



PERTH MODERN SCHOOL

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INDEPENDENT PUBLIC SCHOOL

Semester Two Examination, 2020

Question/Answer booklet

MATHEMATICS SPECIALIST

UNIT 1&2

Section Two:

Calculator-assumed

Your Name _____

Your Teacher's Name _____

Time allowed for this section

Reading time before commencing work: ten minutes
Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet
Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Marks	Max	Question	Marks	Max
9		10	16		6
10		6	17		6
11		5	18		8
12		9	19		8
13		7	20		8
14		10	21		7
15		10			

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	54	36
Section Two: Calculator-assumed	13	13	100	100	64
Total					100

Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you **do not use pencil**, except in diagrams.
- The Formula sheet is **not** to be handed in with your Question/Answer booklet.

See Next Page

This section has **13 (thirteen)** questions. Answer **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

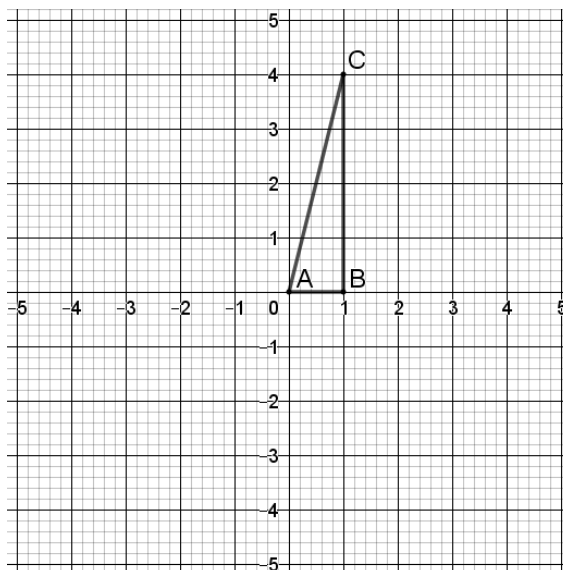
- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 100 minutes.

Question 9 (2.2.1, 2.2.5-2.2.7, 2.2.9, 2.2.10)

(10 marks)

Consider the triangle with vertices $A(0,0)$, $B(1,0)$ and $C(1,4)$, plotted below.



- a) The triangle is transformed by a matrix M to give an image with vertices $A'(0,0)$, $B'(0,1)$ and $C'(-4,1)$. Write down the matrix M . (2 marks)

Solution	
M is a rotation by $\frac{\pi}{2}$, and so	
$M = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$	
Specific behaviours	
✓ states transformation or sketches diagram ✓ states correct matrix	

- b) Triangle $A'B'C'$ (the **image** from part (a)) is transformed by a matrix N to give an image with vertices $A''(0,0)$, $B''(0,-1)$ and $C''(-4,-1)$. Write down the matrix N . (2 marks)

Solution
N is a reflection through $y=0$, and so $N = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$
Specific behaviours
<ul style="list-style-type: none"> ✓ states transformation or sketches diagram ✓ states correct matrix

- c) **Hence** write down the matrix P which would transform triangle ABC to triangle $A''B''C''$, showing your working. (3 marks)

Solution
$P = NM \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$
Specific behaviours
<ul style="list-style-type: none"> ✓ multiplies N and M (in either order) ✓ multiplies in correct order ✓ states correct matrix

- d) The triangle ABC is transformed by a matrix Q to a triangle with coordinates $A'''(0,0)$, $B'''(2,1)$ and $C'''(2,7)$. State the value of $\det Q$, given that $\det Q > 0$, justifying your answer. (3 marks)

(Solution
ΔABC has area $\frac{1}{2} \times 1 \times 4 = 2$ and $\Delta A'''B'''C'''$ has area $\frac{1}{2} \times 6 \times 2 = 6$. Hence $ \det Q = \frac{6}{2} = 3$ and since $\det Q > 0$, it follows that $\det Q = 3$.
Specific behaviours
<ul style="list-style-type: none"> ✓ determines areas of ΔABC and $\Delta A'''B'''C'''$ ✓ divides 6 by 2 ✓ states $\det Q = 3$

Question 10 (1.1.1, 1.1.2, 1.1.3, 1.1.4)

(6 marks)

The genetic code is a set of rules defined by the four nucleotides of DNA, represented by the letters A, T, C and G. Three-letter nucleotide sequences are made from the four nucleotides.

- a) With no restrictions, how many 3-letter nucleotide sequences are possible in DNA?

(1 mark)

Solution
$4 \times 4 \times 4 = 64$
Specific Behaviours
✓ correct number

- b) How many 3-letter nucleotide sequences start with A and end with C?

(2 marks)

Solution
$1 \times 4 \times 1 = 4$
Specific Behaviours
✓ uses multiplicative reasoning
✓ correct number

- c) How many 3-letter nucleotide sequences have a G at least twice?

(3 marks)

Solution
$1 + \binom{3}{1} \times 3 = 10$
Specific Behaviours
✓ identify two cases
✓ uses addition principle
✓ correct number

Question 11 (2.3.7-2.3.11, 2.3.13-2.3.16)

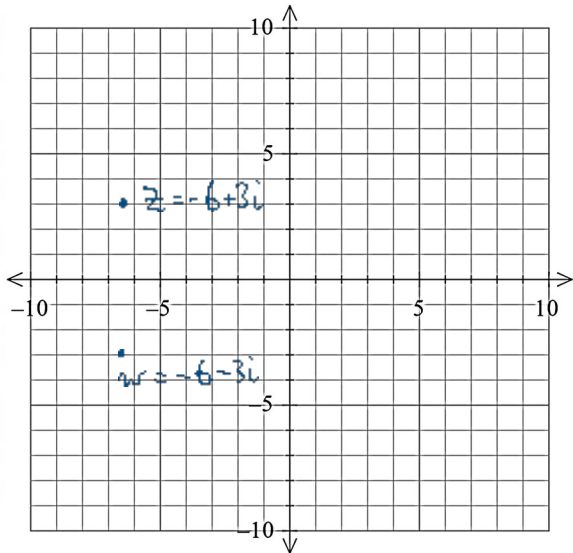
(5 marks)

Consider the following quadratic equation where c is a real number.

$$x^2 + 12x + c = 0$$

One of the solutions to this equation is $z = -6 + 3i$.

- a) Write down the other solution w of the equation, and plot (and label) both solutions in the complex plane below. (3 marks)

Solution
<div style="text-align: center; margin-bottom: 10px;">$w = \bar{z} = -6 - 3i$</div> 
Specific behaviours
<ul style="list-style-type: none"> ✓ writes correct value for w ✓ plots and labels z in correct position ✓ plots and labels w in correct position

- b) Hence (or otherwise) determine the value of c .

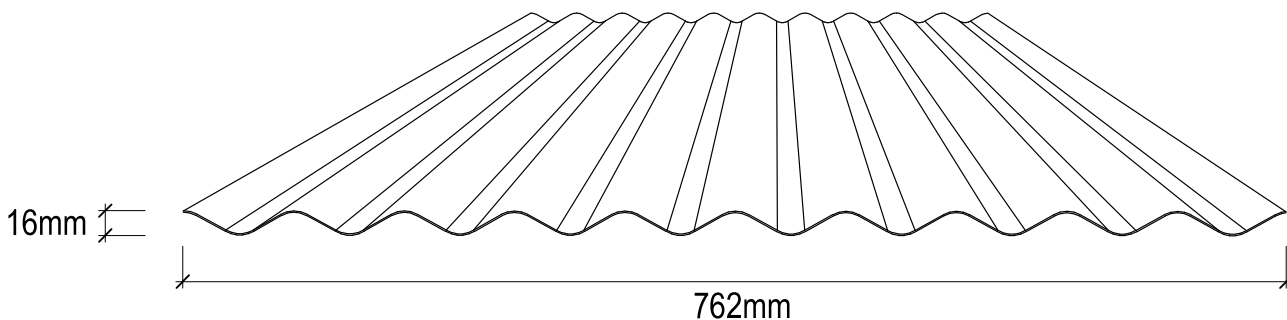
(2 marks)

Solution
$c = z \times w = (-6 + 3i)(-6 - 3i) = 36 + 9 = 45$
Specific behaviours
<ul style="list-style-type: none"> ✓ multiplies z and w ✓ states $c = 45$

Question 12 (2.1.1-2.1.2, 2.1.9)

(9 marks)

A roofing panel with the dimensions shown below has been left on the ground. An ant is walking across the top of the panel from the left end to the right end.



a) Write a function in the form

$$h = a \cos(b(x - c)) + d$$

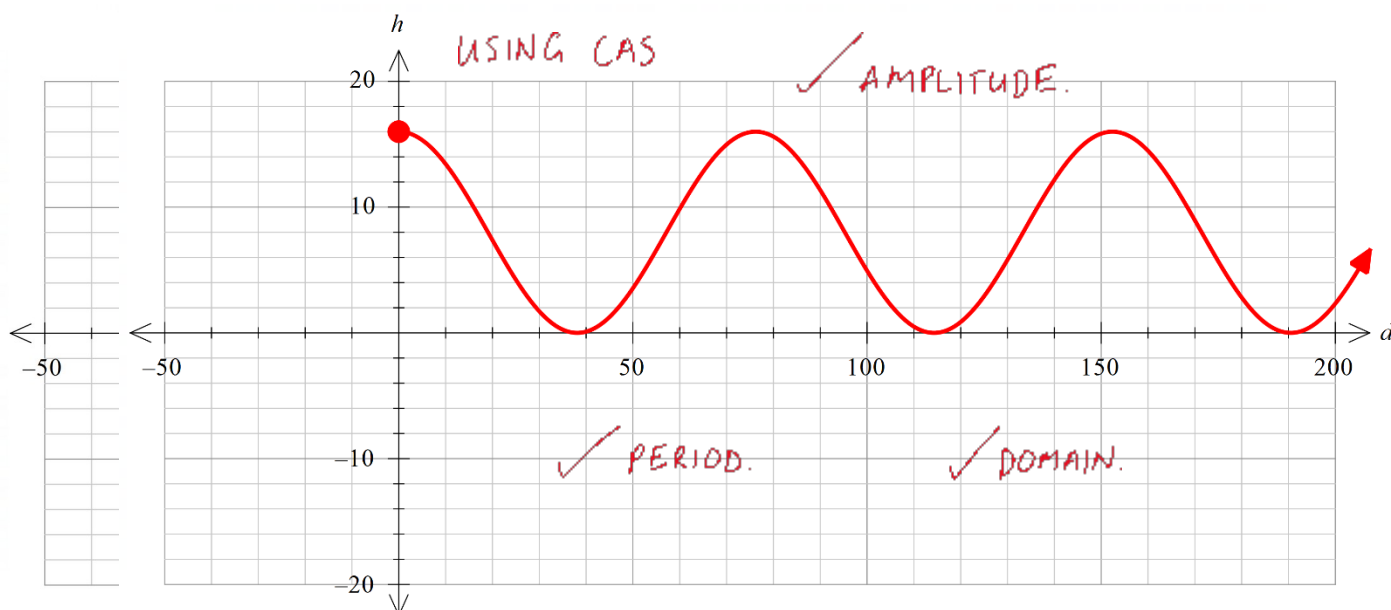
modelling the height h mm that the ant is above the ground in terms of the horizontal distance x mm that the ant is from the left end of the panel. Specify the domain of the function. (Assume the panel has negligible thickness.) (3 marks)

$$h(x) = 8 \cos\left(\frac{2\pi}{762}x\right) + 8, \quad \{x \in \mathbb{R} : 0 \leq x \leq 762\}.$$

✓
✓
✓
VERT DIL
+ TRANS

b) Graph the function on the axes below.

(3 marks)



- c) The ant gets tired and stops to rest the third time he is climbing at a height of 12 mm. How far (horizontally) does he have left to walk? (3 marks)

USING CAS. ✓ SOLVES $h(x) = 12$ ✓ DIST = $762 - 215.9$
 $x = 215.9$. ✓ 6TH SOLUTION. ✓ = 546.1 mm. ✓

Question 13 (2.1.4)

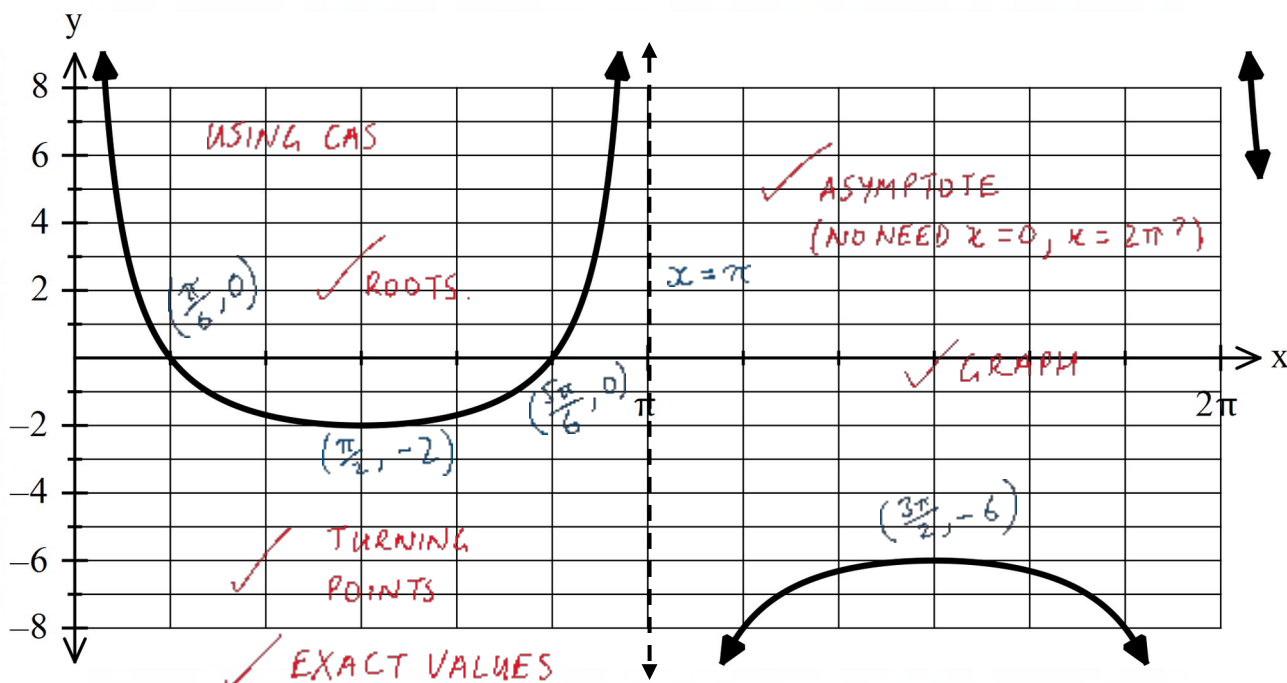
(7 marks)

- a) Describe the transformation of $y = \csc(x)$ to $y = 2\csc(x) - 4$. (2 marks)

1. DILATE BY A FACTOR OF 2 FROM THE X-AXIS ✓
 2. TRANSLATE 4 UNITS DOWN. ✓

- b) Sketch $y = 2\csc(x) - 4$ on the graph shown, labelling all key features. (5 marks)

(5 marks)



Question 14 (1.2.6-1.2.13)

(10 marks)

- a) Three vectors are given by $a=5i-12j$, $b=-15i+10j$ and $c=-7i+yj$ where y is a constant.

- i) Determine the vector projection of b on a (give components as exact values).
(3 marks)

Solution	
$\hat{a} = \frac{1}{13}(5i - 12j)$	
$b \cdot \hat{a} = -15$	
$(b \cdot \hat{a})\hat{a} = \frac{-75}{13}i + \frac{180}{13}j$	
Specific behaviours	
✓	States unit vector for a
✓	States $b \cdot \hat{a}$
✓	States projection as a vector

- ii) Find y if the angle between b and c is 45° .
(3 marks)

Solution	
$\cos(45) = \frac{(-15i+10j) \cdot (-7i+yj)}{\sqrt{-15i+10j} \cdot \sqrt{-7i+yj}}$	
$y=35 \text{ or } y = \frac{-7}{5}$	
Specific behaviours	
✓	Uses scalar product
✓	States one solution
✓	States second solution

$$[-15 \ 10] \Rightarrow b$$

$$[-15 \ 10]$$

$$[-7 \ y] \Rightarrow c$$

$$[-7 \ y]$$

$$\text{norm}(b) * \text{norm}(c) * \cos(45) = \text{dotP}(b, c)$$

$$\frac{5 \cdot \sqrt{26 \cdot (y^2 + 49)}}{2} = 10 \cdot y + 105$$

$$\text{solve}(\text{ans}, y)$$

$$\left\{ y=35, y=-\frac{7}{5} \right\}$$

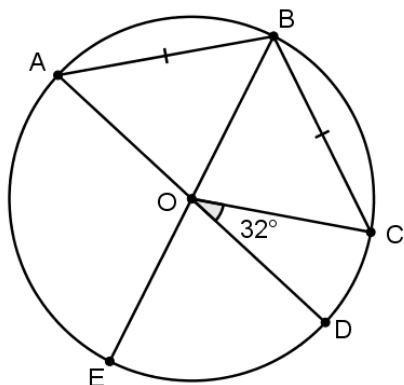
- b) Vectors $ai+(a-3)j$ and $(a-7)i+5j$ are perpendicular. Find the value(s) of a and the corresponding pairs of vectors.
(4 marks)

Solution	
$\begin{pmatrix} a \\ a-3 \end{pmatrix} \cdot \begin{pmatrix} a-7 \\ 5 \end{pmatrix} = a^2 - 2a - 15 = 0$	
$(a+3)(a-5) = 0$	
$a = -3 \text{ or } a = 5$	
$\text{if } a = -3, \text{ the vectors are } -3i - 6j \text{ and } -10i + 5j$	
$\text{if } a = 5, \text{ the vectors are } 5i + 2j \text{ and } -2i + 5j$	
Specific behaviours	
✓	Uses (dot product = 0) to form quadratic equation
✓	Solves for two values of a
✓	States one pair of vectors
✓	States two pairs of vectors

Question 15 (1.3.6-1.3.15)

(10 marks)

- a) Consider the diagram below. \overline{AD} and \overline{BE} are diameters of the circle with centre O , $\angle COD = 32^\circ$ and C lies on the circumference of the circle such that $AB = BC$.



Determine the sizes of the following angles

- i) $\angle AOB$

(2 marks)

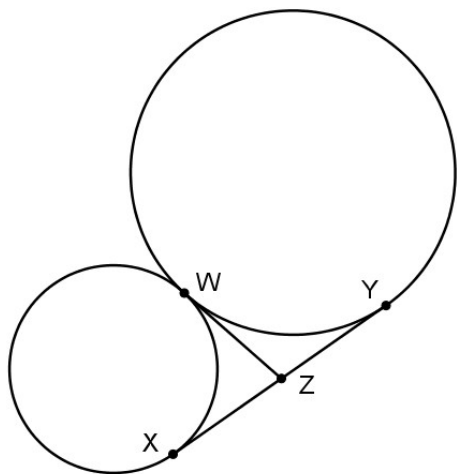
Solution	
$\angle AOB = \angle BOC$	
$\angle AOB + \angle BOC + 32 = 180$	
$\angle AOB = \frac{180 - 32}{2}$	
$\angle AOB = 74^\circ$	
Specific behaviours	
✓	Uses congruent angles
✓	Calculates angle

- ii) $\angle CAE$

(3 marks)

Solution	
$\angle DOE = \angle AOB = 74^\circ$	
$\angle COE = 74 + 32 = 106^\circ$	
$\angle CAE = \frac{106^\circ}{2}$	
$\angle CAE = 53^\circ$	
Specific behaviours	
✓	Indicates size of $\angle DOE$
✓	Uses relationship between angle at centre and at circumference
✓	Calculates angle

- b) In the diagram below, W is the single point of intersection of the two circles. The segment \overline{XY} is tangent to both circles, intersecting with the circles at X and Y . Segment \overline{WZ} is also tangent to both circles, intersecting with \overline{XY} at Z . Prove that $\triangle XWY$ is a right triangle. (5 marks)

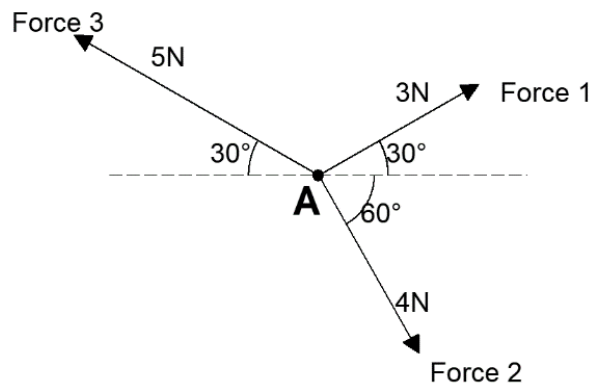


Solution	
$ZX = ZW$ and $ZW = ZY$ (tangents from a common point) Hence X , W and Y lie on a circle with centre Z . \overline{XY} is a diameter of this circle and so $\angle XWY$ is an angle in a semicircle. Hence $\angle XWY = 90^\circ$. It follows that $\triangle XWY$ is a right triangle.	
Specific behaviours	
✓	Notes that $XZ = ZW = ZY$
✓	Gives reason for above
✓	States that X , W and Y lie on a circle with centre Z
✓	States that $\angle XWY$ is an angle in a semicircle
✓	Concludes that $\angle XWY = 90^\circ$

Question 16 (1.2.2, 1.2.8, 1.2.14)

(6 marks)

Three forces act on the point A as shown. What is the magnitude of the resultant force acting on A , and in what direction would A move under these three forces? Give your answers to 2 decimal places, with the direction as an angle measured anticlockwise from the right (like the 30° angle for Force 1).



Solution	
Force 1	$3 \cos 30^\circ i + 3 \sin 30^\circ j$
Force 2	$4 \cos 60^\circ i - 4 \sin 60^\circ j$
Force 3	$-5 \cos 30^\circ i + 5 \sin 30^\circ j$
Resultant force:	
	$F = \left(\frac{3\sqrt{3}}{2} + \frac{4}{2} - \frac{5\sqrt{3}}{2} \right) i + \left(\frac{3}{2} - \frac{4\sqrt{3}}{2} + \frac{5}{2} \right) j = (2 - \sqrt{3})i + (4 - 2\sqrt{3})j$
Magnitude of force:	
	$ F = \sqrt{(2 - \sqrt{3})^2 + (4 - 2\sqrt{3})^2} \approx 0.60 \text{ N}$
Direction of force:	
	$\tan^{-1} \left(\frac{4 - 2\sqrt{3}}{2 - \sqrt{3}} \right) \approx 63.43^\circ$
Therefore the direction is	63.43°
Specific behaviours	
<ul style="list-style-type: none"> ✓ writes correct vector expression for at least one force (accept expressions using polar angles e.g. Force 2 $4 \cos 300^\circ i + 4 \sin 300^\circ j$) ✓ writes correct vector expressions for at least two forces ✓ writes correct vector expressions for all three forces ✓ determines vector expression for resultant force ✓ states correct magnitude of resultant force ✓ state correct direction of resultant force 	

Question 17 (2.2.1, 2.2.2)

(6 marks)

- a) Given invertible $n \times n$ matrices A , B , C and X with $AX - B = CBX$, write X in terms of A , B and C .

(3 marks)

Solution
$AX - B = CBX \quad AX - CBX = B \quad (A - CB)X = B \quad X = (A - CB)^{-1}B$
Specific behaviours
<ul style="list-style-type: none"> ✓ collects terms with X on LHS ✓ factorises X out on the right ✓ multiplies both sides by $(A - CB)^{-1}$

- b) Solve the following matrix equation for Y

$$3Y - Y \begin{bmatrix} 1 & -3 \\ 1 & 6 \end{bmatrix} = 5I$$

(3 marks)

Solution
$3Y - Y \begin{bmatrix} 1 & -3 \\ 1 & 6 \end{bmatrix} = 5I$ $Y \left(3I - \begin{bmatrix} 1 & -3 \\ 1 & 6 \end{bmatrix} \right) = 5I \quad Y \begin{bmatrix} 2 & 3 \\ -1 & -3 \end{bmatrix} = 5I \quad Y = 5I \begin{bmatrix} 2 & 3 \\ -1 & -3 \end{bmatrix}^{-1} \quad \text{; } \frac{5}{3} \begin{bmatrix} 3 & 3 \\ -1 & -2 \end{bmatrix}$
Specific behaviours
<ul style="list-style-type: none"> ✓ factorises Y out on the left ✓ evaluates $3I - \begin{bmatrix} 1 & -3 \\ 1 & 6 \end{bmatrix}$ ✓ multiplies both sides by $\begin{bmatrix} 2 & 3 \\ -1 & -3 \end{bmatrix}^{-1}$ and obtains correct answer

Question 18 (1.1.7, 1.1.8)

(8 marks)

Four Year 10 students and eleven Year 11 students from Western Australia are nominated as candidates for a Mathematics Summer Camp. How many ways can a group of four participants be selected:

a) without restriction?

(2 marks)

Solution
$\binom{15}{4} = 1365$
Specific Behaviours
✓ correct expression ✓ correct number

b) if the only student from Bunbury must be included?

(2 marks)

Solution
$\binom{1}{1} \binom{14}{3} = 364$
Specific Behaviours
✓ correct expression ✓ correct number

c) if there must be exactly two Year 11 students?

(2 marks)

Solution
$\binom{11}{2} \binom{4}{2} = 330$
Specific Behaviours
✓ correct expression ✓ correct number

d) if there must be at least one Year 10 student?

(2 marks)

Solution
$\binom{15}{4} - \binom{11}{4} = 1035$

Specific Behaviours
✓ correct expression
✓ correct number

Question 19 (1.1.5, 1.1.9)

(8 marks)

a) How many integers between 1 and 101 are multiples of 5, 6 or 7?

(4 marks)

Solution
<p>Multiples of 5 : $100 \div 5 = 20$ Multiples of 6 : $100 \div 6 = 16$ (rounded down) Multiples of 7 : $100 \div 7 = 14$ Multiples of 30 and 6 : $100 \div 30 = 3$ Multiples of 35 and 7 : $100 \div 35 = 2$ Multiples of 42 and 7 : $100 \div 42 = 2$ Multiples of 210 and 7 : 0 Multiples of 5, 6, or 7 : $20 + 16 + 14 - 3 - 2 - 2 + 0 = 43$</p>
Specific Behaviours
<p>✓ finds multiples of 5, 6, 7 respectively ✓ finds multiples of 30, 35, 42 respectively ✓ uses inclusion-exclusion principle ✓ correct number</p>

b) Use the fact that ${}^nC_r = \frac{n!}{(n-r)!r!}$ to show that ${}^{n-1}C_{r-1} \times n = {}^nC_r \times r$.

(4 marks)

Solution
$LHS = \frac{(n-1)!}{[n-1-(r-1)]!(r-1)!} \times n$ $= \frac{(n-1)! \times n}{(n-r)!(r-1)!}$ $= \frac{n!}{(n-r)!(r-1)!}$ $= \frac{n!r}{(n-r)!r(r-1)!}$ $= \frac{n!}{(n-r)!r!} \times r$ $= {}^nC_r \times r$
Specific Behaviours
<p>✓ uses ${}^nC_r = \frac{n!}{(n-r)!r!}$</p>

- ✓ writes $n(n-1)!$ as $n!$
- ✓ multiplies by $\frac{r}{r}$
- ✓ writes $r(r-1)!$ as $r!$

Question 20 (2.2.1-2.2.10)

(8 marks)

Let $A = \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$.

- a) Calculate A^2 (that is, $A \times A$). Show working and simplify your answer. (3 marks)

Solution	
$A^2 = \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix} \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix} \rightarrow \begin{bmatrix} \cos^2 \alpha - \sin^2 \alpha & -\cos \alpha \sin \alpha - \cos \alpha \sin \alpha \\ \cos \alpha \sin \alpha + \cos \alpha \sin \alpha & -\sin^2 \alpha + \cos^2 \alpha \end{bmatrix}$ $\rightarrow \begin{bmatrix} \cos 2\alpha & -\sin 2\alpha \\ \sin 2\alpha & \cos 2\alpha \end{bmatrix}$	
Specific behaviours	
<ul style="list-style-type: none"> ✓ writes unsimplified product (2nd line) with at least 2 entries correct ✓ writes unsimplified product (2nd line) with all entries correct ✓ simplifies using double angle formulas 	

- b) Calculate the product A^3 by multiplying your answer to part (a) by A (you do not need to simplify your answer). (2 marks)

Solution	
$A^3 = \begin{bmatrix} \cos 2\alpha & -\sin 2\alpha \\ \sin 2\alpha & \cos 2\alpha \end{bmatrix} \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$ $\rightarrow \begin{bmatrix} \cos 2\alpha \cos \alpha - \sin 2\alpha \sin \alpha & -\cos 2\alpha \sin \alpha - \sin 2\alpha \cos \alpha \\ \sin 2\alpha \cos \alpha + \cos 2\alpha \sin \alpha & -\sin 2\alpha \sin \alpha + \cos 2\alpha \cos \alpha \end{bmatrix}$	
Specific behaviours	
<ul style="list-style-type: none"> ✓ at least 2 entries correct in product ✓ all entries correct in product 	

- c) Determine a value of α (with $0 < \alpha < 2\pi$) such that $A^3 = I$. Justify your answer by referring to the linear transformation corresponding to the matrix A . (3 marks)

Solution	
<p>If $\alpha = \frac{2\pi}{3}$ then $A^3 = I$.</p> <p>Since A represents a rotation by α, A^3 represents 3 rotations by α applied in sequence; that is, A^3 is a rotation by 3α. Thus if $\alpha = \frac{2\pi}{3}$, A^3 is a rotation by 2π, which is equivalent to a rotation by 0, and therefore $A^3 = I$.</p>	
Specific behaviours	

✓ states $\alpha = \frac{2\pi}{3}$

✓ notes that A represents a rotation by α

✓ notes that A^3 is 3 rotations by α , or a single rotation by 3α

Question 21 (1.2.2, 1.2.3, 1.2.7, 1.2.9, 1.2.14)

(7 marks)

An octopus, which can swim with a steady speed of 3.5 m/s through still water, leaves its home at O to visit a sea anemone at S .

The position vector of S relative to O is $165i - 212j$ m, and a current with velocity $-2.3i + 1.1j$ m/s is flowing.

- a) Find the velocity vector v , in the form $ai + bj$, that the octopus should aim to swim with in order to reach the sea anemone in the shortest possible time. (Give a and b to 2 decimal places.)

(5 marks)

Solution	
We require	$ai + bj + (-2.3i + 1.1j) = \lambda(165i - 212j)$
so	$a - 2.3 = 165\lambda$ $b + 1.1 = -212\lambda$
We also know that	$a^2 + b^2 = 3.5^2$
Solving these three equations simultaneously and taking the solution with $\lambda > 0$ gives	$v = 2.93i - 1.91j$
Specific behaviours	
<ul style="list-style-type: none"> ✓ equates sum of v and current velocity to a scalar multiple of displacement vector ✓ equates components to get 2 linear equations ✓ states equation $a^2 + b^2 = 3.5^2$ ✓ states at least one of $v = 2.93i - 1.91j$ and $v = -1.13i + 3.31j$ ✓ states $v = 2.93i - 1.91j$ (i.e. solution corresponding to positive value of λ) 	

- b) Determine the time taken (to the nearest second) for the octopus to reach the sea anemone if it aims to swim with the velocity found in part (a).

(2 marks)

Solution	
<p>EITHER</p> <p>$\lambda = 3.8 \times 10^{-3}$ (from part (a))</p> <p>Hence total time will be $\frac{1}{\lambda} = 261$ s</p>	
<p>OR</p> <p>Horizontal component of resultant velocity $\rightarrow 2.93 - 2.3 = 0.63$</p> <p>$\frac{165}{0.63} = 262$ s</p>	
<p>OR</p> <p>$v + (-2.3i + 1.1j) = 1.0262 165i - 212j = 268.6429$</p> <p>Total time $\rightarrow \frac{268.6429}{1.0262} = 262$ s</p>	
Specific behaviours	
<ul style="list-style-type: none"> ✓ shows appropriate calculation ✓ states 261 s or 262 s 	

CALCULATOR ASSUMED

19MATHEMATICS SPECIALIST UNITS 1&2
END OF QUESTIONS

CALCULATOR ASSUMED
Additional working space

20MATHEMATICS SPECIALIST UNITS 1&2

Question number: _____

CALCULATOR ASSUMED

21MATHEMATICS SPECIALIST UNITS 1&2

Additional working space

Question number: _____

CALCULATOR ASSUMED

22MATHEMATICS SPECIALIST UNITS 1&2

Additional working space

Question number: _____