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L02 – Bayes Classifier

## Bayesian Decision Theory

- Two classes  $\omega_1, \omega_2$
- Class priors P<sub>1</sub>, P<sub>2</sub> Assignment Project Exam Help
  • Class-co
- $(\omega_i)$  or likelihood
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$$P(\omega_i \mid x) = P_i P(x)$$

where the unconditional density is

$$p(x) = P_1 p(x | \omega_1) + P_2 p(x | \omega_2)$$

## Posterior

The posterior probability

$$P(\omega_i \mid x) = P_i p(x \mid \omega_i) / p(x)$$

is proportional Assignment Project Exam Help

prior \* likhttps://eduassistpro.github.io/

$$P(\omega_1|x) + P(\omega_2|x) = \frac{\text{Add}_P \text{WeChat edu\_assist\_pro}_1}{p(x)} + \frac{p(x)}{p(x)} = \frac{p(x)}{p(x)} = 1$$

Proportionality constant insures normalization

# Bayes Decision Rule

Seems intuitive to choose the most likely class, given the feature measurement vector x and the class priors

If 
$$P(\omega_1|x)$$
 signment, Project Exam Helphoose  $\omega_2$ .

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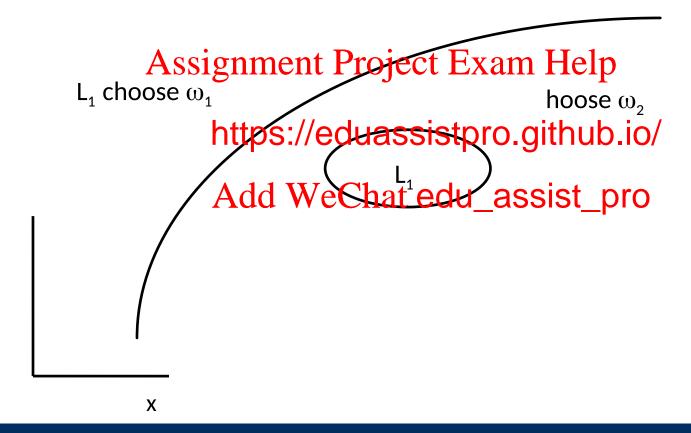
If 
$$p(x | \omega_1) P_1 > p(x | \omega_2) P_2$$
, choose  $\omega_1$ . Otherwise choose  $\omega_2$ .

This is, as we show next, the proper rule to use if we want to minimize the error rate.



## Bayes Error Rate

Bayes decision rule induces a **decision surface** in the feature space --



### Error Rate

### Error rate for the feature vector x is

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$$p(e)$$
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 $w$   $w_1$  Add WeChat edu\_assist\_pro

or

$$P(error \mid x) = \begin{cases} P(\omega_1 \mid x) & x \in L_2 \\ P(\omega_2 \mid x) & x \in L_1 \end{cases}$$

## Minimum Error Rate

### Total error rate is

$$P(error) = \int_{-\infty}^{\infty} P(error \mid x) p(x) dx$$
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=  $\int_{L_1}$  https://eduassistpro.glthub.lo/dx

which is minimize that edu\_assist\_pro

$$P(\omega_1|x) > P(\omega_2|x)$$
 for  $x \in L_1$ 

$$P(\omega_2 | x) > P(\omega_1 | x)$$
 for  $x \in L_2$ 

## Bayes Minimal Error Rule

 Decision rule: Assign x to the class with highest posterior

$$P(\omega_1|x) \stackrel{\omega_1}{\stackrel{>}{\stackrel{>}{\sim}}} P(\omega_2|x)$$

 $P(\omega_1|x) \overset{\omega_1}{\gtrsim} P(\omega_2|x)$ • In terms of learnest Project Exam Help

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$$l(x) = \frac{1}{p(a|a)} > \frac{1}{p(a|a)} (threshold)$$

$$p(a|a) = \frac{1}{p(a|a)} > \frac{1}{p(a|a)} (threshold)$$

Sometimes use log likelihood ratio

$$h(x) = -\log(l(x)),$$
  $h(x) \stackrel{\omega_2}{\underset{\omega_1}{>}} \log\left(\frac{P_1}{P_2}\right) = -\log\eta$ 

# Bayes Decision Surface

e.g. Gaussian class-conditional densities

$$p(x \mid \omega_{i}) = \frac{\text{Assignment Project } \underbrace{\text{Exam Help}}_{\text{exp } - -} (x - \mu_{i})^{\text{P}} \Sigma_{i}^{-1} (x - \mu_{i})}{\text{https://eduassistpro.github.io/}}$$

$$\mu_{i} = \underbrace{\text{Agld}_{x} \text{We}}_{\omega_{i}} \text{Ghat edu\_assist\_pro}$$

$$\Sigma_{i} = \text{cov}[x \mid \omega_{i}] = E[(x - \mu_{i})(x - \mu_{i})^{T} \mid \omega_{i}]$$

#### Bayes Decision Surface for Gaussian Densities

### Likelihood ratio is

$$l(x) = \frac{p(x|\omega_1)}{p(x|\omega_2)} = \sqrt{\frac{\sum_{i=1}^{n} n_i exp^{-i}}{|\Sigma|}} \frac{Project_{i} Exam_{i} Help}{(x-\mu_1)^2 \sum_{i=1}^{n} (x-\mu_2)^2} \sum_{i=1}^{n} (x-\mu_2)^2 \sum$$

its -log is

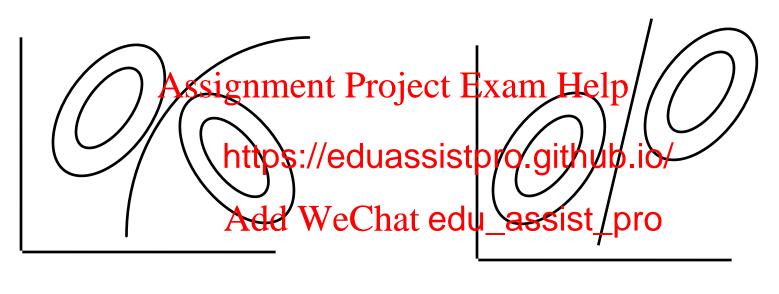
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$$h(x) = -\log(l(x)) = -\frac{1}{2} \log |\Sigma_2| + \frac{1}{2} \log |\Sigma_1|$$

$$+ \frac{1}{2} ((x - \mu_1)^T \Sigma_1^{-1} (x - \mu_1) - (x - \mu_2)^T \Sigma_2^{-1} (x - \mu_2))$$

$$= C + B^T x + x^T M x \qquad quadratic form$$

#### Bayes Decision Surface Gaussian Class Conditional Densities



$$\Sigma_1 \neq \Sigma_2$$

$$\Sigma_1 = \Sigma_2$$

## Generalized Cost

Suppose each of the two classification error types have different cost. What's the ideal decision stra

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