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To Assignment Project Exam Help e https://eduassistpro.github.io/

n/Communication".

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Assignment Project Exam Help Goal: Understand interaction o

- Shortest Paths We Chat edu_assist_pro
 - Dijkstra^a (or BFS with weights)
- Centralized MST^b (Minimum Spanning Tree) Assignment Project Exam Help
 - Prim (Outlin
 - Kruskal (Oulettps://eduassistpro.github.io/
- Distributed MSAdd WeChat edu_assist_pro
 - Gallager-Humblet-Spira (SynGHS)
- Appendix

^aThis can be used as a review since the non-distributed Dijkstra algorithm may have already been covered in other courses,

^bThis can be used as a review since the non-distributed MST material may have also been covered in other courses.

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Motivation: Shortest Paths Assignment Project Exam Help

- Consider a strongly connecte raph, with unidirected Win Chateedu_assist_probors.
- BFS finds shortest path with the hop distance. How do we generalize BFS?
 - Assignment Project Exam Help

 Assume that each (un)directed edge has an associated

nonnegative https://eduassistpro.github.io/

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• The weight of a path is the sum of the weights on its edges.

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- Problem: find a shortest path fro ed source node to every Addr Wachate edu_assist_pro
 - a shortest path is a path with minimum weight.
- A collection of shortest paths from the source to all the other Assignment Project Exam Help nodes in the digraph constitutes a subtree of the digraph, all of whose edges are originally educated whose edges are originally educated the digraph.
 - Does the collection of shortest paths f
 node in an undirected graph form_assist_pro
 bidirectional ring of n nodes.) How about if the edge weights are pairwise different?^a

aWhy?

Applications: Shortest Paths Assignment Project Exam Help

- Motivation for constructing s om the desire to have Addy Michtletuckle assist pro mmunication.
- Weights represent costs associated with the traversal of edges, for instance,
 - Assignment Project Exam Help
 communication delay,
 - bandwidth, https://eduassistpro.github.io/
 - $\ \, {\stackrel{- \ \, \mathrm{monetary \ charge}}{Add}} \ \, {\stackrel{- \ \, \mathrm{monetary \ charge}}{Addd}} \ \, {\stackrel{- \ \, \mathrm{monetary$

Shortest.Paths' Trees (SPTs) Assignment Project Exam Help

- A shortest paths' tree minimiz worst-case cost of communicative with a saist pro rk.
- We assume that every process initially knows
 - 1. the weight of all its incident edges.
 Assignment Project Exam Help
 - 2. the number
- We require that teaps://eduassistpro.github.io/
 - 1. its parent in A dar Welar hap ectu patssist_pro
 - 2. its distance (i.e., the total weight of its shortest path) from the source.

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- If all edges are of equal weight, the shortest Adds We Chat edu_assist_pro
 - a trivial modification of the simple SynchBFS tree construction can be made to produce the distance inform Assignments ProjectnExameHelp
- In synchronous https://eduassistpro.github.io/ ple yet efficient method t
 - in asynchronous systems the edunassist pro the flooding algorithm may be far from BFS.
- In standard BFS constructions (that we have already studied) all edges have weight 1.

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- A classic BFS construction is
 - Dijkstra's Algorithm

 Dijkstra's Algorithm

and can be a sychronous/asynchronous algorithm

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Dijkstra's Algorithm and Relaxation Assignment Project Exam Help

- Based on the **principle of**
 - An approximation to corr assist_produally replaced by more accurate values until reaching the optimum solution.
 - Approximate distance to each vertex is an overestimate of true distance ment Project Exam Help
 - Replaced by https://eduassistpro.github.io/ newly found p
- Greedily selects a node "correspondin" dge" that has not yet been processed, and performs this relaxation process on all of its outgoing edges.
- Processing (usually done with a heap) which also counted as part of the cost

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Basic Idea of Constructing Shortest Paths Assignment Project Exam Help

• Let S_k be the set of k-

he destination s.

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 During the kth step the othe destination s is found by considering

- the distance of nodes in $N \setminus S_k$ to any node in S_k .

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• We will elaborate on this a bit later.^a

^aSee discussion on *blue* edges later.

Dijkstra's Algorithm: Adding Edges (1/3) Assignment Project Exam Help

- Finds the shortest path from th s to all other nodes in Addi Mterbat edu_assist_pro
 - Similar to BFS, except that it keeps track of a distance d(j) (length of the shortest path known so far to node from a "root resignment Project Exam Help
- Instead of examiltps://eduassistpro.github.io/ izes them by the distance d and picks j d node i with the smallest d(i) delowed shateedu_assist_prond updates tentative distance d for all its neighbors.
- The algorithm uses a heap to keep track of its unvisited nodes j, each with a metric d(j).

Dijkstra's Algorithm: Forming a Heap (2/3) Assignment Project Exam Help

- Removing the item with small $O(\log n)$ time if the heap Addit Wis Chat edu_assist_pro
 - If an item's metric changes but it remains in the heap, it takes $O(\log n)$ time to adjust its position in the heap.
 - Initializing ignement Projecta Exam Help.
- Nodes no longehitpts://eduassistpro.github.io/ d(j) is the shortest path from s to j.
 - The shortest path can be traced back projeto j to s by walking the tree from j to its parent p(j), then to p(p(j)), and so on until reaching s.

^aA tree-based data structure satisfying the heap property. In a max heap, for any given node C, if P is a parent node of C, then the key (the value) of P is greater than or equal to the key of C. In a min heap, the key of P is less than or equal to the key of C.

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- Nodes in heap have not been visit d(j) is tentative.
 - They Apld in the Chatied Upfassist_pro nite d (discovered in the frontier), and those with infinite d (undiscovered).
 - Each nacksignment for iteration likely st one edge from the visite
 - The node in https://eduassistpro.githubjjo/las a very useful property on which the algoritassist_pro d(j) is the true shortest distance of the path fro to j.
- The algorithm selects this node and then updates its neighbors as j moves from the frontier into the set of visited nodes.
- Algorithm finds the shortest path from s to all other nodes in $O((|V| + |E|) \log |V|)$ time; asymptotic time can be reduced with a Fibonacci heap; in practice a conventional heap is faster.

Dijkstra's Algorithm: Formally Assignment Project Exam Help

- N set of all the nodes in (undirect
- l(i,j) (non-negative) cost ass assist_pro e $\{i,j\}$.
 - $-l(i,j) = +\infty$ if there is no edge between i,j.
- Let s be the spignment in the least the Helper to find shortest paths fro ork.
 - s is the start types://eduassistpro.github.io/
- Algorithm constants Weenhatedu_assist_prom of nodes:
 - -M is the set of nodes incorporated so far, and
 - algorithm stops when M = N.
- C(n) is the cost of the path from s to node n.

Dijkstra's Algorithm: Formally Assignment Project Exam Help

- Dijkstra's Algorithm
 - $1. M = \frac{\text{Add WeChat edu_assist_pro}}{1}$
 - 2. for each $n \in N \setminus \{s\}$
 - 3. C(n) = l(s, n)
 - 4. while Assignment Project Exam Help
 - 5. $M = \frac{\text{h that}}{C(w) \text{ is}}$ https://eduassistpro.github.io/
 - 6. for each at Wethat edu_assist_pro
 - 7. $C(n) = \min\{C(n), C(w) + l(v)\}$

See example in appendix.

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• Algorithm can be implement where VAdde Woodbate education assist_pro

 $O(|V|^2)$,

• As presented, the algorithm computes weights of paths, not the paths themselves.

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- Can be easily modi
 - The last edgettps://eduassistpro.github.io/shortest path to destination, Add WeChat edu_assist_pro
 - can be used to compute a shortest path t
 - compute routing tables.

^aWe discuss this later.

Application: Route Calculation in LSP Assignment Project Exam Help

- Dijkstra's Algorithm used for r n in Link State Protocol Ards PWeChat edu_assist_pro
- Finds shortest paths from all nodes to some fixed destination (or source)

• Requires that all ed

restriction for mattps://eduassistpro.github.io/

• Shortest paths found in order of increasissist_pro

Dijkstra BFS Tree: Constructing the Routes (1/2) Assignment Project Exam Help

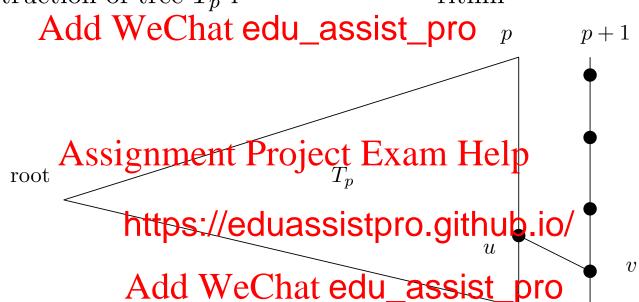
- The algorithm proceeds in pha g trees.
 - In phase p the nodes at di_assist_pro the root are detected.
 - Let T_p denote the tree constructed in phase p.

 Assignment Project Exam Help
- The starting phas
 - Tree T_1 is that the cot which had we chat edu_assist_pro
- We now determine how to update from phase p to phase p + 1;

Dijkstra's Algorithm Tree Construction Assignment Project Exam Help

• Construction of tree T_p i

rithm



- \bullet Broadcast from the root in phase p and echo.
- The root decides which vertex v is selected with a echo/broadcast subroutine.

Dijkstra BFS: Constructing the Routes (2/2) Assignment Project Exam Help

repeat

- 1. The root starts phase p edu_assist_pro_grater p" within T_p .
- When receiving "start p" a leaf node u of T_p (that is, a node that was newly discovered in the last phase) sends a "join p+1" message sometime traignostics. (Annels phase) with a quiet if u has not yet "talk https://eduassistpro.github.io/lies with ACK
 Node v receiving "start p" a leaf node u of T_p (that is, a node u for the last phase) sends a "join phase up the last phase) sends a "join phase up the last phas
- 3. Node v receivi has addenoted assist prosidecline */
- 4. The leaves of T_p collect all the answers of their neighbors; then the leaves start an echo algorithm back to the root.
- 5. When the echo process terminates at the root, the root increments the phase

until there was no new node detected

Analysis of Dijkstra BFS Assignment Project Exam Help

- Theorem 1 In Dijkstra's a
 - the time complexity is edu_assist_pro
 - the message complexity is O(m+nD),

where D is the diameter of the graph, n the number of nodes, a Assignment Project Exam Help and m the number of edges. Adjusting the position of an

element (vertex) itps://eduassistpro.githus.io/

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^aNote that earlier we used V for the number of nodes; here we use n.

Analysis of Dijkstra BFS Assignment Project Exam Help

- Time Complexity
 - A broaddatyechoargordu_assist_eproat most time 2D.
 - Finding new neighbors at the leaves costs 2 time units.
 - Since the BFS tree height is bounded by the diameter, we have D-projections Brojections amplifulty of $O(D^2)$.
- Message Comple
 - Each node par https://eduassistpro.github.io/
 1 message and dentify (clipat) eduncassist pro
 - There are D phases, so message cost is bounded by O(nD).
 - On each edge there are at most 2 "join" messages.
 - Replies to "join" request are answered by 1 "ACK/NACK" (so we have at most 4 additional messages per edge).
 - Message complexity is O(m+nD). Processing using the heap costs a factor $O(\log n)$.

Applications: RIP and BGP Assignment Project Exam Help

- A distributed variant of the Bell orithm is used in distance Addor Watchgtpedu_assist_prole the Routing Information Protocol (RIP).
- The algorithm is distributed and involves a number of nodes (routers) within an Autonomous System (AS), a collection of IP networks typic https://eduassistpro.github.io/
 - 1. Each node calculates elistrate edit tvassist_pro er nodes within the AS and stores this information as a table.
 - 2. Each node sends its table to all neighboring nodes.
 - 3. When a node receives distance tables from its neighbors, it calculates the shortest routes to all other nodes and updates its own table to reflect any changes.

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Questions in Graph Search Assignment Project Exam Help

- When you ask your smartphon best route from Otradat Weshatvedh_assist_pro d route?
- If you ask it to help you drive from Ottawa to Paris, how does it know you cannot do that?

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 If you post somethi

ends

- and friends of frittps://eduassistpro.github.io/
- These questions can all be posed in terms of s (also called graph traversal).

Graph Representation Assignment Project Exam Help

- For an unweighted graph n nodes, storing a binary adjacently example edu_assist_prod array using $O(n^2)$ memory works well in a graph traversal algorithm if the graph is small or if there are edges between many of the nodes.
 - In this Assignment, Project Exam Help $a_{ij} = 1$ if $\{i\}$
 - With edge wei al matrix can represent the weight effected assist opso this assumes that in the problem at hand an edge with zero weight is the same as no edge at all.

Example Graph Representation Assignment Project Exam Help

• A graph and its adjacency matri

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Graph Representation Assignment Project Exam Help

- A road network can be represen irected graph, while all colors assist pro ge a road between them.
- The graph is directed because some roads are one-way, and it is unconnected because you cannot be trained by the paris.
 - The edge weigtps://eduassistpro.gith@blog the road from i to j;
 - all edge weights dnill edge weight dnill edge
- An adjacency matrix works well for a single small town, but it takes too much memory for the millions of intersections in the North American road network.

^aThere are situations where negative weights are natural to use.

Graph Representation Assignment Project Exam Help

- Fortunately, only a handful of r t any one node, and thus Adda Was Charles tilk assist pro arse.
- This kind of matrix or graph is best represented with adjacency lists, where each node *i* has a list of nodes *j* that it is adjacent to, along with the weights reject Example Project Exa

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Assignment Project Exam Help

- Searching a graph from a single s s, discovers all nodes reachable from a single s s, discovers all nodes reachable from a single s s.
- Nodes are marked when visited, so to search the entire graph, a single-source algorithm can be repeated by starting a new search from each mode in the graph, ignoring nodes that have already been visit https://eduassistpro.github.io/
- The graph traversal then performs acti isited, and also records tild order chatted unassist pro
- Often, only a small part of the graph needs to be searched.
- This can greatly speed up the solution of problems such as route planning.

Assignment Project Exam Help

- A spanning tree of a graph is a subg
 - that is a dree e.e., et edu_assist_pro
 - includes all of the nodes of the graph
- If the edges of the network are weighted (expressenting average delay exp inimum weight spanning tree ishttps://eduassistpro.github.io/
- Two non-distributed algorithms for coassist_pro:
 - Prim's algorithm
 - Kruskal's algorithm
- A distributed algorithm for computing MST:
 - GHS (Gallagher, Humblet, Spira).

^aLocal Area Network.

Spanning Tree Terminology Assignment Project Exam Help

- G = (V, E) is an undirected gr
 - V is the get We Chat edu assist pro
 - -E is the set of edges
- $w_{i,j}$ is the weight of the edge $\{i,j\}$
- A spanning spiginmenty Project Example all nodes
- Weight of a tree

https://eduassistpro.github.io/ $w(T) = Add WeChat edu_assist_pro$

where E(T) is the set of edges in T.

• MST (Minimum weight Spanning Tree) is a ST (Spanning Tree) of minimum weight

Two Basic Sequential Spanning Tree Algorithms Assignment Project Exam Help

- 1. Prim's Algorithm (Jarnik, 1930
 - Start Add We Chat edu_assist_pro
 - Always maintain a connected subtree (check for cycles).
 - Among possible choices add a "min weight" edge at a time Assignment Project Exam Help
- 2. Kruskal's Algorith
 - Sort the edgestps://eduassistpro.github.io/
 - Always main and all a the structure of the structure of
 - Add edges in order as long as no cycles created

Prim's Algorithm (Jarnik, 1930)^a
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- Prim's Algorithm
- P is current set of nodes in tree
- D_i is min weight edge from node i to a node in P
- Initially Passignand Project Examples otherwise
 - 1. Find $i \notin P$
 - 2. $P = P \cup \{i \text{ https://eduassistpro.github.io/}\}$
 - 3. For $j \notin P$, $D_j = \min\{D_j, w_j, u_j\}$ 4. Go back to A dd WeChat edu_assist_pro

Can be implemented in $O(|E| + |V| \log |V|)$ time. See example in appendix.

^a1) Jarnk, V. (1930), "O jistm problmu minimlnm" [About a certain minimal problem], Prce Moravsk Prodovdeck Spolenosti (in Czech), 6 (4): 57-63. 2) Prim, R. C. (November 1957), "Shortest connection networks And some generalizations", Bell System Technical Journal, 36 (6): 1389-1401,

.Kruskal's Algorithm (Boruyka, 1926)^a Assignment Project Exam Help

- Kruskal's Algorithm
 - 1. Sort the edges of Gri edu_assist_pro
 - 2. Consider edges in order and add edge to tree if the result does not form a cycle
 Assignment Project Exam Help

• Time complexit i

e in appendix.

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^a1) Kruskal, J. B. (1956). "On the shortest spanning subtree of a graph and the traveling salesman problem". Proceedings of the American Mathematical Society. 7: 48-50. 2) Borvka, Otakar. O Jistm Problemu Minimlum. Prce Moravsk Prodovdeck Spolenosti III, no. 3 (1926): 37-58.

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- Given a graph G, the goal is to ted algorithm that always derived that a sample of G.
- At the end of an execution, each processor knows which of its incident edges belong to the MST and which do not (i.e. the processor writes in a local output register the corresponding incident edges) https://eduassistpro.github.io/
- In the distributed version of the MST, a conetwork is solving a problem where une assist_proken itself.^a
- This is one of the fundamental starting points of (distributed) network algorithms.

^aA "local" version of the MST is not possible: We won't discuss this here.

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• Recall

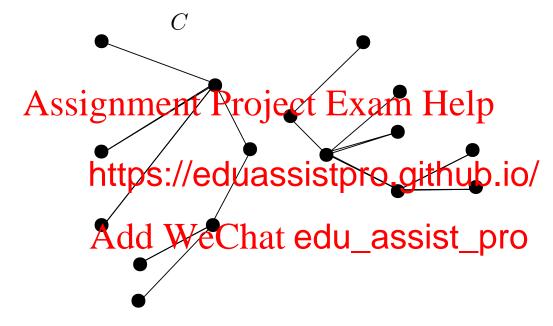
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Assignment Project Exam Help (a) is a tree,

- 1. Start with trivial spa://eduassistpro.github.io/individual nodes and no edges; at the start each vertex pro
- 2. Repeatedly do the following: Select
 - (a) an arbitrary component C (i.e., tree) in the forest, and
 - (b) an arbitrary outgoing edge $e \in C$ having minimum weight among the outgoing edges of C.

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1. For such an edge e, combi component at the other end of e And who Chat edu_assist_proped component.



2. Stop when the forest has a single component.

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• Now we investigate how to desi

lgorithm.

We assume that no two edges of th

ame

weight.

- This simplifies the problem
 Assignment Project Exam Help
- simplificatio
- one can alwhttps://eduassistpro.github.io/ nt
 vertices to the weight.
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Concept of Blue Edges Assignment Project Exam Help

- Let T be a spanning tree of the w
 - A subgraph We Chat edu_assist_proment.
- Edge $e = \{u, v\}$ is an outgoing edge of T' if either
 - $-u \in T'$ And $v \notin T'$ ort Project Exam Help
 - $-u \notin T'$ and
- The minimum we https://eduassistpro.github.io/T', denoted by b(T'), is the so-palled we edu_assist_pro

Examples: Concept of Blue Edges Assignment Project Exam Help

• Example 1:

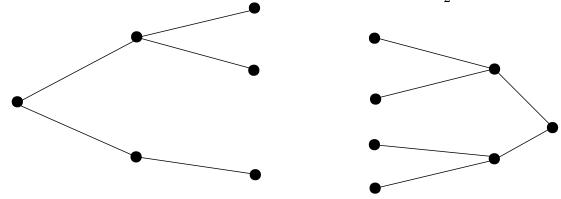
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• Example 2:

 $_{\mathcal{I}_{1}}\!Add\ WeChat\ edu_assist_pro$



A Lemma on Adding Blue Edges Assignment Project Exam Help

- Lemma 1 For a given weigh G (such that no two weights Arelth Weelthat edu_assist_pro
 - let T denote the MST, and
 - -T' be a fragment of T.

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Then the blue edge of T' (denoted by b(T')) is also part of T, $-i.e., T' \cup \{b(T')\} \subseteq T$.

• So, the Lemma says that blue edges can be added to an already constructed MST fragment and maintain the MST property.

Assignment Project Exam Help

- For the sake of contradiction, s MST T there is edge exact We Chattedu_assist_eptoninder of T.
- Adding the blue edge b(T') to the MST T we get a cycle including both e and b(T').

 Assignment Project Exam Help
- If we remove e
 - we still have https://eduassistpro.github.io/
 - since by the definition of the blue edge ist $\geq pro^{T'}$, the weight of that new spanning tree is less
- We have a contradiction.

^aHere we used the fact that the edge weights are different!

 \mathbf{e}

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- Blue edges
 - allow a dragment that edu assist pro
 - seems to be the key to a "distributed algorithm" for the "distributed MST" problem.

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- Since every node it directly has a batters://eduassistpro.github.io/
- All we need to do now is to grow these fragme pro
 - Essentially this is a distributed version of Kruskal's sequential algorithm.

A Distributed Algorithm Assignment Project Exam Help

• At any given time the nodes of the g fragments (do We Chate & du t assist_pro

oned into

ent.

- Each fragment has a designated vertex called root (of the fragment):
 - ID of fragment is defined to be the ID of its root.
- In the course ohttps://eduassistpro.github.io/
 - each node knows its parent and its shill pro
- The algorithm operates in phases.
- At the beginning of a phase, nodes know the IDs of the fragments of their neighbor nodes.

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• The algorithm builds the comp

s" (or phases).

• For each k, the level k c stitute a spanning forest, where each level k component consists of a tree that is a subgraph of the MST.

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- Each level k co
- Each component ttps://eduassistpro.github.io/ der node.
- The processes and da Weethanted uf assist pro O(n), to complete each level.

SynGHS: Base and Inductive Steps Assignment Project Exam Help

• Base Step:

The algorithm Watshattedue_assist_pro nsisting of individual nodes and no edges.

• Inductive Step:

Suppose inductively that the jevel Example have been determined (alphanest)/eduassistpro.github.io/

- the UID (Userdo) Weether the duf assist pro is used as an identifier for the entire component),
- which of its incident edges are in the component's tree.

Assignment Project Exam Help $k \rightarrow k+1$

- To get the level k + 1 component conducts Adda Me Chagtiect parassist pro r the MWOE (Minimum-Weight Outgoing Edge)^a of the component.
- The leader broadcasts search requests along tree edges, using a message broadcasts strategy Exam Help
- Each process filetps://eduassistpro.github.io/ minimum weight that is outgoing from t f there is any such edge,dd WeChat edu_assist_pro
 - it does this by sending test messages along all non-tree
 edges, asking whether or not the other end is in the same
 component.

^aRecall that we called such edges: "blue" edges of the fragment.

Assignment Project Exam Help $k \rightarrow k+1$

- Then the processes convergec -weight edge information down Chatedu_assist_pro a along the way).
- The minimum obtained by the leader is the MWOE^a of the entire component.

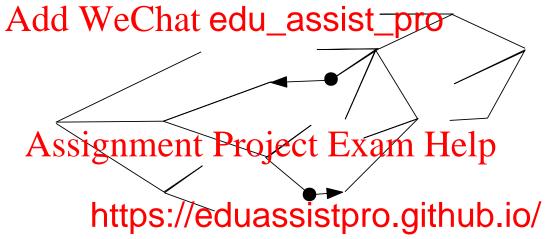
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- When all level WOEs, the components are type://eduassistpro.github.io/ orm the level k+1 components.
 - This involves the leader of each level mponent communicating with the component process adjacent to the MWOE, to tell it to mark the edge as being in the new tree;
 - the process at the other end of the edge is also told to do the same thing.

^aI.e., "blue" edge

SynGHS: New Leader Assignment Project Exam Help

• Two components at level



- Merging two components at level Add WeChat edu_assist_pro
 - minimum weight edge will be select
- Moreover, a component at level k will merge only with another component at level k which corresponds to a minimum weight outgoing edge!

SynGHS: New Leader Assignment Project Exam Help

- Then a new leader is chosen for eac k+1 component, as follows. Add WeChat edu_assist_pro
 - It can be shown that for each group of level k components that get combined into a single level k + 1 component, there is a unique level k com

 2).
 - New leader: is th 2).

 New leader: is th
 - NB: this nexted Weahather uitassist_pro information available locally.
- Finally, the UID of the new leader is propagated throughout the new component, using a broadcast.

^aRecall that edge weights are pairwise distinct.

Assignment Project Exam Help

- Eventually, after some numb nning forest consists of delignated parassist pro li the nodes in the network.
- Then a new attempt to find a MWOE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail, because no process will find a mwoE will fail will fail to the mwoE will fail to the will fail to the mwoE will fai
- When the leadenthes://eduassistpro.github.io/ ing that the algorithm is completed.

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A Key Idea of the Algorithm (1/2)
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• Among each group of level

nts that get

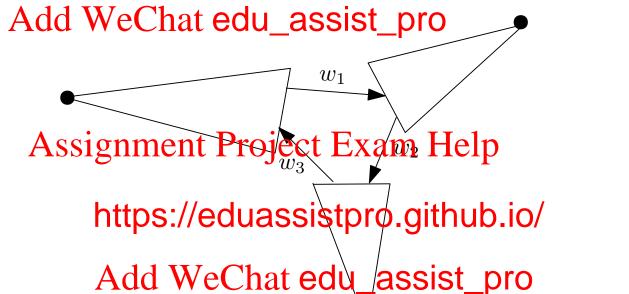
- Among each group of level nts that get combined, there is AddqWethlateetly_eassist_pro mon MWOE of both endpoint components.
 - To see this: consider the **component digraph** G', whose nodes are the horizonte that components that component of the co
 - G' is a weakhttps://eduassistpro.github.io/ de has
 exactly one outgoing edge.^a
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^aA digraph is weakly connected if its undirected version, obtained by ignoring the directions of all the edges, is connected.

A Key Idea of the Algorithm: Example Assignment Project Exam Help

• Can we have a cycle of length

omponent graph



• If yes then, $w_1 > w_3$ and $w_2 > w_1$ and $w_3 > w_2!$

Assignment Project Exam Help (2/2)

- So we have the following proper

 Lemma 2 If for a weakly con assist_pro

 Exactly one outgoing edge then G contains exactly one cycle.
- We apply Lemma 2 to the component digraph G' to obtain the unique cycle of components.
- Because of the https://eduassistpro.github.io/dges in the cycle must have non-increasing weigh this cycle cannot be greater than 2.
- So the length of the unique cycle is exactly 2.
- But this corresponds to an edge that is the common MWOE of both adjacent components.

Importance of Synchrony in SynGHS
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• Synchrony ensures when a pro ries to determine whether

- Synchrony ensures when a pro ries to determine whether or not the other component, both i and j have up-to-date component UIDs.
- If the UID at j is observed to be different from that at i, we would like Assignmeintt Project Exemby Label particle different components, not j eir component UID https://eduassistpro.github.io/
- In order to executed hwere a system as sist_pro llow a predetermined number of rounds for ea
- To be certain that all the computation for the round has completed, this number will be O(n); note that O(diameter) rounds are not always sufficient.
- Need to count this number of rounds is only reason that nodes need to know n.

Complexity Analysis of SynGHS Assignment Project Exam Help

- Note first that the number of nod k component (with the desired exhauted up assist pro $t = 2^k$).
- This can be shown by induction, using the fact that at each level, each component is combined with at least one other component assignment Project Exam Help
- Therefore, the https://eduassistpro.githwb.io/
- Since each level takes time $C_n(n)$ edu_assist_pro time complexity of SynchGHS is O(n)
- The communication complexity is $O((n + |E|) \cdot \log n)$, since at each level, O(n) messages are sent in total along all the tree edges, and O(|E|) additional messages are required for finding the local minimum-weight edges.

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- More details are needed for the as mmunication model. Add WeChat edu_assist_pro
 - It may be that some fragments (subtrees) are much larger than others, and because of that some nodes may need to wait for stigning it frequents that but whether neighbor v e b = (u, v).

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- These details can b
 - We can bound the welchat edu bassist pro hat nodes only start the new phase after the last phase is done, similarly to the phase-technique of Dijkstra's Algorithm.
- This gives rise to the idea of levels which will not be discussed any further.

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• The GHS algorithm is also kno

re as BigMerge.

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 The GHS algorithm can be appl

ys.

- GHS for instance directly solves leader election in general graphs: The leader is simply the last surviving poot!
- GHS is distribute em in that the numbers://eduassistpro.github.io/
 - In general, if Yeld receiptate edubassist_pro ot construct a spanning tree.
 - There exist constant round algorithms on geometric graphs that construct spanners with good spanning properties.

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- Construct "local" planar spa ant stretch factor in Wireledde Wechat edu_assist_pro
- Here is a simple algorithm.
 - 1. Each node u finds its distance 2 neighborhood $N_2(u)$.

 Assignment Project Exam Help
 - 2. Each node h distance wightss) of its distantios://eduassistpro.github.io/
 - 3. $\{u, v\}$ is an edge of the spanner iff T_u and T_v . is an edge of both T_u and T_v .
- The resulting spanner is
 - 1. planar,
 - 2. has small stretch factor,
 - 3. requires information from only two hops away.

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- 1. Consider the following traversa itiator sends out a tolando Waconathedravessist_pro e the parent of a node as one from which the token is received for the first time. All other neighboring nodes will be called neighbors. By definition, the initiator does not have a parent The following two rules define the
 - (a) Send the tolettps://eduassistpro.github.io/
 - (b) If Rule (1a) cannot be used to send the toke token to its parent.

Show that when the token returns to the root, the entire graph has been traversed by proving the following two claims.

- (a) The token has a valid move until it returns to the root.
- (b) Eventually every node is visited by the token.

^aNo to hand in!

- 2. Let G = (V, E) be a directed graph. A maximal strongly Assignment Project Exam Help G' such that 1) for every pair of weekly extices u and u to u and a directed path from u and u and a directed path from u and u of u as its subgraph. Propose a distributed algorithm to compute the maximal strongly connected component of a Assignment Project Exam Help
- 3. Propose an algorithms://eduassistpro.github.io/ e by restoring connectivity when a single no algorithm should complete that redu lassist_pro st number of edges. Compute the time complexity of your algorithm.
- 4. In a spanning tree of a graph, there is exactly one path between any pair of nodes. If a spanning tree is used for broadcasting a message, and a process crashes, some nodes will not be able to receive the broadcast. Our goal is to improve the

connectivity of the subgraph used for broadcast, so that it can Assignment Project Exam Help tolerate the crash of one process.

Given a Anti-Welgharhedu_assist_proinimal subgraph would you use for broadcasting, so that messages will reach every process even if one process fails? Suggest a distributed algorithm for constructing such a subgraph. Argue why your Assignment Project Exam Help algorithm will work, and analyze its complexity.

- 5. The eccentricity https://eduassistpro.githubeio/aximum distance from v to any other vertex. um eccentricity form the center.
 - (a) Show that a tree can have at most two centers.
 - (b) Design a distributed algorithm to find the center of a tree.
- 6. Given an undirected graph G = (V, E), a matching M is a subset of E, such that no two edges are incident on the same vertex. A matching M is called maximal if there is no other

matching M' such that $M \subset M'$. Suggest a distributed Assignment Project Exam Help algorithm for computing a maximal matching. When the algorithm terminates a maximal matching is matching neighbor, if such a match exists.

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 M Trans.

Prog. Lang. Syntteps://eduassistpro.github.io/

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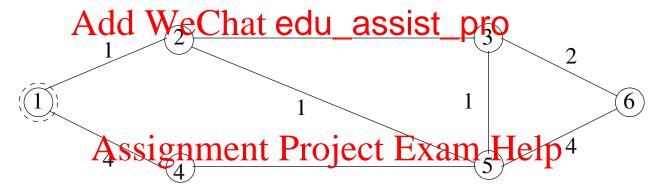
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Example: Dijkstra's Algorithm Assignment Project Exam Help

Start node s := 1

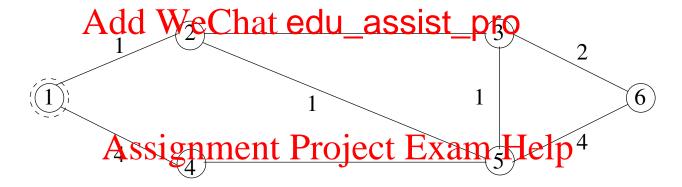


Iteration 1: https://eduassistpro.github.io/

Compute all costs tAdd WeChat edu_assist_pro

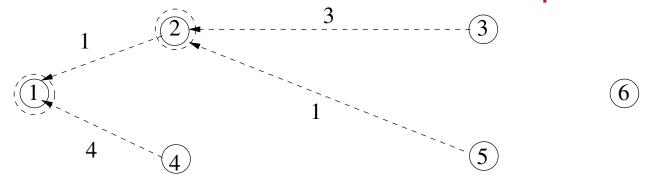


Example: Dijkstra's Algorithm Assignment Project Exam Help Start node is s=1



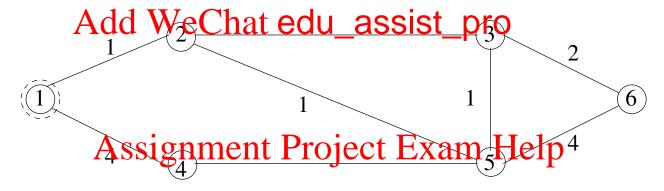
Iteration 2: https://eduassistpro.github.io/

Add min cost node Add weethat edu_assist_pro



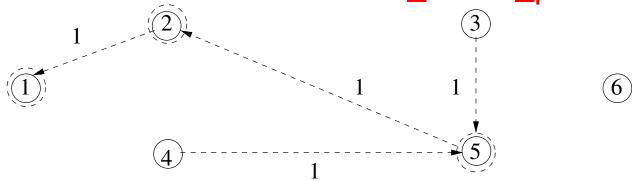
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Example: Dijkstra's Algorithm
Assignment Project Exam Help
Every node executes Dijkstra's algorithm

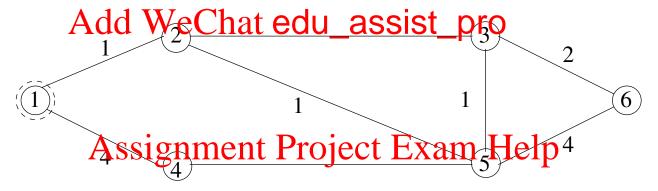


https://eduassistpro.github.io/ Iteration 3:

Add min cost node Add (week 5) at edu_assist_pro

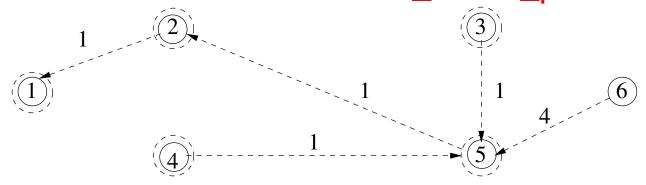


Example: Dijkstra's Algorithm Assignment Project Exam Help Every node executes Dijkstra's alg

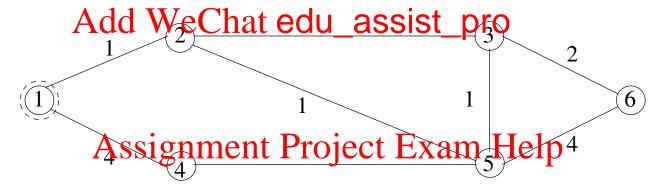


https://eduassistpro.github.io/ Iterations 4:

Add min cost node Add weet at edu_assist_pro



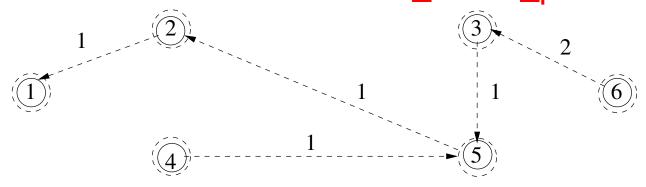
Example: Dijkstra's Algorithm Assignment Project Exam Help Every node executes Dijkstra's alg

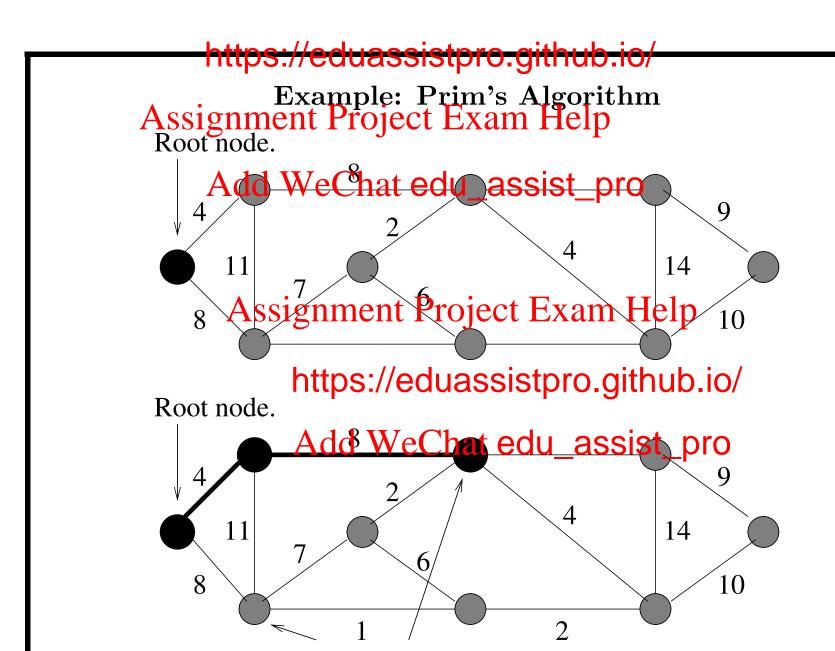


Iteration 5:

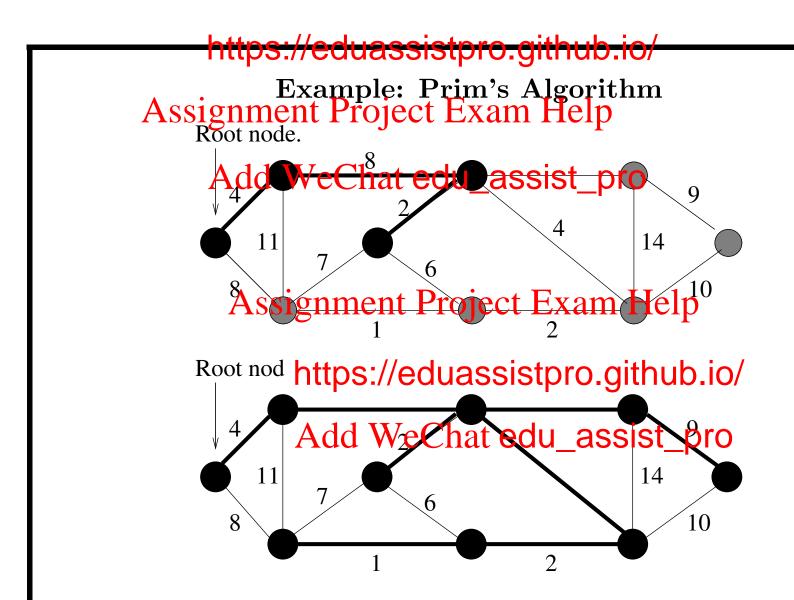
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Add min cost node And weelfat edu_assist_pro





We have a choice: can add either of these two nodes.



Then we add nodes adjacent to links 4. 2. 1. 7. 9 in this order

