# Semester 1 (Unit 3) Examination, 2016

# Question/Answer Booklet

# MATHEMATICS METHODS

Теасћег Иате:	
Student Name/Number:	

**Calculator-free** 

## Time allowed for this section

Working time for this section: Reading time before commencing work: five minutes

### To be provided by the supervisor: Materials required/recommended for this section

This Question/Answer Booklet

Formula Sheet

#### To be provided by the candidate:

correction fluid/tape, eraser, ruler, highlighters systbenet, pens (blue/black preferred), pencils (including coloured), Standard items:

Special items:

Section One:

## Important note to candidates

before reading any further. examination room. If you have any unauthorised material with you, hand it to the supervisor you do not have any unauthorised notes or other items of a non-personal nature in the No other items may be taken into the examination room. It is your responsibility to ensure that

### Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	9	9	50	50	35
Section Two: Calculator-assumed	13	13	100	98	65
					100

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#### Instructions to candidates

- The rules for the conduct of School exams are detailed in the 1. School/College assessment policy. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer Booklet.
- You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
  - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
- **Show all working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

**Acknowledgements** 

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Additional working space

Question number:

Section One: Calculator-free (50 Marks) Weighting 35%

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This section has **9 (nine)** questions. Answer **all** questions. Write your answers in the spaces provided.

Suggested working time: 50 minutes.

Question 1 (7 marks) (a) Determine the derivative of the following. (Do not simplify).

(i)  $0 < (x) \cos x, \quad \frac{1}{(x) \cos y} = y \qquad (i)$ 

(ii)  $\frac{(x-1)nis}{x^{\zeta}_{9}\zeta} = \chi \qquad (ii)$ 

(b) Given the function  $y = 3x^2 (2x+1)^3$ , show that  $\frac{dy}{dx} = 6x(2x+1)^4 (7x+1)$  (3 marks)

See next page

Determine the following indefinite integrals.

(5 marks)

Question 2 (8 marks)

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(a) 
$$\int \frac{x^3}{2} - x + 1 \, dx$$
 (2 marks)

(b) 
$$\int \frac{x^2 - 2}{\sqrt{x}} dx$$
 (2 marks)

(c) 
$$\int 2x(x+1)^2 dx$$
 (2 marks)

(d) 
$$\int e^{\frac{x}{2}} - \cos\left(\frac{2x}{3}\right) dx$$
 (2 marks)

Determine the following

Question 9

(a) 
$$\int_{\frac{\pi}{6}}^{\pi} \cos(3x) \ dx$$
 (2 marks)

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(b) 
$$\frac{d}{dx} \left( \int_2^x \sqrt{3 - 2t^2} dt \right)$$
 (1 mark)

(c) 
$$\int_0^2 \frac{d}{dx} \left( \frac{1 - x^2}{1 + x} \right) dx$$
 (2 marks)

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(1 mark)

(1 mark)

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(ii) P(Y is a prime number)

 $(9 \le X)$ d (i)

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Question 3 (6 marks)

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The probability distribution for a random variable  $\boldsymbol{Y}$  is shown in the table below.

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8	L	9	G	Þ	λ

What is the value of d?

(b) Determine the expected value of X.

) Defermine

(iii)  $P(X < Y \setminus Y > Y)$ 

Question 8 (6 marks)

8

Amy is a keen archer and the probability that she hits the bulls-eye with an arrow is  $\frac{1}{3}$ . In a competition she is given three shots at the target. Calculate the following probabilities, giving your answers as simplified tractions.

(3) She hits the bull's- eye with each shot. (1 mark)

(1 mark) She hits the bull's-eye with the first and third shot but misses the bulls-eye with the second shot.

(c) She hits the bull's-eye only once. (2 marks)

(d) She hits the bull's-eye at least once with her three shots. (2 marks)

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Question 4 (5 marks)

The first derivative of the function f(x) is given by:  $f'(x) = (x^2 + 1)^3 (2x + 6)$ .

(a) Determine f''(x), the second derivative of f(x). (Do not simplify your answer)

(2 marks)

(b) Determine f''(-3).

(1 mark)

(2 marks)

(c) What can be said about the graph of f(x) at the point where x = -3?

Question 5 (4 marks)

A discrete random variable, X, has a mean of 27 and standard deviation of 5.

(a) Consider the random variable H = X + 3. Determine

(i) the expected value of H

(1 mark)

(ii) the variance of H

(1 mark)

- (b) G is a discrete random variable equal to 2H. Determine
  - (i) the expected value of G

(1 mark)

(ii) the standard deviation of G

(1 mark)

Question 6 (4 marks)

Given that 
$$\frac{d^2y}{dx^2} = 3\sqrt{2x-3} - 2$$
, determine  $y$  in terms of  $x$  if  $\frac{dy}{dx} = 4$  when  $x = \frac{7}{2}$  and  $y = -\frac{4}{5}$  when  $x = 2$ .

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Question 7 (5 marks)

Determine the equation of the tangent to the curve  $y = \frac{x+1}{(2x-1)^2}$  at the point (1,8).