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Software Engineering 2

Automated Testing

Concolic Execution

Fuzzing



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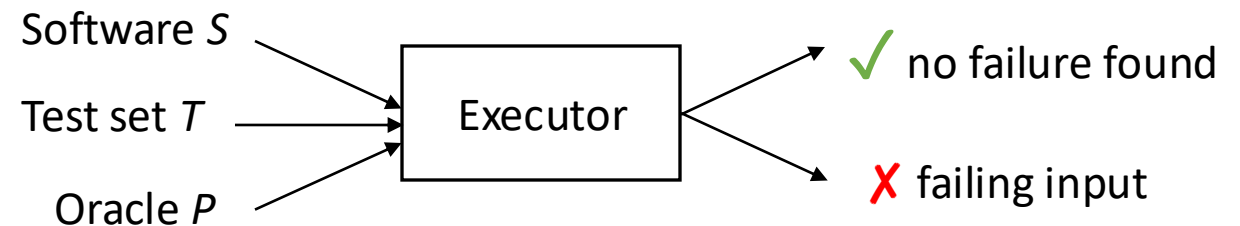
Verification & Validation

Dynamic Analysis, Testing

Dynamic analysis, aka testing

- The very idea

- Analyzes program **behavior**
- Properties are encoded as executable **oracles**, that represent
 - expected outputs, desired conditions (assertions)
- It can run only **finite** sets of **test cases** → it's **not exhaustive** verification
- Failures come with **concrete inputs** that trigger them
- Execution is **automatic** (definition of test cases and oracles may not)



What is the goal of testing?

The goal of testing is
making programs fail.

What is the goal of testing?

The **main** goal of testing is **making programs fail**

- **Other common goals**

- Trigger different parts of a program to increase coverage
- Make sure the interaction between components works (integration testing)
- Support fault localization and error removal (debugging)
- Ensure that bugs introduced in the past do not happen again (regression testing)

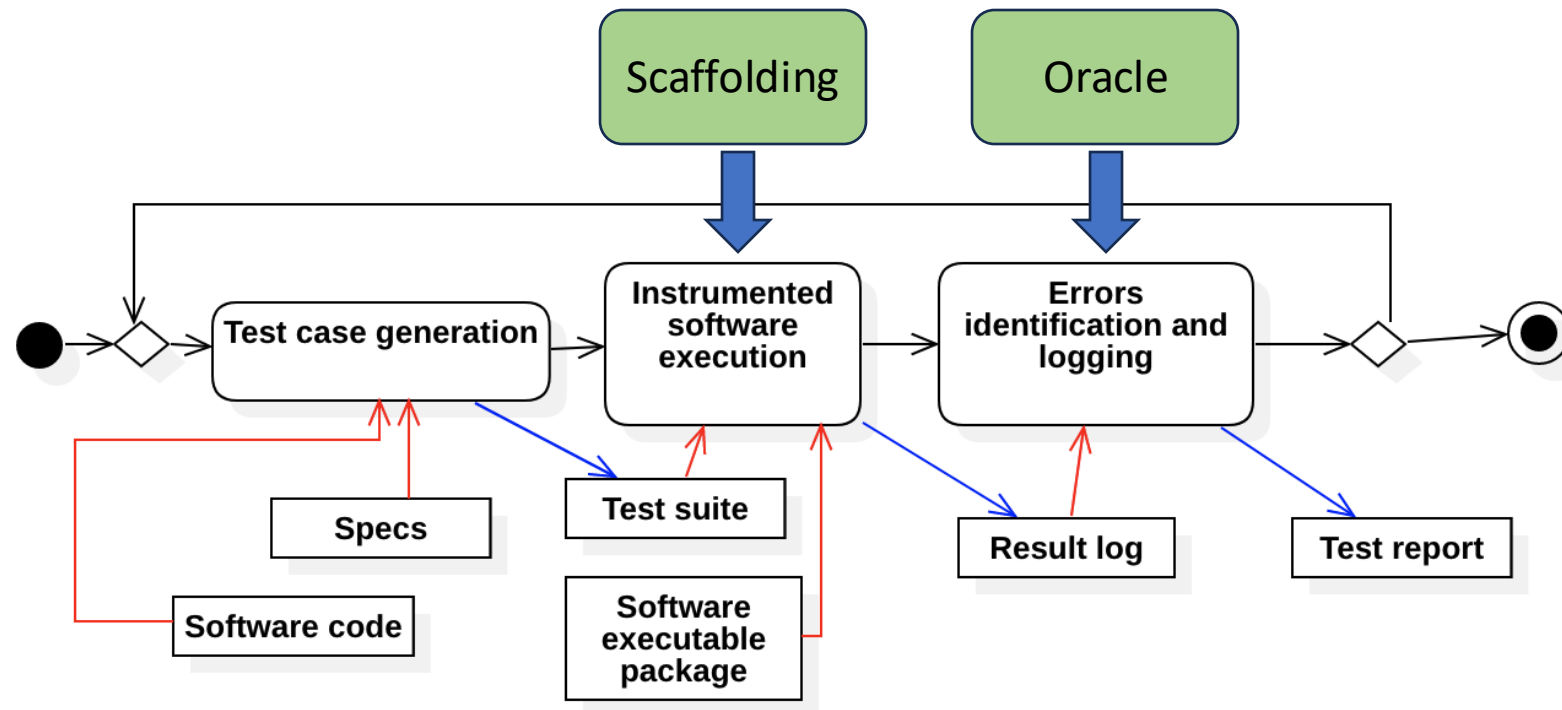
- **Important note**

- *“Program testing can be used to show the presence of bugs, but never to show their absence!” (Edsger W. Dijkstra)*

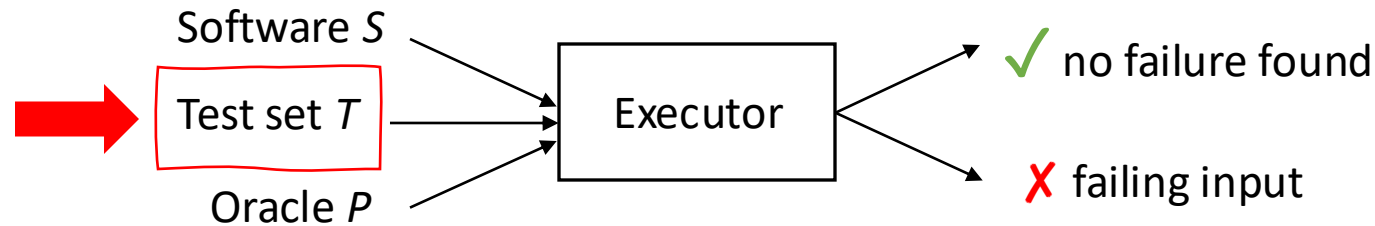
What is a test case?

- A **test case** is a set of **inputs**, **execution conditions**, and a **pass/fail criterion**
- **Running a test case** typically involves
 - **Setup**: bring the program to an **initial state** that fulfils the execution conditions
 - **Execution**: **run** the program on the actual inputs
 - **Teardown**: **record** the output, the final state, and any **failure** determined based on the pass/fail criterion
- A **test set** or **test suite** can include multiple test cases
- A **test case specification** is a requirement to be satisfied by one or more actual test cases
 - Example of test case specification: *“the input must be a sentence composed of at least two words”*
 - Example of test case input: *“this is a good test case input”*

Testing workflow



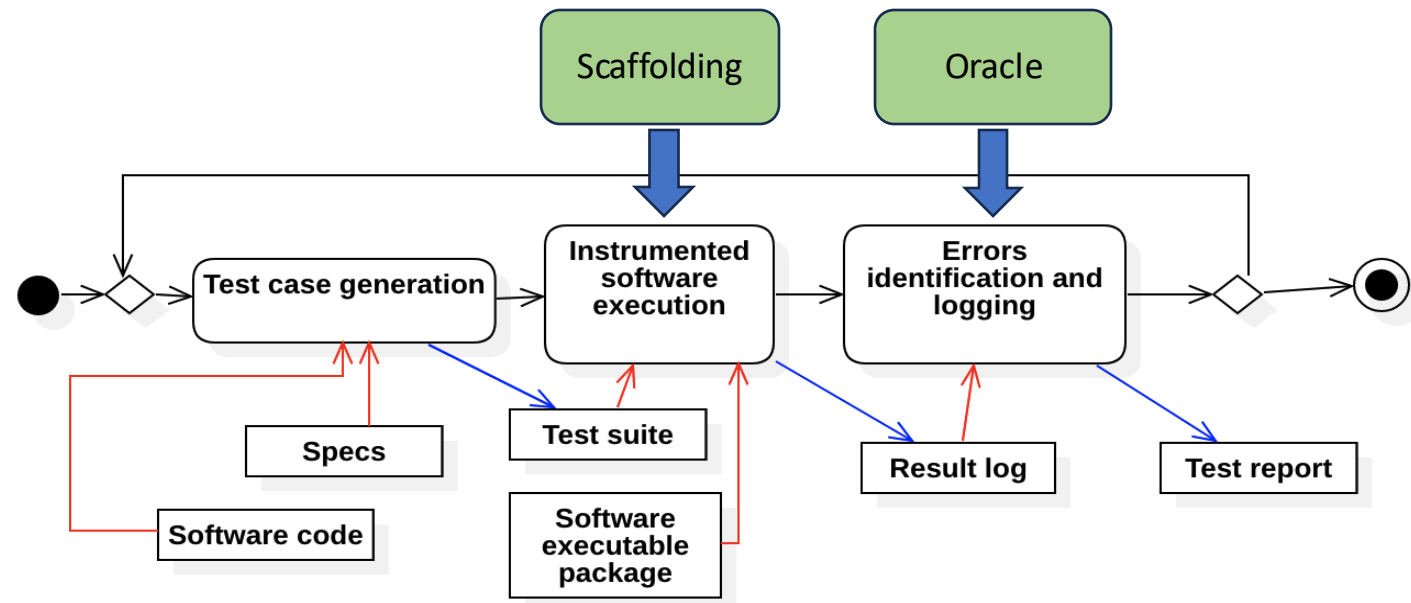
Test case generation



- Purpose: define *good quality* test sets
 - Showing a *high probability* of finding errors
 - Able to cover an *acceptable* amount of cases
 - *Sustainable* (we cannot run tests forever...)

Test case generation

- Test cases can be generated in a **black box** or **white box** manner
 - **White box**: generation is based on code characteristics
 - **Black box**: generation is based on specs characteristics



Test case generation

- Test cases can be defined **manually**
- Test cases can be **automatically** generated (automated testing)
 - Combinatorial testing = enumerate all possible inputs following some policy (e.g., smaller to larger).. not in this course!
 - **Symbolic execution** (we have seen it)
 - **Concolic execution** = pseudo-random generation of inputs guided by symbolic path properties
 - **Fuzz** testing (fuzzing) = pseudo-random generation of inputs including invalid, unexpected inputs
 - **Search-based** testing = explores the space of valid inputs looking for those that improve some metrics (e.g., coverage, diversity, failure inducing capability)

Symbolic execution: test case generation

- **Symbolic execution** can be used to automatically generate test cases
- **Procedure:**
 - Give as input a set of target locations or paths
 - Run symbolic execution
 - If the path condition is **SAT** for a target location or path
 - **Generate** one or more input assignments (i.e., test cases) satisfying the path condition
 - Do it for all identified locations and paths to define a test suite
- However, we already discussed the **weaknesses** of symbolic execution...



Verification & Validation

Automated Testing: Concolic (Concrete-Symbolic) Execution



Concrete-symbolic (concolic) execution

- **The very idea**
 - Perform symbolic execution **alongside** a concrete one (concrete inputs)
 - The **state** of **concolic execution** combines a **symbolic** part and a **concrete** part, used as needed to make progress in the exploration
- **Steps**
 - **Concrete to symbolic**: derive conditions to explore new paths
 - **Symbolic to concrete**: simplify conditions to generate concrete inputs

Concolic execution: example (concrete to symbolic)

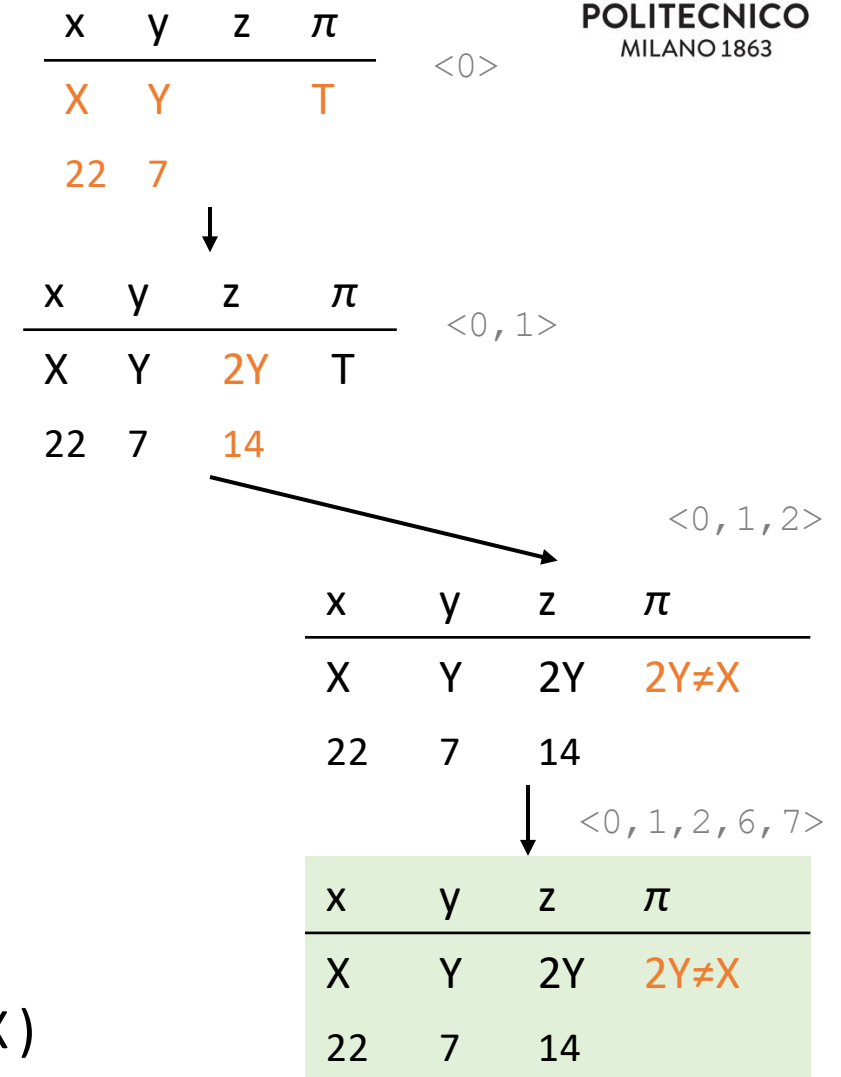
- **Example:** Let's explore all paths of procedure m
- We start from a **(random) concrete input**, at the same time, we build the **symbolic condition** of the explored path

```

0: void m(int x, int y) {
1:   int z := 2 * y
2:   if (z == x) {
3:     z := y + 10
4:     if (x <= z)
5:       print("Log message.")
6:   }
7: }

```

- $\{x=22, y=7\} \rightarrow$ path $\langle 0, 1, 2, 6, 7 \rangle$, path condition: $2Y \neq X$
- To explore another path, **negate** the path condition: $\neg(2Y \neq X)$



Concolic execution: example (symbolic to concrete)

- If we can **solve** the constraint, we **start again** with another concrete input that satisfies the new constraint $\neg(2Y \neq X)$

```
0: void m(int x, int y) {  
1:   int z := 2 * y  
2:   if (z == x) {  
3:     z := y + 10  
4:     if (x <= z)  
5:       print("Log message.")  
6:   }  
7: }
```

x	y	z	π
X	Y		T
2	1		

<0>

Solve: $\neg(2Y \neq X)$

Concolic execution: example (concrete to symbolic)

- We explore the new path and apply again the **concrete-to-symbolic** step

```

0: void m(int x, int y) {
1:   int z := 2 * y
2:   if (z == x) {
3:     z := y + 10
4:     if (x <= z)
5:       print("Log message.")
6:   }
7: }

```

- $\{x=2, y=1\} \rightarrow$ path $\langle 0, 1, 2, 3, 4, 5, 6, 7 \rangle$ with path condition $2Y=X \wedge X \leq Y + 10$

$\langle 0, 1, 2, 3, 4, 5, 6, 7 \rangle$

x	y	z	π
X	Y	Y+10	$2Y=X$
2	1	11	$X \leq Y+10$

x	y	z	π
X	Y		T
2	1		

$\langle 0 \rangle$

x	y	z	π
X	Y	$2Y$	T
2	1	2	

$\langle 0, 1 \rangle$

x	y	z	π
X	Y	$2Y$	$2Y=X$
2	1	2	

$\langle 0, 1, 2 \rangle$

x	y	z	π
X	Y	$Y+10$	$2Y=X$
2	1	11	

$\langle 0, 1, 2, 3 \rangle$

Partial negation: last condition only

$$2Y=X \wedge \neg(X \leq Y + 10)$$

Concolic execution: example (symbolic to concrete)

- New input values are identified

```
0: void m(int x, int y) {  
1:   int z := 2 * y  
2:   if (z == x) {  
3:     z := y + 10  
4:     if (x <= z)  
5:       print("Log message.")  
6:   }  
7: }
```

x	y	z	π
X	Y		T
30	15		



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Solve: $2Y=X \wedge \neg(X \leq Y + 10) \equiv$
 $2Y=X \wedge X > Y + 10$

Concolic execution: example (concrete to symbolic)

- We explore the new path and apply again the concrete-to-symbolic step

```

0: void m(int x, int y) {
1:   int z := 2 * y
2:   if (z == x) {
3:     z := y + 10
4:     if (x <= z)
5:       print("Log message.")
6:   }
7: }

```

- Conclusion: we have been able to cover all paths with the following test cases:
 - $\langle 0, 1, 2, 6, 7 \rangle$: $\{x=22, y=7\}$
 - $\langle 0, 1, 2, 3, 4, 5, 6, 7 \rangle$: $\{x=2, y=1\}$
 - $\langle 0, 1, 2, 3, 4, 6, 7 \rangle$: $\{x=30, y=15\}$

x	y	z	π	
X	Y		T	$\langle 0 \rangle$
30	15			



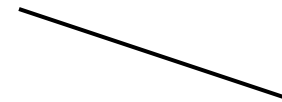
x	y	z	π	
X	Y	2Y	T	$\langle 0, 1 \rangle$
30	15	30		



x	y	z	π	
X	Y	2Y	2Y=X	$\langle 0, 1, 2 \rangle$
30	15	30		



x	y	z	π	
X	Y	Y+10	2Y=X	$\langle 0, 1, 2, 3 \rangle$
30	15	25		



$\langle 0, 1, 2, 3, 4, 6, 7 \rangle$

x	y	z	π
X	Y	Y+10	2Y=X
30	15	25	X>Y+10

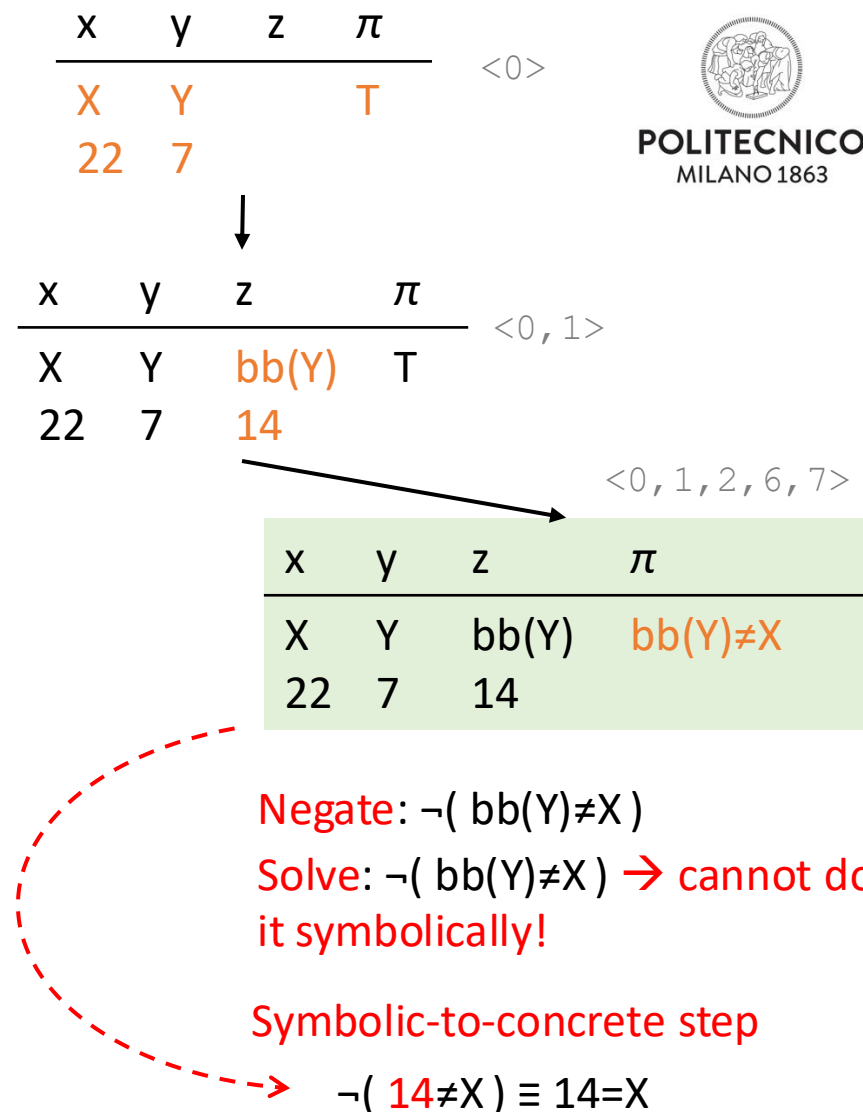


Concolic execution: example2

- **Example:** Let's explore again all paths of the procedure `m2`

```
0: void m2(int x, int y) {  
1:   int z := bb(y) //black-box function  
2:   if (z == x) {  
3:     z := y + 10  
4:     if (x <= z)  
5:       print("Log message.")  
6:   }  
7: }
```

- We try to follow the same approach, but, **in some cases, we cannot** solve the symbolic condition...
- Behavior of `bb` is unknown. We execute it with the identified input cases
 - Example: run `bb(7)` returns `14`
- Now the condition can be solved



Concolic execution: example2

- Now the constraint can be solved and we can start a new exploration

```
0: void m2(int x, int y) {  
1:   int z := bb(y) //black-box function  
2:   if (z == x) {  
3:     z := y + 10  
4:     if (x <= z)  
5:       print("Log message.")  
6:   }  
7: }
```

x	y	z	π	
X	Y		T	<0>
14	7			



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Solve: $\neg(14 \neq X) \equiv 14 = X$

Concolic execution: example2

- New explorations follow the same approach

```

0: void m2(int x, int y) {
1:   int z := bb(y) //black-box function
2:   if (z == x) {
3:     z := y + 10
4:     if (x <= z)
5:       print("Log message.")
6:   }
7: }

```

x	y	z	π	
X	Y		T	$\langle 0 \rangle$
14	7			



x	y	z	π	
X	Y	bb(Y)	T	$\langle 0, 1 \rangle$
14	7	14		



x	y	z	π	
X	Y	bb(Y)	bb(Y)=X	$\langle 0, 1, 2 \rangle$
14	7	14		



x	y	z	π	
X	Y	Y+10	bb(Y)=X	$\langle 0, 1, 2, 3 \rangle$
14	7	17		

$\langle 0, 1, 2, 3, 4, 5, 6, 7 \rangle$



x	y	z	π
X	Y	Y+10	bb(Y)=X
14	7	17	X ≤ Y+10

Negate last condition:

$bb(Y)=X \wedge \neg (X \leq Y+10) \equiv bb(Y)=X \wedge X > Y+10$

Solve: $bb(Y)=X \wedge X > Y+10 \rightarrow \text{cannot!}$

Concolic execution: example2

x	y	z	π
X	Y		T
34	17		

<0>



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- New explorations follows the same approach

```
0: void m2(int x, int y) {  
1:   int z := bb(y) //black-box function  
2:   if (z == x) {  
3:     z := y + 10  
4:     if (x <= z)  
5:       print("Log message.")  
6:   }  
7: }
```

Concretize: $bb(Y)=X \wedge X>Y+10$

We select Y randomly, execute bb(Y) and check if the formula holds

Example: Y=17, bb(Y)=34

Solve: $Y=17 \wedge bb(Y)=34 \wedge bb(Y) =X \wedge X>Y+10$

Concolic execution: example2

- New explorations follows the same approach

```

0: void m2(int x, int y) {
1:   int z := bb(y) //black-box function
2:   if (z == x) {
3:     z := y + 10
4:     if (x <= z)
5:       print("Log message.")
6:   }
7: }

```

x	y	z	π	
X	Y		T	<0>
34	17			



x	y	z	π	
X	Y	bb(Y)	T	<0, 1>
34	17	34		



x	y	z	π	
X	Y	bb(Y)	bb(Y)=X	<0, 1, 2>
34	17	34		



x	y	z	π	
X	Y	Y+10	bb(Y)=X	<0, 1, 2, 3>
34	17	27		

<0, 1, 2, 3, 4, 6, 7>



x	y	z	π
X	Y	Y+10	bb(Y)=X
34	17	27	X>Y+10

Concolic execution: pros and cons

- **Advantages**

- Can deal with black-box functions in path conditions (not possible with symbolic exec)
- As symbolic execution, can generate concrete test cases automatically

- **Limitations**

- Finds just **one input example** per path, however...
 - Failures typically occur with certain inputs only
 - If failures are rare events, it's unlikely to spot them with concolic exec
- #paths explode due to complex nested conditions → **large search space**
- **Does not guide the exploration**, it just explores possible paths one by one as long as we have budget (e.g., time, #runs)

Positioning concolic execution in the testing workflow



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Concolic execution
introduces automation
here, it is white box

