

Semester One Examination,

Question/Answer booklet

# UNIT Methods 1 & 2 **MATHEMATICS**

Section Two:

Calculator-assumed

Изте:

Теасһеґ's Иате:\_

Time allowed for this section

one hundred minutes

Working time: Reading time before commencing work: ten minutes

Materials required/recommended for this section

This Question/Answer booklet To be provided by the supervisor

Formula sheet (retained from Section One)

To be provided by the candidate

correction fluid/tape, eraser, ruler, highlighters Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

and up to three calculators approved for use in this examination drawing instruments, templates, notes on two unfolded sheets of A4 paper, Special items:

Important note to candidates

you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further. No other items may be taken into the examination room. It is your responsibility to ensure that

	Mh			/1
1	\$61	IsioT		91
		23		12
		22		************************************
		21		13
		50		12
		61		11
		18	3	10
	Marks	Question	Marks	Question

## Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free			50	6 <u>8</u>	34 35
Section Two: Calculator-assumed			100	96 92	<i>6</i> 564
				Total	100

### Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR
  course examinations are detailed in the Year 12 Information Handbook 2016. Sitting this
  examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

### MATHEMATICAL METHODS 1 & 2 CALCULATOR - ASSUMED

#### (92 Marks) Section Two: Calculator-assumed

This section has 14 questions. Answer all questions. Write your answers in the spaces

responses and/or as additional space if required to continue an answer. Spare pages are included at the end of this booklet. They can be used for planning your

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the
- in the number of the question that you are continuing to answer at the top of the page. the original answer space where the answer is continued, i.e. give the page number. Fill Continuing an answer: If you need to use the space to continue an answer, indicate in

Working time: 100 minutes.

(2 marks) A circle has a diameter from (2,6) to (10,-9). (8 marks) Question 10

(a) Find its centre and exact radius, hence state the equation of this circle.

 $\frac{1}{\sqrt{2}} = \frac{1}{2} \left( \frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) + \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \right) + \frac{1}{2} \left( \frac{1}$ 1) contect equation stated comect radius. uses the distance formula to find & Exact radius =  $((0-2)^2 + (-q-6)^2) \div 2$ using the midpoint formula to

(b) Determine the centre and the radius of the circle with the equation

$$x^2 - 4x + 4 - 4 + y^2 - 10y + 25 - 25 = -13 \quad \checkmark$$

$$(x - 2)^2 + (y - 5)^2 = -13 + 4 + 25$$

$$(x - 2)^2 + (y - 5)^2 = 16$$
Centre = (2,5) and radius =4
$$Show working$$

$$Show working$$

CALCULATOR-ASSUMED

(3 marks)

(2 marks)

MATHEMATICS METHODS 1 & 2

Cuestion 22

One of the solutions to the equation  $2x^3 + 21x^2 + \epsilon x - 495 = 0$  is x = 5.

Determine the value of c and all other solutions.

$$\frac{1}{\sqrt{(1)}} \int_{\mathbb{R}^{2}} \int_{$$

Question 23 S. + - 10 S 11- = 28 "

Consider the quadratic equation  $2px^2 + (p-1)x + 2p = 0$ .

(b) Find the values of p for which there are 2 solutions.

$$\sqrt{\frac{1}{\varepsilon}} > 1 > \frac{1}{\varepsilon}$$

(c) Find the values of p for which there are no solutions.

(d) Find the value of p for which there is 1 solution.

MATHEMATICS METHODS 1 & 2

Question 11

4 CALCULATOR-ASSUMED

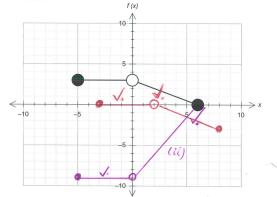
(8 marks)

(a) The point Q has coordinates (-2, 7) and belongs to the furction h(x). Obtain the new coordinates of Q after the following transformations.

(i) 
$$2h(-XL) + 3$$
 (2 marks)

(ii) 
$$h\left(\frac{x}{2}\right) - 1$$
 (i) (2 marks)

(b) The graph of y = f(x) is drawn below.



On the same axes, sketch the graphs of the following functions. Label each one clearly.

(i) 
$$y = f(x-2) - 3$$
 (2 marks)

(ii) A vertical dilation by a factor of 3 and then a horizontal reflection is applied to f(x) (2 marks)

See next page

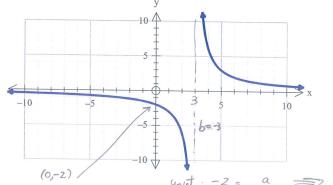
CALCULATOR - ASSUMED

MATHEMATICS METHODS 1 & 2

Question 21

(8 marks)

The graph of the function is defined by  $f(x) = \frac{a}{x+b}$  is shown below.



13

(a) Determine the values of a and b.

y-int: -2= a= (2 marks)

(b) State the domain and range of f(x).

(2 marks)

Dx {R: x +3} /.
Rx {R: y + 0}

(c) Determine the equations of the asymptotes of the graph of y = f(2x).

(2 marks)

 $X = \frac{3}{2}$ 

(d) Describe the transformation required on the graph of y = f(x) to obtain the graph of

i) y = f(x+6). Translation 6 units to the Left / mark)

(ii)  $y = \frac{1}{2}f(x)$ . Dilation  $x \ge parallel$  to y - qx/s. (1 mark)

MATHEMATICS METHODS 1 & 2

CALCULATOR - ASSUMED

Question 12

(8 marks)

cardboard 100 cm by 70 cm as shown below, and folding along the dotted line. An open box is constructed by cutting out square corners, with sides x cm, from a sheet of

100 cm uo 0/ 77-0L 100-22 -001

(a) Find an expression for  $V(cm^3)$ , the volume of the box, in terms of x.

TEND AST 1-(x)(xz-opi)(xz-or) = V

(b) Sketch the graph of V against x without any restriction on x.

(Do not find coordinates of turning points.)

(c) Sketch the graph of V against x with the restriction on x.

(Do not find coordinates of turning points.)

To lacinal place

No 6064 = 1 32.1 and 51.9 () = 4060 = 1.50 intermed. (x) (xz-001) (xz-0L) = +1999 240S

CALCULATOR-ASSUMED

MATHEMATICS METHODS 1 & 2

Question 20

(8 marks) Question 19 15

shead. It there isn't enough snow on the ground, then there is an 70% that an alternate activity on Christmas Day. If there is snow on the ground, there is a 95% chance that sleighing will go Previous winter snow fall readings show that 85% of the time, there is enough snow on the ground However, sleigh rides can only take place when there is enough snow on the ground. As part of their holiday celebrations, they had booked a sleigh ride for Christmas Day. Michael and Emma went to Montalbert in the French Alps for a white winter Christmas.

ot a snowman building competition is organised.

(3 marks)

(8) Complete a tree diagram to represent this situation

Calculate the probability that on Christmas Day Michael and Emma:

(1 mark)

5280°0 = 50.0×58.0 + 8.0×51.0 = (ii) Have no activity planned for that day (S marks)

5270.0 + 540.0

planned for that day. Experience enough snow on the ground, given that they have no activity

(5 marks)

(2 Marks)

Consider the cubic function f(x) has roots at (0,a), (0,a), and (b,0) and (b,0) (a) Fully expand (x+a)(x+a)(x+b)

+ 29+ + x0+ + x+ + x90 + x9+ x0+ x (5 marks)

(J mark) State the coordinate of the y intercept, in terms of a and b

1(907 O) 6 0=x

(2 marks) (c) Given  $f(x) = x^3 + \frac{19}{2}x^2 + 19x - 12$ , find the value of a and b

CALCULATOR-ASSUMED

Question 13

(7 marks)

The square target shown has sides of length 2 metres. Inside the square are a grey circle of radius 1 metre, and a black circle of radius 0.6 metres. Suppose that a dart thrown at the target is equally likely to hit any part of the target

$$A_{\text{rea}} = 2 \times 2$$

$$= 4 m^{2}$$

$$= 0.35 \text{ T}$$

$$= 0.28 \text{ T}$$

$$= 0.28 \text{ T}$$
(a) Calculate the probability that the dart will hit the grey region. (2 ma)

(2 marks)

Area = 
$$\pi \times 1^2 - \pi \times 0.6^2$$
  $P(Grey) = \frac{0.64\pi}{4} = \frac{0.16\pi}{4} \sqrt{0.00}$   
=  $\pi \times 1 - 0.36\pi$  =  $0.5027$ 

(b) Calculate the probability that the dart will hit the white region.

(2 marks)

Area = 
$$4 - \pi \sqrt{.}$$
 :  $P(Wnte) = \frac{4 - \pi}{4} = 1 - \frac{\pi}{4} \sqrt{.}$ 

Suppose that 10 points are awarded if the dart hits the grey region, five points if the dart hits the black region and zero points if the dart hits the white region. If two darts are thrown, state the probability that the total score is 10 points.

Throw, state the probability that the lotal score is to points.

10 pt's = Grey/White or White/Grey

or Black/Black.

= 
$$[0.16 + (1-\frac{\pi}{4})] \times 2 + (0.09\pi) \times (0.09\pi)$$

=  $[0.5027 \times 0.2141] \times 2 + (0.2827) \times (0.2827)$ 

=  $[0.10787] \times 2 + 0.07994$ 

=  $0.2957$  See next page

CALCULATOR - ASSUMED

MATHEMATICS METHODS 1 & 2

### **Question 18**

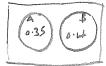
(7 marks)

The probabilities of two events, A and B, are such that P(A) = 0.35 and P(B) = 0.4. Determine;

11

The minimum value of  $P(A \cap B)$ 

(2 marks)



By considering your answer to Part (a), what can you say about events A and B, when  $P(A \cap B)$  is a minimum.

Matually Exclusive 1.

(1 mark)

(1 mark)

P(AUB)= 0-25/

The maximum value of  $P(A \cap B)$ 

(1 mark) max. P(AMB) =035

By considering your answer to Part (d), what can you say about the events of A and B when  $P(A \cap B)$  is a maximum?

ACB A is a Subset of BV

a 6 appears, a person will be selected at random from Group C. random from Group A. If a 4 or 5 appears, a person will be selected at random from Group B. If and 2 girls. An unbiased die is thrown, and if a 1, 2 or 3 appears, a person will be selected at contains 3 boys and 2 girls. Group B contains 1 boy and 3 girls, and Group C contains 2 boys For the purpose of choosing a team for a quiz, a class is split into three groups. Group A 988 (6 marks) ฮ์ส อ ยี Question 14 (3) MATHEMATICS METHODS 1 & 2 CALCULATOR - ASSUMED

1 = (A) d (a) Find the probability that the first person is chosen from Group A. ( ) 2,003

16 P(B) x P(Bd) (S marks) (b) Calculate the probability that a  $\frac{1}{1000}$  from Group B will be chosen when the first choice is

(c) Calculate the probability that a boy will be chosen when the first choice is made.  $\sqrt{(\delta)}$ 

1777 + + x9 + = x7 = (3 marks) or Early or Gray (3 marks)

CALCULATOR-ASSUMED

MATHEMATICS METHODS 1 & 2

(g marks)

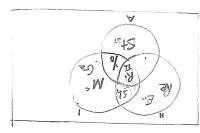
(5 marks)

Question 17

competitions: Have Sum Fun (H), IM2C (I) or APSMO (A). The following teachers are involved in at least one of the following after school Maths

Ms Ensly, Ms Rimando, Mr Strain, Mr Gannon, Mrs Thomas, Mr McClelland, Ms Shah,

Ms Reynolds and Mr Young



The following information about the students is known:

{Ms Reynolds, Ms Ensly} ⊂ H

H n I = {Ms Rimando, Mrs Thomas, Ms Shah}

H n A = {Ms Rimando, Mrs Thomas}

 $H \cup I = \{Mr \ Strain\}$ 

A = {Ms Rimando, Mrs Thomas, Mr Young, Mr Strain, }

I Shah, kimendo, Thomas, lowy, Caryon, Nichellad! Determine:

(2 marks)  $(A \cap I \cap H)n$  (d)

(5 marks)

See next page

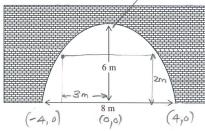
CALCULATOR-ASSUMED

Question 15

(0,6

(8 marks)

The figure below shows the parabolic arch under a railway bridge.



The width of the arch at its lowest level is 8 metres and the highest point of the arch is 6 metres from the ground.

Given that the coordinate of the maximum height of the arch is (0,6). Write a polynomial equation that models the arc under the bridge.

f(x) = a(x+4)(x-4) at (0,6) 6 = a (o+H) (o-H)

$$\alpha = \frac{6}{-16}$$

$$f(x) = -\frac{3}{2}(x+4)(x+4)$$

$$= (\frac{3}{8}/x^2 - 16) = -\frac{3}{8}x^2 + 6$$

Determine showing a clear algebraic method whether a truck with a width of 6 metres and a height of 2 metres can pass through this parabolic arch.

$$f(3) = -\frac{3}{8} \times 3^2 + 6\sqrt{1}$$
 is the height of the arch @3m either side of center of the arch @3m.

If the 2ntruck travels along they centre it will clear the Arch by 0.625m

What is the minimum clearance between the top of the truck and the arc? (1 marks)

See next page

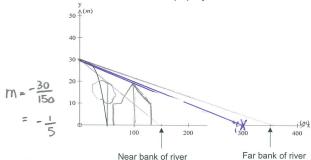
CALCULATOR - ASSUMED

MATHEMATICS METHODS 1 & 2

Question 16

(7 marks)

Louise owns a riverside property that overlooks a vacant block and a river. The diagram below shows a cross-section of the location of the property.



lessas

From Leuise's patio at (0,30) she has a clear view of both the near and far banks of the river with coordinates (150,0) and (350,0) respectively.

Find the equation of the line of sight from the patio to the Near bank of the river (2 marks)

A tree is planted at (50,0) and grows at a rate of 1 meter per year. If this tree grows to a maximum height of 30 meters, how long before the tree obstructs the view of the hear bank?

A house is built on the vacant block with the highest point at (100,20). What would be the nearest point on the river that would be unobstructed by the roof?

$$y_2 = \frac{(30-20)}{(0-100)}x + 30$$
 $y_2 = -\frac{1}{10}x + 30$ 

300m from the origin

 $0 = -\frac{1}{10}x + 30$