# Data Mining and Machine Learning

Assignment Project Exam Help

Page Ran

https://eduassistpro.github.io/

Add WeChat edu\_assist\_pro

Peter Jančovič

### Objectives

- To understand the basic idea of the PageRank of a document in a corpus
- To understand now to calculate PageRank
- To understa https://eduassistpro.githubab/underlies
   PageRank
   Add WeChat edu\_assist\_pro

# Not all documents are equal

- So far, whether or not a document d is retrieved in response to a query q depends only on sim(q,d)
- Assignment Project Exam Help
   Assumption is that all documents are equal relevance of https://eduassistpro.gfthdepends only on the similarity score

  Add WeChat edu\_assist\_pro

  This is clearly not true (co ipedia with my
- home page)
- Prior importance of a document is its Page rank
- Probabilistic interpretation of Page rank

# The *prior* probability of a document

- Suppose that we could assign a probability P(d) to each document d in our corpus
- Think of P(a) as the probability that a is a relevant document b https://eduassistpro.giahalleity/q
- In this case, whether d is returned in response to a query q depends on sim(q,d) and P(d)
- We will treat P(d) as the Page rank of d

## Retrieval using prior probabilities

- Retrieval based only on sim(q,d) assumes that P(d) is the same for all documents
- This case is called equal priors
- Intuitively w https://eduassistpro.gitbolblebestimate more meaningful priors Add WeChat edu\_assist\_pro
- Assumption: the *prior* relevance of a document to any query is related to how often that document is accessed

#### Citation indices

- Similar idea used to measure quality of academic papers
- If a paper p contains important results or ideas, then lots of papers with resignment Project Exam Help
- The <u>citations i</u> <u>https://eduassistpro.github.io/</u>ers refer to a given paper p
- Citations index 43 dotang Ghat edu\_assiste proesearch assessment
- But, quality of a paper depends not only on the <u>quantity</u> of papers that cite it but on their <u>quality</u> – their citation indices

# Basics of Page Rank

- The ranking of a documen onse to q depends on both sim(q,d) and pr(d)
- But not all links are equal

#### The "Random Surfer Model"

- The solution is to allocate a <u>weight</u> of  $w_{de}$  to the hyperlink from document d to document e
- $w_{de}$  can be thought of as the probability of following the link to p https://eduassistpro.gift@bdo/
- If l(d) denotes the number assist proper setting  $w_{de} = 1/l(d)$  corres e random surfer model: on any page any of the available links are chosen with equal probability

#### The "Intentional Surfer Model"

- In reality all links on a page are not clicked with equal probability
- A better alternative is to estimate the w<sub>de</sub>s using actual statist
- This is the in https://eduassistpro.github.io/
- Organizations (I assume!)

# Simplified Page Rank Calculation

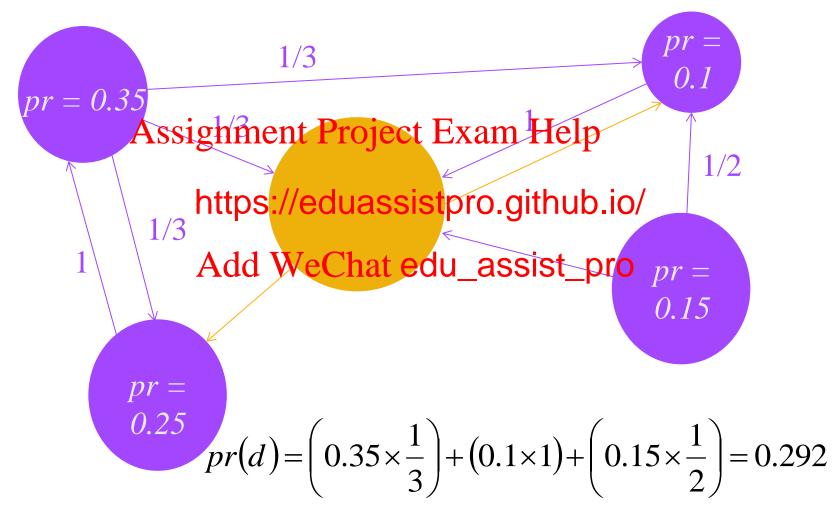
- Once pr(d) is accepted as a measure of the importance of d there is a natural consequence
- In the calculation of pr(d), a hyperlink from a page  $d_1$  to d shoul  $d_2$  to d https://eduassistpro.github.io/
- This motivatexid WeChat edu\_assist\_pro

$$pr(d) = \sum_{e \in L(d)} pr(e) w_{ed}$$

where L(d) is the set of pages which link to page d

This is the <u>simplified Page rank</u> calculation

# Simplified Page Rank Calculation



# Example

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu\_assist\_pro

Taken from wikipedia: see http://en.wikipedia.org/wiki/PageRank

# Simplified Page Rank Calculation

- Of course, changing pr(d) will change the Page Ranks of the other pages, which in turn will change pr(d).... Assignment Project Exam Help
- Hence the d https://eduassistpro.gifh@c.wsive, and pr(d) is calculated iterativ Add WeChat edu\_assist\_pro

$$pr_{n+1}(d) = \sum_{e \in L(d)} pr_n(e) w_{ed}$$

# Markov Chain interpretation

Let

$$W = \begin{bmatrix} w_{11} & w_{12} & \cdots & w_{1D} \\ w_{21} & w_{22} & \cdots & w_{2D} \end{bmatrix}$$

$$W = \begin{bmatrix} w_{d1} & w \\ w_{d1} & w \\ \text{Assignment Project Exam Help} \\ \text{https://eduassistpro.github.io/} \\ w_{D1} & w_{D2} & \cdots & w_{DD} \end{bmatrix}$$

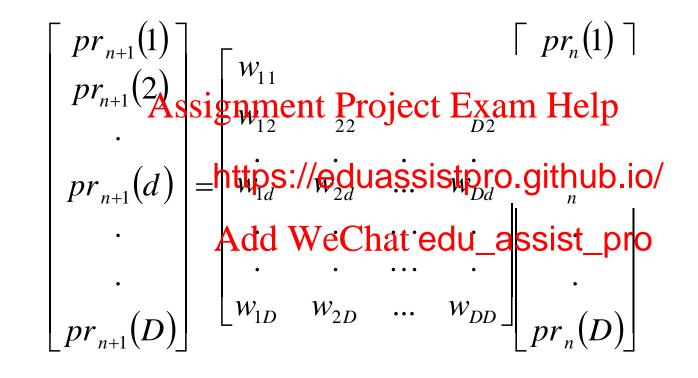
where  $w_{ij}$  is the probabilit following a hyperlink between the  $i^{th}$  and  $j^{th}$  pages and D is the number of pages – this is the page transition probability matrix

Notice that each row of W sums to 1

# Markov Chain interpretation

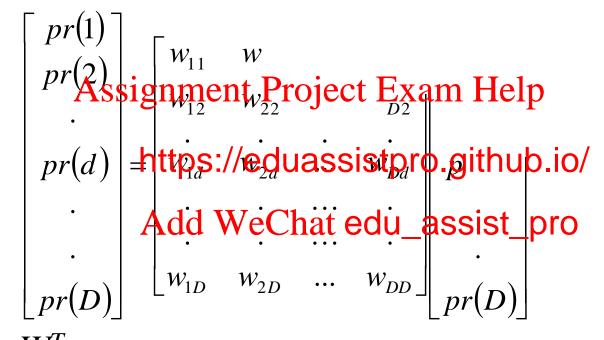
- Let  $pr_n^T = [pr_n(1), pr_n(2), ..., pr_n(D)] pr_n(i)$  is the Page Rank of the  $i^{th}$  page after n iterations
- Then  $pr_{(nA)} = W^T pr_{pr}$  or  $pr_{pr} = (W^T)^n pr_{pr}$
- In Markov C is the <u>transition</u> probability f https://eduassistpro.github.io/
- Can think of Mcda Weelput edu\_assistppge e at time t+1 given page d at time t: P(e @ t+1 | d @ t)
- $pr_n$  is an estimate of the probability distribution over all of the pages after the  $n^{th}$  iteration
- In this case  $\sum_{d} pr_n(d) = 1$

# Markov chain interpretation



# Markov Chain interpretation

If this system converges, then



- $pr = W^T pr$
- In other words pr is an <u>eigenvector</u> of  $W^T$  with eigenvalue 1

### **Damping Factor**

- The model we have used to develop Page Rank is a "random surfer" model with 'proper' hyperlink probabilitiesignment Project Exam Help
- The random https://eduassistpro.gsttopcligking
- The probability that the ractional edu\_assist\_proclicking when he arrives a called the damping factor and denoted by  $\delta$
- A typical value of  $\delta$  is 0.85

#### Page Rank

Taking into account the damping factor,

$$pr(d) = \begin{bmatrix} \frac{1}{2} & \frac{1}$$

where N is the number of documents

#### Notes

- Assuming that p(e) is the probability of the page d,
- then this formula preserves  $\sum_{l} pr(d) = 1$ The formula sissing the Project Variant of P(l) = 1page that has https://eduassistpro.github.io/ non-zero pag
- In addition, the damping ta of past estimates of PageRank on the present estimate

#### **Notes**

- This lecture presents a probabilistic approach to Page rank
- "PageRank" is a trademark of Google
- It was devel https://eduassistpro.git/nerenid/995 and
   1998
   Add WeChat edu\_assist\_pro
- Larry Page is one of the founders of Google Inc.
- A high PageRank is a valuable asset for a www page, for example to attract advertising
- Hence the precise details of the Google PageRank algorithm are secret!