Homework 8

2.1

3. Let

$$A = \begin{bmatrix} 4 & -1 & 1 & 6 \\ 0 & 0 & -3 & 3 \\ 4 & 1 & 0 & 14 \\ 4 & 1 & 3 & 2 \end{bmatrix}$$

Find the following:

a. M_{13} and C_{13} .

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b. M_{23} and C_{23} .

Work.

11. Use the arrow technique to evaluate the determinant of the given matrix.

$$\begin{bmatrix} -2 & 1 & 4 \\ 3 & 5 & -7 \\ 1 & 6 & 2 \end{bmatrix}$$

Work. \Box

18. Find all values of λ for which $\det(A) = 0$.

$$A = \begin{bmatrix} \lambda - 4 & 4 & 0 \\ -1 & \lambda & 0 \\ 0 & 0 & \lambda - 5 \end{bmatrix}$$

Work.

21. Evaluate det(A) by a cofactor expansion along a row or column of your choice.

$$A = \begin{bmatrix} -3 & 0 & 7 \\ 2 & 5 & 1 \\ -1 & 0 & 5 \end{bmatrix}$$

Work.

31. Evaluate the determinant of the given matrix by inspection.

$$\begin{bmatrix} 1 & 2 & 7 & -3 \\ 0 & 1 & -4 & 1 \\ 0 & 0 & 2 & 7 \\ 0 & 0 & 0 & 3 \end{bmatrix}$$

Work.

38. What is the maximum number of zeros that a 3×3 matrix can have without having a zero determinant? Explain your reasoning.

Proof.

2.2

14. Evaluate the determinant of the given matrix by reducing the matrix to row echelon form.

$$\begin{bmatrix} 1 & -2 & 3 & 1 \\ 5 & -9 & 6 & 3 \\ -1 & 2 & -6 & -2 \\ 2 & 8 & 6 & 1 \end{bmatrix}$$

Work.

27. Evaluate the determinant given that

$$\left| \begin{array}{ccc} a & b & c \\ d & e & f \\ g & h & i \end{array} \right| = -6.$$

$$\begin{vmatrix} -3a & -3b & -3c \\ d & e & f \\ g - 4d & h - 4e & i - 4f \end{vmatrix}$$

Work.

- **29.** Use row reduction to show that $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{vmatrix} = (b-a)(c-a)(c-b)$
- 30. description
- 34. description
- 2.3
- 19. description
- 27. description
- **33.** description