

Factor

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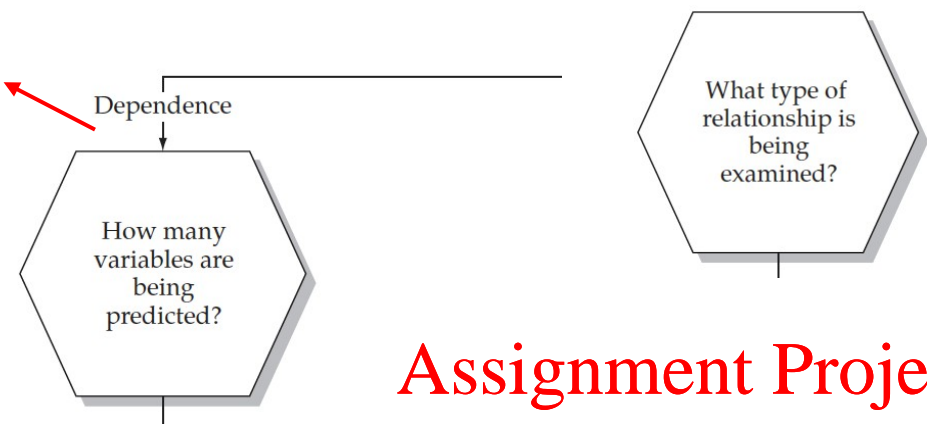
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Ch.3 Multivariate Data Analysis. Joseph Hair et al. 2014. Pearson
Avilash Navlani. 2019. Introduction to Factor Analysis in Python
Jay Narayan. 2019. Multiple Linear Regression & Factor Analysis in R

Interdependence versus Dependence

a variable is identified as the dependent variable to be predicted or explained

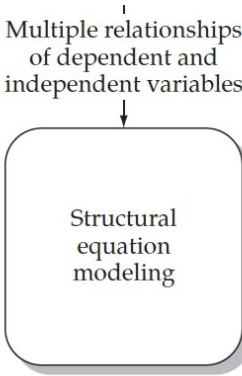


no single variable is defined as being independent or dependent

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Dimensions

Data Matrix M

Each row - an observation in the space (the graph) also called sample
Each column - an attribute, also called dimension

```
np.array(data).shape
```

(150, 4)

150 observations (samples)

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Overfitting

Irrelevant and correlated attributes can even decrease the performance in some algorithms

Factor analysis and PCA play a role in the reduction of these dimensions

Principal Component and Factor Analysis

1

Statistical approaches to analyze interrelationships among a large number of variables and to explain these variables in terms of their common underlying dimensions (factors).

2

The same steps — extraction, interpretation, rotation, and choosing the number of factors or components.

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3

Factor analysis makes assumptions and not. The basic assumption is that there are implicit features responsible for the features of t

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4

FA: we infer the existence of latent variables that explain the pattern of correlations among our observed variables

FA Example

“What underlying attitudes lead people to respond to the questions on a political survey?”

Examining the correlations among the survey items reveals that there is significant overlap across groups of items--questions about taxes tend to correlate with each other, questions about military issues correlate with each other, and so on.

With factor analysis, you can investigate a smaller number of underlying factors. Additionally, you can compute factor scores for each respondent, which can then be used in subsequent analyses. For example, you might build a logistic regression model to predict voting behavior based on factor scores.”

Factor Analysis

Univariate Techniques

a single variable

Multivariate Techniques

a possible correlation between many variables

How to manage these variables?



Factor Analysis

- Examines the interrelationships among a large number of variables and attempts to explain them in terms of their **common underlying dimensions**

factors

- A data reduction technique that does not have dependent and independent variables.

Terminology

Variance

How far the data is spread out

Unique Variance

Variance of the variable is not associated with other variables

Shared Variance

Variance is shared with other variances, creating redundancy in the data

Variate

the linear composite of variables

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Example

Original Correlation Matrix
(no visible patterns)

	V ₁	V ₂	V ₃	V ₄	V ₅	V ₆	V ₇	V ₈	V ₉
V ₁ Price Level	1.00								
V ₂ Store Personnel	.427	1.00							
V ₃ Return Policy	.302	.771	1.00						
V ₄ Product Availability	.470	.497	.427	1.00					
V ₅ Product Quality	.765	.406	.307	.472	1.00				
V ₆ Assortment Depth	.281	.445	.423	.713	.325	1.00			
V ₇ Assortment Width	.354	.490	.471	.719	.378	.724	1.		
V ₈ In-Store Service	.242	.719	.733	.428	.240	.311	.435	1.00	
V ₉ Store Atmosphere	.372	.737	.774	.479	.326	.429	.466	.710	1.00

(Hair et al. 2015. Ch3)

Correlation Matrix in Factor Analysis (three patterns)

	V ₃	V ₈	V ₉	V ₂	V ₆	V ₇	V ₄	V ₁	V ₅
V ₃ Return Policy	1.00								
V ₈ In-store Service	.733	1.00							
V ₉ Store Atmosphere	.774	.710	1.00						
V ₂ Store Personnel	.741	.719	.787	1.00					
	.423	.311	.429	.445	1.00				
	.471	.435	.468	.490	.724	1.00			
	.427	.428	.479	.497	.713	.719	1.00		
V	.302	.242	.372	.427	.281	.354	.470	1.00	
V	.307	.240	.326	.406	.325	.378	.472	.765	1.00

(Hair et al, 2014. Ch3)

Factor 1: *in-store experience*

Factor 2: *product offerings*

Factor 3: *value*

Goal: **Grouping** highly **intercorrelated** variables into distinct sets (**factors**)

Usage: Market research, advertising, finance, operation research etc. (to identify brand features, channel selection criteria...)

Factor Analysis Outcomes

1. **Data summarization** = derives underlying dimensions that describe the data in a much smaller number of concepts than the original individual variables.

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2. **Data reduction** = extends the process of summarization by deriving an empiric (factor score) for each dimension (factor) and then substituting this value for the original values.

The goal of data summarization is achieved by defining a small number of factors that adequately represent the original set of variables

The goal is to retain the **nature and character** of the original variables, but reduce their number to simplify the subsequent multivariate analysis

Types of Factor Analysis

Factor Analysis is **interdependent technique**— no distinction between dependent and independent variables

1. **Exploratory Factor Analysis EFA** is used to discover the factor structure of a construct and examine its reliability. It is data driven.

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2. **Confirmatory Fa** **FA** to confirm the fit of the hypothesized structure to the observed (sample) data. It is theory driven.

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Factor Analysis

Each observable variable is a linear function of independent factors and error term

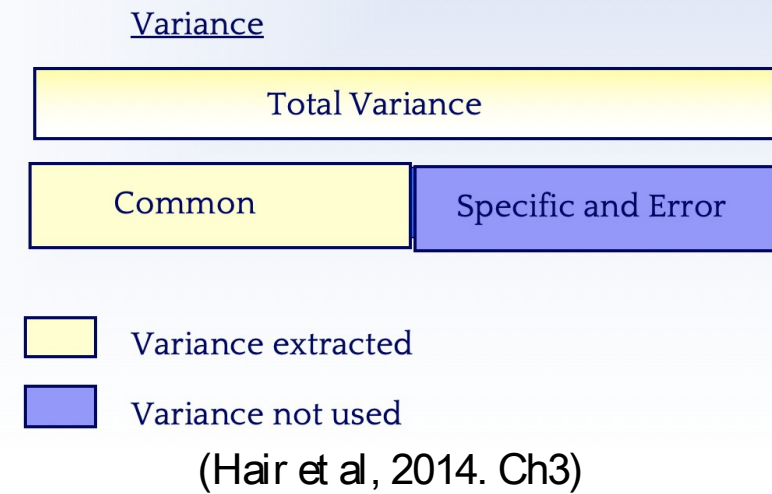
loadings independent factors error term

$$Y_i = \beta_{i0} + \beta_{i1}F_1 + \beta_{i2}F_2 + (1)e_i$$

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The communality of the variable is the part that is explained by the common factors F1 and F2

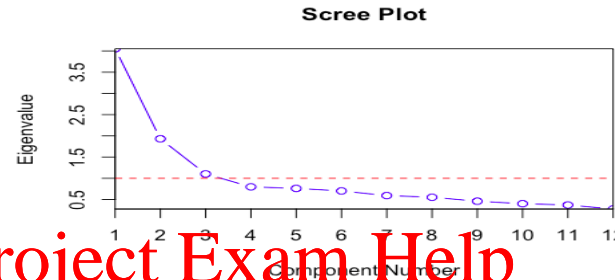
The specific variance is the part of the variance of Y_i that is not accounted by the common factors

Loadings are the weights that the variable has for constructing a factor. The higher the load is, the more relevant in defining the factor's dimensionality.

Two Steps

Factor Extraction

Determine the number of factors: eigenvalue > 1 or “elbow” (Scree plot)



Factor Rotation

The axes
space

rotated within the multidimensional variable

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Varimax Method minimizes the number of variables that have high loadings on each factor.

Factor Analysis in R

Step 1 Data

```
library(readr)
library(psych)
library(tidyverse)
library(Hmisc)
library(car)
data <- read_csv("Factor-Hair-Revised.csv")
```

How many dimensions?

What are the variables types?

What are the variable names?

Remove ID

```
dim(data) 100 x 13
```

```
str(data) all numeric except ID
```

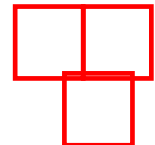
```
-c(1))
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```

Step 2 Correlation Matrix

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```
datamatrix <- cor(data_X)
corrplot(datamatrix, order="hclust", type='upper', tl.srt = 45)
```

1. CompRes and DelSpeed are highly correlated
2. OrdBilling and CompRes are highly correlated
3. WartyClaim and TechSupport are highly correlated
4. OrdBilling and DelSpeed are highly correlated
5. Ecom and SalesFIImage are highly correlated



Factor Analysis in R

Significant Pairs

Step 2 (cont.)

```
res2 <- rcorr(as.matrix(data_X), type="pearson")
# Extract the correlation coefficients
res2$r
# Extract p-values
res2$P
# Insignificant correlations are leav
corrplot(res2$r, type="upper", order
         p.mat = res2$P, sig.level = 0.01, insig = "blank")
```

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Recall Assumptions of Linear Regression: Linearity, Homoscedasticity, Residuals normality, No Multicollinearity

```
model <- lm(Satisfaction ~., data = data_X)
vif(model)
```

VIF (High Variable Inflation Factor) > 2.5

ProdQual	Ecom	TechSup	CompRes	Advertising	ProdLine
1.635797	2.756694	2.976796	4.730448	1.508933	3.488185
SalesFImage	ComPricing	WartyClaim	OrdBilling	DelSpeed	
3.439420	1.635000	3.198337	2.902999	6.516014	

Factor Analysis in R

Step 3 Testing for FA - Kaiser-Meyer-Olkin (KMO)

- Test measures the suitability of data for factor analysis
- KMO values range between 0 and 1
- Value of KMO less than 0.6 is considered inadequate

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```
data_fa <- data_X[,-12]
datamatrix <- cor(data_fa)
KMO(r=datamatrix)
```

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MSA > 0

Factor Analysis is appropriate
on this data

Kaiser-Meyer-Olkin factor adequacy

Call: KMO(r = datamatrix)

Overall MSA = 0.65

MSA for each item =

ProdQual	Ecom	TechSup	CompRes	Advertising	ProdLine
0.51	0.63	0.52	0.79	0.78	0.62
SalesFImage	ComPricing	WartyClaim	OrdBilling	DelSpeed	
0.62	0.75	0.51	0.76	0.67	

Factor Analysis in R

Step 4 Number of Factors

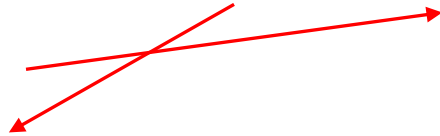
- Calculate eigen values
- Plot eigen values in a scree plot
- Determine Number of factors

```
ev <- eigen(cor(data_fa))  
ev$values
```

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Factor Analysis in R

Step 5 Run Factor Analysis

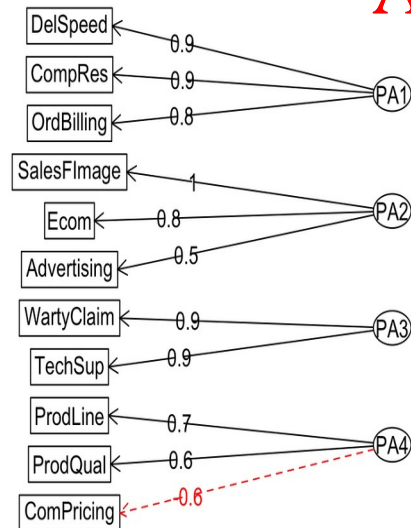
```
nfactors <- 4  
fit1 <- factanal(data_fa, nfactors, scores =  
  c("regression"), rotation = "varimax")  
print(fit1)  
  
fa_var <- fa(r=data_fa, nfactors = 4,  
  rotate="varimax", fm="pa")  
fa.diagram(fanone)
```

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Factor Analysis

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Factor Analysis in R

Step 6 Regression

- Extract scores from factor analysis
- Combine response and predictors
- Label factors

	PA1	PA2	PA3	PA4
[1,]	-0.1338871	0.9175166	-1.719604873	0.09135411
[2,]	1.6297604	-2.0090053	-0.596361722	0.65808192
[3,]	0.3637658	0.8361736	0.002979966	1.37548765
[4,]	-1.2225230	-0.5491336	1.245473305	-0.64421384
[5,]	-0.4854209	-0.4276223	-0.026980304	0.47360747
[6,]	-0.5950924	-1.3035333	-1.183019401	-0.95913571

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```
head(fa_var$scores)
```

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```
regdata <- cbind(data_X[12], fa_var$scores)
#Labeling the data
```

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```
names(regdata) <- c("Satisfaction", "Purchase", "Marketing",
                    "Post_purchase", "Prod_positioning")
```

	Satisfaction <dbl>	Purchase <dbl>	Marketing <dbl>	Post_purchase <dbl>	Prod_positioning <dbl>
1	8.2	-0.1338871	0.9175166	-1.719604873	0.09135411
2	5.7	1.6297604	-2.0090053	-0.596361722	0.65808192
3	8.9	0.3637658	0.8361736	0.002979966	1.37548765
4	4.8	-1.2225230	-0.5491336	1.245473305	-0.64421384
5	7.1	-0.4854209	-0.4276223	-0.026980304	0.47360747
6	4.7	-0.5950924	-1.3035333	-1.183019401	-0.95913571

Factor Analysis in R

Step 6 Regression (cont)

- Split data in train 0.7 and test 0.3
- Train model

```
set.seed(100)
indices= sample(1:nrow(regdata), 0.7*nrow(regdata))
train=regdata[indices,]
test = regdata[-indices,]
```

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```
#Regression Model using train da
model 1 = lm(Satisfaction~., train)
summary(model 1))
```

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Checking for multicollinearity VIF

```
vif(model 1)
```

Purchase	Marketing	Post_purchase	Prod_positioning
1.012217	1.009683	1.009037	1.012533

Factor Analysis in R

Step 7 Prediction

```
library(Metrics)
pred_test1 <- predict(model1, newdata = test, type = "response")

test$Satisfaction_Predicted <- pred_test1
head(test[c(1,6)], 10)
```

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