklet

Semester One Examination, 2017

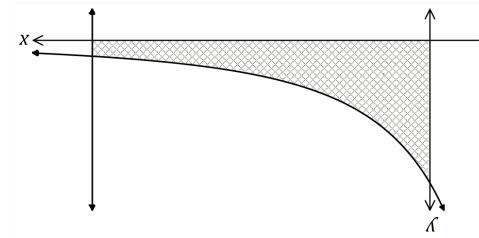


**Structure of this paper**

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	11	11	100	98	65
<b>Total</b>					<b>100</b>

**Instructions to candidates**

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.



Determine the area of the shaded region, enclosed by the  $x$ -? axis, the  $y$ -? axis, the line  $x=5$  and the curve.

The graph below shows the curve  $y = \frac{2x+5}{180}$  and the line  $x=5$ .

(5 marks)

### Question 1

Working time: 50 minutes.

provided.

This section has **eight (8)** questions. Answer all questions. Write your answers in the spaces

**35% (52 Marks)**

Section One: Calculator-free

**Question 2****(8 marks)**

A small body, initially at the origin, moves in a straight line with acceleration  $a(t) = 6t - 10 \text{ ms}^{-2}$ , where  $t$  is the time in seconds,  $t \geq 0$ . When  $t = 5$ , it was observed to have a velocity of  $31 \text{ ms}^{-1}$ .

- (a) Determine an expression for  $v(t)$ , the velocity of the body. (2 marks)

- (b) Determine the acceleration of the body when  $v=19$ . (3 marks)

- (c) Determine the velocity of the body as it passes through the origin for the last time. (3 marks)

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vative to justify that one of the  
r is a local maximum. (3 marks)

(2 marks)

A graph of a function  $f(x)$  on a Cartesian coordinate system. The horizontal axis is labeled  $x$  with an arrow pointing to the right. The vertical axis has arrows at both ends. A smooth curve starts from the bottom left, rises to a peak, and then descends towards the bottom right. The peak of the curve is marked with a small circle. A vertical dashed line extends from this peak to the horizontal axis, marking the point  $c$ . The text '(1 mark)' is written above the graph.

The graph of  $y = f(x)$  is shown below, where  $f(x) = e^x(x - 3)$ .

(6 marks)

METHODS UNIT 3

5

CALCULATOR-FREE

METHODS UNIT 3

12

### **Additional working space**

CALCULATOR-FREE

**Question 4**

(8 marks)

(a) Determine  $\frac{d}{dx} \left( \frac{1+e^{2x}}{1+\sqrt{x}} \right)$ .

(3 marks)

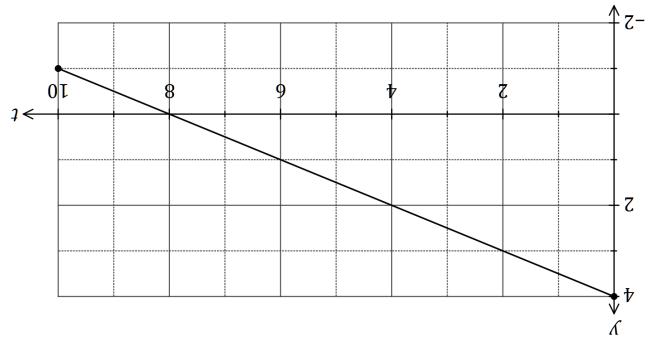
(b) Determine  $\frac{d}{dx} [2x\sin(3x)]$ .

(2 marks)

(c) Use your answer from (b) to determine  $\int 6x\cos(3x)dx$ .

(3 marks)

The graph of  $y=f(t)$  is shown below over the interval  $0 \leq t \leq 10$ .



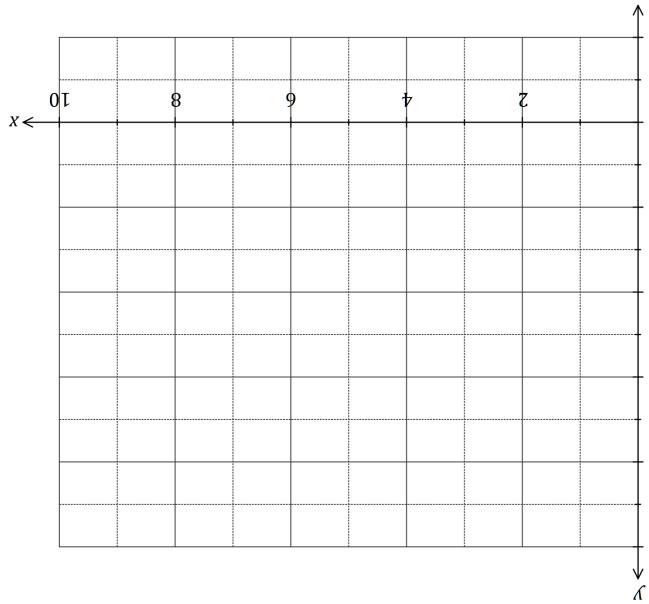
- (a) The table below shows the probability distribution for a random variable  $X$ . It is known that  $E(X)=1.7$  and  $\text{Var}(X)=1.41$ .  
 (4 marks)

$x$	0	1	$a+b$	$b$	$2a$
$p(X=x)$					
0	0	1	$a+b$	$b$	$2a$
1					
2					
3					

- Question 5  
 CALCULATOR-FREE  
 (6 marks)

- (a) Use the graph to determine an estimate for  $\int_2^0 f(t) dt$ .  
 (2 marks)

- (b) On the axes below, sketch the graph of  $y=F(x)$  for  $0 \leq x \leq 10$ , where  $F(x)=\int_x^0 f(t) dt$ .  
 (4 marks)



- Question 4  
 CALCULATOR-FREE  
 (1 mark)
- (i) Determine  $E(3-2X)$ .  
 (ii) Determine  $\text{Var}(3-2X)$ .  
 (iii)  $\text{Var}(3-2X)$ .  
 (1 mark)

**Question 6**

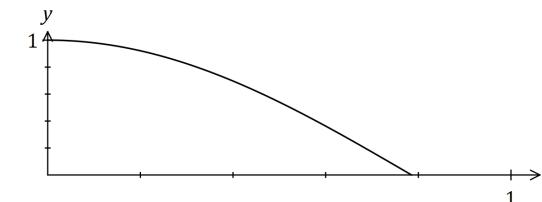
(7 marks)

- (a) The function  $f$  is such that  $f(1) = -2$  and  $f'(x) = \sqrt{3+x^2}$ . Use the increments formula to determine an approximate value for  $f(1.05)$ . (3 marks)

**Question 7**

(6 marks)

- A rectangle has its base on the  $x$ -axis, its lower left corner at  $(0, 0)$  and its upper right corner on the curve shown below,  $y = \cos 2x$ ,  $0 \leq x \leq \frac{\pi}{4}$ .



- (b) The function  $C$  is such that  $C(1) = 10$  and  $C'(x) = 3\sqrt{x+3}$ .

- (i) Explain why the increments formula would not yield an approximate value for  $C(6)$ . (1 mark)

- (a) Sketch a possible rectangle on the graph above and explain why the perimeter of the rectangle is given by the function  $p(x) = 2x + 2\cos 2x$ . (2 marks)

- (ii) Determine  $C(6)$ . (3 marks)

- (b) Determine the largest perimeter of the rectangle. (4 marks)