(3 шяцкг)	a) above.	s)ni iluser att gnisu $\sum\limits_{k=0}^{\infty} \frac{\pi}{2}$ bnit enesult in(s	⊣ (q)
(5 marks) (2 marks)		ת א sin x algerentiate x sin x	Juestioi
	Teacher: _	II part questions worth more than 2 mai	
Calculator Assumed 44 Marks 6 Questions			
Year 12 Methods TEST 7 June 2019 TIME: 45 minutes working		Independent Public School Exceptional schooling. Exceptional students. PERTH MODERN SCHOOL	

Working out space

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Question 2 (3 marks)

Determine the x-coordinates of all points on the graph of $f(x)=2\cos(x)+x$ for $-\pi \le x \le \pi$ where the tangent line is horizontal. (Justify your answers)

Working out space

what would you expect $P(X \ge mean)$ to approach? (2 marks)	(c) If the sample size became very large Briefly explain your answer.
nomial distribution with n=12 and p=0.75, what is the P.X>mean.??	nid a swollot X slabsinsv mobnar att tl (d) si tsrkw bna notitudirtsib sirtt to nasm
sample of 8 customers, at least 75% of them use an (2 marks)	(a) Find the probability that in a random ATM machine at least once a month.
hat 75% of its customers use an ATM at least once a	A survey conducted by a local bank shows the month.
(7 marks)	Question 3

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Question 6 (11 marks)

A game is played by throwing two standard six-sided dice into the air once. The sum of the uppermost numbers are added together and if the sum is greater than 8 the player wins \$5.

Determine:

a) the probability of winning \$5 in one game. (2 marks)

b) the probability of winning exactly \$15 in 5 games. (3 marks)

c) the probability of winning at least \$15 in at most 5 games. (3 marks)

d) the minimum number of games to be played so that the probability of winning at least \$15 is greater than 0.47. (Justify) (3 marks)

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Question 4 (10 marks)

The discrete random variable X can only take the values 2, 3 or 4. For these values the cumulative distribution function is defined by

$$P(X \le x) = \frac{(x+k)^2}{25}$$

for $x=2,3 \land 4$, where k is a positive constant integer.

(a) Find the value for k. (3 marks)

(b) Complete the following table for X.

(3 marks)

X	2	3	4
$P(X \leq x)$			
P(X=x)			

(c) Hence find E(X) and SD(X). (2 marks)

(d) Calculate Var(3-2X) giving your answer to 2 decimal places. (2 marks)

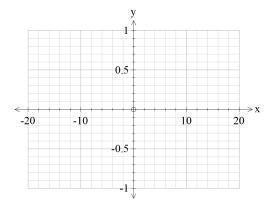
P a g e | **5** Year 12 Mathematics Methods

Question 5 (8 marks)

Consider the function
$$f(x) = \frac{1 - \cos x}{x}$$
 where x is in radians.

a) Sketch f(x) on the axes below for $-20 \le x \le 20$ on the axes below. Clearly label undefined points (if any).

(3 marks)



- b) As $^\chi$ approaches zero from the positive side, state the value that $^{f(\chi)}$ approaches. (1 mark)
- c) As $^\chi$ approaches zero from the negative side, state the value that $^{f(\chi)}$ approaches. (1 mark)
- d) Use the above to define a value for f(x) as x approaches zero, that is the following limit $\lim_{x\to 0} \frac{1-\cos x}{x}$. (1 mark)

It can be shown that $\frac{d}{dx}(\cos x) = -\cos x \lim_{h \to 0} \frac{1-\cosh}{h} - \sin x \lim_{h \to 0} \frac{\sinh}{h}$

e) Using the fact that $\frac{\sinh}{h} = 1$ and the above results, show that $\frac{d}{dx}(\cos x) = -\sin x$. (2 marks)