Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

L17 --- Nonparametric Classifiers

Non-Parametric Classifiers

Kernel or Parzen Classifiers

The obvious approach is to use a kernel density estimate for each of the class-conditional densities and proceed with a likelihood ratio test

Assignment
$$\sum_{i=1}^{N_1} r_{i} p_{i} ect_x$$
 Exam Help $\frac{\hat{p}(x \mid \omega_1)}{\hat{p}(x \mid \omega_1)} = \frac{\sum_{i=1}^{N_1} r_{i} p_{i} ect_x}{\sum_{i=1}^{N_2} v_{i} ect_x}$ uassist programment $\frac{\hat{p}(x \mid \omega_1)}{\hat{p}(x \mid \omega_1)} = \frac{\sum_{i=1}^{N_1} v_{i} ect_x}{\sum_{i=1}^{N_2} v_{i} ect_x}$

Add WeChat edu_assist_pro

Error estimation – use leave-one-out (se) to set kernel width. Leave-one-out is **cheap** for kernel estimators:

$$\hat{p}_L(x_k) = \frac{1}{N-1} \left[\left(\sum_{j=1}^N \kappa(x_k - x_i) \right) - \kappa(0) \right]$$

KNN Classifiers

Two paradigms:

- KNN density estimates followed by likelihood ratio test
 Assignment Project Exam Help
- Voting KNN. Thhttps://eduassistpro.githubwaen they refer to a KNN classifier.
 Add WeChat edu_assist_pro

For each test sample, select K nearest neighbors from the training data (all classes). The sample is classified according to the majority class of the k neighbors.

Asymptotics for Large N Error Rates for Voting KNN

K=1 Classify the point *x* as the class of its nearest neighbor

$$x \longrightarrow x_{NN} \in \omega_i \implies x \in \omega_i$$

Assignment Project Exam Help The conditional risk is (classification error rate given x and x_{NN})

$$r_1 = \text{Prob}[x \in \omega_1 \text{ and } x_{NN} \in \omega_2 \mid x, x_{NN}] + \text{Prob}[x \in \omega_2 \text{ and } x_{NN} \in \omega_1 \mid x, x_{NN}]$$

$$= P(\omega_1 \mid x) P(\omega_2 \mid x_{NN}) + P(\omega_2 \mid x_{$$

In the limit $N \to \infty$ the data points become closer and closer together, and we can replace $P(\omega_i | x_{NN})$ with $P(\omega_i | x)$ leaving

$$r_1^* = \lim_{N \to \infty} r_1 = 2 p(\omega_1 | x) p(\omega_2 | x)$$

For Odd Number of Neighbors in General

Asymptotically, and for odd number of neighbors, the error rate at *x* becomes

$$r_{2k-1}^* = \lim_{N \to \infty} r_{2k-1} = \sum_{k=1}^{k} \frac{1}{i} \binom{2i-2}{i-1} \left[p(\omega_1 \mid x) \ p(\omega_2 \mid x) \right]^i + \frac{1}{2} \binom{2k}{k} \left[p(\omega_1 \mid x) \ p(\omega_2 \mid x) \right]^k$$

$$\text{Assignment Project Exam Help}$$

$$r_1^* = 2 \ p(\omega_1 \mid x) \ p(\omega_2 \mid x) + 4 \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^2 \text{ assist_pro}$$
 $r_3^* = p(\omega_1 \mid x) p(\omega_2 \mid x) + 4 \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^2 \text{ assist_pro}$
 $r_5^* = p(\omega_1 \mid x) p(\omega_2 \mid x) + \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^2 + 12 \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^3$
 $r_7^* = p(\omega_1 \mid x) p(\omega_2 \mid x) + \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^2 + 2 \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^3 + 40 \left(p(\omega_1 \mid x) p(\omega_2 \mid x)\right)^4$

Bayes vs KNN Error

Recall that the **Bayes risk** at *x* is

$$r_B = \min \left(p(\omega_1 | x), \ p(\omega_2 | x) \right) = \frac{1}{2} \left(1 - \sqrt{1 - 4p(\omega_1 | x) \ p(\omega_2 | x)} \right)$$

or by Taylor series expansion

$$r_B = \sum_{i=1}^{\infty} \frac{1}{i} A_i^2 sign$$
 ment Project Exam Help

and the error rate for https://eduassistpro.githulpaining

$$r_{2k-1}^* = \sum_{i=1}^k \frac{1}{i} \left(\begin{array}{c} 2i - 2 \\ i - 1 \end{array} \right) \text{diam'e Chatx diam'e Line } \left[\frac{1}{2} \text{diam'e Chatx diam'e Line } \right]^k$$

One can use these expressions to find the famous bound

$$r_B \le ... \le r_5^* \le r^* \le r^* \le 2 r$$

Bayes vs KNN Error

Assignment Project Examilielp

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

The KNN bound is tighter than the Bhattacharya bound $\sqrt{\ }$

Error Rate for Even Number of Neighbors

With <u>even</u> number of neighbors, we can have a tie (for two classes). When there's a tie, we don't make a choice. This leads to a slightly lower error rate

https://eduassistpro.github.io/

and a sequence of bounded WeChat edu_assist_pro

$$\frac{1}{2}r_B \le r_2^* \le r_4^* \le r_6^* \le \dots \le r_B \le \dots \le r_5^* \le r_3^* \le r_1^* \le 2 r_B$$

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro