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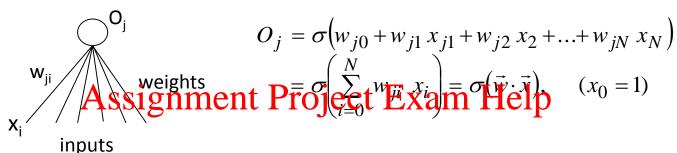
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L19 --- Neural Nets I

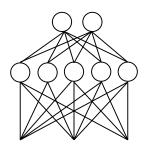
#### What's a Neural Network?

Exceedingly simple processing units.



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#### Characteristics

- Enormous flexibility in maps that can be represented.
- Mapping can be <u>learned</u> from examples.
- Generalize Assignment in Breisteat Lex invaring parameters
- Relatively forgivi
- Extrapolate grac https://eduassistpro.github.io/ Training times c Training times c
- with large datasets.

  Evaluation of learned function is hat edu\_assist\_pro
- Doesn't require programming in target function.
- Success depends on picking appropriate features for inputs x<sub>i</sub>, and representation for output.

### What Are They Good For?

- Enormously flexible, can achieve huge range of maps.
- Mapping can be learned from examples.
- <u>Pattern Classification</u> (statistical pattern recognition)

  - Text-to-speech ment Project Exam Help Handwritten, machine printed (OCR), cursive writing (online) recognition
  - Event dete https://eduassistpro.githhebiso/
  - Medical screening Papnet, adj tional screening, reduces fals Anti-at edu\_assist\_pro http://www.mda. pdf/pap.pdf

(testing on sputum smears too).

- Acoustic front end for speech recognition systems.
- Illegal drug source identification

# What Are They Good For?

- Regression / prediction of continuous-valued systems
  - Time series prediction, e.g. financial forecasting
  - Non-linear regression
- Control
  - Plasmassignmeent Broject Exam Help
  - Chemical p
  - Quality conhttps://eduassistpro.github.io/
  - Trailer truc http://www.handshake.de/user
     Aircraft controller – recovery fr
- Signal Processing
  - Adaptive noise cancellation
  - Adaptive vibration cancellation
  - Image analysis

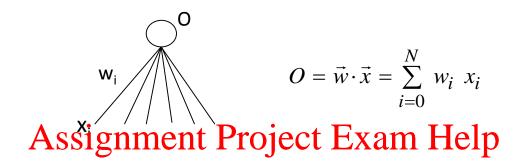
# Why "Neural"?

 Artificial neural network (ANN) function is derived from massive connectivity, real nervous systems are also massively connected.

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ANN units are cartoons of real neurons.
The latter have complex dynamics, and can have tens of thousands of inputs (in cortex).
Real nervous systems have a multitude of neuron types.

## Adaptive Linear Unit (Adaline)



- Training a https://eduassistpro.gitabes.darget values in lea
  - Data: input darget chat edu assist pro
  - Performance metric, or *cost function* mean squared error  $\mathcal{E}(\vec{w}) = \frac{1}{2D} \sum_{d=1}^{D} (t_d O(\vec{x}_d))^2 = \frac{1}{2D} \sum_{d=1}^{D} (t_d \vec{w})^2 = \frac{1}{2D} \sum_{d=1}^{D} (t_d$

#### Linear Unit – Gradient Descent

 Optimization: crawl downhill (steepest descent) on the error surface

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$$\Delta w_{i} = -\eta \frac{\partial \mathcal{E}(\vec{w})}{\partial \mathbf{p}_{i}}: //\hat{\mathbf{e}} d\vec{w} = -\eta \frac{\partial \mathcal{E}(\vec{w})}{\partial \mathbf{p}_{i}}: //$$

So

$$\Delta w_i = \eta \quad \frac{1}{D} \sum_{d=1}^{D} (t_d - O(\vec{x}_d)) \ x_{id}$$

#### Linear Unit – Gradient Descent

 The error function E(w) is <u>quadratic</u> in w, and bounded below by zero. There is unique, global minimum w\*.

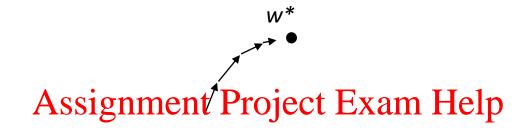
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 Can show that for learning rate η sufficiently small, this algorithm will approach w\* exponentially. How small? Must have

#### Linear Unit – Gradient Descent



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Can show that for real hing rechat edu\_assist properties approach w\* exponentially. How small? Must have

$$0 < \eta < \frac{2}{\lambda}$$

where  $\lambda$  is the largest eigenvalue of the autocorrelation matrix

$$R = \frac{1}{D} \sum_{d=1}^{D} x_d x_d^T$$
 i.e.  $R_{ij} = \frac{1}{D} \sum_{d=1}^{D} x_{di} x_{dj}$ 

### Linear Unit Stochastic Gradient Descent

Gradient descent

$$\Delta w_i = \eta \frac{1}{D} \sum_{d=1}^{D} (t_d - O(\vec{x}_d)) x_{id}$$
 A

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Instead of summing over all data pairs for each update to w, just use one data pair for each u n input/target pair  $\{x_d, t_d\}$  at random from the https://eduassistpro.gfffiub.io/

$$\begin{array}{c|c} \Delta w_i = \eta \left( t_d - O(\vec{x}_d) \right) x_{id} \\ \hline \textbf{Add WeChat edu\_assist\_pro} \end{array}$$

This is the celebrated *Widrow-Huff* or algorithm.

Mean Square)

- Note that the gradient descent (A) is the average of this stochastic gradient descent (B), over all training data.
- The stochastic descent is a noisy version of the true gradient descent.

#### Stochastic vs True Gradient Descent

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gradient descent

### Linear Unit with LMS Training

Used in adaptive filter applications: adaptive noise cancellation and vibration damping, linear prediction problems (linear Fegressian, AR models).

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# Perceptron Classifier

 Early ANN -- Rosenbaltt, Principles of Neurodynamics: Perceptrons and the Theory of Brain Mechanisms, Spartan, 1962.

Single unit with hard-limiter output

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Represents a dichotomy respon

 Input is member of class (+1) or not (-1). Concept is present (+1), or not (-1).

e.g. – Does this picture have a tree in it? This is tough, the inputs x will need to be superbly crafted features.

### Perceptron Classifier - Geometry

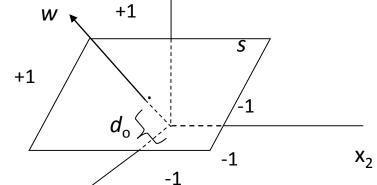
Hypothesis space is space of all possible weights w ( $R^{N+1}$ )

Learning means choosing weight vector w that correctly classifies the training data.

Perceptron weight vector defines a hyperplane s in the

N-dimensional fxhttps://eduassistpro.github.io/

Add WeChat edu\_assist\_pro  $w \cdot x = \sum_{i=1}^{\infty} w_i x_i$   $w \perp s$ 

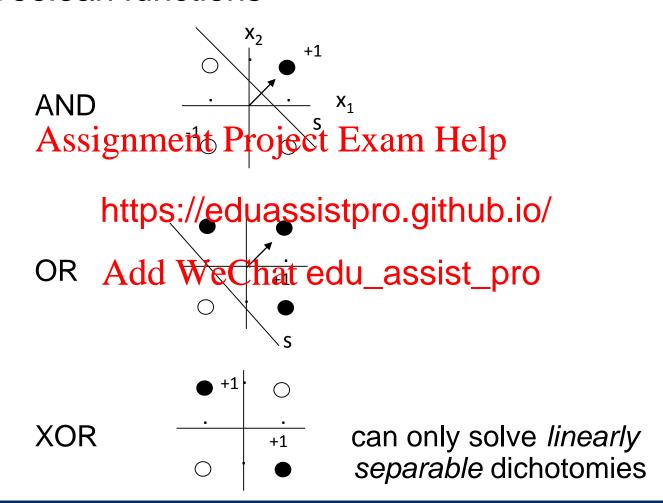


$$d_0 = \frac{-w_0}{|w|}$$

$$O(\vec{x}) = \operatorname{sgn}(\vec{w} \cdot \vec{x})$$

### Perceptron Limitations

#### **Boolean functions**



# Perceptron Learning

- Training data input / target pairs (e.g. pictures with trees, +1 target, and pictures without trees, -1 target) { x<sub>d</sub>, t<sub>d</sub>}
- We want

$$\vec{w} \cdot \vec{x}_d > 0$$
 for  $t_d = +1$ 

$$\vec{w} \cdot \vec{x}_d < 0$$
 for  $t_d = -1$ 

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this is equivale

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$$(w \cdot x_d) t_d > 0$$
 for all data

A given data example Wift Ghatiedu\_assist\_pro $\vec{x}_d$ )  $t_d < 0$ 

- Define cost function  $\mathcal{E}(\vec{w}) = \sum_{misclassified} -(\vec{w} \cdot \vec{x}_d) t_d \ge 0$
- Do stochastic gradient descent on this cost function : If the example  $x_d$  is misclassified, change the weights according to

$$\Delta w_i = \eta \quad t_d \; x_{id}$$

### Perceptron Learning

• If the data are *linearly separable*, this algorithm will converge, in a finite number of steps, to a weight that correctly blaissifies all the training data.

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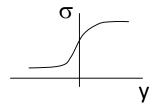
# Soft Threshold Differentiable "Perceptron"

• In order to get past the restriction to *linearly* separable problems, we are going to combine many non-linear neurons. (Why non-linear?)

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 In order to tr introduce a shttps://eduassistpro.github.io/





Smooth, bounded, monotonically increasing.

### Sigmoidal Functions

- Typical choices are
  - Logistic function ment Project, Exam Help

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Hyperbolic tangent

$$\sigma(y) = \tanh(y)$$

# Training the Soft Threshold

Logistic function – targets are {0,1} Hyperbolic tangent – targets are {-1,1}

Cost function

$$\mathcal{E}(\vec{w}) = \frac{1}{2D} \sum_{i=1}^{D} (t_d - O(\vec{x}_d))^2 = \frac{1}{2D} \sum_{i=1}^{D} (t_d - \sigma(\vec{w} \cdot \vec{x}_d))^2$$

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Train by gradient

$$\Delta w_{i} = -\eta \frac{\partial \mathcal{E}(\vec{w})}{\partial w_{i}} \quad \text{https://eduassistpro.github.io/}$$

$$\frac{\partial \mathcal{E}(\vec{w})}{\partial w_{i}} = \frac{1}{D} \sum_{d=1}^{D} (t_{d} - \Delta x_{d}) \frac{\partial \mathcal{W}}{\partial w_{i}} \quad \text{the Charge duoassist}$$

$$= \frac{1}{D} \sum_{d=1}^{D} (t_{d} - O(\vec{x}_{d})) \sigma'(\vec{w} \cdot \vec{x}_{d}) \frac{\partial \vec{w} \cdot \vec{x}_{d}}{\partial w_{i}} = \frac{1}{D} \sum_{d=1}^{D} (t_{d} - O(\vec{x}_{d})) \sigma'(\vec{w} \cdot \vec{x}_{d}) x_{di}$$

So

$$\Delta w_i = \eta \ \frac{1}{D} \sum_{d=1}^D (t_d - O(\vec{x}_d)) \ \sigma'(\vec{w} \cdot \vec{x}_d) \ x_{id}$$

# Training the Soft Threshold

We have the gradient descent rule

$$\Delta w_i = \eta \quad \frac{1}{D} \sum_{d=1}^{D} (t_d - O(\vec{x}_d)) \quad \sigma'(\vec{w} \cdot \vec{x}_d) \quad x_{id}$$
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except for slo

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Stochastic gra

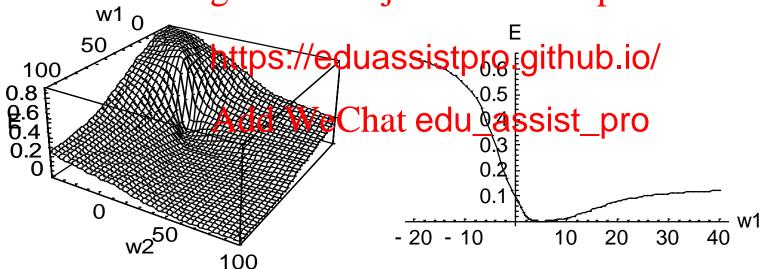
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$$\Delta w_i = \eta \ (t_d - O(x_d)) \ \sigma'(\vec{w} \cdot x_d) \ x_{id}$$

Note that if we get up onto the flat "rails" of the sigmoid, then the slope  $\sigma$  gets very small, and the gradient of the cost function gets very small → slow progress.

#### Cost Function

 The cost surface is now not a simple parabolic function, but instead is more complex looking.

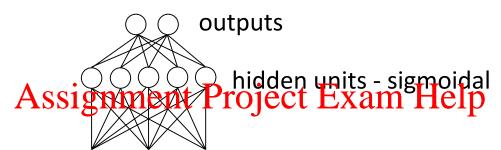
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### Workhorse Neural Networks Multi-Layer Perceptrons (MLP)

Feed forward, layered networks, with sigmoidal hidden units

.



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Can have more than two layers of weights edu\_assist\_pro
Output nodes

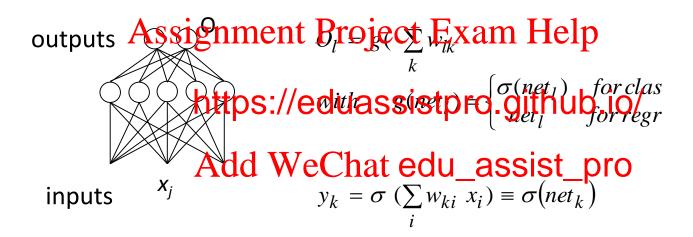
Linear for regression, time series prediction, other problems needing full range of real values in output.

Sigmoidal for classification problems.

Number of inputs, number of outputs determined by problem. Number of hidden units is an <u>architectural parameter.</u>
More hidden nodes → more functions available.

### MLP Output

Signal propagation (forward pass, bottom-up)



### Example Uses

- Classification e.g. from text fig 4.5. Able to produce <u>non-linear</u> class boundaries.
- Fisher Iris data:

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### Example Uses

Non-linear regression



#### Gradient Descent in MLP

Cost function as before:

number of outputs 
$$\mathcal{E}(\vec{w}) = \frac{1}{2D} \sum_{d=1}^{D} \sum_{m=1}^{N_O} (t_{dm} - O_m(\vec{x}_d))^2$$

• Learning by Gradien ent Project Exam Help  $\Delta w_{ij} = -\eta \frac{\partial \mathcal{E}(\vec{w})}{\partial x_{ij}}$ 

 $\Delta w_{ij} = -\eta \frac{\partial \mathcal{L}(\eta)}{\partial w_{ij}}$  https://eduassistpro.github.io/

- Calculating gr
- Surface can haxe multiple hat edu\_assistoppe may have lower cost than others.
- Local optima are in different basins of attraction; where you end depends on where you start.  $_{\mathcal{E}\,|}$

#### Stochastic Gradient Descent in MLP

As above, but <u>no</u> sum over data pairs *d* 

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$$P_{\text{resplect Exam Help}}^{N_O} (t_{dm} - O_m(\vec{x}_d))^2$$

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Stochastic descent has some robustne etting stuck in
poor local minima. Where you end, depends on where you start,
learning rate, and the order the examples are given.

Can also be faster in clock-time for large data sets. Instead of waiting to accumulate errors from all data before making a weight change, make a small weight change in response to each datum.

### Visualization of Stochastic Gradient Descent

- Different 2-d slices through E(w) for 9-d weight space
  - eg 1 Assignment Project Exam Help

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### Visualization of Stochastic Gradient Descent

– eg 2

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#### Next

- Backpropagation training of MLP.
- · Representation powert Emineral approxim https://eduassistpro.github.io/
- Inductive
- Generalization, under rfitting.
- Bayesian methods for neural networks.

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