AERO9660 Advanced Propulsion

Assignment N°2 2022.

Q1

van der Waal's equation may be expressed as:

$$P = \frac{\bar{R}T}{\bar{v} - b} - \frac{a}{\bar{v}^2}.$$

At the critical point:

$$\left(\frac{\partial^2 P}{\partial \bar{v}^2}\right)_T = 0 ,$$

and:

$$\left(\frac{\partial P}{\partial \bar{v}}\right)_T = 0.$$

- i)
- Use this fact to derive expressions for a, b in terms of \overline{v}_c , as well as \overline{t} and T. Then insert these expressions for a and b into various wall's equation at the critical ii) point to get \overline{v} , a, and b in terms of \overline{R} , T, and P.

For hydrogen, the critic https://eduassistpro.github.io/ $T_c = 33.3K$,

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- Therefore find a in $\left\{Pa\frac{\left(m^3\right)^2}{kmol^2}\right\}$ and b in $\frac{m^3}{kmol}$. iii)
- For hydrogen, plot pressure (in Pa) against molar specific volume (in $m^3/kmol$) over iv) the range:

$$0 \le P \le 2.5 \times 10^6 Pa$$
$$0 \le \bar{v} \le 1.5 m^3 / kmol$$

for isotherms of 15K, 18K, 21K, 24K, 27K, 30K, $T_c = 33.3K$, 36K and 39K.

(/35) The Redlich-Kwong equation of state may be expressed as:

$$P = \frac{\bar{R}T}{\bar{v} - b} - \frac{a}{\bar{v}(\bar{v} + b)T^{(0.5)}},$$

where:

$$a = 0.42748 \frac{\bar{R}^2 T_c^{2.5}}{P_c},$$

and:

$$b = 0.08664 \frac{\bar{R}T_c}{P_c}.$$

- i) Find a in $Pa\left(\frac{m^3}{kmol}\right)^2 K^{0.5}$ and b in $\frac{m^3}{kmol}$ given that $T_c = 33.3K$ and $P_c = 1.3MPa$.
- ii) Calculate the density of hydrogen if P = 700bar and T = 400K using the Redlich-Kwong equation of state. This is basically the conditions you would find in a typical hydrogen tank on board an aircraft of a car.

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iii) If R = 4.124k ecific volume of hydrogen if P = 700ba https://eduassistpro.github.io/

iv) Predict the density of hydrogen if Z = 1.40

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$$v = \frac{ZRT}{P} = \frac{1}{\rho}.$$

Now you see why we need these other equations of state.

(/35)

The partition function that accounts for the vibrational component of energy storage in a molecule is:

$$Z_v = \frac{1}{1 - e^{-\frac{\theta_v}{T}}},$$

where θ_v is the characteristic vibrational temperature of the molecule and T is the absolute temperature.

Given that the component of the molar specific internal energy due to the vibrational component of energy storage is:

$$\overline{u_{\nu}} = \bar{R}T^2 \left\{ \frac{\partial}{\partial T} (\ln Z_r) \right\}_{\nu},$$

show that:

$$\overline{u_v} = \bar{R}T \frac{x}{(e^x - 1)},$$

where:

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Then as: https://eduassistpro.github.io/

show that:

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$$\overline{c_{p_v}} = \overline{R} \frac{x^2 e^x}{(e^x - 1)^2}.$$

Marks will be deducted for a lack of working.

/30)