



WESLEY COLLEGE

By darling & by doing

Semester Two Examination, 2016

Question/Answer Booklet

MATHEMATICS
METHODS
UNITS 3 AND 4
Section One:
Calculator-free

If required by your examination administrator, please place your student identification label in this box

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Student Number: In figures

In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes
Working time for section: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total				150	100

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Booklet.

Additional working space

Question number: _____

Question 1 (6 marks)

A particle leaves the origin when $t = 1$ and moves in a straight line with velocity at any time t seconds, where $t \geq 1$, given by

$$v(t) = \frac{t^2}{4} + \frac{t}{7} - \frac{4}{7} \text{ ms}^{-1}$$

- (a) Determine the time when the acceleration of the particle is zero. (2 marks)

- (b) Determine the exact displacement of the particle from the origin when $t = 4$. (4 marks)

Question 2

(7 marks)

- (a) Calculate $f'(0)$ when $f(x) = e^{2x}(1 + 5x)^3$.

(3 marks)

- (b) Determine $\frac{d}{dx} \int_x^5 \sqrt{t^2 + 1} dt$.

(2 marks)

- (c) Given $f'(x) = (1 - 2x)^4$ and $f(1) = -1$, determine $f(x)$.

(2 marks)

Question 7

(8 marks)

The Perth sight-seeing bus departs the Elizabeth Quay station every 12 minutes. If a person arrives at the station at a random time to catch the bus their waiting time, X , until the next bus departs is a uniformly distributed random variable.

- (a) Determine

- (i) the probability density function of X and sketch the associated probability density function. (2 marks)

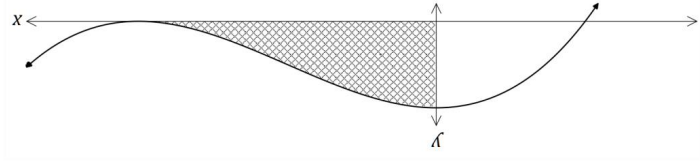
- (ii) the probability that the person has to wait at least 8 minutes. (1 marks)

- (iii) the probability that the person has to wait at least 8 minutes given that she has been waiting at least 6 minutes. (2 marks)

- (b) Someone catches the bus on 3 consecutive days, determine the probability that they have to wait at least 8 minutes on 2 of those days. (3 marks)

Question 6 (8 marks)

The diagram below shows the curve $y = x^3 - 3x^2 + k$, where k is a constant. The curve has a turning point on the x -axis.



- (a) Determine the value of k . (3 marks)

- (b) Determine the set of values of x for which $\frac{dy}{dx}$ is increasing. (2 marks)

- (c) Calculate the area of the shaded region. (3 marks)

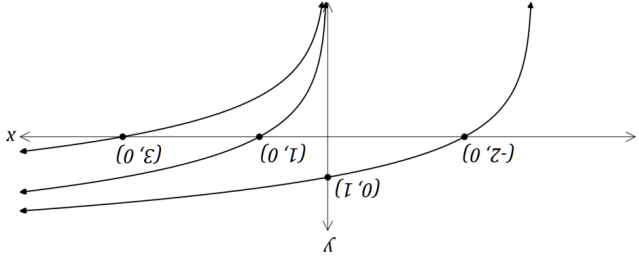
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Question 3 (7 marks)

- (a) The function f is defined by $f(x) = \log_a x$, $x > 0$, where a is a constant, $a > 1$.

The graphs shown below have equations, not in order:

$y = f(x)$, $y = f(x + b)$ and $y = f(x) + c$, where b and c are constants.



Determine the values of the constants a , b and c .

(4 marks)

- (b) Determine (1 mark)

- (i) the equation of the asymptote of the graph of $y = \log_e(x - 3) - 2$.

(1 mark)

- (iii) the coordinates of the y -intercept of the graph of $y = \log_2(x + 8) - 5$.

(2 marks)

See next page

Question 4

(8 marks)

A curve has equation $y = 2x^5 - 5x^4 + 10$.

- (a) Point A lies on the curve at $(-1, 3)$. Use the increments formula $\delta y \approx \frac{dy}{dx} \times \delta x$ to estimate the y -ordinate of point B that has an x -ordinate of -0.99 . (4 marks)

- (b) Point C also lies on the curve, at $(2, -6)$. Verify that C is a stationary point and determine its nature. (4 marks)

Question 5

(8 marks)

- (a) Determine the coordinates of the root of the graph of $y = \log_3(2x + 1) - 2$. (3 marks)

- (b) Solve $\log_5 x + \log_6(x - 5) = 2$ (2 marks)

- (c) If $\log_3 x + \log_3 y - 2 = \log_3 M$, determine an expression for M in terms of x and y . (3 marks)