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Nature-Inspired Learning Algorithms (7CCSMBIM)



Introduction

Assignment Project Exam Help Basic Differential Evolution

- DE
- 1 https://eduassistpro.github.
 - Switching DE strategies
 - Hybrid DE trategles Chart edu_assist_pr
 - Evolutionary Algorithm-Based Hybrids
 - Particle Swarm Optimization Hybrids
 - Self-Adaptive Differential Evolution

Learning Objectives



• To get the concept of Differential Evolution and know how it works.

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Differential Evolution (DE) is a *stochastic*, *population-based* search strategy developed by Storn and Price in 1995.

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Notation

- $\mathbf{x}_i(t) = [x_{i1}, \dots, x_{in_r}]$: the i^{th} individual in the population.
- n_x: number of elements in each individual.

ssignment Project Exam Help u_i(t): trial vector

- \mathbf{x}_{i_1} : target vector, $i \neq i$
- \bullet \mathbf{x}_{i} , $(t) \mathbf{x}_{i}$
- x_k(t), x_k β ∈ (0,∞) https://eduassistpro.github.
- $U(0,1) \in [0,1]$: a uniform random variable in the range of 0 and 1.
- $p_r \in [0,1]$: probability of crossover/recombination
- $x_{min} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$ $x_{max} = \begin{bmatrix} x_{max} & x_{max} \\ x_{max} & x_{max} \end{bmatrix}$
- $\hat{\mathbf{x}}(t)$: the best individual from the population at generation t
- $\hat{\mathbf{y}}(t) = [\hat{y}_1(t), \dots, \hat{y}_{n_r}(t)]$: the global best position since the first generation.
- $\mathbf{x}_{\min} = [x_{1_{\min}}, \cdots, x_{n_{\min}}]$: a vector of constants denoting the lower bound of $\mathbf{x}_i(t)$.
- $\mathbf{x}_{\max} = [x_{1_{\max}}, \cdots, x_{n_{\max}}]$: a vector of constants denoting the upper bound of $\mathbf{x}_i(t)$.
- $\mathbf{v}_i = [v_{i1}, \cdots, v_{in_n}]$: a velocity vector.
- $r_{1i}(t), r_{2i}(t) \in [0, 1]$: a random number.
- t: iteration/generation number

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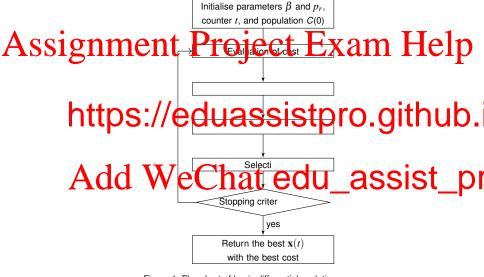


Figure 1: Flowchart of basic differential evolution.

Basic Differential Evolution



Basic Components

- A S Mulation: it is a group of extential solution.

 Help target vector with a weighted differential vector.
 - cro https://eduassistpro.github.
 - Selection: It determines if the parent or the offspring will survive to the next generation.

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Basic Differential Evolution



Differences between Differential Evolution and other evolutionary algorithms

Mutation is applied first before crossover. Mutation generates a trial vector Sold Strenger With the closed Control of Sold and of street D

- Mutation "step sizes" are not sampled from a prior known probability distr diffehttps://eduassistpro.github.
- Cro
- Crossover generates one offspring only.

 Each pared (individual) Cit Cave its after ed. Cultividual) Cit Cave its after ed. Cultividual Cit



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Population

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where n_s https://eduassistpro.github.

c(t) denotes the population at the partial denotes the partial de



Selection for mutation

As significant of target/difference vectors Exam Help

Selectio https://eduassistpro.github.of the offspr



Mutation for each parent

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where

- u_i(t) https://eduassistpro.github.
- $\mathbf{x}_{i_2}(t) \mathbf{x}_{i_3}(t)$: difference vector, $i \neq i_1 \neq$
- x_{i2}(t)A_{i3}(t) drantwy vertection individued u_assist_pr
- $\beta \in (0, \infty)$: scale factor
- $U_I(1,n_s)$: a random integer variable in the range of 1 and n_s
- More than one difference vector can be used.



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Assignment Project Exam Help https://eduassistpro.github. Add WeChat edu_assist_pr $\mathbf{x}_{i_2}(t) - \mathbf{x}_{i_1}(t)$ $\beta(\mathbf{x}_{i_2}(t) - \mathbf{x}_{i_3}(t))$

Figure 2: Mutation operation with beta = 1.5.



Difference vectors

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- Large distance between individuals: individuals should make large step sizes in ord
- sm https://eduassistpro.github.

Basic Differential Evolution



Crossover: It produces an offspring $\mathbf{x}'(t)$ by implementing a discrete recombination of the trial vector $\mathbf{u}(t)$ and the parent vector $\mathbf{x}_i(t)$.

Assignment $X_{ij}(t) = \begin{cases} \text{Project Exam Help} \\ X_{ij}(t) & \text{otherwise} \end{cases}$

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- $x'_{ii}(t)$: the j^{th} element of the offspring vector $\mathbf{x}'_{i}(t)$,
- $u_{ij}(t)$: the j^{th} dement of the trial vector k'(t) if 1, edge as $t = t^{th}$. It the set of element indices that will undergo crossover (the set element).

Basic Differential Evolution



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Crossover: It produces an offspring $\mathbf{x}'(t)$ by implementing a discrete recombination of the trial vector $\mathbf{u}(t)$ and the parent vector $\mathbf{x}_i(t)$.

Assignment $X_{ij}(t) = \begin{cases} x_{ij}(t) & \text{otherwise} \end{cases}$

where of the state of the state

- $x'_{ij}(t)$: the j^{th} element of the offspring vector $\mathbf{x}'_{i}(t)$,
- $u_{ij}(t)$: the j^{th} dement the trial vector k'(t) if 1, equiv = 0 U. It the set of element indices that will undergo crossover (the set equiv = 0).

Example:
$$n_x = 3, J = [1, 3]$$

 $\mathbf{u}_i(t) = \left[u_{i1}(t), u_{i2}(t), u_{i3}(t)\right]$
 $\mathbf{x}_i(t) = \left[x_{i1}(t), x_{i2}(t), x_{i3}(t)\right]$
 $\mathbf{x}'_i(t) = \left[u_{i1}(t), x_{i2}(t), u_{i3}(t)\right]$



Binomial crossover: The crossover points are randomly selected from the set of

1, 2, ..., n_x Assignment Project Exam Help

Algorithm & Binomial Crossover for Selecting Crossover Points

```
J \leftarrow \{\};
i^* \sim U_I(1,
for each j https://eduassistpro.github.
      J \leftarrow J \cup \{i\}:
   end
```

end

Add WeChat edu_assist_pr • $U_I(1,n_x) \in \{1,2,\ldots,n_x\}$: a random integer variable in the range of 1 and n_x

- $U(0,1) \in [0,1]$: a uniform random variable in the range of 0 and 1
- $p_r \in [0,1]$: probability of crossover/recombination

Remark: $j^* \sim U(1, n_x)$ is to make sure that at least one crossover point is selected.



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Exponential crossover: It selects a sequence of adjacent crossover points from a randomly selected index, treating the list of potential crossover points as a circular

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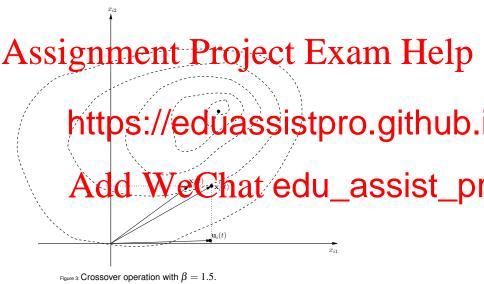
Algorithm 2: Exponential Crossover for Selecting Crossover Points

```
J \leftarrow \{\};\ j \sim U_I(0,n_x) repeat J \leftarrow J https://eduassistpro.github.until U(0,1) \geq p_r or |J| = n_x;
```

- $U_I(0, nA_1 \bigcirc 0 1, W_r$ each arteged u_assist_property and $n_x 1$
- $p_r \in [0,1]$: probability of crossover
- |J| is the number of elements in the set J.
- mod: Modulus (modulo) operator, e.g., 12 mod 5 = 2 (remainder of 12/5)

Remark: The list of potential crossover points is treated as a circular array in $j=(j+1) \bmod n_x$.







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Algorithm 3: General Differential Evolution Algorithm

```
Set the generation counter, t = 0;
Initialize the control parameters, \beta and p_r; and the control parameters of the control parameters of the control parameters. The control parameters of the control parameters of the control parameters of the control parameters of the control parameters.
while stopping condition(s) not true do
     for each individual, \mathbf{x}_i C(t) do
          chttps://eduassistpro.github.
               Add \mathbf{x}'_i(t) to C(t+1);
          <sup>₽</sup>Add∘WeChat edu_assist_pr
     end
     t \leftarrow t + 1
end
```

Return the individual with the best fitness as the solution;

```
Tinitial population: \mathbf{x}_i(0) \sim U(x_{\min,j}, x_{\max,j}) where \mathbf{x}_{\min} = \begin{bmatrix} x_{\min,1} & x_{\min,2} & \cdots & x_{\min,n_x} \end{bmatrix} and \mathbf{x}_{\max} = \begin{bmatrix} x_{\max,1} & x_{\max,2} & \cdots & x_{\max,n_x} \end{bmatrix} define the search boundaries.
```

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Variations to the basic Differential Evolution strategies:

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Diff

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Notation: DE/x/y/z

- x: the nethod of selecting the target vector edu_assist_properties by: the number of difference vectors used
- z: the crossover method used
 - bin: Binomial crossover
 - exp: Exponential crossover



Some common DE strategies

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- * DE/rhttps://eduassistpro.github.
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DE/rand/1/z: This is the basic DE introduced before.

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- Number of difference vectors is 1.
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Trail vector:

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DE/best/1/z:

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- Number of difference vectors is 1.
- ^{• Any} https://eduassistpro.github.

Trail vector:



 $DE/x/n_v/z$:

Assume the control of the control of

Any c

Trail vectohttps://eduassistpro.github.

 $\mathbf{Add}^{\mathbf{u}_{i}(t)} = \mathbf{x}_{i_{1}}(t) + \beta \sum_{k=0}^{\infty} (\mathbf{x}_{i_{k},k}(t) - \mathbf{x}_{i_{k}}(t)) - \mathbf{x}_{i_{k}}(t) - \mathbf{x}_$



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DE/rand-to-best $/n_v/z$:

Assing patients the rand and best strategies. Assing patients to be strategies. Assing patients are the rand and best strategies.

Any crossover methods can be used.

Trail vecto

 $\mathbf{u}_{i(t)}$ https://eduassistpro.github.

where $\gamma \in A$ 10 color of the larth attractor assist_pr operator.

- $\gamma \rightarrow 1$ favours exploitation.
- $\gamma \rightarrow 0$ favours exploration.
- Adaptive $\gamma(t)$ can be used: The value of $\gamma(t)$ increases from $\gamma(0)=0$ with each new generation towards the value 1.



DE/current-to-best/ $1 + n_v/z$:

- As Summer difference vectors is 10^{11} . For this Lifterence vector is formed p the parent vector and the best individual $\hat{\mathbf{x}}(t)$ from the current population.
 - ^{• Any} https://eduassistpro.github.

Trail vector:

u_i(t) Add(xWeChatkiedu_assistns_pr

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Switching DE strategies

Assignment Project Exam Help Evolutionary algorithm-based hybrid DE

- Self_https://eduassistpro.github.
 - Self-adaptive parameters

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Switching DE strategies



Empirical studies:

A Spin mental property (exploration).

(exploitation).

Switching https://eduassistpro.github.

strategy.

- ps,1: Abdid that /ed/hatiledu_assist_pr
- $p_{s,2}=1-p_{s,1}$: probability that DE/current-to-best/2/bin will be applied.
- $p_{s,1}$ and $p_{s,2}$ are needed to be computed in each generation.



Assignment $p_{s,1} = \frac{n_{s,1}(n_{s,2} + n_{f,2})}{(Project^{n_s}Ex^2)}$ Help

- \bullet $n_{s,1}$ for Dhttps://eduassistpro.github.
- Initial probability: $p_{s,1} = p_{s,2} = 0.5$
- Learn A de de FW & 50 hats @ du_assist_pr $p_{s,1} = p_{s,2} = 0.5$ to choose which DE strategy i and record (the average) $n_{s,1}$, $n_{s,2}$, $n_{f,1}$ and $n_{f,2}$.

Switching DE strategies



•

After the learning period, choose the DE strategy to be applied to the i^{th} individual according to the following algorithm.

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Algorithment Switching Differential Evolution Algorithm

Compute $r \sim U(0,$

 $\int_{0}^{\inf r < \hat{p}_{s,1}} https://eduassistpro.github.$

| DE/current-to-best/2/bin is applied;

end

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Hybrid DE strategies



Gradient-based hybrid DE

- As Slage and using gold best individual toward obta
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local optima by increasing population diversity.

Gradient-Based Hybrid Differential Evolution

Return the individual with the best fitness as the solution:



Algorithm 5: Hybrid Differential Evolution with Acceleration and Migration

```
Set the generation counter, t = 0;
Initialize the control parameters, \beta and p_r;
resident mention parameters, part project as Exam Help
    Apply the migration operator if necessary:
    for ea
       https://eduassistpro.github.
       if f(\mathbf{x}_i'(t)) is better than f(\mathbf{x}_i(t)) then
           Add \mathbf{x}'_i(t) to C(t+1);
                d WeChat edu_assist_pr
       end
    end
    Apply the acceleration operator if necessary;
    t \leftarrow t + 1
end
```



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Acceleration operator:

$\underbrace{Assignm^{(t)}}_{\text{where}} \underbrace{\overset{\int \hat{\mathbf{x}}(t+1)}{\mathbf{p}}}_{\text{t-1}} \underbrace{\overset{f \cdot \hat{\mathbf{x}}(t+1)}{\mathbf{p}}}_{\text{t-1}} \underbrace{\mathsf{Exam}}_{\text{where}} \mathbf{Help}$

- x̂(t) d
 mutati
- $\begin{tabular}{l} \bullet \begin{tabular}{l} \hat{\textbf{x}}(t+) \\ \bullet \begin{tabular}{l} \hat{\textbf{x}}($
- η(t) ∈ (0,1] is the learning rate (step size). If the gradient descent ste
 vector, x(i), with better ceet, the Jearning rate is reduced by a factor.
- vector, $\mathbf{x}(t)$, with better cost, the Jeanning-rate is reduced by a factor. $\forall \textit{f} \text{ is the state tof ne cost vector.}$
 - ullet The new vector, $\mathbf{x}(t)$, replaces the worst individual in the new population, C(t+1) (if $\mathbf{x}(t)$ is better than the worst individual).

Remark: When using gradient descent, it can speed up the search but the disadvantage is that the

DE may get stuck in a local minimum, or prematurely converge. It can be alleviated by the migration

operator which increases the population diversity.

Gradient-Based Hybrid Differential Evolution



Migration operator:

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where r_{ij} https://eduassistpro.github. Spawne

 $x_{\min,j}$ \hat{x}_j $x_{\max,j}$ Bounds: $x_{\min,j} \le x_{ij} \le x_{\max,j}$

Gradient-Based Hybrid Differential Evolution



The migration operator is applied only when:

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$\underset{\text{where } \varepsilon_1 > 0 \text{ and } \varepsilon_2 > 0 \text{ are, respectively, the } tolerance for the population diversity and } \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} \underbrace{\sum_{i=1, \mathbf{x}_i(t) \neq \hat{\mathbf{x}}_i(t) j=1}^{l_{\mathbf{x}_i(t)}} l_{ij}(t)}_{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) j=1}^{l_{\mathbf{x}_i(t)} = 1, \mathbf{x}_i(t) j=1}^{l_{\mathbf{x}_i(t)} l_{ij}(t)}$

$$\mathbf{x}_1 = \begin{bmatrix} x_{11} \\ \mathbf{x}_2 = \end{bmatrix} \mathbf{x}_{21}$$
 https://eduassistpro.github.

The migration operator is applied only when the diversity of the current population becomes too small, i.e.,

$$\underbrace{\frac{\mathsf{exclude}\, \mathbf{x}_i(t) \neq \mathbf{\hat{x}}(t)}{I_{11}(t) + I_{12}(t) + \cdots I_{ij}(t) \cdots + I_{n_s n_x}(t)}_{n_x(n_S - 1)}}_{= \mathsf{exclude}\, \mathbf{x}_i(t) \neq \mathbf{\hat{x}}(t)} < \varepsilon_1$$

Evolutionary Algorithm-Based Hybrids



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Three variations:

1. Use DE reproduction process as a crossover operator in a simple GA.

2 Said to Fiduli (a) Albori minimulation (perators is Xseq to make C) DE population diversity by adding noise to the created trial vectors.

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added noise.

- 3. Rank-based prossover and mutation operators

 Park-la ed elector is used to ded which multiply a SSIST_DI calculate difference vectors
 - At each generation, the cost of each individual in the population will be evaluated after crossover and mutation operations.
 - Individuals are arranged in ascending order: $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_{n_c}$ where $f(\mathbf{x}_1) \leq f(\mathbf{x}_2) \leq \cdots f(\mathbf{x}_{n_s})$ (assuming minimisation problem)
 - Note: crossover operation is performed before mutation operation.



Algorithm 6: Rank-Based Crossover Operator for Differential Evolution

```
Rank all individuals in ascending order of cost (assuming in missation): Help r \sim U(0,1); \mathbf{x}_i'(t) = \mathbf{if} f(\mathbf{x}_i') + \mathbf{x}_i'(t) = \mathbf{x}_i'' as https://eduassistpro.github.
```

Evolutionary Algorithm-Based Hybrids



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Algorithm 7: Rank-Based Mutation Operator for Differential Evolution

Rank all individuals in ascending order of cost (assuming minimisation);

for $i = 1, 2, ..., n_s$ do

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https://eduassistpro.github. $|x_{ij}(t) = x_{ij}(t) - (x_{ij} - x_{\min,j})r_3e^{-t/t};$

end d 🔥

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- x_i is the x_i after crossover
- *t* is the current generation number
- n_t is the maximum number of generations
- ullet $r_2 \sim \{0,1\}$ means r_2 randomly takes either 0 or 1

Remark: Elitism is implemented, i,e., \mathbf{x}_1 does not mutate as $p_{m,1} = 1$ ($r_1 > p_{m,1}$ will never be satisfied in the above algorithm).

Dr H.K. Lam (KCL) Differential Evolution



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```
Algorithm 8: Rank-Based Differential Evolution
```

```
Set the generation counter, t = 0;
Initialize the control parameters, \beta and p_r; are violated Exam Help
while stopping condition(s) not true do
   for each individual, x;
                    C(t) do
      https://eduassistpro.github.
         Add \mathbf{x}'_i(t) to C(t+1);
      else
      Add WeChat edu_assist_pr
   end
   t \leftarrow t + 1
end
```

Return the individual with the best fitness as the solution;



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Two variations:

1. Switching between Particle Swarm Optimisation and Differential Evolution strategies.

Sign of the Company of

Upda

https://eduassistpro.github.

where $i=1,2,\ldots,n$ where $i=1,2,\ldots,n$ where $i=1,2,\ldots,n$ where $i=1,2,\ldots,n$ where $i=1,2,\ldots,n$ where $i=1,2,\ldots,n$ and $i=1,2,\ldots,n$ where $i=1,2,\ldots,n$ denotes the personal set $i=1,2,\ldots,n$ and $i=1,2,\ldots,n$ denotes $i=1,2,\ldots,n$ and $i=1,2,\ldots,n$ denotes $i=1,2,\ldots,n$ and $i=1,2,\ldots,n$ denotes $i=1,2,\ldots,n$

The offspring $\mathbf{y}_i'(t)$ replace the personal best $\mathbf{y}_i(t)$ if $f(\mathbf{y}_i'(t)) < f(\mathbf{y}_i(t)), i=1,2,\ldots,n_s$ (assuming minimisation).

Self-Adaptive Differential Evolution



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Two approaches:

1. Dynamic Parameters

A Spreadility of recombination (in Rinor lia Crossover): $p_t(t)$ Exam Help Scale factor (in Mutation): $\beta(t) = \beta(t-1) - (\beta(0)-0.5)/n_t$ where,

2. Self-A

https://eduassistpro.github. $\max_{()=\max_{\{\beta_{\min},1-\left|\frac{f_{\min}(t)}{f_{\max}(t)}\right|\}}\text{ other}$

- . p. Add min i we Chataedu_assist_pr
- max(·) is the maximum operator
- $f_{\min}(t)$ and $f_{\max}(t)$ are respectively the minimum and maximum cost values for the current population, C(t)
- As $f_{\min}(t)$ approaches $f_{\max}(t)$, the diversity of the population decreases, and the value of $\beta(t)$ approaches β_{\min} which is to ensure smaller step sizes when the population starts to converge, otherwise larger step size to favour exploration