



Semester One Examination, 2020

Question/Answer booklet

MATHEMATICS METHODS

UNIT 3

Section One:

Calculator-free

Your Name: _____

Your Teacher's Name: _____

Time allowed for this section

Reading time before commencing work: five minutes
Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet
Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Marks	Max	Question	Mark	Max
1		5	5		8
2		7	6		10
3		7	7		6
4		5			

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	48	34
Section Two: Calculator-assumed	12	12	100	93	66
Total					100

Instructions to candidates

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued. I.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

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Additional working space

Question number: _____

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(10 marks)

Question 6
 A discrete random variable X has the probability function

$$P(X = x) = \begin{cases} k(1 - x)^2 & x = 1, 0, 1, \text{ and } 2 \\ 0 & \text{otherwise} \end{cases}$$

(a) Show that $k = \frac{1}{6}$

(3 marks)

(b) Find $E(X)$.

(2 marks)

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(7 marks)

Question 3
 The diagram below shows the curve $y = (3 - 2x)^3$ and the tangent line to the curve at $\left(\frac{1}{2}, 8\right)$.

(a) Find the equation of this tangent, giving your answer in the form $y = mx + c$.

(3 marks)

(b) Find the area of the shaded region.

(4 marks)

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(6 marks)

Question 7
 Let $f(x)$ be a non-zero function such that $f'(x) = |f(x)|^2$.

(a) Determine an expression for $\frac{d}{dx} \frac{1}{f'(x)}$.

(3 marks)

(b) Determine an expression for $f(x)$ using the result from (a), or otherwise, given $f(0) = \frac{1}{2}$.

(3 marks)

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(7 marks)

Question 2
 Suppose that $f(x)$ and $g(x)$ are differentiable functions and that $h(x) = f(x)g(x)$. You are given the following table of values.

x	-1
$h(x)$	-9
$g(x)$	9
$f(x)$	-2
$h'(x)$	-20

(a) Determine the value for $f'(-1)$ and hence determine $\frac{d}{dx} [f(x)h(x)]$ when $x = -1$.

(3 marks)

(b) Determine the value for $\frac{d}{dx} [h(x)]^2$ when $x = -1$.

(2 marks)

(c) Determine the value for $T'(-1)$, given that $T(x) = f(|f(x)|)$.

(2 marks)

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(d) Find $\ln(1 - 3x)$

(3 marks)

(c) Show that $E(X^2) = \frac{4}{3}$

(2 marks)