QUESTION 17. (2,2,2 marks)

Jock, a keen amateur golfer, calculates the probability that he can land the ball on the green of an easy par 3 to be 0.72. Assuming that the probability remains constant, determine probability that in 30 attempts at this hole he will,

(a) Land on the green exactly 15 times.

$\binom{30}{15}(0.72)^{15}(0.28)^{15}$ ✓ $= 0.00573$ ✓ OR $X \sim b(30, 0.72)$ ✓ $P(X=15) = 0.00573$ ✓

Answer only ok

(b) Land on the green at least 15 times but not more than 25 times.

$X \sim b(30, 0.72)$

$P(15 \leq X \leq 25) = 0.9475$ ✓✓

(c) If Jock would like the probability he hits the green at least 25 times to be above 0.5, find the least number of attempts he should make.

$P(X \geq 25) > 0.5$

✓ any method

✓ answer (answer only ✓✓)

when $n = 35$

$P(X \geq 25) = 0.6137$

$n = 33$

$P(X \geq 25) = 0.3977$

$n = 34$

$P(X \geq 25) = 0.508$

∴ he should take 34 shot at the par 3 green

Rossmoyne SHS Mathematics Department

MATHEMATICS 3CD

Semester 1 2011 EXAMINATION

NAME: Solutions

TEACHER: Mr Birrell Ms Goh Mr Whyte Mr White Mr Longley Mr Jones

Section One: Calculator-free

Time allowed for this section

Reading time before commencing work: 5 minutes

Working time for this section: 50 minutes

Material required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be used in this section of the examination. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available
Section One: Calculator-free	7	7	50	40

Instructions to candidates

1. Write your answers in the spaces provided in this Question/Answer Booklet. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
   - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
   - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

2. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

3. It is recommended that you **do not use pencil** except in diagrams.

The shaded area between the curves $f(x)$ and $g(x)$ is equal to the shaded area between the curves $f(x)$ and $h(x)$.

d) Write an equation involving calculus to represent the above statement.

$$\int_0^{a+5} |g(x)-g(x)|\,dx = \int_0^5 |g(x)-h(g)|\,dx \checkmark$$

$$\int_0^{a+5} |x^3-7x^2+10x-ax(x-2)|\,dx = \int_0^5 |x^3-7x^2+10x-bx(x-5)|\,dx$$

✓ ✓

For parts e) and f) consider the case when $a=1$.

e) Find the area of the shaded region between the curves $f(x)$ and $g(x)$.

$$\int_0^6 |x^3-7x^2+10x-x(x-2)|\,dx \checkmark$$

$$= 49\tfrac{1}{3} \quad [49.\dot{3}] \checkmark$$

$$= \tfrac{148}{3}$$

ANSWER only O·K

f) Use your answers to d) and e) to determine the value of b to 3 decimal places.

$$\int_0^5 |x^3-7x^2+10x-bx^2+5bx|\,dx = \tfrac{148}{3}$$

$$\left[\tfrac{x^4}{4}-\tfrac{7x^3}{3}+5x^2-\tfrac{bx^3}{3}+\tfrac{5bx^2}{2}\right]_0^5 = \tfrac{148}{3}$$

$$\tfrac{625}{4}-\tfrac{7(125)}{3}+125-\tfrac{125b}{3}+\tfrac{125b}{2} = \tfrac{148}{3}$$

✓ WORKING

$$\tfrac{125}{6}b = 59\tfrac{3}{4}$$

$$b = 2\tfrac{217}{250}$$

$$b = 2.868 \checkmark$$

$$\left[\tfrac{126}{b}-\tfrac{125}{12} = \tfrac{148}{3}\right] \checkmark$$

$b = 2\frac{217}{250}$ ✓

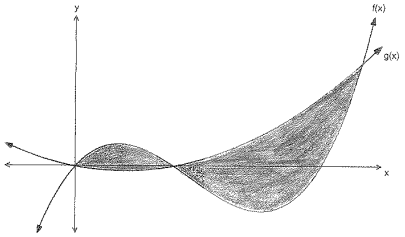
FROM CLASS PAD

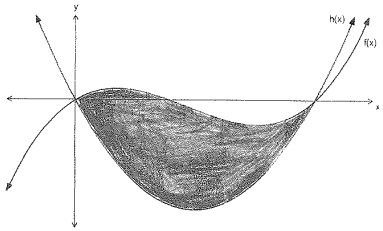
QUESTION 16. (2,2,2,3,2,2 marks)

The graphs drawn on the axes below have equations:

$$f(x) = x^3 - 7x^2 + 10x$$
$$g(x) = ax(x-c)$$
$$h(x) = bx(x-d)$$

The graphs are not drawn to scale.





a) Determine the values of c and d.

$f(x) = x^3 - 7x^2 + 10x$
$= x(x^2 - 7x + 10)$
$= x(x-5)(x-2)$ ✓

$\therefore c = 2$
$d = 5$ } ✓

b) Use your calculator to find, **in terms of** a, the largest value of x such that $f(x) = g(x)$.

$x^3 - 7x^2 + 10x = ax(x-2)$
$x = 0, x = 2, x = a+5$ ✓✓ $\therefore$ largest is $x = a+5$

c) Show how this same result can be determined algebraically.

$x(x-2)(x-5) = ax(x-2)$
$x(x-2)(x-5) - ax(x-2) = 0$ ✓
$x(x-2)(x-5-a) = 0$
$x(x-2)(x-(a+5)) = 0$ ✓
$x = 0, 2$ or $a+5$

$\therefore a+5$ is largest value where $f(x) = g(x)$

only 1 MK
- must show $a+5$ is largest
ie $x(x-2)(x-5) = ax(x-2)$
$x - 5 = a$
$x = a+5$

QUESTION	MARKS AVAILABLE	STUDENT MARK
1	8	
2	8	
3	5	
4	6	
5	4	
6	5	
7	4	
TOTAL	40	

QUESTION 1. (8 marks)

(a) Differentiate the following. You do not need to simplify your answer.

$y = x^3(2-3x)^4$

$y' = (2-3x)^4 \cdot 3x^2 + x^3 \cdot 4(2-3x)^3(-3)$ ✓ ✓

(b) Differentiate the following , leaving your answer in a factorised form.

$y = \frac{e^{-2x}}{(x^2-6)}$

$y' = \frac{(x^2-6).-2e^{-2x} - 2x.e^{-2x}}{(x^2-6)^2}$ ✓ ✓

$= \frac{-2e^{-2x}(x^2+x-6)}{(x^2-6)^2}$ ✓ $\left[\frac{-2e^{-2x}(x+3)(x-2)}{(x^2-6)^2}\right]$

(c) Hence, clearly demonstrate that the function $y = \frac{e^{-2x}}{(x^2-6)}$ has exactly two stationary points. Find the coordinates of these points giving your answers as exact values.

(NOTE: you should not attempt to find the nature of each stationary point.)

Solve $y' = 0$

$(x-2)(x+3) = 0$ ✓ as $(x^2-6)^2 \neq$ and $-2e^{-2x} \neq 0$

$x = 2$ or $x = -3$ ✓

points $\left(2, -\frac{1}{2e^4}\right)$ and $\left(-3, \frac{e^6}{3}\right)$ ✓

please except $\left(2, -\frac{e^{-4}}{2}\right)$

QUESTION 14 (5 marks)

A small spherical ball bearing has a radius of 2.5 mm . Using differentiation, find the percentage increase in the surface area , when the radius changes to 2.6 mm.

increase $= \frac{0.1}{2.5} = 4\%$ ✓

$[SA = 4\pi r^2]$

$\frac{dA}{dr} = 8\pi r$ ✓

$\frac{\delta A}{\delta r} \approx \frac{dA}{dr} \therefore \delta A = \frac{dA}{dr}.\delta r$ ✓

$\frac{\delta A}{A} = \frac{dA}{dr}.\frac{\delta r}{A}$

$= 8\pi r.\frac{\delta r}{4\pi r^2}$ ✓

$= 2 \times \frac{\delta r}{r}$

$= 2 \times 4$

$= 8\%$ ✓

OR

$SA = 4\pi r^2$

$\frac{dA}{dr} = 8\pi r$ ✓ and $\frac{dA}{dr} \approx \frac{\delta A}{\delta r}$

$\frac{\delta A}{A} = \frac{8\pi r.\delta r}{A}$ ✓

$= \frac{8\pi(2.5)(0.1)}{4\pi(6.25)}$ ✓

$= \frac{2}{25}$

$= 8\%$ ✓

QUESTION 15 (2,5,3 marks)

For the function $F(x) = 4x^3 - 6x^2 - 24x + 40$ find ;

(a) The coordinates of the x and y intercepts .

y intercept $(0,40)$ ✓ x intercepts $(-2.5, 0)$ and $(2,0)$ ✓ (both)

(b) Using calculus techniques find all stationary points and clearly demonstrate the nature of these points.

$f'(x) = 12x^2 - 12x + 24$ ✓

$f'(x) = 0$ at $x = -1$ and $x = 2$ ✓

$\therefore$ stationary points are $(-1, 54)$ and $(2, 0)$ ✓ } both

Testnator $f''(x) = 24x - 12$

$f''(-1) = -36$ ie $-VE$ ✓

$\therefore (-1, 54)$ is a local maximum

$f''(2) = 36$ ie $+VE$ ✓

$\therefore (2, 0)$ is a local minimum

(c) The coordinates of any points of inflection.

$f''(0)$

$24x - 12 = 0$ ✓

$x = \frac{1}{2}$ ✓

point of inflection $\left(\frac{1}{2}, 27\right)$ ✓

QUESTION 13 (5,1 marks)

Sachin is in training for the Hawaiian Iron Man and knows he need to put time into running (**x hours**), cycling (**y hours**) , swimming (**z hours**) and visits to the gym (**w hours**) . He has 100 hours of training time available before the actual event and hires a personal trainer to plan a schedule for him to follow. The schedule states:

- The number of hours spent in the gym must equal the hours spent running and swimming combined.
- The number of hours of cycling must be 10 more than the hours spent running and swimming combined.
- The ratio of the hours spent running to the hours spent swimming must be 2 : 3 .

(a) Write down an appropriate system of linear equations for the given information, in terms of x, y, z **and** w .

$x + y + z + w = 100$ ✓

$w = x + z$ ✓ $\Rightarrow x + z - w = 0$

$y - 10 = x + z$ ✓ $\Rightarrow x - y + z = -10$

$x : z$ as $2 : 3 \Rightarrow \frac{x}{z} = \frac{2}{3}$ ✓ $\Rightarrow 3x - 2z = 0$ ✓

$[3x = 2z]$

(b) Solve your system of equations to find the number of hours Sachin spent running, cycling, swimming and in the gym training before the event.

$x = 12$

$y = 40$ ✓

$z = 18$

$w = 30$

running = 12 hours
cycling = 40 hours
swimming = 18 hours
gym = 30 hours

QUESTION 2. (8 marks)

(a) Determine $\int (30x - 30)(x^2 - 2x + 7)dx$

$= \frac{15(x^2 - 2x + 7)^2}{2}$ ✓✓ $+ C$

-1 if no +C

(b) Evaluate $\int_0^2 4e^{2-2x}dx$

$= \left[-2e^{2-2x}\right]_0^2$ ✓

$= -2e^{-2} - (-2e^2)$ ✓

$= -2(e^{-2} - e^2)$

$= -2\left(\frac{1}{e^2} - e^2\right)$ ✓ $\left[-2\left(\frac{1 - e^4}{e^2}\right)\right]$

(c) Find A in terms of t, given that $\frac{dA}{dt} = \frac{324t}{(t^2+2)^4}$ and A =5 when $t = 1$.

Try $A = (t^2+2)^{-3}$

$A' = -6t(t^2+2)^{-4}$

$\therefore A = \frac{-54}{(t^2+2)^3} + C$ ✓ $\therefore A = \frac{-54}{(t^2+2)^3} + 7$ ✓

Find C

$5 = \frac{-54}{27} + C$

$7 = C$ ✓

QUESTION 3. (5 marks)

The probability function for a discrete random variable X is given by,

$$P(X=x)=\begin{cases}\frac{k}{x} & \text{for} \quad x=1,2,3,4,5 \\ 0 & \text{for} \quad \text{all other values of } x\end{cases}$$

(a) Complete the following probability distribution for X, giving the probabilities as fractions.
(i.e. k should be evaluated)

x	1	2	3	4	5
P(X=x)	$\frac{60}{137}$	$\frac{30}{137}$	$\frac{20}{137}$	$\frac{15}{137}$	$\frac{12}{137}$

✓

$k + \frac{k}{2} + \frac{k}{3} + \frac{k}{4} + \frac{k}{5} = 1$ ✓

$60k + 30k + 20k + 15k + 12k = 60$

$137k = 60$

$k = \frac{60}{137}$ ✓

(b) Determine the mean , or expected value of x.

$E(x) = \frac{60}{137} + \frac{60}{137} + \frac{60}{137} + \frac{60}{137} + \frac{60}{137}$ ✓

$= \frac{300}{137}$ ✓ $\left[2\frac{26}{137}\right]$

(c) If 20 of the "1 Kg " bags are selected at random , find the probability that exactly 4 of them are under the marked weight.

$X \sim b(20, 0.1151)$

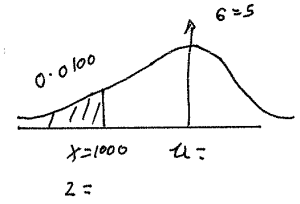
$P(X=4) = \binom{20}{4}(.1151)^4(.8849)^{16}$ ✓

$= 0.1202$ ✓

OR $X \sim b(20, 0.1151)$

$P(X=4) = 0.1202$ ✓✓

(d) The owner of the processing factory decides that no more than 1 % of the bags should be underweight . They increase the mean weight of the bags without changing the standard deviation. What should be the mean weight of seafood to ensure that no more than 1 % of bags are underweight?



$z = -2.326$ ✓

$z = \frac{x-\mu}{\sigma}$

$-2.326 = \frac{1000-\mu}{5}$ ✓

$\mu = 1000 + 5(2.326)$

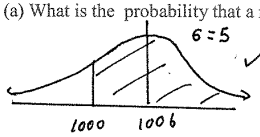
$\mu = 1011.6$ g ✓

Subtract 1 mk if probabilities in (a) and (c) not to 4 dec places and weights in (b) and (d) not to 1 dec place
TOTAL of 1 mark only

QUESTION 12. (2,2,2,3 marks)

Mixed seafood from a north west processing factory is sold in "1 Kg " bags in local supermarkets. In fact the weight of the seafood in the bags is normally distributed with a mean of 1006 g and a standard deviation of 5 g. In the following give all probabilities correct to 4 decimal places and all weights correct to the nearest 0.1 g.

(a) What is the probability that a randomly selected bag of seafood is over the marked weight?



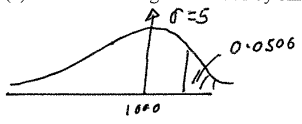
$P(X > 1000) = 0.8849$ ✓

OR $X \sim N(1006, 5^2)$ ✓

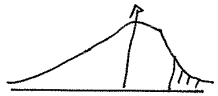
$P(X > 1000) = 0.8849$ ✓

ANSWER only O.K.

(b) What is the weight exceeded by only 5 % of the bags ?



OR



$z = 1.645$ ✓

$X \sim N(1006, 5^2)$

$P(X > K) = 0.0500$

$K = 1014.2$ g ✓✓

$1.645 = \frac{x - 1006}{5}$

$x = 1006 + 1.645(5)$

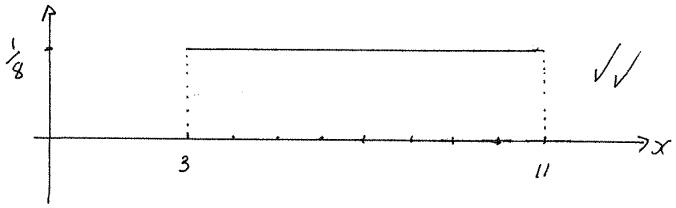
$x = 1014.2$ g ✓

ANSWER only O.K.

QUESTION 4. (6 marks)

The time, in minutes, to complete a survey is found to be between 3 and 11 minutes. If we use a uniform continuous random variable X to model the situation, the time taken to complete the survey.

(a) Show the probability density function of X graphically.



✓✓

Hence find.

(b) $P(X \leq 9) = \frac{6}{8} = \frac{3}{4}$ ✓

(c) $P(X \geq 8) = \frac{3}{8}$ ✓

(d) $P(X \leq 9 \mid X \geq 8) = \frac{1}{3}$ ✓✓

QUESTION 5. (4 marks)

Two events X and Y are such that P(X) = 0.7 and P(X ∪ Y) =0.8

(a) Calculate the P(Y) if X and Y are mutually exclusive.

$P(Y) = 0.1$ ✓

(b) Calculate the P(Y) if X and Y are independent events.

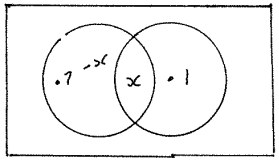
$P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$0.8 = 0.7 + y - (0.7)y$ ✓✓

$0.1 = 0.3y$

$P(y) = \frac{1}{3}$ ✓

OR



$0.8 = 0.7 + (x+0.1) - (.7)(x+0.1)$ ✓

$0.1 = x + 0.1 + 0.7x - 0.07$

$0.07 = 0.3x$

$x = \frac{7}{30}$ ✓

$\therefore P(y) = \frac{7}{30} + \frac{1}{10}$

$= \frac{10}{30}$

$= \frac{1}{3}$ ✓

(f) Given that there is an equal number from each age group, find the **probability** that Samantha and James are selected but Timothy is not.

$P(S \text{ and } J \mid \text{EQUAL NO}) = \frac{2288}{137280}$ ✓ $= \frac{1}{60}$ ✓ [0.1667]

FT from $\frac{d}{c}$

Question 11. (2,4 marks)

A cylinder, open at one end and closed at the other, has a volume of 96π cm^3. The cost of the material used for the bottom (circular) end is \$3 / cm^2 while the cost of the material used to make the curved part is \$2 / cm^2. There is no waste of material.

(a) Show that the total cost of the cylinder can be expressed as

$C = 3\pi r^2 + \frac{384\pi}{r}$

$C = 3(\pi r^2) + 2(2\pi r \cdot \frac{96}{r^2})$ ✓

$C = 3\pi r^2 + \frac{384\pi}{r}$

$V = \pi r^2 h$

$96\pi = \pi r^2 h$

$h = \frac{96}{r^2}$ ✓

If $h = \frac{96}{r^2}$ NOT shown 0/2

(b) Using calculus techniques , find the dimensions of the cylinder that will minimize the cost . (You must use a suitable method to demonstrate that your dimensions are in fact minimum.)

$C = 3\pi r^2 + \frac{384\pi}{r}$

$C' = 6\pi r - \frac{384\pi}{r^2}$ ✓

STATIONARY $C' = 0$

$\frac{384\pi}{r^2} = 6\pi r$

$64 = r^3$

$r = 4$ ✓

answer only from classpad O.K

using Sign test

$r = 3$

$C'(3) = 18\pi - \frac{384\pi}{9}$

$= -VE$

$r = 5$

$C'(5) = 30\pi - \frac{384\pi}{25}$

$= +VE$

$\therefore$ at $r = 4$ ✓ MINIMUM

$h = \frac{96}{16}$

$= 6$ ✓

$\therefore$ radius is 4 cm and height is 6 cm to minimize costs.

[$C'' = 6\pi + \frac{768\pi}{r^3}$]

[$C'' = \frac{6\pi^3 + 768\pi}{r^3}$. from CLASSPAD]

$C''(4) = +VE$

$\therefore$ min at $r = 4$ cm

QUESTION 10. (1,1,2,2,3,2 marks)

A social tennis club has 27 playing members, of whom 10 are under 30 years of age, 13 are between 30 and 50 years of age and 4 are over 50years of age. If a team of 9 members is to be selected for an inter club tournament ,

(a) Find the number of ways of selecting this 9 member team if all members are eligible for selection.

$27C9 = 4686825$

(b) Find the number of possible 9 member teams if only one person over 50 is to be selected.

$\binom{23}{8}\binom{4}{1}$ OR $[{}^{23}C_8 \times {}^{4}C_1] = 1961256$

(c) Find the number of possible 9 member teams if an equal number from each age group must be selected.

$\binom{10}{3}\binom{13}{3}\binom{4}{3}$ or $[{}^{10}C_3 \times {}^{13}C_3 \times {}^{4}C_3] = 137280$

Samantha and James are the star players and both are under 30 years of age, while Timothy is over 50 and prone to injury.

(d) How many 9 member teams contain both Samantha and James but not Timothy and still have an equal number of members from each age group .

$\binom{2}{2}\binom{8}{1}\binom{13}{3}\binom{1}{0}\binom{3}{3}$ or $[{}^{8}C_1 \times {}^{13}C_3 \times {}^{3}C_3] = 2288$

(e) Given that Timothy is not selected find the **probability** that Samantha and James are selected in a 9 member team.

$P(\text{Send } J \mid \bar{T}) \quad \frac{\binom{2}{2}\binom{24}{7}}{\binom{26}{9}\binom{1}{0}} = \frac{346104}{3124550} = \frac{36}{325}$

$[0.11077]$

$\bar{T}$ RDW 3124550

if equal from each group 0/3

QUESTION 6. (5 marks)

Solve the following system of equations

$$x+6y-2z=6 \quad -①$$
$$2x-8y+3z=-12 \quad -②$$
$$3x+2y-z=0 \quad -③$$

$2\times① - ② = 20y - 7z = 24 \quad -④$
$3\times① - ③ = 16y - 5z = 18 \quad -⑤$ ✓

$5\times④ \Rightarrow 100y - 35z = 120$
$7\times⑤ \Rightarrow 112y - 35z = 126$ ✓
$12y = 6$
$y = \frac{1}{2}$ ✓

into ④ $8 - 5z = 18$
$-5z = 10$
$z = -2$ ✓

into ① $x + 3 + 4 = 6$
$x = -1$ ✓

$\therefore \quad x = -1$
$y = 0.5$
$z = -2$

if given as $(-1, \frac{1}{2}, -2)$ OK.

QUESTION 7. (4 marks)

An on line company specializing in kitchen appliances decides to give a free cooking book with every item purchased during the month of May. The cook books are randomly selected by the computer at the time of purchase .

(a) If there are only 4 different cook books available as free gifts. Find the probability of getting a complete set (of cook books) by purchasing exactly 4 items.

$\frac{4}{4} \times \frac{3}{4} \times \frac{2}{4} \times \frac{1}{4} = \frac{3}{32}$ ✓ ✓ ✓

$\left[\frac{4!}{4^4}\right]$ ✓ ✓ ✗ $\left[\frac{3!}{4^3}\right]$ ✓ ✓

(b) If there are "p" different cook books, find the probability of getting a complete set by ordering "p" items.

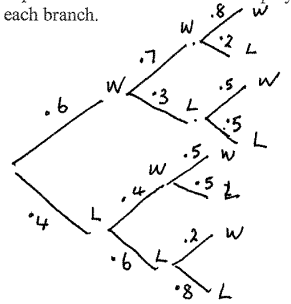
$\frac{p!}{p^p}$ ✓ ✓ or $\left[\frac{(p-1)!}{p^{p-1}}\right]$ ✓ ✓

$\left[\text{if } \frac{p \times (p-1) \times (p-2) \times (p-3) \cdot 1 \cdots}{p \times p \times p \times p \cdots p}\right]$ ✓ ✗ ✓

QUESTION 9. (3,2,2,2 marks)

The local football team the Reds are to play three matches one each week for three weeks. Based on last years results the probability that they will win the first match is 0.6. In fact every time they win a match the probability of winning the next match is increased by 0.1. Unfortunately every time they lose a match the probability of losing the next match is increased by 0.2.
(In this competition a **draw** is not possible.)

(a) Represent the three matches to be played in a tree diagram, clearly showing the probabilities on each branch.



WWW 0·336
WWL 0·084
WLW 0·090
WLL 0·090
LWW 0·080
LWL 0·080
LLW 0·048
LLL 0·192

(b) Find the probability that they win more matches than they lose.

$P(\text{win more than lose}) = P(3W) + P(2W)$
$= 0.336 + 0.084 + 0.090 + 0.080$
$= 0.59$

(c) Given they lost the first match, find the probability that they won the last match.

$P(\text{won last} \mid \text{Lost 1ST}) = \frac{0.080 + 0.048}{0.08 + 0.08 + 0.048 + 0.192} = \frac{0.128}{0.4}$ ✓ ✓
$= 0.32 \left[\frac{8}{25}\right]$

(d) Given they won exactly two matches, what is the probability that they lost the second match.

$P(\text{Lost 2ND} \mid \text{won exactly 2})$
$= \frac{0.090}{0.084 + 0.090 + 080}$ ✓ ✓
$= \frac{.090}{.254} \left[\frac{90}{254}\right]$
$= 0.3543$

QUESTION 8. (2,3 marks)

A large number of leaf eating insects are released into a controlled environment to determine the effect they have on native vegetation . The life span of these insects is relatively short and the number still alive t days after release is such that,

$$\frac{dN}{dt} = -2.773N$$

(a) If 200000 insects are released, how many would be expected to be still alive after 4 days?

$N = N_0 e^{-2.773t}$

$N = 200000\, e^{-2.773(4)}$ ✓

$N = 3.0467$

Approximately 4 ✓ insects would be expected to be alive.

if approx 3 o.k.

(b) What is the expected half life of the insects, to the nearest hour?

$\frac{1}{2} = e^{-2.773t}$ ✓ idea

$t = 0.24996$ ✓ [t = 5.999 hrs]

$t = 6$ hrs ✓

Rossmoyne SHS Mathematics Department

MATHEMATICS 3CD

Semester 1 2011 EXAMINATION

NAME: SOLUTIONS

TEACHER: Mr Birrell Ms Goh Mr Whyte Mr White Mr Longley Mr Jones

Section Two: Calculator-assumed

Time allowed for this section

Reading time before commencing work: 10 minutes
Working time for this section: 100 minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet
Formula Sheet (retained from Section One)

To be provided by the candidate

Standard items: pens, pencils, pencil sharpener, eraser, correction fluid, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators satisfying the conditions set by the Curriculum Council for this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Suggested working time (minutes)	Marks available
Section Two: Calculator-assumed	10	10	100	80

Instructions to candidates

1. The rules for the conduct of Western Australian external examinations are detailed in the *Year 12 Information Handbook 2010.* Sitting this examination implies that you agree to abide by these rules.

2. Answer the questions according to the following instructions.

   Section Two: Write answers in this Question/Answer Booklet. **All** questions should be answered.

   Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

   It is recommended that you **do not use pencil** except in diagrams.

3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.

4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
   - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
   - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

QUESTION	MARKS AVAILABLE	STUDENT MARK
8	5	
9	9	
10	11	
11	6	
12	9	
13	6	
14	5	
15	10	
16	13	
17	6	
TOTAL	80	