Notes for Lecture 13 (Fall 2022 week 6, part 2): Polymorphism: 'Maybe' type

Jana Dunfield

October 16, 2022

The code for this lecture is in lec13.hs.

1 Polymorphism, continued

As seen in lec11, Haskell lets us define 'data' types that are generic (polymorphic). Here is another example of that:

This defines Special The Control of type a, and Elem contains something of type a' and another Sequence. For example, a value of the type Sequence Bool would be

```
Elem False (Elem https://eduassistpro.github.io/
```

If we think of Elem as 'cons' (:), and Last as 'nil' (

list. But it's not quite the same Alixt can be enpry; a contry list in Signal S

Last

but it will have type a -> Sequence a; it is a function that waits for something of type a and then builds a one-element sequence.)

To see how to work with Sequences, let's rewrite mymap (from lec12.hs) to work on sequences instead of lists. The definition of mymap was:

To convert this, I start by renaming the function and changing its type declaration. [a] is a list of as; Sequence a is a sequence of as:

```
seqmap :: (a \rightarrow b) \rightarrow Sequence a \rightarrow Sequence b

seqmap f [] = []

seqmap f (x : xs) = (f x) : (seqmap f xs)
```

This won't compile, because the clauses that define seqmap still use lists. Next, I rewrite the second clause. x : xs becomes Elem x xs, and similarly in the right-hand side.

This still won't compile because the first clause uses a list. We can actually delete the first clause: a Sequence can't be empty, so there is no case corresponding to the empty list [].

```
seqmap :: (a -> b) -> Sequence a -> Sequence b
seqmap f (Elem x xs) = Elem (f x) (seqmap f xs)
```

Attempting to test segmap will show that we're not done:

```
*Lec13> seqmap (\x -> x + 1) (Elem 2 (Last 10))
Elem 3 *A symptom represent 1 Project Exam Help
Non-exhaustive patterns in function seqmap
```

Haskell tried to patter x xs), Haskell "fell of https://eduassistpro.github.io/didn't write a pattern that match

To fix this, we need to add a clause whose pattern is

```
seqmap :: (a -> bActequence Condence Cu_assist_pro seqmap f (Elem x xs) = Elem (f x) (seqmap f xs) seqmap f (Last y) = undefined
```

I want to apply the given function f to the last element as well as the earlier elements. (Functions like map, mymap, seqmap are meant to be widely useful; maybe there would be a situation where I'd want to apply a function to every element *except* the last one, but if I needed to do that, I would write another function to do it.)

```
So, given Last y, I return Last (f y).
```

```
seqmap :: (a -> b) -> Sequence a -> Sequence b
seqmap f (Elem x xs) = Elem (f x) (seqmap f xs)
seqmap f (Last y) = Last (f y)
```

Now, I can call segmap:

```
*Lec13> seqmap (\x -> x + 1) (Elem 2 (Last 10)) Elem 3 (Last 11)
```

We have now defined a type that is very similar to lists, but that doesn't allow "nothing": something of type Sequence a must have at least one thing of type a in it.

2 'Maybe' type

2.1 What's it for?

Let's turn this around. What if we want to represent "nothing"?

Software often needs to represent the absence of information. For example, if we are writing backup software, we probably want to store the time of the last backup. But if we haven't yet backed up, no such time exists. Assuming we have a type Time¹ We could represent this in Haskell:

A less clear alternative would be to represent the last backup by Time alone, and have a value of zero represent "never". This is prone to error: unless we remember to check for a value of zero, our backup system will probably display something like "Last backed up: on Jan 1 1970". (It also can't represent the situation where we really did last do a backup on January 1st, 1970, but that situation is extremely unlikely.)

If we do remember to check, we carplisplay "Last backed up: never" but if we used the BackupTime type, salan hill ent Project Exam Help

```
displayBackupTim
displayBackupTim
https://eduassistpro.github.io/
-- this is going to d
-- but I don't want to bother figuring out how to do it
Needing to represent nothing, and a constructor Just
```

```
data Maybe a = Nothing
| Just a
```

Instead of defining BackupTime, we could use the type Maybe Time: Nothing would represent "never", and Just t would represent "backed up at time t".

2.2 Comparison to other languages

Many languages have something that represents "nothing":

```
Python has None

Java has null

C has NULL

Pascal has nil
```

¹I won't try to use the actual Haskell time library. For simplicity, imagine that Time is "seconds since 00:00, January 1, 1970".

Or, at least, these languages can represent "nothing" in some circumstances:

- In Java, any reference to an Object (including any descendant of the Object class) can be null, but types like int cannot be null.
- In C, pointers can be NULL but non-pointer types (like int, bool, char) can't be NULL.

So you get "nothingness" for some types, but not others.

Programming in languages that have features like None and null is tricky, because you have to be careful that when you think you have something—say, an IP address—you actually have an IP address, and not None or null.

It's difficult to be careful all the time.

The computer scientist Tony Hoare, who put null into the language Algol-W in 1965, called it a "billion-dollar mistake":

"My goal was to ensure that all use of references should be absolutely safe, with checking performed automatically by the compiler. But I couldn't resist the temptation to put in a null reference, simply because it was so easy to implement. This has led to innumerable errors, vulnerabilities, and system crashes, which have probably caused a billion dollar and angle in the last out years."X am He in

https://en.wikipedia.org/wiki/Tony_Hoare

When I program in a lant to methods, instance whittps://eduassistpro.githubhet@/hether they're null before I do a

In Haskell, null-ness is signalled by the Maybe ty need to check if it's really and it where get in a record assist or a second assist.

2.3 The sad story of the NULL licence plate

Some of the problems around "null" values can't exactly be blamed on the programming language. For example:

```
https://www.wired.com/story/null-license-plate-landed-one-hacker-ticket-hell/
```

I think the problem here is the use of a string, which is information, to represent the absence of information. If Haskell were as popular as Java, we might have the same problem with a licence plate that read "NOTHING".

2.4 Finding in trees

lec13.hs includes a function find1 that searches for a key in a binary tree type Tree.

If the key is not found, find1 returns Nothing. If the key is found, find1 returns the associated String.