



## Mathematics: Units 3A and 3B Formula sheet

### Number and algebra: Estimation and calculation

#### Index laws:

For  $a, b > 0$  and  $m, n$  real,

$$a^m a^n = a^{m+n}$$

$$a^m b^m = (ab)^m$$

$$(a^m)^n = a^{mn}$$

$$a^{-m} = \frac{1}{a^m}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$a^0 = 1$$

For  $m$  an integer and  $n$  a positive integer  $a^{\frac{m}{n}} = \sqrt[n]{a^m} = (\sqrt[n]{a})^m$

### Number and algebra: Calculus

#### Differentiation

If  $f(x) = y$ , then  $f'(x) = \frac{dy}{dx}$

If  $f(x) = x^n$ , then  $f'(x) = nx^{n-1}$  and if  $y = x^n$ , then  $\frac{dy}{dx} = nx^{n-1}$

#### Product rule:

If  $h(x) = f(x)g(x)$ , then  $h'(x) = f'(x)g(x) + f(x)g'(x)$

If  $y = uv$  then  $\frac{dy}{dx} = v \frac{du}{dx} + u \frac{dv}{dx}$

#### Integration

$$\int x^n dx = \frac{x^{n+1}}{n+1} + c \quad n \neq -1$$

### Space and measurement: Measurement

In any triangle  $ABC$ ,

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\text{Area} = \frac{1}{2}ab \sin C$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

**Space and measurement: Measurement**

**Trapezium:** Area =  $\frac{1}{2} (a + b) \times \text{height}$ , where  $a$  and  $b$  are the lengths of the parallel sides

**Prism:** Volume = Area of base  $\times$  height

**Cylinder:** Total surface area =  $2\pi r h + 2\pi r^2$

$$\text{Volume} = \pi r^2 \times h$$

**Pyramid:** Volume =  $\frac{1}{3} \times \text{area of base} \times \text{height}$

**Cone:** Total surface area =  $\pi r s + \pi r^2$ ,  $s$  is the slant height

$$\text{Volume} = \frac{1}{3} \times \pi r^2 \times h$$

**Sphere:** Total surface area =  $4\pi r^2$

$$\text{Volume} = \frac{4}{3} \pi r^3$$

**Chance and data: Quantify chance**

$$P(A) + P(\bar{A}) = 1$$

In a normal distribution approximately:

68% of values lie within one (1) standard deviation of the mean

95% of values lie within two (2) standard deviations of the mean

99.7% of values lie within three (3) standard deviations of the mean.

*Note: Any additional formulas identified by the examination panel as necessary will be included in the body of the particular question.*