



PERTH MODERN SCHOOL

Exceptional schooling. Exceptional students.

Independent Public School

Year 12 Methods

TEST 1

Friday 22 February 2019

TIME: 45 minutes working

One page notes allowed

Calculator Assumed

39 marks 7 Questions

Name: _____ Teacher: _____

Note: All part questions worth more than 2 marks require working to obtain full marks.

Question 1

(4 marks)

x	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
1	3	1	-2	-1
2	2	-1	1	0
3	1	-2	2	1

(a) Define $h(x) = \frac{f(x)}{g(x)}$, use the table to find the value for $h'(2)$. (2 marks)

(b) Define $I(x) = [g(x)]^5$, use the table to find the value for $I'(1)$. (2 marks)

Question 2**(3 marks)**

Find the equation of the line tangent to the function $y = (3x^2 - 2)^3$ at the point $(2, 2)$. Give your answer in the gradient-intercept form.

Question 3**(3 marks)**

If $\frac{dy}{dx} = (5x + 3)^3$, and $y = 50$ when $x = 1$, determine the expression of y in terms of x .

Question 4**(7 marks)**

A company is purchasing a type of thin sheet metal required to make a closed cylindrical container with a capacity of $4000\pi \text{ cm}^3$.

(a) Let the radius of the cylindrical base be r . Find the expression for the height h in terms of r .
(1 mark)

(b) Hence, find the expression for the surface area of the cylinder in terms of r .
(2 marks)

(c) Using calculus, determine the least area of metal required to make a closed cylindrical container from thin sheet metal in order that it will have a capacity of $4000\pi \text{ cm}^3$.
(Work to one decimal place)
(4 marks)

Question 5**(6 marks)**

A share portfolio, initially worth \$26000, has a value of f dollars after t months, and begins with a negative rate of growth. The rate of growth remains negative until after 20 months ($t=20$) when the value of the portfolio is momentarily stationary and then continues with negative growth for the life of the investment. The value of the portfolio, $f(t)$ after t months can be modelled by the following model, $f(t) = -2t^3 + bt^2 + ct + d$, $0 \leq t \leq 37$ months where b, c & d are constants.

Determine the values of the constants.

Question 6**(8 marks)**

The volume, V in cubic metres and radius R metres, of a spherical balloon are changing with time,

t seconds. $V = \frac{4\pi R^3}{3}$. The radius of the balloon at any time is given by $R = 2t(t+3)^3$.

Determine the following:

a) The value of $\frac{dR}{dt}$ when $t=1$. (3 marks)

b) The value of $\frac{dV}{dt}$ when $t=1$. (3 marks)

Consider the volume of the balloon at $t=1$.

c) Use the incremental formula to estimate the change in volume 0.1 seconds later (i.e $t=1.1$) (2 marks)

Question 7**(8 marks)**

The position of a train on a straight mono rail, x metres at time t seconds, is modelled by the following formula for the velocity, v in metres/second, $v = pt^2 - 12t + q$ where p & q are constants.

The deceleration of the train is 8ms^{-2} when $t=1$, has a position $x = \frac{4}{3}$ when $t=2$ and is initially at the origin ($x=0$).

- a) Determine the values of the constants p & q .

(4 marks)

b) Determine the time(s) that the velocity is zero. (2 marks)

c) Determine the position of the train when the acceleration is $12ms^{-2}$. (2 marks)

Supplementary Page

Question Number: _____