

Evaluating the Generality and Appropriateness of Abstractions

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DSiS - Dependebility of Software-Intensive Systems Group

Motivation Mental Models



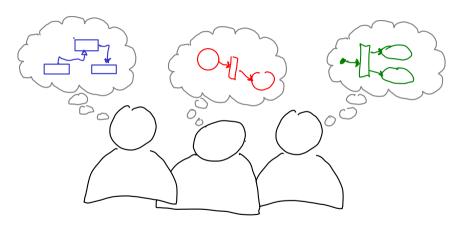


Figure 1: Different mental models formed to comprehend reality

Motivation Common Mental Model



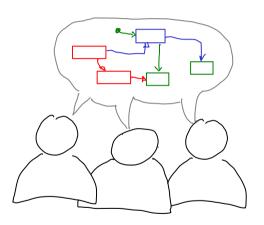


Figure 2: Discussion to come to common understanding (mental model)

Motivation Models in Tools (Programs)



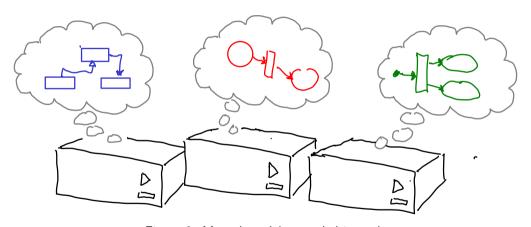


Figure 3: Mental models encoded in tools

Motivation Abstract Model for Tools



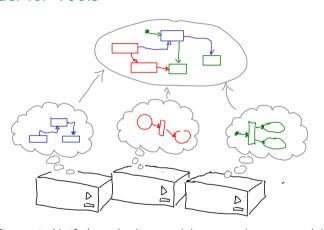


Figure 4: Unify/standardize models to an abstract model

PIBA



Problem: Difficult to evaluate generality and appropriateness of abstractions

Idea: Quantify *generality* and *appropriateness* by computing fractions of abstraction covered by models in tools and vice versa

Benefit:

- Evaluate *generality* and *appropriateness* of abstractions
- Prevent over generalization and over specialization of abstractions

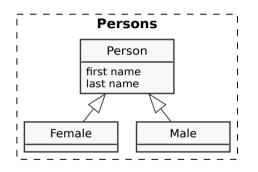
Approach:

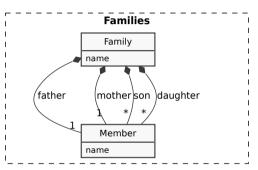
- Metrics for abstractions based on properties by Guizzardi et al. [2005]
- Specify mapping between concepts and relations
- Compute metrics wrt. mappings

Quantifying Abstractions



Example Abstract Model and Tool Model





- Let $m \in M$ be a concept m in model M
- Let $t \in T$ be a construct t in tool T

Properties for Granularity



Laconic

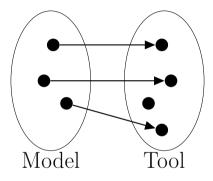


Figure 5: A tool is **laconic**, iff its constructs t implements at most one concept m of the model M [Guizzardi et al., 2005].

Properties for Granularity



Lucid

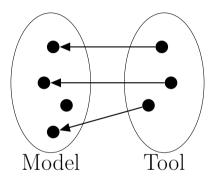


Figure 6: A model is **lucid**, iff its concepts m is implemented by at most one construct t of a tool T [Guizzardi et al., 2005].

Properties for Appropriateness Complete



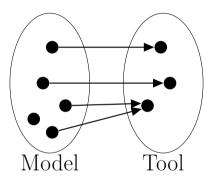


Figure 7: A tool is **complete**, iff its construct t is represented by at least one concept m in the conceptual model M [Guizzardi et al., 2005].

Properties for Appropriateness Sound



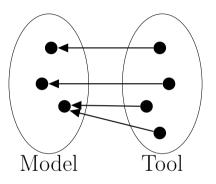


Figure 8: A model is **sound**, iff its concept m is implemented by at least one construct t in the tool T [Guizzardi et al., 2005, cf. proper].

Properties Example Example Abstract Model and Tool Model



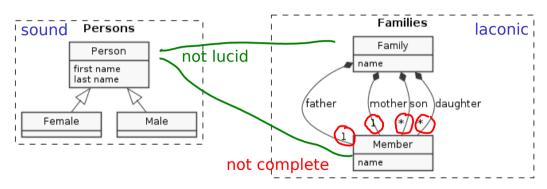


Figure 9: Abstract model is sound but not lucid; tool model is laconic but not complete.

Metrics



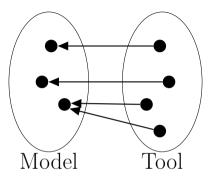


Figure 10: Mapping

- Let *M* be a model and *T* a tool
- Then $\mathbb{R}_T^M \subseteq M \times T$ is a mapping of concepts $m \in M$ to constructs $t \in T$

Metrics for Generality Laconicity



$$\mathsf{laconicity}(M, T) = \frac{\sum_{t \in T} \mathsf{laconic}(M, T, t)}{|T|}$$

$$\mathsf{laconic}(M,T,t) = \left\{ egin{array}{ll} 1 & \mathsf{if} \ |\{m \mid (m,t) \in \mathbb{R}_T^M\}| \leq 1 \ 0 & \mathsf{otherwise} \end{array} \right.$$

Lucidity

$$lucidity(M, T) = \frac{\sum_{m \in M} lucid(M, T, m)}{|M|}$$

$$\mathsf{lucid}(M, T, m) = \begin{cases} 1 & \mathsf{if} \ |\{t \mid (m, t) \in \mathbb{R}_T^M\}| \le 1 \\ 0 & \mathsf{otherwise} \end{cases}$$

Metrics for Appropriateness Completeness



$$\mathsf{completeness}(M,\,T) = rac{\sum_{t \in T} \mathsf{complete}(M,\,T,\,t)}{|T|}$$
 $\mathsf{complete}(M,\,T,\,t) = \left\{egin{array}{l} 1 & \mathsf{if} \ |\{m \mid (m,\,t) \in \mathbb{R}^M_T\}| \geq 1 \ 0 & \mathsf{otherwise} \end{array}
ight.$

Soundness

$$\mathsf{soundness}(M,\,T) = \frac{\sum_{m \in M} \mathsf{sound}(M,\,T,\,m)}{|M|}$$

$$\mathsf{sound}(M,\,T,\,m) = \left\{ \begin{array}{l} 1 & \mathsf{if} \,\,|\{t \mid (m,\,t) \in \mathbb{R}^M_T\}| \geq 1 \\ 0 & \mathsf{otherwise} \end{array} \right.$$

Metrics Example Example Abstract Model and Tool Model



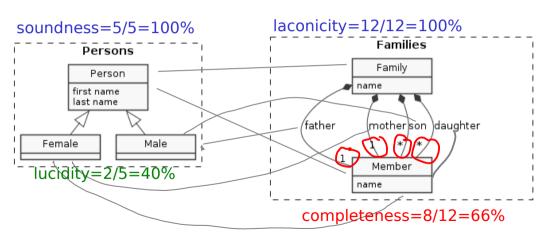


Figure 11: Abstract models *laconicity*, *lucidity*, *soundness*, *completeness*.

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Application Areas



Unified Model for Version and Variability Management Systems

- Establish *Unified Conceptual Model* in workshop discussions.
- Interview tool developers to create mapping to tool's model.
- Quantify appropriateness and generality of Unified Conceptual Model wrt. to selected tools [Ananieva et al., 2020]

Application Areas



Comparison of Taxonomies¹

- Systematic literature review collecting taxonomies for scientific publications in software engineering
- Define "standardized" universal taxonomy for scientific publications in software engineering
- Create mappings between universal and identified taxonomies
- Evaluate appropriateness and generality of universal taxonomy

Limitations



- Manually created mappings might introduce bias
- (Currently) only applicable for structural models (concepts and relations), but not for behavioral models (processes and operations)
- While suitable for vertical abstractions, limited suitability for horizontal abstractions

Conclusion



Problem: Difficult to evaluate generality and appropriateness of abstractions

Idea: Quantify generality and appropriateness by computing fractions of abstraction covered by models in tools and vice versa

Benefit:

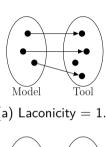
- Evaluate generality and appropriateness of abstractions
- Prevent over generalization and over specialization of abstractions

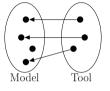
Approach:

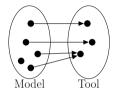
- Establish metrics for abstractions generality and appropriateness [Ananieva et al., 2020]
- Specify mapping between concepts and relations
- Compute metrics wrt. mappings

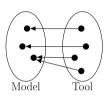
Appendix Abstract Metric Examples





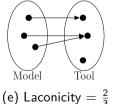


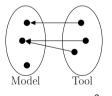


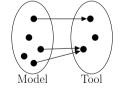


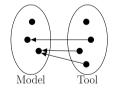
(a) Laconicity = 1.0 (b) Lucidity = 1.0

(c) Completeness = 1.0 (d) Soundness = 1.0









(f) Lucidity = $\frac{2}{3}$

(g) Completeness = $\frac{2}{3}$ (h) Soundness = $\frac{2}{3}$

Generalized Metrics



Given a finite set of tools $T \in \mathcal{T}$, we can generalize these metrics, as follows:

$$\overline{\mathsf{laconicity}}(M,\mathcal{T}) = \frac{\sum_{T \in \mathcal{T}} \sum_{t \in \mathcal{T}} \mathsf{laconic}(M,T,t)}{\sum_{T \in \mathcal{T}} |T|}$$

$$\overline{\mathsf{lucidity}}(M,\mathcal{T}) = \frac{\sum_{m \in m} \left(\min_{T \in \mathcal{T}} \mathsf{lucid}(M,T,m) \right)}{|M|}$$

$$\overline{\mathsf{completeness}}(M,\mathcal{T}) = \frac{\sum_{T \in \mathcal{T}} \sum_{t \in \mathcal{T}} \mathsf{complete}(M,T,t)}{\sum_{T \in \mathcal{T}} |T|}$$

$$\overline{\mathsf{soundness}}(M,\mathcal{T}) = \frac{\sum_{m \in M} \left(\max_{T \in \mathcal{T}} \mathsf{sound}(M,T,m) \right)}{|M|}$$

References I



Sofia Ananieva, Sandra Greiner, Thomas Kühn, Jacob Krüger, Lukas Linsbauer, Sten Grüner, Timo Kehrer, Heiko Klare, Anne Koziolek, Henrik Lönn, Sebastian Krieter, Christoph Seidl, S. Ramesh, Ralf Reussner, and Bernhard Westfechtel. A conceptual model for unifying variability in space and time. In *Proceedings of the 24th ACM Conference on Systems and Software Product Line - Volume A*, SPLC '20, New York, NY, USA, 2020. Association for Computing Machinery. ISBN 9781450375696. doi: 10.1145/3382025.3414955.

Giancarlo Guizzardi, Luís Ferreira Pires, and Marten van Sinderen. An ontology-based approach for evaluating the domain appropriateness and comprehensibility appropriateness of modeling languages. In *International Conference on Model Driven Engineering Languages and Systems*, MODELS. Springer, 2005. doi: 10.1007/11557432_51.