



PERTH MODERN SCHOOL  
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INDEPENDENT PUBLIC SCHOOL

Semester One Examination, 2020

Question/Answer booklet

MATHEMATICS METHODS  
UNIT 3

Section Two:  
Calculator-assumed

Your Name: \_\_\_\_\_

Your Teacher's Name: \_\_\_\_\_

**Time allowed for this section**

Reading time before commencing work: ten minutes  
Working time: one hundred minutes

**Materials required/recommended for this section**

To be provided by the supervisor  
This Question/Answer booklet  
Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,  
correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,  
and up to three calculators approved for use in this examination

**Important note to candidates**

No other items may be taken into the examination room. It is **your responsibility** to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Marks	Max	Question	Mark	Max
8	5	5	15	3	3
9	12	12	16	10	10
10	5	10	17	11	11
11	11	18	18	7	7
12	8	19	19	6	6
13	8	6	6		
14	6				

**Structure of this paper**

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	48	33
Section Two: Calculator-assumed	12	12	100	98	67
<b>Total</b>					<b>100</b>

**Instructions to candidates**

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the Year 12 Information Handbook 2019. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers or working which cannot be followed will not be awarded any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

**Additional working space**

Question number: \_\_\_\_\_

**Section One: Calculator-assumed****(98 Marks)**

This section has twelve questions. Answer all questions. Write your answers in the spaces provided.

- Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
  - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 100 minutes.

**Question 8****(5 marks)**

The position of an object at any time  $t$  (seconds) is given by  $s(t) = 3t^4 - 40t^3 + 126t^2 - 9$

- (a) Determine when the object is at rest.

(2 marks)

- (b) Determine the distance (metres) travelled in the first 10 seconds.

(3 marks)

**See next page****See next page**

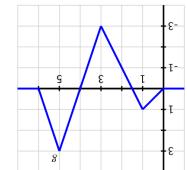
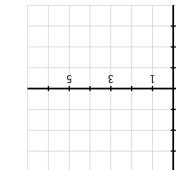
(c) Determine  $f(x)$  and the standard deviation of  $x$ .

(3 marks)

(d) How would the graph of  $f(x)$  compare to  $A(x)$ , other than  $x \geq 0$ ? If

(2 marks)

$$f(x) = \int g(t) dt$$

**See next page**

(3 marks)

(e) Determine  $P(0 < X \leq 2)$ .

(2 marks)

(f) Determine the probability distribution table and state the value of the constant  $k$ .

(3 marks)

(g) Sketch a complete and accurate graph of  $y = A(x)$  for  $x \geq 1$  on the axes provided on the right. Mark all turning points.

(4 marks)

the right.

the right.

(h) Let  $X$  be a discrete random variable with domain  $x = 0, 1, 2, 3, 4$  only. Suppose the probability function of  $X$  is given by

(4 marks)

$P(X = x) = \frac{a}{k}$ , for  $x = 0, 1, 2, 3, 4$  with  $a$  constant.

k

Determine the probability distribution table and state the value of the constant  $a$ .

(3 marks)

(i) Calculate the mean and standard deviation of  $X$ .

(2 marks)

(j) Calculate the probability that  $X$  is even.

(1 mark)

(k) Calculate the probability that  $X$  is odd.

(1 mark)

(l) Calculate the probability that  $X$  is greater than 2.

(1 mark)

(m) Calculate the probability that  $X$  is less than or equal to 2.

(1 mark)

(n) Calculate the probability that  $X$  is greater than or equal to 3.

(1 mark)

(o) Calculate the probability that  $X$  is greater than or equal to 4.

(1 mark)

(p) Calculate the probability that  $X$  is greater than or equal to 5.

(1 mark)

(q) Calculate the probability that  $X$  is greater than or equal to 6.

(1 mark)

(r) Calculate the probability that  $X$  is greater than or equal to 7.

(1 mark)

**See next page**

(s) Calculate the probability that  $X$  is greater than or equal to 8.

(1 mark)

(t) Calculate the probability that  $X$  is greater than or equal to 9.

(1 mark)

(u) Calculate the probability that  $X$  is greater than or equal to 10.

(1 mark)

(v) Calculate the probability that  $X$  is greater than or equal to 11.

(1 mark)

(w) Calculate the probability that  $X$  is greater than or equal to 12.

(1 mark)

(x) Calculate the probability that  $X$  is greater than or equal to 13.

(1 mark)

(y) Calculate the probability that  $X$  is greater than or equal to 14.

(1 mark)

(z) Calculate the probability that  $X$  is greater than or equal to 15.

(1 mark)

(aa) Calculate the probability that  $X$  is greater than or equal to 16.

(1 mark)

(bb) Calculate the probability that  $X$  is greater than or equal to 17.

(1 mark)

(cc) Calculate the probability that  $X$  is greater than or equal to 18.

(1 mark)

(dd) Calculate the probability that  $X$  is greater than or equal to 19.

(1 mark)

(ee) Calculate the probability that  $X$  is greater than or equal to 20.

(1 mark)

(ff) Calculate the probability that  $X$  is greater than or equal to 21.

(1 mark)

(gg) Calculate the probability that  $X$  is greater than or equal to 22.

(1 mark)

(hh) Calculate the probability that  $X$  is greater than or equal to 23.

(1 mark)

(ii) Calculate the probability that  $X$  is greater than or equal to 24.

(1 mark)

(jj) Calculate the probability that  $X$  is greater than or equal to 25.

(1 mark)

(kk) Calculate the probability that  $X$  is greater than or equal to 26.

(1 mark)

(ll) Calculate the probability that  $X$  is greater than or equal to 27.

(1 mark)

(mm) Calculate the probability that  $X$  is greater than or equal to 28.

(1 mark)

(nn) Calculate the probability that  $X$  is greater than or equal to 29.

(1 mark)

(oo) Calculate the probability that  $X$  is greater than or equal to 30.

(1 mark)

(pp) Calculate the probability that  $X$  is greater than or equal to 31.

(1 mark)

(qq) Calculate the probability that  $X$  is greater than or equal to 32.

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(rr) Calculate the probability that  $X$  is greater than or equal to 33.

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(ss) Calculate the probability that  $X$  is greater than or equal to 34.

(1 mark)

(tt) Calculate the probability that  $X$  is greater than or equal to 35.

(1 mark)

(uu) Calculate the probability that  $X$  is greater than or equal to 36.

(1 mark)

(vv) Calculate the probability that  $X$  is greater than or equal to 37.

(1 mark)

(ww) Calculate the probability that  $X$  is greater than or equal to 38.

(1 mark)

(xx) Calculate the probability that  $X$  is greater than or equal to 39.

(1 mark)

(yy) Calculate the probability that  $X$  is greater than or equal to 40.

(1 mark)

(zz) Calculate the probability that  $X$  is greater than or equal to 41.

(1 mark)

(aa) Calculate the probability that  $X$  is greater than or equal to 42.

(1 mark)

(bb) Calculate the probability that  $X$  is greater than or equal to 43.

(1 mark)

(cc) Calculate the probability that  $X$  is greater than or equal to 44.

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(dd) Calculate the probability that  $X$  is greater than or equal to 45.

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(ee) Calculate the probability that  $X$  is greater than or equal to 46.

(1 mark)

(ff) Calculate the probability that  $X$  is greater than or equal to 47.

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(gg) Calculate the probability that  $X$  is greater than or equal to 48.

(1 mark)

(hh) Calculate the probability that  $X$  is greater than or equal to 49.

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(ii) Calculate the probability that  $X$  is greater than or equal to 50.

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(jj) Calculate the probability that  $X$  is greater than or equal to 51.

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(ss) Calculate the probability that  $X$  is greater than or equal to 60.

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(tt) Calculate the probability that  $X$  is greater than or equal to 61.

(1 mark)

(uu) Calculate the probability that  $X$  is greater than or equal to 62.

(1 mark)

(vv) Calculate the probability that  $X$  is greater than or equal to 63.

(1 mark)

(ww) Calculate the probability that  $X$  is greater than or equal to 64.

(1 mark)

(xx) Calculate the probability that  $X$  is greater than or equal to 65.

(1 mark)

(yy) Calculate the probability that  $X$  is greater than or equal to 66.

(1 mark)

(zz) Calculate the probability that  $X$  is greater than or equal to 67.

(1 mark)

(aa) Calculate the probability that  $X$  is greater than or equal to 68.

(1 mark)

(bb) Calculate the probability that  $X$  is greater than or equal to 69.

(1 mark)

(cc) Calculate the probability that  $X$  is greater than or equal to 70.

(1 mark)

(dd) Calculate the probability that  $X$  is greater than or equal to 71.

(1 mark)

(ee) Calculate the probability that  $X$  is greater than or equal to 72.

(1 mark)

(ff) Calculate the probability that  $X$  is greater than or equal to 73.

(1 mark)

(gg) Calculate the probability that  $X$  is greater than or equal to 74.

(1 mark)

(hh) Calculate the probability that  $X$  is greater than or equal to 75.

(1 mark)

(ii) Calculate the probability that  $X$  is greater than or equal to 76.

(1 mark)

(jj) Calculate the probability that  $X$  is greater than or equal to 77.

(1 mark)

(kk) Calculate the probability that  $X$  is greater than or equal to 78.

(1 mark)

(ll) Calculate the probability that  $X$  is greater than or equal to 79.

(1 mark)

(mm) Calculate the probability that  $X$  is greater than or equal to 80.

(1 mark)

(nn) Calculate the probability that  $X$  is greater than or equal to 81.

(1 mark)

(oo) Calculate the probability that  $X$  is greater than or equal to 82.

(1 mark)

(pp) Calculate the probability that  $X$  is greater than or equal to 83.

(1 mark)

(qq) Calculate the probability that  $X$  is greater than or equal to 84.

(1 mark)

(rr) Calculate the probability that  $X$  is greater than or equal to 85.

(1 mark)

(ss) Calculate the probability that  $X$  is greater than or equal to 86.

(1 mark)

(tt) Calculate the probability that  $X$  is greater than or equal to 87.

(1 mark)

(uu) Calculate the probability that  $X$  is greater than or equal to 88.

(1 mark)

(vv) Calculate the probability that  $X$  is greater than or equal to 89.

(1 mark)

(ww) Calculate the probability that  $X$  is greater than or equal to 90.

(1 mark)

(xx) Calculate the probability that  $X$  is greater than or equal to 91.

(1 mark)

(yy) Calculate the probability that  $X$  is greater than or equal to 92.

(1 mark)

(zz) Calculate the probability that  $X$  is greater than or equal to 93.

(1 mark)

(aa) Calculate the probability that  $X$  is greater than or equal to 94.

(1 mark)

(bb) Calculate the probability that  $X$  is greater than or equal to 95.

(1 mark)

(cc) Calculate the probability that  $X$  is greater than or equal to 96.

(1 mark)

(dd) Calculate the probability that  $X$  is greater than or equal to 97.

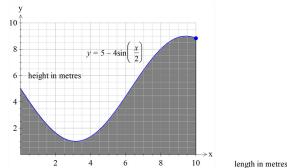
(1 mark)

(ee) Calculate the



**Question 19** (6 marks)

A solid concrete wall has a cross section as shown below. The curve is given by the rule  
 $y = 5 - 4 \sin\left(\frac{x}{2}\right)$  with  $0 \leq x \leq 10$ , both  $x$  &  $y$  are in metres. The wall is uniformly 15 cm thick and of total length of 10 metres.



- a) Determine the coordinates of the turning points and any inflection points on the curve. (3 marks)

**Question 19** (6 marks)

(c) Determine the instantaneous rate of change of the total number of cubic metres of sand on the beach at time 6 hours. (3 marks)

- (d) Over the time interval  $0 \leq t \leq 8$ , at what time does the beach have the least amount of sand? What is this minimum value? Justify your answers fully. (4 marks)

- b) Determine to the nearest cubic centimetre the volume of concrete needed to make the wall. (3 marks)

- e) The probability that for 15 randomly selected students, exactly 10 students have at least 7 coins that land heads-up. (2 marks)

(4 marks)

$$\text{Area}(\text{sector}) = \frac{\theta}{2\pi} \cdot r^2$$

(d) A sector has radius  $r$  cm and angle  $\theta$  radians. Given that the area is  $A$  cm<sup>2</sup>, use the small increases formula to find the approximate percentage change in area covered when its radius decreases by 2%. (4 marks)

- (e) A drug dealer is slowly expanding forming a circular rash trebling in size every 12 hours. Given that the area of the rash is  $200.5 \text{ m}^2$  use the small increments formula to find your answer. (4 marks)

(2 marks)

