# ROSSMOYNE SENIOR HIGH SCHOOL

Semester Two Examination, 2010

**Question/Answer Booklet** 

<b>MATHEMATICS</b>
SPECIALIST
3A/3B
Section Two:
Calculator-assumed

Your name:
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Your Teacher (Circle one)

Mr Longley Ms Robinson Mrs Benko

#### Time allowed for this section

Reading time before commencing work: 10 minutes Working time for paper: 100 minutes

# Material required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

Formula sheet (retained from Section One)

#### To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

and up to three calculators satisfying the conditions set by the Curriculum

Council for this course.

## Important note to candidates

No other items may be used in this section of the examination. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

### **Structure of this paper**

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available
Section One: Calculator-free	7	7	50	40
Section Two: Calculator-assumed	11	11	100	80
				120

#### Instructions to candidates

- 1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2010*. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
    Fill in the number of the question(s) that you are continuing to answer at the top of the page.
- 3. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 4. It is recommended that you **do not use pencil** except in diagrams.

# TRIAL EXAMINATION 2010 SECTION TWO

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MATHEMATICS: SPECIALIST 3A/3B CALCULATOR-ASSUMED

**Section Two: Calculator-assumed** 

(80 Marks)

This section has **eleven (11)** questions. Answer **all** questions. Write your answers in the space provided.

Working time for this section is 100 minutes.

Question 8 (6 marks)

The circumference of a circle of radius 25cm passes through the centre of a circle of radius 15cm. Find the area of intersection of the two circles.

Question 9 (7 marks)

(a) For each of the following, state whether or not the function is continuous over the given domain. If not, explain why and state where it is not continuous. (3 marks)

(i) 
$$f(x) = \frac{2}{x-1}, x \ge 0.$$

(ii) 
$$f(x) = |2 - 3x|, -2 < x < 2$$
.

(b) For each of the following, state whether or not the function is differentiable over the given domain. If not, explain why and state where it is not differentiable. (4 marks)

(i) 
$$f(x) = \sqrt{5-x}$$
,  $-5 \le x \le 5$ .

(ii) 
$$f(x) = |x - 4|, x > 0$$
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MATHEMATICS: SPECIALIST 3A/3B CALCULATOR-ASSUMED

Question 10 (8 marks)

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(a) The two distinct solutions of the quadratic equation  $x^2 - 4x + c = 0$  are both complex. Determine all possible values of c. (3 marks)

(b) If v = 3 + i and w = 2 - 3i, find the complex number z such that  $Re(z) \cdot v + Im(z) \cdot \overline{w} + 14 = 0$ . (5 marks)

Question 11 (7 marks)

At midnight a coastal freighter has position vector  $5\mathbf{i} - 11\mathbf{j}$  km and is steaming with a constant velocity vector of  $15\mathbf{i} + 5\mathbf{j}$  km/h. At this time, the distance between it and a dangerous reef located at  $55\mathbf{i} + 6\mathbf{j}$  is decreasing. Let t be the time in hours after midnight.

(a)	Find a vector for the position of the freighter relative to the reef at any time $t$ .	(2 marks)
(b)	When the distance of the freighter from the reef is a minimum, what can be said scalar product of the velocity vector of the freighter and your answer to (a)?	about the (1 mark)
(c)	Use your answers to (a) and (b) to determine the minimum distance the freighte to the reef.	r will come (4 marks)

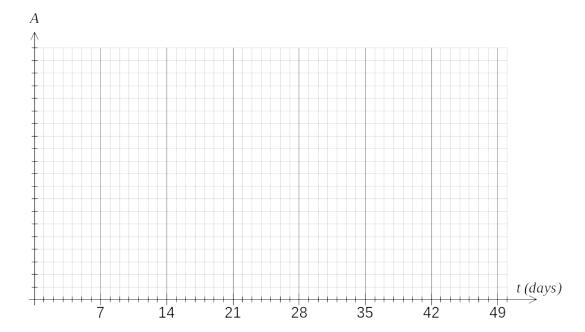
Question 12 (8 marks)

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The initial area of a lupin crop, A, in square metres, infested by cowpea aphids was  $230m^2$ . One week later the area infested had increased to  $270m^2$ .

(a) Assuming that the area infested is increasing exponentially, write a formula for A in terms of t, the number of days since observations began. (3 marks)

(b) Sketch the graph of the area infected against time for the first 7 weeks on the axes below. (3 marks)



(c) If no measures were taken to control the spread of cowpea aphids, after how many days will more than 1400m² of the crop be infested? (2 marks)

Question 13 (5 marks)

The three points A, B and C have position vectors  $\mathbf{a} = 13\mathbf{i} - 3\mathbf{j}$ ,  $\mathbf{b} = -35\mathbf{i} + 17\mathbf{j}$  and  $\mathbf{c} = \mathbf{i} + m\mathbf{j}$  respectively. The point C divides AB internally in the ratio 1: n. Find the values of m and n.

MATHEMATICS: SPECIALIST 3A/3B CALCULATOR-ASSUMED

Question 14 (8 marks)

A current of constant velocity 2 km/h runs parallel to the sides of a straight section of a shipping canal. The skipper of a small boat motors at a speed of 8 km/h on a bearing of 237° in the canal. Due to the current, the boat appears to be moving directly towards a pontoon on the canal edge, which is on a bearing of 245° from the boat.

If the speed of the boat over the canal floor is less than its actual speed through the water determine

(a) the bearing on which the current is flowing.

(5 marks)

(b) the time the boat will take to reach the pontoon, to the nearest minute, if the pontoon is 650m away. (3 marks)

Question 15 (7 marks)

Two functions are given by  $f(x) = \left(1 + \frac{2}{x}\right)^x$  and  $g(x) = \log_e x$ .

(a) Complete the table below, rounding values to 4 decimal places where appropriate.

(3 marks)

X	f(x)	g(f(x))
1		
10		
100		

(b) Determine the limiting value of g(f(x)) as  $x \to \infty$ .

(2 marks)

(c) A conjecture was made that  $f(x) \to e^2$  as  $x \to \infty$ . Explain how your answer from part (b) supports this conjecture. (2 marks)

Question 16 (9 marks)

- (a) A circle with centre C has equation  $|\mathbf{r} \mathbf{i} 2\mathbf{j}| = 5$ .
  - (i) Show that the point A with position vector  $5\mathbf{i} \mathbf{j}$  lies on the circle. (2 marks)

(ii) If AB is a diameter of the circle, determine the position vector of B. (2 marks)

(iii) Determine the vector equation for the tangent to the circle at A. (2 marks)

(b) Given that a = 3i - 2j, b = 5i - j and c = 2i - j, express b in terms of a and c. (3 marks)

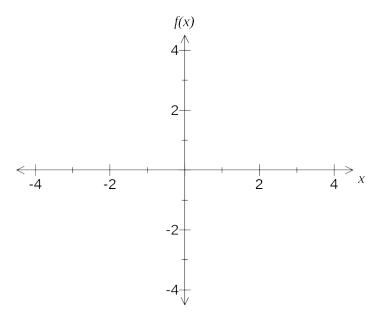
Question 17 (9 marks)

A function is given by  $f(x) = \log_e(x^2 + 1)$ .

(a) Show that f(x) has just one stationary point and find its location. (2 marks)

(b) Show that f(x) has two points of inflection and determine their coordinates in exact form. (2 marks)

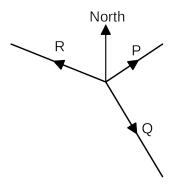
(c) Sketch the graph of f(x) on the axes below. (2 marks)



- (d) On the same axes, sketch the graph of  $f^{-1}(x)$ . (2 marks)
- (e) Explain whether or not  $f^{-1}(x)$  is a function. (1 mark)

Question 18 (6 marks)

A body in equilibrium is acted on by three forces, as shown in the diagram (not to scale).



**P** is of magnitude 350N on a bearing of  $060^{\circ}$ , **Q** is of magnitude 600N on a bearing of  $\theta$ , where  $090^{\circ} < \theta < 180^{\circ}$ , and **R** is of magnitude  $^{X}$ N on a bearing of  $285^{\circ}$ .

Determine x and  $\theta$ .

TRIAL EXAMINATION 2010 SECTION TWO

**Additional working space** 

Question number(s):\_\_\_\_\_

**Additional working space** 

Question number(s):
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