### CMSC5741 Big Data Tech. & Apps.

# Lecture Assignment Project Exam Helptreams

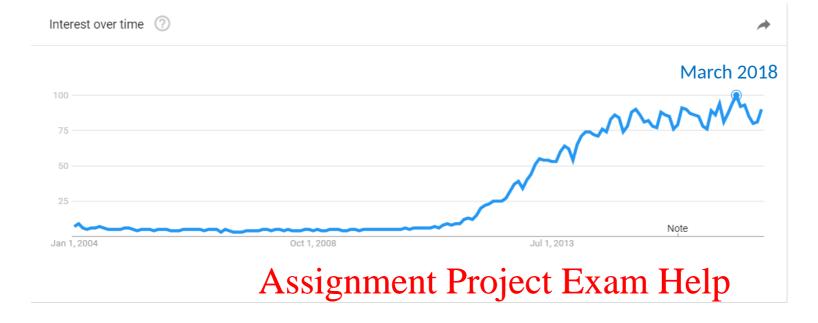
https://eduassistpro.github.io/

Add WeChat edu\_assist\_pro

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## Motivation

- In many data mining situations, we know the entire data set in advance Assignment Project Exam Help
- Stream Man https://eduassistpro.github.io/nt when the input rate is controlled edu\_assist\_pro
  - Google queries
  - Twitter and Facebook status updates
- We can think of the data as infinite and nonstationary (the distribution changes over time)



#### Google **Trends**

When we search for "big data"

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Interest by region ②



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# Election 2016: Trump vs Clinton

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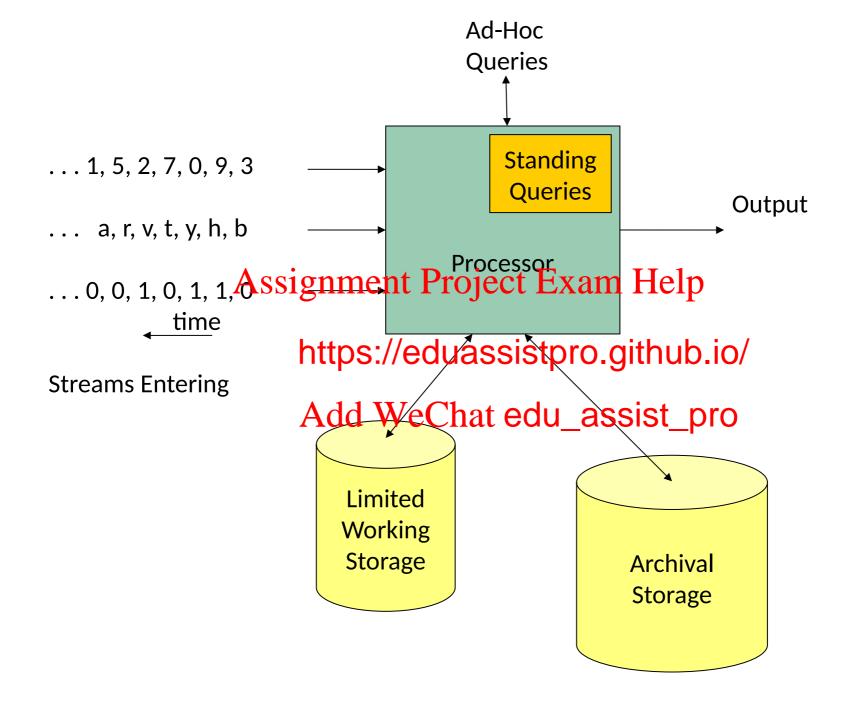
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## The Stream Model

- Input tuples (e.g., [user, query, time]) enter at a rapid rate, at one or more input ports Assignment Project Exam Help
- The system c ntire stream accessibly https://eduassistpro.github.io/

• How do you make critic tions about the stream using a limited amount of (secondary) memory?



## **Problems on Data Streams**

- Types of queries one wants on answer on a stream:
   Assignment Project Exam Help
  - Sampling da
    - Construct https://eduassistpro.github.io/
  - Queries over And We What edu\_assist\_pro
    - Number of items of type x in the last k elements of the stream
  - Filtering a data stream
    - Select elements with property x from the stream

## **Problems on Data Streams**

- Types of queries one wants on answer on a stream:
   Assignment Project Exam Help
  - Counting di
    - Number of https://eduassistpro.github.io/last k elements of the stream Add WeChat edu\_assist\_pro
  - Estimating moments
    - Estimate avg./std. dev. of last k elements
  - Finding frequent elements

# Applications (1)

- Mining query streams
  - Google wants to know what queries are more frequent to
- Mining click https://eduassistpro.github.io/
  - Yahoo! wants to know
     Yahoo! propages are pages are pages and pages are pages
- Mining social network news feeds
  - E.g., look for trending topics on Twitter, Facebook

# Applications (2)

- Sensors Networks
  - Many sensors feeding into a central controller
- Telephone c https://eduassistpro.github.io/
  - Data feeds into custome ell as
     settlements between tel ompanies
- IP packets can be monitored at a switch
  - Gather information for optimal routing
  - Detect denial-of-service attacks

## Outline

- Sampling from a Data Stream
- Queries oxeria (leng) Sliding Windows
- Filtering Dat https://eduassistpro.github.io/
- Counting Distinct Fleme edu\_assist\_pro
- Computing Moments
- Counting Itemsets

## Outline

- Sampling from a Data Stream
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# Sampling from a Data Stream

- Since we cannot store the entire stream, one obvious approach is to store a sample

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  Two different
- - Sample a fixe https://eduassistpro.githublie/stream (say 1 in 10) Add WeChat edu\_assist\_pro
  - Maintain a random sample of fixed size over a potentially in finite stream
    - At any "time" t we would like a random sample of n elements. For all t, each of n elements seen so far has equal prob. of being sampled

# Sampling a Fixed Proportion

- Problem 1: Sampling fixed proportion
- Scenario: Search engine query stream Assignment Project Exam Help
  - Stream of tup
  - Answer ques https://eduassistpro.githubaio/ser run the same query on two wifferen edu\_assist\_pro
  - Have space to store 1/10<sup>th</sup> of query stream
- Naive solution:
  - Generate a random integer in [0..9] for each query
  - Store the query if the integer is 0, otherwise discard

# Problem with Naive Approach

- Simple question: What fraction of queries by an average user are duplicates?
- Suppose each suisente Projetter Tesaon Helphod d queries twice (total of s https://eduassistpro.github.io/
  - Correct answer
  - Sample will contain by the declarate edu\_assistic and 2dp of the duplicate queries at least once
  - But only  $dp^2$  pairs of duplicates
    - $dp^2 = p * p * d$
  - Of d "duplicates" 2p(1-p)d appear once
    - 2p(1-p)d = ((p\*(1-p))+((1-p)\*p))\*d
  - So the sample-based answer is:  $dp^2/(sp+dp^2+2p(1-p)d)$

# Problem with Naive Approach

- A concrete example:
  - Query stream: 1, 2, 3, 4, 5, 6, 7, 7, 8, 8
  - Sample 50% Assignment Project Exam Help s case
  - Correct ans https://eduassistpro.giteubjelicates
  - If our sample isdive, Chat edu\_assis pare duplicates
  - If our sample is 6, 7, 7, 8, 8, then 67% are duplicates
  - What is the expectation of fraction of duplicates if we use sample-based method?

Answer: 1/9

Solution?

# Solution: Sample Users

- Pick 1/10<sup>th</sup> of users and take all their searches in the sample Assignment Project Exam Help
- Use a hash f name or use https://eduassistpro.github.io/ 10 buckets Add WeChat edu\_assist\_pro
- Generalized: Pick 1/dth of users, we need to use d buckets

## **Generalized Solution**

- Stream of tuples with keys:
  - Key is some subset of each tuple's components
    - E.g., tuple i ey is user
  - Choice of k
     https://eduassistpro.github.io/ ation
- To get a sample of size a edu\_assist\_pro
  - Hash each tuple's key uniformly into b buckets
  - Pick the tuple if its hash value is at most a(h(x) = 1, 2, ..., a)

## Maintaining a Fixed-size Sample

- Problem 2: Fixed-size sample
- Suppose we need to maintain a sample *S* of size Assignment Project Exam Help out of *S*=100 space) https://eduassistpro.github.io/
  - E.g., main memory size const edu\_assist\_pro
- Why? Don't know length of stream in advance
  - In fact, stream could be infinite
- Suppose at time t we have seen n items
  - Ensure each item is in the sample S with equal prob. s/n

# Solution: Fixed Size Sample

#### Algorithm:

- Store all the first s elements of the stream to S
- Suppose we have seen *n* elements, and now the *n*+1<sup>th</sup> element arrivehttps://eduassistpro.github.io/

  - With prob. s/n+1, pick the n+1 lse discard it
     If we picked the n+1 element lse discard it elements in the sample S, picked uniformly at random
- Claim: This algorithm maintains a sample S with the desired property, i.e., each item is in the sample S with equal prob.

# **Proof: By Induction**

- We prove this by induction:
  - Assume that after *n* elements, the sample contains each element Project Frankley *n*
  - We need to https://eduassistpro.githeleim/ent n+1
     the sample maintains the edu\_assist\_pro
    - Sample contains each element seen so far with prob. s/(n+1)
  - Obviously, after we see n=s elements the sample has the wanted property
    - Each out of n=s elements is in the sample with prob. s/s=1

## **Proof: By Induction**

- After n elements, the sample S contains each element seen so far with probability s/n
- Now element Project Exam Help
- For elements https://eduassistpro.githម្រស់ខេត្ remaining in SAish WeChat edu\_assist\_pro

- At time n tuples in S were there with prob. s/n
- Time n \rightarrow n+1 tuple stayed in S with prob. n/(n+1)
- So prob. tuple is in S at time n+1 =



## Outline

- Sampling from a Data Stream
- · Queries oxeria (leng) Sliding Windows
- Filtering Dat https://eduassistpro.github.io/
- Counting Distinct Fleme edu\_assist\_pro
- Computing Moments
- Counting Itemsets

# Sliding Windows

- A useful model of stream processing is that queries are about a window of length N the N most rece ed
- Interesting c https://eduassistpro.github.io/ t cannot be stored in memory, or e sk
  - Or, there are so many streams that windows for all cannot be stored

## A Sliding Window Example

```
N = 6
q w e r t y u i o p a s d f g h j k l z x c v b n m
      Assignment Project Exam Help
q w e r t y zx c v b n m
Add WeChat edu_assist_pro
qwertyuiopasdf xcvbnm
q w e r t y u i o p a s d f g h j k l z x c v b n m
                          Future
```

# Counting Bits (1)

#### Problem:

- Given a stream of 0s and 1s Assignment Project Exam Help
- Be prepare f the form How many 1's in https://eduassistpro.github.ip/
- Obvious solution: WeChat edu\_assist\_pro
  - Store the most recent N bits
  - When a new bit comes in, discard the N+1st bit

# Counting Bits (2)

- You cannot get an exact answer without storing the entire window Assignment Project Exam Help
- Real Proble ot afford to store N bits? https://eduassistpro.github.io/
  - E.g., we are processing 1 reams and N = 1 billion
- But we're happy with an approximate answer

## An Attempt: Simple Solution

- How many 1s are in the last N bits?
- Simple solution that does not really solve our problem:

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  Uniformity ass
- Maintain 2 cou https://eduassistpro.github.io/
  - S: number of 1s4softaWeChat edu\_assist\_pro
  - Z: number of 0s so far
- How many 1s are in the last N bits? N·S/(S+Z)
- But, what if stream is non-uniform?
  - What if distribution changes over time?

## **DGIM Method**

• Store O(log<sup>2</sup>N) bits per stream

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• Gives approx https://eduassistpro.github.io/by more than 50%

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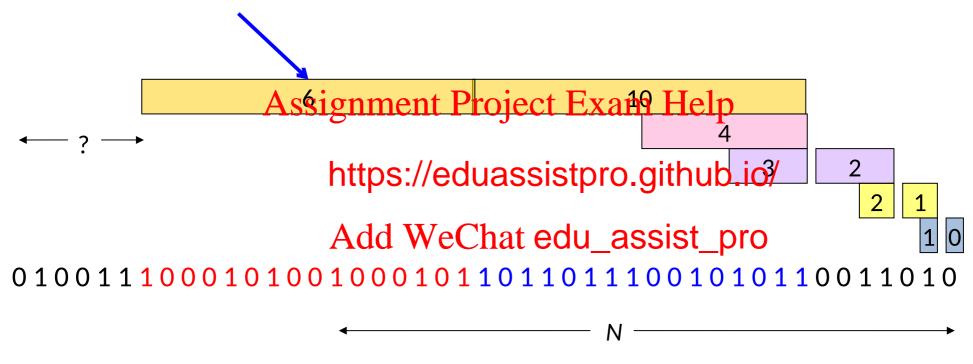
Error factor can be redu fraction > 0,
 with more complicated algorithm and
 proportionally more stored bits

## Idea: Exponential Windows

- Solution that doesn't (quite) work:
  - Summarize exponentially increasing regions of the stream, loo
  - Drop small r https://eduassistpro.github.jo/ at the same point as a larger regionWeChat edu\_assist\_pro

## An Exponential Window Example

Window of width 16 has 6 1s



We can construct the count of the last *N* bits, except we're not sure how many of the last 6 are included.

### What's Good?

- Stores only O(log<sup>2</sup>N) bits
  - O(log N) counts of log N bits each Help

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- Easy update as more bit Add WeChat edu\_assist\_pro
- Error in count no greater than the number of 1s in the "unknown" area

## What's Not So Good?

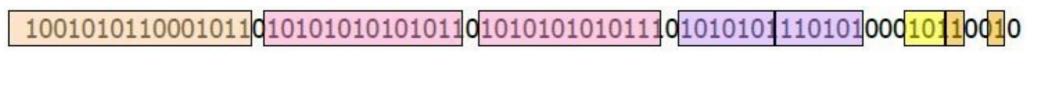
- As long as the 1s are fairly evenly distributed, the error ratio due to the unknown region is small – no m
- But it could https://eduassistpro.github.io/re in the unknown area at the en
- In that case, the error is unbounded

# Fixup: DGIM Method

- Instead of summarizing fixed-length blocks,
   summarize blocks with specific numbers of 1s
   Let the bloc

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   increase
  - Let the bloc increase exponential https://eduassistpro.github.io/
- When there and the Classic edu\_assist down, block sizes stay small, so errors are small



## **DGIM: Timestamps**

- Each bit in the stream has a *timestamp*, starting 1, 2.

  \*\*Assignment Project Exam Help
- Record times (the window https://eduassistpro.github.io/ size), so we c vant timestamp in O(log<sub>2</sub>N)

#### **DGIM:** Buckets

- A bucket in the DGIM method is a record consisting of:

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  - The times g N ) bits]
     The numb https://eduassistpro.github.io/beginning and
  - 2. The numb works we have beginning and end: [O(log46g WeGhet edu\_assist\_pro
- Constraint on buckets: Number of 1s must be a power of 2
  - That explains the O(log log N) in (2)

# Representing a Stream by Buckets

- Either one or two buckets with the same power-of-2 number of 1s Assignment Project Exam Help
- stamps https://eduassistpro.github.io/ Buckets do n
- Buckets are sorted by si
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   Earlier buckets are not s
   n later buckets
- Buckets disappear when their end-time is > N time units in the past

### **Example:** Bucketized Stream

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https://eduassistpro.github.io/

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#### Properties we maintain:

- Either one or two buckets with the same power-of-2 number of 1s
- Buckets do not overlap in timestamp
- Buckets are sorted by size

# **Updating Buckets – (1)**

• When a new bit comes in, drop the last (oldest) bucket if its end-time is prior to N time units Assignment Project Exam Help before the cu

https://eduassistpro.github.io/

• 2 cases: Current bit is 0 o

 If the current bit is 0, no other changes are needed

# **Updating Buckets – (2)**

- If the current bit is 1:
  - Create a new bucket of size 1, for just this bit
    - End timest
  - If there are https://eduassistpro.github.io/size 1, combine the oldest twodihtwes but edu\_assist\_pro
  - If there are now three buckets of size 2, combine the oldest two into a bucket of size 4
  - And so on …

## Example

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## How to Query?

- To estimate the number of 1s in the most recent *N* bits:

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  - Sum the siz
     the last
  - Add half the

    https://eduassistpro.github.io/
- Remember: We don't kn assist pro many 1s of the last bucket are still within the window

### **Example: Bucketized Stream**

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#### **In-Class Practice 1**

Go to <u>practice</u>

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#### **Error Bound: Proof**

- Suppose the last bucket has size 2<sup>r</sup>
- Then by assuming 25-1 of its 1s are still within the window, https://eduassistpro.github.io/
- Since there is at least o tof each of Add WeChat edu\_assist\_pro the sizes less than  $2^r$ , th m is no less than  $1 + 2 + 4 + ... + 2^{r-1} = 2^r 1$
- Thus, error ratio is at most  $2^{r-1} / (2^r 1) \approx 50\%$

# **Extensions (For Thinking)**

Can we use the same trick to answer queries
 "How many 1s in the last k?" where k < N?</li>
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• Can we handle the case he stream is Add WeChat edu\_assist\_pro not bits, but integers, a nt the sum of the last *k*?

# Reducing the Error

- Instead of maintaining 1 or 2 of each size bucket, we allow either r-1 or r for r > 2
  - Except for t any number https://eduassistpro.github.io/ those
- Error is at most WeChat edu\_assist\_pro
- By picking r appropriately, we can tradeoff between number of bits and the error

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# Filtering Data Streams

- Each element of data stream is a tuple (a finite list of elements)
- Given a list of keys S Project Exam Help
- How to deter <a href="https://eduassistpro.githuff.ist/ream">https://eduassistpro.githuff.ist/ream</a> have keys in S?

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- Obvious solution: Hash table
  - But suppose we do not have enough memory to store all of S in a hash table
    - E.g., we might be processing millions of filters on the same stream

# **Applications**

- Example: Email spam filtering
  - We know 1 billion "good" email addresses
  - If an email c ese, it is NOT spamhttps://eduassistpro.github.io/
- Publish-subscribe syste
  - People express interest in certain sets of keywords
  - Determine whether each message matches user's interest

## First Cut Solution – (1)

- Given a set of keys S that we want filter
- Create a bit array B of n bits, initially all 0s Assignment Project Exam Help
- Choose a has range [0,n] https://eduassistpro.github.jo/
- Hash each m

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   and set that bit to 1, i.e.

   1
- Hash each element a of the stream and output only those that hash to bit that was set to 1
  - Output a if B[h(a)] == 1

ts,

# First Cut Solution – (2)

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- Creates false positives but no false negatives
  - If the item is in S we surely output it, if not we may still output it

# First Cut Solution – (3)

- |S| = 1 billion email addresses
  - |B| = 1GB = 8 billion bits
- Assignment Project Exam Help
  If the email a it surely hashes
  to a bucked t https://eduassistpro.github.ie/it always
  gets through (Addfal/sechae edu\_assist\_pro
- Approximately 1/8 of the bits are set to 1, so about 1/8<sup>th</sup> of the addresses not in S get through to the output (false positives)
  - Actually, less than 1/8<sup>th</sup>, because more than one address might hash to the same bit

# **Analysis: Throwing Darts**

- More accurate analysis for the number of false positives
   Assignment Project Exam Help
   ...
- Consider: If nto n equally https://eduassistpro.github.io/bility that a target gets at least one nto n equally properties nto n equally https://eduassistpro.github.io/bility that a
- In our case:
  - Targets = bits/buckets
  - Darts = hash values of items

# Analysis: Throwing Darts – (2)

- We have m darts, n targets
- What is the probability that a target gets at Assignment Project Exam Help least one dar

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# Analysis: Throwing Darts – (3)

 Fraction of 1s in the array B == probability of false positive == Assignment Project Exam Help

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- Example: dar
  - Fraction of 1s in B = = 0.1
  - Compare with our earlier estimate: 1/8 = 0.125

Can we improve this error?

#### **Bloom Filter**

- Consider: |S| = m, |B| = n
- Use k independent hash functions Assignment Project Exam Help
   Initialization:
- - Set B to all 0 https://eduassistpro.github.io/
  - Hash each element esting edu\_assist\_for tion, set (for each)

#### Run-time:

- When a stream element with key x arrives
  - If for all, then declare that x is in S
  - Otherwise discard the element x

# Bloom Filter – Analysis

- What fraction of the bit vector B are 1s?
  - Throwing k·m darts at n targets
    Assignment Project Exam Help
  - So fraction

https://eduassistpro.github.io/ sh functions

But we have

• So, false positive proba

# Bloom Filter - Analysis (2)

- m = 1 billion, n = 8 billion
  - -k = 1: = 0.1175
  - -k = 2: = Assignment Project Exam Help

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- What happens as We ke edu\_assist\_pro increasing k?
- "Optimal" value of k:
  - − E.g.:

## Bloom Filter: Wrap-up

- Bloom filters guarantee no false negatives, and use limited memory Assignment Project Exam Help
  - Great for pr more expensive checks https://eduassistpro.github.io/
  - E.g., Google's big War edu\_assist proxy
- Suitable for hardware implementation
  - Hash function computations can be parallelized

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### **Counting Distinct Elements**

#### Problem:

- Data stream consists of a universe of elements chosen fro
- Maintain a https://eduassistpro.github.io/ of distinct
   elements seenled hat edu\_assist\_pro
- Obvious approach:
  - Maintain the set of elements seen so far

# **Applications**

- How many different words are found among the Web pages being crawled at a site? Assignment Project Exam Help
  - Unusually lo ould indicate artificial paghttps://eduassistpro.github.io/

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 How many different Web pages does each customer request in a week?

### **Using Small Storage**

 Real Problem: What if we do not have space to store the complete set? Assignment Project Exam Help

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- Estimate the count in a dway Add WeChat edu\_assist\_pro
- Accept that the count may be in error, but limit the probability that the error is large

# Flajolet-Martin Approach

- Pick a hash function h that maps each of the n elements to at least log N bits Assignment Project Exam Help
- For each stre https://eduassistpro.github.io/
  - -r(a) = position of first 1 co m the right
- Record R = the maximum r(a) seen
  - $-R = \max_{a} r(a)$ , over all the items a seen so far
- Estimated number of distinct elements = 2<sup>R</sup>

# Why It Works

- The probability that a given h(a) ends in at least r 0s is  $2^{-r}$ 
  - Assignment Project Exam Help y at random
  - Probabilit https://eduassistpro.githerbeinds in at least r Os is A2dd WeChat edu\_assist\_pro
- If there are m different elements, the probability that  $R \ge r$  is  $1 (1 2^{-r})^m$

Prob. all h(a)'s end in fewer than r Os.

Prob. a given h(a) ends in fewer than r Os.

# Why It Works – (2)

- Note:
- Prob. of NOT finding a tail of length r is:
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   If, then prob.
  - - https://eduassistpro.github.io/
    - So, the probability of find edu\_assist\_pro
  - If, then prob. tends to 0
    - as
    - So, the probability of finding a tail of length r tends to 1
- Thus, will almost always be around *m*.

## Why It Doesn't Work

- E[2<sup>R</sup>] is actually infinite
  - Probability halves when R R +1, but value doubles
- Workaround involves using many hash functions and getting m https://eduassistpro.github.io/
- How are samples for binse edu\_assist\_pro
  - Average? What if one very large value?
  - Median? All values are a power of 2
  - Solution:
    - Partition your samples into small groups
    - Take the average of groups
    - Then take the median of the averages

#### **In-Class Practice 2**

Go to <u>practice</u>

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## One-Slide Takeaway

- Sampling from a streaming data
  - How to get a fixed proportion or a fixed-size Sample
- Queries over a l'Assignment Project Exam Help
  - understand DGhttps://eduassistpro.github.io/
- Filtering Data StreamWeChat edu\_assist\_pro
  - understand first cut solution and Bloom Filter
- Counting distinct elements
  - Understand Flajolet-Martin Approach
- Appendix: computing moments and counting item sets

#### References

- Book:
  - Mining of Massive Datasets
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- Massive Online Analysis oftware: Add WeChat edu\_assist\_pro
  - http://moa.cms.waikato

### Appendix

- Sampling from a Data Stream
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#### **Generalization:** Moments

 Suppose a stream has elements chosen from a set of N values Assignment Project Exam Help

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• Let  $m_a$  be the number o alue a occurs Add WeChat edu\_assist\_pro

• The k<sup>th</sup> moment is

### **Special Cases**

- 0th moment = number of different elements
  - The problem just considered
- 1st moment = Project Exam Help bers of
  - elements = I https://eduassistpro.github.io/
    - Easy to complete WeChat edu\_assist\_pro
- 2<sup>nd</sup> moment = *surprise number* = a measure of how uneven the distribution is

## **Example: Surprise Number**

- Stream of length 100; 11 values appear
- Item counts: 90, 1, 1, 1, 1, 1, 1, 1, 1, 1 Add WeChat edu\_assist\_pro

  Surprise # = 8,110

#### **AMS Method**

- Works for all moments
- Gives an unbiased estimate
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- We'll just con https://eduassistpro.gitment/

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- Based on calculation of many random variables X:
  - For each random variable X, we store X.el and X.val
  - Each random variable represents one separate item
  - Note this requires a count in main memory, so number of Xs is limited

#### One Random Variable

- Assume stream has length n
- Pick a random time to start so that any time is equally likely https://eduassistpro.github.io/
- X = n \* ((twice the number of as in the stream starting at the chosen time) 1)
  - Note: store n once, count of as for each X

## Expected Value of X

- 2<sup>nd</sup> moment is
- $E(X) = \frac{*}{all \text{ times so n' multivice the number of times}}$  the stream e https://eduassistpro.ghthb.ib/ from that time on] Add weChat edu\_assist\_pro

Group times by the value seen

Time when the last *a* is seen

Time when the penultimate *a* is seen

Time when the first *a* is seen

## **Combining Samples**

- One random variable only represent one sampled item;
   we should do many concurrent samples
- Compute as many variables X as can fit in available memory
   https://eduassistpro.github.io/
- Average them in groups Chat edu\_assist\_pro
- Take median of averages
- Proper balance of group sizes and number of groups assures not only correct expected value, but expected error goes to 0 as number of samples gets large

#### **Problem: Streams Never End**

- We assumed there was a number *n*, the number of positions in the stream help
- But real stre so n is a https://eduassistpro.github.io/s seen so far Add WeChat edu\_assist\_pro

## Stream Never End: Fixups

- The variables X have n as a factor keep n separately; just hold the count in X
- Suppose we calculate the Suppose we calculat
  - Objective: each starting tim Add WeChat edu\_assist\_pro
  - Solution: (fix-size sampling!)
    - Choose the first k times for k variables
    - When the  $n^{th}$  element arrives (n > k), choose it with probability k/n
    - If you choose it, throw one of the previously stored variables out, with equal probability



### Appendix

- Sampling from a Data Stream
- Queries oxesignment projecties and incloses
- Filtering Dat https://eduassistpro.github.io/
- Counting Distinct Fleme edu\_assist\_pro
- Computing Moments
- Counting Itemsets

### Counting Itemsets

- New Problem: Given a stream, which items appear more than stimes in the window? Assignment Project Exam Help
- Possible solu https://eduassistpro.github.io/ er item
  - 1 = item present; 0 = not
  - Use DGIM to estimate counts of 1s for all items

#### Extensions

- In principle, you could count frequent pairs or even larger sets the same way Assignment Project Exam Help
  - One stream

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- Drawbacks:
  - Only approximate
  - Number of itemsets is way too big

# **Exponentially Decaying Windows**

- Exponentially decaying windows: A heuristic for selecting likely frequent itemsets
  - What are c movies?
    - Instead of https://eduassistpro.githulaid/N elements
    - Compute a smooth eggreedu\_assist the whole stream
- If stream is  $a_1$ ,  $a_2$ ,... and we are taking the sum of the stream, take the answer at time t to be:
  - c is a constant, presumably tiny, like or
  - When new arrives: Multiply current sum by (1-c) and add

## **Example: Counting Items**

- If each is an "item" we can compute the characteristic function of each possible item x as an exponentially weet a rinig window (EDD.W.).
  - That is: https://eduassistpro.github.io/
  - where if , and 0 otherwise
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     Imagine that for each item a binary stream  $(1 \dots x \text{ appears}, 0 \dots x \text{ does not appear})$
  - New item x arrives:
    - Multiply all counts by (1-c)
    - Add +1 to count for x
- Call this sum the "weight" of item x

## Sliding Versus Decaying Windows

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Important property: Sum over all weights is

=

### Counting Items

Suppose we want to find those items of weight

 $> \frac{1}{2}$ 

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| weights is = https://eduassistpro.github.io/ Important p

Thus:

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  There cannot be more t with weight of ½ or more
- So, is a limit on the number of movies being counted at any time

### **Extension to Larger Itemsets**

- Count (some) itemsets in an E.D.W.
  - Problem: Too many itemsets to keep counts of all of them in Assignment Project Exam Help
- When a bask https://eduassistpro.github.io/
  - Multiply all caddtwether edu\_assist\_pro
  - For uncounted items in B, create new count
  - Add 1 to count of any item in B and to any itemset contained in B that is already being counted
  - Drop counts  $< \frac{1}{2}$
  - Initiate new counts (next slide)

#### **Initiation of New Counts**

- Start a count for an itemset if every proper subset of S had a count prior to arrival of basket B
  - Intuitively. If all subsets of stare being counted this means they a https://eduassistpro.githbuso/has a potential to be "hot"

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#### Example

- Start counting {i, j} iff both i and j were counted prior to seeing B
- Start counting {i, j, k} iff {i, j}, {i, k}, and {j, k} were all counted prior to seeing B

## **How Many Counts?**

- Counts for single items < (2/c) \* (average number of items in a basket)

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- Counts for la https://eduassistpro.github.io/
- But we are conservative tarting counts Add WeChat edu\_assist\_pro of large sets
  - If we counted every set we saw, one basket of 20 items would initiate 1M counts

#### **In-Class Practice 1**

• There are several ways that the bit-stream 1001011011101 could be partitioned into buckets. Fin

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### **In-Class Practice 2**

• Suppose our stream consists of the integers 3, 1, 4, 1, 5, 9, 2, 6, 5. Our hash functions will all be of the form for some a and b. You should treat the result as a 5-bit binary inte https://eduassistpro.githlength for each stream element and the renumber of distinct element in the result as a 5-bit binary inte https://eduassistpro.githlength for each stream element and the renumber of the number of distinct element sh function is: