Perth Modern School

39 marks 7 Questions

Year 12 Mathematics Methods

Page | 1

PERTH MODERN SCHOOL

Exceptional schooling, Exceptional students
Independent Public School

TIME: 45 minutes working
One page Notice allowed
Calculator Assumed
Calculator Assumed
Calculator Assumed

Name: All part questions worth more than 2 marks require working to obtain full marks.

(4 marks)

f noiteauD

 $(x)_{i}\beta$

(2 marks)

(a) Define $h(x) = \frac{f(x)}{g(x)}$ use the table to find the value for h'(2).

(2 marks)

(b) Define I(x) = f(g(x)), use the table to find the value for I'(3).

$$|J| = |J|$$

$$|J|$$

$$|J| = |J|$$

$$|J| = |J|$$

$$|J|$$

Question 2

(3 marks)

Find the equation of the line tangent to the function $y = (3x^2 - 2)^3$ at the point (2,2). Give your answer in the gradient-intercept form.

$$y' = 3(3x^2-2)^2(6x)$$

 $x = 2$ $y' = 3600$ $y = 3600x + C$
 $z = 7200 + C$ $\sqrt{\text{solve for constant}}$
 $C = -7198$ $\sqrt{\text{states eqn of tangent}}$.

Question 3

(3 marks)

The time period T for a simple pendulum of length l is given by $T=2\pi\sqrt{\frac{l}{g}}$ where g is a constant.

If the length changes by 3%, use the incremental formula to estimate the percentage change in the period.

$$\Delta T \approx d \int \Delta I$$

$$= \frac{\pi}{\sqrt{g}} \int_{0}^{2\pi} \Delta I$$

$$= \frac{\pi}{\sqrt{g}} \int_{0}$$

Perth Modern School

Year 12 Mathematics Methods

Page | 3

Perth Modern School

Year 12 Mathematics Methods

Page | 6

(7 marks) Question 4

with a capacity of 4000π cm3. A company is purchasing a type of thin sheet metal required to make a closed cylindrical container

(j wstk) (a) Let the radius of the cylindrical base be r. Find the expression for the height h in terms of r.

4-12- 5-5 (b) Hence, find the expression for the surface area of the cylinder in terms of r.

thin sheet metal in order that it will have a capacity of 4000π cm³. (c) Therefore, find the least area of metal required to make a closed cylindrical container from

$$\frac{1}{36} = 2\pi z + \frac{1}{36008} = 2\pi z = 2$$

$$\frac{1}{36} = 2\pi z + \frac{1}{36000} = 2\pi z = 2$$

$$\frac{1}{36} = 2\pi z = 2$$

2 2992.2 Em

(6 marks) Question 7

The investment. The value of the portfolio, f(t) after t months can be modelled by the following value of the portfolio is momentarily stationary and then continues with negative growth for the life of negative rate of growth. The rate of growth remains negative until after 20 months (t = 20) when the A share portfolio, initially worth \$26000, has a value of f dollars after t months, and begins with a

model, $f(t) = -2t^3 + bt + ct + d$, $0 \le t \le 37$ months where b, c & d are constants.

0012-=0

0=-6(26)2+ 240(20)+C P=15Q 92 + (02) 21- = 0 0 = + (20) = + (20) Tathection pt (hores) \ 50/1085 for C. 9 rot compos/ 92+721-=(t),,t determines top for tilt) 7 + +972 + zt9 - = (t), + (1), + of dea commotob d = 26000 $\sqrt{100 - 2000}$ $\sqrt{100 - 2000}$ $\sqrt{100 - 2000}$ b esternines d Determine the values of the constants.

(8 marks)

The position of a train on a straight mono rail, x metres at time t seconds, is modelled by the following formula for the velocity, ν in metres/second, $\nu = pt^2 - 12t + q$ where p & q are constants. The deceleration of the train is $8ms^{-2}$ when t=1, has a position $x=\frac{4}{3}$ when t=2 and is initially at the origin (x = 0).

a) Determine the values of the constants p & q.

(4 marks)

$$\alpha = 2pt - 12$$

$$-8 = 2p(1) - 12$$

$$p = 2$$

$$V = 2t^{2} - 12t + 9$$

$$x = 2t^{3} - 6t^{2} + 9t + C$$

$$(=0)$$

$$4 = 2(2)^{3} - 6(2)^{2} + 29$$

$$\sqrt{\frac{1}{3}} = \frac{2}{3}(2)^{3} - 6(2)^{2} + 29$$

$$\sqrt{\frac{1}{3}} = \frac{2}{3}(2)^{3} - 6(2)^{2} + 29$$

$$\sqrt{\frac{1}{3}} = \frac{2}{3}(2)^{3} - 6(2)^{2} + 29$$

b) Determine the time(s) that the velocity is zero.

$$V = 2t^{2} - 12t + 10$$

$$= (2t - 2)(t - 5)$$

$$t = 1 \text{ or } 5$$

Voltains expression for Velocity V states both times

c) The distance travelled when the acceleration is $12ms^{-2}$. t=5 t=6 t=0 t=1 t=1V diagram (labella) distance = 1/4 + 1/3 + 50 + (50 +2)

Page | 5

Year 12 Mathematics Methods

Perth Modern School

Question 6

(8 marks)

(3 marks)

The volume, V in cubic metres and radius R metres, of a spherical balloon are changing with time, t seconds. $V = \frac{4\pi R^3}{3}$. The radius of the balloon at any time is given by $R = 2t(t+3)^3$.

Determine the following:

a) The value of $\frac{dR}{dt}$ when t = 1. $\frac{dR}{dt} = 2+3(t+3)^{3} + 2(t+3)^{3}$ $= 6(t)^{2} + 2(t+3)^{3}$ $= 6(t)^{2} + 2(t+3)^{3}$ $= 6(t)^{2} + 2(t+3)^{3}$ $= 6(t)^{2} + 2(t+3)^{3}$ $= 6(t+3)^{2} + 2(t+3)^{3}$ $= 6(t+3)^{2} + 2(t+3)^{3}$ $= 6(t+3)^{2} + 2(t+3)^{3}$ $= 6(4)^2 + 2(4)^3$ / obtains rate at += 1

b) The value of $\frac{dV}{dt}$ when t=1.

= 774

av = av ar = 471 R2 (224) = 47 (128) (224) = 46118781.77 $R = 2/4)^3$ (3 marks) / uses chain rule 1 determines Rat +=1 Jobbans of at t=1

Consider the volume of the balloon at t = 1.

c) Use the incremental formula to estimate the change in volume 0.1 seconds later (i.e t = 1.1)