

Semester Two Examination, 2021

Question/Answer booklet

MATHEMATICS METHODS UNIT 3 & 4

hand it to the supervisor before reading any further.

Important note to candidates

Special items:

Section One:

To be provided by the candidate Standard items: pens (blue/black prefer correction fluid/tape, er	'ed), pencils (including coloured), sharpener, sser, ruler, highlighters
Materials required/recommend To be provided by the supervisor This Question/Answer booklet Formula sheet	ed for this section
Time allowed for this section Reading time before commencing work: Working time:	firty minutes fifty minutes
Допг Теасher's Name:	
Your Name:	
Calculator-free	

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Max	Mark	noiteauQ	Max	Marks	Question

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material with you,

MATHEMATICS METHODS 2 CALCULATOR-FREE

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	6	6	50	50	33
Section Two: Calculator- assumed	11	11	100	100	67
				Total	100

Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR
 course examinations are detailed in the Year 12 Information Handbook 2019. Sitting this
 examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- 3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

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Additional working spac	Additiona	ı workina	space
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Question	number:	

least one night of 8+ hours of sleep (3 marks)	the student getting at	(c) Determine the probability of during the 4 nights.
(5 marks)		(b) Determine $E(X)$ and $Var(X)$
(S marks)	X to noituding	(a) Determine the probability dis
the sleeping achedule is independent ships as the stable to state at the stable in the	it the number of night	A student gets at least 8 hours of sle set of your A table to fix the fixed X to fixed and the fixed by the fixed X to fixed the fixed X to f
(7 marks)		Question 1
		Working time: 50 minutes.
e an answer. ate this clearly at the top of the page. continue an answer, indicate in the e. give the page number. Fill in the	e if required to continue, ges for planning, indics d to use the space to c answer is continued, i.	Spare pages are included at the end responses and/or as additional space Planning: If you use the spare pa Continuing an answer: If you nee
your answers in the spaces	ver all questions. Write	This section has six questions. Ansuprovided.
(20 Marks)		Section One: Calculator-free
MATHEMATICS METHODS	3	CALCULATOR-FREE

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Question 2

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CALCULATOR-FREE

(9 marks)

(a) $F(x) = \frac{1}{e^{f(x)}}, f(3) = 0$ and f'(3) = -1, determine the value for F'(3). (3 marks)

(b) Determine the gradient of the line tangent to the graph of $y=\ln(\sqrt{3x+1})$ at x=1. (3 marks)

(c) Given that $g(x)=[f(x)]^3$, $f(0)=\frac{-1}{2}$ and $f'(0)=\frac{8}{3}$, determine an equation of the line tangent to the graph of g(x) at x=0. (3 marks)

CALCULATOR-FREE

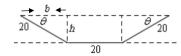
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Question 6

(7 marks)

A trough for holding water is formed by taking a piece of sheet metal $60\,cm$ wide and folding the $20\,cm$ on either end up as shown below.



(a) Determine the expression for the base b and the height h in terms of θ .

(2 marks)

(b) Determine the angle θ that will maximise the amount of water that the trough can hold. Hint: $\sin^2\theta = 1 - \cos^2\theta$.

(5 marks)

(3 marks) (b) Determine the maximum height the projectile will rise and the time when that (5 marks) (a) Determine the velocity at t=4 sand t=6 s. acceleration $a = -20 \text{ m/s}^2$. A projectile is launched upward from ground level with an initial velocity of v_0 =100 m/sand (7 marks) Question 3 MATHEMATICS METHODS g CALCULATOR-FREE

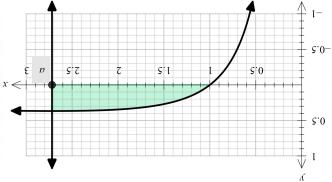
(5 шақка) (c) Determine the speed of the projectile when it hits the ground.

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(d) Determine the value for a, so that the area of the region enclosed by f(x), x-axi sand

x=a is exactly $\frac{1}{2}$. (4 marks)



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CALCULATOR-FREE

Question 4

(8 marks)

The discrete random variable X has a probability distribution as follows.

X	1	2	3	4
P(X=x)	а	b	0.3	С

Where a, b and c are constants.

The cumulative distribution function $C(x) = P(X \le x)$ of X is given in the following table.

X	1	2	3	4
	0.1	0.5	d	1

Where d is a constant.

(a) Determine the values for a, b, c and d.

(4 marks)

(b) Determine E(X).

(2 marks)

(c) Determine $P(3X+2\geq 8)$

(2 marks)

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CALCULATOR-FREE

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(12 marks)

(2 marks)

Question 5

(a) $\frac{d}{dx}(lnx)^2$.

Consider the function $f(x) = \frac{\ln(x)}{x}$, for x > 0.

(b) Determine the coordinate of the turning point of f(x).

(3 marks)

(3 marks)

(c) Determine the coordinate of the point(s) of inflection of f(x).

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