

COMP 250

INTRODUCTORY SCIENCE

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Week 11-3 Bin

Giulia Alberini, Fall 2020

Slides adapted from Michael Langer's

WHAT ARE WE GOING TO DO IN THIS VIDEO?



- Binary Trees Assignment Project Exam Help
- Expression Tree <https://eduassistpro.github.io/>
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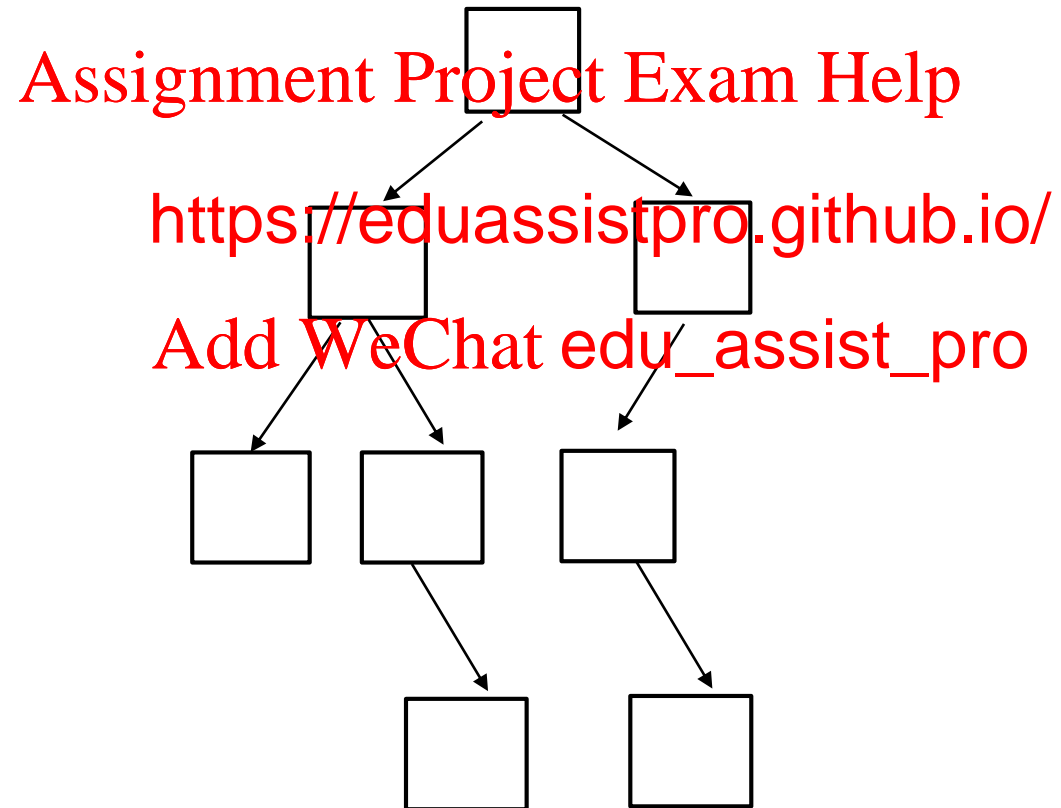
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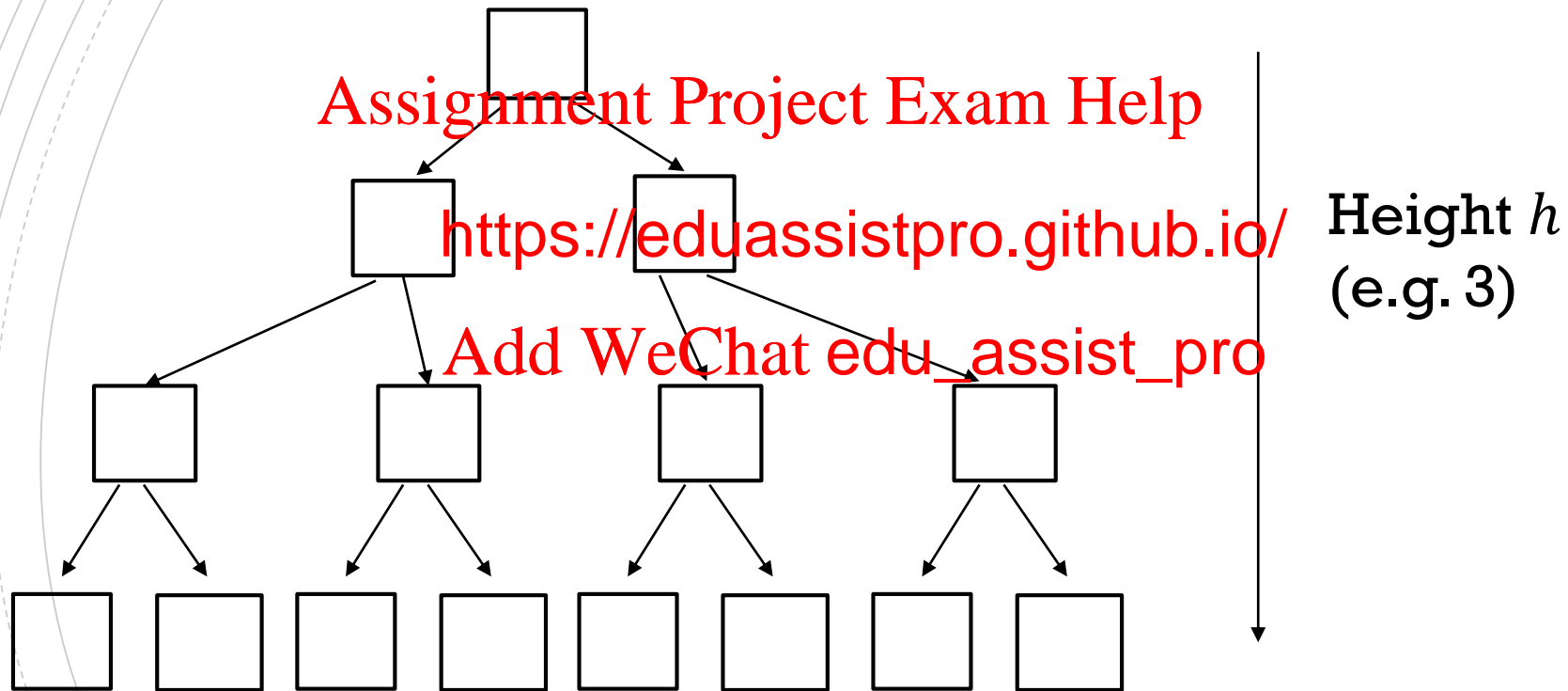
BINARY TREES

Each node has at most 2 children!



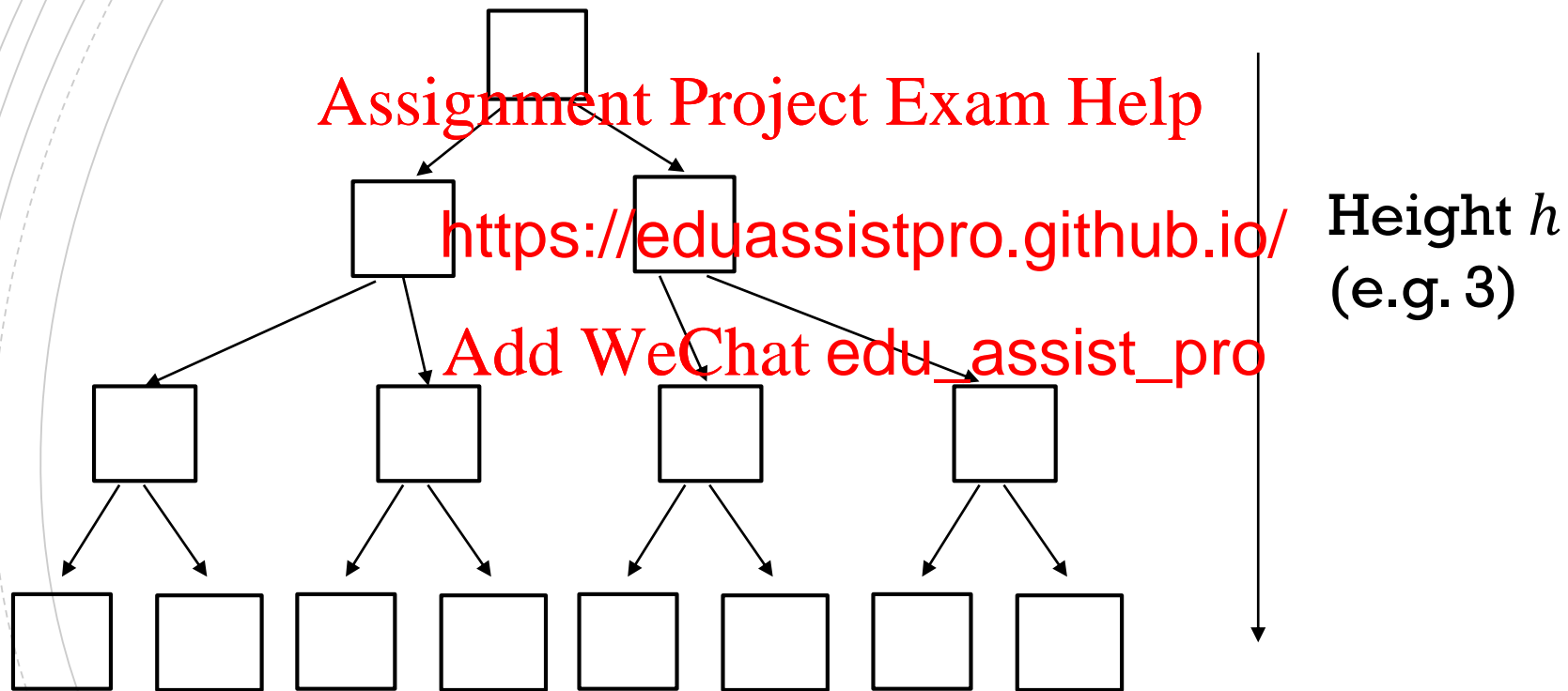
BINARY TREES

Q: What is the maximum number of nodes n in a binary tree of height h ?



BINARY TREES

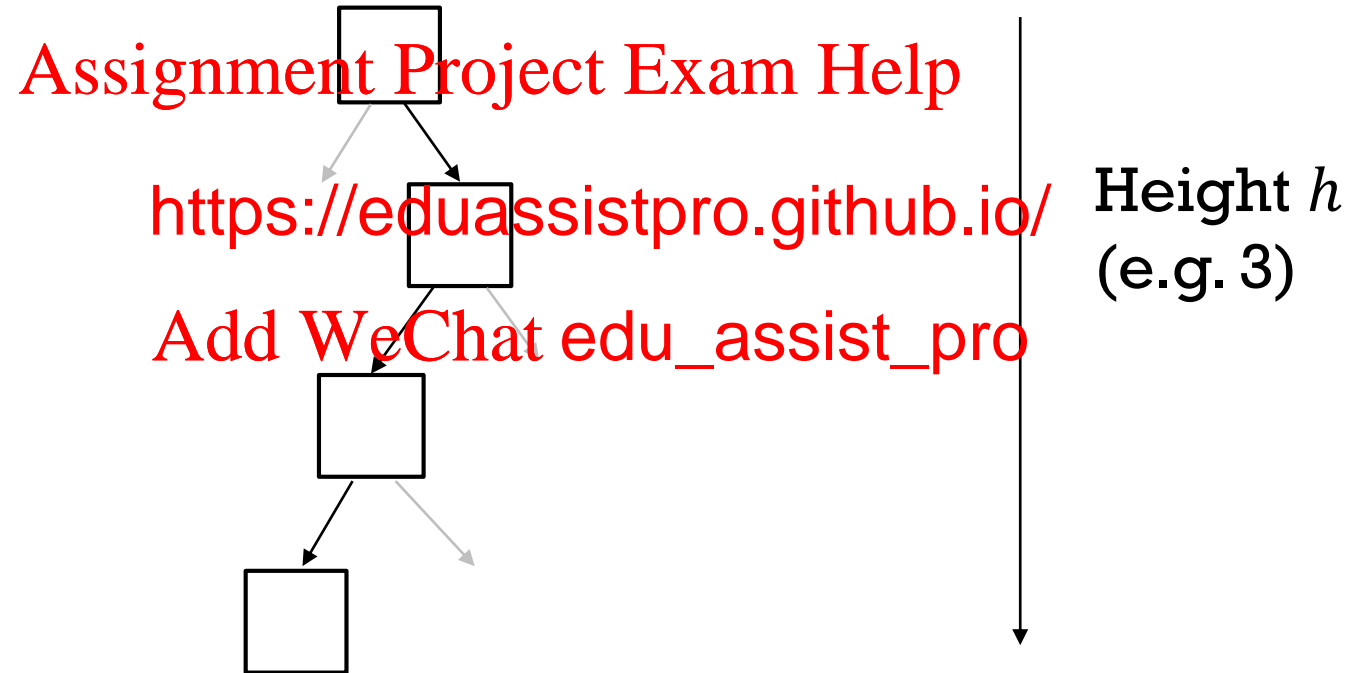
Q: What is the maximum number of nodes n in a binary tree of height h ?



A:
$$n = 1 + 2 + 4 + \dots + 2^h = 2^{h+1} - 1$$

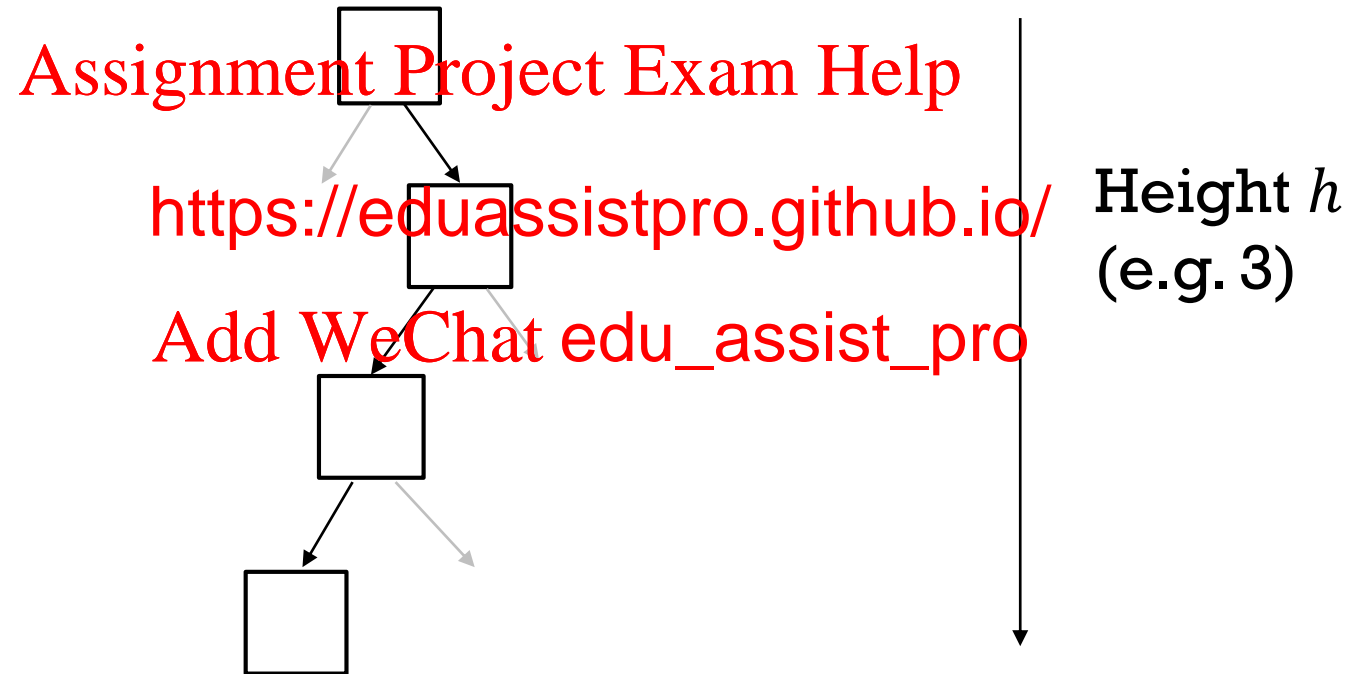
BINARY TREES

Q: What is the minimum number of nodes n in a binary tree of height h ?



BINARY TREES

Q: What is the minimum number of nodes n in a binary tree of height h ?



A: $n = h + 1$

BINARY TREES - IMPLEMENTATION

```
class BTree<T>{
```

```
    BTreeNode<T>    root;
```

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```
class
```

```
    T element;
```

```
    BTreeNode<T> leftchild;
```

```
    BTreeNode<T> rightchild;
```

```
        :
```

```
    }
```

```
}
```

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BINARY TREE TRAVERSAL (DEPTH FIRST)

Rooted Tree
(last lecture)

Binary Tree

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```
depthFirst(root) {  
  if (root is not empty) {  
    visit root  
    for each child of root  
      depthFirst( child )  
  }  
}
```

BINARY TREE TRAVERSAL (DEPTH FIRST)

Rooted Tree
(last lecture)

Binary Tree

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```
preorder (root) {  
    if (root is not empty) {  
        visit root  
        for each child of root  
            preorder ( child )  
    }  
}
```

```
rBT (root) {  
    if (root is not empty) {  
        visit root  
        preorderBT (root.left)  
        preorderBT (root.right)  
    }  
}
```

BINARY TREE TRAVERSAL (DEPTH FIRST)

```
preorderBT (root) {  
    if (root is not empty) {  
        visit root  
        preorderBT (root.left)  
        preorderBT (root.  
    }  
}
```

```
postorderBT (root) {
```

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BINARY TREE TRAVERSAL (DEPTH FIRST)

```
preorderBT (root) {  
    if (root is not empty) {  
        visit root  
        preorderBT (root.left)  
        preorderBT (root.  
    }  
}
```

```
postorderBT (root) {  
    if (root is not empty) {  
        postorderBT (root.left)  
        postorderBT (root.right)  
        visit root  
    }  
}
```

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BINARY TREE TRAVERSAL (DEPTH FIRST)

```
preorderBT (root) {
    if (root is not empty) {
        visit root
        preorderBT (root.left)
        preorderBT (root.
    }
}
```

```
postorderBT (root) {
    if (root is not empty) {
        postorderBT (root.left)
        postorderBT (root.right)
        visit root
    }
}
```

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```
inorderBT (root) {
```

}

BINARY TREE TRAVERSAL (DEPTH FIRST)

```
preorderBT (root) {  
    if (root is not empty) {  
        visit root  
        preorderBT (root.left)  
        preorderBT (root.  
    }  
}
```

```
postorderBT (root) {  
    if (root is not empty) {  
        postorderBT (root.left)  
        postorderBT (root.right)  
        visit root  
    }  
}
```

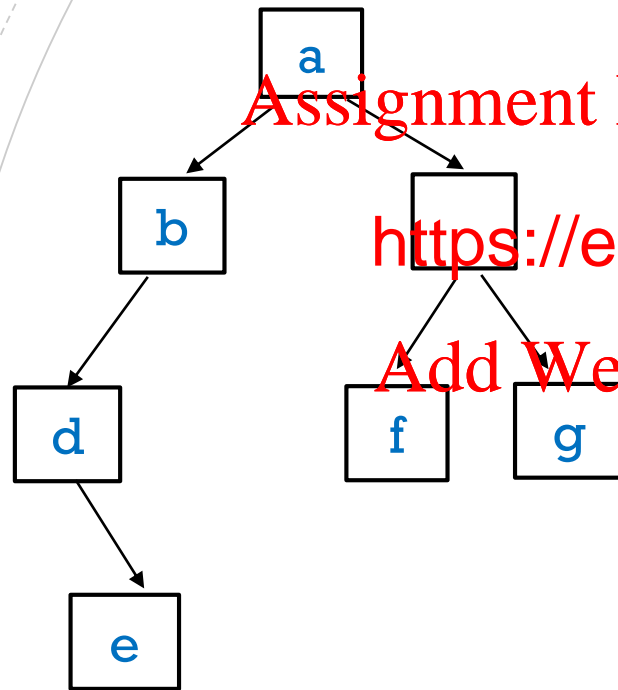
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```
inorderBT (root) {  
    if (root is not empty) {  
        inorderBT (root.left)  
        visit root  
        inorderBT (root.right)  
    }  
}
```

EXAMPLE



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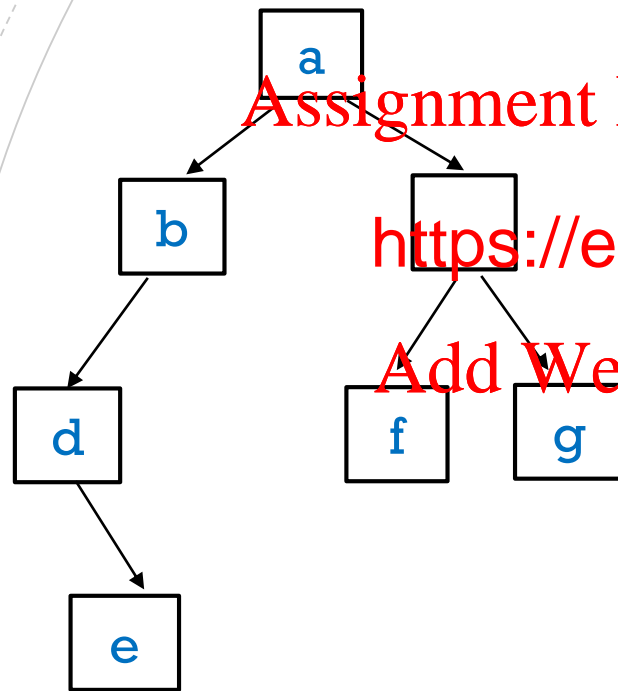
der:

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Post order:

EXAMPLE



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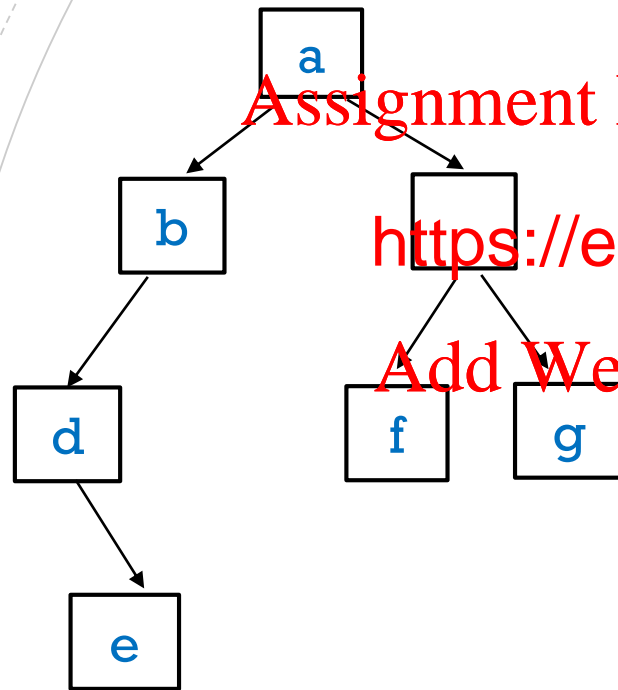
der: a b d e c f g

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Post order:

EXAMPLE



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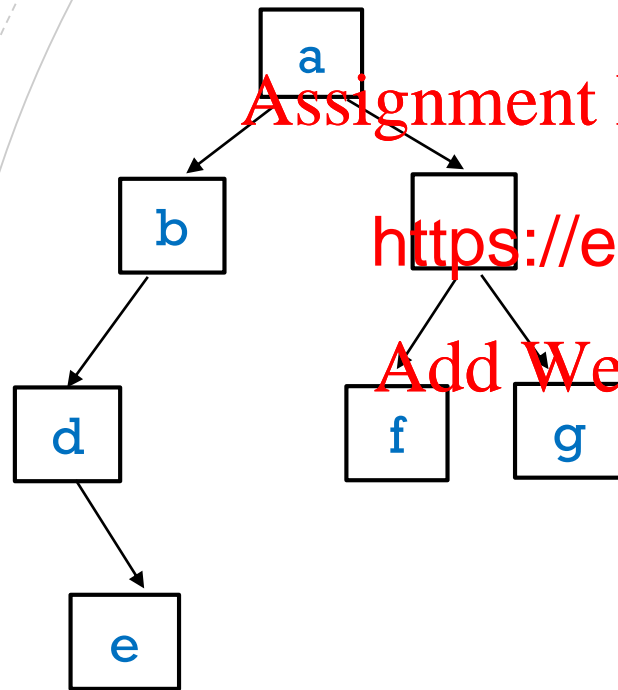
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der: a b d e c f g

d e b a f c g

Post order:

EXAMPLE



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der: a b d e c f g

d e b a f c g

Post order: e d b f g c a

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EX <https://eduassistpro.github.io/> EES
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EXPRESSION TREES

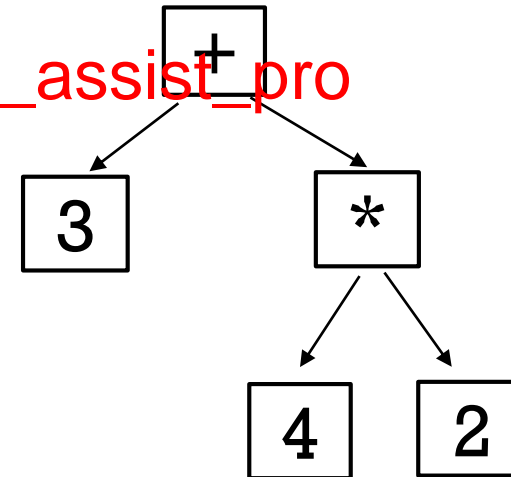
e.g. $3 + 4 * 2$

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$3 + (4 * 2)$

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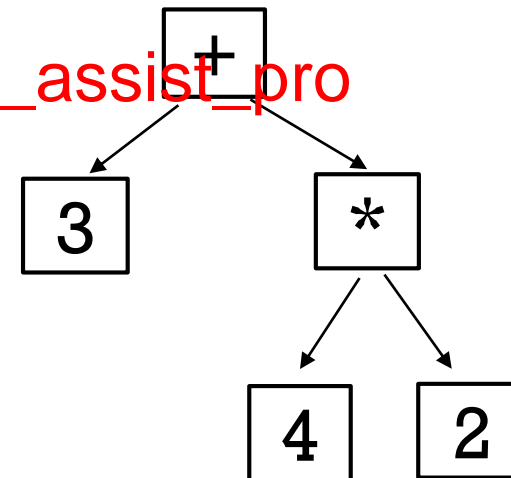
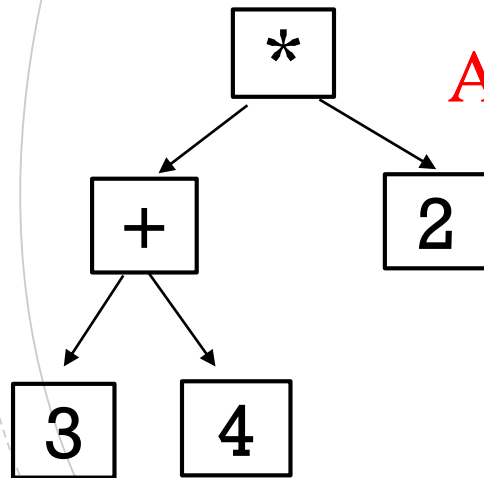
EXPRESSION TREES

e.g. $3 + 4 * 2$

$(3 + 4) * 2$ $3 + (4 * 2)$

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My Windows calculator says

$$3 + 4 * 2 = 14.$$

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<https://eduassistpro.github.io/> + 4) * 2 = 14.

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if I google “3+4*2”, I get 11.

$$3 + (4*2) = 11.$$

EXPRESSIONS

We can make expressions using binary operators $+$, $-$, $*$, $/$, $^$

e.g. $a - b / c + d * e ^ f ^ g$

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$^$ is exponentiation: <https://eduassistpro.github.io/>

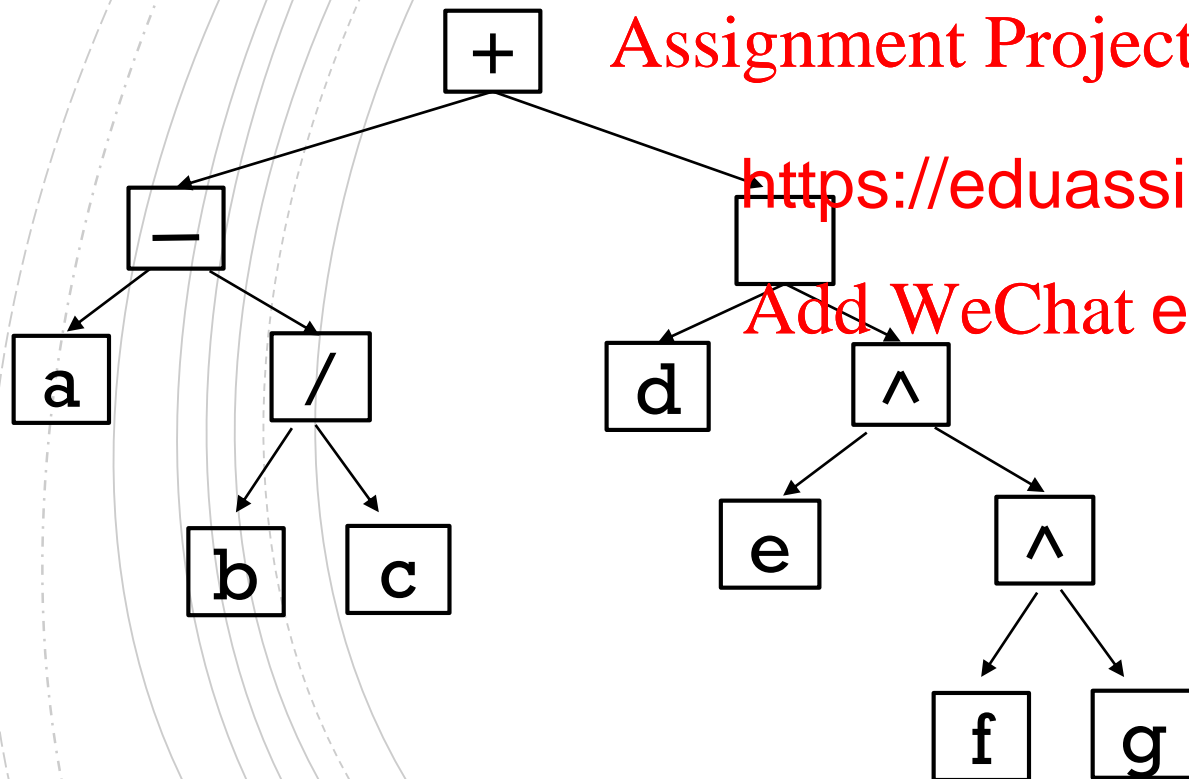
We don't consider unary operators e $3 + (-4)$
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Operator precedence ordering makes brackets unnecessary.

$$(a - (b / c)) + (d * (e ^ (f ^ g)))$$

EXPRESSION TREE

$$a - b / c + d * e ^ f ^ g \equiv (a - (b / c)) + (d * (e ^ (f ^ g)))$$



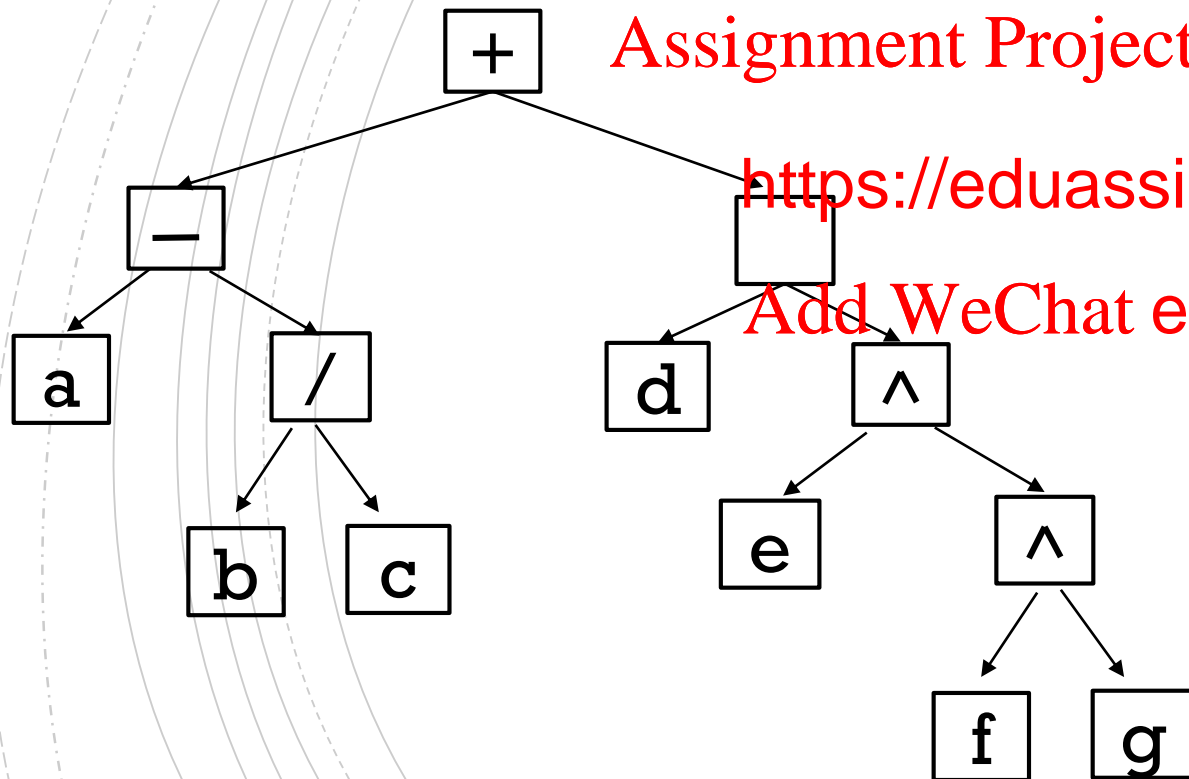
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1 nodes are operators.
s are operands.

EXPRESSION TREE



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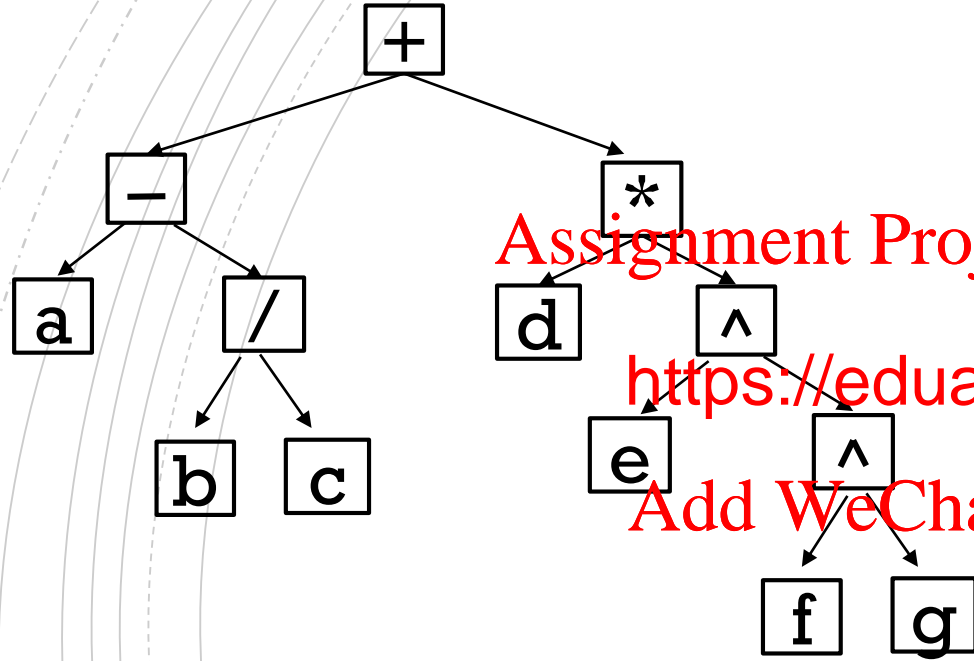
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An expression tree can be a way of *thinking about* the ordering of operations used evaluating an expression.

But to be concrete, *let's assume we have a binary tree data structure.*

EXPRESSION TREE – TRAVERSAL



preorder traversal gives:

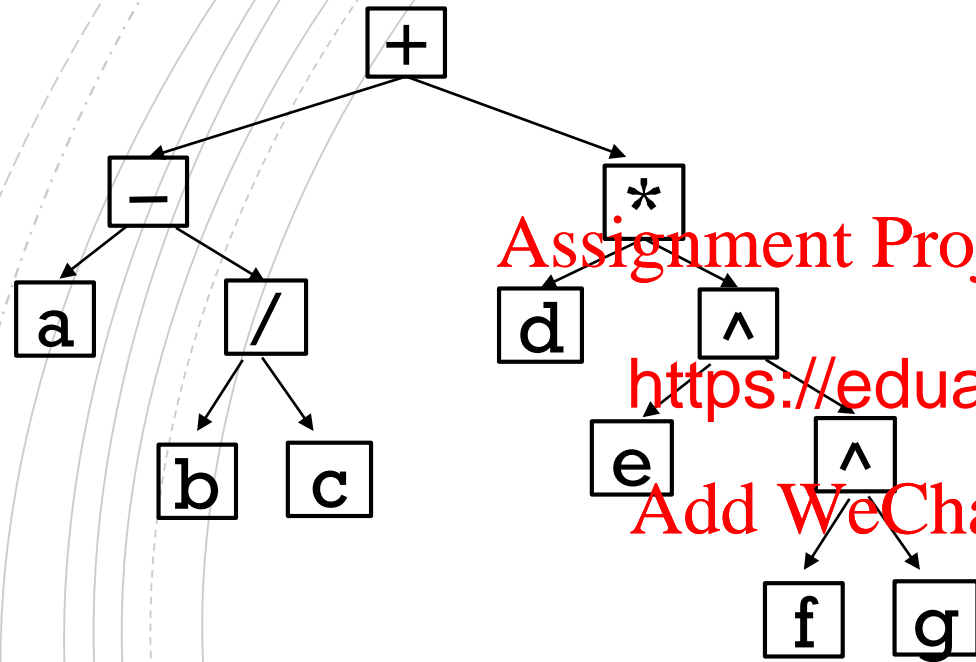
If we traverse an expression tree,
and *print out* the node label, what
expression printed out?

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EXPRESSION TREE – TRAVERSAL



If we traverse an expression tree,
and *print* out the node label, what
expression printed out?

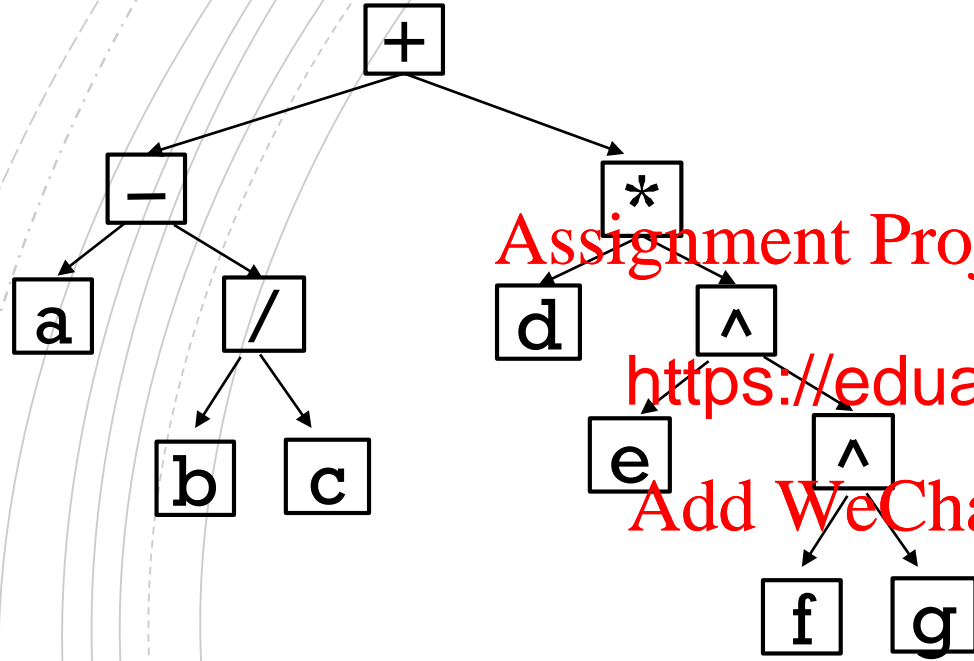
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preorder traversal gives: $+ - a / b c * d ^ e ^ f g$

EXPRESSION TREE – TRAVERSAL



If we traverse an expression tree,
and *print* out the node label, what
expression printed out?

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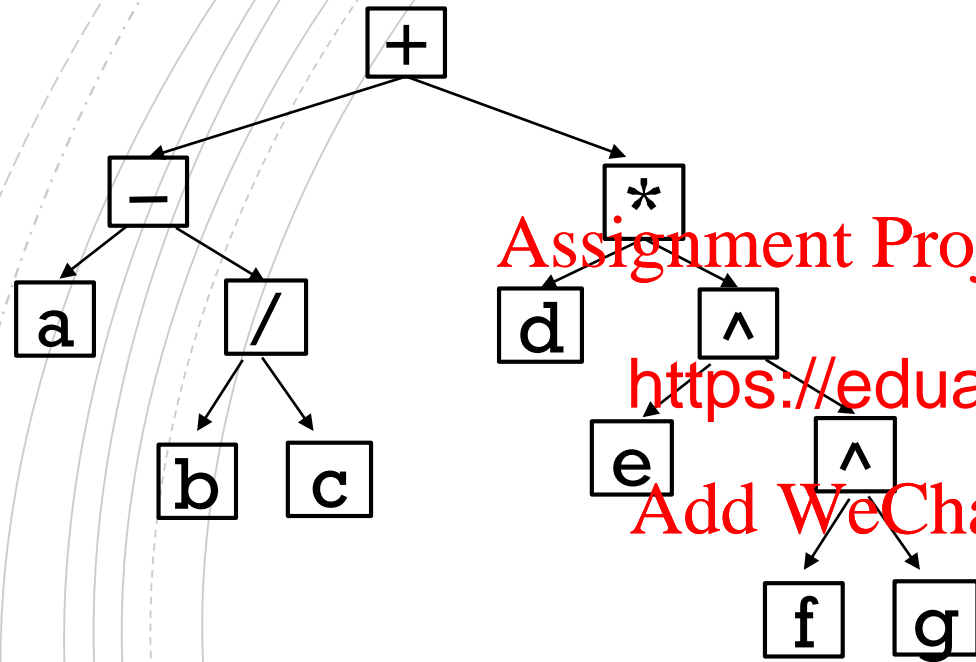
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preorder traversal gives: + - a / b c * d ^ e ^ f g

inorder traversal gives:

EXPRESSION TREE – TRAVERSAL



If we traverse an expression tree,
and *print* out the node label, what
expression printed out?

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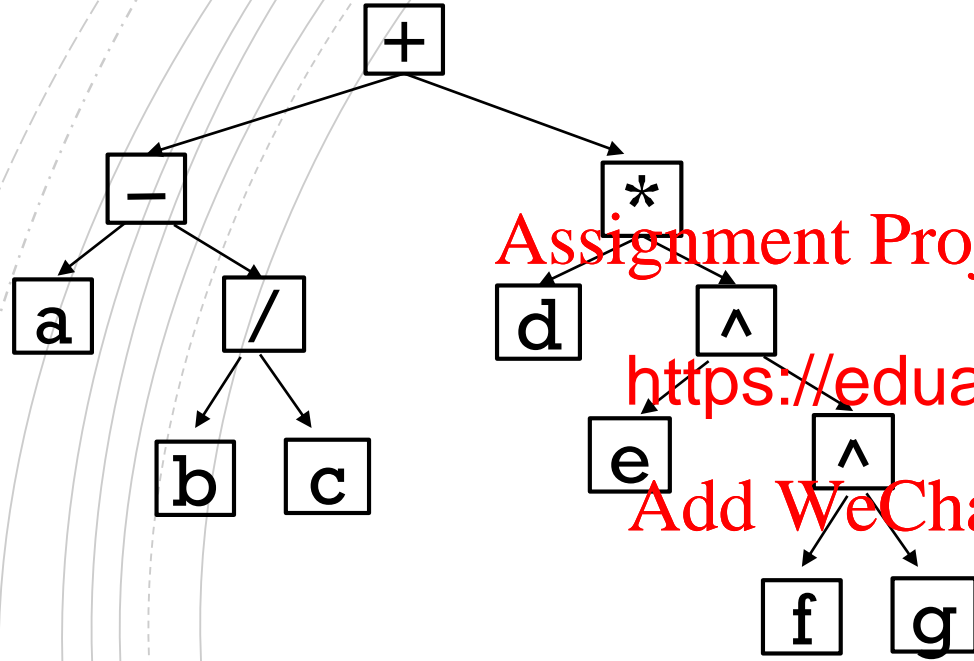
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preorder traversal gives: $+ - a / b c * d ^ e ^ f g$

inorder traversal gives: $a - b / c + d * e ^ f ^ g$

EXPRESSION TREE – TRAVERSAL



If we traverse an expression tree,
and *print* out the node label, what
expression printed out?

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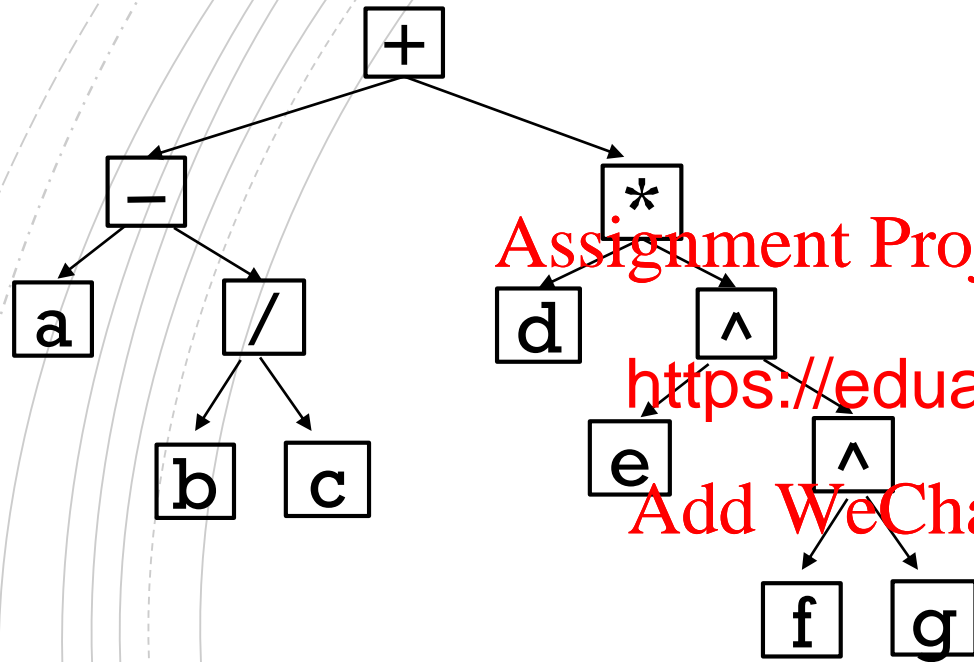
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preorder traversal gives: $+ - a / b c * d ^ e ^ f g$

inorder traversal gives: $a - b / c + d * e ^ f ^ g$

postorder traversal gives:

EXPRESSION TREE – TRAVERSAL



If we traverse an expression tree,
and *print* out the node label, what
expression printed out?

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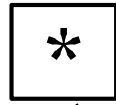
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preorder traversal gives: $+ - a / b c * d ^ e ^ f g$

inorder traversal gives: $a - b / c + d * e ^ f ^ g$

postorder traversal gives: $a b c / - d e f g ^ ^ * +$

PREFIX, INFIX, POSTFIX EXPRESSIONS



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prefix: * a b

infix: a * b

postfix: a b *

PREFIX, INFIX, POSTFIX EXPRESSIONS

baseExp = variable | integer

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op = + | <https://eduassistpro.github.io/>

preExp = baseExp | op **preExp**

where | means 'or'

PREFIX, INFIX, POSTFIX EXPRESSIONS

baseExp = variable | integer

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op = + | <https://eduassistpro.github.io/>

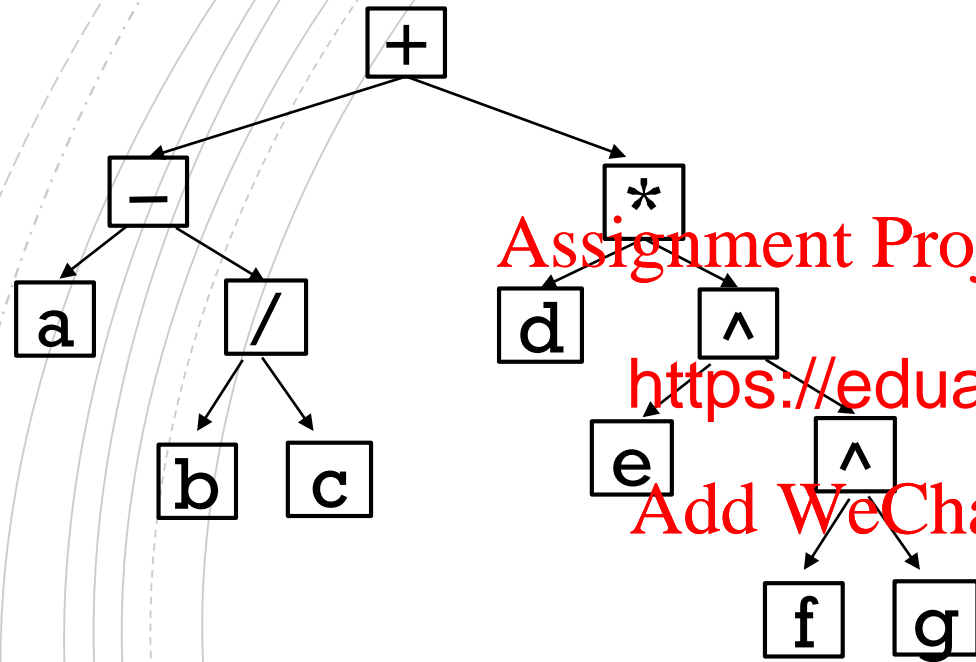
preExp = baseExp | op preExp

inExp = baseExp | inExp op inExp

postExp = baseExp | postExp postExp op

Use
only
one.

EXPRESSION TREE – TRAVERSAL



If we traverse an expression tree,
and *print* out the node label, what
expression printed out?

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preorder traversal gives **prefix expression**: $+ - a / b c * d ^ e ^ f g$

inorder traversal gives **infix expression**: $a - b / c + d * e ^ f ^ g$

postorder traversal gives **postfix expression**: $a b c / - d e f g ^ ^ * +$

TERMINOLOGY

- **Prefix** expressions called “Polish Notation”
(after Polish logician Jan Lucasewicz 1920's)
<https://eduassistpro.github.io/>
Assignment Project Exam Help
- **Postfix** expressions
<https://eduassistpro.github.io/> “Polish notation” (RPN)
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Some calculators (esp. Hewlett Packard) require users to input expressions using RPN.

TERMINOLOGY

- **Prefix** expressions called “Polish Notation”
(after Polish logician Jan Lucasewicz 1920's)

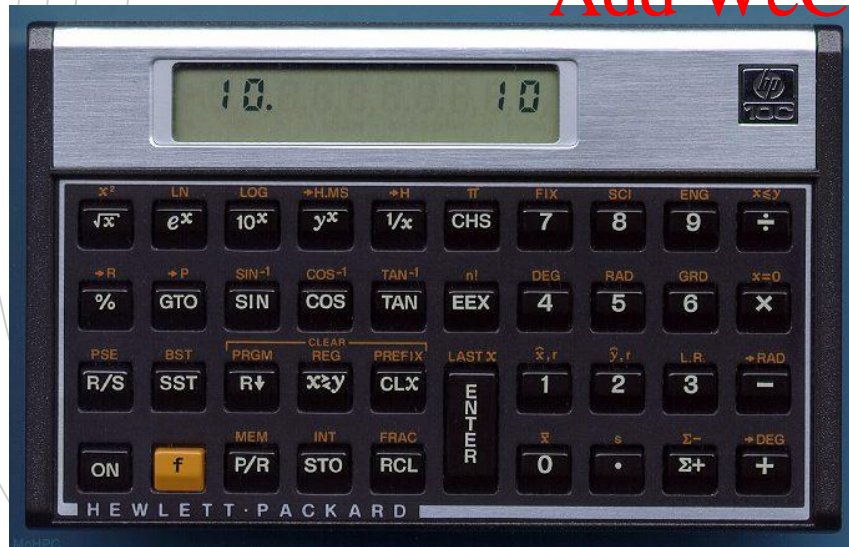
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- **Postfix** expressions

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lish notation” (RPN)

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* 4 + 3 :



5 <enter>
4 <enter>
* <enter>
3 <enter>
+ <enter>

No “=” symbol on keyboard.

An orange paint roller with a red handle, positioned horizontally. The roller is partially filled with orange paint, and there are orange paint splatters and drips around it. The text "Coming Soon" is written in white on the orange background of the roller.

Coming Soon

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In the next

- Binary S <https://eduassistpro.github.io/>
- Heaps Add WeChat edu_assist_pro