

## Western Australian Certificate of Education 2012 Examination, 2012

### Question/Answer Booklet

Special items:			unfolded sheets of A4 paper, the WACE examinations
<b>To be provided</b> Standard items:	by the candidate perserved the candidate correction tape/fluid, era		colonred), sharpener,
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	for this section rection:	səfunim nəf	Number of additional answer booklets used (if applicable):
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MATHEM 3A/3B Section Two Calculator-6	:c	Please place your stude	nt identiffication label in this box

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Important note to candidates

before reading any further.



examination room. If you have any unauthorised material with you, hand it to the supervisor

No other items may be taken into the examination room. It is your responsibility to ensure that

you do not have any unauthorised notes or other items of a non-personal nature in the

SS-BAETAM

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<b>MATHEMATICS</b>	3A/3R
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### CALCULATOR-ASSUMED

### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of total exam
Section One: Calculator-free	7	7	50	50	33⅓
Section Two: Calculator-assumed	12	12	100	100	663/3
			Total	150	100

### Instructions to candidates

- The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2012. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages
  are included at the end of this booklet. They can be used for planning your responses
  and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in
    the original answer space where the answer is continued, i.e. give the page number.
     Fill in the number of the question(s) that you are continuing to answer at the top of the
    page.
- 3. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 4. It is recommended that you do not use pencil, except in diagrams.
- 5. The Formula Sheet is **not** handed in with your Question/Answer Booklet.

See next page

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CALCULATOR-ASSUMED Additional working space	19	MATHEMATICS 3A/3B
Question number:		
Question number.		

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s it hits the ground for the seventh (3 marks)	an by the ball just as	ÉIME?	(c)
digovos odi soi banoso odi siid ii s	ic tarii llod odt vd be	Movest coactaib letot odt ai ted/M	(0)
(S marks)		decimal places?	
er the third bounce, correct to two (2)	ched by the ball aft	What is the maximum height rea	(q)
(2007)			
by each successive downward (2 marks)	e distance travelled	Write a recursive rule to show th motion of the ball.	(a)
urface. The height reached by the vious bounce.		is aropped from a height of 60 cm fter each bounce is two-thirds of th	
(7 marks)		8 noit	
		ssted working time: 100 minutes.	Sugge
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		led.	provic
ns. Write your answers in the spaces	Answer all questio	ection has <b>twelve (12)</b> questions.	s sidT
(100 Marks)		on Two: Calculator-assumed	
MATHEMATICS 3A/3B	3	GEMUSSA-ROTALUS	CALC

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	CALCULATOR-ASSUMED	81	MATHEMATICS 3A/3B Additional working space

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CALCULATOR-ASSUMED

Question 9

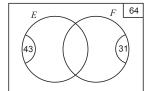
(5 marks)

E and F are two sets for which n(E) = 43, n(F) = 31 and n(U) = 64.

Using the Venn diagrams or otherwise, determine

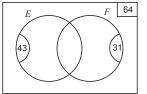
(a)  $n(E \cap F)$  if  $n(\overline{E \cup F}) = 0$ .

(2 marks)



(b)  $P(E \mid \overline{F}) \text{ if } n(\overline{E \cup F}) = 10.$ 

(3 marks)



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### GALCULATOR-ASSUMED 5 MATHEMATICS 3A/3B

Ot marks)

Researchers believe that a lake is inhabited by a native species of fish thought to be endangered. At a point approximately in the middle of the lake, 50 of these fish were captured, tagged and released. The following day, at the same point, another 50 fish were caught and, before they were released, it was noted that 10 of these were tagged.

(a) Show how the researchers could use this information to estimate that the total population (P) of these fish in the lake was 250. (2 marks)

In general, the number of tagged fish caught (i) allowed the researchers to estimate  ${\bf P}$  according to the relationship in this table.

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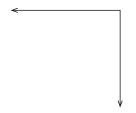
(b) (i) Complete the table above for population estimates (P) for different numbers of tagged fish caught (r) in lots of 50. (3 marks)

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(ii) Describe the relationship between  $\iota$  and P.

(iii) Write an equation for P in terms of  $\ell$ .

(iv) On the axes provided, sketch the relationship found in Part (b) (iii).



(v) Comment on the rate of change of P as t nears zero and how this might have
consequences on the stability of this model for making predictions with very
small values of t.

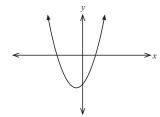
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CALCULATOR-ASSUMED

Question 11

(10 marks)

The quadratic function y = f(x) is shown below. The turning point has coordinates (a, b) and y-intercept has coordinates (0, c).



(a) Determine the equation of the line of symmetry for y = f(x - 1).

(2 marks)

(b) Determine the coordinates of the turning point of y = f(x + 4) + 5.

(2 marks)

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Determine the coordinates of the *y*-intercept of y = -f(x) - 2.

(3 marks)

Another quadratic function y = g(x) has a turning point at (1, 8) and intersects the *x*-axis at (3, 0).

(d) Determine the coordinates of the *x*-intercepts of y = g(2x).

(3 marks)

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CALCULATOR-ASSUMED

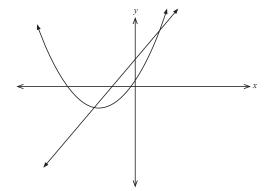
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MATHEMATICS 3A/3B

Question 19

(6 marks)

The functions  $f(x) = x^2 + 4x + 1$  and g(x) = 3x + d, where d is a constant, are shown below.



For what value(s) of d does the equation f(x) = g(x) produce:

(a) one solution?

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(5 marks)

(b) two solutions?

(1 mark)

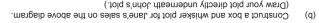
End of questions

## CALCULATOR-ASSUMED Question 12 Question 12 Question 15 34 47 1 15 57 24 20 11 19 50 28 37 John's data are displayed on the following box and whisker plot.









(a) Calculate the median and interquartile range of phone sales for Jane.



(2 marks)

(3 marks)

(2 marks)

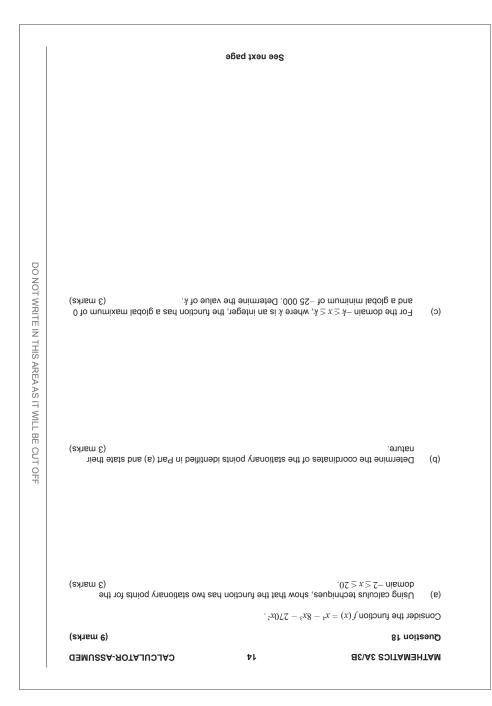
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(c) Who had the better sales performance? Justify your answer.

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CALCULATOR-ASSUMED

Question 13 (3 marks)

Joanne, a Year 10 student, achieved a final Semester Two mark of 79% in mathematics. The table below gives the weightings and her mean score for the given categories.

	Weighting (%)	Mean score (%)
Homework	10	78
Tests	25	x
Investigations	20	75
Examinations	45	80

Calculate her mean score for tests. Give your answer to the nearest whole percentage.

Question 14 (4 marks)

The marks for a mathematics examination at a school are normally distributed with a mean of 54% and a standard deviation of 16.5%.

(a) State the median examination score.

(b) Determine the interquartile range of the examination scores.

(3 marks)

(1 mark)

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CALCULATOR-ASSUMED 13 MATHEMATICS 3A/3B (c) Calculate x and hence state the times taken by Simone and Lucy to complete their respective journeys. Give your answers correct to the nearest minute. (4 marks) DO NOT WRITE IN THIS AREAAS IT WILL BE CUT OFF Assuming Simone maintains her constant speed of 95 km/h, at what speed would Lucy need to be travelling to finish her journey in the same time as Simone? Give this speed in metres per second. (4 marks)

MATHEMATICS 3A/3B CALCULATOR-ASSUMED

(13 marks) Question 15

The attendances, in hundreds, at the evening performances, are shown in the following table. A theatre company performed for three weeks at a large venue capable of seating 4200 people.

Residual	Three-point moving average	Attendance (in hundreds)	(t) əmiT	Day	
		50	l	Wednesday	1-2:7
<b>b</b> -	50	91	2	Friday	First Week
£.1	7.22	24	3	Saturday	NOOAA
2	56	28	Þ	Wednesday	puoses
£.£-	29.3	56	G	Friday	Meek
8.8	7.08	34	9	Saturday	210044
6.0	7.18	32	L	Wednesday	PaidT
В	34	V	8	Friday	Third
		lτ	6	Saturday	

(3 marks) Calculate the value of the missing entries marked by A and B.

(2 marks) Calculate the seasonal component for the Wednesday performances. DO NOT WRITE IN THIS AREAAS IT WILL BE CUT OFF

the equation of this regression line correct to two (2) decimal places. (S marks) (c) A regression line was fitted to the three-point moving averages given above. Determine

(4 marks) Wednesday in the fourth week to the nearest hundred. together with the seasonal component for Wednesday, to predict the attendance for (d) This equation was used to represent the trend of the time series. Use this equation,

(2 marks) (e) Should performances be extended for a fourth week? Give a reason for your answer.

See next page

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF to complete their respective journeys. Write an expression in terms of x for the time taken, in hours, for both Simone and Lucy Let the distance Lucy travels be x km. respectively. Lucy drives 15 kilometres further than Simone. Simone and Lucy are driving along a highway at constant speeds of 95 km/h and 85 km/h (12 marks) Auestion 17 CALCULATOR-ASSUMED **MATHEMATICS 3A/3B** 

Simone completes her journey in 15 minutes less than Lucy.

 $\frac{1}{\hbar} = \frac{2I - x}{29} - \frac{x}{28} \text{ yhw nislqx} \qquad (d)$ (2 marks)

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CALCULATOR-ASSUMED

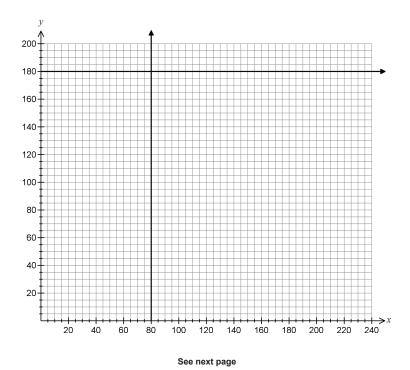
Question 16 (12 marks)

A laboratory that distils natural oils from plant materials produces two types of oil concentrate: an olive oil product for general lubricating use and a refined eucalyptus oil product for use as a cosmetic base and in natural medicines.

Fixed demands require the production of at least 80 litres of the olive oil and at least 70 litres of eucalyptus oil each week. The laboratory has the capacity to produce up to 300 litres of distilled oil each week, of which a maximum of 200 litres can be olive oil or a maximum of 180 litres can be eucalyptus oil.

Let x be the number of litres of olive oil produced and y be the number of litres of eucalyptus oil produced.

- (a) Given that  $x \ge 80$  and  $y \le 180$ , state **three (3)** further inequalities involving x and y, other than  $x \ge 0$  and  $y \ge 0$ . (3 marks)
- (b) Graph these inequalities on the grid below and shade the feasible region. (4 marks)



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(d) Specific orders require the distillery to produce exactly 160 litres of olive oil in one week. What is the maximum profit it can make in that week? (2 mark)
(d) Specific orders require the distillery to produce exactly 160 litres of olive oil in one week.  What is the maximum profit it can make in that week? (2 mark