

# 1 INTRODUCTION TO HEAT TRANSFER

Cengel Chapter 1, or Welty *et al.* p 201-214 or Incropera *et al.* p 1-12

## Learning objectives, *tasks*, readings, Learn ChemE Videos

1. Explain the differences between:
  - a. Conduction
  - b. Convection
  - c. Radiation
  - d. Driving forces, resistances, constants ( $k$ ,  $h$ ,  $\sigma$ )
2. Use the following equations to calculate heat transfer rates and explain the meanings of the terms in each equation:
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  - b. Ne
  - c. Bol
  - d. Learn ChemE – “Heat Tran
  - e. Multi-modal (Learn ChemE
3. *Begin filling in the table of symbols, definitions and units*

By the end of this week you should be able to:

- Determine which modes of heat transfer will be relevant for a given problem, and which are negligible
- Find, reference and use appropriate values of thermal conductivity and emissivity (along with other standard thermal properties of common fluids – e.g. density, heat capacity, etc)
- Set out a solution to a problem based on the method described (end of lecture notes), including diagrams, assumptions, data, analysis, calculations (with appropriate significant figures), and critical review of the answer

## WHAT IS HEAT TRANSFER?

### THERMODYNAMICS

- Energy (heat) can be transferred between system and surrounds.
- Heat goes from hot to cold regions.

**Temperature difference = driving force**

- Deals only with End states (eg at equilibrium).
- Tells nothing about modes or rates of Heat Transfer.

### HEAT TRANSFER

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Example:

You have a 330 mL can of drink, which has density  $1000 \text{ kg m}^{-3}$  and specific heat  $4.2 \text{ kJ kg}^{-1} \text{ K}^{-1}$ . The can has been sitting in your car on a hot day, and is now at  $35^\circ\text{C}$ . You would like to cool it down to  $5^\circ\text{C}$ .

a. how much ice at  $0^\circ\text{C}$  (latent heat of  $334 \text{ kJ kg}^{-1}$ ) is required to cool the can to  $5^\circ\text{C}$ ?

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b. how much water (density  $1000 \text{ kg m}^{-3}$ , specific heat  $4.2 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ) at  $1^\circ\text{C}$  is required to cool the can to  $5^\circ\text{C}$ ?

c. how much air (density  $1.3 \text{ kg m}^{-3}$ , specific heat  $1.0 \text{ kJ kg}^{-1} \text{ K}^{-1}$ ) at  $1^\circ\text{C}$  is required to cool the drink to  $5^\circ\text{C}$ ?

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d. what would <https://eduassistpro.github.io/>  
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# HEAT TRANSFER SYMBOLS AND UNITS

Actions for students:

- complete the units column in the table of symbols, and indicate which variables are vectors; and
- update table of symbols as course progresses.

TABLE OF HEAT TRANSFER SYMBOLS AND UNITS (note – textbooks vary widely!!!)

Symbol		Definition	Units
Study guide	Textbook (Incropera)		
$q$			W
$A$		heat transfer	$m^2$
$T$		temperature	$^{\circ}C$ or K or $^{\circ}F$
$R$		resistance to heat transfer	
$q''$		heat transfer flux	$W/m^2$
Symbol		Definition	Units
Study guide	Textbook (Incropera)		
$k$		thermal conductivity	$W/mK$
$h$		heat transfer coefficient	$W/m^2 K$

$\sigma$		Stefan-Boltzmann constant, $5.669 \times 10^{-8}$	$\text{W/m}^2 \text{K}^4$
$\varepsilon$		Emissivity ( $0 \leq \varepsilon \leq 1$ ) radiative property of a surface	
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## 1.1 RATE EQUATIONS FOR PHYSICAL PROCESS

$$\text{Rate} = \frac{\text{Driving Force}}{\text{Resistance}}$$

EXAMPLES:

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## 1.2 THE GENERAL RATE EQUATIONS

The general form of the rate equation

$$q = \frac{A\Delta T}{R}$$

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Equation H-1

Where:  $q$  = heat transfer rate (W)

$A$  = heat transfer area ( $\text{m}^2$ )

$T$  = temperature ( $^{\circ}\text{C}$  or K)

$R$  = resistance to heat transfer

Commonly expressed as heat flux:

$$q'' = \frac{q}{A} = f(\Delta T)$$

Equation H-2

Where:  $q''$  = heat flux ( $\text{W}/\text{m}^2$ )

## Modes of heat transfer

**Conduction:** In a stationary medium, energy is transferred due to interactions between particles.

In gases:

In liquids:

In solids:

**Convection:** Energy transfer between a surface and the adjacent fluid. Convection arises from the combined effects of *conduction* and *fluid flow*.

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**Radiation:** Electromagnetic energy emitted at the molecular or atomic level, which transmits through space and is absorbed, transmitted or reflected by receiving molecules.



## CONDUCTION

### Rate of heat transfer: Fourier's Law

For 1-dimensional steady-state conduction, rate of heat transfer from  $T_2$  to  $T_1$ :

Fourier's Law: 
$$q = -kA \frac{(T_1 - T_2)}{(x_1 - x_2)}$$
 Equation H-3

Where:

- Negative sign: denotes heat flow in x direction down thermal gradient ( $\frac{\Delta T}{\Delta x}$ ).
- $k$  = thermal conductivity (W/mK)

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$$\text{Rate} = \frac{\text{Driving Force}}{\text{Resistance}}$$

For 1-d, steady state conduction, define in words, symbols and units:

Rate:

Driving force:

Resistance:

Which will have higher conductivity?

- Steel or brick? \_\_\_\_\_
- Wood or rock? \_\_\_\_\_
- Banana or air? \_\_\_\_\_

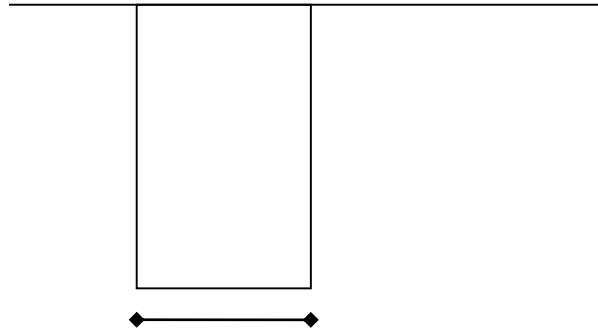
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### 1.3 EXAMPLE – WHAT IS THE RATE OF CONDUCTION THROUGH A CONCRETE WALL?

What is the rate of heat conducted through a concrete wall of width 20 cm, if the outside surface temperature is 35 °C, and the inside surface is kept at 22 °C, through air conditioning?



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## CONVECTION

Convection involves heat transferred from a surface to a fluid.

Examples:

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Rate of heat transferred from surface at  $T_s$  to surrounding fluid, bulk temperature

$$q = hA(T_s - T_\infty)$$

*Equation*

H-4

Where:

- $h$  = heat transfer coefficient ( $\text{W/m}^2\text{K}$ )
- $T_s$  is the surface temperature,  $^\circ\text{C}$  or  $\text{K}$
- $T_\infty$  is the bulk fluid temperature,  $^\circ\text{C}$  or  $\text{K}$

$h$  is dependent on:

- Fluid velocity;
- System geometry,
- Nature of convection
- Fluid properties.

Values for  $h$  are usually derived from empirical dimensionless correlations.

### Modes of Convection

1. Forced Convection: fluid flow is driven by external force

- Gases:  $h = 25 - 250 \text{ Wm}^{-2}\text{K}^{-1}$
- Liquids:  $h = 50 - 20,000 \text{ Wm}^{-2}\text{K}^{-1}$

e.g.

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2. Natural

Flow induced by buoyancy forces due to (or concentration) generated density differences.

- Gases:  $h = 2 - 25 \text{ Wm}^{-2}\text{K}^{-1}$
- Liquids:  $h = 50 - 1,000 \text{ Wm}^{-2}\text{K}^{-1}$

e.g.

### 3. Boiling & Condensation Convection:

Phase change induced flow creates latent heat transfer and fluid mixing.

- Gases & Liquids:  $h = 2,500 - 100,000 \text{ Wm}^{-2}\text{K}^{-1}$

e.g.

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## RADIATION FROM SURFACE TO/FROM SURROUNDS

Examples:

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Rate of heat emitted from a surface at temperature  $T_s$

$$q = A\epsilon\sigma T_s^4$$

Equation H-5

$\sigma$  = Stefan-Boltzmann constant =  $5.669 \times 10^{-8} \text{ (W/m}^2\text{K}^4\text{)}$

$T_s$  = absolute temperature

$\epsilon$  = emissivity ( $0 \leq \epsilon \leq 1$ ) radiative property

Radiation energy,  $E$ , striking a surface

- Absorbed,  $\alpha$ , or
- Reflected,  $\rho$ , or
- Transmitted  $\tau$ .

That is,

Equation H-6



**Absorptivity,  $\alpha$ , Reflectivity,  $\rho$ , Transmissivity,  $\tau$  and Emissivity,  $\epsilon$ :**

- Are optical properties;
- Depend on \_\_\_\_\_ and \_\_\_\_\_

Radiation differs from conduction and convection in that it

- Does not require the presence of matter
- \_\_\_\_\_

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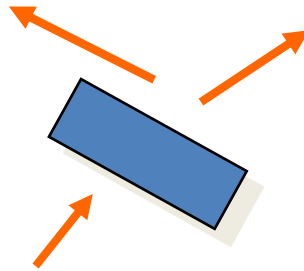
Rate of heat transferred between 2 bodies due to radiation depends on:

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- \_\_\_\_\_
- \_\_\_\_\_

## COMBINED MODES

Many real situations involve heat transfer by more than 1 mode:

*Solve by an energy balance using appropriate equations.*



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## 1.4 SUMMARY: CONDUCTION, CONVECTION AND RADIATION

### 1-D STEADY STATE CONDUCTION IN A SOLID

$$q = -kA \frac{\Delta T}{\Delta x}$$

$q$  = rate of heat conduction from  $T_1 \rightarrow T_2$  (units: W)

$A$  = cross-sectional area (units:  $m^2$ )

$k$  = thermal conductivity (units: )

### CONVECTION FROM A SURFACE TO A FLUID

$$q = hA(T_s - T_\infty)$$

$q$  = rate of heat transfer (units: W)

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$h$  = heat transfer coefficient ( $W/m^2K$ )

$T_s$  = surface temperature (units: )

$T_\infty$  = ambient fluid temperature (units: )

### RADIATION FROM A SURFACE TO SURROUNDS

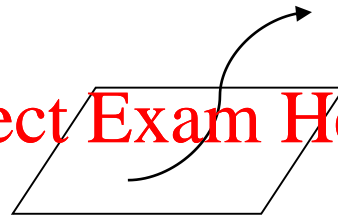
$$q = \epsilon \sigma A T_s^4$$

$\epsilon$  = surface emissivity (units: )

$\sigma$  = Stefan-Boltzman constant =  $5.67 \times 10^{-8} Wm^{-2}K^{-4}$

$T_s$  = surface temperature (units: )

$A$  = surface area (units: )



surrounding fluid

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## HOW TO SET OUT SOLUTIONS TO PROBLEMS: GUIDELINES/MARKING CRITERIA

Your solutions should to satisfy the following criteria:

1. **Diagram.** Draw a useful diagram of the physical system. Symbols, dimensions, materials, flows of energy and other relevant properties should be defined on the diagram.
2. **Define the problem.** State what you will determine, e.g. heat loss from furnace to surrounding air.
3. **Assumptions.** List and justify assumptions and simplifications.
4. **Data.** Clearly state data needed for calculations, including units and reference source
5. **Analysis.** Define appropriate equations, define all symbols.
6. **Calculation.** After completely developing the analysis in symbols, substitute numerical values and calculate results. Clearly show and explain working. Final answer should be stated clearly, with correct units and significant figures.
7. **Interpretation**
  - a. **C**

Under what circumstances is it valid  
Is the answer likely to be an underestimate?  
Can I check for sense against general knowledge of the problem?
  - b. **ANALYSE** - what does it tell me about the system? e.g.  
What is controlling heat loss?
  - c. **APPLY** - what actions should be taken because of what I learn from these calculations? e.g. How can heat loss be reduced?

The guidelines above will make it easier for you to solve new problems, and to check your work and correct errors.

Following the guidelines will also make it easier for others to understand your work, which is important for professional engineers. And the added bonus is that lecturers and tutors will find it easier to follow your work, and so better able to help you during the tutorial, and to award part marks during assessment when you have made an error.