

Important note to candidates

You do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

No other items may be taken into the examination room. It is **your responsibility** to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room.

Special items: nil

To be provided by the candidate:

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

To be provided by the supervisor:

Materials required/recommended for this section

Formula Sheet

Working time for this section: fifty minutes

Reading time before commencing work: five minutes

Time allowed for this section

Teacher Name: _____

Student Name/Number: _____

Section One: Calculator-free

MATHEMATICS METHODS

Question/Answer Booklet

Semester 2 (Units 3 and 4) Examination, 2017

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	9	9	50	52	35
Section Two: Calculator-assumed	13	13	100	99	65
					100

Instructions to candidates

1. The rules for the conduct of School exams are detailed in the *School/College assessment policy*.
Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

Acknowledgements

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(3 marks)

- (c) For a Binomial distribution with parameters n and p , the mean is 90 and the standard deviation is 6. Determine n and p .

(2 marks)

- (b) State, with reason(s), whether $p(x) = \frac{6}{1} (4 - x)$, $x \in [0, 1, 5]$ is a discrete probability distribution.

$\Pr(G = g)$	k	$2k$	$0.5k$	$0.5k$	k
9	1	3	4	5	

(1 mark)

Find the value of the constant k .

(6 marks)

- (a) A random variable, G , has the following probability distribution.

Question 1

Suggested working time: 50 minutes.

This section has 9 (nine) questions. Answer all questions. Write your answers in the spaces provided.

Section One: Calculator-free (53 Marks) Weighting 35%

SEMESTER 2 (UNITS 3 AND 4) EXAMINATION

CALCULATOR-FREE

MATHEMATICS METHODS

3

Additional working space _____

Question number: _____

Question 2**(4 marks)**

- (a) State what you understand by a census.

(1 mark)

Each stove produced by AK Appliances is stamped with a unique serial number. AK Appliances produces stoves in batches of 2000. Before selling them, they test a random sample of 5 to see what electric current overload they will take before breaking down.

- (b) Give one reason, other than to save time and cost, why a sample is taken rather than a census.

(1 mark)

- (c) Suggest a suitable method to obtain this sample. (1 mark)

- (d) Identify the units to be sampled using this method. (1 mark)

(3 marks)

(b) If $\int f(x) dx = 1$ show that $\int f(x) dx = -1$

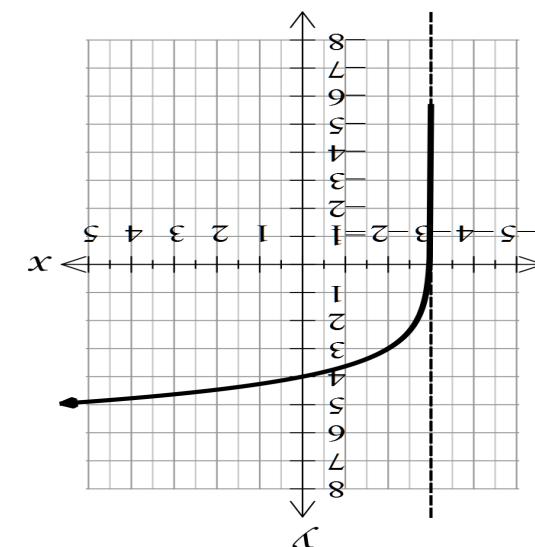
(2 marks)

(ii) $f(x) = e^{3x + \sin 2x}$

(2 marks)

(i) $f(x) = \frac{2 + \cos x}{x}$

(a) Determine the derivative $f'(x)$ given that



The graph of $y = \log_a(x+b) + c$, where a , b , and c are positive integers, is shown below:

(3 marks)

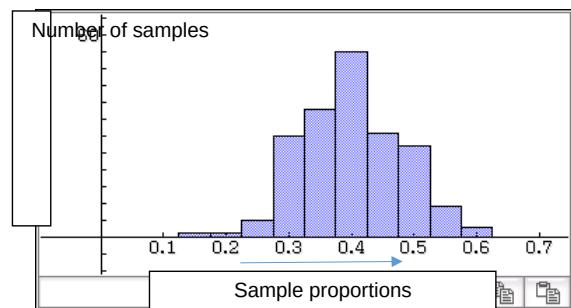
(a) Use the graph to determine the values of a , b , and c .

(b) Sketch on the same axes the graph of $y = 3 - \log_2(4 - x)$. Make sure that you show the intercepts on the two axes accurately. (4 marks)

Question 4

(5 marks)

- (a) A number of sample proportions (\hat{p}) each of the same size (50) gave rise to the graph shown below.



- (i) Approximately, how many samples were involved (1 mark)
- (ii) Estimate P , the population proportion. (2 marks)

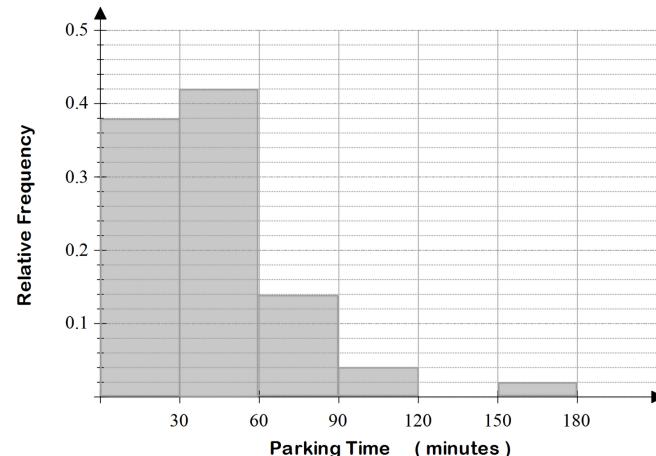
- (b) A local radio station carries out regular polls of its listeners on items of current interest. In one such poll, listeners were asked to telephone the station and just answer yes or no to the following question:

Should the AFL introduce the red card send-off rule into all games?

The poll was carried out between 8:00 am and 9:00 am one morning.

Give two problems associated with this method of sampling and suggest why each problem might cause misleading conclusions to be drawn. (2 marks)

- (c) 200 vehicles were parked in a parking lot during a 3 hour period. The recorded data is shown on the histogram drawn below.



Use this data to answer the following:

- (i) Determine the probability that a randomly selected vehicle was parked for at most 60 minutes. (1 mark)
- (ii) State the number of vehicles that were parked for between 1 and 1.5 hrs. (1 mark)
- (iii) Where might you assume that this parking lot was located? Justify your answer. (1 mark)
- (iv) As a statistician, you need to analyse and inquire about data to draw conclusions and make suggestions. Different to (c), what is a question you could ask to help understand if there is a bias in collecting this data? (1 mark)

(4 marks)

Question 5

$$\int_{-1}^1 10x^3 dx$$

Determine

- (a) Let X be a continuous random variable whose probability density function is $f(x) = \frac{1}{4}x^3$ for an interval $0 < x < c$. What is the value of the constant c that makes $f(x)$ a valid probability density function? Clearly show all working. (3 marks)

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CALCULATOR-FREE
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Question 8

SEMESTER 2 (UNITS 3 AND 4) EXAMINATION
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MATHEMATICS METHODS

Question 6

(5 marks)

- (a) Express y in terms of x given that $\log(x + 24y) - 2 = \log(x + y)$. (2 marks)

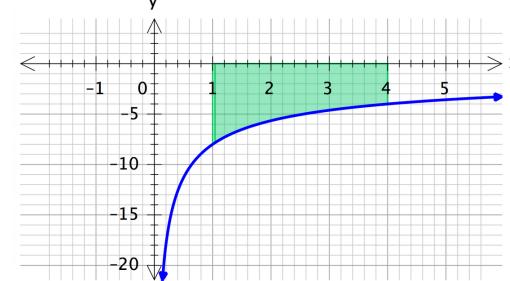
- (b) Suppose that a and b are positive real numbers.

- (i) What is sign of $\log_a b$ if $a > b$? (1 mark)

- (ii) Deduce that $a = b$ if $\log_a b = \log_b a$ (2 marks)

Question 7

The graph of the function $f(x) = \frac{-8}{\sqrt{x}}$, where $x > 0$ is shown below. The shaded region is between the graph and the x -axis from units $x = 1$ to $x = 4$.



- (a) Write down an expression for the area of the shaded region shown on the graph above. (1 mark)

- (b) Evaluate the area of the shaded region. (2 marks)

- (c) Given $\int_1^a \left(-\frac{8}{\sqrt{x}} \right) dx = -25$, where $a > 1$, determine the exact value of a . (2 marks)