15-213 Introduction to Computer Systems

Final Exam

May 10, 2007

Name: _____

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Recitation Section: _____

- This is an open-book exam.

- Notes and calculators are permitted, but not computers.

- Write your answer legibly in the space provided.

- You have 180 minutes for this exam.

			ore
Assembly Language	2		
Optimization	3	**20**	
Cache Memory	4	**20**	
Signals	5	**20**	
Garbage Collection	6	**20**	
Threads	7	**20**	
Synchronization	8	**20**	
Total		**150+10**	

1. Floating Point (20 points)

In this problem we consider properties of floating point operations. For each property state whether it is true or false. If false, give a counterexample as a (possibly negative) power of 2 within the range of precision for the variables. We assume that the variables on an x86_64 architecture are declared as follows

```
float x,y,z;
double d,e;
```

and initialized to some unknown value **different from NaN,** $+\infty$, **and** $-\infty$. We have given the first answer as an example.

`(x + y) + z == x + (y + z)`	**false**	$x = 1, y = 2^{127}, z = -2^{127}$
If `x > 0` then `x / 2 > 0`		
`(x + y) * z == x * z + y * z`		
If `x >= y` and `z <= 0` then `x * z <= y * z`		
If `x > y` then (		
If `d > e` then		
`x` ... `x`		

2. Assembly Language (20 points)

In this problem we consider an illustrative program for multiplication of two unsigned `int`'s, returning an unsigned `long int` holding the product.

```c
unsigned long mult (unsigned i, unsigned k) {
  unsigned long p = 0;
  unsigned long q = k;
  while (i != 0) {
    if (i & 1)
      p = p + q;
    q = q << 1;
    i = i >> 1;
  }
  return p;
}
```

The following is the resulting machine code when compiled on an x86_64 machine with `gcc -O2`, omitting two instructions.

```
mult:
        xorl    %ecx, %e
        mov     %esi, %edx
        testl   %edi
        jmp     .L8
.L10:
        leaq    (%rdx,%rdx), %rax
        testb   $1, %dil

        _____     # missing conditional move
        addq    %rdx, %rdx
        shrl    %edi
.L8:
        jne     .L10

        _____     # missing move
        ret
```

1. (5 pts) For each register, give the value it holds during the iteration, expressed in terms of the C program.

Register	C expression
%rcx	
%rdx	
%rax	
%edi	
%dil	

2. (5 pts) Fill in the missing two instructions in the code.

3. (4 pts) Rewrite the loop to use a conditional jump instead of a conditional move.

4. (3 pts) Explain briefly why the compiler preferred to use a conditional move instruction.

5. (3 pts) Assume we declared and initialized

```
int i,k;
long m;
```

and called

```
m = (long)mult((unsigned)i, (unsigned)k);
```

using the above definition of `mult`. Will `m` hold the correct value of the signed product of `i` and `k`? Circle the correct answer.

yes   no

Briefly explain your answer.

3. Optimization (20 points)

Consider the following code for calculating the dot product of two vectors of double precision floating point numbers.

```
double dot_prod(double A[], double B[], int n) {
  int i;
  double r = 0;
  for (i = 0; i < n; i++)
    r = r + A[i] * B[i];
  return r;
}
```

Assume that multiplication has a latency of 12 cycles and addition a latency of 7 cycles and load 4 cycles. Also assume that there are an unlimited number of functional units. [**Hint:** Under this assumption, theoretically optimal performance is dominated by the critical data dependency path.]

1. (5 points) What is the theoretically optimal CPE for this loop?

Assignment Project Exam Help

2. (10 points) Show th
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   are insignificant.   ding errors

```
double dot_prod(double A[], double B[]) {
  int i;
  double r = 0;
```

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```
  return r;
}
```

3. (5 points) What is the theoretically optimal CPE for this loop?

4. Cache Memory (20 points)

In this problem we explore the operation of a basic TLB as a cache. Assume the following

- Virtual addresses are 32 bits.

- The virtual page number (VPN) is 24 bits.

- The physical page number (PPN) is 32 bits.

- The TLB is 2-way set associative containing a total of 512 lines.

1. (6 points) Please fill in the following blanks by giving a bit range, such as "0–15".

    (a) The VPO of a virtual address consists of bits _____ of the VA.

    (b) The VPN of a virtual address consists of bits _____ of the VA.

    (c) The PPO of a physical address consists of bits _____ of the PA.

    (d) The PPN of a physical address consists of bits _____ of the PA.

    (e) The TLB index (TLBI) consists of bits _____ of the VPN.

    (f) The TLB tag (TLBT) consists of bits _____ of the VPN.

    We show a part of t

3D	1	0x08	
		0x08	
3E	0	0xF3	
	1	0x083F	0xAB18ED24
3F	1	0x409A	0x0913ABDE
	1	0x083F	0xAB18ED24
40	0	0x083E	0x0913ABDE
	1	0x3E40	0xAB18ED24

2. (7 points) Assume the virtual address is `0x083F3E9A`. Fill in the following table in hexadecimal notation. Write **U** for any value that is unknown, that is, not determined from the parameters and the table above.

Parameter	Value
VPN	
VPO	
TLBI	
TLBT	
Cache Hit? (Y/N/U)	
PPN	
PA	

3. (7 points) Assume the virtual address is `0x083E40CB`. Fill in the following table in hexadecimal notation. Write **U** for any value that is unknown, that is, not determined from the p

Parameter	Value
VPN	
VPO	
TLBI	
TLBT	
Cache Hit? (Y/N/U)	
PPN	
PA	

5. Signals (20 points)

Consider the following program.

```c
int counter = 0;

void handler (int sig) {
  counter++;
}

int main() {
  signal(SIGUSR1, handler);
  signal(SIGUSR2, handler);
  int parent = getpid();
  int child = fork();

  if (child == 0) {

    /* insert code here */

    exit(0);
  }

  sleep(1);
  waitpid(child
  printf("Received %d USR{1,2} signals\n", coun
  return 0;
}
```

For each of the following four versions of the above code, list the possible outputs of this program, assuming that all function and system calls succeed and exit without error. You may also assume no externally issued signals are sent to either process.

1. (5 pts)

```c
kill(parent, SIGUSR1);
kill(parent, SIGUSR1);
```

2. (5 pts)

```
kill(parent, SIGUSR1);
kill(parent, SIGUSR1);
kill(parent, SIGUSR1);
```

3. (5 pts)

```
kill(parent, SIGUSR1);
kill(parent, SIGUSR2);
```

4. (5 pts)

```
kill(parent, SIGUSR1);
kill(parent, SIGUSR1);
kill(parent, SIGUSR1);
kill(paren
```

6. Garbage Collection (20 points)

In this problem we consider a tiny list processing machine in which each memory word consists of two bytes: the first byte is a pointer to the tail of the list and the second byte is a data element. The end of a list is marked by a pointer of `0x00`. We assume that the data element is never a pointer.

    We start with the memory state on the left, where the range `0x10–0x1F` is the from-space and the range `0x20–0x2F` is the to-space. All addresses and values in the diagram are in hexadecimal.

    Write in the state of memory after a copying collector is called with root pointers `0x10` and `0x12`, in this order. You may leave cells that remain unchanged blank.

    Please be sure to use the proper breadth-first traversal algorithm covered in lecture.

Before GC

Addr	Ptr	Data
10	14	A2
12	1A	1F
14	1E	02
16	1E	
18	00	
1A	18	BC
1C	12	DE
1E	10	8F

After GC

Addr	Ptr	Data	Addr	Ptr	Data
10			20		
12			22		
14			24		
16			26		
18			28		
1A			2A		
1C			2C		
1E			2E		

After garbage collection, free space starts at address _____

7. Threads (20 points)

Consider three concurrently executing threads in the same process using two semaphores s1 and s2. Assume s1 has been initialized to 1, while s2 has been initialized to 0.

What are the possible values of the global variable x, initialized to 0, after all three threads have terminated?

```
/* thread A */
  P(&s2);
  P(&s1);
  x = x*2;
  V(&s1);

/* thread B */
  P(&s1);
  x = x*x;
  V(&s1);

/* thread C */
  P(&s1);
  x = x+3;
  V(&s2);
  V(&s1);
```

8. Synchronization (20 points)

We explore the so-called *barbershop problem*. A barbershop consists of a n waiting chairs and the barber chair. If there are no customers, the barber waits. If a customer enters, and all the waiting chairs are occupied, then the customer leaves the shop. If the barber is busy, but waiting chairs are available, then the customer sits in one of the free chairs.

Here is the skeleton of the code, without synchronization.

```
extern int N;    /* initialized elsewhere to value > 0 */
int customers = 0;

void* customer() {


  if (customers > N) {

    return NULL;
  }


  customers += 1;


  getHairCut();


  customers -= 1;


  return NULL;
}

void* barber() {
  while(1) {



    cutHair();



  }
}
```

For the solution, we use three binary semaphores:

- `mutex` to control access to the global variable `customers`.

- `customer` to signal a customer is in the shop.

- `barber` to signal the barber is busy.

1. (5 points) Indicate the initial values for the three semaphores.

    - `mutex`
    - `customer`
    - `barber`

2. (15 points) Complete the code above filling in as many copies of the following commands as you need, but no other code.

```
P(&mutex);
V(&mutex);
P(&customer);
V(&customer);
P(&barber)
V(&barber)
```