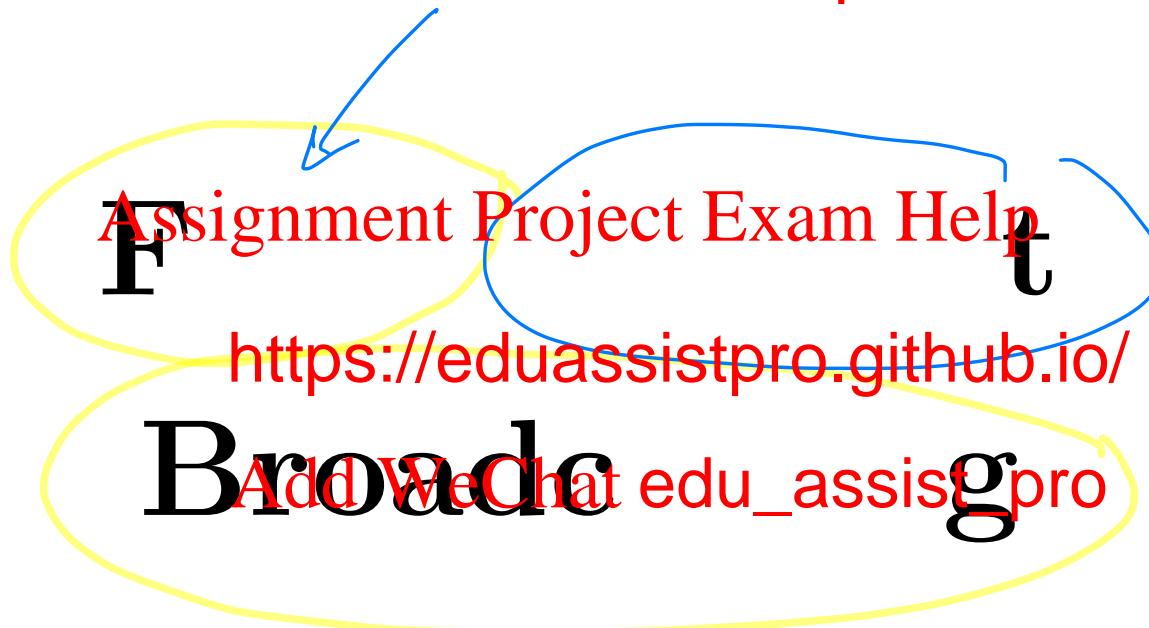


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Definition of faulty
is important.

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Assignment Project Exam Help

- Broadcasting
- Fault-free Broadcasting
- Fault-Tolerant Broadcasting
- Multiple Initiators

Outline

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Broadcasting (1/2)

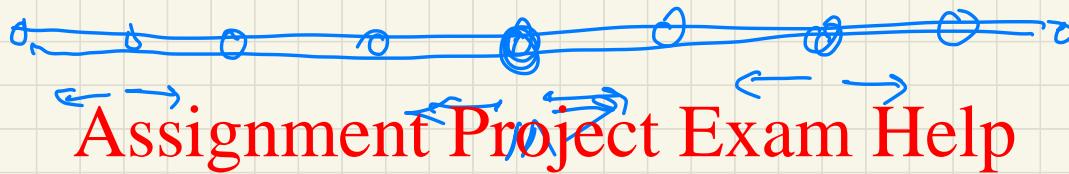
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- Broadcasting refers to sending simultaneously to many users.
- It is usually initiated by a user in a network.
- We are interested in efficient broadcasting, as measured by
 - number of messages
 - time required
- Broadcasting uses available communication channels.
 - We must specify the communication channels to be used and in what order.

Wireless Network



Ethernet



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Flat
routing Add WeChat edu_assist_pro

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Broadcasting (2/2) Assignment Project Exam Help

- Broadcasting is a preferred route because it is flat.

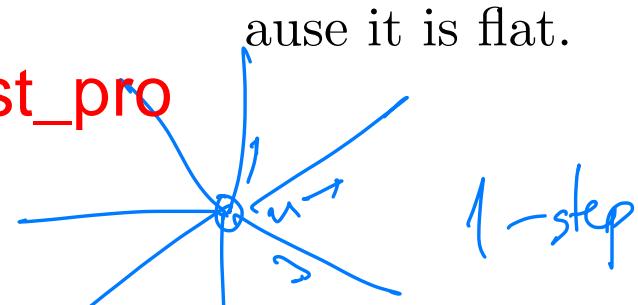
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- Broadcasting is used in

- Ethernet,

- Wireless,

and other networks



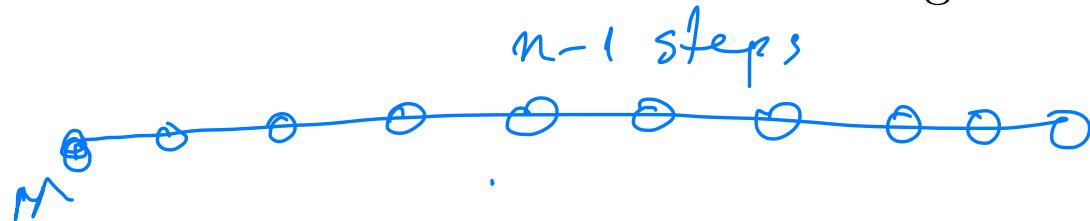
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- Efficiency of broadcasting is determined by the underlying graph $G = (V, E)$.

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- Broadcasting in general graphs is multihop.

- Typically, message transmission for broadcasting is based on building a BFS tree from the “broadcast initiating” node.



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General Setting Assignment Project Exam Help

- Consider a (strongly) connected graph with N processes $0 \dots N - 1$. **Add WeChat edu_assist_pro**
 - This may be a multi-hop graph.
- Each process i has a “stable (unchanging) value” $s(i)$ associated with it. **Add WeChat edu_assist_pro**
 - The goal is to devise a broadcast scheme so that each process i can receive all values $s(j)$ from other processes in the system. **Add WeChat edu_assist_pro**
 - This may require multiple hops.
 - At the end, each process i will have the set of all possible values $V_i = \{s(k) : 0 \leq k \leq N - 1\}$.
 - Generally, the problem is solved with a so-called “heart beat” algorithm.

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Heartbeat Algorithms

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- Initially $V_i = \{s(i)\}$. *↳ has value s(i)*
- To complete the broadcast. In round ^a every process i will periodically

- send its current V_i along each of its outgoing channels,
- receive whatever values have been received by it along the incoming channels.
- update V_i .

- The operation resembles the pumping of a balloon. These types of algorithms are called heartbeat algorithms.
- Two important issues need attention:
 - The termination of the algorithm
 - The message complexity

^aEach round involves **Send; Receive; Process;**

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Heartbeat Algorithm (1/2) Assignment Project Exam Help

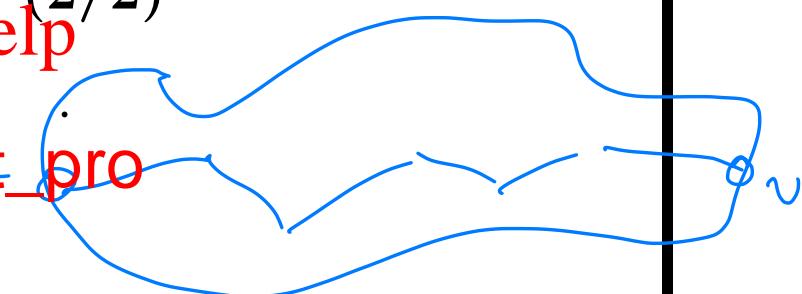
- No need to send V_i , if it has n
he last send
operation. Suffices to send the in
ge only
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- Each process i is associated with two sets of values:
 - V_i denotes the current set of values collected so far,
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 - W_i will repre
nt along the
outgoing cha
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- Let (i, j) represent the channel to j
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- The algorithm terminates when no process receives any new value, and every channel is empty.

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Heartbeat Algorithm (2/2) Assignment Project Exam Help

- The program for process

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*decreases #
of steps*

- Correctness is proved in two steps.
 - 1st step: show that when $\text{empty}(i, k)$ holds, $W_i \subseteq V_k$.
 - 2nd step: show that at the end every process must have received the value $s(i)$ from every other process i .

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Main Question Assignment Project Exam Help

- Is broadcasting possible in a net
nodes (may) fail to transmit messages?

- Two main issues:

- In which networks?
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- What does it mean

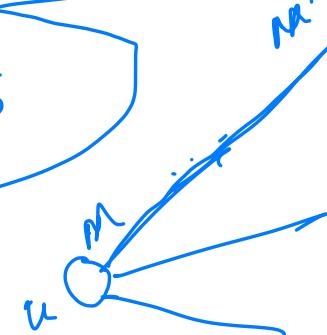
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These faults are known

as crash faults

byzantine:



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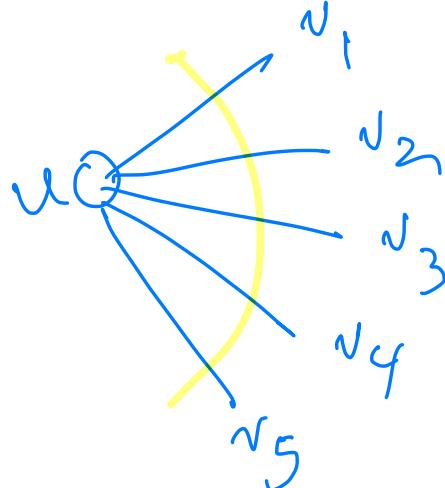
Broadcasting Assignment Project Exam Help

- In the sequel we look at broadcasting when the underlying network is a complete graph on n nodes.
 - In this setting, broadcasting is an instance of flat routing.
- Further, the communication model does not allow for “multicasting”, whereby a given node can communicate with specific nodes at a time.

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Add WeChat Can only send

one message at a time.



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Calling

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- Alice wants to organize a party for everyone (including herself). Add WeChat `edu_assist_pro`

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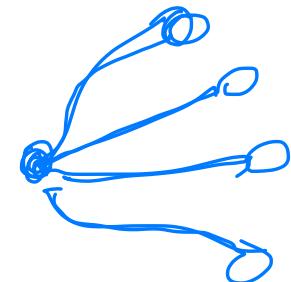
- She does not know their email addresses, but
 - she has a list of all 120 students with their phone numbers which was recently given to by every student.

non-multiplexing
model

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Calling and Broadcasting Assignment Project Exam Help

- Broadcasting depends on the number of channels used.
 - If Alice can shout simultaneously to all channels then it takes only one step (Ethernet uses this idea!).
- However this may cause collisions and in any case it is not an option in our current study.
- Here the communication is point-to-point
 - This is the so-called point-to-point model. A processor can talk to another processor.
 - We will approach the problem imposing “message scheduling and processor coordination”.
 - We also call this the *phone call* model.



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Broadcasting Assignment Project Exam Help

- In the *phone call* model, belf would require the availability of 120 separate channels for 120 phone calls:
 - which may not be available.
- Alice could try to do 120 phone calls herself.
 - which would c

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New Idea: Assisted Broadcasting Assignment Project Exam Help

- Any other nodes^t can assist in the b
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 - Not only Alice can call but certai
er users.
 - Therefore the design would require some form of coordination of who can send to whom and by when.
- [Assignment Project Exam Help](#)

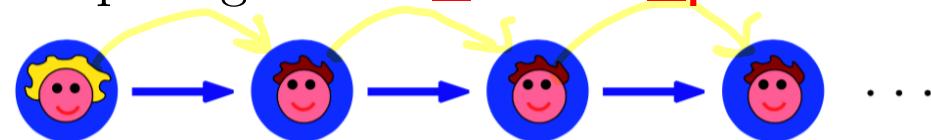
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- The first strategy that comes to me resembling whispering



- Alice just calls the first person on the list and asks him/her to call the next one.
- who will then call the next one on the list,
- and so on,
- until everybody on the list has been reached.

- The advantage of this strategy is that every student only has to make one call.
- To make this work, an order of users must have been agreed on.

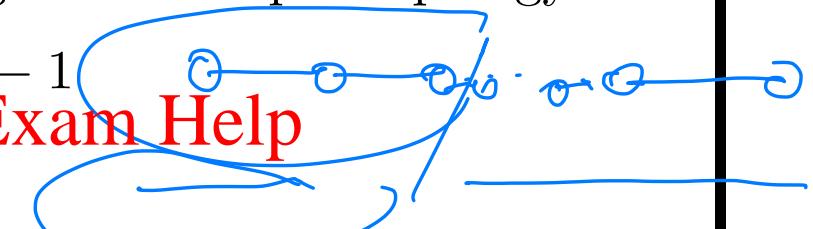
Cost is 1 message per student

A: 1 msg
St: 1 msg

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Alternative Approach (2/2) Assignment Project Exam Help

- Since the calls have to be performed one by one, a very long time can go by until all students are informed.
 - Algorithm imposes an underlying ‘Line Graph’ topology’.
 - For n students this takes time $n - 1$.
- Some issues:
 - If just 10% of the students are informed, the next one on the list within the same day will be informed. If called, it takes at least 12 days until everyone is informed.
 - Even worse: if someone does not bother to call the next one on the list, the whole system will break down!



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New Idea: Binary Search Assignment Project Exam Help

- A master uses two helpers to cut a sorting problem into two smaller sorting problems,
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 - who themselves use two helpers each to cut their sorting problems into even smaller problems,
 - and so on, ...
 - ... until just one element.
- The idea resembles binary search.
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- Couldn't something similar to this also work for the distribution of calls?

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- Alice could divide the phone list into two halves and call the first person on each of the two halves.

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- Each of them will then be asked to cut their list into two further halves and call the first person on these halves.
- This is continued until everybody has been called, i.e., we reach a level in which people are called who just have to take care of an empty list.

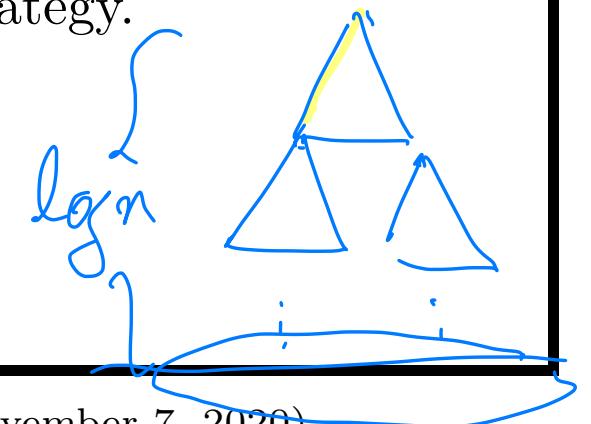
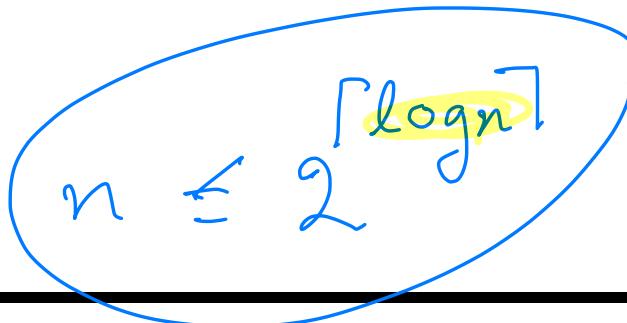
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Partitioning Assignment Project Exam Help

- In this way, the students can be re
cker.
– For n students this take $\log n$)
- Alice determines that just seven rounds of calls are sufficient to reach all 120 fellow students.

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- This is much better t
- However, the stra
nical,
– it's questionable whether the other s
ade to
adhere to the rules without errors.
- Thus, Alice thinks about an alternative strategy.



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Natural Calling Rounds Assignment Project Exam Help

- Alice calls the first two people on the list. Then she asks them to call the students at positions 3 and 4. They do the same, and so on.
 - User i calls users $2i + 1$ and $2i + 2$.
- General rule: everybody at position i in the list will call the students at positions $2i + 1$ and $2i + 2$ (if they exist).

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- Assume $n = 31$ (Alice includ

- Rule: $i \rightarrow 2i + 1, 2i + 2$

Alice = 0

- Start: Alice $\rightarrow 1, 2$

– $1 \rightarrow 3, 4$ and $2 \rightarrow 5, 6$

– $3 \rightarrow 7, 8$ and $4 \rightarrow 9, 10$

– $7 \rightarrow 15, 16$ and $8 \rightarrow 17, 18$

and $11 \rightarrow 23, 24$ and $12 \rightarrow 25, 26$ and

$14 \rightarrow 29, 30$

$1 \rightarrow 2, 3, 4$ and $2 \rightarrow 3, 4, 5, 6$

$6 \rightarrow 13, 14$

$20 \rightarrow 21, 22$

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- Information spreads as fast as the previous strategy,

– calling rule seems much more natural and

– easier to understand.

Use overlaps

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Not Robust Enough Assignment Project Exam Help

- Alice is not quite happy with this c .
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- What if one of her fellow students ht and calls a wrong pair of students on the list?
- Moreover, there can still be a couple of students who just forget or do not both
[Assignment Project Exam Help](#)
- In this case, some st
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- Therefore, Alice thinks about a more robust
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New Idea: Allow Overlap Assignment Project Exam Help

- allow overlappnig calls
 - to ensure fault tolerance

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- allow calls from multiple initiators!

- to ensure fault tolerance

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More Robust (1/2) Assignment Project Exam Help

- One possibility would be that for each i , the person in “list” position i would call the four functions

$$2i + 1, 2i + 2, 2i + 3, 2i + 4.$$

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- Thus, for each i ,

$$i \rightarrow 2i + 1, 2i + 2, 2i + 3, 2i + 4.$$

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- In Summary

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$$i \rightarrow 2i$$

$$i+3, 2i+4$$

$$i+1 \rightarrow 2i+3, 2i+4, 2i+5, 2i+6$$

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$2i+4$
received from
 $i, i+1$

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- Notice the overlap between consecutive [Add WeChat \[edu_assist_pro\]\(https://eduassistpro.github.io/\)](https://eduassistpro.github.io/)s!

$$i+1 \rightarrow 2(i+1)+1, 2(i+1)+2,$$

$$2(i+1)+3, 2(i+1)+4$$

Given k , who has sent the message to k

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Calling Patterns Assignment Project Exam Help

- Who is going to call user
- Assume $k = 2l$ is even.
 - k is called by users $l - 1$ and $l - 2$.

$$k = 2l - 4 + 4$$

$$l - 2 \rightarrow 2(l - 2) + 1, 2(l - 2) + 2, 2(l - 2) + 3, 2(l - 2) + 4$$

$$\rightarrow l - 1 \rightarrow 2(l - 1) + 1, 2(l - 1) + 2, 2(l - 1) + 3, 2(l - 1) + 4$$

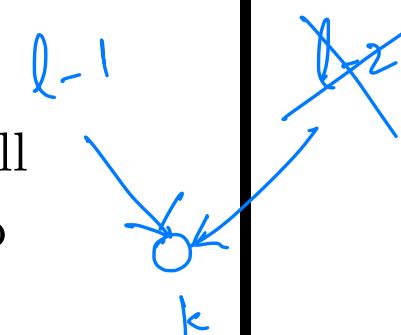
- Assume $k = 2l$

- k is called by $l - 1$ and l

$$l - 1 \rightarrow 2(l - 1) + 1, 2(l - 1) + 2, 2(l - 1) + 3, 2(l - 1) + 4$$

$$l \rightarrow 2l + 1, 2l + 2, 2l + 3, 2l + 4$$

- All students (except for the first four on the list who will directly be called by Alice) will be called by exactly two students in the ideal case.



A node k will always receive the message

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provided that one of

the two senders did

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not fail to send.

"Limited" Fault Tolerance that is quantified with the # of faults

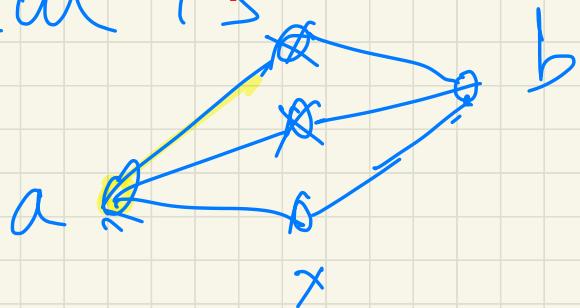
i.e. when we study a distributed system.

Assignment Project Exam Help does

not work if then
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the algorithm is

robust.



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- Assume $n = 17$ (Including Alice)
- Start: Alice $\rightarrow 1, 2, 3, 4$

- Rule: $i \rightarrow 2i + 1, 2i + 2, 2i + 3, 2i + 4$

$$- 1 \rightarrow 3, 4, 5, 6, 2 \rightarrow 5, 6, 7, 8,$$

$$- 3 \rightarrow 7, 8, 9,$$

$$- 4 \rightarrow 9, 10, 11,$$

$$- 5 \rightarrow 11, 12, 13, 14,$$

$$- 6 \rightarrow 13, 14, 15, 16,$$

$$- 7 \rightarrow 15, 16$$

Example (1/2)

With $f = 0$
Partition Alg.

$$f = 1$$

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^a**NB:** user 7 sends only to two users instead of four. To overcome this problem the algorithm can wrap-around to the beginning nodes 1, 2, We will not discuss this issue in detail.

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- Information spreads as fast as t
– calling rule sounds now m
– the system is now fault tolerant.
- egy,
nd

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More Robust Assignment Project Exam Help

- Thus, as long as for each such pair a student is unreliable (by not being reachable), all of the reliable students will still be informed.
- Intuitively, this can be argued as follows:
 - If one can select a caller for each student who works reliably, then a call chain from him will reach all reliable students.
- This strategy can be made even more robust by really sure to reach everybody who is reachable:

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Even More Robust (1/2) Assignment Project Exam Help

- For some fixed r :^a

If every student at position i sends to $2r$ students at positions

$$i \Rightarrow 2i + 1, 2i + 2, \dots, 2i + 2r$$

i sends to
 $2r$ nodes

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then every student (except for the first $2r$ ones who are directly called by Alice) will be called by exactly r many students in the ideal case.

^aThe parameter r is related to the desired fault tolerance.

If Alice fails the whole
party will not take place!

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Design algorithms with
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multiple indicators
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① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨

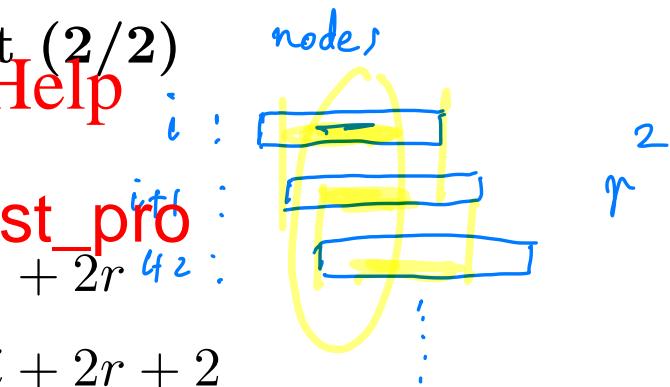
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Even More Robust (2/2) Assignment Project Exam Help

- In Summary

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$$i \rightarrow 2i + 1, 2$$



$$i + 1 \rightarrow 2i + 3, 2i + 4, \dots, 2i + 2r + 2$$

i [Assignment Project Exam Help](https://eduassistpro.github.io/)

⋮

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$$i + r - 1 \rightarrow 2(i + r) - 1, 2(i + r) + 2r - 2$$

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⋮ → ⋮

- Notice the overlap of consecutive transmissions!

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- How many users will call user k by $2r$ and let $j < 2r$
- Use the Euclidean algorithm to find k by $2r$ and let $j \geq 1$ the quotient so that

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- Observe that

$$k = 2qr + j = 2(2s) + j,$$

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for all s (positive or negative).

- Recall the calling rule for $i = qr + s$:

$$i \rightarrow 2i + 1, 2i + 2, \dots, 2i + 2r$$

- Hence user k will be called by users i such that $i = qr + s$, provided that $0 \leq j - 2s \leq 2r$.

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- Therefore, if r was used in the broadcast each user is called by r alternate users
- Hence, as long as **at most** $r - 1$ of these are faulty (e.g., they are not calling) all reliable students will still be reached.

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- Thus, the algorithm has $r - 1$ faults!

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If ~~Add WeChat edu_assist_pro~~ does not exceed $r - 1$ then the strategy is fault tolerant.

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Initia
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Question: If Alice Fails?
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- A weakness of the algorithm is the single initiator, namely Alice.
- Consider the following scenario:
 - k initiator nodes wake-up at the same time
 - A given number, k , may fail.
- Can we design a fault-tolerant algorithm?



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1. Prove the correctness of the Heart by proving.
 - (a) show that when $\text{emp} \in \mathcal{V}_i \subseteq V_k$.
 - (b) show that at the end every process must have received the value $s(i)$ from every other process i .
2. List some of the issues that may arise in the complete network K_n by the simultaneous execution by many nodes.
3. Verify the calling pattern discussed in the figure. A student at position i calls the students at positions

$$2i + 1, 2i + 2, \dots, 2i + 2r$$
4. Show that for n students the partitioning algorithm takes time $O(\log n)$.

^aNot to submit

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5. (*) Design a broadcast algorithm which is fault tolerant under k initiators.
6. (*) Extend the previous broadcast to be fault tolerant under $< r$ participants.
7. (**) An interesting analysis for broadcasting is the average case. For a given number x (e.g., 10) of unreliable students, who are assumed to want to determine <https://eduassistpro.github.io/> for which the probability that all reliable students are reached is above, say, 90%. In other words,

Given n participants and a parameter $0 < p < 1$, what is the minimum value of r such that

$$\Pr[\text{all reliable students are reached}] \geq p$$

Give a broadcasting algorithm and analyze its complexity. As a

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hint this can be based on an array A that is defined as follows:

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- (a) N is the total number of students.
- (b) A : array $[1 \dots N]$ of integers; $A[i]$ counts, for a reliable student at position i , the number of calls that student would get from [Assignment Project Exam Help](https://eduassistpro.github.io/)
- (c) For every reliable student, $A[i]$ will initially be set to 0.
- (d) For all unreliable students at position i , $A[i]$ will initially be set to $-r$ (so that even after r calls there will not be a positive value in $A[i]$).

In order to determine this r , one can use the algorithm presented below (Below Steffi = Alice).

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Simulate this algorithm and test its performance.

8. Design fault tolerant broadcasting algorithms assuming multiple initiators.

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9. Design a probe-echo algorithm to compute the topology of a network whose topology is a strongly connected graph. When the algorithm terminates, the algorithm should have knowledge about all the nodes in the network.

10. Design an algorithm to count the total number of processes in a unidirectional ring. The process in the ring can initiate processes can concurrently run the algorithm to use process ids.

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