

9.

[2, 2, 5 = 9 marks]
A cuboid has a total surface area of 150 cm² with a square base of side

length x cm.

(a) Show that the height, h cm, of the cuboid is given by $h = \frac{75-x^2}{2x}$.

(b) Express the volume of the cuboid in terms of x .

(c) Hence, use calculus to determine its maximum volume as x varies.

End of Section Two

(b) $y = \frac{5-4x}{7x+3}$

(a) $y = (2x - 1)^2(6 - 3x^2)$

Find $\frac{dy}{dx}$ for each of the following using the best method, simplifying the answers.

1. [3, 3 = 6 marks]

SECTION 1 – Resource Free
Working Time: 20 minutes

All working is to be shown in the space provided.
Your answers should be in sufficient detail to allow your answers to be checked readily so part marks may be awarded if the answer is incorrect. For any question worth more than 2 marks valid working or justification must be shown to be awarded full marks.

%	Total		
	Section 1	20	
	Section 2	40	
	Total	60	



Year 12 Mathematics
METHODS UNIT 3
TERM 4, 2018
TEST 0
Test Date: Thursday, 23 November

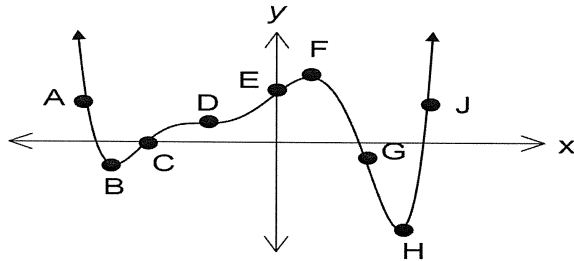
Name: _____

2. [3 marks]

The function $y = x^3 + ax + b$ has a local minimum point at $(2, 3)$.
Use differentiation to find the values of a and b .

3. [1, 1, 1, 1 = 4 marks]

Consider the graph of the function $y = f(x)$. Use the features of this graph to answer the following questions.



(a) List all stationary points.

(b) State the points of inflection.

(c) Highlight the sections with a negative value of $\frac{dy}{dx}$.

(d) Which point on this curve has the properties that $f(x) > 0$ and $f''(x) < 0$?

8. [1, 2, 1, 1, 3, 2 = 10 marks]

A bullet is fired upwards. After t seconds the height of the bullet is found from the rule

$$H(t) = 150t - 4.9t^2 + 2 \text{ where } t \text{ is measured in seconds and } H \text{ in metres.}$$

(a) Find the height of the bullet after 5 seconds.

(b) Determine the average speed of the bullet during the fifth second. Indicate your method.

The speed of the bullet is the instantaneous rate of change of the height of the bullet.

(c) Find a rule for the speed of the bullet at any time t .

(d) Find the speed of the bullet after 5 seconds.

(e) Find the maximum height of the bullet, to the nearest metre. Indicate your method.

(f) Determine the bullet's speed as it hits the ground, on the way down, to 2 decimal places.

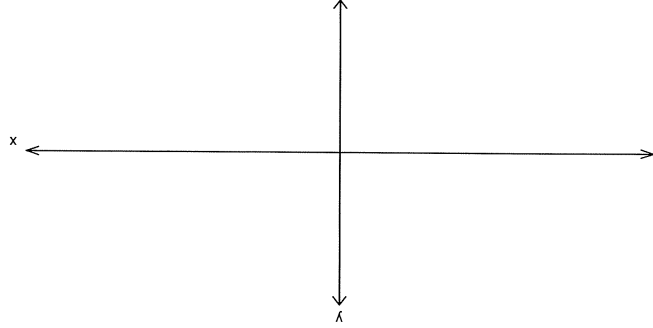
7.

[2, 4, 3, 2 = 10 marks]

- (a) The curve $y = (x + 2)(x^2 - 11x + 37)$ cuts the x-axis at $(-2, 0)$.
Is this the only place the curve cuts the x-axis? Justify your answer.

- (b) Find the coordinates and nature of any stationary points on the curve.

- (c) Hence sketch the curve indicating **clearly** the intercepts with the axes and the coordinates of all stationary points.

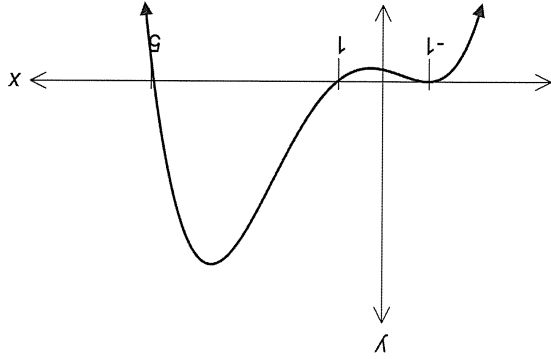


- (d) Determine the greatest and least values of $(x + 2)(x^2 - 11x + 37)$ for values of x in the interval $-2 \leq x \leq 8$.

4.

[7 marks]

The graph below shows the graph of $y = f'(x)$ for a function $y = f(x)$.
Find the values of x for which the graph of $y = f(x)$ has a stationary point and state the nature of each stationary point.



End of Section One



**Year 12 Mathematics
METHODS UNIT 3**

TEST 0

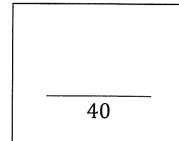
TERM 4, 2018

Test Date: Thursday, 23 November

APPLECROSS
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Name: _____

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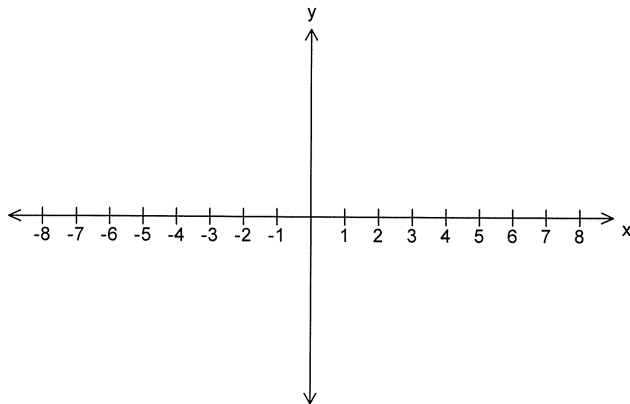
SECTION 2 – Resource Rich

Working Time: 40 minutes

5. [3 marks]

On the axes below, sketch a possible graph satisfying all cases:

- the function has roots at -5 and 6
- there are stationary points at $x = -2$ and at $x = 3$
- for $x < -2$ the gradient is positive
- for $-2 < x < 3$ and for $x > 3$ the gradient is negative



6. [5, 2 = 7 marks]

Consider the curve whose equation is $y = (4x^2 - 1)^5$.

- (a) Use **calculus methods** to determine the nature and location of all stationary points.

- (b) Hence, draw a neat sketch of the curve of the function on the set of axes below. Label the significant points with their coordinates.

