

Question 5 (6 marks)

Twenty teachers have been marking the same set of exam papers and after double checking it was found that the teachers made the following number of errors.
1, 1, 3, 1, 4, 1, 3, 5, 1, 2, 2, 4, 4, 5, 0, 6, 5, 5, 5.

- (a) Construct a table that defines the **probability distribution** of X . (3 marks)

Let $X = \text{the number of errors of a teacher}$.

Question 6 (10 marks)

In a shop an average of 1 out of 5 pay with cash, 3 out of every 5 customers use a credit card, and the rest use a debit card to pay. A single customer is selected from the shop. The random variable X is defined as the number of customers who pay with cash.

(a) Complete the probability distribution for X shown below. (2 marks)		
$P(X=x)$	0	1
x		

- (c) Determine the mean and standard deviation of the distribution. (2 marks)

Four customers are waiting in a queue to pay. The random variable X is defined as number of customers from this queue who pay with **credit card**. (2 marks)

- (e) Evaluate the probability of at most one customer paying with credit card. (3 marks)
(No need to simplify)

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Semester One Examination, 2019
Question/Answer booklet

MATHEMATICS METHODS
UNIT 3

Section One:
Calculator-free

Your Name: _____
Your Teacher's Name: _____

Time allowed for this section
Reading time before commencing work: five minutes
Working time: fifty minutes

Materials required/recommended for this section
To be provided by the supervisor
This Question/Answer booklet
Formula sheet

To be provided by the candidate
Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,
correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates
No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Question	Marks	Max	Question	Mark	Max
1		6	5		6
2		6	6		10
3		8	7		10
4		6			

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	34
Section Two: Calculator-assumed	13	13	100	104	66
Total					100

Instructions to candidates

- The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the Year 12 *Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
- Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
- Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you **do not use pencil**, except in diagrams.
- The Formula sheet is **not** to be handed in with your Question/Answer booklet.

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(b) Using calculus, determine the number of transistors that will minimize the pollution produced. (4 marks)

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Additional working space

Question number: _____

Section One: Calculator-free (52 Marks)

This section has seven questions. Answer all questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 50 minutes.

Question 1 (6 marks)

Differentiate the following with respect to x :

(a) $e^x \sin(x^2 + 2)$ (2 marks)

(b) $\frac{\cos x}{x^2 + 5}$ (do not simplify) (2 marks)

(c) $\int_0^2 t^3 dt$ (2 marks)

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(d) Determine the area under the curve $y = f(x)$ from $-5 \leq x \leq 4$. (3 marks)

It is known that $f(x) \leq 0$ for $-3 \leq x \leq 4$ and $f(x) \geq 0$ for $-5 \leq x \leq -3$.

(e) the stationary points of $g(x)$ given that $g'(x) = \int_1^{x+5} f(t) dt$ with $-5 \leq x \leq 10$ (3 marks)

(f) $\int_x^{-5} f(x) dx$ (2 marks)

(g) $\int_4^{-3} f'(x) dx$ (2 marks)

Determine the following:

$\int_0^2 f(x) dx = 15$.

$f(x) > 0$ for all other values. It is also given that $\int_{10}^{-5} f(x) dx = 19$ and $\int_7^9 f(x) dx = -6$ and

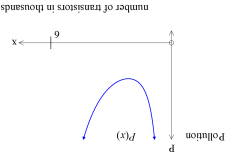
$f(-3) = -22$ and $f(4) = 13$. It is known that $f(x) \geq 0$ for $-5 \leq x \leq 0$ and $7 \leq x \leq 10$ with

Consider a smooth and continuous function $f(x)$ where $f(-5) = 0 = f(7) = f(10)$.

Question 7 (10 marks)

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(a) Describe how the pollution changes as the number of transistors made, varies from $0 < x \leq 5.5$ thousands. (2 marks)



where $0 < x \leq 5.5$ thousands.

$P(x) = \frac{x^3}{e^x}$

The amount of pollution, P , in tonnes, to build x thousands number of transistors by an electronic manufacturer, is given by the following formula:

Question 4 (6 marks)

Question 2 (6 marks)

"Blood flow" is defined as the volume V of blood flowing through an artery per unit of time. It can be modelled by the formula $V = kr^3$, where r is the radius of the artery and k is a constant.

- (a) By what fraction is the blood flow in the artery reduced when its radius is halved? (2 marks)

End of questions

(4 marks)

$$\int_{\frac{\pi}{2}}^0 13e^{2x} \cos 3x dx \quad (c)$$

Hence, determine the following integral by considering both expressions above.

- (b) $\frac{dp}{\rho} = \cos \lambda \, dx$ (2 marks)

- (c) Explain why the incremental formula does not give a good estimate for the change in V in part (a). (1 mark)

(2 marks)

$$\left(x \xi \sin_{x\xi} \vartheta \right) \frac{x\rho}{\rho} \quad (\text{a})$$

Determine the following:

Question 3 (8 marks)