Section 8.10

8.10.1

a. Give a recursive algorithm to compute the sum of the cubes of the first n positive integers. The input to the algorithm is a positive integer n. The output is $\sum_{j=1}^{n}$. The algorithm should be recursive, it should not compute the sum using a closed form expression or an iterative loop.

```
CubeSum(n)
{
  if(n == 1) return(1);
  return(n**3 + CubeSum(n-1));
}
```

8.10.2

a. Give a recursive algorithm which takes as input a positive integer n and returns the sum of the first n positive odd integers.

```
OddSum(n)
{
   if(n == 1) return(1);
   return(2*n+1 + OddSum(n-1));
}
```

8.10.3

The input to the maximum and minimum problems is a sequence of numbers, $a_1
ldots a_n$, where n, the length of the sequence, is a positive integer. The function length $(a_1
ldots a_n)$ returns n, the length of the sequence. If n > 1, you can also create a new sequence $a_1
ldots a_{n-1}$, which is the original sequence $a_1
ldots a_n$, with the last number a_n omitted.

a. Give a recursive algorithm which takes as input a sequence of numbers and returns the minimum (i.e., smallest) number in the sequence. Your algorithm should not use an iterative loop.

```
 \begin{array}{l} SequenceMin(a,\ n) \\ \{ & \text{if}\,(n=\!\!-1)\ \text{return a.1}; \\ b = a.1 \ldots a.\{n-1\}; \\ \text{return Min}(a.n,\ SequenceMax(b,\ n-1)); \\ \} \end{array}
```

b. Give a recursive algorithm which takes as input a sequence of numbers and returns the maximum (i.e., largest) number in the sequence. Your algorithm should not use an iterative loop.

```
 \begin{cases} & \text{ if } (n == 1) \text{ return } a_{-}1; \\ & \text{ b} = a_{-}1 \dots a_{-}\{n-1\}; \\ & \text{ return } \operatorname{Max}(a_{-}n, \operatorname{SequenceMax}(b, n-1)); \end{cases}
```