

Rossmanyne Senior High School

No other items may be taken into the examination room. It is **Your responsibility** to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to candidates

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in the WACE examinations

Standard items: pens (blue/black preferred), pencils (including coloured), correction fluid/tape, eraser, ruler, highlighters

To be provided by the candidate

Formula Sheet (retained from Section One)

This Question/Answer Booklet

Materials required/recommended for this section

Reading time before commencing work: ten minutes

Working time for this section: one hundred minutes

Your name

In words

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If required by your examination administrator, please place your student identification label in this box.

MATHEMATICS
3AB
Section Two:
Calculator-assumed

Student Number: In figures

Question/Answer Booklet

Year 12 Trial WACE Examination, 2015

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Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	50	33½
Section Two: Calculator-assumed	13	13	100	100	66½
Total			150	100	

Additional working space

Question number: _____

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

(1 mark)

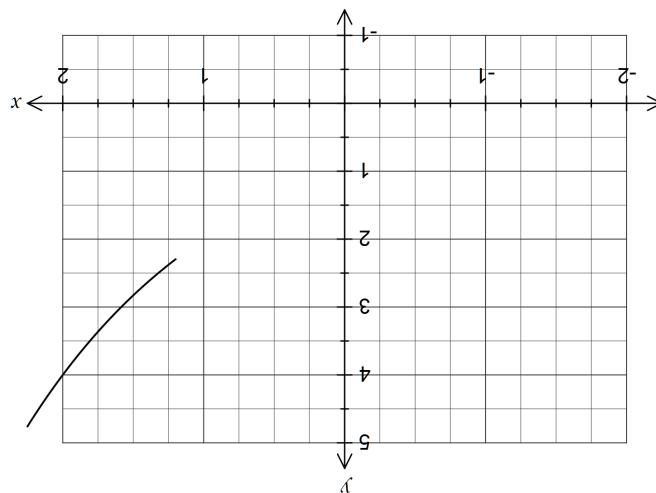
- (c) Use the graph to explain why $2^x = -0.5$ has no solutions.

(1 mark)

- (b) Use the graph to solve $2^x = 3$.

(2 marks)

- (a) Complete the graph of $y = 2^x$.



Part of the graph of $y = 2^x$ has been drawn on the axes below.

(4 marks)

Question 8

Working time: 100 minutes.

provided.

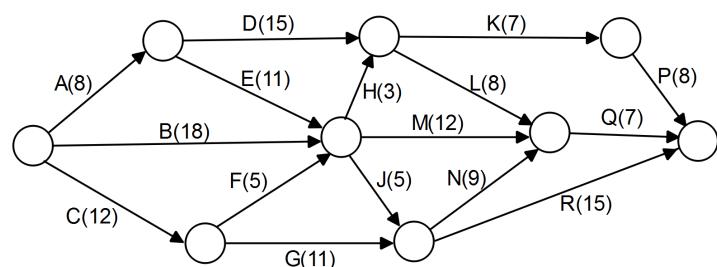
This section has **thirteen (13)** questions. Answer all questions. Write your answers in the spaces provided.

**Section Two: Calculator-assumed
(100 Marks)**

(7 marks)

Question 9

The project network below consists of 16 tasks, with completion times shown in days.



- (a) List, in order, the tasks on the critical path and determine the minimum completion time for this project. (3 marks)

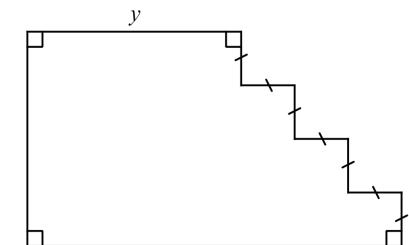
- (b) The time to complete task F increases by four days. Determine the effect, if any, on your answers to part (a). (2 marks)

- (c) An additional task that is not a predecessor for any other task, is to be added to the network and can commence once task D is complete. How many days can this new task be allocated without increasing the minimum completion time? (2 marks)

Question 20

(8 marks)

A 66 cm length of wire is to be bent into the shape below, where all adjacent sides of the shape are perpendicular to each other.



- (a) If $x = 1$ cm, determine the area of the shape. (2 marks)

- (b) By considering the perimeter of the shape, show that $y = 33 - 7x$. (1 mark)

- (c) Show that the area of the shape is given by $A = 132x - 22x^2$. (2 marks)

- (d) Use calculus techniques to determine the maximum possible area of the shape. (3 marks)

(1 mark)

- (ii) the standard deviation.

(1 mark)

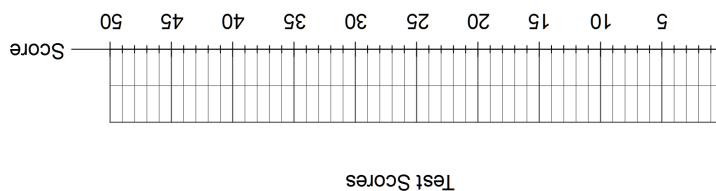
- (i) the mean.

(c) If all scores less than 20 were cropped from the set of data, state the effect (decrease, increase or stay the same) this would have on the following summary statistics.

(b) The lowest score in the dataset can be decreased by n , where n is an integer, so that the score becomes an outlier. Determine the minimum possible value of n .

(3 marks)

(b) Prove that the difference of any two odd numbers is always even.



(3 marks)

- (a) Construct a boxplot for these scores.

13, 16, 20, 21, 22, 23, 25, 27, 30, 31,
33, 33, 34, 34, 35, 35, 37, 38, 40, 41, 45

(3 marks)

State whether or not the conjecture is true. Justify your answer.

(a) A conjecture was made that all the terms of the sequence given by

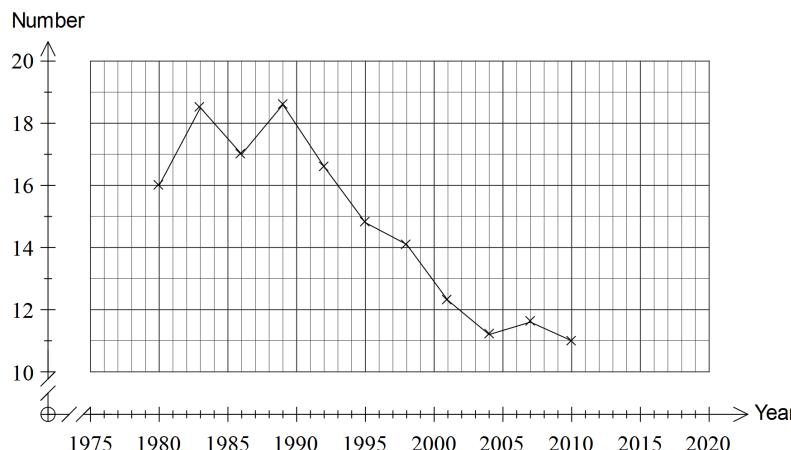
$T_n = (2n - 1)(2n + 3)$ for all positive integers n , are divisible by five.

Question 19
Question 10
CALCULATOR-ASSUMED
CALCULATOR-ASSUMED
MATHEMATICS 3AB
8 marks

(11 marks)

Question 11

The graph below shows the average number of cigarettes smoked per week by smokers aged 18 to 24 for the years 1980 to 2010.



The table below shows the same data for 1989 to 2010.

Year, x	1989	1992	1995	1998	2001	2004	2007	2010
Number, y	18.6	16.6	14.8	14.1	12.3	11.2	11.6	11

(a) For the data in the table, determine

(i) the correlation coefficient r_{xy} . (1 mark)

(ii) the least squares regression model, giving coefficients rounded to five significant figures. (2 marks)

(b) Describe how your answers in (a) would be affected if all the data shown in the graph was used rather than the cropped data in the table. (2 marks)

(8 marks)

A password is to be made by selecting five different characters from the seven characters in the set { 8, 9, X, Y, Z, \$, % }, such as Z%9X8.

(a) Determine the number of different passwords that can be made if

(i) there are no other restrictions. (1 mark)

(ii) the password must not end with a number. (2 marks)

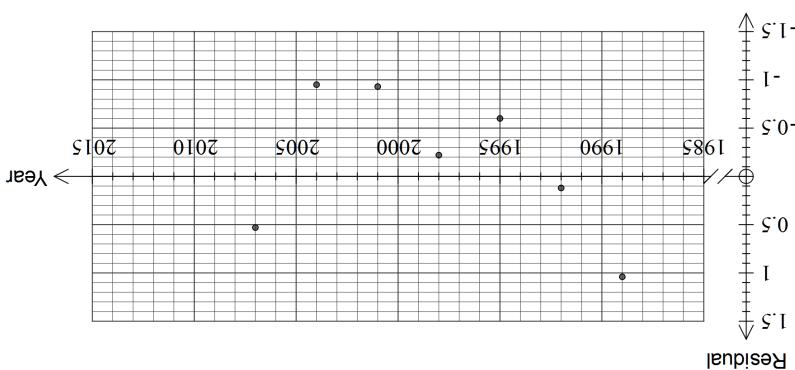
(iii) the first three characters of the password must be letters. (2 marks)

(b) Determine the probability that a randomly selected password

(i) does not end with a number. (1 mark)

(ii) has letters as the first three characters and does not end with a number. (2 marks)

(a) Calculate the residual number for 2010 using the regression model from (a) and plot this residual on the graph below. Show all your working. (3 marks)



(b) The moisture content of timber increases, so the compressive strength of the timber decreases. A particular builder will only use timber with a moisture content below 12% for structural purposes, with the rest of the timber being used for non-structural purposes. If this builder buys an assortment of 500 lengths of timber, how many of these lengths of timber will be suitable for structural purposes? (2 marks)

(c) Above what percentage of moisture content will just 5% of timber exceed? (2 marks)

(d) Use the regression model from (a) to predict the average number of cigarettes smoked per week by smokers aged 18 to 24 in the year 2015. (1 mark)

(e) Comment on the reliability of the prediction in (d). (2 marks)

(f) As the moisture content of timber increases, so the compressive strength of the timber decreases. A particular builder will only use timber with a moisture content below 12% for structural purposes, with the rest of the timber being used for non-structural purposes. If this builder buys an assortment of 500 lengths of timber, how many of these lengths of timber will be suitable for structural purposes? (2 marks)

Question 17
CALCULATOR-ASSUMED
(8 marks)

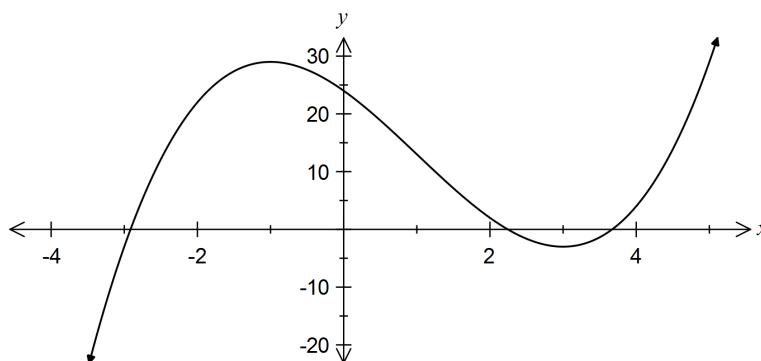
(c) Calculate the residual number for 2010 using the regression model from (a) and plot this residual on the graph below. Show all your working. (3 marks)

(d) The moisture content, as a percentage by weight, of timber sold by a company is normally distributed with a mean of 10.6% and a standard deviation of 1.2%. Give your answer rounded to three significant figures. (2 marks)

(7 marks)

Question 12

The function $y = x^3 - 3x^2 - 9x + 24$ is shown below.



- (a) Determine $\frac{dy}{dx}$ for this function. (1 mark)
- (b) Determine the equation of the tangent to the curve when $x = 2$, and draw it on the axes. (3 marks)
- (c) Use a calculus method to determine the coordinates of the turning points of the curve. (3 marks)

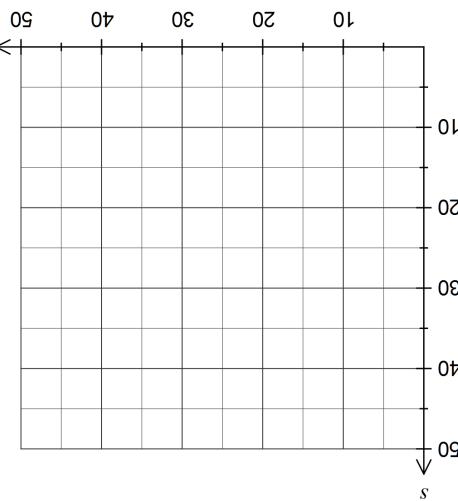
(c) Determine the residual for Monday of Week 3. (The residual is the number of parcels delivered minus the moving average, for any given day.) (2 marks)

(d) All possible residuals that can be calculated from the graphed data for Fridays are -49.63, -39.75 and -30.38. Use these values to determine the seasonal component for Friday. (1 mark)

(e) The regression model calculated from the data is $p = 4.745t + 186.9$, where p is the number of parcels delivered. Use the regression model and seasonal component to best estimate the number of parcels delivered on Friday of Week 4. (3 marks)

(3 marks)

- (d) Sketch the relationship between s and t on the axes below.



(2 marks)

- (c) Write an equation for s in terms of t .

(1 mark)

- (b) Describe the type of proportionality that exists between the two variables.

(1 mark)

- (a) Describe what happens to the value of s when t doubles.

t	100	50	40	25	10
s	2	4	5	8	10

The relationship between two variables, t and s , is shown in the table below.

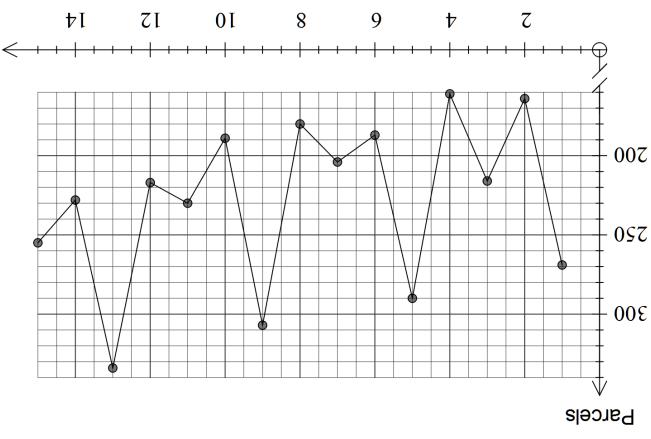
(7 marks)

- (a) What feature of the graph suggests that smoothing the data with a four-point centred moving average would be appropriate?

- (b) Calculate the four-point centred moving average for Friday of Week 2. (2 marks)

Time (i)	Week	Day	Packages delivered
4	1	Fri	
5	2	Mon	290
6	2	Tue	187
7	2	Thu	204
8	2	Fri	180
9	3	Mon	307
10	3	Tue	189
11	3	Thu	230
12	3	Fri	227
13	4	Mon	

The table below shows the data for the second and third weeks of the delivery service.



- A parcel delivery service visits a rural town every Monday, Tuesday, Thursday and Friday in the period leading up to Christmas. The number of parcels delivered on each visit are shown below.

Question 16 (9 marks)

CALCULATOR-ASSUMED

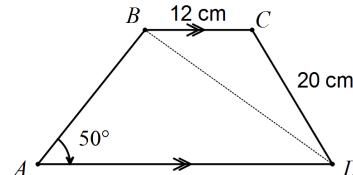
CALCULATOR-ASSUMED

MATHEMATICS 3AB

(8 marks)

Question 14

Trapezium $ABCD$ below has parallel sides AD and BC . The lengths of BC and CD are 12 cm and 20 cm respectively, the length of the diagonal BD is 26 cm and the size of angle BAD is 50° .



Determine

- (a) The size of angle
- CBD
- .

(2 marks)

- (b) The length of side
- AB
- .

(3 marks)

- (c) The area of the trapezium
- $ABCD$
- .

(3 marks)

Question 15

(9 marks)

To save money towards a deposit on a house, Anh and Bo started an investment account. They made an initial deposit of \$3 700, and then deposited an extra \$850 at the end of each month for the next year. Interest on the account was payable monthly.

The table below shows the progress of their savings for the first few months.

Month (n)	Balance of account at start of month (T_n)	Interest added at end of month	Deposit made at end of month	Balance of account at end of month (T_{n+1})
1	\$3 700.00	\$14.80	\$850.00	\$4 564.80
2	\$4 564.80	\$18.26	\$850.00	\$5 433.06
3	\$5 433.06	\$21.73	\$850.00	\$6 304.79
4	\$6 304.79	A	\$850.00	B

- (a) What was the monthly percentage interest rate?

(1 mark)

- (b) Determine the values of
- A**
- and
- B**
- in the table.

(2 marks)

- (c) Write a recursive rule to determine the balance of the account at the start of each month.
-
- (2 marks)

- (d) Determine, to the nearest dollar, the balance of the account at the start of month 13.
-
- (2 marks)

- (e) Calculate, to the nearest dollar, the total interest earned up to the start of month 13.
-
- (2 marks)