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Rende

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Mobile Agent
Robots

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Drones

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Assignment Project Exam Help

- MA Model
 - Tokens
 - RV Algorithms
 - Two MAs
 - Time/Mem
 - Rendezvous
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Rendezvous

Leader Election

- Two Mobile Agents (MAs) init of a graph ~~Add WeChat edu_assist_pro~~ arbitrary nodes can move along edges at same speed.
- **RV** (Rendezvous) means the MAs meet. It is a form of gathering and a very basic form of information exchange.
- **RVP** (Rendezvous) Problem.
 - Give an algorithm <https://eduassistpro.github.io/>ous regardless of their starting position ~~Add WeChat edu_assist_pro~~ may never terminate
 - The requirement is to cause rendezvous is not possible rendezvous will never happen, and the algorithm will be running for ever!
- **RVD**: Rendezvous Problem with Detection
 - A rendezvous algorithm is required to detect whether or not rendezvous is possible and if it is to cause rendezvous.

Graph Model

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Meeting Point

2D Geometric Model



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3D Geometric Model

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Gathering Assignment Project Exam Help

- For more than two agents in a graph (referred to) as Gathering.
Also known as [Add WeChat edu_assist_pro](#)
- $Gather(k)$ means that k MAs meet.
- $Gather(2)$ is the same as [BV](#)

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MAs vs Message Passing Assignment Project Exam Help

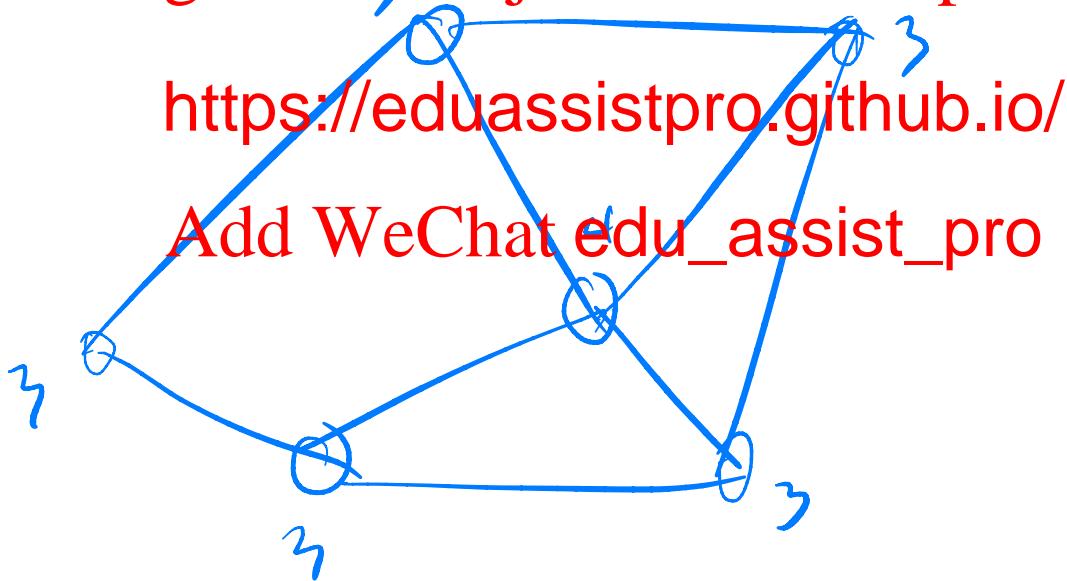
- So far, in distributed computation, messages that were being sent along vertices of a network
 - The nodes were the processors that enabled the distributed computation.
- This *distributed* setting remains, but now also
 - we have autonomy on vertices of a distributed network
 - the agents are mobile; not only they can move so they can participate in distributed computations.
- The rendezvous problem can be stated for any topology.

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Where/How can you rendezvous?
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- Exploit network assymetrie
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- Exploit topological (geometries)
- In a general graph the problem is quite complex!

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Special Topology: Ring Assignment Project Exam Help

- We look only at ring topologies.
- Even in a ring the problem is quite c
- k MAs are initially located on k nodes of an n node ring.

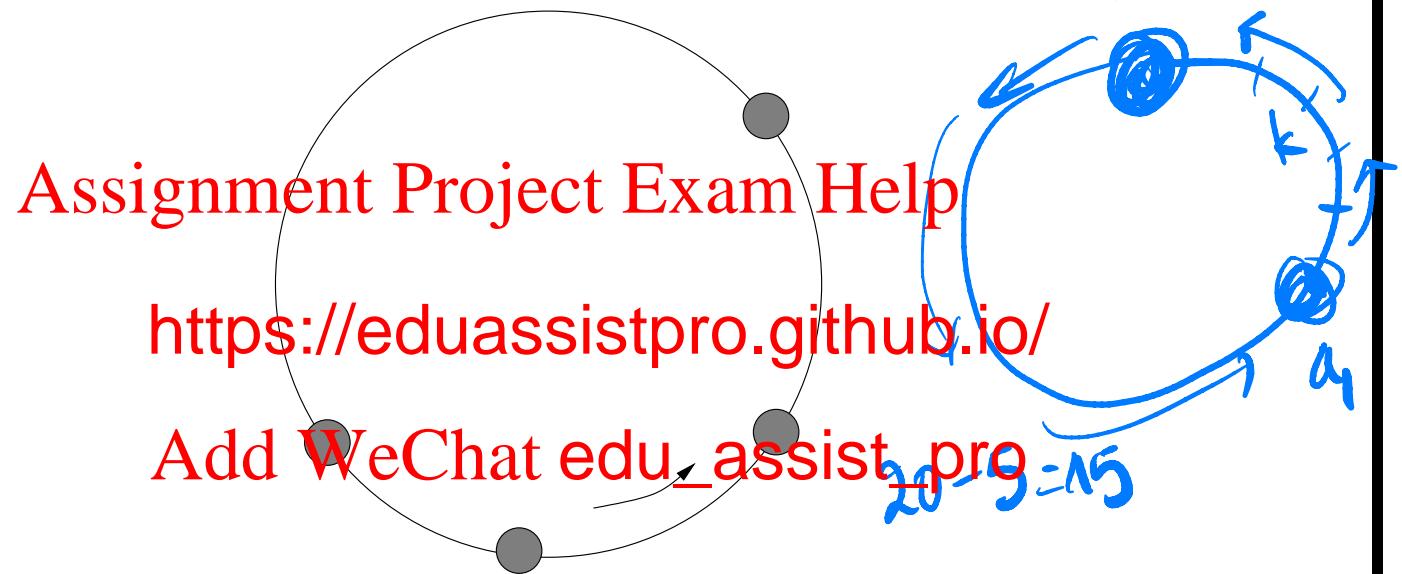


- Assume a synchronous system with common sense of direction.
- Will be restricted to the case of $k = 2$ MAs.

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Ring, Mobile Agents, and Tokens Assignment Project Exam Help

- Each of the MAs has a token which to leave) [Add WeChat edu_assist_pro](https://eduassistpro.github.io/)



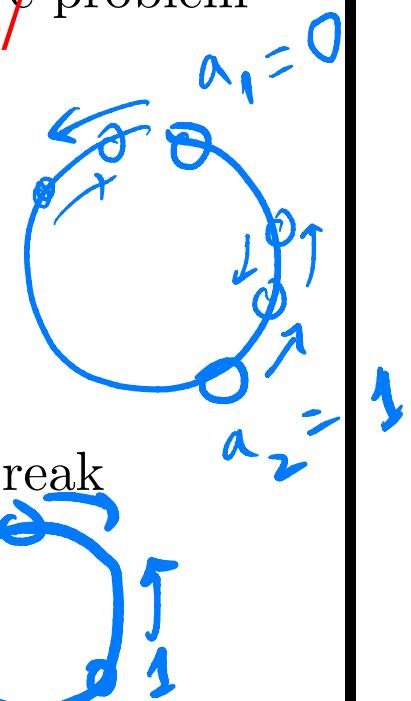
Every agent owns its own token and can release it at any node; the tokens are indistinguishable

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Approaches to Rendezvous (1/2)

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- In general, to solve the rendezvous problem just try to break the inherent symmetry.
1. If the MAs have unique IDs you can break symmetry and the problem becomes, sometimes, easier to solve!
2. If the MAs do not have unique IDs and the network nodes are anonymous, the problem is difficult and so
- In principle, we have to break symmetry.
 - either deterministically, or
 - using randomization.
 - Sometimes we can use the underlying topology to break symmetry.



$$k < \frac{n}{2}$$

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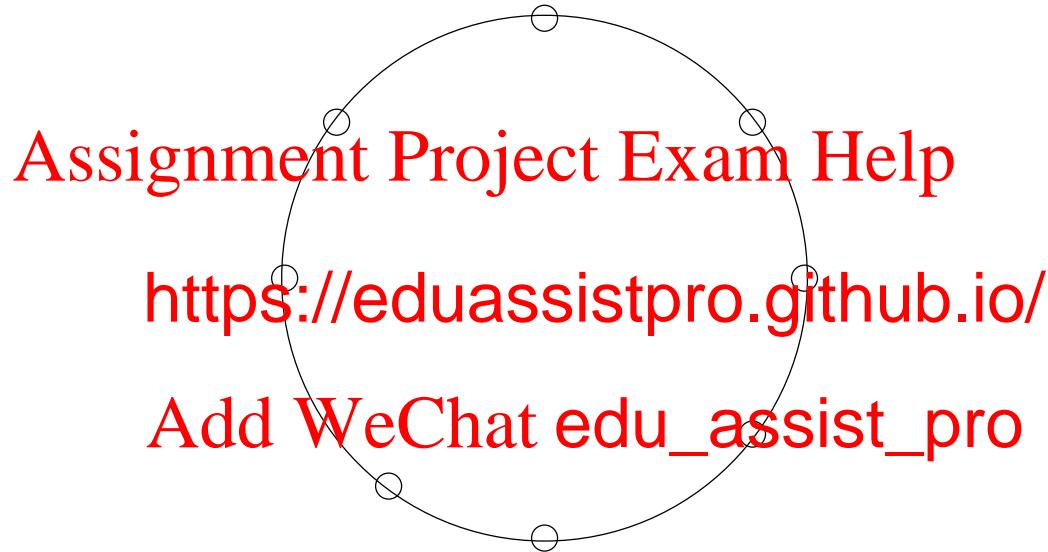
Approaches to Rendezvous (2/2) Assignment Project Exam Help

- Mobile agents have **identifiable** distinguishable tokens, one token per MA, that they can recognize by position.
- We are interested in tradeoffs among
 - 1. number of tokens
 - 2. knowledge <https://eduassistpro.github.io/>
 - 3. time
 - 4. memory.

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The Model: Topology and the Nodes Assignment Project Exam Help

- There are n identical nodes that may reside.
- The topology is a ring.
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- For example, in the ring above there are $n = 8$ nodes and the MAs can traverse its vertices and edges.

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The Model: Synchronicity/Orientation Assignment Project Exam Help

- The characteristics of the topo
algorithms.



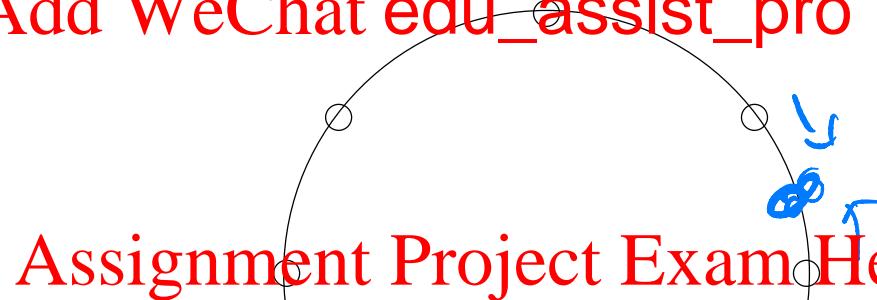
- Oriented means that there is a consistent sense of direction:
either CW or CCW.
 - As usual this is specified with ports.

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Where Can Rendezvous Occur? Assignment Project Exam Help

- Can rendezvous for two agents occur at an edge of the ring?

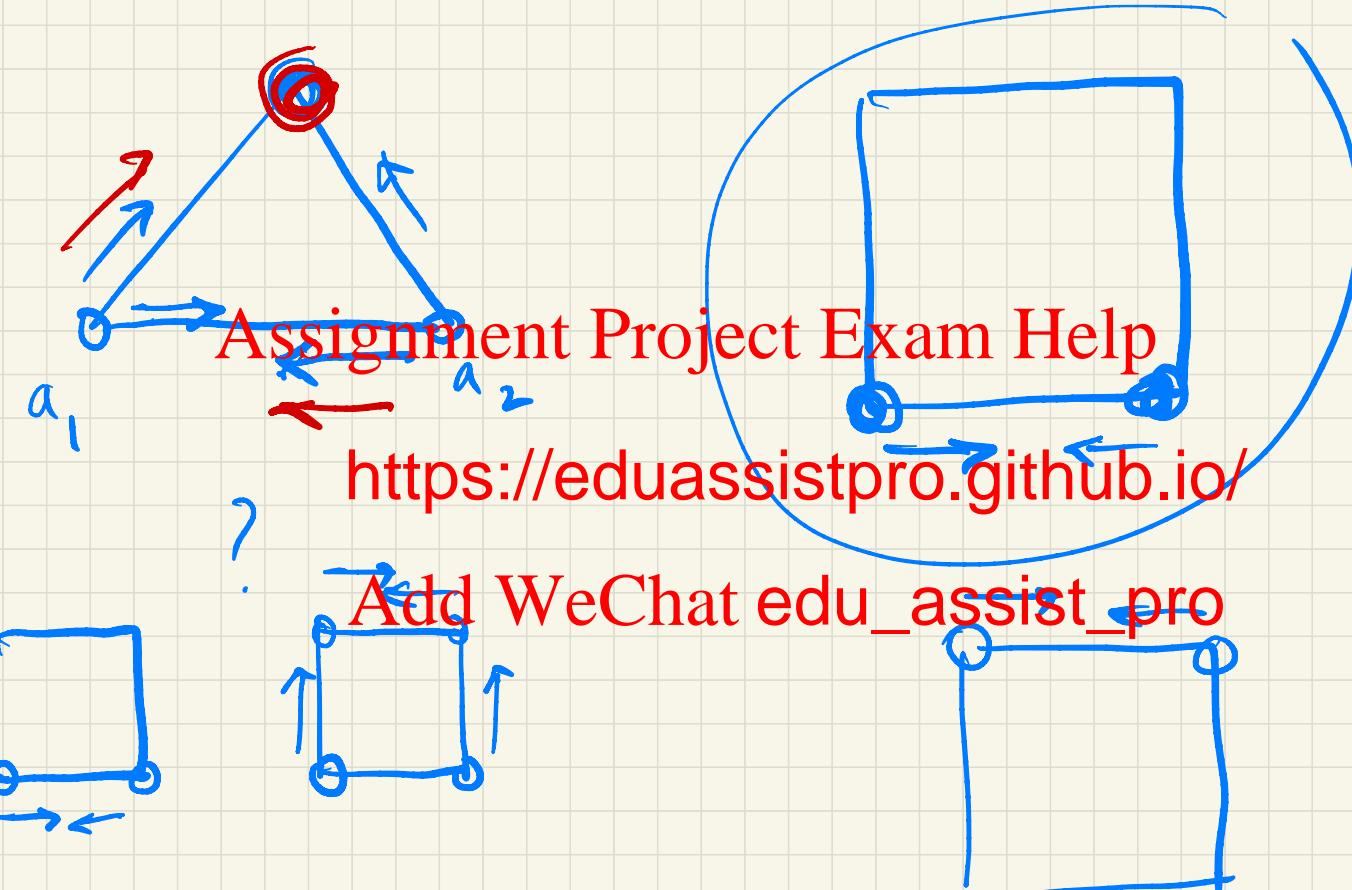
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- Can rendezvous for two agents occur at an edge of the ring?
- Yes, to both questions!



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Model Assignment Project Exam Help

- Anonymous, synchronous, a nted n node ring.
- A given node requires only enou st a token.
- Each MA, owns a single identical stationary token,
 - the tokens are indistinguishable and once they are positioned in t
- A token or MA at a giv same node
 - The MAs follow the **same** deterministic algorithm and begin execution at the same time
- Memory permitting, a MA can count the number of nodes visited, the number of nodes between tokens, or the total number of nodes in the network.

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Impossibility of RVD Assignment Project Exam Help

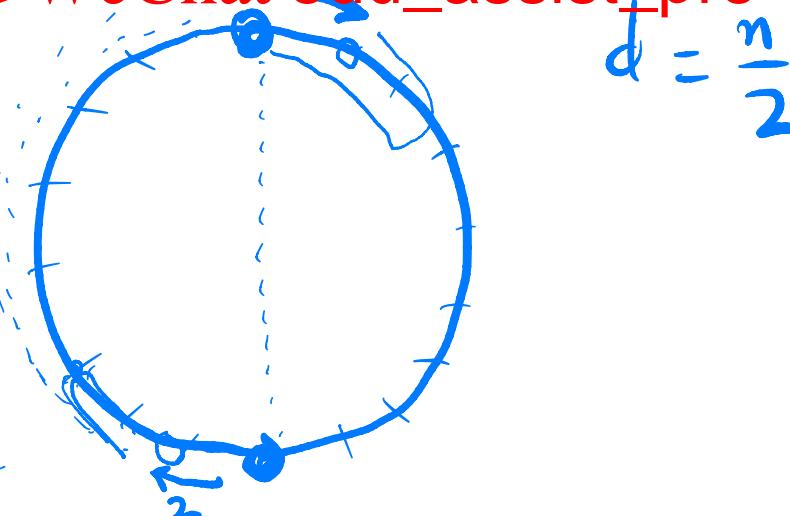
- Consider two identical, anonymous agents in a ring of size n . **Add WeChat edu_assist_pro**
- The agents have constant memory and can leave a token at their starting position.

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- **Theorem 1** N *ch that the MAs always converge appropriately, i.e., stop if $d = \frac{n}{2}$ and rendezvous*

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If one robot
can move
with speed 1
and the other
with speed 2!



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Rendezvous for two MAs
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- RV in a ring
 1. There are two identical MAs at distance d from each other.
 2. The ring may or may not be oriented.
 3. The ring has size n .

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- There are a lot of (simple) subtleties!

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1. Orientation Known, d Known
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$$d + \frac{d}{2}$$

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$$n - d > d$$

1. Release the token at starting position.
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2. Walk around ring in a counterclockwise direction.
3. If a token found within d steps, continue in same direction.
4. If no token found by d steps, reverse direction and continue.

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Correctness Assignment Project Exam Help

- There are two “competing” distances between the MAs:
 - d and $n - d$.
- Rendezvous is achieved if $d < n/2$.
 - What if $d = n/2$?
- How many steps do

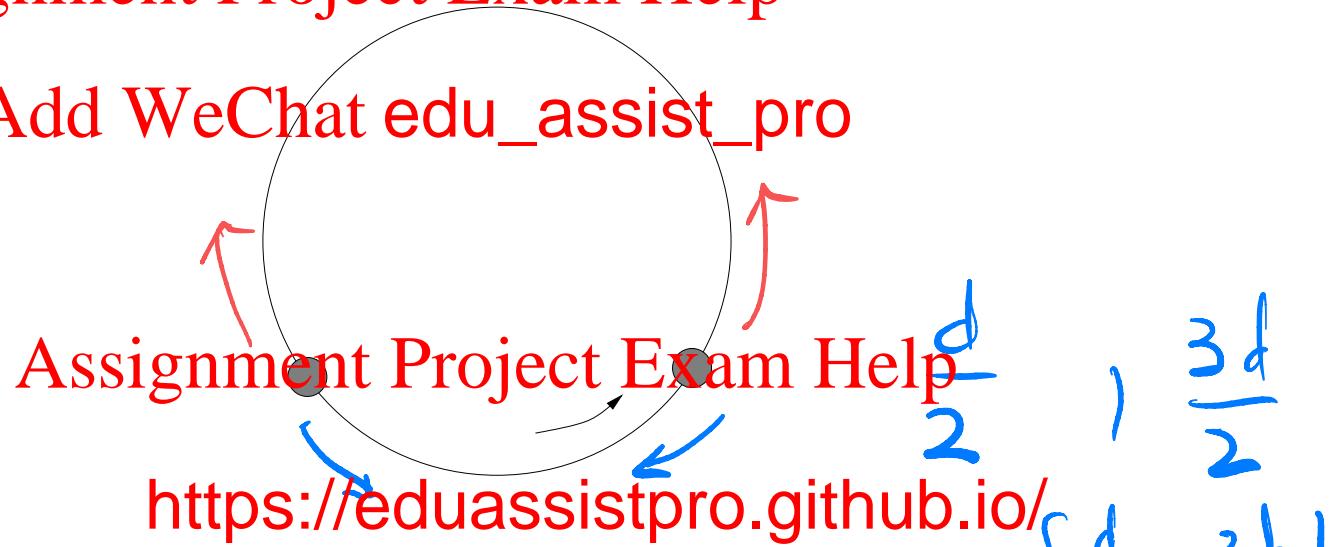
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2. Orientation not Known, d Known Assignment Project Exam Help

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1. Release the token.
2. Choose a direction and begin walking around the ring.
3. If a token is found within d steps, walk in the same direction.
4. If no token is found by d steps, reverse direction and continue.

$$\max \left\{ \frac{n-d}{2}, \frac{3(n-d)}{2}, \frac{d}{2}, \frac{3d}{2} \right\}$$

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Correctness Assignment Project Exam Help

- Similar to previous algorithm e elect either direction [Add WeChat edu_assist_pro](https://eduassistpro.github.io/)
- There are two “competing distances” measured by the MAs:
 - d and $n - d$.
- Rendezvous is ach
 - What if $d = \frac{n}{2}$?
- How many steps does it take to rendezvous?

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(initial distance
is $< \frac{n}{2}$)

$< \frac{n}{2}$

($\log n$)

1. Release the token.
2. Choose a direction and begin walking around the ring.
3. If a token is found within $\frac{n}{2}$ steps, continue in same direction.
4. Otherwise, reverse direction at $\frac{n}{2}$ steps and continue.

$d + (\text{reverse trip})$

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Correctness Assignment Project Exam Help

- Here algorithm does not need to know k
 - $n/2$ is being used as a threshold
- How many steps does it take to rendezvous?

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4. Orientation, d and n Are not Known.
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δ_1

Here the MAs must discover what is their distance!

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Time / <https://eduassistpro.github.io/> tradeoffs

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- Algorithm:

1. Release the token.
2. Choose a direction and begin walking around the ring.

3. Count # of steps to 1st token, δ_1 , and continue.
4. Count # of steps to 2nd token, δ_2 .

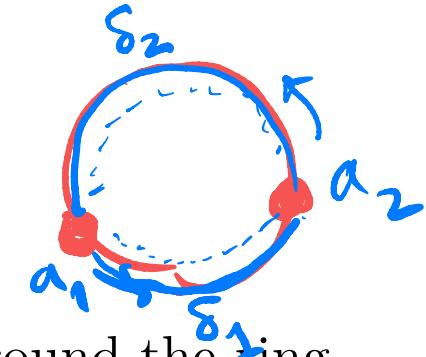
/* The MAs need memory <https://eduassistpro.github.io/>

5. If $\delta_1 < \delta_2$, continue walking in the same direction.
6. Otherwise, reverse direction and continue walking.

- MAs need memory $O(\log n)$.
- Under what conditions on δ_1, δ_2 does the algorithm work?

a_1 sees
 a_2

(δ_1, δ_2) (δ'_1, δ'_2) $\delta_1 < \delta_2$ stop
 $\delta_2 = \delta'_1 > \delta'_2 = \delta_1$

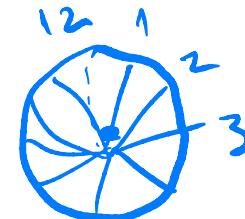


$\delta_1 \neq \delta_2$

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Improving on the Memory Assignment Project Exam Help

- A question remains:
 - can we improve on the memory $\log n$?



- Knowledge of n requires $\log n$ bits.
 - How can we test using less than $\log n$ bits?
 - Answer: Use m
- Previous algorithm was stringing whether or not $d \mid n - d$.
 - We will find a way to carry out the same test, but we will generate prime numbers to do so!
 - In fact, it will be a sequence of tests: in the end it will be confirmed which of $d < n - d$ or $n - d < d$ is valid

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Modular Arithmetic

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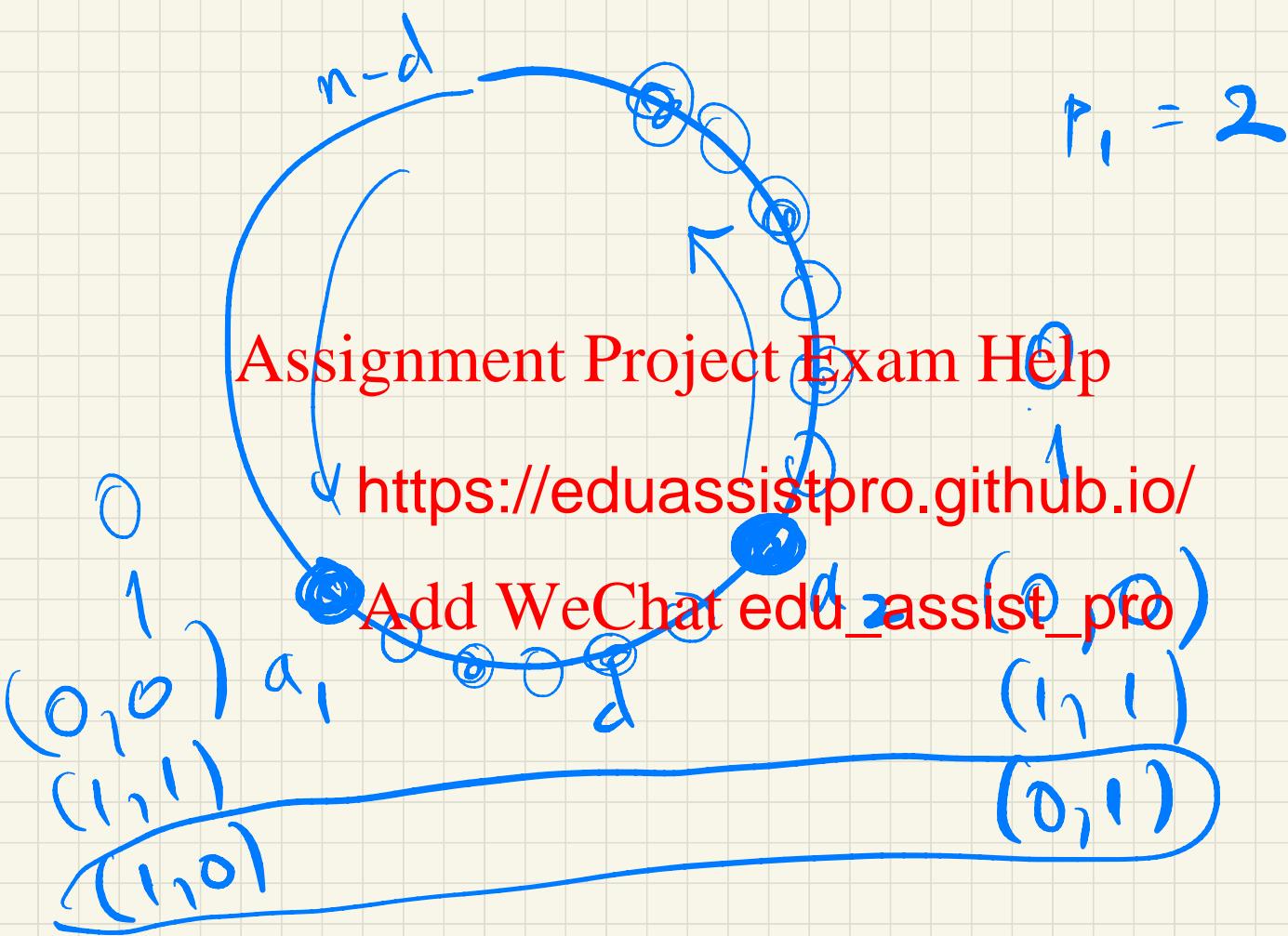
$$11054 : 45$$

$$11,055 : 45$$

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Algorithm Assignment Project Exam Help

1. Release the token.
 2. Set $m = p_1 \cdot \dots \cdot p_k$ Add WeChat edu_assist_pro
 3. Choose a direction and begin travelling around the ring.
 4. Count # of steps, mod m , to the first token, δ_1 , and continue walking. Assignment Project Exam Help
 5. Count the number of steps to the second token, δ_2 . /*
The MA is back at ISS https://eduassistpro.github.io/
 6. If $\delta_1 \bmod m = \delta_2 \bmod m$, set $m = p_1 \cdot \dots \cdot p_k$ Add WeChat edu_assist_pro repeat from step 4.
 7. If $\delta_1 \bmod m < \delta_2 \bmod m$, continue in the same direction.
 8. Else, reverse direction and continue travelling.
- All we are doing is trying to test whether or not $d < n - d$, but modulo consecutive primes!
 - MAs need to generate: p_1, \dots, p_k first k primes s.t. $\prod_{i=1}^k p_i > n$



$$P_2 = 3$$

0
1
2

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(0,0)
(1,1)
(2,2)
(1,2)

(0,1)
(1,2)
(2,1)

$$P_3 = 5$$

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Prime numbers are the
"building atoms" of numbers

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X, 2, 3, 5, 7, 11, 13, 17, 19
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Euclid (2,000 yrs ago)) Alexandria
There are infinitely many primes!

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Memory $O(\log \log n)$:

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- Theorem 2 The previous

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ires Memory

$O(\log n)$

and accomplishes rendezvous in time

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$\frac{n \log n}{\prod_{i=1}^k p_i}$

$O(n)$

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- Algorithm terminates after first

\dots, p_k s.t.

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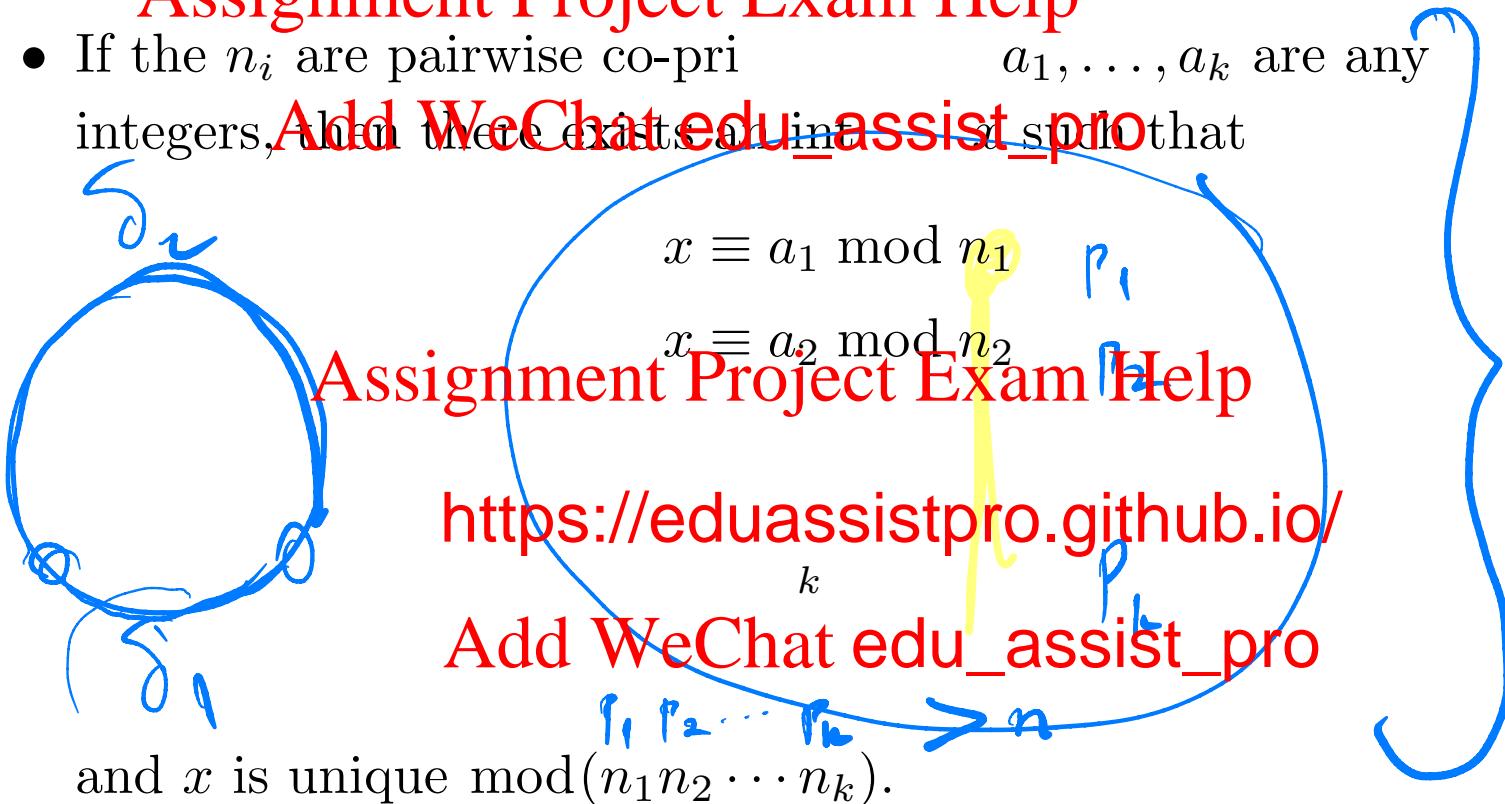
$$\prod_{i=1}^k p_i > n$$

- To prove termination use the Chinese Remainder Theorem.
- To prove time complexity use the Prime Number Theorem.

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Using the Chinese Remainder Theorem^a Assignment Project Exam Help

- If the n_i are pairwise co-prime integers, then there exists an integer x such that



and x is unique $\pmod{(n_1 n_2 \cdots n_k)}$.

- In our case $n_i := p_i$, for $i = 1, 2, \dots, k$, and there are the two solutions δ_1, δ_2 .

^aProblem with specific numbers, appears in the 3rd-century book Sunzi Suanjing by the Chinese mathematician Sunzi

I cannot do the details of this!
in this class

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Using the Prime Number Theorem Assignment Project Exam Help

- The worst case occurs when nce the max number k of prime numbers have to be checked
- Resulting running time is $O(kn)$, but we need to determine the value of k . Consider smallest k such that $\prod_{i=1}^k p_i > n$.
- This implies that $\prod_{i=1}^{k-1} p_i \leq n$ and $p_k \approx k \ln k \leq \frac{n}{k(k-1)/2} \leq n$. Thus
- Therefore $\prod_{i=1}^k p_i \leq n p_k \leq n^2$
- By the prime number theorem we have that

$$n^2 \geq \prod_{i=1}^k p_i \geq \prod_{i=1}^k \frac{i \log p_i}{8} \geq k! 8^{-k} \geq 2^{\Omega(k \log k)}$$

^aKnowledge of number theory is needed here!

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Rendezvous with $O(1)$ memory Assignment Project Exam Help

- The main question:

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Can you solve the rendezvo-

constant memory?

As have

- One way or the other you must change the rules of the game!

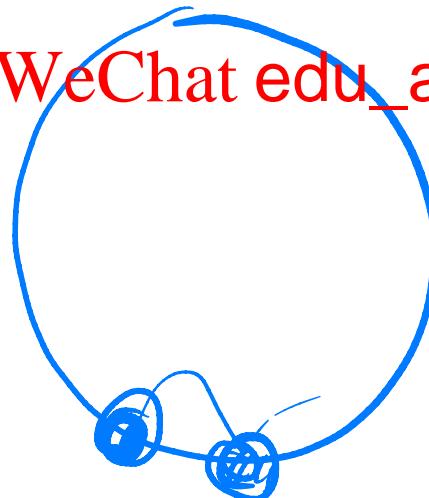
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- How about if yo

token?

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Movable Tokens and $O(1)$ memory
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 $n, d,$ orientation unknown.

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d
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1. Release the token
2. Choose a direction and begin walking
3. Upon finding a token, reverse direction.
4. Move the token one node in the new direction
5. Continue walking in the new direction
6. Repeat from step 3 until rendezvous occurs

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RVP vs RVD Assignment Project Exam Help

- **RVP:** denotes the Rendezvous
 - The requirement is to cause a rendezvous. If rendezvous is not possible then an algorithm may be running forever without termination, e.g., when the agents are initially placed at distance $n/2$.
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- **RVD:** denotes the rendezvous
 - A rendezvous algorithm is required to ensure a rendezvous or not. If rendezvous is possible and if it is to cause a rendezvous, then terminate the algorithm.
- **NB.** Previous algorithm solves RVP but not RVD.

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RVD with Two Movable Tokens Assignment Project Exam Help

- **Theorem 3** *Rendezvous VD) is solvable in a unidirectional ring for two mobile agents with instant memory and two indistinguishable movable tokens each, in time $O(n^2)$.*
- This is based on an algorithm which at the cost of using two tokens per mobile agent detects the possibility of rendezvous and can eventually

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RVD with Two Movable Tokens Assignment Project Exam Help

1. Drop first token at your home base a o node located to the right.
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2. **repeat**
3. Travel right and move every second token you meet one position to the right.
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4. **until** agent dete
5. **if** two token <https://eduassistpro.github.io/> d and check if other two tokens are also on top of ea
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6. **if** yes then rendezvous is not po else agent waits at last position.
7. **endif**
8. **endif**

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RVD with Two Movable Tokens Assignment Project Exam Help

- Each mobile agent drops one token and the other token to the node located to its right.
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- Then it travels right and moves every second token one position to the right (note that this will keep the home node tokens at their original locations).
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- The process is repeated until the two tokens are on top of each other.
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- When this happens, it goes around and changes direction. If the other two tokens are also on top of each other.
- If they are, then the home nodes were $n/2$ away, the whole computation was symmetric and the agents can never rendezvous.

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RVD with Two Movable Tokens Assignment Project Exam Help

- If the other tokens are not on top of each other, one agent waits as the other agent will eventually meet it.
- Let us divide the whole computation into rounds of n time steps each – during one round each agent completes a cycle around the ring and both second tokens are moved two steps.
- As the initial distance between the two tokens of the next agent is at most $d - 1$, the worst case running time of this algorithm is bound by d times the number of rounds plus $n/2$ for the final check, resulting in $n((n/2 - 1)/2) + n/2$, which is in $O(n^2)$.
- This completes the proof of Theorem 3.

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Detecting Rendezvous Assignment Project Exam Help

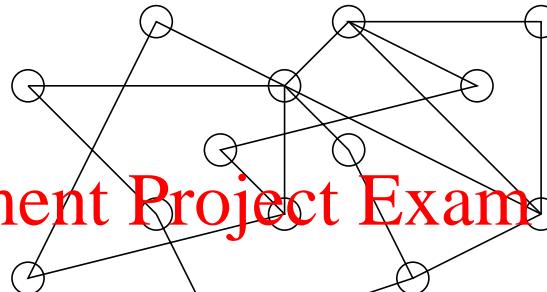
Table 1: Time bounds for two mobile agents to detect if rendezvous with detected memory (RVD) and to rendezvous when input is asymmetric (RVP) on an n node synchronous uni-, bi-directional ring with one or two tokens.

Assignment Project Exam Help		Condition for Rendezvous	
# of Tokens	# of Tokens	RVP	RVD
1	1	$\Theta(n^2)$	$\Theta(n^2)$
1	2	∞	$\Theta(n^2)$
2	1	$\Theta(n^2)$	$\Theta(n^2)$
2	2	$\Theta(n^2)$	$\Theta(n^2)$

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Exercises^a Assignment Project Exam Help

1. Give a rendezvous algorithm for the distinguished node of the graph. What vertex will it meet?



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2. Consider a geometric graph (nodes have coordinates). Can you show how to solve the rendezvous problem in a geometric graph (geometric means the nodes know their (x, y) coordinates)?
3. Consider a planar graph. Can you show how to solve the rendezvous problem in a planar graph if nodes have no

^aDo not submit.

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knowledge of their (x, y) coordinates?

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4. Prove Theorem 1 by showing that n agents such that the MAs always converge to $d = \frac{n}{2}$ and act appropriately, i.e., stop if $d = \frac{n}{2}$ and rendezvous otherwise
5. Prove the following for two agents with tokens

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n	Knowledge		Lower	Upper	Memory Requirement
YES					$O(\log d)$
YES					$O(\log d)$
YES	NO	YES			$O(\log n)$
YES	NO	NO			$O(\log n)$
NO	YES	YES	$3n/4$	$3n/4$	$O(\log d)$
NO	YES	NO	$3n/4$	$5n/6$	$O(\log d)$
NO	NO	YES	$5n/4$	$5n/4$	$O(\log n)$
NO	NO	NO	$5n/4$	$5n/4$	$O(\log n)$

6. Consider 4 Mobile Agents (MAs) located on 4 different nodes of an n node ring. They are equipped with indistinguishable tokens which they release at their starting positions.

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its correctness. Let the intertoken distance be d_1, d_2, d_3, d_4 .

Give a rendezvous algorithm and determine the initial distances which ensure rendezvous.

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References
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2. E. Kranakis, D. Krizanc, and E. Markou, The Mobile Agent Rendezvous Problem in the Ring, Morgan-Claypool, 2010.

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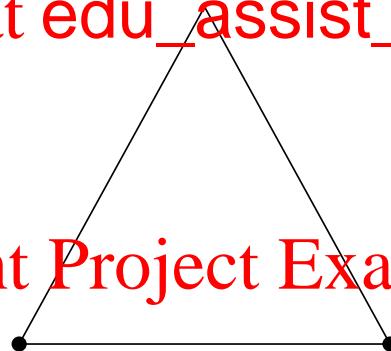
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Example: Triangle (3-Ring)
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- Can two MAs rendezvous in a 3-

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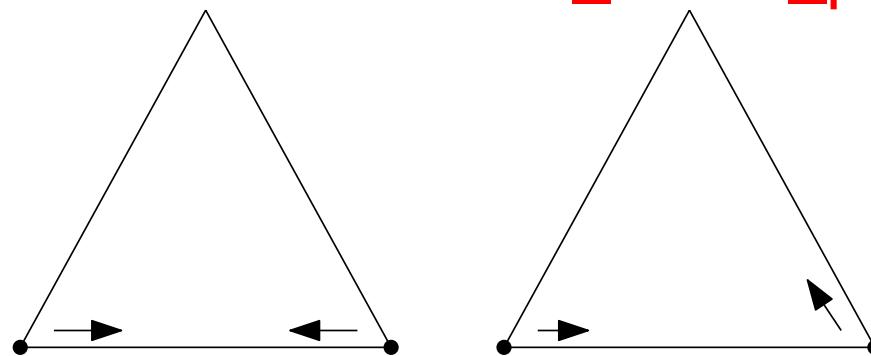


- In lefthand side ren
side!

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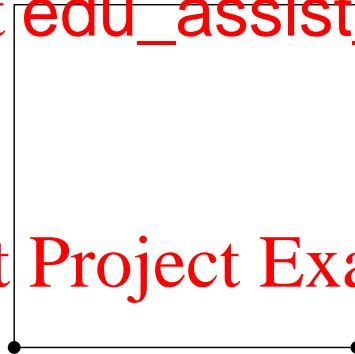


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Example: Square (4-Ring)
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- Consider two MAs rendezvous

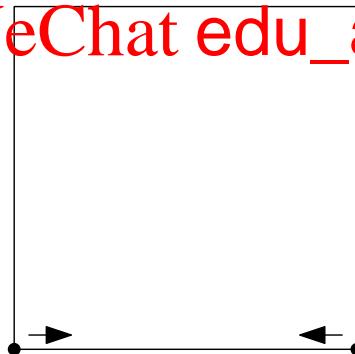
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- Rendezvous is never ..

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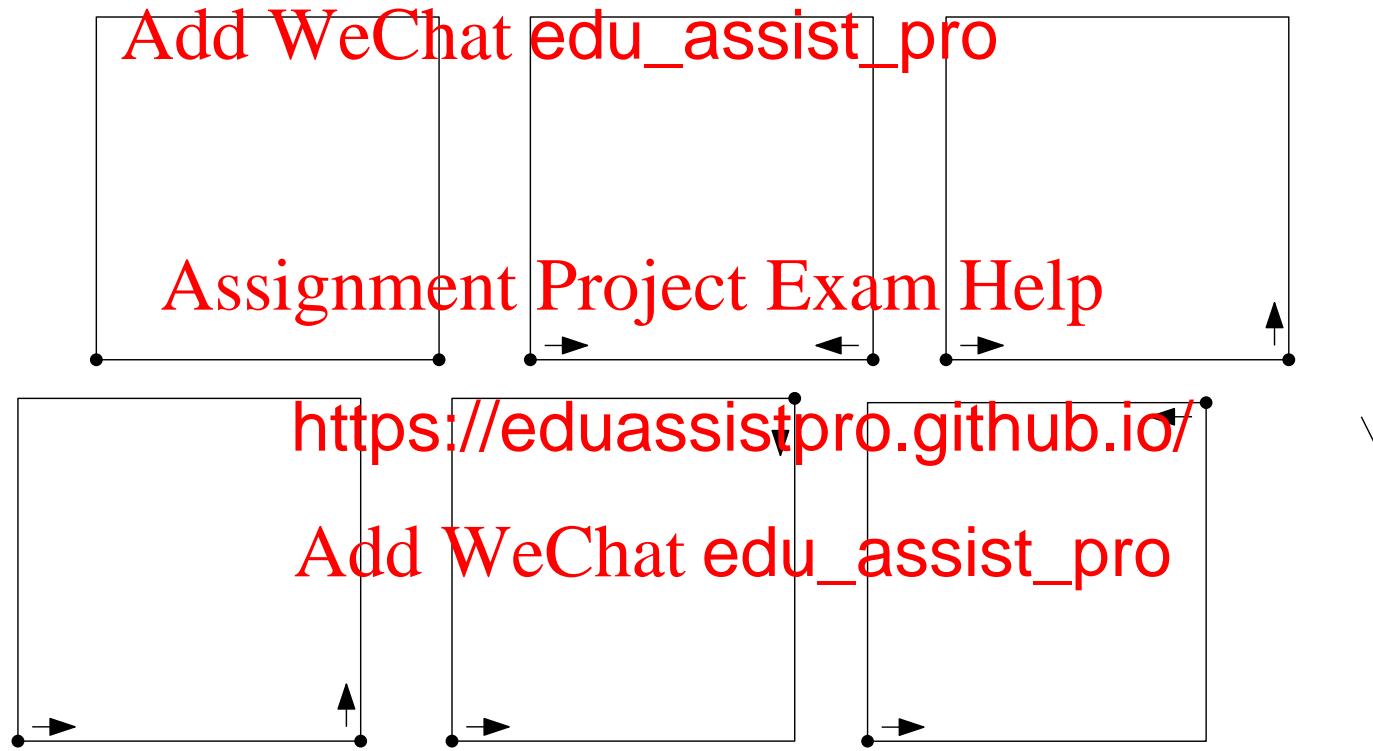


... but is possible on an edge!

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- Consider two MAs

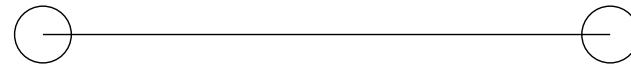


- Algorithm must work in all situations as specified by the given conditions.

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A Solution: Rendezvous in an Edge Assignment Project Exam Help

- If the system is synchronous and endpoints of the line they may meet at different nodes.



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- Assumption:** rendezvous should either at a node or a link of the network!
 - This simplifies algorithms, otherwise we have to mention the parity of n ,
- In general, two different MAs could rendezvous on some node/edge of a network.

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The Model: Knowledge Assignment Project Exam Help

- Knowledge refers to what the agents know about themselves, other agents, and the ring itself.
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- Consider k MAs in a ring of n nodes.
 - Do MAs know k (the total number of MAs in the network)?
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 - Do MAs know their initial (inter)-distance in the network?
 - Do MAs know the size of the ring?
 - Do MAs know their initial (inter)-distance in the network?
 - How much memory do the agents need to solve rendezvous?
 - Do the agents have tokens?
- All these characteristics may affect the rendezvous algorithm.

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Lonely Runner Conjecture: Wills (1967) and Cusick (1973) [Assignment Project Exam Help](https://eduassistpro.github.io/)

Suppose k runners having different speeds start at

a common point and run laps on a circular track. [Add WeChat edu_assist_pro](https://eduassistpro.github.io/)

Then for any given runner i , there is a time at which runner i is distance at least $1/k$ away from every other runner. [Assignment Project Exam Help](https://eduassistpro.github.io/)

This conjecture was verified by Pomerance (1974) with the assistance of a computer program. <https://eduassistpro.github.io/>

Goddyn, Gvozdjak, Sebo, and Tarsi (1998) provided a counterexample proof of the case $k = 5$, and established a connection between this problem and a question concerning flows on graphs.

Recently Bohman, Holzman, and Kleitman (2001) have solved this problem for $k = 6$ runners.