# **Digital Image & Video Processing**

Lecture 9 (cont)
Image Segmentation





## 9.2. Method

### 9.2.3. HAC (Hierarchical Agglomerative Clustering)

Suppose that

 $X = \{x_i, i = 1..N\}$  is the set of l dimensional feature vectors should be clustered.

 $R = \{C_j, j = 1..M\}, C_j$  is cluster of feature vectors, M is the number of clusters.

#### 9.2.3. HAC



#### \*Image Segmentation

Generalized Agglomerative Scheme

Step 1. Suppose 
$$R_0 = \{C_i = \{x_i\}, i = 1..N\}$$
, N is the number of feature vectors.

*Step* 2. 
$$t = 0$$
,

*Step* 4. 
$$t = t + 1$$

Step 5. Select cluster pair  $(C_i, C_j)$  in  $R_{t-1}$  such that

$$d_N(C_i, C_j) = \min_{r,s=1..N; r\neq s} d_N(C_r, C_s), d_Nis \ dissimilarity \ distance \ between the \ clusters.$$

Step 6. Suppose  $C_q$  is the cluster created by merging cluster pair  $(C_i, C_j)$ ,

$$C_q = C_i \cup C_j$$

Create new cluster partition  $R_t = (R_{t-1} - \{C_i, C_j\}) \cup \{C_q\}$ 

Step 7. Until 
$$t = N-1$$



#### \*Image Segmentation

Tree Generative Scheme (inherited from Generalized Agglomerative Scheme)

Step 1. Suppose  $T_0 = \{n_i = \{x_i\}, i = 1..N\}$ , N is the number of feature vectors.

*Step* 2. t = 0,

Step 3. Re peat

*Step* 4. t = t + 1

Step 5. Select node pair  $(n_i, n_j)$  in  $T_{t-1}$  such that

 $d_N(n_i, n_j) = \min_{r,s=1..N; r\neq s} d_N(n_r, n_s), d_Nis dissimilarity distance between the nodes.$ 

Step 6. Suppose  $n_q$  is the node created by merging node pair  $(n_i, n_j)$ ,  $n_q = n_i \cup n_j$ ,

Create new tree  $T_t = (T_{t-1} - \{n_i, n_j\}) \cup \{n_q\}$ 

Step 7. Until t = N-1



#### \*Image Segmentation

Cluster Generative Scheme

Step 1. Reduce hierarchical tree based on DM between parent node and child node

Step 2. The leafnodes with the same parent node will be put to one cluster.

The criteria to remove the nodes based on DM between the child nodes and their parent.

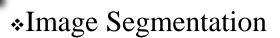
Suppose a,b are two nodes (not be leaf modes),

$$d_{\min}(a,b) = \min \{d(l_a, l_b)\}$$

$$d_{\max}(a,b) = \max\{d(l_a,l_b)\}$$

 $l_a, l_b$  are the leaf nodes.

#### 9.2.3. HAC



Cluster Generative Scheme

During the hierarchical tree generating process, we have:

*Node*  $p_l$  *is created and linked two values:* 

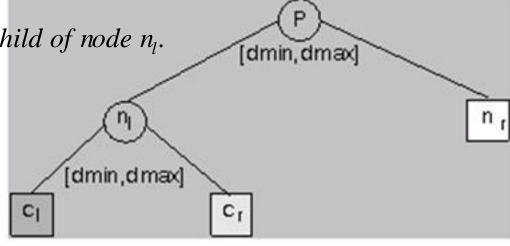
$$d_{\min}(n_l, n_r), d_{\max}(n_l, n_r),$$

 $n_l, n_r$  are the left child and right child of node  $p_l$ .

Node  $n_l$  is created and linked two values:

$$d_{\min}(c_l, c_r), d_{\max}(c_l, c_r),$$

 $c_1, c_r$  are the left child and right child of node  $n_l$ .



#### 9.2.3. HAC



#### Image Segmentation

Suppose node n is the child of node p, consider the following quantities

$$\Delta_{\min}(p,n) = \frac{d_{\min}^p - d_{\min}^n}{d_{\min}^n}$$
 The relative difference of d<sub>min</sub> at node n and p

$$\Delta_{\max}(p,n) = \frac{d_{\max}^p - d_{\max}^n}{d_{\max}^n}$$

 $\Delta_{\max}(p,n) = \frac{d_{\max}^p - d_{\max}^n}{d^n}$  The relative difference of  $d_{\max}$  at node n and p

Node n will be removed if

$$\Delta_{\min} < \varepsilon \ \ \mathrm{Va} \ \left| \Delta_{\max} \right| < \varepsilon$$

After node n is removed, the child of node n is node c is not lost but it is linked to node p.