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CO580 Algorithms

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### Asymptotic Notation

Algorithm performance is often expressed using asymptotic notation which

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- The s
- \* A funt the state of the state
  - $\Omega(g)$  if g is an asymptotic lower bound for f;

•  $\Theta(g)$  if g is an asymptotically tight bound f where Gaharkers fundant edu\_assist\_property of the standard edu\_assist\_property of the

- The definitions of O,  $\Omega$  and  $\Theta$  are broad coefficients are not significant.
- So, (A) and (B) above are both in O(N), but (C) and (D) are not because they grow too fast.

Big O: Upper Bound

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$$O(g(N)) = \left\{ egin{array}{ll} f(N) \mid & ext{there are positive constants $c$ and $n_0$} \\ & ext{such that } 0 \leq f(N) \leq c \, g(N) ext{ for all } N \geq n_0 \end{array} 
ight. 
ight.$$

Big Omega: Lower Bound

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$$\Omega(g(N)) = \left\{ \begin{array}{cc} f(N) \mid & \text{there are positive constants } c \text{ and } n_0 \\ & \text{such that } 0 \leq c \, g(N) \leq f(N) \text{ for all } N \geq n_0 \end{array} \right\}$$

Big Theta: Tight Bound

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$$\Theta(g(N)) = \left\{ egin{array}{ll} f(N) \mid & ext{there are positive constants $c_1$, $c_2$ and $n_0$} \\ & ext{such that} \\ & 0 \leq c_1 \, g(N) \leq f(N) \leq c_2 \, g(N) ext{ for all } N \geq n_0 \end{array} 
ight\}$$

#### Asymptotic Notation

# Assignment Project Examine Milelp

- T(
- (rat https://eduassistpro.github.)
  Also, even t
  (abusively) applied to algorithms too.
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We use the same notation to talk about other resources:

• We say "the space complexity of MergeSort is  $\Theta(N)$ "

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### Space Complexity

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- $\Theta(1)$  space for the best case
- $\bullet$   $\Theta(1)$
- <sup>o(1</sup>https://eduassistpro.github.

"1" is the no

- The space used by the input is ignored
   If not the dolld Mask Conference due County assist\_presented the conference of the conference o
- SimpleSearch only needs space for a few local variables (e.g. a loop counter). This does not depend on N.

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#### Better Search

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- You have already seen Binary Search. edu\_assist\_pr
- It uses the fact that elements are ordered.
- Checking an element in the middle means you can discount half the remaining data.

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Binary Search: Design

# Assignment Project Exam Help Binary Search creates regions in a. What properties should the algorithm

maintain f

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#### Loop Invariants: A Design Tool

A loop invariant is a property that is true before every iteration of a loop.

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In Binary Search we assert that:

- Elements left of index I are known to be less than k;
- Elements at index r or above are known to be greater than k;
- so a[1, ..., r-1] is unsearched.

#### Loop Invariants

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initialisa

mainten

https://eduassistpro.github.i termination When the loop ends the invariant implies a useful property of

the algorithm

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• The three conditions help see how (and if) it would work in detail

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#### **Loop Invariants**

For Binary Search:

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#### **Loop Invariants**

Assignmental left of / are less than k.

Assignmental are less than k.

a[/,...,r] is unsearched

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#### Performance

What is the worst case time complexity of Binary Search?

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Intuition: loop executes log<sub>2</sub> N times.

#### Performance

Alternative: analyse the recursive form of the program.

```
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                                               if (1 \ge r)
                                           https://eduassistpro.github.
                                                               return True
                                               else if (k < a[m])
                                              else Add WeChat edu assist_properties assist_properties and the control of the co
                                                              return BinSearch(a, m+1, r, k)
                                                                                                                                                                                                                                                                                                                                                                        T(N'')
```

- where N' and N'' are numbers left to search
- Exercise: what are N' and N'' in the worst case? Be exact.

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#### Worst Case Recursion

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- m is a way place with e with at edu\_assist\_property is odd: W = W'' e w/2 at edu\_assist\_property is odd: W =
- if N is even: N' = |N/2|, N'' = |N/2| 1
- So the worst case is when k < a[0]
  - If N > 0, will have |N/2| unsearched elements

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#### Performance

```
We now have enough information to write a worst-case formula for T(N) BinSearck(a, I, r, k)
     ຼື ຖ້າກຸ້ຽວ://eduassistໍ້ກາດ.github
     if (k == a[m])
    else Adda We Chat ed assist_preturn Binsearch (a, 1, m, k) ted to assist_preturn Binsearch (a, 1, m, k)
     else
       return BinSearch(a, m+1, r, k)
```