

Rossmoyne Senior High School

Semester One Examination, 2019

Question/Answer booklet

MATHEMATICS METHODS YEAR 12 (ATMAM) Section Two: Calculator-assumed

	In words			
Student number: In	sənugif nl			
Sircle your Teacher's Name:	onsila Koulianos	Bestall Luzuk	Fraser-Jones Murray	Kigodi Tanday

Time allowed for this section

Reading time before commencing work:

One hundred minutes

Materials required/recommended for this section To be provided by the supervisor

To be provided by the supervisor
This Question/Answer booklet

Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

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Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- 6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

(ovupu. z)	CONTINUE OF ION THE OWN THE OW	(n)
(2 marks)	Determine how much fuel is in the tank after 20 minutes.	(9)
$\frac{1}{2} + \frac{37}{2}$ litres per minute, where t	lows into a storage tank that is initially empty at a rate of \sqrt{s} time in minutes and $0 \le t \le 100$.	
(5 marks)	e noit	gnes
	ing time: 100 minutes.	Work
Mile your answers in the spaces	section has thirteen (13) questions. Answer all questions. <i>V</i> jed.	provic
	(C) activities and activities	· -: ЧТ

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Section Two: Calculator-assumed

CALCULATOR-ASSUMED

It the tank is completely full after $100\,\mathrm{minutes}$, determine the time required for the tank to become one-quarter full.

(3 шяцка)

65% (98 Marks)

METHODS UNIT 3

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METH	HODS (JNIT 3	4	CALCULATOR-ASSUMED
	tion 10	n discrete random variable where .	v — 2 2 E 7 11 12	(7 marks)
(a)	Deter		x — 2, 3, 3, 7, 11, 13.	
(-)	(i)	$P(X \ge 5)$.		(1 mark)
	(ii)	$P(X < 12 \mid X \ge 3).$		(2 marks)
(b)	Calcu	late the exact value of		
	(i)	E(X).		(2 marks)
	(ii)	Var(X).		(2 marks)

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potential difference to fall from its maximum to 1.8 volts. Determine the maximum potential instantly recharged to its maximum every 3 minutes, which is the time required for the

(2 marks)

METHODS UNIT 3 20 CALCULATOR-ASSUMED

difference for this capacitor.

METHODS UNIT 3

6

CALCULATOR-ASSUMED

CALCULATOR-ASSUMED

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METHODS UNIT 3

(2 marks)

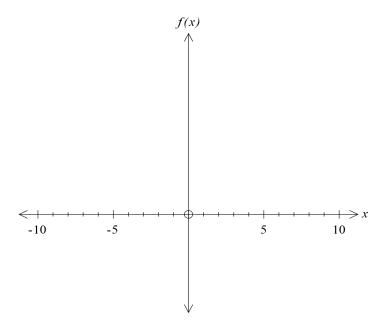
(2 marks)

Question 12 (6 marks)

(a) Draw a graph that satisfies all the conditions listed below. Label the critical features clearly.

$$f(-2) = f(6) = f(8) = 0$$
 (3 marks)
$$f''(4) = 0 \text{ and } f''(x) < 0 \text{ for } x < 4 \text{ only}$$

$$f'(1) = f'(7) = 0$$



Calculate

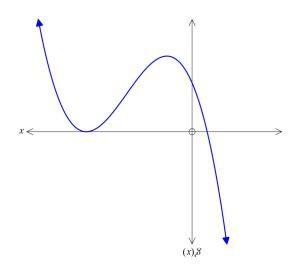
the mean bonus paid per match.

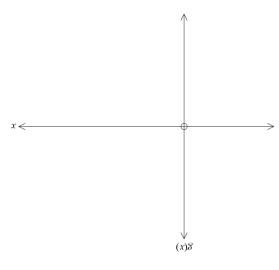
(ii) the standard deviation of the bonus paid per match.

(d) The owner of the team plans to increase the current bonuses by \$50 next season (so that the players will get a bonus of \$50 even when no goals are scored) and then further raise them by 12% the following season. Determine the mean and standard deviation of the bonus paid per match after both changes are implemented. (3 marks)

(3 marks) possible graph of its antiderivative. The graph of a gradient function is shown below. On the set of axes provided sketch a

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81

CALCULATOR-ASSUMED

(12 marks) Question 21

The random variable X is the number of goals scored by a team in a soccer match, where

Variation of ...,
$$\xi$$
, ζ , ζ , ζ , $0 = x$ for $\frac{2.2 - 9.x \zeta$, ζ

(2 marks) $.2988.0 = (1 \le X)^{q}$ Show that the probability that the team scores at least one goal in a match is

and for one goal \$100 is paid. No bonus is paid if no goals are scored. of goals the team scored. For four or more goals \$500 is paid, for two or three goals \$250 is paid The random variable Y is the bonus each player is paid after a match, depending on the number

(3 marks) Complete the probability distribution table for Y.

9081.0				$(\chi = \gamma)q$
200			0	(\$) K
<i>ħ</i> ≤ <i>x</i>	$\mathcal{E} \ge x \ge \mathcal{L}$	I = x	0 = x	Goals scored

(1 mark)

CALCULATOR-ASSUMED

Question 13 (8 marks)

A manufacturing process begins and the rate at which it produces gas after t minutes ($t \ge 0$) is

$$r(t) = 45(1 - e^{-0.4t}) \text{ m}^3/\text{minute}$$

State the maximum rate that gas can be produced at.

Calculate the rate that gas is being produced after 2 minutes. (1 mark)

Use the increments formula to determine the approximate change in r between 30 and 33 seconds after production began. (3 marks)

Use the increments formula to determine the approximate volume of gas produced in the 5 seconds following t = 2. (3 marks)

17 Question 20 (7 marks)

(a) Given that
$$f(t) = \sin\left(3t + \frac{\pi}{3}\right)$$
 and $F(x) = \int_0^x f(t) dt$, determine the exact value of

(i)
$$F\left(\frac{\pi}{2}\right)$$
. (1 mark)

(ii)
$$F'\left(\frac{\pi}{2}\right)$$
. (2 marks)

(b) Given that
$$G(x) = \int_1^x g(t) dt$$
, $\frac{d^2G}{dx^2} = 4 + 3\sqrt{x}$ and $G(4) = 56$, determine $g(t)$. (4 marks)

after t seconds is given by A small body has displacement x=0 when t=8 and moves along the x-axis so that its velocity

$$s/m \left(\frac{t\pi}{4}\right) mis 01 = (t)$$

Determine an equation for x(t), the displacement of the body after t seconds. (3 marks)

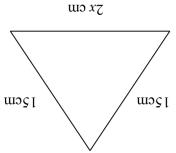
Describe, with justification, how the speed of the body is changing when t=32. (4 marks)

(6 marks) Question 19

CALCULATOR-ASSUMED

METHODS UNIT 3

A triangle has dimensions as shown below:



(S marks)

(4 marks) Use calculus methods to find the maximum area of the triangle.

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METHODS UNIT 3

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CALCULATOR-ASSUMED

CALCULATOR-ASSUMED

15

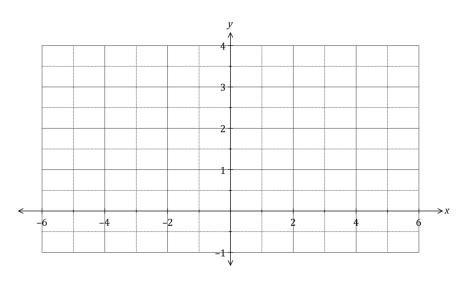
METHODS UNIT 3

Question 15 (7 marks)

Let $f(x) = 2 + e^{-0.4x-2}$.

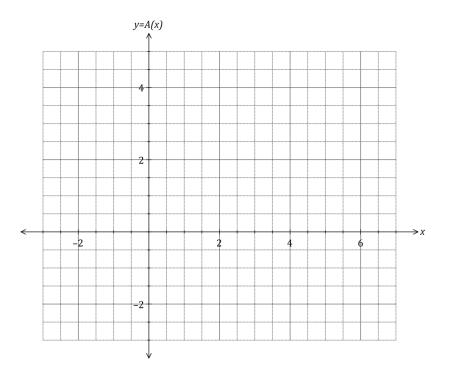
(a) Sketch the graph of y = f(x) on the axes below.

(2 marks)



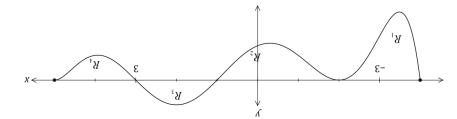
- (b) The line y = 1 0.4x is a tangent to the curve y = f(x) at x = -5, and it intersects the x-axis at the point (k, 0). Add the line to the graph above and shade the area enclosed by the line, the curve and x = k. (2 marks)
- (c) Determine the area enclosed by the line, the curve and x = k. (3 marks)

c) Sketch the graph of y = A(x) on the axes below, indicating and labelling the location of all key features. (5 marks)



See next page

The graph of y = f(x) is shown below for $-4 \le x \le 5$.



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and 24 square units respectively. The area trapped between the x-axis and the curve for regions R_1 , R_2 , R_3 and R_4 are 35,52, 28

Determine the value of

2 duestion 16

(i)
$$\int_{-2}^{-2} f(x) dx.$$

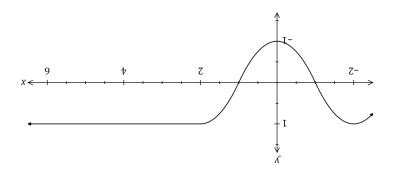
(ii)
$$\int_{2}^{5} f(x) dx.$$

(iii)
$$\int_1^5 (f(x) - 7) dx.$$

(iv)
$$\int_{-4}^{1} f(x) \, dx - \int_{1}^{5} f'(x) \, dx.$$

(9 marks) **&l noiteau** ォレ

The graph of y = f(x) is shown below.



Let A(x) be defined by the integral $A(x) = \int_{x}^{x} \int (t) dt$ for $x \ge -2$.

(2 marks) the x-coordinate and nature of each point. (a) Use the graph of y = f(x) to identify all the turning points of the graph of y = A(x), stating

It is also known that the A(2) = 0.

Using the graph of y = f(x) or otherwise, explain why A(5) = 3. (z warks)

METHODS UNIT 3 12 CALCULATOR-ASSUMED

Question 17 (9 marks)

Seeds were planted in rows of five and the number of seeds that germinated in each of the 120 rows are summarised below.

Number of germinating seeds	0	1	2	3	4	5
Number of rows	1	1	3	16	46	53

- (a) Use the results in the table to determine
 - (i) the probability that no more than 4 seeds germinated in a randomly selected row. (1 mark)

(ii) the mean number of seeds that germinated per row. (1 mark)

(b) Another row of five seeds is planted. Determine the probability that no more than 4 seeds germinate in **this** row. Assume the number that germinate per row is binomially distributed with the above mean. (2 marks)

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CALCULATOR-ASSUMED 13 METHODS UNIT 3

Suppose it is known that 66% of all seeds planted will germinate and that seeds are now planted in rows of 16.

- (c) Assuming that seeds germinate independently of each other, determine
 - i) the most likely number of seeds to germinate in a row.

(1 mark)

(ii) the probability that at least 9 seeds germinate in a randomly chosen row.

(2 marks)

(iii) the probability that in eight randomly chosen rows, exactly six rows have at least 9 seeds germinating in them. (2 marks)

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