

- June 12th the end of week 7 of term 2, 2020

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Marking Key

MAWA Semester 1 (Unit 3) Examination 2020

Calculator-assumed

MATHEMATICS METHODS

Section One: Calculator-assumed**Question 8(a)****(3 marks)**

Solution	
$c = Ae^{-kt}$	
$t = 0, c = 0.03 \Rightarrow A = 0.03.$	
$t = 36.5, c = \frac{A}{2} \Rightarrow \frac{A}{2} e^{-k \times 36.5} = 0.5 = e^{-k \times 36.5} \Rightarrow k \approx 0.019.$	
Mathematical behaviours	Marks
• uses initial condition to construct equation and solves for A	1
• constructs equation related to half life	1
• solves for k	1

Question 8(b)**(2 marks)**

Solution	
For isotope B, $A = 0.02.$	
$0.5 = e^{-k \times 62.9} \Rightarrow k \approx 0.011.$	
Solving	
$0.02e^{-0.011t} = 2 \times 0.03e^{-0.019t} \Rightarrow t \approx 137.3$	
Hence approximately 137 years from now.	
Mathematical behaviours	Marks
• states equation to be solved	1
• solves for t and states time (in years)	1

1			
1			
1			
	Marks		
		Marks	

Mathematical behaviours

(i) $K = 1, P = 25e^{-\frac{t}{5}} + t + 25$

As $t \rightarrow \infty, P \rightarrow \infty$
i.e. population of infected people increases indefinitely

(ii) $K = 0, P = 25e^{-\frac{t}{5}} + t(0) + 25 = 25e^{-\frac{t}{5}} + 25$

As $t \rightarrow \infty, P \rightarrow \infty$
i.e. population of infected people increases indefinitely

(iii) $K = 0, P = 25e^{-\frac{t}{5}} + t + 25$
As $t \rightarrow \infty, P \rightarrow 25$
i.e. population of infected people stabilises to 25

(iii) ie. population of infected people stabilises to 25
• recognises that when $K = 0$ and as $t \rightarrow \infty, P \rightarrow 25$

(ii) ie. population of infected people increases indefinitely
• recognises that when $K = 1$, and as $t \rightarrow \infty, P \rightarrow \infty$

(i) ie. population of infected people stabilises to 25
• recognises that when $K = 0$ and as $t \rightarrow \infty, P \rightarrow 25$

Mathematical behaviours

Marks

(4 marks)

Question 9(b)

1			
1			
	Marks		
		Marks	

Mathematical behaviours

(i) $\frac{dp}{dt} = -5e^{-\frac{t}{5}} + K$ $\Rightarrow p = 25e^{-\frac{t}{5}} + Kt + d$

$t = 0, p = 50 \Rightarrow 50 = 25e^0 + d \Rightarrow d = 25$

$\therefore p = 25e^{-\frac{t}{5}} + Kt + 25$ as required.

(ii) $t = 0, p = 50 \Rightarrow 50 = 25e^0 + d \Rightarrow d = 25$

$\frac{dp}{dt} = -5e^{-\frac{t}{5}} + K$ $\Rightarrow p = 25e^{-\frac{t}{5}} + Kt + d$

Solution

(2 marks)

Question 9(a)

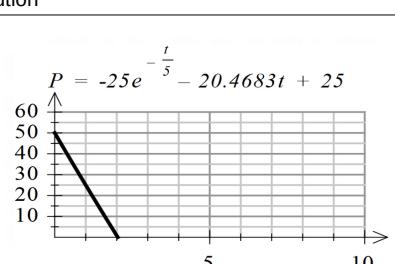
- correct graph for $K = 0$
- correct graph for $K = 1$

1

Question 9(c)

(3 marks)

Solution	
$P = 25e^{\frac{t}{5}} + Kt + 25$	
$t=1, P=25 \Rightarrow 25 = 25e^{\frac{1}{5}} + K + 25$	
$K = -25e^{\frac{1}{5}} \approx -20.4683$	
Hence, $P = 25e^{\frac{t}{5}} - 20.4683t + 25$	
From CAS, this is a decreasing function.	
$P=0 \Rightarrow t=2.0345$	
ie Population of infected people will reduce to zero after 2.0345 weeks	
Mathematical behaviours	Marks
• uses $t=1$ and $P=25$ to find the correct value of K	1
• uses $P=0$ to find the value of t	1
• states a valid prediction	1



Question 10(a)

(3 marks)

Solution	
$\text{Area of triangle} = \frac{1}{2} \times x \times x \times \sin 60^\circ = \frac{\sqrt{3}x^2}{4}$	
Hence,	
$A = xy + \frac{\sqrt{3}x^2}{4}$	$3x + 2y = 10$
$= x\left(\frac{10-3x}{2}\right) + \frac{\sqrt{3}x^2}{4}$	$y = \frac{10-3x}{2}$
ie $A = 5x - \frac{3x^2}{2} + \frac{\sqrt{3}x^2}{4} = \frac{(\sqrt{3}-6)x^2 + 5x}{4}$	
Mathematical behaviours	Marks
• determines area of triangle as an exact value	1
• states formula for total area in terms of x	1
• clearly demonstrates rearrangement of formulae to achieve required result.	1

Question 19(c)

Solution

$$\frac{1.2064 + 1.5059}{2} = 1.3562$$

Hence $1.4038193 < x < 2$

$$1.3562 - 1.2064 = 0.1498$$

$$\int_{1.4038193}^c \left(\frac{2}{1 - \sin\left(\frac{x}{2}\right)} - \left(-(x-2)^2 + 6 \right) \right) dx = 0.1498 \Rightarrow x = -0.7550, 1.1253, 1.6282$$

Hence $c \approx 1.63$

Mathematical behaviours	Marks
• determines average of two areas	1
• states appropriate equation to be solved involving integral	1
• solves equation and concludes solution	1

Marks	Marks	<ul style="list-style-type: none"> evaluates the sum of probabilities to 1 evaluates b states expression for $E(X)$ evaluates a
1	1	$E(X) = 1 \times b + 3 \times \frac{1}{5} + 4 \times \frac{1}{5} + a \times \frac{5}{2} = 3.5$ $\text{ie } \frac{1}{5} + \frac{5}{5} + \frac{4}{2a} = 3.5 \Leftrightarrow a = 5$ $\frac{1}{10} + b + \frac{1}{1} + \frac{2}{5} = 1 \Leftrightarrow b = \frac{1}{10}$

Solution

Question 11(a)

Marks	Marks	<ul style="list-style-type: none"> calculates maximum area determines $\int_a^b A$ or otherwise justifies maximum area determines point of intersection of f and g evaluates one integral correctly determines correct result to two decimal places
1	1	$x = 2.34 \Rightarrow A = -1.067 \times (2.34)^2 + 5 \times 2.34 \approx 5.86$ $\text{Hence the maximum area is approximately } 5.86 \text{ m}^2.$ $\frac{dA}{dx} = -2.134 < 0 \Rightarrow \text{maximum}$ $\frac{dA}{dx} = 0 \Rightarrow -2.1340x + 5 = 0 \Rightarrow x \approx 2.34.$ $\text{solve } \left(\frac{dA}{dx} \right)_{(x=0)} = 0, x = 2.3405699$ $\frac{d^2A}{dx^2} = 2 \times (\sqrt{3} - 6) \frac{dA}{dx} \quad \text{done}$ $A = \frac{(\sqrt{3} - 6)}{4} x^2 + 5x \quad \text{done}$ $\text{Define } f(x) = \frac{(\sqrt{3}-6)}{4} x^2 + 5x$ $\text{Define } g(x) = -(x-2)^2 + 6$ done $\text{Area} = \int_{-1.4038193}^{2.712317078} \left[(-x-2)^2 + 6 - \left(\frac{1}{2} \sin \left(\frac{x}{2} \right) - (x-2)^2 + 6 \right) \right] dx$ $= 1.2064 + 1.5059$ $= 2.7123 \approx 2.71$

Solution

Question 10(b)

MATHEMATICS METHODS	CALCULATOR-ASSUMED	SEMESTER 1 (UNIT 3) EXAMINATION SEMESTER 1 (UNIT 3) EXAMINATION
5	5	5 marks)

Solution	$f(x) = g(x) \Rightarrow \frac{2}{2 - \sin \frac{x}{2}} = -(x-2)^2 + 6$ $\text{Define } f(x) = \frac{2}{2 - \sin \frac{x}{2}}$ done $\text{Define } g(x) = -(x-2)^2 + 6$ done $\text{solve } f(x) = g(x), x$ $\{x=0, x=1, 4.0381927\}$ $\int_0^1 4.0381927 \quad (g(x) - f(x)) dx$ $1.206378321 \quad \left[\frac{2}{2 - \sin \left(\frac{x}{2} \right)} - \left((x-2)^2 + 6 \right) \right] dx$ $1.505938757 \quad 1.206378321 + 1.505938757$ $= 2.712317078 \quad 2.712317078$
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Questions 19(b)	5 marks)
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SEMESTER 1 (UNIT 3) EXAMINATION

16

16

Question 11(b)

Solution	
(i)	
$\sigma^2 = \sum(x - \mu)^2 p(x) = (0 - 3.5)^2(0.1) + (1 - 3.5)^2(0.1) + (3 - 3.5)^2(0.2) + (4 - 3.5)^2(0.2)$ $+ (5 - 3.5)^2(0.4) = 2.85 \Rightarrow \text{std dev} = \sqrt{2.85} \approx 1.69$	
(ii)	
Standard deviation of $3 - 2X = 2 \times \text{standard deviation of } X = 2 \times 1.69 = 3.38$	
Mathematical behaviours	Marks
(i)	
• states expression to determine the variance of X	1
• evaluates variance	1
• evaluates standard deviation	1
(ii)	
• states correct result	1

Question 12(a)

(2 marks)

Solution		
h	a	$\frac{a^h - 1}{h}$
0.1	2	0.7177
0.01	2	0.6956
0.001	2	0.6934
0.0001	2	0.6932
Mathematical behaviours	Marks	
• completes two rows of the table correctly	1	
• completes all rows of the table correctly	1	

Question 12(b)

(1 mark)

Solution	
$\lim_{h \rightarrow 0} \frac{2^h - 1}{h} = 0.693$, correct to 3 decimal places.	
Mathematical behaviours	Marks
• evaluates limit correctly	1

<p>MATHEMATICS METHODS</p> <p>CALCULATOR-ASSUMED</p> <p>SEMESTER 1 (UNIT 3) EXAMINATION</p> <p>(2 marks)</p>		<p>Question 12(c)</p>											
		<p>7</p>											
<p>Question 12(g)</p>		<p>Solution</p>											
<p>(i)</p> $\lim_{h \rightarrow 0} \frac{a^h - 1}{h} = 3 \Rightarrow a \approx 20.1$	<p>• states solution</p>	<p>Marks</p>	<p>1</p>										
<p>(ii)</p> $\lim_{h \rightarrow 0} \frac{a^h - 1}{h} = \lim_{h \rightarrow 0} \frac{a^h - e^h + e^h - 1}{h} = \lim_{h \rightarrow 0} \frac{a^h - e^h}{h} + \lim_{h \rightarrow 0} \frac{e^h - 1}{h} = 1 + e$	<p>• states exact solution</p>	<p>Marks</p>	<p>1</p>										
<p>Question 13(a)</p>		<p>Solution</p>											
<table border="1"> <tr> <td>x</td> <td>1</td> <td>2</td> <td>$\frac{3}{4}$</td> <td>$\frac{9}{16}$</td> </tr> <tr> <td>y</td> <td>4</td> <td>$\frac{25}{9}$</td> <td>$\frac{1}{16}$</td> <td>36</td> </tr> </table>	x	1	2	$\frac{3}{4}$	$\frac{9}{16}$	y	4	$\frac{25}{9}$	$\frac{1}{16}$	36	<p>• states all three correct values</p>	<p>Marks</p>	<p>1</p>
x	1	2	$\frac{3}{4}$	$\frac{9}{16}$									
y	4	$\frac{25}{9}$	$\frac{1}{16}$	36									
<p>Question 13(b)</p>		<p>Solution</p>											
<p>(i)</p> $\text{Area of lower rectangles} = 2 + 2 \cdot \frac{1}{4} + 3 \cdot \frac{1}{9} = \frac{265}{36}$	<p>• sums the correct rectangles</p>	<p>Marks</p>	<p>1</p>										
<p>(ii)</p> $\text{Area of upper rectangles} = \frac{1}{4} + \frac{1}{9} + \frac{1}{16} = \frac{5428}{1357} = \frac{576}{144} = 144$	<p>• reduces correctly</p>	<p>Marks</p>	<p>1</p>										
<p>Question 13(c)</p>		<p>Solution</p>											
<p>(i)</p> $\text{Area of lower rectangles} = 2 + 2 \cdot \frac{1}{4} + 3 \cdot \frac{1}{9} = \frac{265}{36}$	<p>• sums the correct rectangles</p>	<p>Marks</p>	<p>1</p>										
<p>(ii)</p> $\text{Area of upper rectangles} = \frac{1}{4} + \frac{1}{9} + \frac{1}{16} = \frac{5428}{1357} = \frac{576}{144} = 144$	<p>• evaluates correctly</p>	<p>Marks</p>	<p>1</p>										

<p>Question 18(c)</p>					
<p>6</p>	<p>$\int 12 + 2.5 \cos(0.5236t + 0.1571) dt \approx 19.54$</p>				
<p>Solution</p>					
<p>(i)</p> $\lim_{h \rightarrow 0} \frac{a^h - 1}{h} = \lim_{h \rightarrow 0} \frac{a^h - e^h + e^h - 1}{h} = \lim_{h \rightarrow 0} \frac{a^h - e^h}{h} + \lim_{h \rightarrow 0} \frac{e^h - 1}{h} = 1 + e$	<p>• uses correct integral</p>	<p>Marks</p>	<p>1</p>		
<p>(ii)</p> $\lim_{h \rightarrow 0} \frac{a^h - 1}{h} = 3 \Rightarrow a \approx 20.1$	<p>• states solution</p>	<p>Marks</p>	<p>1</p>		
<p>Question 18(d)</p>					
<p>So the average daily amount in May and June is 9.77 hours</p>	<p>• states solution</p>	<p>Marks</p>	<p>1</p>		
<p>$\text{So average} = \frac{19.54}{2} \approx 9.77.$</p>	<p>• uses correct integral</p>	<p>Marks</p>	<p>1</p>		
<p>Question 18(e)</p>					
<p>Hence the maximum value of $\frac{ds}{dt}$ is $2.5 \times 0.5236 \approx 1.31$ hours per month</p>	<p>Using the increments formula $\frac{\Delta S}{\Delta t} \approx \frac{S_2 - S_1}{t_2 - t_1}$, the maximum change in successive days is</p>	<p>i.e. 2.62 minutes (or 3 minutes to the nearest minute).</p>	<p>• identifies maximum value of $\frac{ds}{dt}$</p>	<p>Marks</p>	<p>1</p>
<p>$S = 12 + 2.5 \cos(0.5236t + 0.1571)$</p>	<p>$\frac{ds}{dt} = -2.5(0.5236) \sin(0.5236t + 0.1571)$</p>	<p>• substitutes into increments formula</p>	<p>• identifies answer to the nearest minute</p>	<p>Marks</p>	<p>1</p>
<p>Question 19(a)</p>					
<p>The function is undefined at $m = \pi$ since f is undefined at $x = \pi$.</p>	<p>$A(m) = \int f(x) dx$</p>	<p>represents the area bounded by the curve,</p>	<p>the line $x = 0$ and the line $x = m$.</p>	<p>Marks</p>	<p>1</p>
<p>The area is given by $\int_0^\pi \sin \frac{x}{m} dx = \left[-\cos \frac{x}{m} \right]_0^\pi = \left(-\cos \frac{\pi}{m} + \cos 0 \right) = 1 - \cos \frac{\pi}{m}$</p>	<p>$\int_0^\pi \sin \frac{x}{m} dx = 1 - \cos \frac{\pi}{m}$</p>	<p>hence the area cannot be calculated</p>	<p>• concludes that the area cannot be calculated – it is not bounded</p>	<p>Marks</p>	<p>1</p>

**CALCULATOR-ASSUMED
SEMESTER 1 (UNIT 3) EXAMINATION
(1 mark)**

Question 13(c)

Solution	
Estimated area	$= \frac{1}{2} \left[\frac{265}{36} + \frac{5428}{576} \right] \approx 8.39$
Mathematical behaviours	Marks
• calculates the average of the lower and upper areas	1

Question 13(d) (1 mark)

Solution	
Area under the curve is	$\int_1^4 x + \frac{1}{x^2} dx = \frac{33}{4} = 8.25$
Mathematical behaviours	Marks
• states the correct answer	1

Question 14(a) (1 mark)

Solution	
Some people would read both digital and print. If these entries are summed those people will be counted twice.	
Mathematical behaviours	Marks
• recognises that some people will read both forms of publication	1

Question 14(b) (2 marks)

Solution	
$P(\text{reading print media}) = \frac{6547000}{20289938} = 0.322 \approx 32\%$	
Mathematical behaviours	Marks
• uses correct numerator	1
• uses correct denominator and deduces result	1

Question 14(c) (3 marks)

Solution	
$X \sim \text{Bin}(10, 0.32)$	
$\mu = 10 \times 0.32 = 3.2$	
$\sigma^2 = 10 \times 0.32 \times 0.68 \approx 2.176$	
Mathematical behaviours	Marks
• states Binomial	1
• calculates mean	1
• calculates variance	1

**CALCULATOR-ASSUMED
SEMESTER 1 (UNIT 3) EXAMINATION
(6 marks)**

Question 18(a)

Solution	
(i)	
Since the maximum and minimum values are 14.5 and 9.5	
$a + b = 14.5$ and $a - b = 9.5 \Rightarrow a = 12$ and $b = 2.5$.	
or	
$\frac{14.5 + 9.5}{2} \Rightarrow a = 12$	and $b = \frac{14.5 - 9.5}{2} = 2.5$
mean line	amplitude
	$c = \frac{2\pi}{12} \approx 0.5236$.
Since the period of the oscillation is 12,	
(ii)	
$S = 12 + 2.5 \cos(0.5236t + d)$,	
$\frac{dS}{dt} = -2.5 \times (0.5236) \sin(0.5236t + d)$	
$\frac{dS}{dt} = 0 \Rightarrow \sin(0.5236t + d) = 0$	
Maximum at $t = 11.7$	
$\Rightarrow 0.5236 \times 11.7 + d = 2\pi$	
$d \approx 0.1571$	
Mathematical behaviours	
(i)	
• explains exactly one of a and b values	1
• explains both a and b values	1
• identifies the period to explain the value of c	1
(ii)	
• differentiates correctly	1
• equates to 0 and equates angle to 2π	1
• solves equation to determine d	1

Question 18(b) (1 mark)

Solution	
On April 30 th , $t = 4$	
$S = 12 + 2.5 \cos(0.5236 \times 4 + 0.1571) \approx 10.4$ hours	
So we can expect 10.4 hours of sunlight on April 30 th .	
Mathematical behaviours	
• states correct answer	1

CALCULATOR-ASSUMED MATHEMATICS METHODS		
SEMESTER 1 (UNIT 3) EXAMINATION (5 marks)		
<p>Question 14(d)</p> <p>Solution</p> <p>$P(X=5) \approx 0.1229$</p> <p>(i)</p> <p>$P(X > 5) \approx 0.0637$</p> <p>(ii)</p> <p>$C_1(0.32)(0.68)^2 \times (0.32) \approx 0.1420$</p> <p>(iii)</p> <p>• states correct probability</p> <p>• states appropriate probability expression</p> <p>• calculates probability</p> <p>• calculates fourth outcome and calculates probability</p> <p>• states correct expression for first three outcomes</p> <p>Let F be the random variable denoting the number of people in the 200 who read print media.</p> <p>$Y \sim Bi(200, 0.32)$</p> <p>$P(Y < 50) = P(25\% \text{ or more do read})$</p> <p>Let Y be the random variable denoting the number of people in the 200 who read print media.</p> <p>$P(Y \geq 50) = 0.9874$</p> <p>Question 14(e)</p> <p>Solution</p> <p>Question 15(a)</p> <p>Solution</p> <p>$f(x) + x^3 f'(x)$</p> <p>$\frac{d}{dx} \int_x^0 f(t) dt + \frac{d}{dx} \int_x^1 f(t) dt$</p> <p>$\left[\frac{d}{dx} \int_x^0 f(t) dt + \int_x^1 f(t) dt \right]$</p> <p>• applies linearity for derivatives</p> <p>• applies the Fundamental Theorem and evaluates, stating the correct result</p> <p>Marks</p>	<p>Question 14(e)</p> <p>Solution</p> <p>Question 15(a)</p> <p>Solution</p> <p>$f(x) + x^3 f'(x)$</p> <p>$\frac{d}{dx} \int_x^0 f(t) dt + \frac{d}{dx} \int_x^1 f(t) dt$</p> <p>$\left[\frac{d}{dx} \int_x^0 f(t) dt + \int_x^1 f(t) dt \right]$</p> <p>• applies linearity for derivatives</p> <p>• applies the Fundamental Theorem and evaluates, stating the correct result</p> <p>Marks</p>	<p>Question 15(a)</p> <p>Solution</p> <p>$f(x) + x^3 f'(x)$</p> <p>$\frac{d}{dx} \int_x^0 f(t) dt + \frac{d}{dx} \int_x^1 f(t) dt$</p> <p>$\left[\frac{d}{dx} \int_x^0 f(t) dt + \int_x^1 f(t) dt \right]$</p> <p>• applies linearity for derivatives</p> <p>• applies the Fundamental Theorem and evaluates, stating the correct result</p> <p>Marks</p>

CALCULATOR-ASSUMED MATHEMATICS METHODS		
SEMESTER 1 (UNIT 3) EXAMINATION (5 marks)		
<p>Question 17(f)</p> <p>Solution</p> <p>Let the random variable F represent the operator's financial position for each game.</p> <p>$E(F) = -2 \times \frac{52}{100} + 5 \times \frac{48}{100} = 1.36$</p> <p>Hence the operator will expect to make \$1.36 per game in the long term. With 500 contestants he will expect to make $500 \times \\$1.36 = \\680</p> <p>• determines expected value for 1 game</p> <p>• calculates gain for the day</p> <p>• states final outcome, with unit and explains</p> <p>Marks</p>	<p>Question 17(g)</p> <p>Solution</p> <p>Let k be the charge to play the game.</p> <p>$E(F) = (k - 7) \times \frac{52}{100} + k \times \frac{364}{100} = 0 \Leftrightarrow k = 3.64$</p> <p>Hence the operator would need to charge \$3.64.</p> <p>• constructs equation for expected value</p> <p>• solves equation to determine k</p> <p>Marks</p>	<p>Question 17(g)</p> <p>Solution</p> <p>Let k be the charge to play the game.</p> <p>$E(F) = (k - 7) \times \frac{52}{100} + k \times \frac{364}{100} = 0 \Leftrightarrow k = 3.64$</p> <p>Hence the operator would need to charge \$3.64.</p> <p>• constructs equation for expected value</p> <p>• solves equation to determine k</p> <p>Marks</p>

**CALCULATOR-ASSUMED
SEMESTER 1 (UNIT 3) EXAMINATION
(2 marks)**

Question 15(b)**Solution**

$$\begin{aligned} \int_0^x f(t)dt + \int_1^x f(t)dt &= x^3 + \frac{1}{2}x^6 \\ \Rightarrow \frac{d}{dx} \left[\int_0^x f(t)dt + \int_1^x f(t)dt \right] &= \frac{d}{dx} \left[x^3 + \frac{1}{2}x^6 \right] \\ ie \quad f(x) + x^3 f(x) &= 3x^2 + 3x^5 \\ ie \quad f(x)(1+x^3) &= 3x^2(1+x^3) \\ ie \quad f(x) &= 3x^2 \end{aligned}$$

Mathematical behaviours**Marks**

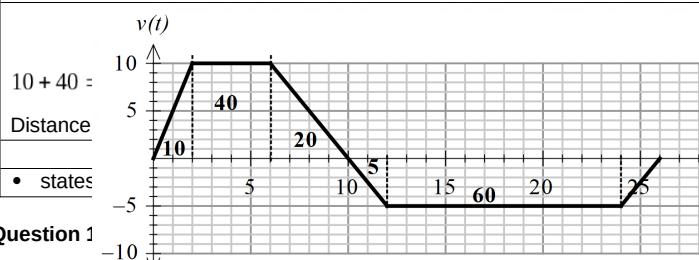
- differentiates both sides of the equation (or applies result from part (a))
- determines result

Question 16(a)**(1 mark)****Solution**

$$a = \frac{dv}{dt} = 0$$

Mathematical behaviours**Marks**

- states correct answer

Question 16(b)**(1 mark)****Solution****Question 1****mark)**

$$(10 + 40 + 20) - 5 = 65$$

Displacement after 12 seconds is 65 m

Mathematical behaviours**Marks**

- states correct answer

Question 16(d)**(1 mark)****Solution**

Distance travelled after 12 seconds is $10+40+20+5 = 75$ m

**CALCULATOR-ASSUMED
SEMESTER 1 (UNIT 3) EXAMINATION**

Mathematical behaviours	Marks
• states correct answer	1

Question 16(e)**(1 mark)****Solution**

At $t = 11$ both the velocity and the acceleration are negative hence the particle is speeding up.

Mathematical behaviours	Marks
• states the particle is speeding up	1

Question 17(a)**(2 marks)**

Solution		y	0	1	
P(Y=y)			$\frac{6}{10}$	$\frac{4}{10}$	

Mathematical behaviours	Mark
• completes first probability correctly	1
• completes second probability correctly	1

Question 17(b)**(2 marks)**

Solution		$\frac{4}{10}$
It is a Bernoulli distribution with mean = $\frac{4}{10}$.		
Mathematical behaviours		Marks
• states the distribution name		1
• states the mean		1

Question 17(c)**(2 marks)**

Solution	
$X = 0, 1$ or 2	
Mathematical behaviours	Marks
• states all values	1

Question 17(d)**(1 mark)**

Solution	
$P(X = 0) = P(\text{not prime and not prime}) = \frac{6}{10} \times \frac{6}{10} = \frac{36}{100}$	
Mathematical behaviours	Mark
• calculates probability	1

Question 17(e)**(3 marks)**

Solution
