tobacco_consumption

April 10, 2022

1 Tobacco Consumption

Tobacco consumption is one of the primary causes of lung cancer in the World. Tobacco in the form of cigars and cigarettes is usually available to adult population in many supermarkets and grocery stores. The data obtained for this analysis describes Tobacco Consumption in USA from 2000 to 2020. From behavior of the data in those 21 years, the aim of the project is to predict total tobacco consumption in 2021 and 2022.

At first, the libraries used for this project are imported.

```
[]: import pandas as pd
  import matplotlib.pyplot as plt
  import statsmodels.api as sm
  import numpy as np
  import seaborn as sns
  import random
  import math
  from statsmodels.tsa.seasonal import seasonal_decompose
  from statsmodels.tsa.api import Holt
  from statsmodels.tsa.arima.model import ARIMA
  from sklearn.linear_model import LinearRegression
  from sklearn.metrics import mean_squared_error, mean_absolute_percentage_error
```

An additional import is included in order to ignore some warnings while processing the data.

```
[]: import warnings
warnings.simplefilter(action="ignore", category=FutureWarning)
```

1.1 Extraction

The data for this project is stored in a .csv file. The path to the file is defined in the variable $DATA_PATH$.

```
[]: DATA_PATH = "../data/Tobacco_Consumption.csv"
```

The file is read and a sample of the data is shown.

```
[]: tobacco_data_raw = pd.read_csv(DATA_PATH)
tobacco_data_raw.sample(10)
```

```
[]:
          Year LocationAbbrev LocationDesc
                                              Population
                                                                              Topic \
          2011
     151
                            US
                                    National
                                                237657645
                                                            Noncombustible Tobacco
     69
          2005
                            US
                                    National
                                                222003984
                                                            Noncombustible Tobacco
     207
          2015
                            US
                                    National
                                                247773709
                                                               Combustible Tobacco
         2010
                            US
                                                               Combustible Tobacco
     134
                                    National
                                                235153929
     148
          2011
                            US
                                    National
                                                237657645
                                                               Combustible Tobacco
     177
          2013
                            US
                                    National
                                                242542967
                                                               Combustible Tobacco
     209
          2016
                            US
                                    National
                                                249485228
                                                               Combustible Tobacco
          2004
                            US
                                                               Combustible Tobacco
     59
                                    National
                                                219552929
     229
          2017
                            US
                                    National
                                                252063800
                                                               Combustible Tobacco
     96
          2007
                            US
                                                227239768
                                                               Combustible Tobacco
                                    National
                                                              Data Value Unit
                     Measure
                                           Submeasure
     151
          Smokeless Tobacco
                                                Snuff
                                                                        Pounds
          Smokeless Tobacco
     69
                                     Chewing Tobacco
                                                                        Pounds
     207
                                         Small Cigars
                                                                        Cigars
                      Cigars
     134
              Loose Tobacco
                                        Pipe Tobacco
                                                                        Pounds
     148
              Loose Tobacco
                              Roll-Your-Own Tobacco
                                                        Cigarette Equivalents
     177
              Loose Tobacco
                                 Total Loose Tobacco
                                                                        Pounds
     209
                      Cigars
                                        Large Cigars
                                                                        Cigars
     59
              Loose Tobacco
                                        Pipe Tobacco
                                                                        Pounds
     229
              Loose Tobacco
                               Roll-Your-Own Tobacco
                                                        Cigarette Equivalents
                                                       Cigarette Equivalents
     96
              Loose Tobacco
                              Roll-Your-Own Tobacco
            Domestic
                           Imports
                                           Total
                                                  Domestic Per Capita
     151
                           464519
                                                                 0.434
           103097456
                                      103561975
                                                                 0.175
     69
                           315916
             38883276
                                       39199192
                                                                 2.000
     207
           530680751
                         23505000
                                      554185751
     134
                                                                 0.000
             22266231
                           2822447
                                        25088678
     148
          2412067938
                        209522215
                                     2621590154
                                                                10.000
     177
            42645920
                           3456679
                                        46102599
                                                                 0.000
     209
          5056761893
                       6974839000
                                    12031600893
                                                                20.000
     59
             3904810
                           794487
                                         4699297
                                                                 0.000
     229
          1212400738
                         99499323
                                     1311900062
                                                                 5.000
     96
          8508941785
                        816734031
                                     9325675815
                                                                37.000
                                Total Per Capita
          Imports Per Capita
     151
                        0.002
                                            0.436
     69
                        0.001
                                            0.177
     207
                        0.000
                                            2.000
     134
                        0.000
                                            0.000
     148
                        1.000
                                           11.000
     177
                        0.000
                                            0.000
     209
                       28.000
                                           48.000
     59
                        0.000
                                            0.000
     229
                        0.000
                                            5.000
     96
                        4.000
                                           41.000
```

Exploratory Data Analysis

Describe data table

```
[]: tobacco_data_raw.info()
```

<class 'pandas.core.frame.DataFrame'> RangeIndex: 273 entries, 0 to 272 Data columns (total 14 columns):

Data	COLUMNIS (COURT 14 CO.	rumis).	
#	Column	Non-Null Count	Dtype
0	Year	273 non-null	int64
1	LocationAbbrev	273 non-null	object
2	LocationDesc	273 non-null	object
3	Population	273 non-null	int64
4	Topic	273 non-null	object
5	Measure	273 non-null	object
6	Submeasure	273 non-null	object
7	Data Value Unit	273 non-null	object
8	Domestic	273 non-null	int64
9	Imports	273 non-null	int64
10	Total	273 non-null	int64
11	Domestic Per Capita	273 non-null	float64
12	Imports Per Capita	273 non-null	float64
13	Total Per Capita	273 non-null	float64
dtype	es: float64(3), int64	(5), object(6)	
	00 0. 170		

memory usage: 30.0+ KB

In this table, there are categorial and numerical variables.

The exploration will initially focus on categorical variables and later on the numerical ones.

1.2.1 Categorical Data Exploration

The categorical data columns are filtered from the original dataframe.

```
[]: # Filter categorical variables from data
    tobacco_categorical_data = tobacco_data_raw.select_dtypes(exclude=['int',_
     # Show head of tables
    tobacco_categorical_data.head(10)
```

\	Measure	Topic		LocationDesc	${\tt LocationAbbrev}$	[]:
	Smokeless Tobacco	tible Tobacco	Noncombustible	National	US	0
	Cigarettes	tible Tobacco	Combustible	National	US	1
	Cigars	tible Tobacco	Combustible	National	US	2
	Loose Tobacco	tible Tobacco	Combustible	National	US	3
	Loose Tobacco	tible Tobacco	Combustible	National	US	4
	Cigars	tible Tobacco	Combustible	National	US	5
	Loose Tobacco	tible Tobacco	Combustible	National	US	6

```
7
              US
                      National
                                   Combustible Tobacco
                                                             Loose Tobacco
8
                                   Combustible Tobacco
              US
                      National
                                                             Loose Tobacco
9
              US
                      National
                                   Combustible Tobacco
                                                                     Cigars
              Submeasure
                                 Data Value Unit
0
         Chewing Tobacco
                                          Pounds
      Cigarette Removals
1
                                      Cigarettes
2
            Total Cigars
                                          Cigars
3
     Total Loose Tobacco Cigarette Equivalents
4
     Total Loose Tobacco
                                          Pounds
            Small Cigars
5
                                          Cigars
6
            Pipe Tobacco
                                          Pounds
7
  Roll-Your-Own Tobacco Cigarette Equivalents
8
 Roll-Your-Own Tobacco
                                          Pounds
            Large Cigars
9
                                          Cigars
```

Categorical data columns are identified.

```
[]: # Show numbers of columns

print(f"There is a total of {len(tobacco_categorical_data.columns)}_

categorical data columns")

# Show name of the columns

print(f"The columns are: {tobacco_categorical_data.columns}")

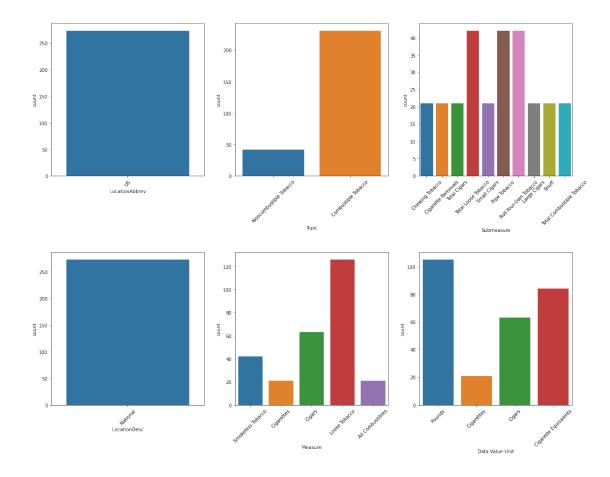
There is a total of 6 categorical data columns
```

```
The columns are: Index(['LocationAbbrev', 'LocationDesc', 'Topic', 'Measure', 'Submeasure',

'Data Value Unit'],

dtype='object')
```

To explore the frecuency of elements for each column, frecuency is plotted in a bar chart, where x axis is the name of the elements in the column, and yaxis is the number of times the element is in the column.



For LocationDesc and LocationAbbrev columns there is only one unique value each. Therefore, these columns are constants.

Most values in submeasure have a 21 apperances in the table.

The combinations of values in the columns "Measure", "Submeasure" and "Units" is further explored, to identify how many time each different combinations is shown in the table.

Categorical data combinations Unique combinations of categories are obtained.

[]: # Get unique combinations by dropping duplicated categorical columns tobacco_categorical_data.drop_duplicates()

\	Measure	Topic		LocationDesc	LocationAbbrev	[]:
	Smokeless Tobacco	Tobacco	Noncombustible	National	US	0
	Cigarettes	Tobacco	Combustible	National	US	1
	Cigars	Tobacco	Combustible	National	US	2
	Loose Tobacco	Tobacco	Combustible	National	US	3
	Loose Tobacco	Tobacco	Combustible	National	US	4
	Cigars	Tobacco	Combustible	National	US	5
	Loose Tobacco	Tobacco	Combustible	National	US	6

7	US National	Combustible Tobacco	Loose Tobacco
8	US National	Combustible Tobacco	Loose Tobacco
9	US National	Combustible Tobacco	Cigars
10	US National	Combustible Tobacco	Loose Tobacco
11	US National	Noncombustible Tobacco	Smokeless Tobacco
12	US National	Combustible Tobacco	All Combustibles
	Submeasure	Data Value Unit	
0	Chewing Tobacco	Pounds	
1	Cigarette Removals	Cigarettes	
2	Total Cigars	Cigars	
3	Total Loose Tobacco	Cigarette Equivalents	
4	Total Loose Tobacco	Pounds	
5	Small Cigars	Cigars	
6	Pipe Tobacco	Pounds	
7	Roll-Your-Own Tobacco	Cigarette Equivalents	
8	Roll-Your-Own Tobacco	Pounds	
9	Large Cigars	Cigars	
10	Pipe Tobacco	Cigarette Equivalents	
11	Snuff	Pounds	
12	Total Combustible Tobacco	Cigarette Equivalents	

Describe combinations and unique combinations.

Total combinations of categories (rows): 273 Find 13 unique category combinations Relation: 21.0

13 combinations are repeated 21 times in the table.

This number match the number of years in the data. The dataset included 13 different values per year.

1.2.2 Numerical Data Exploration

The numerical data columns are filtered from the original dataframe.

```
[]:
```

```
# Filter numerical variables from data

tobacco_numerical_data = tobacco_data_raw.select_dtypes(include=['int',u'])

# Show head of tables

tobacco_numerical_data.head(10)
```

[]:		Year	Population	Domestic	Imports	Total	\
	0	2000	209786736	45502156	91965	45594121	
	1	2000	209786736	423250355675	12319663000	435570018675	
	2	2000	209786736	5612867329	548243000	6161110329	
	3	2000	209786736	8291276800	702741662	8994018462	
	4	2000	209786736	16841656	1427444	18269100	
	5	2000	209786736	2243135044	36049000	2279184044	
	6	2000	209786736	5352683	739887	6092570	
	7	2000	209786736	5656109785	338489600	5994599385	
	8	2000	209786736	11488973	687557	12176530	
	9	2000	209786736	3369732285	512194000	3881926285	
		Domes	tic Per Capit	a Imports Pe	r Capita Tot	al Per Capita	
	0		0.21		0.0	0.217	
	1		2018.00	00	59.0	2076.000	
	2		27.00	00	3.0	29.000	
	3		40.00	00	3.0	43.000	
	4		0.00	00	0.0	0.000	
	5		11.00	00	0.0	11.000	
	6		0.00	00	0.0	0.000	
	7		27.00	00	2.0	29.000	
	8		0.00	00	0.0	0.000	
	9		16.00	00	2.0	19.000	

Numerical data columns are identified.

```
[]: # Show numbers of columns

print(f"There is a total of {len(tobacco_numerical_data.columns)} numerical_

data columns")

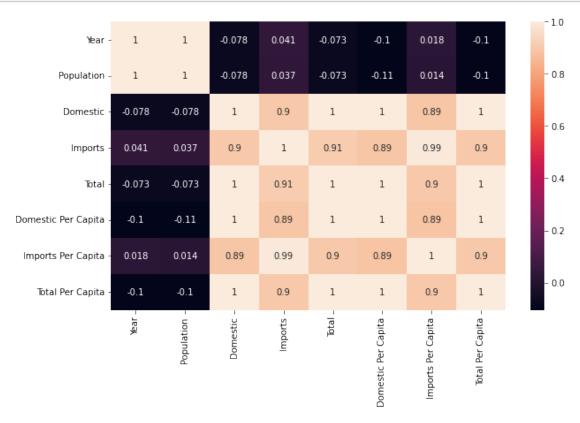
# Show name of the columns

print(f"The columns are: {tobacco_numerical_data.columns}")
```

To understand how each variable is related to each other, correlations are obtained and plotted.

```
[]: # Explore correlations
    correlations = tobacco_numerical_data.corr()
    # Plot correlations
```

sns.heatmap(correlations, annot=True)
plt.show()



Year and Population have a strong correction with each other, but a low correction to tobacco values.

Per capita values have a strong correlation with normal values.

A test is applied to verify if per capita values are obtained from total values and population.

[]: 0.003

The difference is close to 0. Therefore, the next expressions can be established from the data:

$$Domestic_per_capita = \frac{Domestic}{Population}$$

$$Imports_per_capita = \frac{Imports}{Population}$$

$$Total_per_capita = \frac{Total}{Population}$$

For further analysis, per capita columns are excluded.

Domestic and Imports have a strong correlation to Total column.

[]: 0.0

The difference is 0, so

$$Total = Imports + Domestic$$

To have a better understading of this variables, it is needed to combine numerical exploration with the unique categories exploration. After that analysis, the relation between submeasures is expected to be identified.

1.2.3 Integrated Exploration (Categories & Numerical Data)

As each year has the same category combinations, one year (2000) is used as a sample. As this analysis focuses in tobacco consumption, only units related to products are taken in to account. Therefore, unit "Pounds" is excluded.

```
[]: # Get filtered df
products_df = tobacco_data_raw[(tobacco_data_raw["Data Value Unit"] !=
□
□"Pounds") & (tobacco_data_raw["Year"] == 2000)]
products_df
```

[]:	Year	LocationAbbrev	LocationDesc	Population	Topic	\
1	2000	US	National	209786736	Combustible Tobacco	
2	2000	US	National	209786736	Combustible Tobacco	
3	2000	US	National	209786736	Combustible Tobacco	
5	2000	US	National	209786736	Combustible Tobacco	
7	2000	US	National	209786736	Combustible Tobacco	
9	2000	US	National	209786736	Combustible Tobacco	
10	2000	US	National	209786736	Combustible Tobacco	
12	2000	US	National	209786736	Combustible Tobacco	
		M		Q 1		. ,

\	Data Value Unit	Submeasure	Measure	
	Cigarettes	Cigarette Removals	Cigarettes	1
	Cigars	Total Cigars	Cigars	2
	Cigarette Equivalents	Total Loose Tobacco	Loose Tobacco	3
	Cigars	Small Cigars	Cigars	5
	Cigarette Equivalents	Roll-Your-Own Tobacco	Loose Tobacco	7

10 Loose Tobacco Pipe Tobacco Cigarette Equivale 12 All Combustibles Total Combustible Tobacco Cigarette Equivale Domestic Imports Total Domestic Per Capita 1 423250355675 12319663000 435570018675 2018.0 2 5612867329 548243000 6161110329 27.0 3 8291276800 702741662 8994018462 40.0	ars
Domestic Imports Total Domestic Per Capita \ 1 423250355675 12319663000 435570018675 2018.0 2 5612867329 548243000 6161110329 27.0	nts
1 423250355675 12319663000 435570018675 2018.0 2 5612867329 548243000 6161110329 27.0	nts
1 423250355675 12319663000 435570018675 2018.0 2 5612867329 548243000 6161110329 27.0	
2 5612867329 548243000 6161110329 27.0	
2 9201276900 702741662 9004019462 40.0	
5 6291276600 702741662 6994016462 40.0	
5 2243135044 36049000 2279184044 11.0	
7 5656109785 338489600 5994599385 27.0	
9 3369732285 512194000 3881926285 16.0	
10 2635167015 364252062 2999419077 13.0	
12 437154499804 13570647662 450725147466 2084.0	
Imports Per Capita Total Per Capita	
1 59.0 2076.0	
2 3.0 29.0	
3 3.0 43.0	
5 0.0 11.0	
7 2.0 29.0	
9 2.0 19.0	
10 2.0 14.0	
12 65.0 2148.0	
12 65.0 2148.0	

Total Loose Tobacco is compared to Pipe Tobaco and Roll-Your-Own Tobacco

```
[]: # Compare diff between Total Loose Tobacco and Pipe Tobacco
products_df["Domestic"][3] - products_df["Domestic"][7] -□

□products_df["Domestic"][10]
```

[]: 0

Therefore,

$$Total_Loose_Tobacco = Pipe_Tobacco + Roll_Your_Own_Tobacco$$

The Loose Tobacco values are in the table twice (as pounds and as cigarette equivalents), that's the reason the frequency was the double than other cases in categorical data analysis.

Total Cigars are compared to Small and Large Cigars...

```
[]: products_df["Domestic"][2] - products_df["Domestic"][5] -⊔

□ products_df["Domestic"][9]
```

[]: 0

For Cigars:

$$Total_Cigars = Small_Cigars + Large_Cigars$$

```
[]: # Get sum of non-total submeasures
sum_cigarettes = products_df["Domestic"][~products_df["Submeasure"].str.

→contains("Total")].sum()
# Compare sum to Total Combustible Tobacco variable
products_df["Domestic"][products_df["Submeasure"]=="Total Combustible Tobacco"]

→- sum_cigarettes
```

[]: 12 0
Name: Domestic, dtype: int64

 $Total_Combustible_Tobacco = Total_Cigars + Total_Loose_Tobaccoo + Cigarette_Removals$

Cigarette, Cigarette Equivalents, and Cigars units have a 1:1:1 relationship.

Total Combustible Tobacco contains information of all types of tobacco products submeasures. This value will be the target variable that is going to be predicted in the analysis.

1.3 Data Wrangling

The original dataframe is filtered and transfromed to get a useful table focused in the target variable. Unnecessary columns are drop and year is set as index of the table.

```
[]: total_combustible_tobacco_df =
      →tobacco_data_raw[tobacco_data_raw["Submeasure"] == "Total Combustible Tobacco"]
     # Drop columns with constant information
     total_combustible_tobacco_df.drop(columns=["LocationAbbrev", "LocationDesc", __
      ⇔"Topic", "Measure",
         "Submeasure", "Data Value Unit"], inplace=True)
     # To reduce data with similar behavior, per capita values will be also ignored _{f L}
      →in the transformation
     total_combustible_tobacco_df.drop(columns=["Domestic Per Capita", "Imports Per_
      →Capita", "Total Per Capita"], inplace=True)
     # Year to index and datetime object
     total_combustible_tobacco_df.set_index("Year", inplace = True)
     total_combustible_tobacco_df.index = pd.
      →to_datetime(total_combustible_tobacco_df.index, format = "%Y")
     # Show time series
     total_combustible_tobacco_df
```

 $\begin{tabular}{ll} $C:\Users\edson\appData\Local\Temp\ipykernel_10308\332722847.py:3: SettingWithCopyWarning: \end{tabular}$

A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy total_combustible_tobacco_df.drop(columns=["LocationAbbrev", "LocationDesc", "Topic", "Measure",

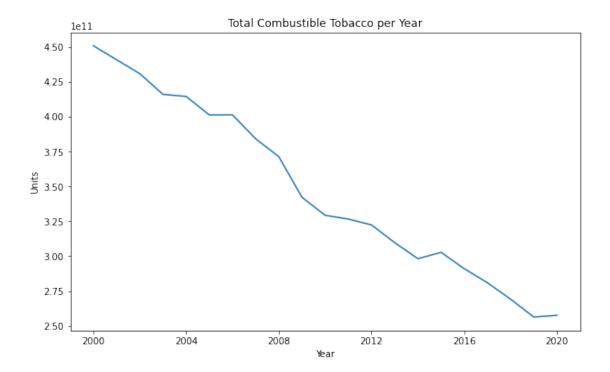
 $\begin{tabular}{l} C:\Users\edson\AppData\Local\Temp\ipykernel_10308\332722847.py:6: Setting\WithCopyWarning: \end{tabular}$

A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy total_combustible_tobacco_df.drop(columns=["Domestic Per Capita", "Imports Per Capita", "Total Per Capita"], inplace=True)

[]:		Population	Domestic	Imports	Total
	Year				
	2000-01-01	209786736	437154499804	13570647662	450725147466
	2001-01-01	212345162	424447310483	16245487123	440692797606
	2002-01-01	214754648	408303465673	22459975923	430763441596
	2003-01-01	217068101	391196952717	24733051892	415930004609
	2004-01-01	219552929	390166439041	24254733538	414421172579
	2005-01-01	222003984	380712422031	20474781600	401187203631
	2006-01-01	224583123	382748665603	18493161400	401241827003
	2007-01-01	227239768	367880476823	16206169554	384086646377
	2008-01-01	229945137	357080696204	14183410908	371264347112
	2009-01-01	232458335	329491123539	12632961400	342124084939
	2010-01-01	235153929	317475052695	11764157615	329239210311
	2011-01-01	237657645	315683514293	10893776123	326577290416
	2012-01-01	240185952	310009439421	12386990662	322396430083
	2013-01-01	242542967	295476582903	14164450662	309641033564
	2014-01-01	245273438	282020020624	16175868538	298195889163
	2015-01-01	247773709	285537129046	17214155385	302751284431
	2016-01-01	249485228	273881993213	17154801323	291036794536
	2017-01-01	252063800	263359518483	17581121431	280940639914
	2018-01-01	253768092	249351495626	19823602569	269167785869
	2019-01-01	255200373	234601291857	21813751754	256415043611
	2020-01-01	256662010	235888722742	21726898662	257615621404

Plot total over the years



Store new table as csv.

```
[]: # Export ts to df
OUTPUT_PATH = "../data/Transformed_Tobacco_Consumption.csv"
total_combustible_tobacco_df.to_csv(OUTPUT_PATH, index=False)
```

1.4 Exploration of Transformed Data

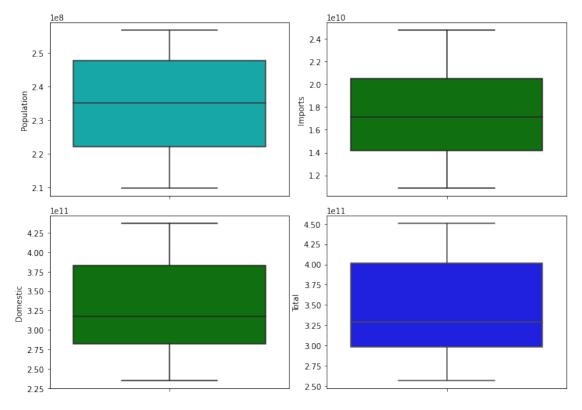
```
[]: # Explore variables distribution total_combustible_tobacco_df.describe().convert_dtypes()
```

				<u>_</u>	
[]:		Population	Domestic	Imports	\
	count	21.0	21.0	21.0	
	mean	234547860.285714	330117467277.190491	17331140748.761906	
	std	15123590.490099	63129184488.71344	4140066674.594648	
	min	209786736.0	234601291857.0	10893776123.0	
	25%	222003984.0	282020020624.0	14164450662.0	
	50%	235153929.0	317475052695.0	17154801323.0	
	75%	247773709.0	382748665603.0	20474781600.0	
	max	256662010.0	437154499804.0	24733051892.0	

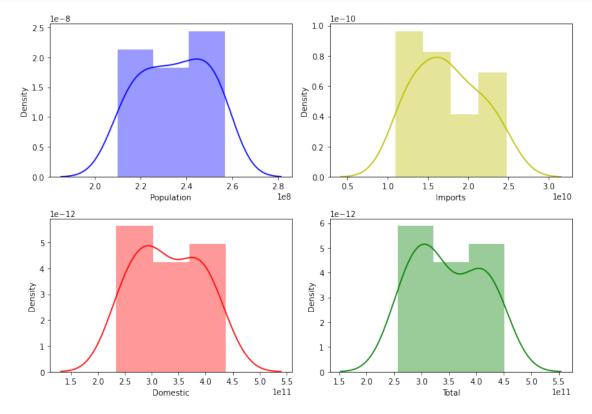
Total count 21.0 mean 347448271248.571411 std 63456602238.587479

```
min 256415043611.0
25% 298195889163.0
50% 329239210311.0
75% 401241827003.0
max 450725147466.0
```

Show boxplots and histograms

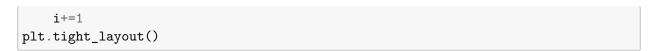


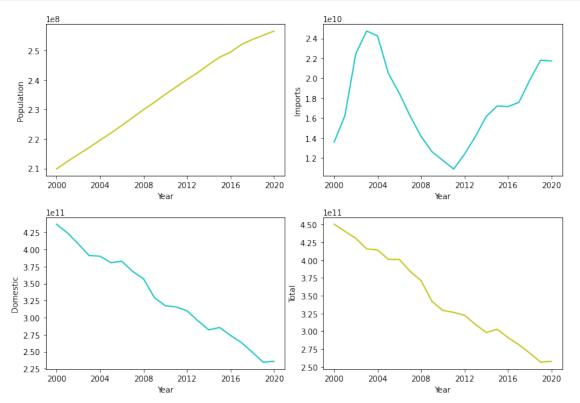
For population and total, data seems to be symmetric. However, Domestic and Total are a little right-skewed.



All variables seem close to be symetric. The previously identified as skewed variables are also close to the center of the data.

Plots all trends by year.





The percentage of change of variables over time is explored.

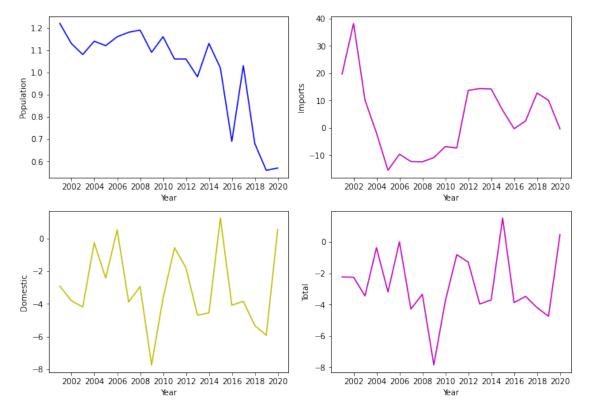
1.4.1 % Change over the years

Get % of change of each variable and plot.

```
[]: ts_change_df = total_combustible_tobacco_df.pct_change().dropna()
ts_change_df = round(ts_change_df *100,2)
ts_change_df.head(5)
```

```
[]:
                 Population Domestic
                                         Imports
                                                  Total
     Year
     2001-01-01
                        1.22
                                 -2.91
                                           19.71
                                                  -2.23
     2002-01-01
                        1.13
                                 -3.80
                                           38.25
                                                  -2.25
     2003-01-01
                        1.08
                                 -4.19
                                           10.12
                                                  -3.44
     2004-01-01
                        1.14
                                 -0.26
                                           -1.93
                                                  -0.36
     2005-01-01
                        1.12
                                 -2.42
                                          -15.58
                                                  -3.19
```

```
[]:  # Plot % of change of varibles
COLORS = ["b", "g", "r", "c", "m", "y"]
```



There is no clear behavior related to how much does each vairables changes per year.

1.4.2 Stationarity

Augmented Dickey-Fuller test is applied to verify if the data is stationary.

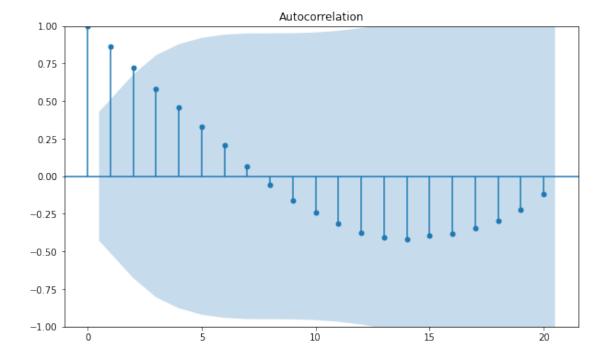
ADF Statistic: -4.365042

p-value: 0.000342 Critical Values: 1%: -4.138 5%: -3.155 10%: -2.714

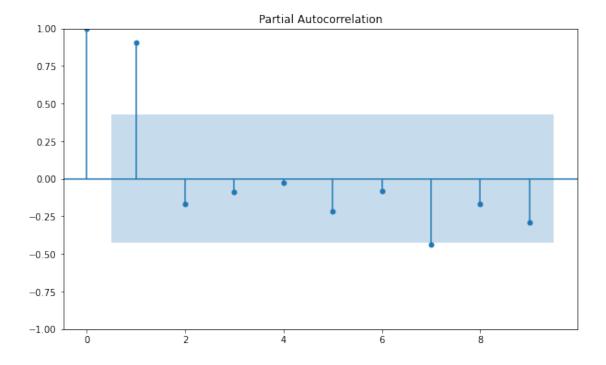
The p-value is really small (less than 5% threshold), so it is confirmed the total column is a stationary time series.

1.4.3 ACF and PACF

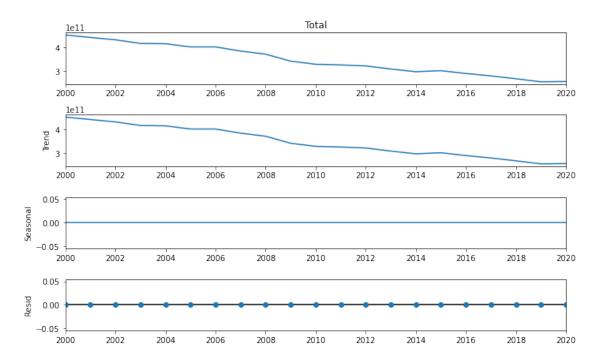
```
[]: plt.rc("figure", figsize=(10,6))
sm.graphics.tsa.plot_acf(total_combustible_tobacco_df["Total"], lags=20)
plt.show()
```



```
[]: plt.rc("figure", figsize=(10,6))
sm.graphics.tsa.plot_pacf(total_combustible_tobacco_df["Total"], lags=9)
plt.show()
```



1.4.4 Time Series Decomposition



There is neither seasonal component or resid.

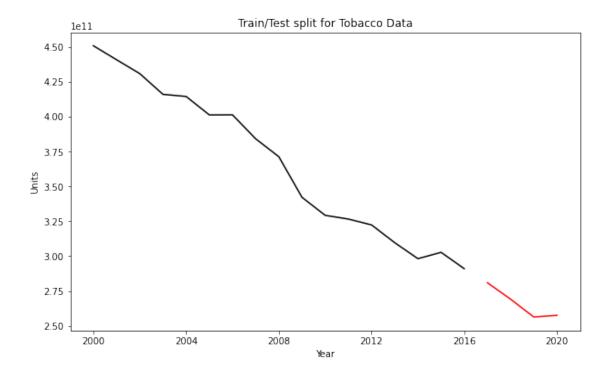
1.5 Modeling

In this project, three models are compared: - Linear Regression - AutoRegresive Integrated Moving Average (ARIMA) - Holt's Exponential Smoothing

Two metrics are used for comparing and selecting a model: - Relative Root Mean Square Error (rRMSE) - Mean Absolute Percentage Error (MAPE)

One of the models will be selected to predict the total tobacco consumption over the next years.

At first, data is splitted in test and train datasets



1.5.1 Linear Regression Model

In this model, indepedent variable is Year and dependent variable is the total tobacco consumption. Based on that, X and Y are defined.

```
[]: # Get X and Y from training data
X = train.index.year.values.reshape(-1, 1)
Y = train.values.reshape(-1, 1)
```

The model is created and trained.

```
[]: LR_model = LinearRegression()
    LR_model.fit(X, Y)
```

[]: LinearRegression()

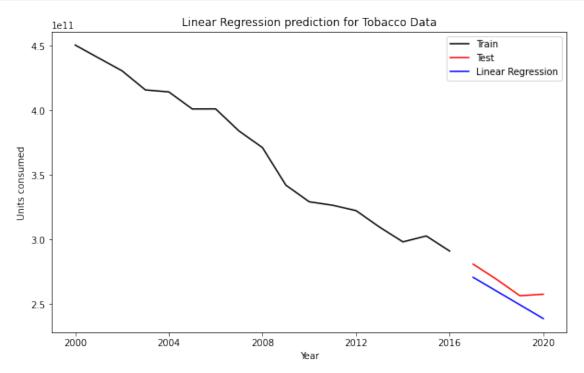
To test the model, predictions of the years in the test set (2017-2020) are made.

[]: Year 2017-01-01 2.706961e+11 2018-01-01 2.600396e+11 2019-01-01 2.493831e+11

```
2020-01-01 2.387266e+11
```

dtype: float64

```
[]: plt.plot(train, color="black", label = "Train")
   plt.plot(test, color = "red", label = "Test")
   plt.plot(y_pred_lr, color = "blue", label= "Linear Regression")
   plt.ylabel("Units consumed")
   plt.xlabel("Year")
   plt.title("Linear Regression prediction for Tobacco Data")
   plt.legend(loc="upper right")
   plt.show()
```



1.5.2 ARIMA Model

Train model and tune hyperparameters.

```
[]: ARIMA_model = ARIMA(train, order=(3,3,2))
ARIMA_model = ARIMA_model.fit()
print(ARIMA_model.summary())
```

c:\Users\edson\Documents\Repositorios\Data-Science\Tobacco-Consumption-Prediction\code\jenv\lib\site-packages\statsmodels\tsa\base\tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used.

```
self._init_dates(dates, freq)
```

c:\Users\edson\Documents\Repositorios\Data-Science\Tobacco-Consumption-Prediction\code\jenv\lib\site-packages\statsmodels\tsa\base\tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used.

self._init_dates(dates, freq)

c:\Users\edson\Documents\Repositorios\Data-Science\Tobacco-Consumption-Prediction\code\jenv\lib\site-packages\statsmodels\tsa\base\tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used.

self._init_dates(dates, freq)

c:\Users\edson\Documents\Repositorios\Data-Science\Tobacco-ConsumptionPrediction\code\jenv\lib\site-

packages\statsmodels\tsa\statespace\sarimax.py:978: UserWarning: Non-invertible starting MA parameters found. Using zeros as starting parameters.

warn('Non-invertible starting MA parameters found.'

SARIMAX Results

Dep. Variable: Total			======= otal No.	Observations:	:=======	======================================
Model:		ARIMA(3, 3,				-341.950
Date:		ın, 10 Apr 2	_			695.901
Time:	2.2	•	1:09 BIC			699.735
Sample:			2000 HQIC	!		695.546
2 cmp = 0 :		- 01-01-2				0001010
Covariance			opg			
=======	coef	std err	z	P> z	[0.025	0.975]
ar.L1	-1.0102	0.479	-2.108	0.035	-1.950	-0.071
ar.L2	-0.2133	0.257	-0.830	0.407	-0.717	0.291
ar.L3	-0.0263	0.088	-0.301	0.763	-0.198	0.145
ma.L1	-0.2394	0.612	-0.391	0.696	-1.439	0.960
ma.L2	-0.7161	0.851	-0.842	0.400	-2.383	0.951
sigma2	1.172e+20	7.68e-21	1.53e+40	0.000	1.17e+20	1.17e+20
====	========	=======		========		
Ljung-Box 0.83	(L1) (Q):		0.25	Jarque-Bera	(JB):	
Prob(Q):			0.60	Prob(JB):		
. •			0.62	Prob(Jb):		
0.66 Heteroskedasticity (H):		6 17	Classes			
0.53	asticity (n):		6.17	Skew:		
Prob(H) (t	wo-sided):		0.07	Kurtosis:		
2.44	wo bidody.		0.01	nar oobib.		
========						

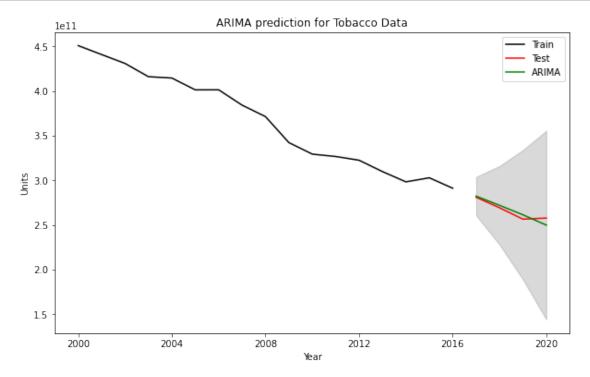
Warnings:

===

- [1] Covariance matrix calculated using the outer product of gradients (complex-step).
- [2] Covariance matrix is singular or near-singular, with condition number 2.06e+56. Standard errors may be unstable.

To test the model, predictions of the years in the test set (2017-2020) are made.

```
[]: arima_pred = ARIMA_model.get_forecast(len(test))
# Get confidence interval
y_conf_int_df = arima_pred.conf_int(alpha=0.05)
y_conf_int_df
# Get predictions for test set years
y_pred_arima = ARIMA_model.predict(start=test.index[0], end=test.index[-1])
```



1.5.3 Holt's Exponential Smoothing Model (ETS)

Train model

```
[]: holt_model = Holt(train, initialization_method="estimated").

fit(smoothing_level=0.8, smoothing_trend=0.2, optimized=False)
```

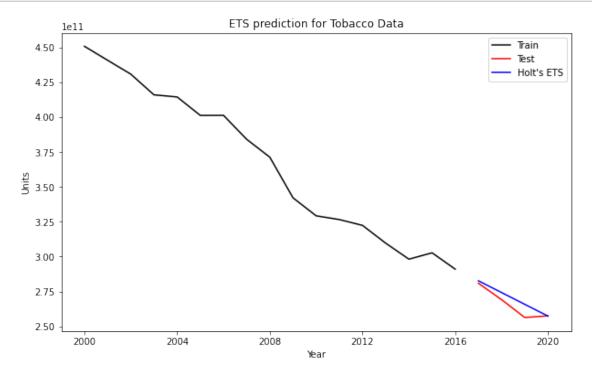
c:\Users\edson\Documents\Repositorios\Data-Science\Tobacco-Consumption-Prediction\code\jenv\lib\site-packages\statsmodels\tsa\base\tsa_model.py:471: ValueWarning: No frequency information was provided, so inferred frequency AS-JAN will be used.

```
self._init_dates(dates, freq)
```

To test the model, predictions of the years in the test set (2017-2020) are made.

```
[ ]: y_pred_ets = holt_model.forecast(len(test))
```

```
[]: plt.plot(train, color="black", label = "Train")
   plt.plot(test, color = "red", label = "Test")
   plt.plot(y_pred_ets, color = "blue", label= "Holt's ETS")
   plt.ylabel("Units")
   plt.xlabel("Year")
   plt.title("ETS prediction for Tobacco Data")
   plt.legend(loc="upper right")
   plt.show()
```



1.5.4 Evaluation and Selection

Define function to obtain relative root mean square error of predicted values.

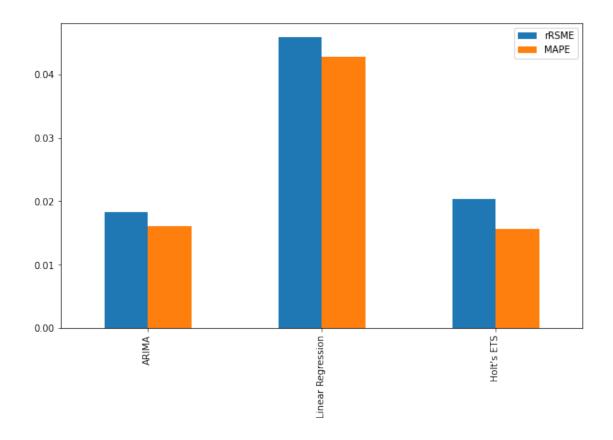
```
[]: def rRMSE(actual_values, predicted_values, mean_value):
    rmse_value = np.sqrt(mean_squared_error(actual_values, predicted_values))
    rrmse_value = rmse_value/mean_value
    return rrmse_value
```

Create table that summarizes results of evaluation metrics.

```
[]: rRSME MAPE
ARIMA 0.018342 0.016066
Linear Regression 0.045826 0.042781
Holt's ETS 0.020407 0.015655
```

```
[]: evaluation_df.plot.bar()
```

[]: <AxesSubplot:>



Linear Regression model provided a worse performance than the other two models. ARIMA and ETS got similar results in MAPE metric, but performance of ARIMA was better than ETS in rRMSE metric. For ARIMA, both metric results are under 2%.

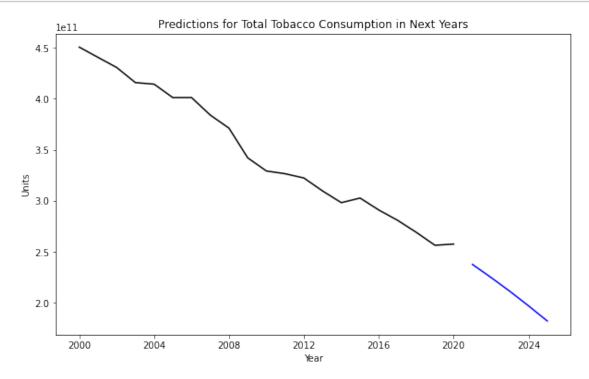
ARIMA model is selected.

1.6 Results

Get tobacco consumption for 2021, 2022 and 2023.

```
[]: y_predictions_future = ARIMA_model.predict(start="2021", end="2025")
     y_predictions_future
[]: 2021-01-01
                   2.376935e+11
                   2.247738e+11
    2022-01-01
     2023-01-01
                  2.113127e+11
    2024-01-01
                   1.970416e+11
    2025-01-01
                   1.821700e+11
    Freq: AS-JAN, Name: predicted_mean, dtype: float64
[]: plt.plot(total_combustible_tobacco_df["Total"], color="black", label = "Train")
     plt.plot(y_predictions_future, color = "blue", label= "Predictions")
     plt.ylabel("Units")
```

```
plt.xlabel("Year")
plt.title("Predictions for Total Tobacco Consumption in Next Years")
plt.show()
```



1.7 Conclusions

Total Tobacco Consumption is decreasing through the years in the United States.

For the next years, the total consumption is expected to keep decreasing.