PERTH MODERN SCHOOL
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Semester Two Examination, 2022

Question/Answer booklet

MATHEMATICS METHODS
UNIT 3 & 4
Section Two:
Calculator-assumed

Your Name: _____

Your Teacher's Name: _____

Time allowed for this section
Reading time before commencing work: ten minutes
Working time: one hundred minutes

Materials required/recommended for this section
To be provided by the supervisor
This Question/Answer booklet
Formula sheet (retained from Section One)

To be provided by the candidate
Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates
No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Marks	Max	Question	Marks	Max
7		8	13		11
8		15	14		12
9		8	15		10
10		8	16		8
11		10			
12		10			

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	6	6	50	49	33
Section Two: Calculator-assumed	11	11	100	99	67
				Total	100

Instructions to candidates

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in this Question/Answer booklet.

3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.

4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.

5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

6. It is recommended that you **do not use pencil**, except in diagrams.

7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed **(99 Marks)**

This section has **eleven** questions. Answer **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 100 minutes.

Question 7 **(5 marks)**

The time, T minutes, for a group of University students to complete a Mathematics task is assumed to be normally distributed.
It is known that 3% of students complete the task in at least 32 minutes, while 0.2% complete the task in less than 15 minutes.
Determine the mean and standard deviation of T. (5 marks)

Solution
$P(T > 32) = 0.03 \rightarrow z_1 = 1.8808$ and $P(T < 15) = 0.002 \rightarrow z_2 = -2.8782$ $1.8808 = \frac{32 - \mu}{\sigma}$ and $-2.8782 = \frac{15 - \mu}{\sigma}$ $\mu = 25.28$ and $\sigma = 3.57$
Specific behaviours
⏭ determines one z score ⏭ determines both z scores ⏭ sets up one equation for mean and stdev ⏭ sets up two equations for mean and stdev ⏭solves for mean and stdev Note: max of 2 marks is no working shown

Question 8 **(8 marks)**

A car insurance company models claims it pays out with a random variable \$$X$ which has a probability density function defined to be:

$$f(x) = \begin{cases} \frac{k}{x} & 1 < x < a \\ 0 & \text{otherwise} \end{cases}$$

The median claim is \$500.

(a) Show that $k = \frac{1}{2\ln 500}$. (3 marks)

Solution
$\int_1^{500} \frac{k}{x}\, dx = 0.5$ $\odot \quad \left[k\ln\lvert x\rvert\right]_1^{500} = 0.5$ $\odot \quad k\ln 500 = 0.5 \rightarrow k = \frac{1}{2\ln 500}$
Specific behaviours
⏭ sets up integral equation ⏭ integrates and subs limits ⏭ shows final result

(b) Determine what percentage of claims are less than $2500. (2 marks)

Solution
$P(X < 2500) = \int_1^{2500} \frac{1}{(2\ln 500)x}\, dx$ $= 0.629 = 62.9\%$
Specific behaviours
⏭ uses correct limits ⏭ obtains correct result

(c) The car insurance company determines that 6% of their clients submitted a claim in the past year. A sample of 320 clients is randomly selected. Describe and state the parameters of the sampling distribution of $\hat{p}$, the sample proportion of clients who submitted a claim in the past year. (3 marks)

Solution
$sd = \sqrt{\frac{0.06(1 - 0.06)}{320}} = 0.01328$ $\hat{p} \sim N\left(0.06,\ 0.01328^2\right)$
Specific behaviours
⏭ states normal

End of questions

⏭ states mean
⏭ states stdev or variance to at least 3 dp (accept calculation as answer for variance)

Question 9 (9 marks)

The score when a spinner is spun is given by the discrete random variable X with the following probability distribution, where a and b are probabilities.

x	– 1	0	2	4	5
$P(X = x)$	b	a	a	a	b

(a) Explain why $E(X) = 2$. (1 mark)

Solution
The data is symmetrical around the value of x = 2
Specific behaviours
⏭ explains symmetry (accept solving for a & b using two equations)

(b) Given that $Var(X) = 7.1$, determine the probabilities a and b. (3 marks)

Solution
$3a + 2b = 1$ $7.1 = (-1-2)^2 b + (0-2)^2 a + (2-2)^2 a + (4-2)^2 a + (5-2)^2 b$ $20a + 26b = 11.1$ a = 0.1 and b = 0.35
Specific behaviours
⏭ uses total prob=1 or equation for E(x) = 2 ⏭ uses series for variance ⏭ solves for a & b

The discrete random variable $Y = 10 – 3X$.

(c) Find the following:

(i) $E(Y)$ (1 mark)

Solution
$E(Y) = 10 – (3)(2) = 4$
Specific behaviours
⏭ determines value

(ii) Hence, explain why it is not possible to conclude that the lockdown lead to Australians eating more take away food? (2 marks)

Solution
The two confidence intervals overlap, and hence it is possible that the true proportion has not increased. (SCSA approved)
Specific behaviours
✓ States the two confidence intervals overlap. ✓ Explains how this indicates that the true proportion may not have changed. OR ✓ Not every confidence interval contains the true population proportion. ✓ Therefore no inference can be made.

(f) Assuming that sample proportion does not change, and a 95% confidence interval is used, determine how many people should be included in the survey to ensure that the researchers could conclude that Australians were eating more take away food in 2020 compared to 2019. (3 marks)

Solution
$E = 0.698 - 0.6668 = 0.0312$ $0.0312 > 1.96\sqrt{\frac{0.698 \times 0.302}{n}}$ $n = 831.89$ (832.07 if unrounded numbers used, 842.66 if 3 decimal places used) $i.e.\ 832 (\text{¿}\ 833 \vee 843)\ people$
Specific behaviours
✓ Uses Upper Boundary of previous Confidence Interval to calculate E ✓ Substitutes correct z value, sample proportion, E (followed through) to at least 3 decimal places ✓ Determines n and rounds up to whole number of people

Specific behaviours
✓ Clearly IDENTIFY the SOURCE of the bias (Wording, Vocabulary, Healthy, Leading Question). ✓ Clearly EXPLAINS WHY this is biased (logic / prediction / specific to scenario)

(ii) The interviewer selected their sample from 1000 people at a shopping centre food court. (2 marks)

Solution
This is biased because of the location. People attending the food court will be more likely to eat fast food.
Specific behaviours
✓ Clearly IDENTIFY the SOURCE of the bias (Location / Venue / food court). ✓ Clearly EXPLAINS WHY this is biased (logic / prediction / specific to scenario)

For the rest of this question, assume the above sample is random and unbiased, and was conducted by a group of scientific researchers.

The researchers conducted another survey in 2020 to see if nationwide lockdowns had changed the eating habits of Australians.

The 2020 survey of 500 Australians aged 14 and above found that 349 people ate take away food at least once a week.

(d) Explain why the researchers might conclude that the lockdown lead to Australians eating more take away food? (2 marks)

Solution
$\hat{p} = 0.698$ As the new sample proportion is above the upper boundary of the confidence interval in part (b)(ii).
Specific behaviours
✓ Determines new sample proportion. ✓ States new sample proportion is ABOVE the upper bound of the confidence interval (must state it is above, rather than outside).

(e) (i) Determine a 95% confidence interval for the population proportion of Australians who ate take away food at least once a week in 2020. (1 mark)

Solution
$0.6578 \leq p \leq 0.7382$
Specific behaviours
√ Determines confidence interval to at least 3 decimal places

(ii) Var(Y) (1 mark)

Solution
$7.1 \times (-3)^2 = 63.9$
Specific behaviours
⏭ determines value

The spinner is spun once. Find P($Y > X$). (3 marks)

(d)

Solution
$Y > X \ \therefore 10 - 3X > X$ $X < 2.5 \ \therefore X = -1, 0, 2$ $P(Y > X) = 2a + b = 0.55 \quad (\text{or } \frac{11}{20})$
Specific behaviours
⏭ sets up inequality for x only or maps out y values ⏭ solves for allowable x values ⏭ states total prob

Question 10 (7 marks)

The manager of a swimming pool wanted to confirm their estimate that 25% of local school students visited the pool at least once a month. The manager considered the following three ways of selecting a sample:

A Create an online survey and publish a link to it in the local newspaper.

B Visit local homes chosen at random and ask students who live there.

C Ask students who turn up to the pool after school.

(a) Briefly discuss a source of bias in each sampling method and suggest a better sampling procedure. (4 marks)

Solution
A: Undercoverage, will not sample students who don't see link in newspaper. A: Self-selection, only sample students who volunteer to take survey. B: Non-response, students might not want to divulge information when asked. B: Students may not be at home / bias towards those not at the pool C: Undercoverage, will not sample students who don't visit pool after school.

C: Convenience, only sample students who visit pool after school.
C: Non-response, students might not want to divulge information when asked.

Specific behaviours

- discusses a source of bias in A
- discusses a source of bias in B
- discusses a source of bias in C
- describes procedure involving random sampling from whole population

(b) It was found that 42 out of a random sample of 120 students visited the centre at least once a week. Determine the 95% confidence interval for the proportion based on this data and use it to comment on the manager's estimate. (3 marks)

Solution

$$p=\frac{42}{120}=0.35,\ 0.35\pm 1.96\sqrt{\frac{0.35(1-0.35)}{120}}\approx(0.2647,\ 0.4353)$$

The 95% confidence interval does not contain the manager's estimate of 0.25, and it suggests that the true value of the proportion is likely to be **higher** than 25%.

Specific behaviours

- indicates correct method to construct confidence interval
- correct confidence interval (to at least 2 dp)
- uses interval to dispute manager's estimate

Question 17 **(16 marks)**

A 2019 survey of 1000 Australians aged 14 and above found that 637 people in the sample indicated that they ate take away food at least once a week.

(a) Determine the sample proportion for this sample. (1 mark)

Solution

$$\hat{p}=0.637$$

Specific behaviours

√ Determines sample proportion.

The survey report included a 95% confidence interval for the population proportion of Australians who ate take away food at least once a week.

(b) (i) Complete the boxes below to form a 95% confidence interval for the population proportion of Australians who ate take away food at least once a week. (2 marks)

$$0.637-¿\ \boxed{1.96}\ \times\ \boxed{\sqrt{\frac{0.637\times 0.363}{1000}}}\ \leq p\leq 0.637+¿\ \boxed{1.96}\ \times\ \boxed{\sqrt{\frac{0.637\times 0.363}{1000}}}$$

Solution

Specific behaviours

√ Uses z value for confidence interval.

√ Writes in standard deviation (accept $\sqrt{\frac{0.637\times 0.363}{1000}}=\sqrt{0.000231}=0.01520623$).

(ii) Hence, determine a 95% confidence interval for the population proportion of Australians who ate take away food at least once a week. (1 mark)

Solution

$$0.6072\leq p\leq 0.6668$$

Specific behaviours

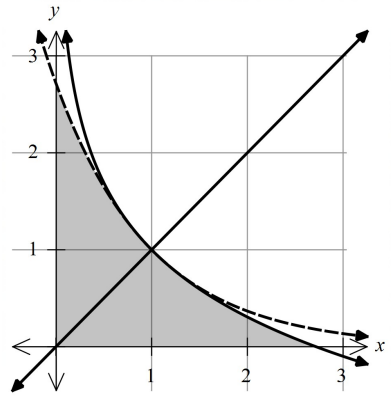
√ Determines confidence interval to at least 3 decimal places

(c) Identify and explain a possible source of bias with the following two sample schemes.

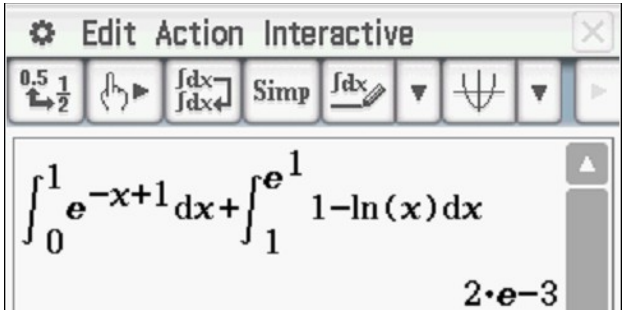
(i) The interviewer said they were from a company that offers a healthy meal delivery service. (2 marks)

Solution

This is biased because of the interviewer mentioned healthy meals. People may be reluctant to be honest about how much fast food they eat as they may be judged so less people would admit to eating take away food as it is regarded as not healthy.



(d) Determine the exact shaded area shown on the graph, justifying your answer. (2 marks)

Solution
The new area is a reflection of the old area in the line $y=x$. Hence $A=2\left(e-\frac{3}{2}\right)=(2e\text{-}3)\,units^2$ OR 

Specific behaviours
✓ Explains how to find the area by recognising that the graph is the inverse of $y=e^{-x+1}$ or states two integrals as above with exact limits.
✓ Determines exact area which is consistent with part (c). (max 1 mark if answer only as must justify for full marks)

Question 11 **(10 marks)**

An online retailer of auto parts knows that on average, 18.5% of parts sold will be returned.

(a) Let the random variable X be the number of parts returned when a batch of 88 parts are sold.

(i) Describe the distribution of X. (2 marks)

Solution
X is binomially distributed with parameters $n=88$ and $p=0.185$. or $X \quad B(88, 0.185)$
Specific behaviours
⏭ states binomial
◀ states correct parameters

(ii) Determine the probability that less than 15% of the parts sold in this batch will be returned. (2 marks)

Solution
$0.15\times 88=13.2$ $P(X\le 13)=0.2264$
Specific behaviours
⏭ indicates correct binomial probability to calculate
◀ correct probability

The retailer takes a large number of random samples of 150 parts from its sales data and records the proportion $\hat{p}$ of returned parts in each sample. Under certain circumstances, the distribution of $\hat{p}$ will approximate normality.

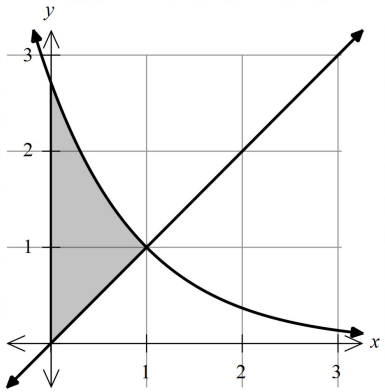
(b) Explain why the retailer can expect the distribution of $\hat{p}$ to closely approximate normality in this case. (3 marks)

Solution
The sampling is random (each observation is independent). The sample size is sufficiently large (typically 30 or more). Central limit Theorem Population proportion is not too near zero nor one.

Specific behaviours
⏭ states samples are randomly selected
◀ states sample size sufficiently large
◀ Mentions central limit Theorem OR p not too close to zero nor one.

(c) State the parameters of the normal distribution that $\hat{p}$ approximates and use this distribution to determine the probability that the proportion of returns in a random sample of 150 parts is less than 15%. (3 marks)

Solution
$\hat{p} \quad N(\mu_{\hat{p}}, \sigma^2_{\hat{p}})$
$\mu_{\hat{p}} = p = 0.185$
$\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}} = \sqrt{\frac{0.185(1-0.185)}{150}} \approx 0.0317, \sigma^2_{\hat{p}} \approx 0.0010052$
Hence normally distributed with mean 0.185 and standard deviation 0.0317.
$P(\hat{p} < 0.15) = 0.1348$
Specific behaviours
⏭ states mean of distribution
◀ states standard deviation or variance of distribution
◀ correct probability



(b) Show that the two graphs intersect when $x = 1$. (1 mark)

Solution
When $x = 1$, $y = e^{-1+1} = 1$
Specific behaviours
√ Substitutes in $x = 1$ and shows coordinates are the same.

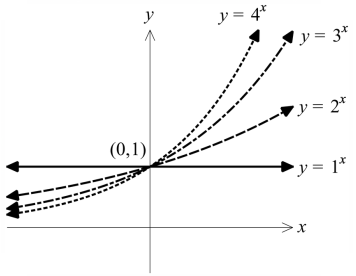
(c) Determine the exact shaded area shown on the graph. (3 marks)

Solution
$A = \int_0^1 e^{-x+1}\,dx - \int_0^1 x\,dx$
¿ $\left[-e^{-x+1}\right]_0^1 - \frac{1}{2}$
¿ $\left(-1-(-e)\right) - \frac{1}{2}$
¿ $\left(e - \frac{3}{2}\right) units^2$
Specific behaviours
✓ Writes down an appropriate integral to find the required area.
✓ Integrates and substitutes in boundaries.
✓ Determines area.

The axes below show the graphs of $y = x$ and $y = 1 - \ln x$. The graph of $y = e^{-x+1}$ is included as a dotted line.

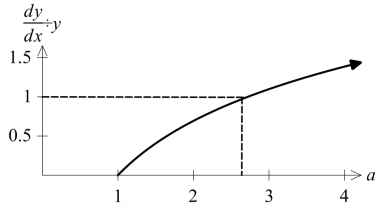
Question 16 **(7 marks)**

The family of curves with equation $y=a^x$ where $a>0$, are exponential curves, and are shown at right.



For each of these curves the value of $\frac{dy}{dx} \div y$ is constant for all values of x.

The values of $\frac{dy}{dx} \div y$ are graphed at right for different bases a.



Using first principles $\frac{dy}{dx} \div y$ can be written as:

$$\frac{dy}{dx} \div y = \frac{a^x\left(\lim\limits_{h \to 0} \frac{a^h-1}{h}\right)}{a^x} = \lim_{h \to 0} \frac{a^h-1}{h}$$

(a) State the value of a, for which $\lim\limits_{h \to 0} \frac{a^h-1}{h}=1$. (1 mark)

Solution
$a=e$
Specific behaviours
√ States the correct value of a.

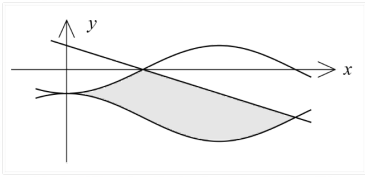
The axes below show the graphs of $y=x$ and $y=e^{-x+1}$.

Question 12 **(7 marks)**

Functions f, g and h are defined by

$$f(x)=10\cos\left(\frac{\pi x}{5}\right)-20 \quad g(x)=-10\cos\left(\frac{\pi x}{5}\right)$$
$$h(x)=10-4x.$$

The graphs of these functions are shown to the right.



(a) Determine the area between $y=f(x)$, the x-axis, $x=3.75$ and $x=5$. (3 marks)

Solution
$I=\int_{3.75}^{5} f(x)\,dx = -\frac{25\sqrt{2}}{\pi}-25$
Hence area is $\frac{25\sqrt{2}}{\pi}+25 \approx 36.3$ sq units.
Specific behaviours
⏭ writes integral (may preface with negative sign - see last mark)
◀ evaluates integral
◀ clearly deals with negative value of integral to obtain area

(b) Determine the area of the shaded region enclosed by the three functions. (4 marks)

Solution
Using CAS, $f=h$ when $x=2.5$ and $g=h$ when $x=7.5$.
$A=\int_{0}^{2.5} g(x)-f(x)\,dx+\int_{2.5}^{7.5} h(x)-f(x)\,dx = \left(50-\frac{100}{\pi}\right)+\left(50+\frac{100}{\pi}\right) = 100$ sq units
Specific behaviours
⏭ writes correct integral for area between $x=0$ and $x=2.5$
◀ evaluates first integral
◀ writes correct integral for area between $x=2.5$ and $x=7.5$
◀ evaluates second integral and states area of shaded region

Question 13 **(9 marks)**

In a random sample of 225 adult female Australians, 72 were born overseas. This data is to be used to construct a 90% confidence interval for the proportion of adult female Australians born overseas.

(a) Determine the margin of error for the 90% confidence interval. (3 marks)

Solution
$p=72\div 225=0.32, \sigma=\sqrt{\dfrac{0.32(1-0.32)}{225}}=0.0311$ $z_{0.9}=1.645, E=1.645\times 0.0311=0.0512$
Specific behaviours
⏭ correct proportion ◀ correct standard deviation of sample proportion ◀ correct margin of error

(b) State the 90% confidence interval. (1 mark)

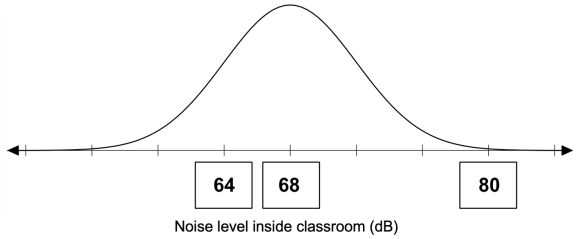
Solution
$p\pm E\rightarrow(0.2688, 0.3712)$
Specific behaviours
⏭ correct interval

(c) The 90% confidence interval for the proportion of adult male Australians born overseas constructed from another random sample was $(0.288, 0.412)$. Determine the number of adult males who were born overseas in this sample. (5 marks)

Solution
$E=(0.412-0.288)\div 2=0.062, p=0.288+0.062=0.35$ $\sqrt{\dfrac{0.35(1-0.35)}{n}}=\dfrac{0.062}{1.645}\rightarrow n=160$ $X=160\times 0.35=56\,\text{males}.$
Specific behaviours
⏭ calculates p and E ◀ uses sample proportion stdev expression ◀ calculates sample size n
✓ Substitutes into standardised score formula. ✓ Determines new mean.

High school students spend 45-75% of their time in the classroom listening to their teacher or classmates. Hence, classrooms can be prone to high noise levels. The noise levels inside a large number of busy classrooms were found to be normally distributed with a mean of 68 dB, and variance of 16 dB.

(f) Write a number in each box to provide to indicate the scale of the distribution. (2 marks)

Solution

Specific behaviours
✓ Correctly places mean of 68. ✓ Determines standard deviation and correctly places 64 and 80.

✓ Correctly determines probability.

(c) Describe one feature of the histogram that supports using a normal distribution to model the ambient noise levels. (1 mark)

Solution
The graph has a bell shaped curve
Specific behaviours
√ Refers to the shape of the distribution (Bell shape or almost symmetrical)

For the data, the mean ambient noise level is 37.3 dB and the standard deviation is 7.1 dB.

(d) (i) Using a normal distribution determine the probability a classroom has an ambient noise level of between 30 and 45 dB. (1 mark)

Solution
$Y \quad N(37.3, 7.1^2)$ $P(30 \le Y \le 45) = 0.7090$
Specific behaviours
√ Calculates correct probability

(ii) Using the histogram above, determine the probability that a classroom as an ambient noise level of between 30 and 45 dB, and explain whether this supports using a normal distribution to model this data. (2 marks)

Solution
$P(30 < X < 45) = 0.74$ Since 0.74 is close to 0.7090, it is appropriate to model this data with a normal distribution.
Specific behaviours
✓ Determines probability from histogram. ✓ Compares probability to part (d)(i) and concludes it is appropriate.

Assuming the data can be modelled using a normal distribution with a mean of 37.3 dB and the standard deviation of 7.1 dB, determine

(e) the value to which the mean ambient noise level would have to be reduced in order to ensure that at most 2% of the classrooms would fail to meet the standard. Assume that the standard deviation remains unchanged. (3 marks)

Solution
$P(Z > z) = 0.02$ $z = 2.0537$ $2.0537 = \frac{45 - \mu}{7.1}$ $\mu = 30.4\,dB$
Specific behaviours
✓ Determines standardised score.
◂ states z quantile ◂ correct number of males

Question 14 (8 marks)

To stop the spread of Covid it is advised to cover your nose when sneezing.

When humans sneeze the speed of the droplets expelled decrease at a constant rate of 3 ms^{-2}.

(a) Clearly show that $v(t) = -3t + c$. (2 marks)

Solution
$a = -3$ $v = \int -3\,dt = -3t + c$
Specific behaviours
⏭ Recognises $a = -3$. (or $v'(t) = -3$) ⏭ Integrates acceleration to get velocity.

(b) Determine, in terms of c, how long it takes the droplets to come to rest. (1 mark)

Solution
$-3t + c = 0$ $t = \frac{c}{3}$
Specific behaviours
⏭ Sets velocity to zero and solves for t.

(c) (i) Write down an integral expression for d, the distance travelled by the droplets from $t = 0$ until they come to rest. (2 marks)

Solution
$d = \int_0^{\frac{c}{3}} \lvert -3t \rvert\,dt$
Specific behaviours
✓ Recognises distance is the integral of the absolute value of velocity function. ✓ Integral includes boundaries from part (b).

(ii) The *New Scientist* magazine reported in 2020 that some droplets in a sneeze can travel upwards of 8 m.
Use your answer to part (c)(i) to find the initial speed of a sneeze, correct to two decimal places. (3 marks)

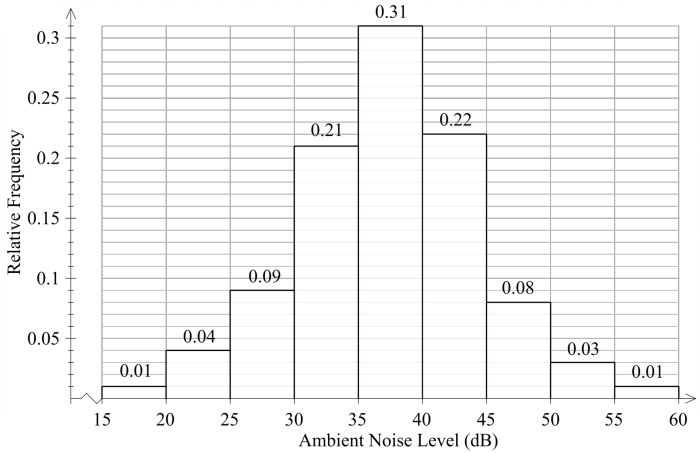
Solution
$8 = \left[\frac{3t^2}{2} \right]_0^{\frac{c}{3}}$ $8 = \frac{c^2}{6}$ $c = 6.93$ $i.e.\ initial\ speed\ is\ 6.93\,ms^{-1}$

Specific behaviours
✓ Correctly integrates expression in part (c)(i).
✓ Substitutes in boundaries and solves for c.
✓ States initial speed with unit

Question 15 (13 marks)

Current Australian standards currently recommend the maximum ambient noise level for an empty classroom is 45 dB.

Acoustic consultants tested the ambient noise level in the classrooms of a newly built school. Their results are shown in the relative frequency histogram below.



(a) Determine the proportion of classrooms that fail to meet the standard. (1 mark)

Solution
0.12
Specific behaviours
√ Determines correct proportion.

(b) Determine the probability that a classroom had an ambient noise level greater than 42.5 dB, given that it has an ambient noise level within 10 dB of the standard. (3 marks)

Solution
$P(X>42.5 \mid 35<X<55)$ $¿ \frac{P(42.5<X<55)}{P(35<X<55)}$ $¿ \frac{\frac{1}{2}\times 0.22+0.08+0.03}{0.31+0.22+0.08+0.03}$ $¿ \frac{0.22}{0.64}=\frac{11}{32}=0.34375$
Specific behaviours
✓ Correctly interprets conditional probability.
✓ Correctly determines $P(42.5<X<55)$.