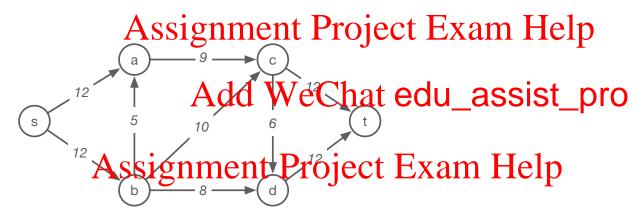
| Name: |
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| 15-351 / 15-650 / 02-613 (Fall 2019): Midterm #2 |
| Note: Please solve each of the following problems. This is a closed-notes and closed-book exam. You also should not use your laptops and cell phones. If you need additional space, use the back of the exam pages and indicate that you did so. |
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| i. What is the was soil ginnment a Pinnoje Gte? Exam Help |
| Add WeChat edu_assist_pro ii. What is the worst-case running time to insert a key into a skip list? |
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| iii. After we insert a value https://eduassistpro.github.io/ |
| iv. Recall the dynamic $\frac{1}{2}$ \frac |
| v. We can use network flow to solve maximum bipartite matching. Suppose there are $2n$ nodes and m edges in the bipartite graph G . What is the runtime to find maximum bipartite matching in G ? |

vi. Provide a short proof: Let f be an s-t flow and (A,B) be an s-t cut. Then $v(f)=f^{out}(A)-f^{in}(A)$, where v(f) is the value of the flow being sent out from s.

Problem 2. (25 points) Use Ford-Fulkerson algorithm to solve the max-flow problem based on the following network where the capacity of each edge has been labeled.

- (15 pts) Draw, separately, the residual graph when you *cannot* find any augmenting path any more (i.e., when Ford-Fulkerson algorithm stops).
- (5 pts) Draw the max-flow on th running Ford-Fulkerson. S
- (5 pts) Draw/Indicate the cut type://eduassistpro.github.io/



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Problem 3. (25 points) A subsequence is a sequence that can be derived from another sequence by deleting characters without changing the relative ordering of the remaining characters. For example, "ABD" is a subsequence of "ACBFDG". The longest common subsequence (LCS) problem asks for the longest subsequence that is common to both input strings. For example, let $s_1 = \text{``}ACBFDG$ " and $s_2 = \text{``}CAXBFWG$ ". The longest common subsequence of s_1 and s_2 is "CBFG".

Design a dynamic programming algorithm to find the LCS between two input strings. Briefly explain why your algorithm is correct and provide runtime analysis.

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Problem 4. (25 points) You are designing an exam for a class. You have a collection of problems $P = p_1, ..., p_n$. Each problem has an estimated time $t(p_i)$ in minutes that you think it will take a prepared student to answer. Each problem also has a quality score $q(p_i)$ that is your estimation of how good a problem it is (higher $q(p_i)$ means a better problem). Your class will have K minutes to take the exam.

- i. (25 pts) Design a dynamic programming algorithm to select a subset of problems from P such that: (1) the total time to take the test is K, and (2) the sum of the qualities of the selected problems is as large as possible.
- ii. (Extra credit 15 pts) Novtsupos i / eduassist projection of "concepts" $C = \{1, \ldots, m\}$ i = 1 namic programming"), and each problem tests one concept $v(p_i) \in C$ (for example, problem p_1 might test concept $v(p_1) = 1$ "network flow" Design a dynamic programming resurrence that select caps not brother from P that (1) can be completed in P minutes, (2) tests every concept in P at least once (it can test a concept more than once), and (3) maximizes the sum of the qualities of the selected proble |C| is a small constant.

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For both questions, briefly describe why the algorithm is correct and provide run

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