

# L<sup>A</sup>T<sub>E</sub>X for Peter

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# 1 Logic

## 1.1 Propositions and Logical Operations

**Proposition:** a statement that is either true or false

Some examples include: "It is raining today", " $3 \cdot 8 = 20$ ".

However, not all statements are propositions: "open the door"

Name	Symbol	alternate name	$p$	$q$	$\neg p$	$p \wedge q$	$p \vee q$	$p \oplus q$
NOT	$\neg$	negation	T	T	F	T	T	F
AND	$\wedge$	conjunction	T	F	F	F	T	T
OR	$\vee$	dijunction	F	T	T	F	T	T
XOR	$\oplus$	exclusive or	F	F	T	F	F	F

XOR is very useful for encryption and binary arithmetic.

## 1.2 Evaluating Compound Propositions

$p$  : The weather is bad.

$q$  : The trip is cancelled.

$r$  : The trip is delayed.

**then**

$p \wedge q$  : The weather is bad *and* the trip is cancelled

$p \vee q$  : The weather is bad *or* the trip is cancelled

$p \wedge (q \oplus r)$  : The weather is bad *and* either the trip is cancelled *or* delayed

**Order of Evaluation**  $\neg$ , then  $\wedge$ , then  $\vee$ , but parenthesis always help for clarity.

## 1.3 Conditional Statements

## 1.4 Logical Equivalence

## 1.5 Laws of Propositional Logic

## 1.6 Predicates and Quantifiers

## 1.7 Quantified Statements

## 1.8 DeMorgan's law for Quantified Statements

## 1.9 Nested Quantifiers

## 1.10 More Nested Quantifiers

## 1.11 Logical Reasoning

## 1.12 Rules of Inference with Propositions

## 1.13 Rules of Interence with Quantifiers