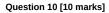
(c) Find the number of ways to feed \$10 and \$20 notes into the machine to pay \$130. Explain why the number of ways follows the pattern.

377	233	744	68	99	34	7.7	13	Number of ways to pay
\$130	\$150	011\$	00T\$	06\$	08\$	02\$	09\$	JnuomA

so the sequence 1, 2, 3, 5, 8 can be used to calculate the number of ways	
\$130 is in the pattern (+10) for the amounts \$	τ
The number of ways is 377 ×	τ
Description	2 marks

MARKING KEY 2CMATI2DMAT

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(a) (i) Four ways in which Frank can pay an account of \$40 are listed below:

\$10, \$10, \$10, \$10

\$10, \$10, \$20

\$10, \$20, \$10 \$20, \$10, \$10

Find another way.

1 mark	Description
1	\$20 \$20 🗸

(ii) Are there more than 5 ways in which Frank can feed the notes to pay \$40? Explain.

1 mark	Description
1	No, all combinations of only \$10 notes, both \$10 and \$20, only \$20 have been listed in a systematic way ✓

(b) (i) Consider other amounts that Frank could pay and complete the table below.

Amount to pay	\$10	\$20	\$30	\$40	\$50	\$60	\$70
Number of							
ways to feed	1	2	3	5	8	13	21
into machine							

A systematic way to approach this is to start with number of ways for \$10 and build up by \$10 amounts by adding a \$10 note to each of the previous examples and adding \$20 to the examples two steps back.

\$10 10	\$20 10 10 20	(add 10 (1 with	0 to previous 10) 20)	\$30 10 10 20 1 0		(add	d 10 to \$20 examples)
				10 20		(add	d 20 to \$10 example)
	\$40			\$50			
	10 10 1	0 10	(add 10 to \$30 examples)	10 10	10 10	10	(add 10 to \$40 examples)
	20 10 1	0		20 10	10 10)	
	10 20 1	0		10 20	10 10)	
				10 10	20 10)	
	10 10 2	0	(add 20 to \$20 examples)	20 20	10		
	20 20						
				10 10	10 20)	(add 20 to \$30 examples)
	20 10 2	0					,
				10 20	20		

2 marks	Description
2	Number of ways 1 2 3 ✓ 5 8 13 21 ✓

(ii) Describe the pattern in the number of ways to feed the notes into the machine.

1 mark	Description
1	To get the next term you add the previous two terms ✓

(iii) How do you know the pattern will continue?

	3 mark	Description
Γ	1	The amounts are going up by \$10 ✓
		and
	1	The ways are obtained by adding \$10 to each of the ways in the previous step ✓
	1	and adding \$20 to the examples two steps back ✓
		(in the absence of the above, one mark for stating the pattern is a Fibonacci sequence)



RESOURCE-FREE EXAMINATION

Simplify: 4b - 2[3b - (b+7)]Question 1 [9 marks]

/ tT =	τ
$\Rightarrow \forall b - 2 (2b - 7) \checkmark$	τ
$\forall b - 2 [3b - (b+7)]$	
Descubriou	z warks

(b) Solve the following equation algebraically, showing working: (2a - 4)(a + 1) = 0.

That is, $a = 2$ or $a = -1$ (numbers) \checkmark ('or' in the expression) \checkmark	T'T
So either $(2a-4)=0$ or $(a+1)=0$	τ
If a product is equal to zero, at least one of the terms must be zero.	
0 = (L + n)(h - nS)	
Describtion	3 marks

(c) Show that 3k(3k-1) = 4(4-k) + k is equivalent to $9k^2 - 16 = 0$.

$\partial Y_5 - 10 = 0$	τ
Adding 3k to each side gives the required result:	
That is, $9k^2 - 3k = 16 - 3k$	
Expanding each side gives: $9k^2 - 3k = 16 - 4k + k$	τ
3k(3k-1) = 4(4-k) + k	
Description	2 marks

(d) Use factorisation to solve $9k^2 - 16 = 0$.

That is, $k = 4/3$ or $k = -4/3$ \checkmark (do not penalise for lack of 'or' here)	Į
So either $(3k - 4) = 0$ or $(3k + 4) = 0$.	
If a product is equal to zero, at least one of the terms must be zero	
$(3k - 4)(3k + 4) = 0. \checkmark$	τ
$\partial \mathcal{V}_{5} - \mathcal{I} \mathbf{P} = 0$	
Description	2 marks

Describe a graphical method of solving the equation $5-x^2=2x+1$. Provide a sketch as part of your Question 2 [6 marks]

Read off the x coordinates \(\sigma\) of the points of intersection \(\sigma\)	τ'τ
Description: Graph $f(x) = -x^2 + 9$ and $g(x) = 2x + 1$ on the same axes	11
y intercept 1, x intercept − 0.5 ✓	τ
straight line with positive gradient and positive y intercept 🗸	τ
y intercept 9, x intercepts -3 and 3 V	τ
parabola shape, symmetrical about the y axis, inverted 🗸	-
Sketch showing $f(x) = -x^2 + 9$ and $g(x) = 2x + 1$ on the same axes	ı
Description	6 marks

re then released back into the river. Estimate the nonulation of bream in the river at this time.	θW
e year later, environmental officers netted 56 bream from the river, of which 7 had tags. The fish	(a) On
3 [2 warks]	Question

Mathematics 2C/2D: Sample Examination Marking Key

were then released back into the river. Estimate the population of bream in the river at this time.	
One year later, environmental officers netted 56 bream from the river, of which 7 had tags. The fish	(y)
enou e [e uuake]	anλ

H	7 ÷ 20 = 800 ÷ b √ Descubtion	3 warks
		Ţ
	Arr 6400 $ Arr$	τ

Mathematics 2C/2D: Sample Examination Marking Key

Line C is the only line that fits both criteria.

a minimum number of 1500 weeds

(valid reasoning shown on the graph --4 marks)

or $N(t) = 2t^3 - 75t^2 + 600t + 3500$ and N(t) = 4200

4500 = 543 - 75t2 + 600t + 3500 V

The number of weeds = 4200 when

4875 in the first 5 days

of days since the poisoning occurred.

Correct equation is C V

Score for History is 80 🗸

e.g. The line of best fit would have positive gradient V

OΤ

з шяқк

Ţ WSIK

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з шяқкг

τ

τ

τ

τ

4 marks

Question 9 [6 marks]

× 8.50 = 8 + (20) 9.0 = H	τ
Description	2 marks
ıraphy test during the lunch-hour the next day, and her History mark was estimated from Iraphy mark. Ashley's mark for Geography is 62.Use your answer for (c) to determine the Ashley was given for History.	ე ეიჟე

k Ashlev was given for History.	nem
ցraphy mark. Ashley's mark for Geography is 62.Use your answer for (c) to determine the	იმე
graphy test during the lunch-hour the next day, and her History mark was estimated from her	იმე
IEY WAS SICK ON THE GRY THE GEOGRAPHY AND MISTORY TESTS WERE HEID. SHE SAL THE	usw (

•	Motoria gives to Horizon
)	Geography mark. Ashley's mark for Geography is 62.Use your answer for (c) to determine the
)	Geography test during the lunch-hour the next day, and her History mark was estimated from her
/ (ɔ)	ASNICY was sick on the day that the Geography and History tests were held. She sat the

Therefore, if the line was extended further the y - intercept would be well below 40. \checkmark The y-intercept would be around 40 on the graph provided but there is a break in scale.

Description

the following could be the equation of the line that best fits the scattergraph? Explain your answer. (b) If G represents the Geography mark and H the corresponding History mark of a student, which of

Description

successful ✓ (any valid summary observation and a conclusion that is consistent with it)

• the number of weeds increased after the 20th day so eventually may have exceeded

after 5 days the number of weeds started to decrease until the 20th day when there was

initially process appeared unsuccessful with number of weeds increasing from 3500 to Description

the above time period. This report should refer to the number of weeds recorded and the number Write a short descriptive report on the success (or otherwise) of the weed-killing process during

Therefore, there were 8 days in which the number of weeds recorded exceeded 4200 V

Description

so days when the recording exceeded 4200 were day 2 to day 9 inclusive >

(b) For how many of the 25 days was the recording more than 4 200 weeds? Show reasoning.

solving this gives $t \approx 1.4$, 9.3 and not again in [0, 25] \checkmark (1.4 and 9.3 sufficient)

1500 was fewer than the original number of weeds, so the poisoning could be judged the original number 🗸 🗸 (2 valid statements describing the weed killing)

(a) John's score was the second highest in the Geography test. What score did he get in History?

Therefore, Ashley should receive a mark of 64 (or 63.8) ✓	τ
▶ 8.E3 = 8 + (S3) 9.0 = H	τ
Description	2 marks

(b) What, if any, assumptions did you make in your answer to (a)?

2 marks	Description
	Assumed:
1	All 800 of restocked fish still in river ✓
1	Restocked fish thoroughly mixed with existing bream (or similar) ✓

Question 4 [5 marks]

(a) Find the gradient of the line passing through A and B.

2 marks	Description
1,1	gradient = $-\frac{10}{6}$ \checkmark (fraction) \checkmark (negative sign) = $-\frac{5}{3}$

(b) Determine the equation of the line that is perpendicular to the side AB and that passes through the point C.

3 marks	Description	
1	Perpendicular gradient to AB is $\frac{3}{5}$ \checkmark	
	Required line is $y - (-1) = \frac{3}{5} \times (x - (-3))$	
1	Which simplifies to $y = \frac{3}{5}x + \frac{4}{5}$	

Question 5 [8 marks]

- (a) For each of the following conjectures, state whether it is true or false. If it is true, give three examples of when it is true. If it is false, give one example of when it is false. The set of counting numbers is {1, 2, 3, 4, ...}.
 - (i) If n is an odd counting number greater than 1, then $n^2 1$ is a multiple of 8.

2 marks	Description
1	Three trials with correctly simplified answers ✓
	When $n = 1$, $n^2 - 1 = 1 - 1 = 0$
	$n=3, n^2-1=9-1=8$
	$n=5$, $n^2-1=25-1=24$ which are multiples of 8
1	It appears this conjecture will hold true ✓

(ii) The product of two consecutive counting numbers is a multiple of 4.

2 marks	Description				
1	One trial ✓				
	$1 \times 2 = 2$	(False)			
	or 2 × 3 = 6	(False)			
	or $5 \times 6 = 30$	(False)			
1	This conjecture is false ✓				

(b) Justify the claim that the sum of three consecutive numbers is always a multiple of 3.

	· · · · · · · · · · · · · · · · · · ·		
4 marks	Description		
1	Let the first number be <i>x</i> ✓		
1	The next consecutive numbers would be $x + 1$ and $x + 2$		
1	Sum = $x + (x + 1) + (x + 2)$		
	= 3x + 3		
1	$=3(x+1)$ which is a multiple of 3 \checkmark		

Question 7 [8 marks]

(a) Find the distance BD.

2 marks	Description		
	$BD^2 = 27.4^2 + 31.5^2 - 2(27.4)(31.5)\cos(85^\circ)$ \checkmark (mark for stating the cosine rule with correct		
1	substitutions)		
1	BD = 39.9m ✓		

(b) Find the area of triangle ABD.

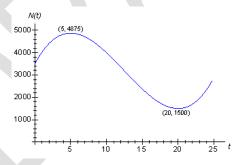
2 marks	Description
	Area = $0.5 \times 31.5 \times 27.4 \times \sin(85^\circ)$ \checkmark (mark for stating the area expression with correct
1	substitutions)
1	= 429.9m² ✓

(c) Find the area of the whole block of land ABCD.

4 marks	Description
	Treats polygon as two triangles
	Area of ABD = 429.9m ²
	In triangle CBD $19.2^2 + 41.8^2 - 2(19.2)(41.8)\cos(C^\circ) = 39.9^2 \checkmark$ (cosine rule stated with
1	correct substitutions)
1	Hence C = 71° ✓
	Area of CBD = $0.5 \times 19.2 \times 41.8 \times \sin(71^{\circ})$
1	= 379.4m² ✓
1	Total area = 429.9 + 379.4 = 809.3m ² ✓

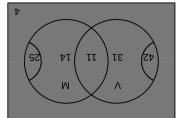
Question 8 [10 marks]

(a) Sketch a graph to show how the number of weeds varies from day to day, indicating clearly any maximum or minimum values.



3 marks	Description
1	shape, domain and y intercept correct \checkmark
1	Indicates max (5, 4875) clearly ✓
1	Indicates min (20, 1500) clearly ✓

(a) Use the above information to complete the Venn diagram below. Question 6 [7 marks]



	obtains 11 for the intersection \ \[\sqrt{1} \text{the intersection} \]	Ť
,	correct placement of 4, 42 and 25 on the Venn diagram	ī
	Description	3 шяқк

visiting The Valley of the Giants also intends to visit Monkey Mia?		
What is the probability that one of the tourists selected at random from those who intend	(i)	(q)

	Λ 09 Λ ΤΤ 09 π	τ'τ
Description		z marks

visit Monkey Mia, only? (ii) What is the probability that one of the whole group of tourists selected at random intends to

$ ho \frac{09}{pT}$	τ
Description	J mark

(iii) Write the question in (ii) in using probability notation.

			P(VOM)	τ
uo	Descripti			Ţ Wark

Mathematics 2C/2D: Sample Examination Marking Key

<u>√(M∩V)</u> 9	τ
nescubrou	т шчк

Mathematics 2C/2D: Sample Examination Marking Key

^ 1833.37 × 1.03°0 × 1.03°0 × 2.00 000 = \$241 833.37 √		
Description	usiks	3 m

in value of the house exceed the amount owing after 20 years? If so, by how much? The house was initially valued at \$300 000, increasing at a rate of 3% per annum. Will the increase

= \$209 743.07 ✓ (correct answer to 2 dp for the mark)	τ
\$\psi 000 \times \text{T'.08} \text{000 St}\$	τ'τ
Description	3 marks

(b) What amount would be owed after 20 years?

Interest and amount correct for Year 4 🗸	τ
Interest and amount correct for Year 3 V	Ţ
Description	2 marks

\$61 222.00	96'789 7\$	Þ
40.786 687.04	⊅0'66T ⊅\$	3
52 488.00	3 888.00	2
00.009 84	3 600.00	Ţ
(\$) gniwo tnuomA	Interest (\$)	Year (t)

last two rows.

The table below shows the annual interest and the total amount owing after t years. Complete the Question 6 [8 marks]

	\therefore for any x \ge 3 bypass will be used \checkmark	τ'τ
	30 – (15 + 12) = 3 (some indication of working) \checkmark	τ
Γ	Descubriou	3 WYLKS

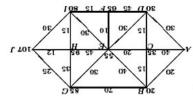
by x km. For what values of x will the shortest path from A to J use the bypass?	
L bass under construction will reduce the distance along the section connecting centres I and	(၁)

		Distance: 112 km 🗸	τ
		Shortest path: ADEFIHJ 🗸	τ
	unnduacac	1	CHIMILIZ

(b) Find the shortest path from A to J that passes through D. What is the length of this path?

.		 1		•			•			•		-	` .,
							, m	707 K	; :əɔı	Distar]		τ
						↑ CHI:	BCEL	∀ :կյբ	d ise	pour	S		τ
						ι	iagran	p uo	osths	gold p	3	ĺ	





RESOURCE-RICH EXAMINATION

Question 1 [6 marks]

(a) For the suburb of Riverton, six houses were sold in January. The prices were:

\$180 000, \$200 000, \$165 000, \$210 000, \$175 000, \$220 000

For these prices, find the

- (i) mean
- (ii) median

2 marks	Description
1	Mean: \$191 667 ✓
1	Median: \$190 000 ✓

(b) Give an example of the five prices that fit this description.

2 marks	Description
2	an example \$310 000, \$320 000, \$330 000, \$340 000, \$2 000 000

(c) Explain why the median is generally a better representative value than the mean for this type of data.

2 marks	Description								
2	One extreme value can make the mean increase so that it is no longer representative of the								
_	majority of the values.								

Question 2 [6 marks]

- (a) What is the total numbers of words she will have learnt after:
 - (i) 7 days?

1 mark	Description
1	31 + 7 × 8 = 87 ✓

(ii) n days?

1 mark		Description	
1	31 + 8n ✓		

- (b) Use algebraic recursive notation to describe:
 - (i) T_n , the total number of words she will have learnt after n days;

2 marks		Description
1.1	$T_0 = T_{n-1} + 8 \checkmark T_0 = 31 \checkmark$	

(ii) T_w , the total number of words she will have learnt after w weeks.

2 marks				Description
1,1	$T_w = T_{w-1} + 56$	✓	$T_0 = 31 \checkmark$	

Question 3 [13 marks]

(a) Give TWO different reasons for having confidence in the data in the table.

2 marks	Description
	Two good reasons, e.g.
2	It would have been a large sample
	Credibility of ABS, national government agency
	Published official results (likely to be checked more carefully)

(b) Describe as precisely as you can the meaning of the 37 in the second column of figures in the table.

3 marks	Description
1,1,1	Of the children questioned, 37% of 9-11 year olds accessed the internet at school. ✓ ✓ ✓
1,1,1	(three elements %, age, school needed for three marks)

(c) What percentage of the children (aged 5-14) did not access the internet over the twelve months represented in the table?

	1 mark	Description
Г	1	53% (i.e., 1 – 0.47, from bottom right of table, converted to %) ✓

(d) Describe, in detail, the internet access of the 9-11 year olds.

3 marks	Description
2	(i) School use of 37% > home use of 30% > other home use of 10%√ (ii) 55% access internet at any site ✓
3	(iii) Public library access negligible (3%)√

(e) Explain how to use the table to conclude that some students must have accessed the internet both at home and at school.

2 marks	Description
	If students accessed in home or school, but not both, then 'Any site' percentage would be
1	greater than 'home' + 'school' percentages ✓
	In each row of the table, 'home' + 'school' < 'any site', so some students must be counted twice
1	and thus have accessed internet in both home and school ✓

(f) What conclusions can you draw from the table about a relationship between internet access and age of children? Justify your answer.

2 marks	Description
1	It seems that access increases with age for children aged 5-14 ✓
1	This effect is evident in the first three rows of every column of the table.✓

Question 4 [5 marks]

(a) Greg simulated 20 rolls of a fair eight-sided die and averaged the results of the rolls. He repeated this process two times. Give examples of the averages he is likely to produce and justify your choices.

ı	3 marks	Description
	1	4 and 5 ✓
		Expect a different result each time, averages between 1 and 8 are possible, expect them to
	1.1	be fairly close to the average of 1. 28 (4.5) \checkmark (two properties)

(b) Next Greg simulated 200 rolls of the die and averaged the results of the rolls. Describe how averages produced in this way are likely to be different from those in part (b). Justify your description.

2 marks	Description
	With 200 rolls, the averages would most likely be closer to 4.5 than with 20 rolls (or narrow
1	range stated) ✓
1	because of larger sample size ✓