V COFFEGE OF THE UNITING CHURCH IN AUSTRALIA PRES BY TERIAN LADIES , COLLEGE



MATHEMATICAL METHODS YEAR 12 - TEST 4 MATHEMATICS DEPARTMENT

DATE: 15th August 2016

Reading Time: 3 minutes

SECTION ONE: CALCULATOR FREE

WORKING TIME: Maximum 20 minutes

18 marks :JATOT

pens, pencils, pencil sharpener, highlighter, eraser, ruler, SCSA formula sheet EQUIPMENT:

(brovided)

WORKING TIME: Minimum 30 minutes SECTION TWO: CALCULATOR ASSUMED

EQUIPMENT: 32 marks :JATOT

instruments, templates, up to 3 calculators, SCSA formula sheet (provided), pens, pencils, pencil sharpener, highlighter, eraser, ruler, drawing

one A4 page of notes (one side only)

	90	JATOT			
	32	Sect 2 Total		81	Sect 1 Total
	8	L			
	7	9		9	3
	13	9		8	2
	L	7		9	ı
Marks awarded	Marks available	Question	Marks awarded	Marks available	Guestion

The given diagrams show the shaded regions as a percentage of the entire area under the curve. Using the "68, 95, 99.7" rule determine the values of a or a and b in each of the following:

 $\mu = 5$

(2 marks)

 $\sigma = 2$



a = 1 v

6=9

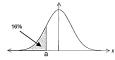
(b)

 $\mu = 30$

(1 mark)

(2 marks)

 $\sigma = 8$



a=22 V

(c)

 $\mu = a$ $\sigma = b$

. .

13.5%

b = 2 V

The continuous random variable, X, has the probability density function f, where

$$| \ge x \ge 0 \qquad x\lambda \\ \xi \ge x > 1 \qquad (x - \xi) \lambda_{\zeta}^{\perp}$$

(4 marks)

$$\begin{cases} 1 = \frac{h}{10} \\ 1$$

(4 marks)

Explain why each of the following sampling methods does not represent a random sample.

To predict the outcome of a State Government election, a public opinion poll telephones people randomly selected from a telephone directory to ask which political party they intend voting for on the day of the election. (Give two reasons)

- Not all people have a phone Any

2 or

ther phone when someone calls (eg at work)

Any

- Not all people listed in the directory

some people may not be able to answer

their phone when someone calls (eg at work)

- In order to obtain an estimate of the average income of PLC graduates ten years after their graduation all 2006 graduates are to be sent a questionnaire. An estimate of the average income is to be made using the ones that were returned.
 - Would expect less returns from those with lower (or perceived lower) incomes than those with high incomes
- At a school assembly the principal of a school with 720 students asks for 20 students to put themselves forward to represent the school at an Anzac Day Dawn Service. (Give two reasons)

- Not random as people asked to volunteer - Biased towards those with regard / respect
for Anzacs

validas

- Due to time of service, many may not be
able to attend due to transport issues ele

End of Section 1

Question 7 (8 marks)

The mean $\,\mu\,$ and standard deviation $\,\sigma\,$ of the uniform distribution on the interval [a,b] are given by

$$\mu = \frac{a+b}{2}$$
 and $\sigma = \frac{b-a}{2\sqrt{3}}$

A calculator can generate random numbers that are uniformly distributed between 0 and 1.

For this distribution of the random numbers generated by the calculator, calculate

(1 mark)

M= 0+1 = 1

the standard deviation (to three (3) decimal places). (1 mark)

$$\sigma = \frac{1-0}{2\sqrt{3}} = 0.289 \text{ V}$$

What is the probability that a randomly generated number lies between $\frac{1}{4}$ and $\frac{1}{2}$?

What is the probability that a randomly generated number contains no seven in its first five (5)

What is the probability that a randomly generated number contains at most three odd digits in its first five digits? Give your answer to four (4) decimal places.

Another uniform distribution on an interval [a, b] has a standard deviation of $2\sqrt{3}$. How wide is the

$$\frac{b-a}{2\sqrt{3}} = 2\sqrt{3} \quad \sigma = (2\sqrt{3})^2 = 12\sqrt{2}$$

End of Test

(7 marks) 4 noiteaup

containers. The weights of the yoghurts are found to be normally distributed with mean 205 grams and The Yol Yoghurt Company, a manufacturer of flavoured yoghurts, packages its snack yoghurts in 200 gram

standard deviation 2.55 grams. $\times \sim \mathcal{N}$ (200 S) $\times \times \times$ (s) What percentage of these yoghurts are underweight?

... 20420.0 = (002>X)9

= 2,50 % anderweight V

(J wsuk)

production department that only half of one percent of yoghurts leaving the factory may be underweight. Management is concerned about the high percentage of yoghurfs which are underweight and instructs the

(z marks) and achieve the management requirement by altering the standard deviation. What must the new The production department decides to maintain the mean weight of the yoghurts at 205 grams

500.0 10 standard deviation be set at?

502 WO 1146.1=9 007 00 00 - 70

the standard deviation at 2.55 grams and altering the mean weight of yoghurts. What must the new Alternatively, the production sector could achieve the management requirements by maintaining

WD V € € 8 06 : ABAM : 206 . 59 00 00 00 00 00

(z warks) Explain your answer. As both methods would achieve the management goal, would it matter which one was adopted?

Pait (c) has a higher mean so wellable Cheaper to adopt option in part (6), i

> (4 marks) Question 6

> mathematics scores, giving answers to one decimal place. gift-voucher for achieving a mark in excess of 90%. Find the mean and standard deviation of the excess of 80% and the top 5% of candidates in addition to the Distinction award also received a prize of a distributed. The award of Distinction was presented to 15% of the candidates for achieving a mark in The percentage marks of students sitting for a national mathematics competition were found to be normally

(E) - 06 = 9858hh9.1 (D) N-08 = h88h980.1 98584791 = E 1.6448896 1 = 12 50.0=(06(X)) 4 51.0=(08(X))

0.89 = W " . - 506,89 = W

984.91 = 0

supports on buyers 1 Lass & pribrist V 4.9/ = 0 "

V correct rounding V Mand & (Ecach)

The lifetimes of Briteglobe light bulbs are normally distributed with mean 3500 hours and standard deviation

Calculate t, given that 5% of Briteglobe bulbs last longer than t hours.

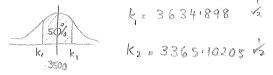
$$t = 3828.97 \text{ hours}$$

$$(2.3829 \text{ hours})$$

What is the probability that a Briteglobe bulb lasts exactly 3520 hours?

(1 mark)

Calculate the inter-quartile range for this distribution.



: IQR = 269,7959 (269,8 hrs)

Question 5 continues on next page ...

Question 5 continued ...

Find the 0.7 quantile and explain what it means

P(X< k)=0.7

(2 marks)

0.7 (or 70%) of the lifespan were less than /

What is the probability that a Briteglobe bulb will last no more than 3500 hours, if it has already

$$P(X \le 3500 | X > 3200) = \frac{0.433...}{0.9332...}$$

Find the probability that in a sample of five Briteglobe bulbs, exactly two will last between 3000