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WACE MATHEMATICS 3C 3D

40 Warks

SECTION ONE: CALCULATOR-FREE

This section has **MINE** (9) questions. Attempt all questions.

Question 1 [3 marks]

Simplify the following:

$$\frac{2a^{3}-5a-3}{2a^{3}-7a^{2}-4a} \qquad x \qquad \frac{16-a^{2}}{6a-18}$$

Question 2 [1 + 1 + Δ = 4 marks]

$$(a) \quad \lambda = \pi - x^3 + e^4$$

$$(p) \quad \lambda = e_{vx-3x_5}$$

(c)
$$\lambda = \sqrt{4x^2 + 2x - 3}$$

Question 3 [2 + 2 + 2 = 6 marks]

Given
$$f(x) = x^2 + 6$$

 $g(x) = \sqrt{x-4}$
 $h(x) = x^2 (x-1)$

find:

(a) $f \circ g(x)$ expressing your answer in a simplified form

(b) the domain and range of f o g(x)

(c) the value(s) of x where g o h(x) exists.

↑ RESPANIOU PAPER 1

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Question 4 [] +] + Δ = 4 marks]

Determine the following integrals:

$$xp \quad x \wedge \varepsilon - \frac{x}{2} \int (b)$$

$$(p) \int_{0}^{2} 3(x + e^{3x}) dx$$

$$\int \frac{(x^4-4x)^3}{(x^4-4x)^3} dx$$

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Hence the sum of two odd integers is even

√ S yd eldisivib si n + m ,S yd eldisivib

= 5(x + y + 1) v

 $(\Gamma + \chi S) + (\Gamma + \chi S) = n + m$

Let m and n be the odd integers

= 2x + 2y + 2

[+ x2 = m

(a) <11

8 (a)
$$f(x) = x^3 - 3x^2$$

8 (a) $f(x) = 3x^2 - 6x$

0 = (x) if nedw string grinnut γ and x strenger in smooth of $1 + \gamma C = 0$

$$2x + 2y + 2$$

$$= 2x + 2y + 1$$

$$= 2(x + y + 1) \times (0,0)$$
Since $x + y + 1$ is an integer and $2(x + y + 1)$ is $x = 0, x = 2$
divisible by $2, y = 0$ (0,0) (2,-4)

 \searrow muminim $\delta = (S)^{n}$ $S = \times$ nodw mumixam ... $6- = (0)^{11}$ 0 = x nadw

O = (x)" I not w not of inflection when f(x) = 0

stnioq (b) Values will occur at end points or critical

$$(k-,2)$$
 : niM
OS- = (S-)

$$S_{-} = \{1\}$$

√ O2- = (2-)f: Sulpy muminiM \wedge 0 = (0)]: əulav mumixaM

9 (a)
$$P(A \cap B) = 0$$
 for mutually exclusive events $V = V \cap B$

tnebneqebni 10} (A) P(B) = (A \cap A) P(b) (d)

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$$(x + 3)(x + 4) = \frac{(x + 3)(x + 4)}{(x + 3)(x + 4)}$$

$$6x + 3x^2 = 8 + 6x + x^2 \checkmark$$

$$8 = {}^2x \Sigma$$

(×)"+ 1/ (9)

(c) $\sqrt{\frac{(x_{\tau} - \tau x)_3}{x_3 - 1}} \quad dx$

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TRIAL EXAMINATION PAPER 1

Question 5 [5 marks]

A shopkeeper imports three varieties of fruit to sell in her shop. The three varieties of fruit were apples, oranges and bananas The weight of apples was four kilograms less than eight times the weight of the oranges. The weight of apples was three times the total weight of the bananas and oranges

If the latest order of fruit was 80 kg, determine by setting up a system of equations how many kilograms of oranges were ordered

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TRIAL EXAMINATION PAPER 1

SOLUTIONS TO TRIAL PAPER

Section One: Calculator Free

$$\frac{1}{(2\alpha^{2} - 7\alpha^{2} - 4\alpha)} \times \frac{(6\alpha - 18)}{(16 - \alpha^{2})}$$

$$= \frac{\alpha(2\alpha + 1)(\alpha - 4)}{(12\alpha + 1)(\alpha - 3)} \times \frac{6(\alpha - 3)}{(4 - \alpha)(4 + \alpha)}$$

$$= \frac{6\alpha(-\alpha + 4)}{(4 - \alpha)(4 + \alpha)}$$

(b)
$$\int_{0}^{2} 3(x + e^{3x}) dx$$

$$= \int_{0}^{2} (3x + 3e^{3x}) dx$$

$$= \left[\frac{3x^{2}}{2} + e^{3x} \right]_{0}^{2}$$

$$= (6 + e^{6}) - (0 + 1)$$

 $= \int 2x^{-\frac{1}{2}} - x^{\frac{1}{3}} dx$

 $= 4x^{\frac{1}{2}} - \frac{3x^{\frac{4}{3}}}{4} + c \checkmark$

$$= e^6 + 5 \checkmark$$

(c) $\int \frac{x^3 - 1}{(x^4 - 4x)^3} dx$

 $= \frac{1}{4} \int \frac{(4x^3 - 4)}{(x^4 - 4x)^3} dx \checkmark$ $= \frac{1}{4} \int (x^4 - 4x)^{-3} (4x^3 - 4) dx$ $= \frac{1}{4} \frac{(x^4 - 4x)^{-2}}{(-2)} + c$

(a) $\int \frac{2}{\sqrt{x}} - 3\sqrt{x}$

(a)
$$y = \pi - x^3 + e^4$$

$$\frac{dy}{dx} = -3x^2 \checkmark$$

$$y = e^{4x - 3x^{2}}$$

$$\frac{dy}{dx} = (4 - 6x)e^{4x - 3x^{2}}$$

(c)
$$y = (4x^2 + 2x - 3)^{1/3}$$

 $\frac{dy}{dx} = \frac{1}{2} [4x^2 + 2x - 3]^{-1/3} [8x + 2] \checkmark \checkmark \qquad 5.$
Let

$$a + b + c = 80 \checkmark$$

 $a = 8c - 4 \checkmark$
 $a = 3(b + c) \checkmark$

$$8c - 4 + b + c = 80$$
$$8c - 4 - 3b - 3c = 0$$

$$9c + b = 84$$
 . ①
 $5c - 3b = 4$ ② \checkmark

$$27c + 3b = 252$$
 ① x 3 = ③
 $5c - 3b = 4$ ②
 $32c = 256$ ③ +②
 $c = 8 \checkmark$

There were 8 kg of oranges

3.

2

(a)
$$f(\sqrt{x-4})$$

$$= (\sqrt{x-4})^2 + 6 \checkmark$$

$$= x + 2 \checkmark$$

(b)
$$D_{fog} = \{x : x \ge 4\} \checkmark$$

$$R_{fog} = \{y : y \ge 6\} \checkmark$$

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(c) Value(s) of x where
$$goh(x)$$
 exist is $x \ge 2 \checkmark \checkmark$

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Question 6 [3 marks]

After investigating the addition of integers, Simon makes a conjecture that: 'The sum of two odd integers is even'

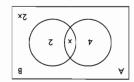
Is Simon correct? Prove using algebra

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Question 9 [1 + 3 = 4 marks]

Given the following Venn diagram showing events A and B



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(a) \forall and β are mutually exclusive

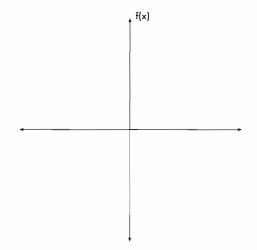
(b) A and B are independent

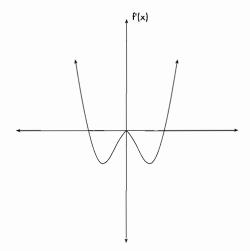
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Question 7 [3 + 2 = 5 marks]

Sketch possible graphs of f(x) and $f^n(x)$ on the axes provided below given the graph of the derivative function f'(x)

(a)



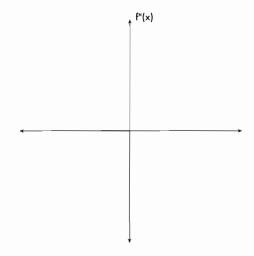


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(b)



Question 8 [4 + 2 = 6 marks]

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(a) Determine all turning points, their nature and points of inflection for the function $f(x) = x^3 - 3x^2$

(b) Find the maximum and minimum values of the function $f(x) = x^3 - 3x^2$ over the interval $-2 \le x \le 1$