



Name _____

SOLUTIONS

1. [2, 1, 2, 2 marks]

(a) How much will a bottle of liquor be worth in 2 years time, if it presently sells for \$45?

$$A = P(1 + r)^n$$

$$= 45(1 + 0.048)^2 = 49.42$$

(b) How much will a bottle of liquor be worth in n years time, if it presently sells for \$45?

$$A = 45(1.048)^n$$

(c) The winemaker plans to release the liquor when it reaches a value of \$100. How long will they have to wait for this to be the case?

$$100 = 45(1.048)^n$$

(d) Another red wine produced by the winery is increasing in value at 2.3% p.a. If a large flagon presently sells for \$74, how long will it be before the Liquor becomes more expensive than the flagon?

$$45 = 74(1.023)^n$$

$$0.61 = 1.023^n$$

$$\ln 0.61 = n \ln 1.023$$

$$-0.4845 = n \times 0.0228$$

$$n = 21.25$$

2. [2, 1, 2, 2 marks]

Given $p(x) = 5x + 3$ and $q(x) = 2 - x$, find the following:

(a) the point of intersection of the two lines,

$$5x - 3 = 2 - x$$

$$6x = 5$$

$$x = \frac{5}{6}$$

(b) $p(4) = 23$ (c) $p(q(-1))$

$$q(-1) = 2 - (-1) = 3$$

$$p(3) = 5(3) + 3 = 18$$

(d) the value of k for which $p(k) = -2$

$$5k + 3 = -2$$

$$5k = -5$$

$$k = -1$$

3. [1, 1, 3 marks]

A function has a defining rule $y = 2x^2$

Determine the defining rule for the new function if the graph of this function is

(i) moved 2 units left,

$$y = 2(x+4)^2$$

(ii) reflected in the y-axis,

$$y = 2(-x)^2$$

(iii) reflected in the x-axis, then moved 3 units right and then 1 unit up.

$$y = -2(x-3)^2 + 1$$

4. [4 marks]

A cubic polynomial intersects the x-axis at $x = -2, 3, 5$.

Given that the graph goes through the point $(4, 2)$ find the equation for the polynomial in the form, $y = ax^3 + bx^2 + cx + d$.

$$(-2, 0)$$

$$(3, 0)$$

$$(5, 0)$$

$$(4, 2)$$

$$y = -\frac{1}{3}x^3 + 2x^2 + \frac{1}{3}x - 10 \leftarrow \begin{matrix} \text{starts} \\ \text{Cubic Reg} \end{matrix}$$

$$y = a(x+2)(x-3)(x-5)$$

$$\text{At } (4, 2) \quad 2 = a(4+2)(4-3)(4-5)$$

$$2 = a(6)(1)(-1)$$

$$2 = -6a$$

$$a = -\frac{2}{6}$$

$$= -\frac{1}{3}$$

$$y = -\frac{1}{3}(x+2)(x-3)(x-5)$$

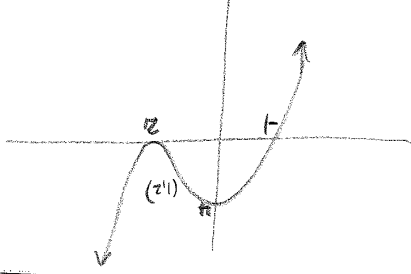
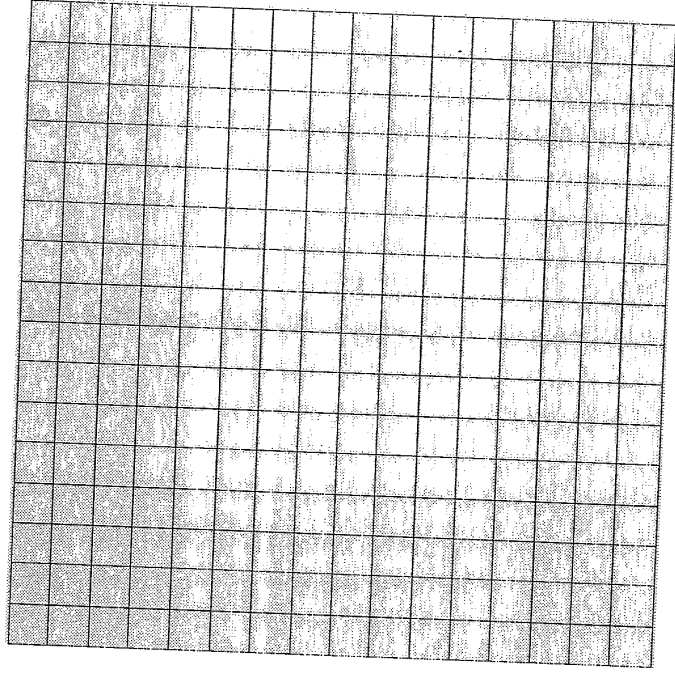
$$= -\frac{1}{3}(x^2+x-6)(x-5)$$

5. [6 marks]

With the aid of a graphic calculator produce a sketch of

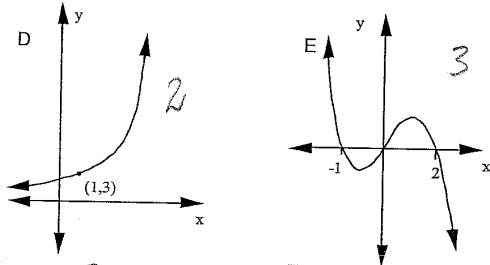
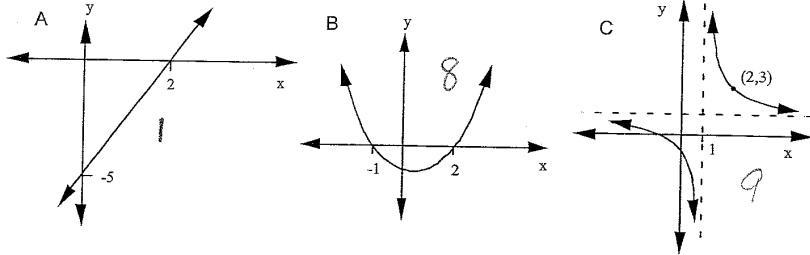
$$y = x^3 - 3x^2 + 4$$

Indicate any turning points, intercepts with the axes and points of inflection. If any rounding is necessary give answers correct to 2 decimal places.



6. [2, 2, 2, 2, 2 marks]

Match each of the graphs below with its corresponding function.
Choose from the functions listed below, where a, b, c, d and e are positive integers:



1. $y = ax - b$ ✓ 2. $y = d^x + 1$ 3. $y = -ax^3 + x^2 + dx$

4. $y = x^3 - ax - b$ 5. $y = c^x - 1$ 6. $y = \frac{1}{x+c}$

7. $y = x^2 + x - e$ 8. $y = x^2 - x - d$ 9. $y = \frac{1}{x-b} + a$

10. $y + ax = b$ 11. $y = \frac{1}{x-a}$ 12. $y = x + c$

$y = (x+1)(x-2)$
 $= x^2 - x - 2$

$y = \frac{1}{x-1} + 1$

7. [2, 3, 3 marks]

State the domain and range for the following functions:

(a) $\{(2, 3), (1, -9), (0, 4), (-3, 4), (-2, 5), (6, 1)\}$

$x = \{2, 1, 0, -3, -2, 6\}$
 $y = \{3, -9, 4, 5, 1\}$

(b) $y = x^2 + 4x + 3$

$\frac{-b}{2a} = \frac{-4}{2} = -2$
 $y = 4 - 8 + 3$
 $y = -1$

$x \in \mathbb{R}$
 $y \geq -1$

(c) $y = \frac{1}{2x-3} + 1$

$x \in \mathbb{R}, x \neq \frac{3}{2}$
 $y \in \mathbb{R}, y \neq 1$

8. [3 marks]

Given the graphs for $f(x) = ax^3 + bx^2 + cx + d$ and $g(x) = ex^2 + fx + g$, for real constants a, b, ..., g, solve to 1 decimal place, the equation $f(x) = g(x)$.

