How to Balance Equations for Oxidation-Reduction Reactions

Oxidation-reduction (redox) reactions are reactions in which oxidation numbers change. Oxidation numbers are either real charges or formal charges which help chemists keep track of electron transfer. In practice, oxidation numbers are best viewed as a bookkeeping device.

Oxidation cannot occur without reduction. In a redox reaction the substance which is oxidized contains atoms which increase in oxidation number. Oxidation is associated with electron loss (helpful mnemonic: $LEO = \underline{Loss}$ of $\underline{Electrons}$, $\underline{Oxidation}$). Conversely, the substance which is reduced contains atoms which decrease in oxidation number during the reaction. Reduction is associated with electron gain (helpful mnemonic: $GER = \underline{Gain}$ of Electrons, Reduction).

Chemists often talk about oxidizing and reducing agents. Be careful with these terms! An oxidizing agent is a substance which oxidizes something else: it itself is reduced! Also, a reducing agent is a substance that reduces another reactant: it itself is oxidized. A disproportionation reaction is a reaction in which the same element is both oxidized and reduced.

How to Assign Oxidation Numbers: The Fundamental Rules

Rules for assigning oxidation numbers are as follows:

- The oxidation number of any *pure element* is *zero*. Thus the oxidation number of H in H₂ is zero.
- The oxidation number of a *monatomic ion* is equal to its *charge*. Thus the oxidation number of Cl in the Cl⁻ ion is -1, that for Mg in the Mg⁺² ion is +2, and that for oxygen in O²⁻ ion is -2.
- The *sum* of the oxidation numbers in a compound is *zero if neutral*, or *equal to the charge if an ion*.
- The oxidation number of alkali metals in compounds is +1, and that of alkaline earths in compounds is +2. The oxidation number of F is -1 in all its compounds.
- The oxidation number of H is +1 in most compounds. Exceptions are H_2 (where H=0) and the ionic hydrides, such as NaH (where H=-1).
- The oxidation number of oxygen (O) is -2 in most compounds. Exceptions are O_2 (where O = 0) and peroxides, such as H_2O_2 or Na_2O_2 , where O = -1.
- For other elements, you can usually use rule (3) to solve for the unknown oxidation number.

Examples:

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\overline{NO(g)} has O = -2, so N = +2.

NO_2(g) has O = -2, so N = +4.

SO_4^{2-} has O = -2. Thus S + 4(-2) = -2. Solving the equation gives S = -2 + 8 = +6.

K_2Cr_2O_7 has K = +1 and O = -2. Thus 2(+1) + 2 Cr +7(-2) = 0; 2 Cr = 12; Cr = +6.
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How to Balance Redox Reactions Using the Method of Half-Reactions

Oxidation-reduction reactions are often tricky to balance without using a systematic method. We shall use the method of half-reactions which is outlined in detail below.

Method in Acidic (or Neutral) Solution

Suppose you are asked to balance the equation below:

$$NO_2^- + MnO_4^- \rightarrow NO_3^- + Mn^{+2}$$
 (in acid solution)

Begin by writing the *unbalanced* oxidation and reduction *half-reactions* (you do not need to know which is which):

$$NO_{2}^{-} \rightarrow NO_{3}^{-}$$

$$MnO_4^- \rightarrow Mn^{+2}$$

Next, *balance for atoms*. First do this for atoms *other than* O and H. (Both equations above are already balanced for N and Mn, so no change is needed in this example.) Then balance for O atoms by adding H₂O to the reaction side deficient in O:

$$H_2O$$
 + $NO_2^- \rightarrow NO_3^-$
 $MnO_4^- \rightarrow Mn^{+2}$ + $4 H_2O$

This leaves H atoms unbalanced. In *acidic* (or neutral) solution, balance for H atoms by adding H+ to the side deficient in H:

$$H_2O + NO_2^- \rightarrow NO_3^- + 2H^+ 8H^+ + MnO_4^- \rightarrow Mn^{+2} + 4H_2O$$

The next step is to *balance for charge*. To do this, add electrons (e⁻) to the more positive side:

$$H_2O + NO_2^- \rightarrow NO_3^- + 2 H^+ + 2 e^-$$

 $5 e^- + 8 H^+ + MnO_4^- \rightarrow Mn^{+2} + 4 H_2O$

Now you need to *multiply the equations by appropriate factors* so that the number of electrons lost in the oxidation half-reaction (LEO) is equal to the number of electrons gained in the reduction half-reaction (GER):

$$5 x [$$
 $H_2O + NO_2^- \rightarrow NO_3^- + 2 H^+ + 2 e^-]$ $2 x [$ $5 e^- + 8 H^+ + MnO_4^- \rightarrow Mn^{+2} + 4 H_2O]$

Then, sum the above equations to obtain

$$5 H_2 O + 5 N O_2^- + \ 10 \ e^- \ + \ 16 H^+ \ + \ 2 M n O_4^- \ \rightarrow \ 5 N O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + \ 10 \ e^- \ + \ 2 M n^{+2} \ + \ 8 H_2 O_3^- + 10 H^+ \ + \ 10 \ e^- \ + \ 10 H^+ \ + \ 10 \ e^- \ + \ 10 H^+ \ + \ 10 H^$$

Finally, *simplify* by subtracting out species that are identical on both sides. Our final balanced redox equation is

$$5 \text{ NO}_{2}^{-} + 6 \text{ H}^{+} + 2 \text{ MnO}_{4}^{-} \rightarrow 5 \text{ NO}_{3}^{-} + 2 \text{ Mn}^{+2} + 3 \text{ H}_{2}\text{O}$$

Check this equation to confirm that it is balanced for atoms and balanced for charge.

Method in Basic Solution

Suppose you are asked to balance the equation below:

$$I^- + MnO_4^- \rightarrow I_2 + MnO_2$$
 (in basic solution)

Begin by writing the *unbalanced* oxidation and reduction *half-reactions* (you do not need to know which is which):

$$\begin{array}{ccc} I^{\text{-}} & \to & I_2 \\ MnO_4^{\text{-}} & \to & MnO_2 \end{array}$$

Next, balance for atoms. First do this for atoms other than O and H:

$$\begin{array}{ccc} 2 \ I^{\text{-}} & \rightarrow & I_2 \\ MnO_4^{\text{-}} & \rightarrow & MnO_2 \end{array}$$

Then balance for O atoms by adding H₂O to the reaction side deficient in O:

$$\begin{array}{cccc} 2 \ I^{\text{-}} & \rightarrow & I_2 \\ MnO_4^{\text{-}} & \rightarrow & MnO_2 & + & 2 \ \textit{H}_2\textit{O} \end{array}$$

This leaves H atoms unbalanced. In *basic solution* (just as in acidic or neutral solution) first balance for H atoms by adding H⁺ to the side deficient in H:

$$4 H^+ + \text{MnO}_4^- \rightarrow \text{MnO}_2 + 2 \text{H}_2\text{O}$$

In basic solution, follow this step by <u>neutralizing the H+</u>; do this by adding an equivalent amount of OH- to both sides of the equation.

$$4 OH^{-} + 4 H^{+} + MnO_{4}^{-} \rightarrow MnO_{2} + 2 H_{2}O + 4 OH^{-}$$

Then form water on the side which has both H⁺ and OH⁻ (recall that H⁺ + OH⁻ \rightarrow H₂O): in this case we form 4 H₂O on the left:

$$4 H_2O + MnO_4^- \rightarrow MnO_2 + 2 H_2O + 4 OH^-$$

Next simplify the water by subtracting 2 H₂0 from both sides. The half-reactions are now:

$$2 \text{ I}^{-} \rightarrow \text{I}_{2}$$

 $2 H_{2}O + \text{MnO}_{4}^{-} \rightarrow \text{MnO}_{2} + 4 \text{ OH}^{-}$

At this point the equations should be balanced for atoms. The next step is to *balance for charge*. To do this, add electrons (e⁻) to the more positive side:

$$2 I^{-} \rightarrow I_2 + 2 e^{-}$$

 $3 e^{-} + 2 H_2 O + MnO_4^{-} \rightarrow MnO_2 + 4 OH^{-}$

Now you need to *multiply the equations by appropriate factors* so that the number of electrons lost in the oxidation half-reaction (LEO) is equal to the number of electrons gained in the reduction half-reaction (GER):

$$3 x [$$
 $2 I^{-} \rightarrow I_{2} + 2 e^{-}]$
 $2 x [3 e^{-} + 2 H_{2}O + MnO_{4}^{-} \rightarrow MnO_{2} + 4 OH^{-}]$

Sum the equations to obtain

$$6 I^{-} + 6 e^{-} + 4 H_{2}O + 2 MnO_{4}^{-} \rightarrow 3 I_{2} + 6 e^{-} + 2 MnO_{2} + 8 OH^{-}$$

Finally, *simplify* by subtracting out species that are identical on both sides:

$$6 I^{-} + 4 H_{2}O + 2 MnO_{4}^{-} \rightarrow 3 I_{2} + 2 MnO_{2} + 8 OH^{-}$$

Check our final equation above to confirm that it is balanced for atoms and balanced for charge.

Exercises:

Balance the following redox reactions. In each case

- (a) give the balanced half-reactions; identify the oxidation half-reaction and the reduction half-reaction.
- (b) give the balanced net reaction.
- (c) identify the oxidizing agent and the reducing agent.

1. $Cl_2(g) + S_2O_3^{2-}(aq) \rightarrow Cl^{-}(aq) + SO_4^{2-}(aq)$ in acid solution.

Answers:

(a) $S_2O_3^{2-}(aq) + 5 H_2O \rightarrow 2 SO_4^{2-}(aq) + 10 H^+(aq) + 8 e^-$ (oxidation half-reaction – LEO); $Cl_2(g) + 2 e^- \rightarrow 2 Cl^-(aq)$ (reduction half-reaction – GER). (b) $S_2O_3^{2-}(aq) + 5 H_2O + 4 Cl_2(g) \rightarrow 2 SO_4^{2-}(aq) + 10 H^+(aq) + 8 Cl^-(aq)$ (c) $S_2O_3^{2-}(aq)$ is the reducing agent; $Cl_2(g)$ is the oxidizing agent.

2. $O_3(g) + Br^-(aq) \rightarrow O_2(g) + BrO^-(aq)$ in basic solution.

Answers:

(a) Br $^-$ (aq) + H₂0 + 2 OH $^-$ (aq) \rightarrow BrO $^-$ (aq) + 2H₂O + 2 e $^-$ or, after simplifying, Br $^-$ (aq) + 2 OH $^-$ (aq) \rightarrow BrO $^-$ (aq) + H₂O + 2 e $^-$ (oxidation half-reaction – LEO); O₃(g) + 2 H₂O + 2 e $^-\rightarrow$ O₂(g) + H₂O + 2 OH $^-$ (aq) or, after simplifying, O₃(g) + H₂O + 2 e $^-\rightarrow$ O₂(g) + 2 OH $^-$ (aq) (reduction half-reaction – GER). (b) Br $^-$ (aq) + O₃(g) \rightarrow BrO $^-$ (aq) + O₂(g) (c) Br $^-$ (aq) is the reducing agent; O₃(g) is the oxidizing agent.

3. Balance the reaction, $Br_2(l) \rightarrow Br^-(aq) + BrO_3^-(aq)$ in basic solution. *Hint*: this is a *disproportionation reaction*!

Answer: $6 \text{ Br}_2(l) + 12 \text{ OH}^-(\text{aq}) \rightarrow 10 \text{ Br}^-(\text{aq}) + 2 \text{ BrO}_3^-(\text{aq}) + 6 \text{ H}_2\text{O}$