

Marks	Question	Marks	Question	Marks
17				
16				Total
15				192
14				
13				
12				
11				
10				
9				
8				
7				
6				
5				
4				
3				
2				
1				

No other items may be taken into the examination room. It is **your responsibility** to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Important note to Candidates

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination.

To be provided by the candidate Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

To be provided by the supervisor Formula sheet (referred from Section One)

Materials required/recommended for this section This Question/Answer booklet

Time allowed for this section Working time: one hundred minutes
Reading time before commencing work: ten minutes

Teacher's Name: _____
Name: _____

MATHEMATICS

UNIT Methods 1 & 2

Section Two:

Calculator-assumed

Question/Answer booklet

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	9	9	50	52	36
Section Two: Calculator-assumed	14	14	100	92	64
Total					100

Instructions to candidates

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2016*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

(3 marks)

$$x^2 + y^2 - 4x - 10y + 13 = 0.$$

- (b) Determine the centre and the radius of the circle with the equation

(a)

Find its centre and exact radius, hence state the equation of this circle.

(b)

A circle has a diameter from (2,6) to (10,9).

(5 marks)

(8 marks)

Question 10

Working time: 100 minutes.

number of the question that you are continuing to answer at the top of the page.

original answer space where the answer is continued, i.e. give the page number. Fill in the continuing an answer: if you need to use the space to continue an answer, indicate this in the planning: if you use the spare pages for planning, indicate this clearly at the top of the page.

responses and/or as additional space if required to continue an answer.
Space pages are included at the end of this booklet. They can be used for planning your provided.

This section has 14 questions. Answer all questions. Write your answers in the spaces

(92 Marks)

Section Two: Calculator-assumed

CALCULATOR – ASSUMED MATHEMATICS METHODS 1 & 2

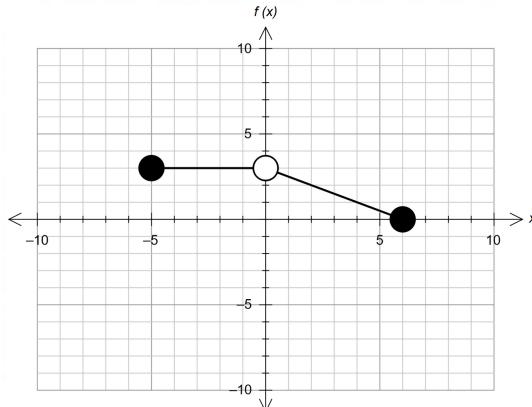
Question 11**(8 marks)**

- (a) The point Q has coordinates $(-2, 7)$ and belongs to the function $h(x)$.
Obtain the new coordinates of Q after the following transformations.

(i) $2h(-x)+3$ (2 marks)

(ii) $h\left(\frac{x}{2}\right)-1$ (2 marks)

- (b) The graph of $y = f(x)$ is drawn below.

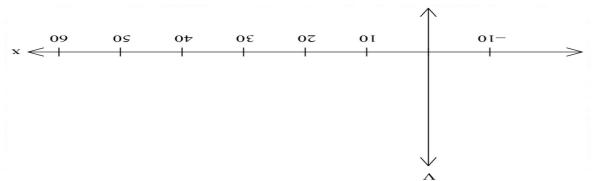


On the same axes, sketch the graphs of the following functions. Label each one clearly.

(i) $y = f(x-2) - 3$ (2 marks)

(2 marks)

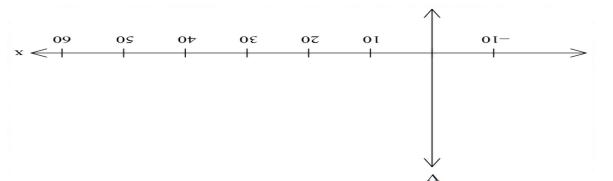
- (d) For what value(s) of x is $V = 66647$? Give your answer(s) to 1 decimal.



(2 marks)

(Do not find coordinates of turning points.)

- (c) Sketch the graph of V against x with the restriction on x .



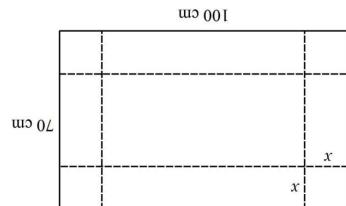
(2 marks)

(Do not find coordinates of turning points.)

- (b) Sketch the graph of V against x without any restriction on x .

(2 marks)

- (a) Find an expression for V (cm^3), the volume of the box, in terms of x .



An open box is constructed by cutting out square corners, with sides x cm, from a sheet of cardboard 100 cm by 70 cm as shown below and folding along the dotted line.

(8 marks)

Question 12

- (ii) A vertical dilation by a factor of 3 and then a horizontal reflection is applied to $f(x)$
- CALCULATOR - ASSUMED
CALCULATOR - ASSUMED
MATHEMATICS METHODS 1 & 2

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See next page

See next page

(2 marks)

throws, state the probability that the total score is 10 points.

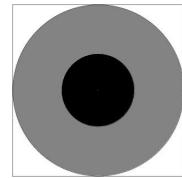
- (c) Suppose that 10 points are awarded if the dart hits the black region and zero points if the dart hits the white region. If two darts are thrown, state the probability that the total score is 10 points.

(2 marks)

(b) Calculate the probability that the dart will hit the white region.

(2 marks)

(a) Calculate the probability that the dart will hit the grey region.



The square target shown has sides of length 2 metres. Inside the square are a grey circle of radius 1 metre, and a black circle of radius 0.6 metres. Suppose that a dart thrown at the target is equally likely to hit any part of the target.

(6 marks)

Question 13

Question 14**(6 marks)**

For the purpose of choosing a team for a quiz, a class is split into three groups. Group A contains 3 boys and 2 girls. Group B contains 1 boy and 3 girls, and Group C contains 2 boys and 2 girls. An unbiased die is thrown, and if a 1, 2 or 3 appears, a person will be selected at random from Group A. If a 4 or 5 appears, a person will be selected at random from Group B. If a 6 appears, a person will be selected at random from Group C.

- (a) Find the probability that the first person is chosen from Group A. (1 mark)

- (b) Calculate the probability that a boy from Group B will be chosen when the first choice is made. (2 marks)

- (c) Calculate the probability that a boy will be chosen when the first choice is made. (3 marks)

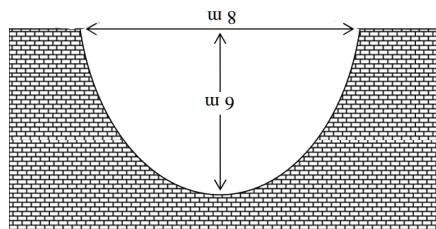
Additional working space

(c) What is the minimum clearance between the top of the truck and the arch? (1 marks)

(b) Determine showing a clear algebraic method whether a truck with a width of 6 metres and a height of 2 metres can pass through this parabolic arch. (2 marks)

(a) Given that the coordinate of the maximum height of the arch is (0, 6). Write a polynomial equation that models the arch under the bridge. (3 marks)

The width of the arch at its lowest level is 8 metres and the highest point of the arch is 6 metres from the ground.



The figure below shows the parabolic arch under a railway bridge.

Question 15

(6 marks)

(c) Find the values of p for which there are no solutions.

(d) Find the values of p for which there is 1 solution.

Additional working space

End of questions

MATHEMATICS METHODS 1 & 2 CALCULATOR - ASSUMED

MATHEMATICS METHODS 1 & 2 CALCULATOR - ASSUMED

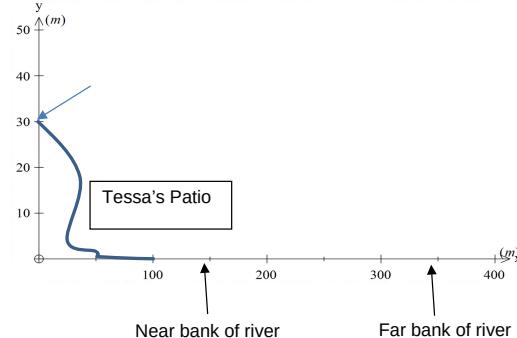
(d) Describe the transformation required on the graph of $y=f(x)$ to obtain the graph of

(i) $y=f(x+6)$.

(1 mark)

Question 16**(7 marks)**

Tessa owns an expensive riverside property that overlooks a vacant block and a river. The diagram below shows a cross-section of the location of the property.



From Tessa's patio at $(0,30)$ she has a clear view of both the near and far banks of the river with coordinates $(150,0)$ and $(350,0)$ respectively.

- (a) Find the equation of the line of sight from the patio to the Near bank of the river.
(2 marks)

- (b) A tree is planted at $(50,0)$ and grows at a rate of 1 meter per year. If this tree grows to a maximum height of 30 meters, how long before the tree obstructs the view of the Near bank?
(2 marks)

- (c) A house is built on the vacant block with the highest point at $(100,20)$. What would be the nearest point on the river that would be unobstructed by the roof?
(3 marks)

Question 22**(3 marks)**

One of the solutions to the equation $2x^3 + 21x^2 + cx - 495 = 0$ is $x=5$.

Determine the value of c and all other solutions.

Question 23**(5 marks)**

Consider the quadratic equation $2px^2 + (p-1)x + 2p = 0$.

- (a) Find the discriminant.

- (b) Find the values of p for which there are 2 solutions.

(8 marks)

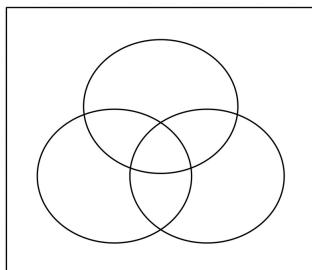
Question 17

The following teachers are involved in at least one of the following after school Maths competitions: Have Sum Fun (H), IM²C (I) or APSMO (A).

Ms Ensy, Ms Rimando, Mr Strain, Mr Gannon, Mrs Thomas, Mr McClelland, Ms Shah,

Ms Reynolds and Mr Young

Use the Venn diagram opposite to assist you in setting up your solution.



- The following information about the teachers is known:
- H \cup I = {Ms Rimando, Mrs Thomas, Ms Shah}
 - H \cap I = {Ms Reynolds, Ms Ensy} \subset H
 - {Ms Reynolds, Ms Ensy} \subset H
 - H \cup A = {Ms Rimando, Mrs Thomas, Ms Shah}
 - H \cap A = {Ms Rimando, Mrs Thomas}
 - A = {Ms Rimando, Mrs Thomas, Mr Young, Mr Strain, Mr Gannon}

Determine:

(a) I

(b) $n(H \cup I \cup A)$

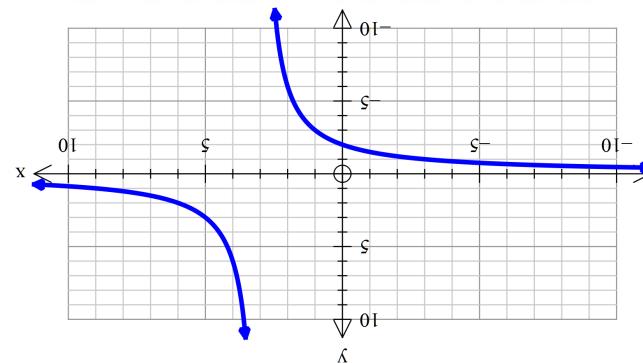
(2 marks)

(c) $n(A)$

(2 marks)

(8 marks)

The graph of the function is defined by $f(x) = \frac{x+b}{x-a}$ is shown below.

**Question 21**

(8 marks)

Question 17

The following teachers are involved in at least one of the following after school Maths competitions: Have Sum Fun (H), IM²C (I) or APSMO (A).

Ms Ensy, Ms Rimando, Mr Strain, Mr Gannon, Mrs Thomas, Mr McClelland, Ms Shah,

Ms Reynolds and Mr Young

Use the Venn diagram opposite to assist you in setting up your solution.

- Determine:

(a) I

(b) $n(H \cup I \cup A)$

(2 marks)

(c) $n(A)$

(2 marks)

(c) State the domain and range of $f(x)$.

(b) Determine the values of a and b .

(a) Determine the values of a and b .

(c) Determine the equations of the asymptotes of the graph of $y = f(2x)$.

Question 18

(6 marks)

The probabilities of two events, A and B, are such that $P(A) = 0.35$ and $P(B) = 0.4$.
Determine;

- (a) The minimum value of $P(A \cap B)$ (2 marks)

- (b) By considering your answer to Part (a), what can you say about events A and B, when $P(A \cap B)$ is a minimum.
(1 mark)

- (c) $P(A \cup B)$ (1 mark)

- (d) The maximum value of $P(A \cap B)$ (1 mark)

- (e) By considering your answer to Part (d), what can you say about the events A and B when $P(A \cap B)$ is a maximum? (1 mark)

Question 19

(8 marks)

Michael and Emma went to Mont Albert in the French Alps for a white winter Christmas. As part of their holiday celebrations, they had booked a sleigh ride for Christmas Day. However, sleigh rides can only take place when there is enough snow on the ground. Previous winter snow fall readings show that 85% of the time, there is enough snow on the ground on Christmas Day. If there is snow on the ground, there is a 95% chance that sleighing will go ahead. If there isn't enough snow on the ground, then there is an 70% that an alternate activity of a snowman building competition is organised.

- (a) Complete a tree diagram to represent this situation. (3 marks)

- (b) Calculate the probability that on Christmas Day Michael and Emma:

- (i) Go for a sleigh ride: (1 mark)

- (ii) Have no activity planned for that day: (2 marks)

- (iii) Experience enough snow on the ground, given that they have no activity planned for that day. (2 marks)

Question 20
Marks

Consider the cubic function $f(x)$ has roots at $(-4, 0)$, $(a, 0)$ and $(b, 0)$

- (a) Fully expand $(x+4)(x+a)(x+b)$ (2 marks)

- (b) State the coordinate of the y intercept, in terms of a and b (1 mark)