6=++h++zh+91+28-22 b = z(z+h) + z(h-x)(3 marks) (ii) Determine the equation of the circle in the form $x^2 + y^2 = ax + by + c$. > {x = 1 } = 1 } : ((1 mark) (i) State the domain of this relation. A circle of radius 3 has its centre at the point (4,-2). (g) (6 marks) 2 Noithold Working time: 50 minutes. This section has eight (8) questions. Answer all questions. Write your answers in the spaces 36% (24 Warks) Section One: Calculator-free METHODS UNIT 1 3 CALCULATOR-FREE

I write equation of and 11- hy- 28 = 7 h + 2

I convectly expand's

The graph of $x = y^2$ passes through the point (1,q). Determine the value(s) of q and hence explain why y is a relation but not a function of x.

Not a function as it is a veryolowation our to-mony rulotion. I boll possible voluce of of 6 =

See next page

METHODS UNIT 1 CALCULATOR-ASSUMED 9١

Question number:

Supplementary page

CALCULATOR-FREE

Question 2

(7 marks)

Solve the following equations for x.

(a) (4x-7)(x+5)=0.

(1 mark)

$$\gamma C = \frac{7}{9}$$
 , $\kappa = -$

 $x = \frac{7}{4}$, x = -5 / both solutions

(b)
$$\frac{x}{4} = \frac{3x-2}{3}$$
.

(2 marks)

$$3x = 12x - 8$$

I cross multiplies

$$\chi = \frac{8}{9}$$

1 convert

(c) $6x = 3x^2$.

$$3x^2-6x=0$$

3x(x-2)=0

 $\chi = 0, \chi = 2$

(2 marks)

I our convect solution

I both correct

(d)
$$x^2 + 4x - 11 = 0$$

(2 marks)

$$x = -\frac{4 \pm \sqrt{16 - 4(1)(-11)}}{2}$$

$$\chi = \frac{-4 \pm \sqrt{60}}{2}$$

(1)(-11) I correct wethod

I both solutions,

$$9 = 7 = -2 + \sqrt{15}$$

 $y = -2 - \sqrt{15}$

METHODS UNIT 1

(8 marks)

The circle shown has centre O and diameter AC of length 60 cm. Determine the shaded area given that $7 \times \angle AOB = 5 \times \angle BOC$.

15



CALCULATOR-ASSUMED

Question 21

LAOB = $\frac{5}{7}$ LBOC + $\frac{5}{7}$ LBOC = π i. LBOC = $\frac{7\pi}{12}$ or 105 for sequent

 $A = \frac{1}{2} \left(30\right)^2 \left(\frac{707}{12} - \sin\frac{747}{12}\right) \qquad \text{appropriately}$

I correct area A = 390 cm

A sector of a circle with radius r and subtended angle θ has a perimeter of 91 cm and an area of 490 cm². Determine the possible values of r and θ that satisfy these conditions.



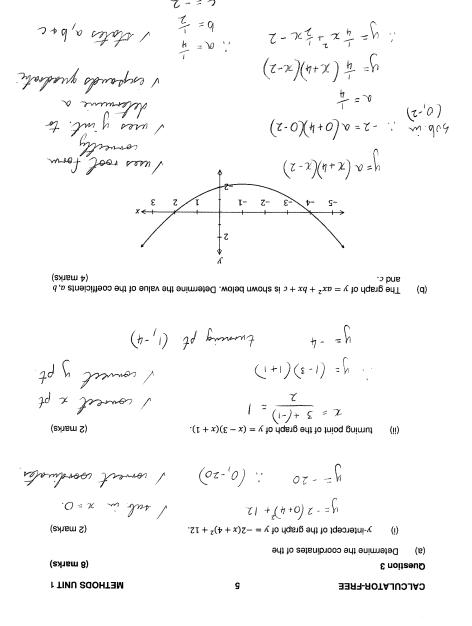
91=2r+0r / equation for perimeter

490='2r'0 / equation for area

beloing simultaneously.

r=28cm, 0=\frac{5}{4} or 68.75° equations

T= 17.5 am, 0 = 16 or 183.35° sets of solutions



See next page

I convert probability

(5 marks)

A random selection of 4 books is to be made from the shelf. tiction and the rest were poetry. A shelf held a collection of 22 different books, of which 5 were encyclopedias, 10 were science **Gnestion 20** (7 marks) CALCULATOR-ASSUMED 11 NETHODS UNIT 1

(a) Determine the number of ways

Jesus / 1315 / whent this can be done. (i) (1 mark)

1 wowest value of combinehous I conect we 0827 = °7 × "7 (S warks) a selection can be made that will not contain any encyclopedias.

(i) the selection will only contain poetry. Defermine the probability that (q)

.. p. 35 = 20.000 \ somest | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 | 20.0000 The x Connect number har

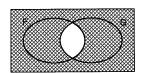
eucyclopedias. the selection will contain exactly one poetry book given that it does not contain any (ii)

Question 4

(7 marks)

Use set notation to describe the shaded region shown below.

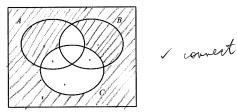
(1 mark)



F16 / correct

Hence or otherwise, shade $(\overline{A} \ U \ \overline{B}) \cap \overline{C}$

(1 mark)

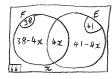


64 people applied for a job, of whom 38 were female and 41 had experience in a similar job. The number of females with experience was four times the number of males with no experience.

Determine

the number of females with no experience.

(3 marks)



41 + x + 38 - 4x = 64 / process for -3x = -15 solving for unknown. x = 5

". 38-4(5)=18 / convert females

: 18 Females have no experience

the probability that a randomly chosen applicant had no experience, given that they (2 marks) I connect numerator are male.

I convert devoucinator

See next page

CALCULATOR-ASSUMED

13

METHODS UNIT 1

Question 19

(6 marks)

Let
$$p = \cos \frac{13\pi}{18}$$
 and $q = \sin \frac{7\pi}{36}$.

Give your answers to the following in terms of p and/or q.

Write down an expression for

i)
$$\sin \frac{29\pi}{36}$$

(1 mark)

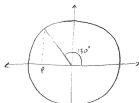
/ cornert

(ii)
$$\cos \frac{5\pi}{18}$$

(1 mark)

1 convect

Using your understanding of the unit circle, determine all other values of θ , within two revolutions whereby $\cos \theta = p$. Give your answers in degrees. (4 marks)



$$p = cos \frac{13\pi}{18}$$
, $\frac{13\pi}{18} = 130^{\circ}$ shows are of with circle

i. 0: 230°, 490°, 590° I convents to dequees

I gives auswer within I nevolution

I gives all convert answers

Jx mt (-1,0)
and some ymt

Substitutes, starting

there are two solutions. See next page I explains why 50 (x+1)(16x2-24x+9) = 0 folution box for both one graduatic use it to explain how many solutions the equation $(x+1)(16x^2-24x+9)=0$ will have. (c) Determine the value of the discriminant for the quadratic equation $16x^2 - 24x + 9 = 0$ and ishing Lew cusus \ 01- \pm (3-5) rowwall \ when \ 2001 201 011; (x-6)=-10 Jenethon equals

(x-6)=-10-3 0=5-,(9-2)=-Show that the equation has no real zeroes (i.e. no real roots) (2 marks) I golds in point and (12-17-) 5-2(9-2-) = L2completed agrand 5-2(9-x) 0=h I sule in t. P wite Determine the equation of the function. (b) A parabola has a turning point at (6, -5) and passes through the point (-2, -37).

I convect value

(9 marks)

CALCULATOR-ASSUMED

I was a mothod

Determine the value of k, using a method that does not refer to the graph of the parabola.

The equation of the axis of symmetry for the graph of $y = 3x^2 + 6x + 7$ is x = k.

15

(s)

Question 18

WETHODS UNIT 1

8

CALCULATOR-FREE

Question 6

(6 marks)

Let $f(x) = x^3 + 2x^2 - 11x - 12$.

(a) Identify the leading coefficient of f(x).

(1 mark)

1 / convect

(b) Determine f(-1).

(1 mark)

$$f(-1) = (-1)^3 + 2(-1)^2 - 11(-1) - 12$$

 $f(-1) = 0$ cornect

(c) Solve f(x) = 0.

(4 marks)

$$\begin{array}{lll} \chi + \chi & -12 \\ \chi + 1) \chi^{2} + 2\chi^{2} - 1/\chi - 12 & & & & & & & & & & & & \\ -(\chi^{2} + \chi^{2}) & & & & & & & & & & & & \\ \chi^{2} - 1/\chi - 12 & & & & & & & & & & \\ -(\chi^{2} + \chi) & & & & & & & & \\ \hline -12\chi - 12 & & & & & & & \\ -12\chi - 12 & & & & & & & \\ -(-12\chi - 12) & & & & & & & & \\ (\chi + 1)(\chi^{2} + \chi - 12) & & & & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & & \\ \chi^{2} + \chi^{2} - 1 & & & & \\ \chi^{2} + \chi^{2} - 1 & & \\ \chi$$

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CALCULATOR-ASSUMED

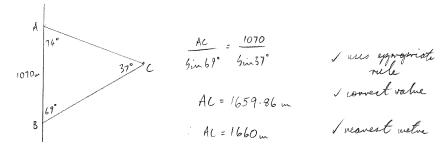
11

METHODS UNIT 1

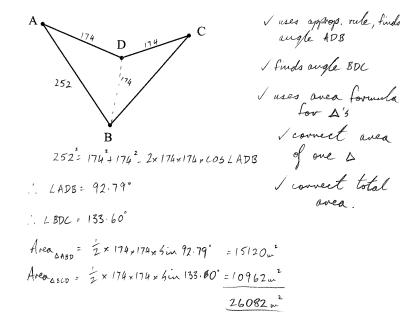
Question 17

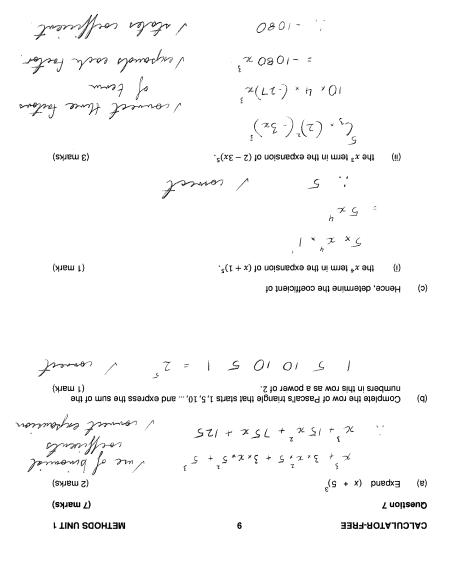
(8 marks)

(a) A and B are two points on a coastline, and C is a point at sea. The points A and B are 1070m apart. The angles CAB and CBA have magnitudes of 74° and 69° respectively. Find the distance from C to A to the nearest metre. (3 marks)



(b) Determine the area of the quadrilateral shown below given that $\angle BDC = \angle ADC$ AB = 252m and AD = BD = CD = 174m. (5 marks)





See next page

METHODS UNIT 1 CALCULATOR-ASSUMED 10

Question 16 (7 marks)

second paper (event B) whilst 87% did not gain a distinction in either paper. candidates gained a distinction in the first paper (event \mathbb{A}) and $\mathbb{A}\%$ gained a distinction in the An examination consisted of two papers, one of which was much harder than the other. 12% of

Using an appropriate diagram, determine the probability that a randomly chosen

gained a distinction in both papers. (i) (3 marks)

I completed diagram P(1, 2, d) = 0.03 m diagram

(1 mark)

gained a distinction in one paper but not the other.

0.09 + 0.01 = 0.1

gained a distinction in the second paper given that they gained a distinction in the

 $57.0 = \frac{21.0}{20.0}$

I connect water

0.12 × 0.04 \$ 0.03 (with wown)

. not wateredout to something of out p(111) x p(120) = p(120, 20d) / wet welghunder (b) State, with justification, whether events A and B are independent.

10

CALCULATOR-FREE

Question 8

(5 marks)

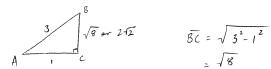
(a) Evaluate $\sin\left(\frac{35\pi}{42}\right)$.

(2 marks)

I simplifies consetly

:= 2 / convert value

An acute angle A exists such that $\cos A = \frac{1}{3}$. Show that $\sin A = \frac{2\sqrt{2}}{3}$ and hence, determine the value of tan A. (3 marks)



$$\therefore \sin A = \frac{opp}{hyp} = \frac{2\sqrt{2}}{3}$$

... tan
$$A = \frac{2\sqrt{2}}{1}$$

= 2-12 / use of pyth. to find opp.

I use of sin

I finds tou A

CALCULATOR-ASSUMED

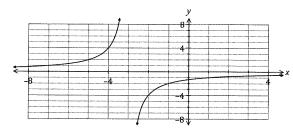
9

METHODS UNIT 1

Question 15

(7 marks)

The graph of y = f(x) is shown below where $f(x) = \frac{-a}{x-h}$



The hyperbola shown above has two asymptotes. State their equations. (2 marks)

7 = -3 / one convert

y=0 I both convect

State the values of constants a and b.

(2 marks)

I value of b

$$f(x) = \frac{-a}{x + 3}$$

I value of a

$$\frac{606}{(-1,-2)}$$
 $-2 = \frac{-\alpha}{-1+3}$

Describe how to transform the graph of y=f(x) to obtain the graph of y=f(x)+1 and state the domain and range of the transformed function. (3 marks

Translate the graph with up.

Domain: {x ∈ 1K; x ≠ -3} \ \transformation

Range: {y ∈ 1K; y ≠ 1} \ \ \transformation

\text{Vounge}

CALCULATOR-FREE

11

Supplementary page

Cuestion number:

CALCULATOR-ASSUMED

METHODS UNIT 1

(8 marks)

(1 mark)

Question 14

Two events, A and B, have probabilities P(A) = 0.4 and P(B) = 0.65.

8

Determine $P(A \cap B)$ in each of the following cases:

A and B are independent.

1 would

05 w 92.0 = 59.0 × 4.0 = (3) d × (4) d

(S marks)

(30) = P(A) + P(S) - P(A) = P(A) + P(S) + P(A) = P(P(ANB) = P(B) + P(B) - P(BNB)

 $.8.0 = (8 \cup A)q \qquad (ii)$

7 = 52.0 = (8VY)d:

(3 warks)

 $\frac{4}{6} = ((B \cup A)|A)^{q} \quad \text{(iii)}$

4 p.0 = 4

9.0 = (8LA) 9 ... P(A) 8) = 0.9 + 4.0 = (8LA) 9 ...

(b) Is it possible that A and B are mutually exclusive events? Explain your answer. (2 marks)

No, as P(A) + P(B) > 1 , ; wet possible.

I council reason (will wearow) on state to

12

CALCULATOR-FREE

Supplementary page

Question number: _

CALCULATOR-ASSUMED

7

METHODS UNIT 1

Question 13

(7 marks)

A triangle ABC has a = 36 cm, c = 52 cm and an area of 748 cm².

Sketch a triangle to show this information.

(1 mark)

A = 748 m² 52 cm

If $\angle B$ is an obtuse angle in the triangle

Determine the size of $\angle B$.

(2 marks)

.. 2B = 126.95°

Vues avea formula

I cowect angle

(c) Show that $b \approx 79$ cm.

(2 marks)

. b = 79.06 cm

= 79 cm

w that $b \approx 79 \text{ cm}$. $b^2 = 52^2 + 36^2 - 2(52)(36) \cos 126.95$ Uses appropriate b = 79.06 cmequation

I notices correctly

(d) Show that $\angle C \approx 32^{\circ}$.

: = 32°

(2 marks)

52 79.06
Sin L 5in 126.95

LC = 31.71°

/ solves convertly

CALCULATOR-ASSUMED

94% (86 Marks)

Section Two: Calculator-assumed

This section has thirteen (13) questions. Answer all questions. Write your answers in the spaces

3

Working time: 100 minutes.

(6 marks)

Question 9

A and C, determine the coordinates of C. The points A and B have coordinates (4,-6) and (5,8) respectively. If B is the midpoint of

Janoon 2 / (ZZ'9)) 4+ x = 5 -6+ y = 8 \ une midgle equation

y = mx + c. Determine the relationship for q in terms of p, if: x and y are linearly related variables such that the points D(5p, -q) and E(2q, 3p) lie on

(S marks)

(i) the gradient of the line is 2.

4-109 = 3p+9 = 13p g in terms of p

(26,9) (156,9) (156,9) (156,9) (156,9)

ing int is (0.43) 1 stoke y int.

See next page

CALCULATOR-ASSUMED

METHODS UNIT 1

The distortion of a signal, D, can be modelled by $D(x) = 4.55 - 4.5x + 1.95x^2 - 0.2x^3$, where x is Question 12 (8 marks) 9

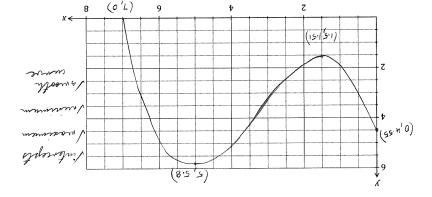
Determine D when x = 1. (9) (1 mark)

8.1 = (1)(

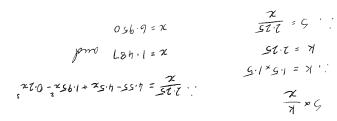
the distance from the signal source in metres and $0 \le x \le 7$.

(4 marks)

(b) Draw the graph of y = D(x) on the axes below.



distances at which the distortion, D, is equal to the signal strength, S. (3 marks) source, x, such that at 1.5 metres from the source, the strength is 1.5. Determine the The strength of the signal, S, is inversely proportional to the distance from the signal



I solveng regred by Vineral propertion

CALCULATOR-ASSUMED

Question 10 (8 marks)

A random sample of 121 passengers arriving at an airport were asked to complete a brief survey. They were asked to categorise their main place of residence as Australia or overseas and the main purpose of their travel as work, holiday or other. It was found that

- · half of the 84 passengers who resided overseas were on holiday
- 14 passengers were on holiday and resided in Australia
- of the 27 who were travelling for other reasons, 11 more resided overseas than in Australia.
- Use the above information to complete the two-way table below.

(3 marks)

| | Work | Holiday | Other | Total |
|-----------|------|---------|-------|-------|
| Australia | 15 | 14 | 8 | 37 |
| Overseas | 23 | 42 | 19 | 84 |
| Total | 38 | 56 | 27 | 121 |

I holiday column table correct

- If one passenger was selected at random from those surveyed, determine the probability (to 4 decimal places)
 - that the main purpose of their travel was work.

(1 mark)

that they resided overseas, given that the main purpose of their travel was work.

that the main purpose of their travel was work, given that they resided in Australia.

Explain whether the survey indicates that purpose of travel appears to be independent of

Explain whether the survey indicates that purpose of travel appears to be independent of main place of residence for these passengers. (2 marks)

Purpose of travel is not independent of vericleuce

P(
$$T_{\omega} \mid R_{A}) \neq P(T_{\omega})$$

Veccon

0.4054 \neq 0.3140

Verobabilities

See next page

CALCULATOR-ASSUMED

5

METHODS UNIT 1

(1 mark)

Question 11

(7 marks)

A positive integer less than 11 is chosen at random.

The outcome sets for events O, T and S are such that: $0 = \{odd\ numbers\} = \{1, 3, 5, 7, 9\}$

 $T = \{triangular numbers\} = \{1, 3, 6, 10\}$ and $S = \{square numbers\} = \{1, 4, 9\}.$

List the elements of the following sets:

 $0 \cap T$.

(ii) $T \cup (O \cap S')$.

Determine

(i)
$$n(O \cap S \cap T')$$
. (1 mark)

(ii)
$$P(O' \cap (T \cap S))$$
. (1 mark)

(iii)
$$P(T'|(O \cup S))$$
. (2 marks)