PEXCEPTIONAL SCHOOL Exceptional students.

INDEPENDENT PUBLIC SCHOOL

WAEP Semester One Examination, 2020

Question/Answer booklet

L		uoitae
_		Your name
_		ln words
		ln figures
	If required by your examination administrator, please place your student identification label in this box	

METHODS

UNIT 3
Section Two:
Calculator-assumed

Number of additional answer booklets used (if applicable):	ten minutes one hundred minutes	Time allowed for this section Reading time before commencing work: Working time:
	əu	Your nan

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet

This Question/Answer booklet Formula sheet (retained from Section One)

:YA student number:

SOITAMENTICS

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators, which can include scientific, graphic and

Computer Algebra System (CAS) calculators, are permitted in this ATAR

course examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

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METHODS UNIT 3 2 CALCULATOR-ASSUMED

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	8	8	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
				Total	100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this
 examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet preferably using a blue/black pen.
 Do not use erasable or gel pens.
- 3. You must be careful to confine your answers to the specific question asked and to follow any instructions that are specific to a particular question.
- 4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 5. It is recommended that you do not use pencil, except in diagrams.
- Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

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CALCULATOR-ASSUMED	40	METHODS UNIT 3
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Supplementary page

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Question number:

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CALCULATOR-ASSUMED 3 METHODS UNIT 3 Section Two: Calculator-assumed 65% (98 Marks)

This section has thirteen questions. Answer all questions. Write your answers in the spaces

Working time: 100 minutes.

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Question 9 (6 marks)

A seatood processor buys batches of n prawns from their supplier, where n is a constant. In any given batch, the probability that a prawn is export quality is p, where p is a constant and the quality of an individual prawn is independent of other prawns.

The discrete random variable X is the number of export quality prawns in a batch and the mean of X is 79.2 and standard deviation of X is 6.6.

State the name given to the distribution of X and determine its parameters n and p. (4 marks)

(b) Determine the probability that more than 50% of prawns in a randomly selected batch are export quality.

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METHODS UNIT 3 18 CALCULATOR-ASSUMED

Question 21

(8 marks)

(9 page 419)

When a byte of data is sent through a network in binary form (a sequence of bits - 0's and 1's), there is a chance of bit errors that corrupt the byte, i.e. a 0 becomes a 1 and vice versa.

Suppose a byte consists of a sequence of 8 bits and for a particular network, the chance of a bit error is 0.300%.

(a) Determine the probability that a byte is transmitted without corruption, rounding your answer to 5 decimal places.

 b) Determine the probability that during the transmission of 32 bytes, at least one of the bytes becomes corrupted.

A Hamming code converts a byte of 8 bits into a byte of 12 bits for transmission, with the advantage that if just one bit error occurs during transmission, it can be detected and corrected.

Determine the probability that during the transmission of 32 bytes using Hamming codes, at least one of the bytes becomes permanently corrupted. (3 marks)

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METHODS UNIT 3

CALCULATOR-ASSUMED

Question 10

(8 marks)

The voltage, V volts, supplied by a battery t hours after timing began is given by

$$V = 8.95e^{-0.265t}$$

- Determine
 - the initial voltage.

(1 mark)

the voltage after 3 hours.

(1 mark)

the time taken for the voltage to reach 0.03 volts.

(1 mark)

(b) Show that $\frac{dV}{dt} = aV$ and state the value of the constant a.

(2 marks)

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Determine the rate of change of voltage 3 hours after timing began.

(1 mark)

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Determine the time at which the voltage is decreasing at 5% of its initial rate of decrease. (2 marks)

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CALCULATOR-ASSUMED

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METHODS UNIT 3

Question 20

(6 marks)

Given that f(2) = -3, f'(2) = 4, g(2) = 2 and g'(2) = 5, evaluate h'(2) in each of the following

(a) $h(x) = f(x) \cdot g(x).$

(2 marks)

 $h(x) = (g(x))^4.$

(2 marks)

h(x) = f(g(x)).

(2 marks)

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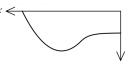
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METHODS UNIT 3

AGuestion 19

The edges of a swimming pool design, when viewed

The edges of a swimming pool design, when viewed



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from above, are the *x*-axis, the *y*-axis and the curves $y=-0.2x^2+3x-6.25 \text{ and } y=2.75+e^{x-5}$

where x and y are measured in metres.

a) Determine the gradient of the curve at the point where the two curves meet. (2 marks)

Determine the surface area of the swimming pool. (4 marks)

Given that the water in the pool has a uniform depth of 135 cm, determine the capacity of the pool in kilolitres (1 kilolitres of water occupies a volume of 1 m³). (1 mark)

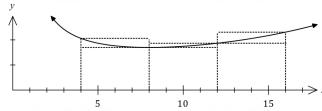
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(4 marks)

Question 12 (7 marks)

The function f is defined as $f(x) = \frac{5e^{0.125x}}{x}$, x > 0, and the graph of y = f(x) is shown below.



(a) Complete the missing values in the table below, rounding to 2 decimal places. (1 mark

х	4	8	12	16
f(x)		1.70	1.87	

(b) Use the areas of the rectangles shown on the graph to determine an under- and overestimate for $\int_4^{16} f(x) dx$. (3 marks)

- (c) Use your answers to part (b) to obtain an estimate for $\int_{-1}^{16} f(x) dx$. (1 mark)
- (d) State whether your estimate in part (c) is too large or too small and suggest a modification to the numerical method employed to obtain a more accurate estimate. (2 marks)

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(b) Use calculus to determine the coordinates of *P* that minimise *A*.

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CALCULATOR-ASSUMED 7 METHODS UNIT 3

Question 13

A bag contains four similar balls, one coloured red and three coloured green. A game consists of selecting two balls at random, one after the other and with the first replaced before the second is drawn. The random variable X is the number of red balls selected in one game.

(3 marks) Complete the probability distribution for X below.



(b) Determine E(X) and Var(X).

A player wins a game if the two balls selected have the same colour. Determine the
probability that a player wins no more than three times when they play five games.
 (3 marks)

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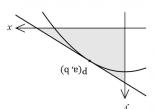
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METHODS UNIT 3 14 CALCULATOR-ASSUMED Question 18 (8 marks)

Let P(a,b) be a point in the first quadrant that lies on the curve $y=8-x^2$ and A be the area of the triangle formed by the tangent to the curve at P and the coordinate axes.



Show that $A = \frac{(a^2 + 8)^2}{4a}$.

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METHODS UNIT 3

Question 14

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CALCULATOR-ASSUMED

(8 marks)

A curve has equation $y = (x - 3)e^{2x}$.

 (a) Show that the curve has only one stationary point and use an algebraic method to determine its nature.
 (3 marks)

(b) Justify that the curve has a point of inflection when x = 2.

(3 marks)

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CALCULATOR-ASSUMED

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METHODS UNIT 3

Question 17

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(6 marks)

Some values of the polynomial function f are shown in the table below:

х	-2	-1	0	1	2	3	4
f(x)	-8	0	5	6	4	1	-3

(a) Evaluate $\int_{1}^{4} f'(x) dx$.

(2 marks)

The following is also known about f'(x):

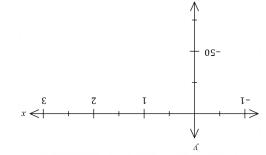
Interval	$-2 \le x \le 1$	x = 1	$1 \le x \le 4$
f'(x)	f'(x) > 0	f'(x)=0	f'(x) < 0

(b) Determine the area between the curve y = f'(x) and the x-axis, bounded by x = -2 and x = 3. (4 marks)

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CALCULATOR-ASSUMED 9 METHODS UNIT 3 (C) Sketch the curve on the axes below. (2 marks)



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METHODS UNIT 3 12 CALCULATOR-ASSUMED

Question 16 Question 16 When a machine is serviced, between 1 and 5 of its parts are replaced. Records indicate that 7%

of machines need 1 part replaced, 8% need 5 parts replaced, 12% need 4 parts replaced, and the mean number of parts replaced per service is 2.82.

Let the random variable χ be the number of parts that need replacing when a randomly selected machine is serviced.

Complete the probability distribution table for X below.

(4 marks)

					(x = X)d
ς	₽	ξ	7	T	χ

Determine Var(X).

The cost of servicing a machine is \$56 plus \$12.50 per part replaced and the random variable Y is the cost of servicing a randomly selected machine.

(c) Determine the mean and standard deviation of Y.

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(3 marks)

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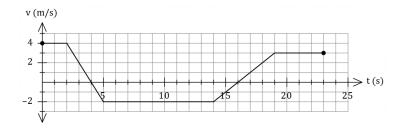
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CALCULATOR-ASSUMED

Question 15

(9 marks)

A small body leaves point A and travels in a straight line for 23 seconds until it reaches point B. The velocity v m/s of the body is shown in the graph below for $0 \le t \le 23$ seconds.



(a) Use the graph to evaluate $\int_0^4 v \, dt$ and interpret your answer with reference to the motion of the small body. (3 marks)

(b) Determine an expression, in terms of t, for the displacement of the body relative to A during the interval $2 \le t \le 5$. (3 marks)

CALCULATOR-ASSUMED

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METHODS UNIT 3

(c) Determine the time(s) at which the body was at point A for $0 < t \le 23$.

(3 marks)

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