b. t-

(ii) Calculate the pH if the hydrogen concentration in $1.25{\times}10^{-6}$.

on insposition of a "H and where the fill clothest state of the fill which self. (d) $\frac{\partial u}{\partial x} = \frac{1}{2} \frac{\partial u}{\partial x} = \frac{\partial u}{\partial x} = \frac{1}{2} \frac{\partial u}{\partial$

9=7 7-=9 8=0

 $\lambda = \log^n(x-c)$ bins $\delta + x$, $gol = \eta$, x , $gol = \eta$ another soft the functions of the section of the sec

3.8,3.L

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 $\frac{\frac{7}{4}z}{\frac{7}{4}} = \frac{\frac{7}{4}z}{\frac{7}{4}} = \frac{\frac{7}{4}z}{\frac{7}{4}z} = \frac{\frac{7}$

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hil+ x++ + x == (x) f : 2+4(2-)0==06==(5-)+

b1(8)4+(8)2==5f=(8)4

H1=A

>+, x9-=(x), j

Guestion 12. [4 marks]

(/x) - 8x - 6x-3

y' = 2dx³

b) $y = \sqrt{(2x^2 + 5x)^2}$ [2] (fully simplify) $\frac{2}{3} (4i_X + 5) (2\chi^2 + 5\chi)^{1/3}$ a) $f(x) = 4x^2 + 4 + \frac{3}{x^2}$ [2]

(12x+15) \(\sqrt{12x} \cdot 11\sqrt{15}\)

d) $g(x) = \frac{6x-1}{3(4x+6)^2}$ [3] c) $y = 2dx^4 + 3d^2$

 $g(t_Y) := \frac{5(4x+6)^{\frac{3}{4}}(6) - (6x-1)[b(4x+6)]}{9(4x+6)^{\frac{3}{4}}}$

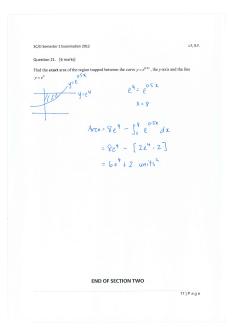
3|Page

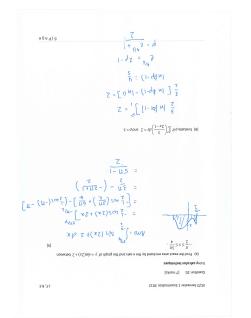
MM Sem 3 Practice Damination 2016

Question 2. If marks)

If the points on the curve $y = y \sin^2 x$ for $0 \le x \le 2x$ where the gradient of the curve is x.

If $x = \frac{1}{2} \sin (-x + \frac{\pi}{1})$ $\frac{1}{2} = \cos (\frac{13\pi}{6})$ $\frac{1}{2} = \cos ($







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Question 20. [8 marks]

The Mass M (in guaras) of a substance decaying afthe t years can be represented by $\frac{dM}{dt} = -kM$ where k is a positive econtant. There is 250 grams of the substance initially and after 2 years the mass of the automace. An extension of the automace of the automace M and M are M are given and M and M and M and M are M and M and M and M are M and M are M and M and M are M and M and M are M and M and M are M and M and M are M and M and M are M and

b. Determine the value of A and the value of k to 4 decimal places. $\label{eq:decimal} 190 \approx 250 \, e^{-K \, \text{T}}$

K= 0-1372

c. How long will it take for the mass of the substance to reduce to 80 grums? [2] $80 = 250e^{0.1372.6}$

d. Determine the amount of time for the mass to reduce by half. $\frac{1}{2}: e$

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 $\int (4x^{2} + x^{2} + 2) dx$ $x^{4} + \frac{x^{3}}{3} + 2x + C.$

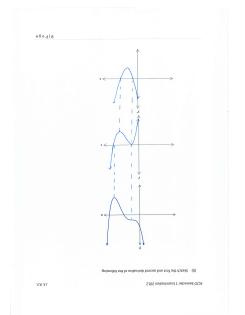
3C/D Semester 1 Examination 2012

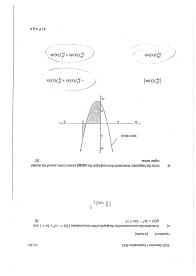
 $\int_0^4 (x+1)(2x-6)\, dx$ $\int_{0}^{6} 2\chi^{2} - 4\chi \chi - (\omega \cos^{2} \phi)$ $\int_{0}^{6} 2\chi^{2} - 4\chi \chi - (\omega \cos^{2} \phi)$ $\left[\frac{2\chi^{4}}{3} - 2\chi^{2} - 6\chi^{2} \right]_{0}^{4}$ $\left(\frac{12^{2}}{3} - 2\chi^{2} - 2\chi^{2} - \chi \psi_{+} \right) - (O)$ $\frac{12^{3}}{3} - \frac{16\chi^{3}}{400}$ $= -\frac{16\chi^{3}}{400}$ The part point of the contracted by the function Ω

Seturning to. $2 \times \int_{0}^{\infty} -\chi^{2} + 6 \, dx$

2× [(-446 ,646)-0]
846 units2

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3C/D Semester 1 Examination 2012

Question 4. [5 marks]

Use the axis below to draw a sketch of a graph with the following characteristics.



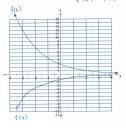


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3C/D Semester 1 Examination 2012

Question19. [6 marks]

(a) The following shows the graph of the function $f(x) = e^{-4.5(x-2)}$. On the same set of axes draw a sketch of its derivative, f'(x)1,(x) = -0.26 -0.2(x-5)



(b) Given that
$$y = e^{3x}$$
, prove that $\frac{d^3y}{dx^3} = \frac{dy}{dx} = 0$
 $\frac{dy}{dx} = 3e^{5x} = \frac{d^3y}{dx^2} = 9e^{5x}$
 $9e^{3x} = 3e^{5x} - be^{5x} = 0$

J.F, R.F.

-5/W9- = (T) 221 = V (d) The velocity of the particle when $t = \frac{\lambda}{2}$.

(42) 47521- =n

· 5/w9

(b) The maximum velocity of the particle.

.3 and the solution of the velocity of the particle at time \mathcal{C} (a) \mathcal{L}

Question 8. [7 marks]

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a6e4|0t

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[2]
$$(\frac{2}{3}+3)^{\frac{1}{2}} - 2(3+\lambda) \text{ divadavia all bias are attrial was:}$$

$$(\frac{2\sqrt{3}}{3}-2)\left(-\frac{2}{3}\right) + 2(3+\lambda)^{\frac{1}{2}} - 2\sqrt{1} \frac{1}{4} \frac{1}{4}$$

$$(\frac{2\sqrt{3}}{3}-1)\left(-\frac{2}{3}\right) + 2(3+\lambda)^{\frac{1}{2}} - 2\sqrt{1} \frac{1}{4} \frac{1}{4}$$

$$(\frac{2\gamma}{3}+1)^{\frac{1}{2}} - 2\sqrt{1} - 2\sqrt{1} \frac{1}{4}$$



SC/D Somester J. Doministion 2012

Question 18. [8 marks]

a. If it is known that y = 80 - 2x, show that $h = \sqrt{80x - 1600}$

$$h = \sqrt{x^{\frac{1}{2}} \cdot (\frac{1}{2}\eta)^{\frac{1}{2}}}$$

$$= \sqrt{x^{\frac{1}{2}} \cdot \frac{1}{4}(90^{-2}x)^{\frac{1}{2}}}$$

$$= \sqrt{x^{\frac{1}{2}} \cdot \frac{1}{4}(600^{-5}20x + 4x^{\frac{1}{2}})}$$

$$= \sqrt{x^{\frac{1}{2}} \cdot \frac{1}{4}(600^{+5}20x - x^{\frac{1}{2}})}$$

= J2 - 1600+80x-2 = V80x-1600

Using Calculus, determine the values of x and y if the area of the triangle is maximized.

[5]

$$A = \frac{1}{2} y h$$

$$= \frac{1}{2} (80 - 2x) \sqrt{80 x - 1600}$$

$$\frac{dA}{dx} = -\frac{(605 x - 1605)}{\sqrt{x - 160}} = 0$$

$$\chi = \frac{90}{3} \frac{d^{2}A}{dx^{2}} = -3\sqrt{3}$$
 . Max.
 $\chi = \frac{90}{3} \frac{d^{2}A}{dx^{2}} = -3\sqrt{3}$. $\chi = \frac{90}{3}$

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```
Question 5. [8 marks]
Quantition 3. Grand (a) Simplify the following:
(b) \frac{\log 16}{\log 2} = \frac{100 \cdot 2}{\log 2} = \frac{4 \cdot \log^2 2}{\log 2}
= 4
             \begin{aligned} & & \frac{2}{3} \log_3 8 + 6 \log_3 \sqrt{2} \cdot \frac{1}{2} \log_3 \frac{1}{4} \\ & & = \frac{2}{3} \log_3 2^2 + 6 \log_3 2^{3/2} - \frac{1}{2} \log_3 2^{2/2} \\ & & = 3 \times \frac{2}{3} + 6 \times \frac{1}{3} - \frac{1}{2} \times 2 \\ & & = 2 + 2 + 1 \end{aligned}
                                = 5
         (b) Solve the following equations: (i) \qquad \quad 6^{i-\epsilon} = 2^{3\epsilon+5}
               \begin{array}{ll} 00 & 6^{-2\pi i n} \\ (1-x) & \log b = (3x+5) \log^2 2 \\ \log b - x & \log b = 3x \log 2 + 5 \log^2 2 \\ \log b - 5 \log 2 = x (3 \log^2 2 - \log^6 2) \\ 2z & \log \frac{1}{2} \log \frac{1}{2} \\ 00 & 6^{-2\pi i n} \end{array}
                               e 1-2x = 60
                            1-2a = |n60
                                 -2x = In60 -1
                                       x = 1-1nb0
```

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11|Page
areason surjoin of most one you
            the height mould decrease
                                      1.0 x ( 1/2 - 7-) = MS
         (a) Suppose that a state (C) is becomed by 10m. That the approximate change, safety of the whistow will take from all thinker residents on till applies. |C-C| = \sqrt{C-C} = 0.01
                                    248 = 1
                               가(고나용) 이미
                     7(3) + 4)2 -01 =0
                      7 = 10 - 2/4 · 2)
```

END OF SECTION ONE

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The curve $y=\mu x^2+qx^2-4x$ has furthing point is $x=-\frac{2}{x}$ and a point of inflection at x=0 beauting the values of y and q.

3C/D Semester 1 Examination 2012

a) Evaluate $\int_{j}^{j+k} f(x) dx$ (simplify your answer)

4) Toolsen,
$$\int_{0}^{\infty} f(x) dx$$
 (simply year anomaly $\int_{0}^{\infty} f(x) x \ln dx$.

$$= \left[-\frac{kx^{2}}{2} + nx \right]_{0}^{\infty} + \left[-\frac{kx^{2}}{2} + n^{2} \right]_{0}^{\infty}$$

$$+ \left[\frac{k(j_{1}k)^{2}}{2} + n(j_{1}k) \right] - \left[-\frac{kj^{2}}{2} + n^{2} \right]_{0}^{\infty}$$

$$+ \left[\frac{k^{2}}{2} + \frac{k}{2} + \frac{k^{2}}{2} + \frac{k}{2} + \frac{k}{2} + n \right]_{0}^{\infty}$$

$$+ \left[\frac{kj}{2} + \frac{k}{2} + \frac{k}{2} + h \right]_{0}^{\infty}$$

$$+ \left[\frac{kj}{2} + \frac{kj}{2} + \frac{k}{2} + h \right]_{0}^{\infty}$$

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(a) If $y = \frac{4}{h^2 + 1}$ and $h = x^5 + x$, use the chain rule to determine $\frac{dy}{dt}$. (a) if $y = \frac{1}{h^2 + 1}$ and h = x + x, we the continuous $\frac{dy}{dx} \times \frac{dy}{dx}$ $\frac{dy}{(\mu^2 + 1)^2} \times (5x^4 + 1)$ $= -\frac{8(x^5 + x)(5x^4 + 1)^2}{((x^5 + x) + 1)^2}$

(b) For $\frac{dy}{dt} = \frac{(x_1 + y_1)^2}{(x_1 + y_2)^2}$, determine the change in y when x changes from x=2 to x = 5.

J2 6x-4x dx

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J.F, R.F.

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Wir) - Kilir) + w & p n ∈ nild=(j))

12| 6 8 8 6 $\frac{2^{4}}{2^{4}} = 1810^{-4}$ 2-1378 = V

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