

COSC 76, Fall 2020, PA-4, Edmund Aduse Poku

Q1b.:

a) Description

GENERIC CSP CLASS AND SOLUTION CLASS

I implemented a generic CSP class that has 4 instance attributes: variables, domains, constraints and neighbors. It also has 3 methods: `arc_is_consistent` (determines if a given arc is consistent or satisfies the problem constraints), `ass_is_consistent` (checks to see if, after an assignment, the assignment is consistent). The solution class takes the solution to a given csp problem and represents it in succinct, human readable form using the representation methods described in the corresponding specific CSP class.

BACKTRACKING SEARCH, HEURISTIC AND INFERENCES FUNCTIONS

I implemented the backtracking search method in its own file called `search.py`. The backtracking search method has the ability to switch between using none, some or all of the heuristic functions: "mrv", "lcv", and `degree_heuristics`. The heuristic functions have been implemented in their own file called `heuristics.py`. It also has the ability to switch between none or one of the implemented inferences functions: `forward_checking` and "mac". All the heuristic and inferences methods function as described in the textbook.

MAP COLORING PROBLEM

I extended the generic CSP class to implement a specific class for the Map Coloring Problem. The class has a `convert_to_csp` method that converts the human readable Map Coloring Problem into a generic csp that can be solved by the CSP class. The class `convert_to_readable` also has a method that reverts the solution into a human readable form.

CIRCUIT LAYOUT PROBLEM

Similar to what I did for the Map Coloring Problem, I extended the generic CSP class defined in the `csp.py` file and added methods to convert a given circuit problem to a generic csp. There is also a method to convert the solution back to a human readable form (`circuit`).

b) Yes, all the algorithms implemented work (perfectly). Running the test cases for the Map Coloring Problem and the Circuit Board Problem gives the following results, just as expected:

MAP COLORING PROBLEM

MapColoringCSP solved by backtracking in runtime: 0.000053 seconds using the following: no heuristics and no inference the solution suggests that the colors be assigned in the manner: {'WA': 'g', 'NT': 'b', 'Q': 'g', 'NSW': 'b', 'SA': 'r', 'V': 'g', 'T': 'g'}

MapColoringCSP solved by backtracking in runtime: 0.000742 seconds using the following: 'MRV' heuristics and no inference the solution suggests that the colors be assigned in the manner: {'WA': 'g', 'NT': 'b', 'Q': 'g', 'NSW': 'b', 'SA': 'r', 'V': 'g', 'T': 'g'}

MapColoringCSP solved by backtracking in runtime: 0.000687 seconds using the following: 'MRV', 'LCV' heuristics and no inference the solution suggests that the

colors be assigned in the manner: {'WA': 'g', 'NT': 'b', 'Q': 'g', 'NSW': 'b', 'SA': 'r', 'V': 'g', 'T': 'g'}

MapColoringCSP solved by backtracking in runtime: 0.000159 seconds using the following: degree_heuristics, 'MRV', 'LCV' heuristics and no inference the solution suggests that the colors be assigned in the manner: {'SA': 'g', 'WA': 'b', 'NT': 'r', 'Q': 'b', 'NSW': 'r', 'V': 'b', 'T': 'g'}

MapColoringCSP solved by backtracking in runtime: 0.000202 seconds using the following: degree_heuristics, 'MRV', 'LCV' heuristics and 'forward checking' inference the solution suggests that the colors be assigned in the manner: {'SA': 'g', 'WA': 'b', 'NT': 'r', 'Q': 'b', 'NSW': 'r', 'V': 'b', 'T': 'g'}

MapColoringCSP solved by backtracking in runtime: 0.000056 seconds using the following: degree_heuristics, 'MRV', 'LCV' heuristics and 'mac' inference the solution suggests that the colors be assigned in the manner: {'SA': 'g', 'NT': 'r', 'NSW': 'r', 'WA': 'b', 'Q': 'b', 'V': 'b', 'T': 'g'}

CIRCUIT LAYOUT PROBLEM

CircuitBoardCSP solved by backtracking in runtime: 0.000104 seconds using the following: no heuristics and no inference the components should be laid out as:

bbbbbb. aa.gg.. aa.gg.. aa.... aa.eeee aa.eeee

using the coordinates: {'a': (0, 0), 'b': (0, 6), 'e': (3, 0), 'g': (3, 3)}

CircuitBoardCSP solved by backtracking in runtime: 0.000094 seconds using the following: 'MRV' heuristics and no inference the components should be laid out as:

bbbbbb. aa.gg.. aa.gg.. aa.... aa.eeee aa.eeee

using the coordinates: {'a': (0, 0), 'b': (0, 6), 'e': (3, 0), 'g': (3, 3)}

CircuitBoardCSP solved by backtracking in runtime: 0.000389 seconds using the following: 'MRV', 'LCV' heuristics and 'mac' inference the components should be laid out as:

bbbbbb. aa.eeee aa.eeee aa.... aa..gg. aa..gg.

using the coordinates: {'a': (0, 0), 'b': (0, 6), 'e': (3, 3), 'g': (4, 0)}

CircuitBoardCSP solved by backtracking in runtime: 0.000222 seconds using the following: degree_heuristics, 'MRV', 'LCV' heuristics and 'mac' inference the components should be laid out as:

bbbbbb. aa.eeee aa.eeee aa.... aa..gg. aa..gg.

using the coordinates: {'a': (0, 0), 'b': (0, 6), 'e': (3, 3), 'g': (4, 0)}

CircuitBoardCSP solved by backtracking in runtime: 0.000356 seconds using the following: degree_heuristics, 'MRV', 'LCV' heuristics and 'forward checking' inference the components should be laid out as:

bbbbbb. eeee.aa eeee.aaaa ..gg.aa ..gg.aa

using the coordinates: {'a': (5, 0), 'b': (0, 6), 'e': (0, 3), 'g': (2, 0)}

CircuitBoardCSP solved by backtracking in runtime: 0.000423 seconds using the following: degree_heuristics, 'MRV', 'LCV' heuristics and 'mac' inference the components should be laid out as:

bbbbbb. eeee.aa eeee.aaaa ..gg.aa ..gg.aa

using the coordinates: {'a': (5, 0), 'b': (0, 6), 'e': (0, 3), 'g': (2, 0)}

c) Let (x, y) be an arbitrary location of a variable X (ie the lower left corner of a component) on the board. Then the domain of X corresponding to a component of width w and height h , on a circuit board of width n and height m is given by all (x, y) locations on the board such that $x+w \leq n$ and $y+h \leq m$.

The code converts an arbitrary location (x, y) on a board of size n by m to an integer location by the formula: $y*n + x$. The formula works in the given manner: given that the width of the board is n , there are n spots (indices) on a given row. Since the location (x, y) has $y+1$ rows, there must be at least $y*n$ spots (indices) to get to this location. On the row that this location is on, x indicates the column number where the location is, implying that we have to add x many spots to $y*n$ to get the number of spots of how many rows up on the board has been covered.