

## Practice FRQ

1. This question involves reasoning about a simulation of a frog hopping in a straight line. The frog attempts to hop to a goal within a specified number of hops. The simulation is encapsulated in the following `FrogSimulation` class. You will write two of the methods in this class.

```
public class FrogSimulation
{
    /** Distance, in inches, from the starting position to the goal. */
    private int goalDistance;

    /** Maximum number of hops allowed to reach the goal. */
    private int maxHops;

    /** Constructs a FrogSimulation where dist is the distance, in inches, from the starting
     * position to the goal, and numHops is the maximum number of hops allowed to reach the goal.
     * Precondition: dist > 0; numHops > 0
     */
    public FrogSimulation(int dist, int numHops)
    {
        goalDistance = dist;
        maxHops = numHops;
    }

    /** Returns an integer representing the distance, in inches, to be moved when the frog hops.
     */
    private int hopDistance()
    { /* implementation not shown */ }

    /** Simulates a frog attempting to reach the goal as described in part (a).
     * Returns true if the frog successfully reached or passed the goal during the simulation;
     * false otherwise.
     */
    public boolean simulate()
    { /* to be implemented in part (a) */ }

    /** Runs num simulations and returns the proportion of simulations in which the frog
     * successfully reached or passed the goal.
     * Precondition: num > 0
     */
    public double runSimulations(int num)
    { /* to be implemented in part (b) */ }
}
```

- (a) Write the `simulate` method, which simulates the frog attempting to hop in a straight line to a goal from the frog's starting position of 0 within a maximum number of hops. The method returns `true` if the frog successfully reached the goal within the maximum number of hops; otherwise, the method returns `false`.

The `FrogSimulation` class provides a method called `hopDistance` that returns an integer representing the distance (positive or negative) to be moved when the frog hops. A positive distance represents a move toward the goal. A negative distance represents a move away from the goal. The returned distance may vary from call to call. Each time the frog hops, its position is adjusted by the value returned by a call to the `hopDistance` method.

The frog hops until one of the following conditions becomes true:

- The frog has reached or passed the goal.
- The frog has reached a negative position.
- The frog has taken the maximum number of hops without reaching the goal.

The following example shows a declaration of a `FrogSimulation` object for which the goal distance is 24 inches and the maximum number of hops is 5. The table shows some possible outcomes of calling the `simulate` method.

```
FrogSimulation sim = new FrogSimulation(24, 5);
```

	Values returned by <code>hopDistance()</code>	Final position of frog	Return value of <code>sim.simulate()</code>
Example 1	5, 7, -2, 8, 6	24	true
Example 2	6, 7, 6, 6	25	true
Example 3	6, -6, 31	31	true
Example 4	4, 2, -8	-2	false
Example 5	5, 4, 2, 4, 3	18	false

Class information for this question

```
public class FrogSimulation

private int goalDistance
private int maxHops

private int hopDistance()
public boolean simulate()
public double runSimulations(int num)
```

Complete method `simulate` below. You must use `hopDistance` appropriately to receive full credit.

```
/** Simulates a frog attempting to reach the goal as described in part (a).
 * Returns true if the frog successfully reached or passed the goal during the simulation;
 *     false otherwise.
 */
public boolean simulate()
```

- (b) Write the `runSimulations` method, which performs a given number of simulations and returns the proportion of simulations in which the frog successfully reached or passed the goal. For example, if the parameter passed to `runSimulations` is 400, and 100 of the 400 `simulate` method calls returned `true`, then the `runSimulations` method should return 0.25.

Complete method `runSimulations` below. Assume that `simulate` works as specified, regardless of what you wrote in part (a). You must use `simulate` appropriately to receive full credit.

```
/** Runs num simulations and returns the proportion of simulations in which the frog
 * successfully reached or passed the goal.
 * Precondition: num > 0
 */
public double runSimulations(int num)
```

4. This question involves reasoning about arrays of integers. You will write two static methods, both of which are in a class named `ArrayTester`.

```
public class ArrayTester
{
    /** Returns an array containing the elements of column c of arr2D in the same order as
     * they appear in arr2D.
     * Precondition: c is a valid column index in arr2D.
     * Postcondition: arr2D is unchanged.
     */
    public static int[] getColumn(int[][] arr2D, int c)
    { /* to be implemented in part (a) */ }

    /** Returns true if and only if every value in arr1 appears in arr2.
     * Precondition: arr1 and arr2 have the same length.
     * Postcondition: arr1 and arr2 are unchanged.
     */
    public static boolean hasAllValues(int[] arr1, int[] arr2)
    { /* implementation not shown */ }

    /** Returns true if arr contains any duplicate values;
     * false otherwise.
     */
    public static boolean containsDuplicates(int[] arr)
    { /* implementation not shown */ }

    /** Returns true if square is a Latin square as described in part (b);
     * false otherwise.
     * Precondition: square has an equal number of rows and columns.
     * square has at least one row.
     */
    public static boolean isLatin(int[][] square)
    { /* to be implemented in part (b) */ }
}
```

- (a) Write a static method `getColumn`, which returns a one-dimensional array containing the elements of a single column in a two-dimensional array. The elements in the returned array should be in the same order as they appear in the given column. The notation `arr2D[r][c]` represents the array element at row `r` and column `c`.

The following code segment initializes an array and calls the `getColumn` method.

```
int[] [] arr2D = { { 0, 1, 2 },
                   { 3, 4, 5 },
                   { 6, 7, 8 },
                   { 9, 5, 3 } };

int[] result = ArrayTester.getColumn(arr2D, 1);
```

When the code segment has completed execution, the variable `result` will have the following contents.

```
result: {1, 4, 7, 5}
```

Complete method `getColumn` below.

```
/** Returns an array containing the elements of column c of arr2D in the same order as they
 * appear in arr2D.
 * Precondition: c is a valid column index in arr2D.
 * Postcondition: arr2D is unchanged.
 */
public static int[] getColumn(int[] [] arr2D, int c)
```

- (b) Write the static method `isLatin`, which returns `true` if a given two-dimensional square array is a *Latin square*, and otherwise, returns `false`.

A two-dimensional square array of integers is a Latin square if the following conditions are true.

- The first row has no duplicate values.
- All values in the first row of the square appear in each row of the square.
- All values in the first row of the square appear in each column of the square.

#### Examples of Latin Squares

1	2	3
2	3	1
3	1	2

10	30	20	0
0	20	30	10
30	0	10	20
20	10	0	30

#### Examples that are NOT Latin Squares

1	2	1
2	1	1
1	1	2

Not a Latin square  
because the first row  
contains duplicate  
values

1	2	3
3	1	2
7	8	9

Not a Latin square  
because the elements of  
the first row do not all  
appear in the third row

1	2
1	2

Not a Latin square  
because the elements of  
the first row do not all  
appear in either column

The `ArrayTester` class provides two helper methods: `containsDuplicates` and `hasAllValues`. The method `containsDuplicates` returns `true` if the given one-dimensional array `arr` contains any duplicate values and `false` otherwise. The method `hasAllValues` returns `true` if and only if every value in `arr1` appears in `arr2`. You do not need to write the code for these methods.

Class information for this question

```
public class ArrayTester
```

```
public static int[] getColumn(int[][] arr2D, int c)  
public static boolean hasAllValues(int[] arr1, int[] arr2)  
public static boolean containsDuplicates(int[] arr)  
public static boolean isLatin(int[][] square)
```

Complete method `isLatin` below. Assume that `getColumn` works as specified, regardless of what you wrote in part (a). You must use `getColumn`, `hasAllValues`, and `containsDuplicates` appropriately to receive full credit.

```
/** Returns true if square is a Latin square as described in part (b);
 *     false otherwise.
 * Precondition: square has an equal number of rows and columns.
 *     square has at least one row.
 */
public static boolean isLatin(int[] [] square)
```