



Faculty of Engineering, Architecture and Science


Department of Electrical and Computer Engineering

Course Number	<b>ELE 532</b>
Course Title	<b>Signals and Systems 1</b>
Sem/Year	<b>Fall 2020</b>
Instructor	<b>Dr. Soosan Beheshti</b>

## **Lab/Tutorial Report # 1**

Report Title	<b>System Properties and Convolution</b>
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Submission Date	<b>12</b>
Due Date	<b>25th October 2020</b>

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Student ID	<b>500894595</b>
Signature	

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*<http://www.ryerson.ca/senate/policies/pol60.pdf>.*

### Problem A1 (C=1uF)

Code:

```
% CH2MP1.m : Chapter 2, MATLAB Program 1
% Script M-file determines characteristic roots of op-amp circuit.
% Set component values:
R = [1e4, 1e4, 1e4];
C = [1e-6, 1e-6];
% Determine coefficients for characteristic equation:
A = [1, (1/R(1)+1/R(2)+1/R(3))/C(2), 1/(R(1)*R(2)*C(1)*C(2))];
% Determine characteristic roots:
lambda = roots(A);
p = poly(A);
```

#### Command Window

```
>> CH2MP1
>> lambda

lambda =

    -261.8034
    -38.1966

>> p

p =

    1.0e+06 *

    0.0000    -0.0103    3.0103   -3.0000

fx >>
```

### Problem A1 (C=1uF->1nF)

Code:

```
% CH2MP1.m : Chapter 2, MATLAB Program 1
% Script M-file determines characteristic roots of op-amp circuit.
% Set component values:
R = [1e4, 1e4, 1e4];
C = [1e-9, 1e-6];
% Determine coefficients for characteristic equation:
A = [1, (1/R(1)+1/R(2)+1/R(3))/C(2), 1/(R(1)*R(2)*C(1)*C(2))];
% Determine characteristic roots:
lambda = roots(A);
p = poly(A);
```

### Command Window

```
>> CH2MP1
>> lambda

lambda =

    1.0e+03 *
   -0.1500 + 3.1587i
   -0.1500 - 3.1587i

>> p

p =

    1.0e+09 *
    0.0000   -0.0100    3.0100   -3.0000

fx >>
```

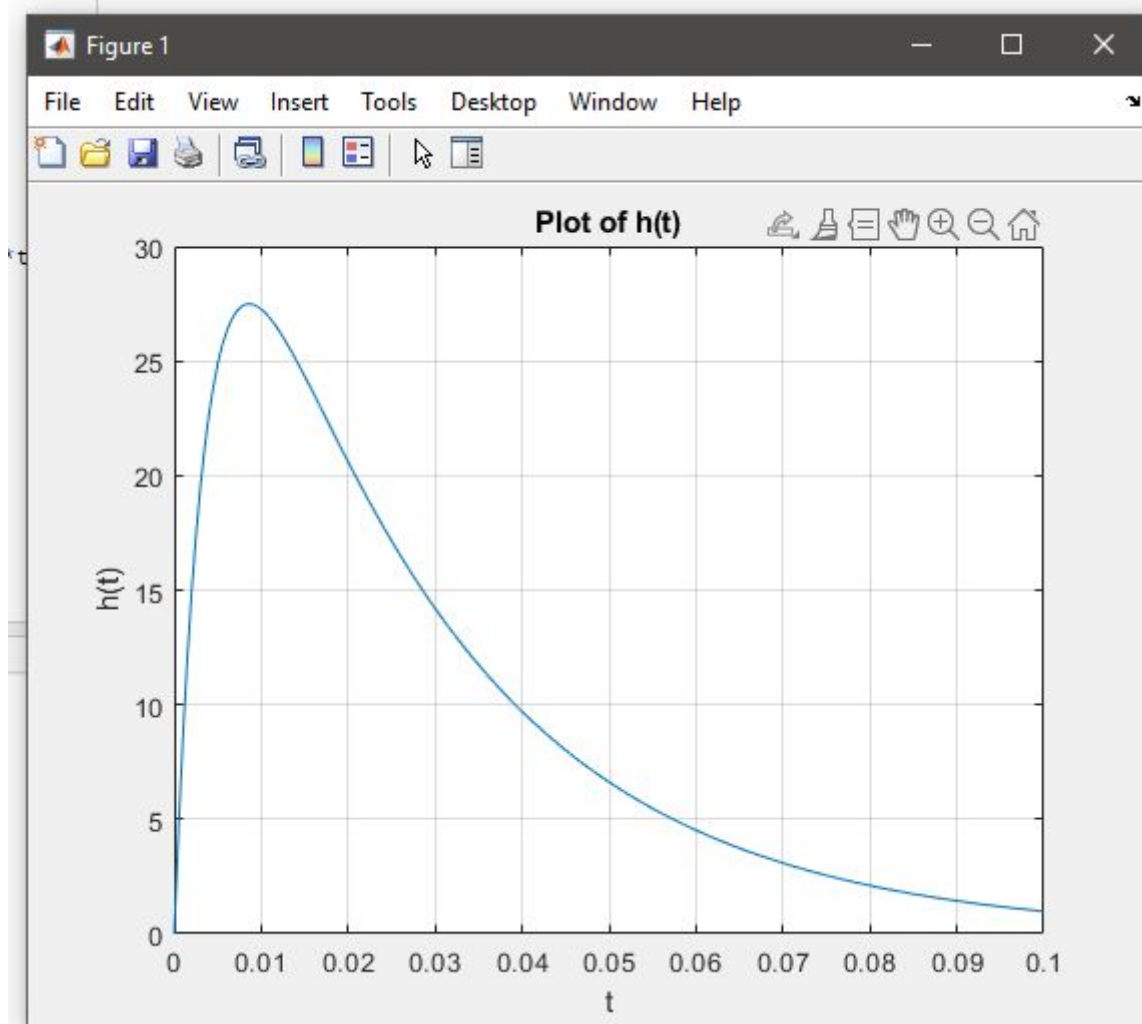
### Problem A.2

Code:

```
% CH2MP1.m : Chapter 2, MATLAB Program 1
% Script M-file determines characteristic roots of op-amp circuit.
% Set component values:
R = [1e4, 1e4, 1e4];
C = [1e-6, 1e-6];
% Determine coefficients for characteristic equation:
A = [1, (1/R(1)+1/R(2)+1/R(3))/C(2), 1/(R(1)*R(2)*C(1)*C(2))];
% Determine characteristic roots:
lambda = roots(A);
p = poly(A);

% solve for LTE of h(t) function accordingly with roots given
t = (0:0.0005:0.1);
u = @(t) 1.0.*(t>=0);
h = @(t) -44.721359 .* exp(-261.8034 .*t) + 44.721359 .* exp(-38.1966.*t).*u(t);

plot(t, h(t));
xlabel('t');
ylabel('h(t)');
title('Plot of h(t)');
axis([0 0.1 0 30]);
grid;
```



### Problem A3

Code:

```
function [lambda] = CH2MP2(R,C)
% CH2MP2.m : Chapter 2, MATLAB Program 2
% Function M-file finds characteristic roots of op-amp circuit.
% INPUTS: R = length-3 vector of resistances
% C = length-2 vector of capacitances
% OUTPUTS: lambda = characteristic roots
% Determine coefficients for characteristic equation:
A = [1, (1/R(1)+1/R(2)+1/R(3))/C(2), 1/(R(1)*R(2)*C(1)*C(2))];
% Determine characteristic roots:
lambda = roots(A);
```

### Command Window

```
>> lambda = CH2MP2([1e4, 1e4, 1e4],[1e-9, 1e-6])

lambda =

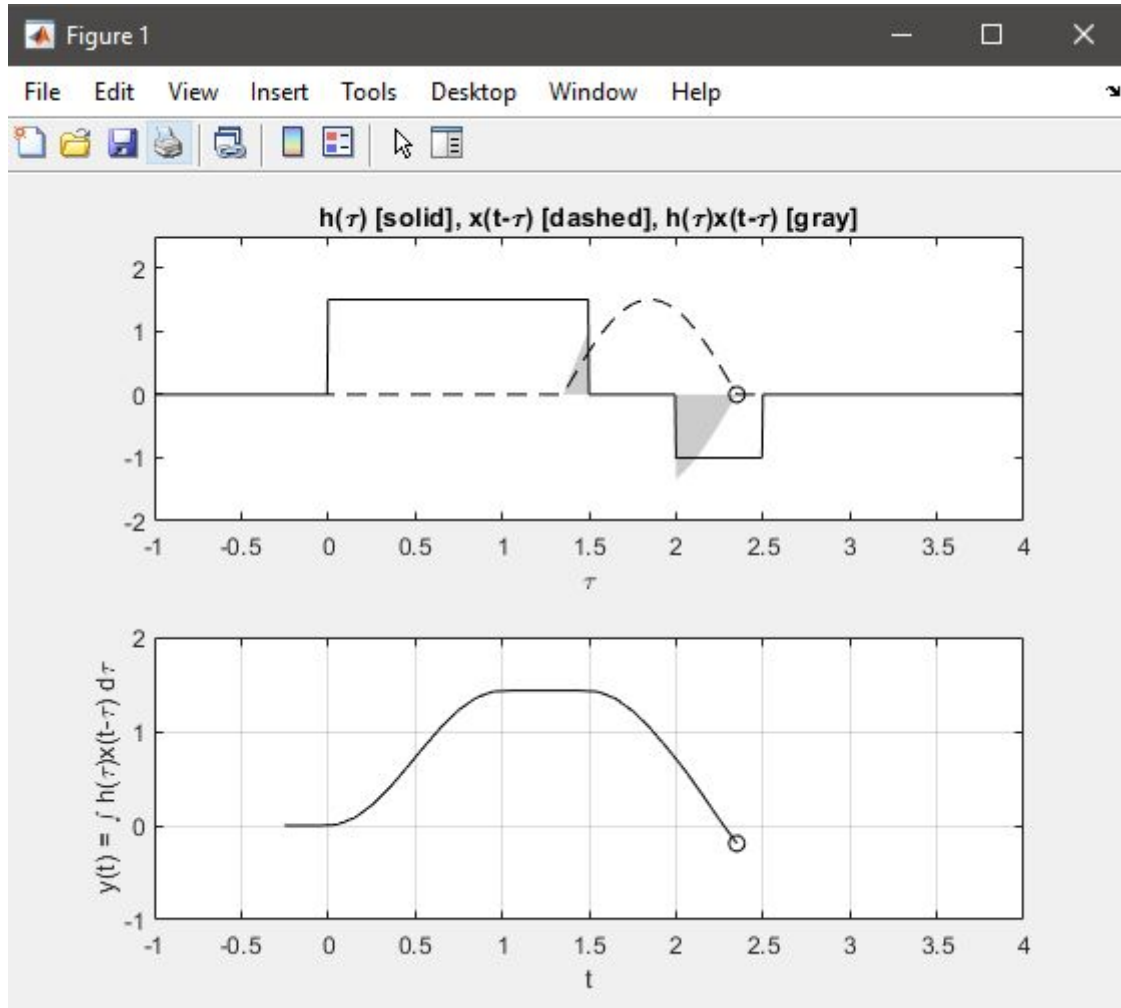
    1.0e+03 *

   -0.1500 + 3.1587i
   -0.1500 - 3.1587i
```

### Problem B.1

Code:

```
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0*(t>=0);
x = @(t) 1.5*sin(pi*t).*(u(t)-u(t-1));
h = @(t) 1.5*(u(t)-u(t-1.5))-u(t-2)+u(t-2.5);
dtau = 0.005; tau = -1:dtau:4;
ti = 0; tvec = -.25:.1:3.75;
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
    ti = ti+1; % Time index
    xh = x(t-tau).*h(tau); lxh = length(xh);
    y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
    subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
    axis([tau(1) tau(end) -2.0 2.5]);
    patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
    [zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
    [.8 .8 .8],'edgecolor','none');
    xlabel('\tau'); title('h(\tau) [solid], x(t-\tau) [dashed], h(\tau)x(t-\tau) [gray]');
    c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
    subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
    xlabel('t'); ylabel('y(t) = \int h(\tau)x(t-\tau) d\tau');
    axis([tau(1) tau(end) -1.0 2.0]); grid;
    drawnow;
end
```



## Problem B.2

Convolute

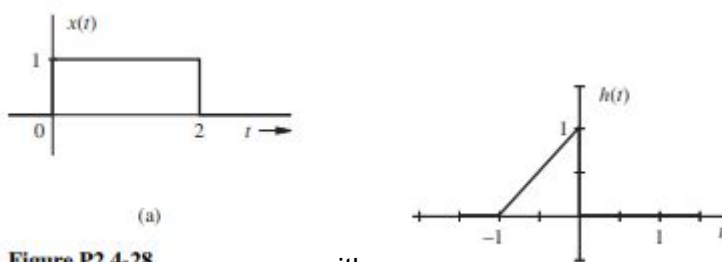


Figure P2.4-28

with

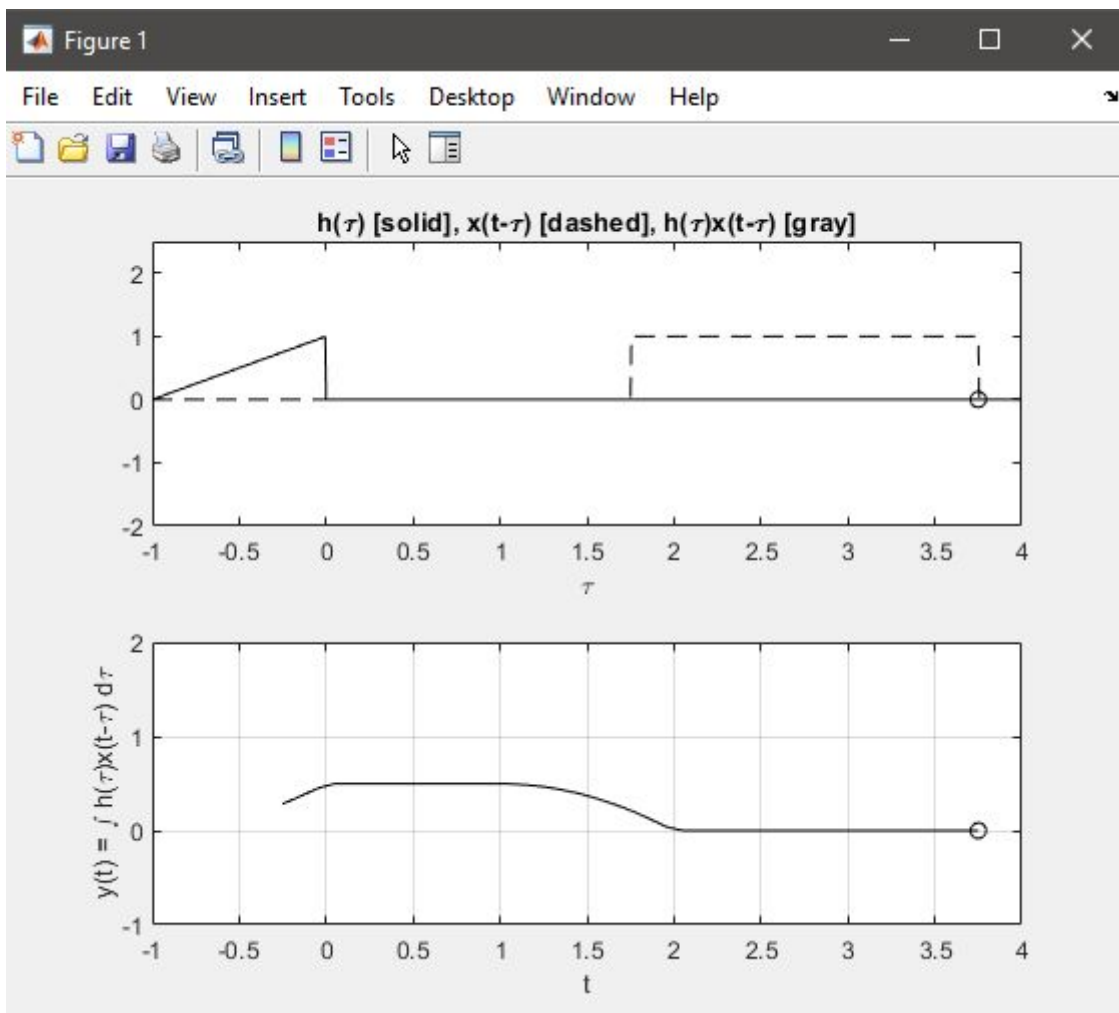
Code:

```
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) 1.0.*(u(t) - u(t-2));
h = @(t) 1.0.*(t+1).*(u(t+1)-u(t));
dtau = 0.005; tau = -1:dtau:4;
ti = 0; tvec = -.25:1:3.75;
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
```

```

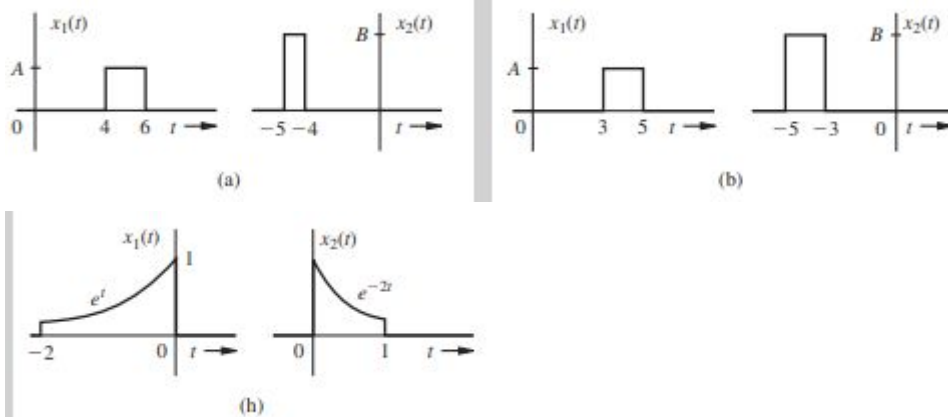
ti = ti+1; % Time index
xh = x(t-tau).*h(tau); lxh = length(xh);
y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
axis([tau(1) tau(end) -2.0 2.5]);
patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
[zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
[.8 .8 .8],'edgecolor','none');
xlabel('\tau'); title('h(\tau) [solid], x(t-\tau) [dashed], h(\tau)x(t-\tau) [gray]');
c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
xlabel('t'); ylabel('y(t) = \int h(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow;
end

```



### Problem B.3

Convolute a, b, h

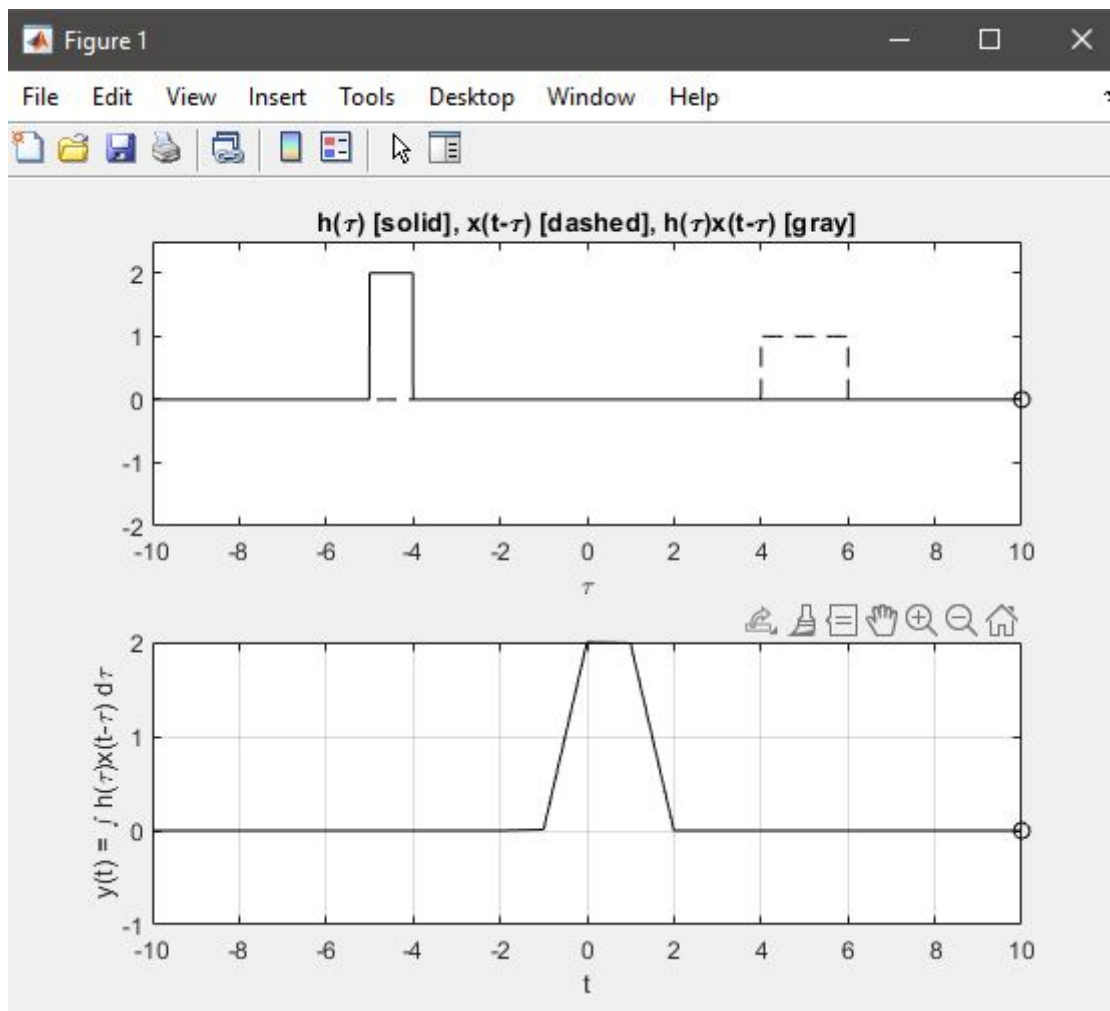


### Convolute A:

Code:

```
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) 1.0.*(u(t-4) - u(t-6));
h = @(t) 2.0.*(u(t+5) - u(t+4));
dtau = 0.005; tau = -10:dtau:10;
ti = 0; tvec = [-10:1:10];
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
    ti = ti+1; % Time index
    xh = x(t-tau).*h(tau); lxh = length(xh);
    y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
    subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
    axis([tau(1) tau(end) -2.0 2.5]);
    patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
    [zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
    [.8 .8 .8],'edgecolor','none');
    xlabel('\tau'); title('h(\tau) [solid], x(t-\tau) [dashed], h(\tau)x(t-\tau) [gray]');
    c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
    subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
    xlabel('t'); ylabel('y(t) = \int h(\tau)x(t-\tau) d\tau');
    axis([tau(1) tau(end) -1.0 2.0]); grid;
    drawnow;
end
```





## Convolute B

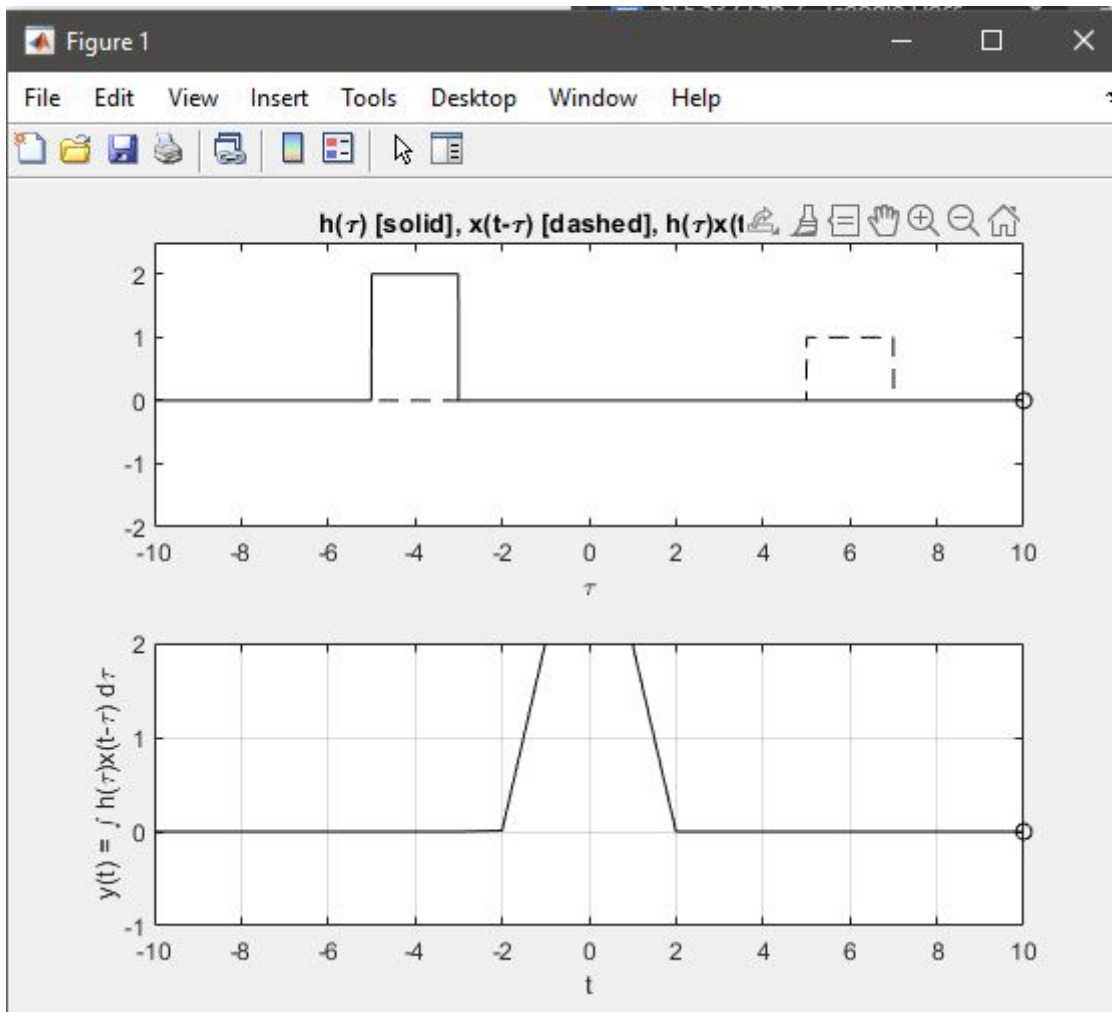
Code:

```
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) 1.0.*(u(t-3) - u(t-5));
h = @(t) 2.0.*(u(t+5) - u(t+3));
dtau = 0.005; tau = -10:dtau:10;
ti = 0; tvec = [-10:1:10];
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
    ti = ti+1; % Time index
    xh = x(t-tau).*h(tau); lxh = length(xh);
    y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
    subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
    axis([tau(1) tau(end) -2.0 2.5]);
    patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
    [zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
    [.8 .8 .8],'edgecolor','none');
    xlabel('\tau'); title('h(\tau) [solid], x(t-\tau) [dashed], h(\tau)x(t-\tau) [gray]');
    c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
    subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
```

```

xlabel('t'); ylabel('y(t) = \int h(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow;
end

```



## Convolute h

Code:

```

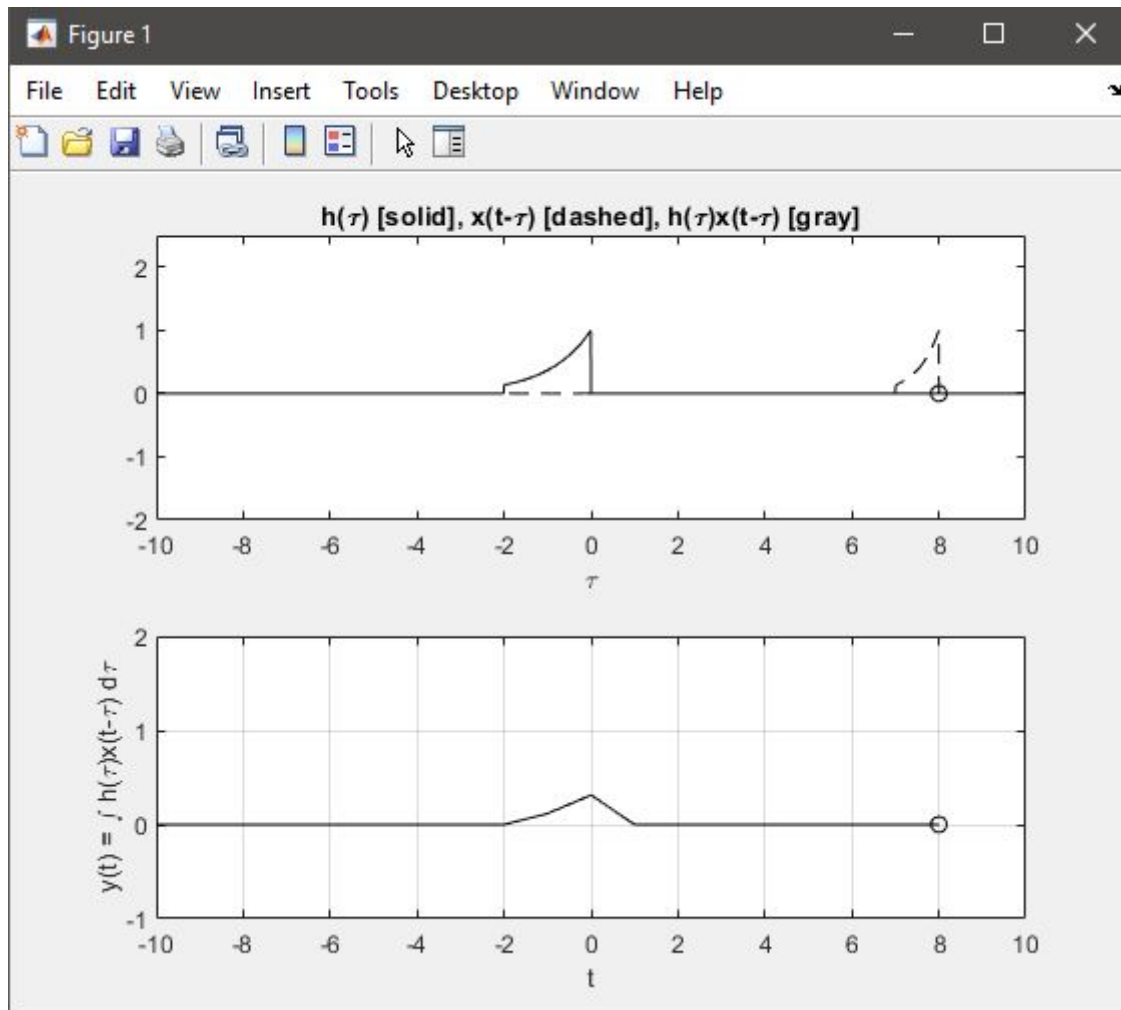
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) exp(-2*t).*(u(t) - u(t-1));
h = @(t) exp(t).*(u(t+2) - u(t));
dtau = 0.005; tau = -10:dtau:10;
ti = 0; tvec = [-10:1:8];
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
    ti = ti+1; % Time index
    xh = x(t-tau).*h(tau); lxh = length(xh);
    y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
    subplot(2,1,1), plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
    axis([tau(1) tau(end) -2.0 2.5]);

```

```

patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
[zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
[.8 .8 .8],'edgecolor','none');
xlabel('\tau'); title('h(\tau) [solid], x(t-\tau) [dashed], h(\tau)x(t-\tau) [gray]');
c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
xlabel('t'); ylabel('y(t) = \int h(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow;
end

```

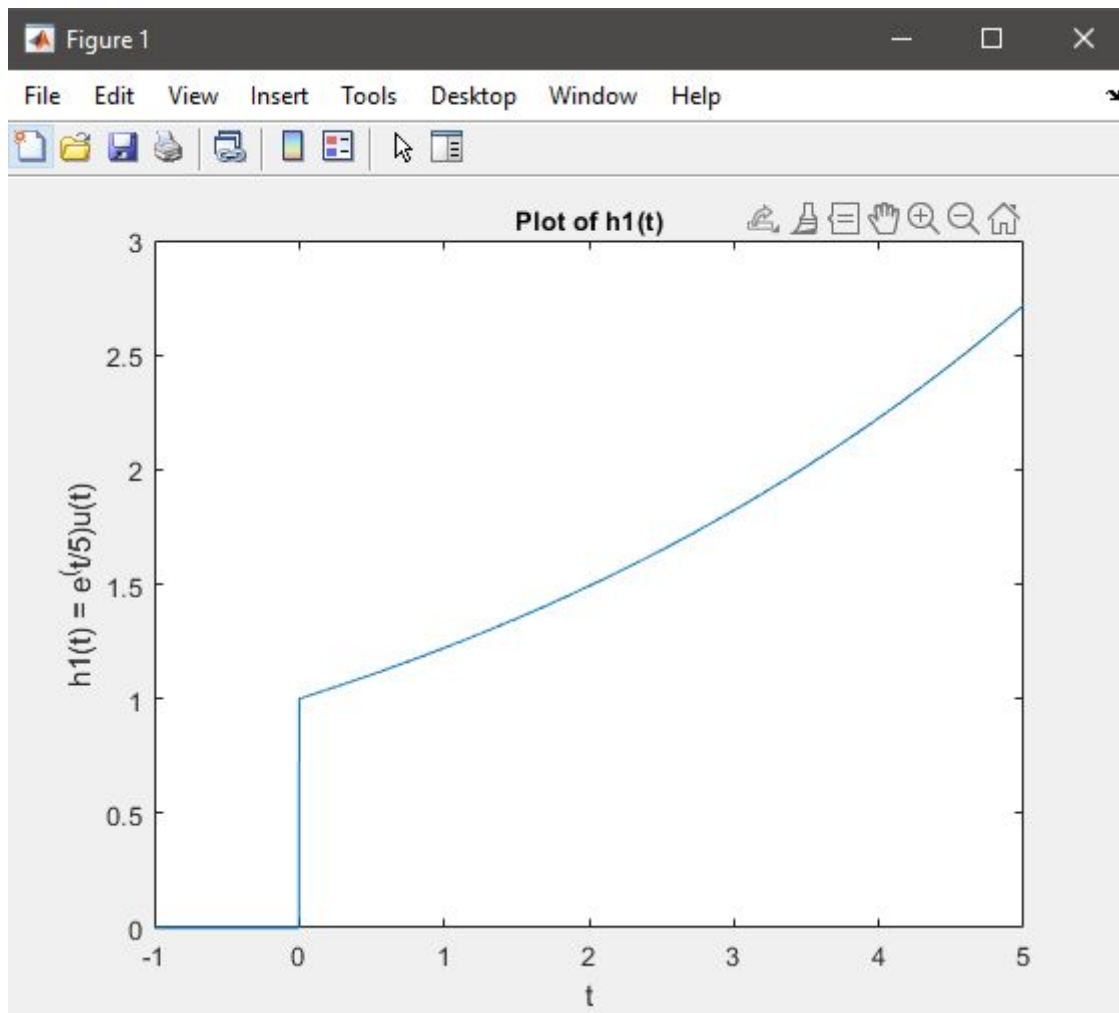


### Problem C.1

### Plot h1(t)

Code:

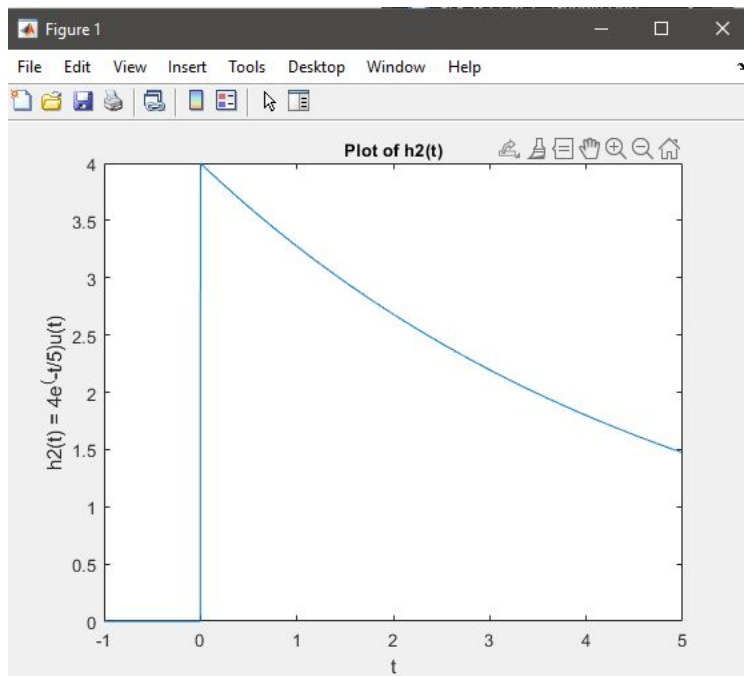
```
u = @(t) 1.0.*(t>=0);  
t = (-1:0.001:5);  
h1 = @(t) exp(t/5).*u(t);  
plot(t,h1(t));  
xlabel('t');  
ylabel('h1(t) = e^(t/5)u(t)');  
title('Plot of h1(t)')
```



### Plot h2(t):

Code:

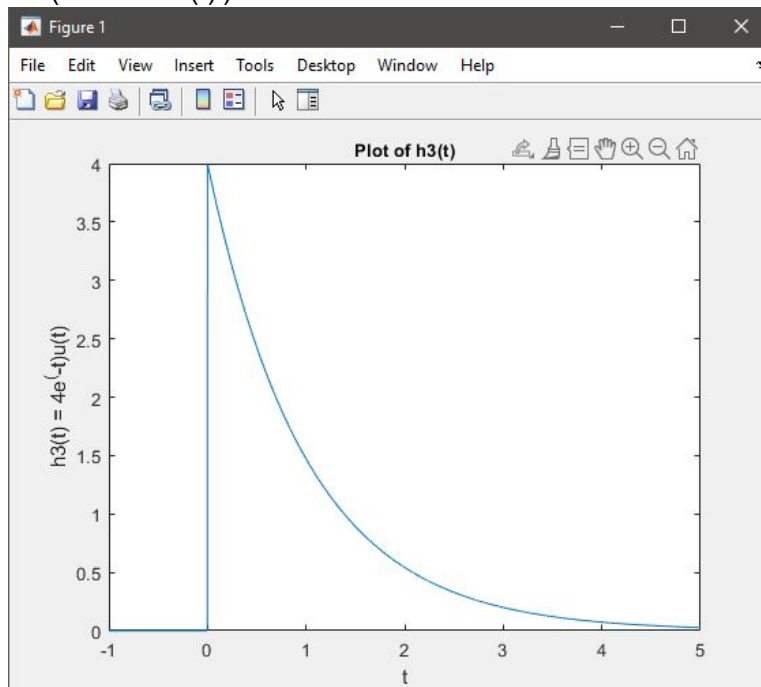
```
u = @(t) 1.0.*(t>=0);  
t = (-1:0.001:5);  
h2 = @(t) 4*exp(-t/5).*u(t);  
plot(t,h2(t));  
xlabel('t');  
ylabel('h2(t) = 4e^(-t/5)u(t)');  
title('Plot of h2(t)')
```



### Plot $h_3(t)$

Code:

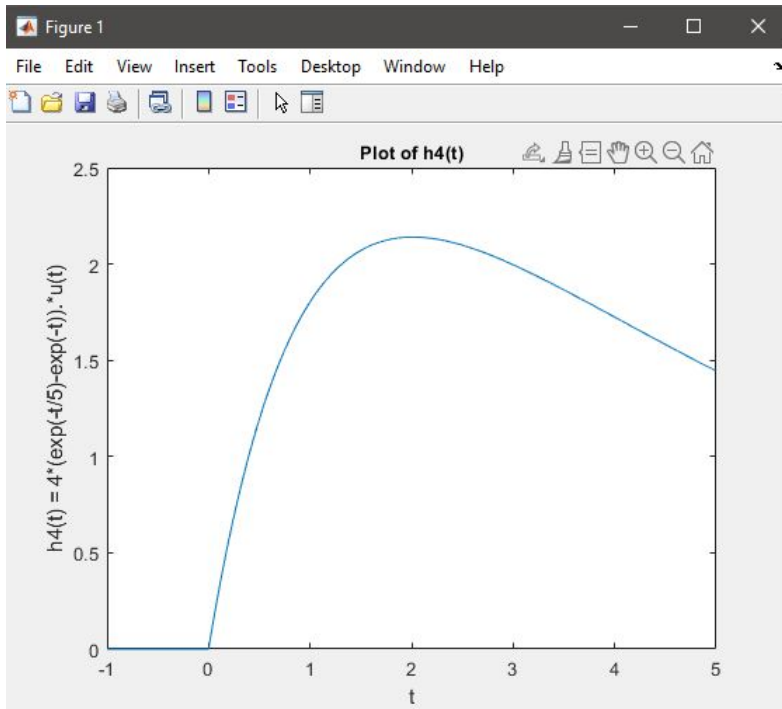
```
u = @(t) 1.0.*(t>=0);
t = (-1:0.001:5);
h3= @(t) 4*exp(-t).*u(t);
plot(t,h3(t));
xlabel('t');
ylabel('h3(t) = 4e^(t)u(t)');
title('Plot of h3(t)')
```



### Plot h4(t)

Code:

```
u = @(t) 1.0.*(t>=0);  
t = (-1:0.001:5);  
h4= @(t) 4*(exp(-t/5)-exp(-t)).*u(t);  
plot(t,h4(t));  
xlabel('t');  
ylabel('h4(t) = 4*(exp(-t/5)-exp(-t)).*u(t)');  
title('Plot of h4(t)')
```



### Problem C.2

Eigenvalues:

$h_1(t) = \frac{1}{5}$

$h_2(t) = -\frac{1}{5}$

$h_3(t) = -1$

$h_4(t) = -\frac{1}{5}$  and  $-1$

### Problem C.3

For h1(t)

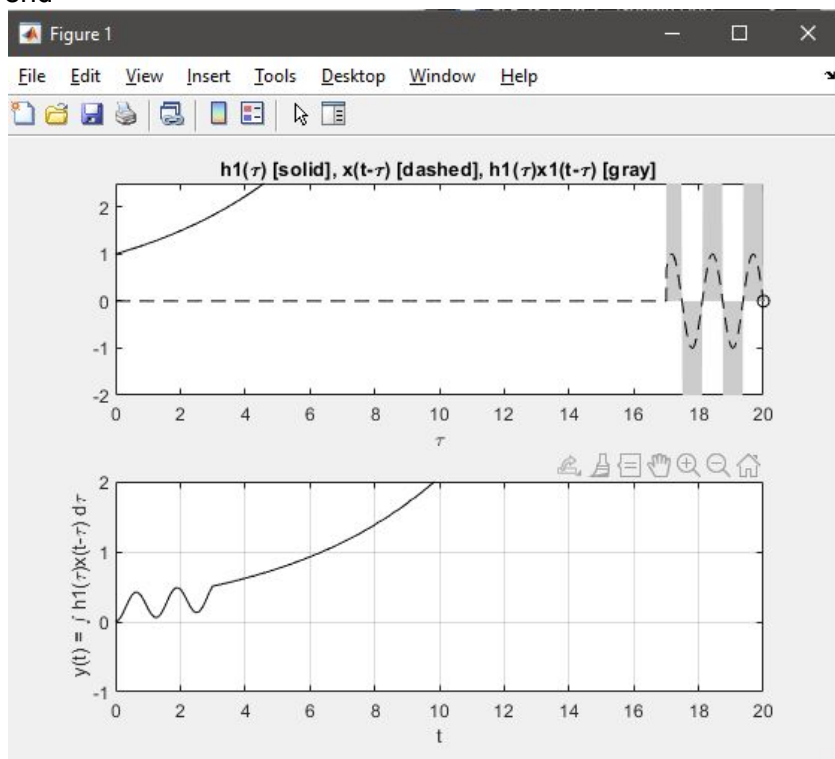
Code:

```
% CH2MP4.m : Chapter 2, MATLAB Program 4  
% Script M-file graphically demonstrates the convolution process.  
figure(1) % Create figure window and make visible on screen  
u = @(t) 1.0.*(t>=0);  
x = @(t) sin(5.*t).*(u(t)-u(t-3));  
h = @(t) exp(t/5).*u(t);  
dttau = 0.005; tau = 0:dttau:20;  
ti = 0; tvec = [0:0.1:20];  
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
```

```

for t = tvec,
ti = ti+1; % Time index
xh = x(t-tau).*h(tau);lxh = length(xh);
y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
axis([tau(1) tau(end) -2.0 2.5]);
patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
[zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
[.8 .8 .8],'edgecolor','none');
xlabel('\tau'); title('h1(\tau) [solid], x(t-\tau) [dashed], h1(\tau)x1(t-\tau) [gray]');
c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
xlabel('t'); ylabel('y(t) = \int h1(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow
end

```



## For h2(t)

Code:

```

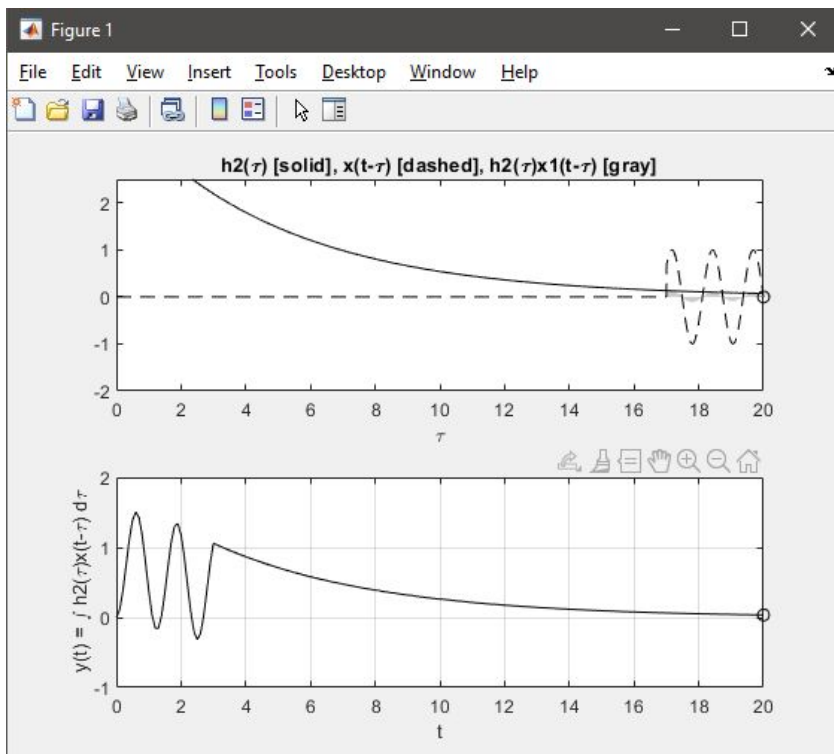
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) sin(5.*t).*(u(t)-u(t-3));
h = @(t) 4*exp(-t/5).*u(t);
dtau = 0.005; tau = 0:dtau:20;
ti = 0; tvec = [0:0.1:20];
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
ti = ti+1; % Time index
xh = x(t-tau).*h(tau);lxh = length(xh);

```

```

y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
axis([tau(1) tau(end) -2.0 2.5]);
patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
[zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
[.8 .8 .8],'edgecolor','none');
xlabel('\tau'); title('h2(\tau) [solid], x(t-\tau) [dashed], h2(\tau)x1(t-\tau) [gray]');
c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
xlabel('t'); ylabel('y(t) = \int h2(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow
end

```



### For h3(t)

Code:

```

% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) sin(5.*t).*(u(t)-u(t-3));
h = @(t) 4*exp(-t).*u(t);
dtau = 0.005; tau = 0:dtau:20;
ti = 0; tvec = [0:0.1:20];
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
    ti = ti+1; % Time index
    xh = x(t-tau).*h(tau);lxh = length(xh);
    y(ti) = sum(xh.*dtau); % Trapezoidal approximation of convolution integral
    subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
    axis([tau(1) tau(end) -2.0 2.5]);

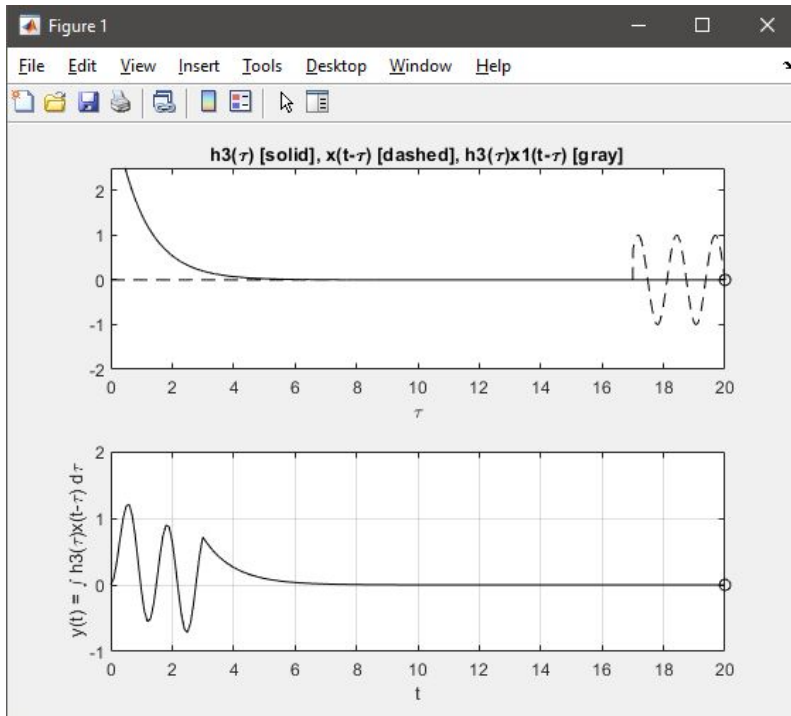
```



```

patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
[zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
[.8 .8 .8],'edgecolor','none');
xlabel('\tau'); title('h3(\tau) [solid], x(t-\tau) [dashed], h3(\tau)x1(t-\tau) [gray]');
c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
xlabel('t'); ylabel('y(t) = \int h3(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow
end

```



### For h4(t)

Code:

```

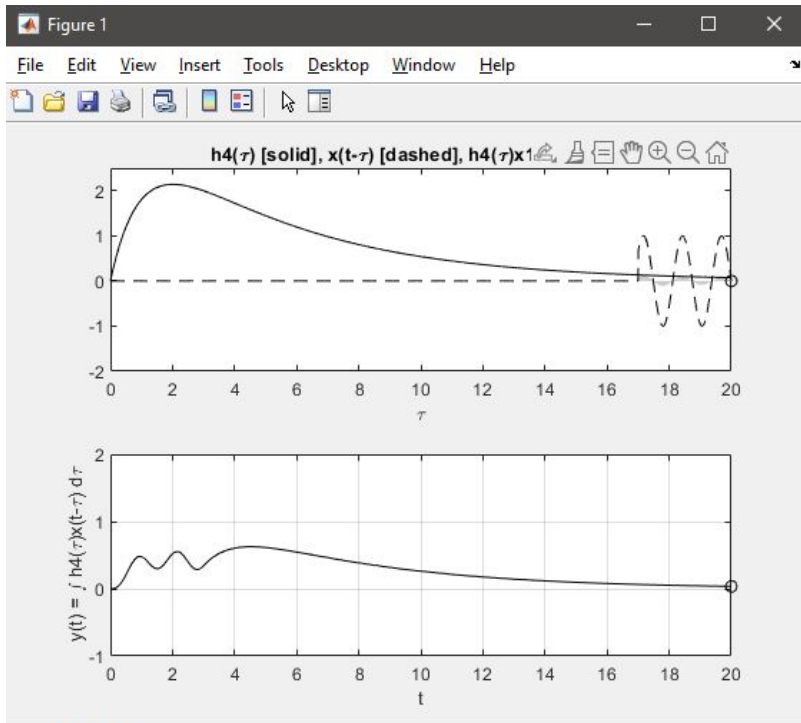
% CH2MP4.m : Chapter 2, MATLAB Program 4
% Script M-file graphically demonstrates the convolution process.
figure(1) % Create figure window and make visible on screen
u = @(t) 1.0.*(t>=0);
x = @(t) sin(5.*t).*(u(t)-u(t-3));
h = @(t) 4*(exp(-t/5)-exp(-t)).*u(t);
dttau = 0.005; tau = 0:dttau:20;
ti = 0; tvec = [0:0.1:20];
y = NaN*zeros(1,length(tvec)); % Pre-allocate memory
for t = tvec,
    ti = ti+1; % Time index
    xh = x(t-tau).*h(tau);lxh = length(xh);
    y(ti) = sum(xh.*dttau); % Trapezoidal approximation of convolution integral
    subplot(2,1,1),plot(tau,h(tau),'k-',tau,x(t-tau),'k--',t,0,'ok');
    axis([tau(1) tau(end) -2.0 2.5]);
    patch([tau(1:end-1);tau(1:end-1);tau(2:end);tau(2:end)],...
[zeros(1,lxh-1);xh(1:end-1);xh(2:end);zeros(1,lxh-1)],...
[.8 .8 .8],'edgecolor','none');

```

```

xlabel('\tau'); title('h4(\tau) [solid], x(t-\tau) [dashed], h4(\tau)x1(t-\tau) [gray]');
c = get(gca,'children'); set(gca,'children',[c(2);c(3);c(4);c(1)]);
subplot(2,1,2),plot(tvec,y,'k',tvec(ti),y(ti),'ok');
xlabel('t'); ylabel('y(t) = \int h4(\tau)x(t-\tau) d\tau');
axis([tau(1) tau(end) -1.0 2.0]); grid;
drawnow
end

```



The relationship between these three systems is that  $y_4(t)$  is an interconnected parallel system of  $y_2(t)$  and the negative of  $y_3(t)$ . Thus  $y_4(t) = y_2(t) + (-y_3(t))$

### Problem D.1

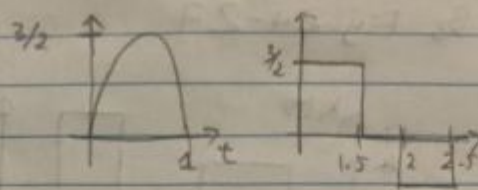
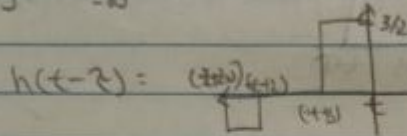
B.1

D1 B2

$$x(t) = 1.5 \sin(\pi t) [u(t) - u(t-1)]$$

$$h(t) = 1.5 [u(t) - u(t-1)] - u(t-2) + u(t-2.5)$$

$$y(t) = \int_{-\infty}^{\infty} x(\tau) h(t-\tau) d\tau$$



(R1)  $t < 0 \therefore y(t) = 0$

(R2)  $0 \leq t \leq 1$   $y(t) = \int_0^t \frac{3}{2} (\frac{2}{3} \sin(\pi \tau)) d\tau = -\frac{9}{4} \pi \cos(\pi \tau) \Big|_0^t = -\frac{9}{4\pi} \cos(\pi t) + \frac{9}{4\pi}$

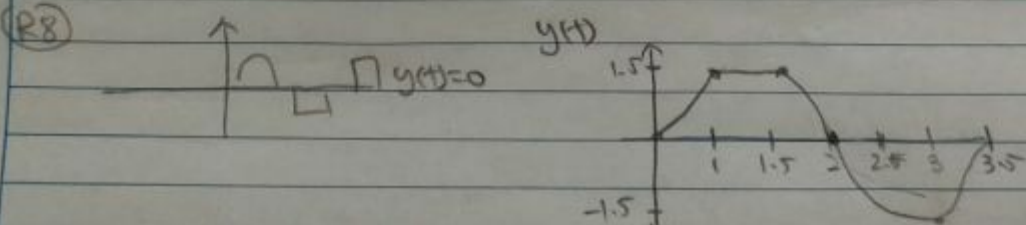
(R3)  $1 \leq t \leq 3/2$   $y(t) = \int_0^1 \frac{3}{2} d\tau = \frac{3}{2}$

(R4)  $3/2 \leq t \leq 2$   $y(t) = \int_{t-1/2}^1 \frac{3}{2} (\frac{2}{3} \sin(\pi \tau)) d\tau = -\frac{9}{4\pi} (\cos(\pi \tau)) \Big|_{t+3/2}^1$   
 $= \frac{9}{4\pi} - \frac{9}{4\pi} \cos(\pi(t+3/2))$

(R5)  $2 \leq t \leq 2.5$   $y(t) = \int_0^{t-2} -\frac{3}{2} \sin(\pi \tau) d\tau$   
 $= \frac{3}{2\pi} (\cos(\pi \tau)) \Big|_0^{t-2} = \frac{3}{2\pi} (\cos(\pi(t-2)) - 1)$

(R6)  $2.5 \leq t \leq 3$   $y(t) = \int_{t-2.5}^{t-2} -\frac{3}{2} \sin(\pi \tau) d\tau = \frac{3}{2\pi} (\cos(\pi \tau)) \Big|_{t-2.5}^{t-2}$   
 $= \frac{3}{2\pi} (\cos(\pi(t-2)) - \cos(\pi(t-2.5)))$

(R7)  $3 \leq t \leq 3.5$   $y(t) = \int_{t-2.5}^1 -\frac{3}{2} \sin(\pi \tau) d\tau = \frac{3}{2\pi} (\cos(\pi \tau)) \Big|_{t-2.5}^1$   
 $= -\frac{3}{2\pi} - \frac{3}{2\pi} \cos(\pi(t-2.5))$

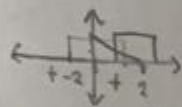


Doing B2

$$x(t) = u(t) - u(t-2)$$

$$h(t) = \left(1 - \frac{t}{2}\right) [u(t) - u(t-2)]$$

Region 2



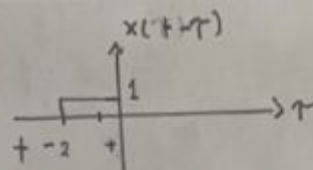
$$0 \leq t-2 \leq 2$$

$$2 \leq t \leq 4$$

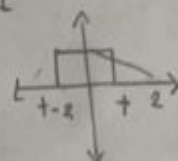
$$y(t) = \int_{-2}^2 \left(1 - \frac{\tau}{2}\right) d\tau = \left[\tau - \frac{\tau^2}{4}\right]_{-2}^2$$

$$= (2-1) - \left(-1 - \frac{4}{4}\right)$$

$$= 1 - \left(-1 + \frac{4-2}{4}\right)$$



Region 1



$$0 \leq t \leq 2$$

$$\int_0^2 \left(1 - \frac{\tau}{2}\right) d\tau = \left[\tau - \frac{\tau^2}{4}\right]_0^2$$

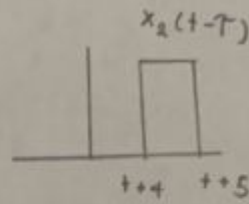
$$= 2 - \frac{4}{4}$$

B.3a

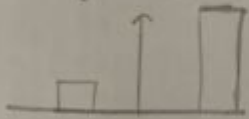
B.3a

$$x_1(t) = A[u(t-4) - u(t-6)]$$

$$x_2(t) = B[u(t+5) - u(t+4)]$$

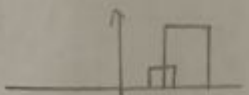


Region 1



No overlap for  $t+5 \leq 4$   
 $t \leq -1$

R2



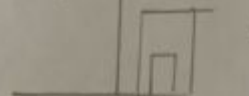
$$4 \leq t+5 \leq 5 \quad -1 \leq t \leq 0$$

$$y(t) = \int_4^{t+5} AB d\tau$$

$$= AB\tau \Big|_4^{t+5}$$

$$= AB(t+1)$$

R3

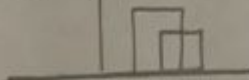


$$0 \leq t \leq 1$$

$$y(t) = \int_0^1 AB d\tau$$

$$= AB$$

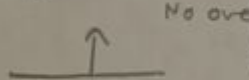
R4



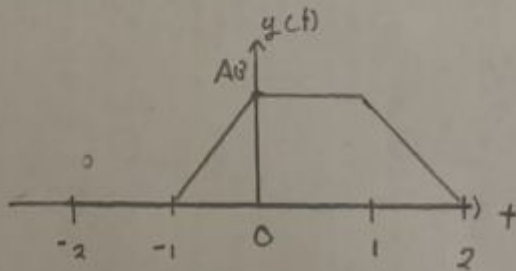
$$1 \leq t \leq 2$$

$$y(t) = \int_{t+4}^6 AB d\tau = 6 - (t+4)AB = (2-t)AB$$

R5

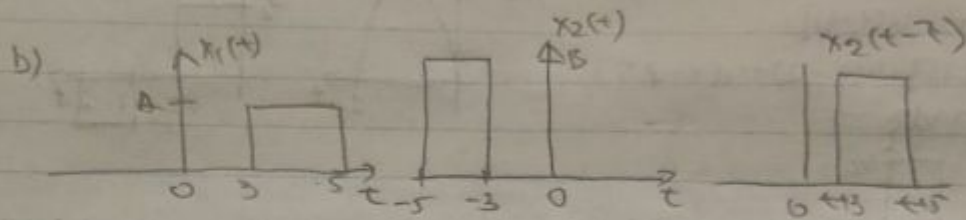


No overlap for  $t+5 > 6$   
 $t > 1$

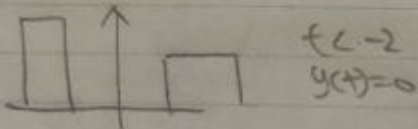


B.3b

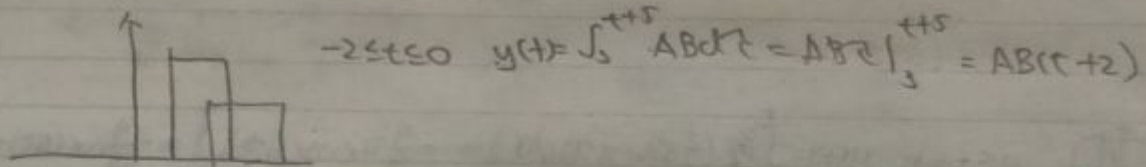
A B<sub>3</sub> Fig. 2.4-2.7



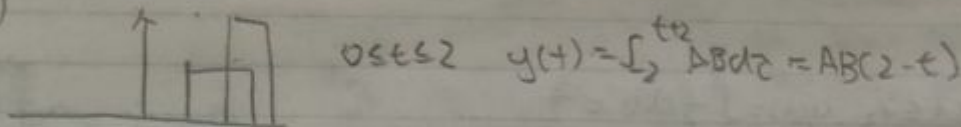
(R<sub>1</sub>)



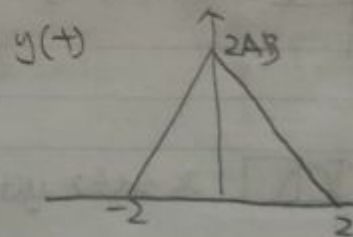
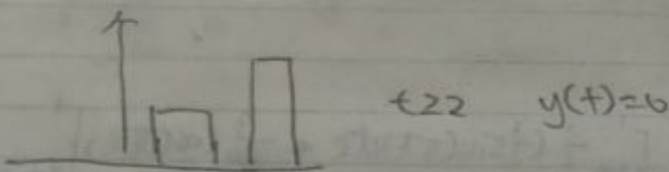
(R<sub>2</sub>)

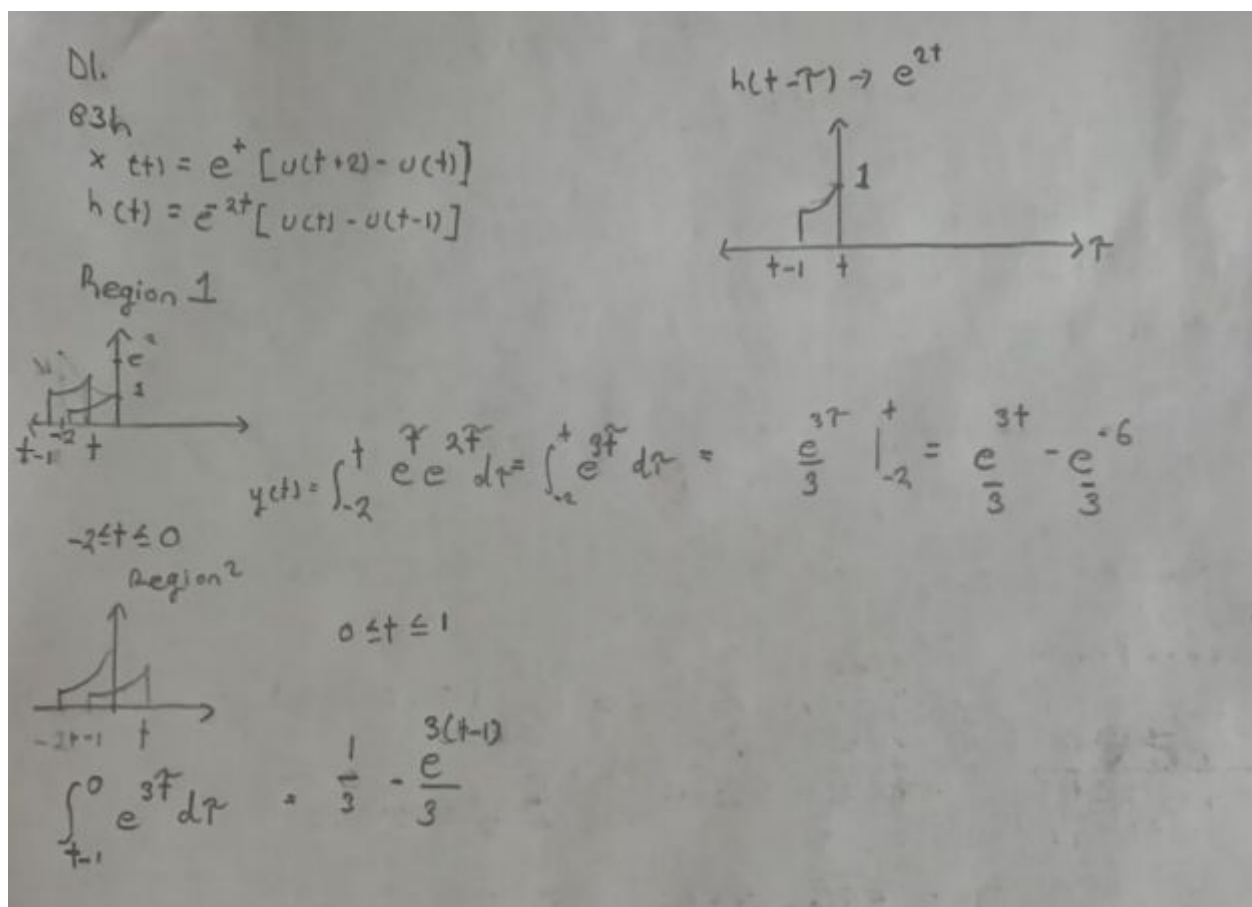


(R<sub>3</sub>)



(R<sub>4</sub>)





### Problem D.2

The sum of the lengths of each function is equal to the length of the convolution of two functions