Rossmoyne Senior High School

before reading any further.

Year 12 Trial WACE Examination, 2014 Question/Answer Booklet

| Important note to candidates |
|--|
| Special items: nil |
| To be provided by the candidate Standard items: pens, pencils, pencil sharpener, eraser, correction fluid/tape, ruler, highlighters |
| Materials required/recommended for this section To be provided by the supervisor This Quesion/Answer Booklet Formula Sheet |
| Time allowed for this section Reading time before commencing work: five minutes Working time for this section: fifty minutes |
| Тоиг пате |
| ln words |
| Student Number: In figures |
| MATHEMATICS 3C/3D If required by your examination administrator, please place your student identification label in this box Calculator-free |

that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor

No other items may be used in this section of the examination. It is your responsibility to ensure

CALCULATOR-FREE 12 MATHEMATICS 3C/3D

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CALCULATOR-FREE 2 MATHEMATICS 3C/3D

Structure of this paper

| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of exam |
|--|-------------------------------|------------------------------------|---------------------------|--------------------|--------------------|
| Section One: Calculator-free | 8 | 8 | 50 | 50 | 33⅓ |
| Section Two: Calculator- assumed | 13 | 13 | 100 | 100 | 66¾ |
| | | | Total | 150 | 100 |

Instructions to candidates

- 1. The rules for the conduct of Western Australian external examinations are detailed in the Year 12 Information Handbook 2013. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages
 are included at the end of this booklet. They can be used for planning your responses
 and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in
 the original answer space where the answer is continued, i.e. give the page number.
 Fill in the number of the question(s) that you are continuing to answer at the top of the
 page.
- 3. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 4. It is recommended that you **do not use pencil**, except in diagrams.

CALCULATOR-FREE 11 MATHEMATICS 3C/3D

| Additional | working | snace |
|------------|---------|-------|
| | | |

This section has eight (8) questions. Answer all questions. Write your answers in the spaces (20 Marks) Section One: Calculator-free **MATHEMATICS 3C/3D** CALCULATOR-FREE

Working time for this section is 50 minutes.

provided.

I = I anima for I = I bus I = I(3 marks) Question 1

> (7 marks) 8 noiteauQ OΤ

MATHEMATICS 3C/3D

Let $B = n^2 + an + a$, where a and n are both positive integers.

- (3 warks) example that shows it is true. If a conjecture is false, give an example that shows it is (a) For each conjecture below state whether it is true or false. If a conjecture is true, give an
- B is always odd when n is even. (i)

CALCULATOR-FREE

- (ii) $^{\it D}$ is always odd when $^{\it D}$ is odd.
- $^{\mathrm{D}}$ is always even when $^{\mathrm{D}}$ is even.

(4 marks) (b) Prove the conjecture from part (a) that is true. CALCULATOR-FREE

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MATHEMATICS 3C/3D

Question 2

(5 marks)

(1 mark)

The function $f(x) = ax^2 + bx + c$, where a, b and c are constants, passes through the three points (3, 10), (2, -1) and (1, -6).

(a) Explain why a, b and c the satisfy the equation 9a + 3b + c = 10.

(b) Write down another two equations satisfied by a, b and c. (1 mark)

(c) Solve the above equations to determine the values of a, b and c. (3 marks)

See next page See next page

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In a pack of six identical rechargeable batteries, it is known that two are flat and the other four are fully charged.

Four batteries are removed at random from the pack.

(a) Determine the probability that

Question 7

(i) three of them are fully charged.

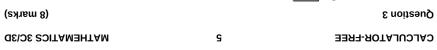
(2 marks)

(5 marks)

(ii) no more than two of them are fully charged.

(2 marks)

(b) The first battery removed is flat, the second is fully charged, but the condition of the last two removed is not known. Determine the probability that three out of the four batteries removed are fully charged. (1 mark)



(a) If
$$f(x) = (1 - 3x)^3 \cdot \sqrt{3x - 7}$$
, evaluate $f'(1)$.

(4 marks)

(b) Determine the area enclosed between the curve
$$y=3(x-1)^2$$
 and the line $y=3$. (4 marks)

 CALCULATOR-FREE
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 MATHEMATICS 3C/3D

 Question 6
 (8 marks)

Let $f(x) = \frac{x(12 - x^2)}{3}$ and g(x) = (ax + 2)(x - 7), where a is a constant.

(a) Show that $\int (x) = (2 + x)(2 - x)$.

(b) The tangents to the graphs of y = f(x) and y = g(x) are parallel when x = 3. Determine the value of a.

(c) What are the minimum and maximum values of ${}^{\int (x)}$ over the domain $-1 \le x \le 4$?

CALCULATOR-FREE

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MATHEMATICS 3C/3D

Question 4

Let $f(x) = \sqrt{2 - x}$ and $g(x) = \frac{1}{x - 2}$.

(a) Determine

(i) an expression for $f \circ g(x)$.

(1 mark)

(7 marks)

(ii) the domain of $f \circ g(x)$.

(2 marks)

(b) Determine

(i) the domain of $g \circ f(x)$.

(2 marks)

(ii) the range of $g \circ f(x)$.

(2 marks)

CALCULATOR-FREE 7 MATHEMATICS 3C/3D

Question 5 (7 marks)

The radius, in centimetres, of a circular ink spot t seconds after it first appears is given by $r=\frac{3+4t}{2+t}$.

(a) Determine

(i) the time taken for the radius to double its initial value.

(2 marks)

(ii) the rate at which the radius is increasing when t=3. (3 marks)

(b) Use the formula $\int_{0}^{\delta r} \approx \frac{dr}{dt} \cdot \delta t$ to approximate the increase in the radius of the ink spot between t=3 and t=3.05 seconds. (2 marks)