CIS 471/571(Fall 2020): Introduction to Artificial Intelligence

Lecture 18 https://eduassistpro.github.io/ Add WeChat edu_assist_pro Filters

Thanh H. Nguyen

Source: http://ai.berkeley.edu/home.html

Announcement

- •Class on Thursday, Dec 03rd
 - Exam review

Assignment Project Exam Help

- End-of-course Surv https://eduassistpro.github.io/
 - Open until 06:00 PM and Frie Dec edu_assist_pro

Thanh H. Nguyen 11/30/20

Today

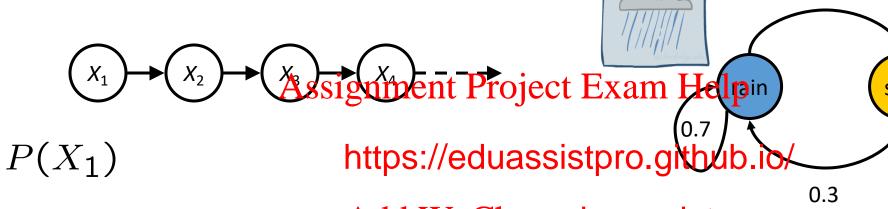
- •HMMs
 - Particle filters

Assignment Project Exam Help

- Applications: https://eduassistpro.github.io/
 - Robot localization / mapping Add WeChat edu_assist_pro

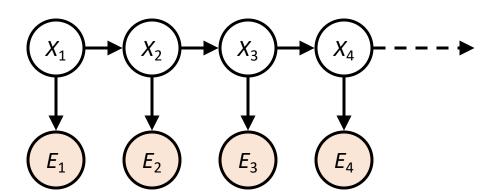
Recap: Reasoning Over Time

Markov models



Add WeChat edu_assist_pro P(E|X)

Hidden Markov models



| - | | |
|------|-------------|-----|
| X | E | P |
| rain | umbrella | 0.9 |
| rain | no umbrella | 0.1 |
| sun | umbrella | 0.2 |
| sun | no umbrella | 0.8 |

0.3

Filtering / Monitoring

- Filtering, or monitoring, is the task of tracking the distribution $B_t(X) = P_t(X_t \mid e_1, ..., e_t)$ (the belief state) over time Assignment Project Exam Help
- We start with $B_1(X)$ i https://eduassistpro.githlybuip/form

Add WeChat edu_assist_pro

• As time passes, or we get observati date B(X)

The Forward Algorithm

We are given evidence at each time and want to know

$$B_t(X) = P(X_t|e_{1:t})$$

Assignment Project Exam Help

• Induction: assuming • Intermediate belief upd https://eduassistpro.github.io/ = $P(X_t|e_{1:t})$

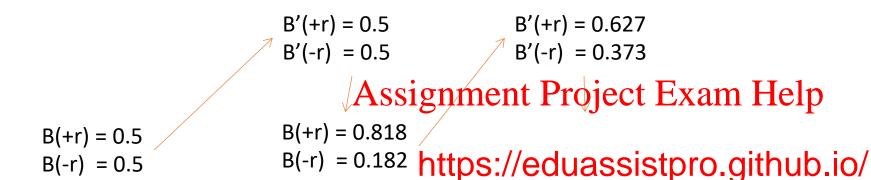
Add WeChat edu_assist_pro

$$P(X_{t+1}|e_{1:(t+1)}) \leftarrow P(X_{t+1}|e_{1:t}) \leftarrow P(X_t|e_{1:t})$$

update

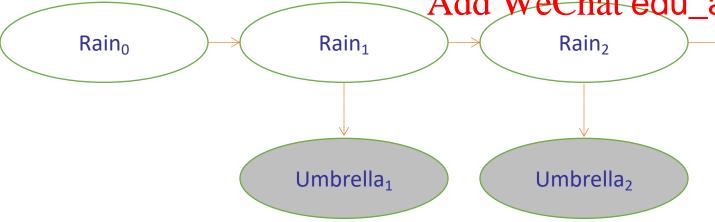
Observation Passage of time update

Example: Weather HMM









| R_{t} | R _{t+1} | $P(R_{t+1} R_t)$ |
|---------|------------------|------------------|
| +r | +r | 0.7 |
| +r | -r | 0.3 |
| -r | +r | 0.3 |
| -r | -r | 0.7 |

| R_{t} | U _t | $P(U_t R_t)$ |
|---------|----------------|----------------|
| +r | +u | 0.9 |
| +r | -u | 0.1 |
| -r | +u | 0.2 |
| -r | -u | 0.8 |



Particle Filtering

Assignment Project Exam Help

https://eduassistpro.github.io/

Particle Filtering

- Filtering: approximate solution
- Sometimes |X| is too big to use exact inference
 - |X| may be too big the significant | X| may be too big the signi
 - E.g. X is continuous
- Solution: approximate i https://eduassistpro.github.iop.0 0.2 0.5
 - Track samples of X, not all values
 Samples are called particles

 WeChat edu_assist_pro
 - Time per step is linear in the number of samples
 - But: number needed may be large
 - In memory: list of particles, not states
- This is how robot localization works in practice
- Particle is just new name for sample

| 0.0 | 0.1 | 0.0 |
|-----|-----|-----|
| 0.0 | 0.0 | 0.2 |
| 0.0 | 0.2 | 0.5 |

| | • |
|---|---|
| • | |

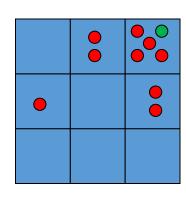
Representation: Particles

- Our representation of P(X) is now a list of N particles (samples)
 - Generally, N << |X|
 - Storing map from X to counts would defeat the point Assignment Project Exam Help



- So, many x may have P(x) = 0 Add WeChat edu_assist_pro
- More particles, more accuracy

• For now, all particles have a weight of 1



Particles:

(3,3)

(2,3)

(3,3)

(3,2)

(3,3) (3,2)

(1,2)

(1,2)

(3,3)

(3,3)

(2,3)

Particle Filtering: Elapse Time

Each particle is moved by sampling its next position from the transition model

x' = sample(PAssignment Project Exam Help)

Particles:

(3,3)

■ This is like prior sampling _https://eduassistpro.gith(以为.io/

frequencies reflect the transition probabiliti

Here, most samples move clockwise, but som

move in another direction or stay in place

This captures the passage of time

 If enough samples, close to exact values before and after (consistent)

Particles:

(3,2)

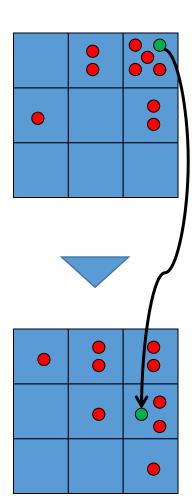
(2,3)(3,2)

(1,3)

(2,3)

(3,2)

(2,2)



Particle Filtering: Observe

Slightly trickier:

- Don't sample observation, fix it
- Similar to likelihood weightigg, ment Project Exam^(3,3)Help samples based on the evide

https://eduassistpro.github.io/
$$w(x) = P(e|x)$$

Add WeChat edu_assist_pro

$$B(X) \propto P(e|X)B'(X)$$

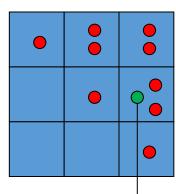
■ As before, the probabilities don't sum to one, since all have been downweighted (in fact they now sum to (N times) an approximation of P(e))

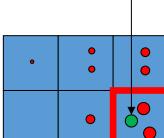
Particles:

Particles:

(3,2) (2,3) (3,2)

- (3,2) w=.9
- (2,3) w=.2
- (3,2) w=.9
- (3,1) w=.4
- (3,3) w=.4
- (3,2) w=.9
- (1,3) w=.1
- (2,3) w=.2
- (3,2) w=.9
- (2,2) w=.4







Particle Filtering: Resample

Rather than tracking weighted samples, we resample
 Rather than tracking weighted samples, we resample

Assignment Project Exame Help

N times, we choose from our weighted

sample distribution (i.e. dr https://eduassistpro.github.io/

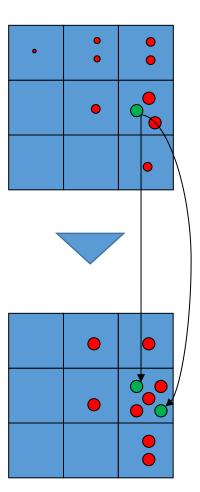
Add WeChat edu_assist_pro

This is equivalent to renormalizing the distribution

 Now the update is complete for this time step, continue with the next one (New) Particles:
(3,2)
(2,2)
(3,2)
(2,3)
(3,3)
(3,2)
(1,3)
(2,3)

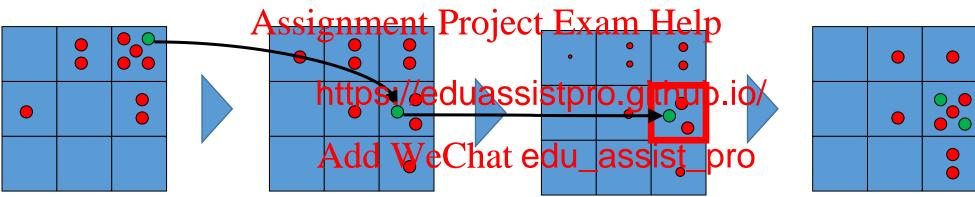
(3,2) (3,2)

(3,2) w=.9



Recap: Particle Filtering

Particles: track samples of states rather than an explicit distribution
 Blapse
 Weight
 Resample

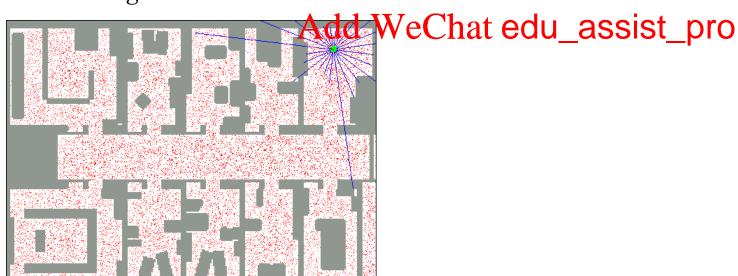


| Particles: | Particles: | Particles: | (New) Particles: |
|------------|------------|------------|------------------|
| (3,3) | (3,2) | (3,2) w=.9 | (3,2) |
| (2,3) | (2,3) | (2,3) w=.2 | (2,2) |
| (3,3) | (3,2) | (3,2) w=.9 | (3,2) |
| (3,2) | (3,1) | (3,1) w=.4 | (2,3) |
| (3,3) | (3,3) | (3,3) w=.4 | (3,3) |
| (3,2) | (3,2) | (3,2) w=.9 | (3,2) |
| (1,2) | (1,3) | (1,3) w=.1 | (1,3) |
| (3,3) | (2,3) | (2,3) w=.2 | (2,3) |
| (3,3) | (3,2) | (3,2) w=.9 | (3,2) |
| (2,3) | (2,2) | (2,2) w=.4 | (3,2) |

Robot Localization

- In robot localization:
 - We know the map, but not the robot's position
 - Observations may be vectors of range finder readings

 - Particle filtering is a main te



Particle Filter Localization (Sonar)

Assignment Project Exam Help

https://eduassistpro.github.io/

Dynamic Bayes Nets

Assignment Project Exam Help

https://eduassistpro.github.io/

Dynamic Bayes Nets (DBNs)

 We want to track multiple variables over time, using multiple sources of evidence

• Idea: Repeat a fixed Bayes net structure at each time Help

Variables from time t can co
 https://eduassistr

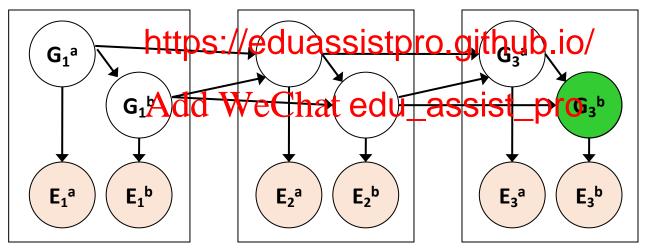
Dynamic Bayes nets are a generalization of HMMs

 E_2^a



Exact Inference in DBNs

- Variable elimination applies to dynamic Bayes nets
- Procedure: "unroll" the network for T time steps, then eliminate variables until $P(X_T | e_{1:T})$ is computed Assignment Project Exam Help = 3



• Online belief updates: Eliminate all variables from the previous time step; store factors for current time only

DBN Particle Filters

- A particle is a complete sample for a time step
- Initialize: Generate prior samples for the t=1 Bayes net
 Example particle: G₁^a A (Signment) poject Exam Help
- Elapse time: Sample a succe https://eduassistpro.github.io/
 - Example successor: $G_2^a = (2A3)G_2^b = (6A3)$ edu_assist_pro
- Observe: Weight each *entire* sample by the likelihood of the evidence conditioned on the sample
 - Likelihood: $P(\mathbf{E_1}^a \mid \mathbf{G_1}^a) * P(\mathbf{E_1}^b \mid \mathbf{G_1}^b)$
- **Resample:** Select prior samples (tuples of values) in proportion to their likelihood

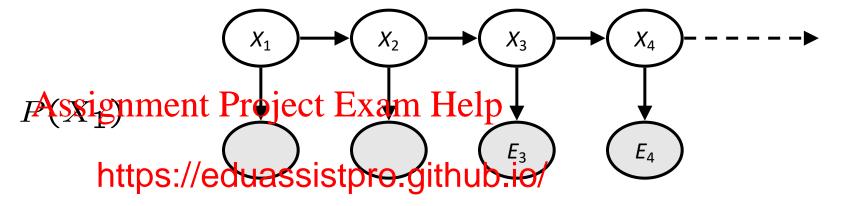
Most Likely Explanation

Assignment Project Exam Help

https://eduassistpro.github.io/

HMMs: MLE Queries

- HMMs defined by
 - States X
 - Observations E
 - Initial distribution:
 - Transitions:
 - Emissions:



Add WeChat edu_assist_pro

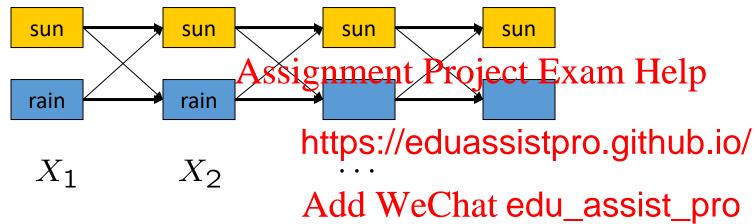
• New query: most likely explanation:

$$\underset{x_{1:t}}{\operatorname{arg\,max}} P(x_{1:t}|e_{1:t})$$

• New method: the Viterbi algorithm

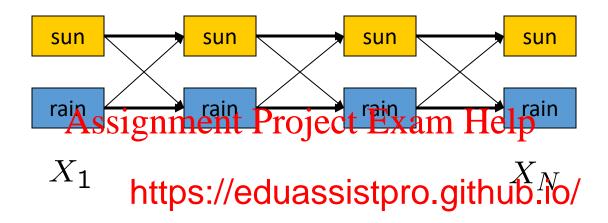
State Trellis

State trellis: graph of states and transitions over time



- Each arc represents some transition $x_{t-1} \rightarrow x_t$
- Each arc has weight $P(x_t|x_{t-1})P(e_t|x_t)$
- Each path is a sequence of states
- The product of weights on a path is that sequence's probability along with the evidence
- Forward algorithm computes sums of paths, Viterbi computes best paths

Forward / Viterbi Algorithms



Forward Algorithm (Sum) Chat edu_assist_proligorithm (Max)

$$f_t[x_t] = P(x_t, e_{1:t})$$

$$m_t[x_t] = \max_{x_{1:t-1}} P(x_{1:t-1}, x_t, e_{1:t})$$

$$= P(e_t|x_t) \sum_{x_{t-1}} P(x_t|x_{t-1}) f_{t-1}[x_{t-1}]$$

$$= P(e_t|x_t) \max_{x_{t-1}} P(x_t|x_{t-1}) m_{t-1}[x_{t-1}]$$