CO 353 Winter 2018: Project 3

Due: March 19 at 8pm

1 Objective

The project consists in implementing the dual simplex method for linear programming with general lower and upper bounds. The implementation must be *correct* and *robust* to the numerical inaccuracies of floating-point arithmetic. In particular, given $c \in \mathbb{R}^n$, $\ell \in \mathbb{R}^n$, $u \in \mathbb{R}^n$, $u \in \mathbb{R}^n$ and $u \in \mathbb{R}^n$, a linear programming problem is formulated as

min
$$c^T x$$

s.t. $Ax = b$
 $\ell \le x \le u$
 $x \in \mathbb{R}^n$.

If the problem is feasible, the implementation must find a basic solution that is (a) feasible within the tolerance ε , i.e., $\ell_B - \varepsilon \le x_B^* \le u_B + \varepsilon$ where x_B^* are the values of the basic variables, and (b) optimal within the same tolerance ε . Letting \bar{c} be herefore problem bound, and $\bar{c}_j \le \varepsilon$ if x_j is at lower bound, and $\bar{c}_j \le \varepsilon$ if x_j is at upper bound. We will use $\varepsilon = 10^{-6}$. Note that your code must implement the dual simplex method, so, for exampl

would be exceedingly slow. https://eduassistpro.github.io/
This project can be completed in groups of 1 or 2. You can also form groups of 3, but *only* if you first get my

This project can be completed in groups of 1 or 2. You can also form groups of 3, but *only* if you first get my approval by email (lpoirrier (at uwaterloo)) by March 5th. If you already had approprevious assignment, then Augrentically allowed by the duire assignment (no need to contact me in this case).

2 Input and output

The input consists in $m \in \mathbb{Z}_+$, $n \in \mathbb{Z}_+$, $c \in \mathbb{R}^n$, $\ell \in \mathbb{R}^n$, $u \in \mathbb{R}^n$, $b \in \mathbb{R}^m$ and $A \in \mathbb{R}^{m \times n}$. They are given in a file of

```
the form:
           n
 c_0
           c_1
                     c_2
                                          c_{n-1}
 \ell_0
                     \ell_2
 u_0
 a_{0,0}
              a_{0,1}
                          a_{0,2}
                                                 a_{0,n-1}
 a_{1,0}
              a_{1.1}
                          a_{1,2}
                                                 a_{1,n-1}
 a_{m-1,0} a_{m-1,1} a_{m-1,2} ... a_{m-1,n-1}
```

All the numbers given in input will have an absolute value smaller than 10^9 , and $\ell_j \leq u_j$ for all $j = 0, 1, \ldots, n-1$.

The output file contains two lines (aside from optional comment and empty lines that are ignored, see below). The first line is either the word **infeasible** if the problem is infeasible, or the word **optimal** if the problem is feasible. The second line contains n + m numbers that can be -1, 0, or 1. Each of these numbers describes the status of the corresponding column in the final tableau: -1 means at lower bound, 1 means at upper bound, and 0 means basic. If the problem is feasible, then this tableau must be optimal. Otherwise, it is the tableau that is in use when the ratio test detects infeasibility.

Note that there are n+m columns and not just n: indices $n, \ldots, n+m-1$ correspond to artificial variables fixed to zero that are used to create a starting basis. They are the z variables in the equivalent problem

$$\begin{aligned} & \text{min} & & c^Tx + 0^Tz \\ & \text{s.t.} & & Ax + Iz = b \\ & & & \ell \leq x \leq u \\ & & & 0 \leq z \leq 0 \\ & & & & x \in \mathbb{R}^n, z \in \mathbb{R}^m. \end{aligned}$$

In order to (optionally) let you include more information in the output file, everything between a # sign and the end of a line with significant and the end of a line with si

Example input and output files are given at https://www.math.uwaterloo.ca/lpoirrie/co353.html.

https://eduassistpro.github.io/ Running the code

Your code must take exactly two arguments. The first argument is the name of a file where the output is to be written.

You have a choice between the following languages for the implementation: C, C++ or Python.

3.1 In C or C++

Your code must be portable to any environment with a standards-conforming C or C++ compiler. It must be possible to compile and run it by using the following commands:

In other words, you must implement your code in a file called dsm.c (in C) or dsm.cpp (in C++). DSM stands for Dual Simplex Method.

Note: Optionally, you may provide a Makefile, in which case your code will be compiled by running make. The resulting executable must be named dsm. If you choose to do this, it is your responsibility to ensure that the Makefile is correct, so do it only if you are familiar with Makefiles already.

3.2 In Python

It must be possible to run your code by executing the following command:

```
python dsm.py input.txt output.txt
```

In other words, you must provide a source file called dsm.py (if you want, dsm.py can import code from other files). DSM stands for Dual Simplex Method. If you need a specific version of the Python language, include the string "python2" or "python3" somewhere in dsm.py, for example in a comment.

4 Submitting the project

You submit your implementation by sending a single email to both lpoirrier (at uwaterloo) and witoth (at uwaterloo), by 8pm on Monday, March 19th, 2018. Late submissions will not be accepted. The subject line of your email must contain the string C0353. Your email must contain a single attachment file: an archive in the format .zip or .tgz. The name of the archive is formed by the UWaterloo IDs of your group members, in any order, separated by underscores. For example: jwtoth_lpoirrie.tgz. The archive contains (at least) two files:

Assignment Project Exam Help

- a file called notes.

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The file notes.txt only specifies the names of the (1, 2 or 3) members of your group. No further explanations are required for this assignment (although you are allowed to put explanation you did particularly well in our Gle). We Chat edu_assist_property of the control ething

5 Contribution

You can use the standard library in your language of choice. In addition, you are allowed (and strongly advised) to use an external library that handles linear algebra, in particular matrix operations. For C++ you can use Eigen, for Python you can use NumPy. Do not include these libraries in the archive that you send by email: you can assume that they are installed and available (for example, #include "Eigen/Dense", #include <Eigen/Dense>, import numpy and from numpy import * will all work in their respective languages). If you prefer, you can choose another library for linear algebra (i.e. not Eigen or Numpy), but **only if** you first get my approval by email by March 5th (in particular, libraries that feature an implementation of the simplex method will not be allowed).

Aside from that, no other library is allowed. In case of doubt ask me. You can consult any source of information you want (books, internet, scientific papers, etc.), but copying code is not allowed, regardless of the source. Every single line of your code must be written by a member of the group. Each member of the group must understand (and must be able to justify) every line of the code, including the ones they did not write. After the due date, I may call an individual group member to come to my office hours; if that member does not show sufficient understanding of the code, *all* group members will get zero.

6 Grading criteria

The project will be graded on a total of 15 marks, divided in 5 categories. Pay attention to the first one: if your code does not follow the specification, it will not be tested, and you will get zero for all the rest.

- Specification (1 mark). Your submission must follow the specifications given in this document (your email must have the correct recipients/subject/attachment, your source files must follow the template given above, your code must compile and take the right arguments). The rules are rigid because testing will be automated.
- Code quality (2 marks). It should be reasonably easy to understand your code. Comments can be used to help in that regard, but with moderation. The code itself must be clear and readable.
- Correctness (4 marks). Your code must be an implementation of the dual simplex method with general lower and upper points and upper points are the properties feasible in put of authorized an optimal solution. When the EP instance is infeasible, this must be correctly identified.
- Robustness (4 marks).

 floating-point inaccinttps://eduassistpro.github.io/ nd handle them properly.
- Efficiency (4 marks). Your code prest not be more than 100 use language. Add WeChat edu_assist_pro