This document defines the formulas required for a Kalman filter that is used to localize the EduArt robots globally.

1 Prediction Model for Eduard with Mecanum

1.1 Acceleration

$$\mathbf{a}_{t-1} = \begin{pmatrix} a_{x_{t-1}} \\ a_{y_{t-1}} \end{pmatrix} \tag{1}$$

$$\mathbf{a}_t = \begin{pmatrix} a_{x_{t-1}} \\ a_{y_{t-1}} \end{pmatrix} \tag{2}$$

1.2 Velocity

$$\mathbf{v}_{t-1} = \begin{pmatrix} v_{x_{t-1}} \\ v_{y_{t-1}} \end{pmatrix} \tag{3}$$

$$\mathbf{v}_{t} = \begin{pmatrix} a_{x_{t-1}} dt + v_{x_{t-1}} \\ a_{y_{t-1}} dt + v_{y_{t-1}} \end{pmatrix} \tag{4}$$

1.3 Yaw

$$\phi_{z_t} = \phi_{z_{t-1}} + \phi_{z_{t-1}} \frac{d}{dt} dt \tag{5}$$

$$\phi_{z_t} \frac{d}{dt} = \phi_{z_{t-1}} \frac{d}{dt} \tag{6}$$

1.4 Position

$$\mathbf{R}_{t-1} = \begin{pmatrix} \cos\left(\phi_{z_{t-1}}\right) & -\sin\left(\phi_{z_{t-1}}\right) \\ \sin\left(\phi_{z_{t-1}}\right) & \cos\left(\phi_{z_{t-1}}\right) \end{pmatrix} \tag{7}$$

$$\mathbf{p}_{t-1} = \begin{pmatrix} p_{x(t-1)} \\ p_{y(t-1)} \end{pmatrix} \tag{8}$$

$$\mathbf{p}_{t} = \mathbf{p}_{t-1} + \mathbf{R}_{t-1}\mathbf{v}_{t-1} + \frac{1}{2}\mathbf{R}_{t-1}\mathbf{a}^{2}$$
(9)

$$= \begin{pmatrix} dt \left(0.5a_{x_{t-1}}^2 \cos \left(\phi_{z_{t-1}} \right) - 0.5a_{y_{t-1}}^2 \sin \left(\phi_{z_{t-1}} \right) \right) + dt \left(v_{x_{t-1}} \cos \left(\phi_{z_{t-1}} \right) - v_{y_{t-1}} \sin \left(\phi_{z_{t-1}} \right) \right) + p_{x(t-1)} \\ dt \left(0.5a_{x_{t-1}}^2 \sin \left(\phi_{z_{t-1}} \right) + 0.5a_{y_{t-1}}^2 \cos \left(\phi_{z_{t-1}} \right) \right) + dt \left(v_{x_{t-1}} \sin \left(\phi_{z_{t-1}} \right) + v_{y_{t-1}} \cos \left(\phi_{z_{t-1}} \right) \right) + p_{y(t-1)} \end{pmatrix}$$
 (10)

1.5 \mathbf{Model}

$$\mathbf{F}_{t} = \begin{pmatrix} p_{x_{t}} \\ p_{y_{t}} \\ v_{x_{t}} \\ v_{y_{t}} \\ v_$$

(13)