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- How can we use port labeling sch communately WeChat edu_assist pro
- What role do port labeling schemes play in distributed computing?

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• The execution of a di the sequence of https://eduassistpro.github.io/ distributed algorithm at that node.

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Can we solve a problem in a way that all node sequences at each node?

nds on

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- Probabilistic Method
 - Add WeChat edu_assist_pro
 Universal traversals

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- Using probability to prove the e hematical object is Add Whe Chat and Utiassist pro
- It has many applications, especially in graph theory.
- It uses the following principle ct Exam Help

 If, in a given set of o
 randomly chattps://eduassistpro.github.io/perty
 is less than 1 then there must exist a
 this property.

Union Form of the Probabilistic Method Assignment Project Exam Help

• Consider n events A_1, A_2

ecessarily independent).

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 The union (or Boole) Inequalit

$$\text{Assignment} \underbrace{Pr}_{1} \underbrace{A_{i}}_{1} \underbrace{\leq \sum_{i=1}^{n} \Pr[A_{i}]}_{\text{ect}}$$

• Therefore if we https://eduassistpro.github.io/

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$$We$$
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it is enough to show that

$$\sum_{i=1}^{n} \Pr[A_i] < 1.$$

Expectation Form of the Probabilistic Method Assignment Project Exam Help

- Consider an integer valued ran X which takes only non-negatidelimeger hatuedu_assist_pro
- Observe that

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Therefore

$$\Pr[X > 0] \le E[X] \tag{1}$$

Expectation Form of the Probabilistic Method Assignment Project Exam Help

• Equation (1) is a special cas of Mar ty wchich states thatdd WeChat edu_assist_pro

$$\Pr[X > kE[X]] \le \frac{1}{k}$$

• Therefore using Equation (1) if we want to prove that Assignment Project Exam Help

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it is enough to prove that Add WeChat edu_assist_pro E[X]

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- Graph traversal (also known a fers to the process Addit McChakadunassist_pro) each vertex in a graph. E.g.,
 - BFS
 - DFS Assignment Project Exam Help
- Used in Search https://eduassistpro.github.io/
- Each starting node is weighed with a assist_pro
 - typically a sequence of port labels that it must follow from node to node) which is used to traverse the graph.
- However, the program used may depend on the starting node.

- A sequence is universal for grap n vertices if for every graph and der washate edutiassist pro he (same) sequence will visit every vertex in the graph.
- Can you produce a universal traversal program that will work for every graphent Project Exam Helpaph?
- To produce a whiteps://eduassistpro.github.io/ tion of graph labeling.
 - For each vertex u, label the edges assist_pro_u (ports) from 1 to deg(u) (in fact any numbering will do).
 - This is what we defined as port labelings!
- Then a sequence is a string of edge labels which determines some walk through the graph.

Universal Traversals on Labyrinths Assignment Project Exam Help • A robot is placed in a labyrinth in a $\times n$ square grid.

- It runs a program: a sequence of coist pro rmN(orth), S(outh), E(ast), W(est),

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- As an example consider the program NESWEW which is given to every node.
- A robot has the sequence "NESWEW" and starting at a node makes movements following the sequence of labels.

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- In addition to external walls on t ter, walls are also placed between the charged assist pro
- Executing each command, the robot moves in the prescribed direction if possible (and does nothing when there is a wall in this direction) ignment Project Exam Help

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E.g., NESWEEEW

- We can show that
 - Theorem $\operatorname{Chat}_{\operatorname{equ}}$ assist $\operatorname{pro}_{\operatorname{any}} n$, there exists a program that works correctly for all labyrinths of size at most $n \times n$ (independently of the positions of walls inside the square and the robotism $\operatorname{prop}_{\operatorname{and}}$ $\operatorname{pro}_{\operatorname{and}}$ $\operatorname{pro}_$
- "Works correct https://eduassistpro.github.io/ hable cells.
- To solve the traversal problem,

 we prove that a sufficiently long random program will work with positive probability.
- We will do this using the union bound.

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- For each $n \times n$ labyrinth of size $4n^4$ that works fo Aid, the Watchell Education of n^2 steps (round-trip) and there are at most n^2 admissible cells.
- To prove this note that for each starting cell there is a spanning the signment Project Trans Help labyrinth, think of it as a distrib

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• Assign ports to each vertex (edge labels associated to the edges connected)

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• Using a pre-order traversal of th which has length at Ardost We Chargedu_assist_pro at most $4n^2$ steps (round trip).

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• Therefore, a random program of size $N = 4n^4$ will work with probability at least $\epsilon = (1/4)^{4n^4}$ and fail with probability at most $1 - \epsilon$.

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- Select among such programs of $=4n^2$ independently and uniformly Weightainedu_assist_pro
- Now for each k concatenate k such programs:

- By independe N will fail with probabilities://eduassistpro.github.io/
- More generally at most $(1 \epsilon)^k$.
- This probability is computed for a fixed labyrinth L.
- Let F_L be the event that a program of size kN fails for the labyrinth L.
- It follows from the above that $\Pr[F_L] \leq (1 \epsilon)^k$.

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• Now take the union \bigcup_L runs over all labyrinths. As a consequence Chat edu_assist_pro

$$\Pr\left[\bigcup_{F_L} F_L\right] \leq \sum_{Pr[F_L]} \Pr[F_L]$$
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$$\ell (1 \quad \epsilon)^k$$

where ℓ_n is the https://eduassistpro.githubgiq/.

• However, we candow & Shart edu_assist_pro

$$\ell_n < \frac{1}{(1-\epsilon)^k} \tag{2}$$

• So,

$$\Pr\left[\bigcup_{L} F_{L}\right] < 1$$

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• In particular, for a k sati ity (2), we have that

Add WeChat edu_assist_pro $\Pr\left[\bigcap_{L} \neg F_{L} = 1 - \Pr\left[\bigcup_{L} F_{L}\right]\right]$

- Therefore for k https://eduassistpro.github.io/of size kNworks for all labyri
- Therefore such a program must exist! assist_pro

Efficiency of Universal Traversals Assignment Project Exam Help

- How about the length of the sequ
 - Can wedd WeChat edu_assist_pro ence of polynomial length in polynomial time (in the size n of the graph)?
- How about efficiency? Project Exam Help
 - Can we give https://eduassistpro.github.io/ aversal sequence?

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Can we make the construction distribu

Universal Traversals on Graphs Assignment Project Exam Help

- The Universal Traversal the n phs of a given size n. Add WeChat edu_assist_pro
- Instead of N, S, E, W used in $n \times n$ grids one now uses ports and port-labelings.

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- 1. The traversal of the labyrinth was ce that was provaided two hatoeand assist_pro st follow. Consider the situation where the robot constructs the sequence "on the fly": looks at the surrounding environment and based on what it is protected to protect the protection of the latest protection of the latest protection of the latest protection of the latest latest protection of the latest late
 - Add WeChat edu_assist_pro
- 2. (*) Use the probabilistic method to prove versal theorem on graphs of a given size.n. **Hint:** Instead of N, S, E, W used in $n \times n$ grids one now uses ports.

 Consider a set of points in the plane. Form n sets A_1, A_2, \ldots, A_n on the plane each of which has k points.

aNot to submit.

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The sets are arbitrary and may share points. Assume that

The sets are arbitrary and may share points. Assume that $n < 2^k$. Show that p://eduassistpro.github?io/lor each point red or blue in such a way that every set A_i has both colors. Hint: Adde We Chat edu_assist_enternty and use the probabilistic method.

3. A certain commodity is sold with two lottery tickets, a and b, for Prize A and Prize B, respectively. Suppose the winning probability for A and that for B are both 2/3. Show that there

must exist a commodity with two winning tickets.^b
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- 4. (*) The sets S_1, S_2, \ldots, S ubsets of a set S that has 2n eladents C_1 by edu_assist_lears Sperner family if $S_i \not\subseteq S_j$, for all $i \neq j$. Use the probabilistic method to prove Spener's theorem, namely "If $\{S_1, S_2, \ldots, S_k\}$ is a Sperner family then S_1 below.
 - (a) Consider the foll ptyset and add ranhttps://eduassistpro.githuhtip/after 2n steps) we get the whole set S that $A \subset S$ of size a show that A will appear $A \subset S$ of probability $\Pr[A] = 1/\binom{2n}{a}$.
 - (b) Consider k random variables X_1, X_2, \ldots, X_k so that the value of X_i is equal to 1 if the given set S_i appears during the process, otherwise, it is equal to 0. Show that the

bNote that the conclusion is derived without using event dependence.

^cSperner families have applications in Cryptography and elsewhere.

Assignment Project Exam Help s_i is the number of elements in S_i ,

(c) Now, Addi Wretchamed wassist X pro $X_1 + X_2 + \cdots + X_k$. Show that this sum is less than 1 in expectation.

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- Alon, N., Spencer, J. H. (2004). T c method.

 John Wiked We Chat edu_assist_pro
- Hirokasu Iwasawa, Using Probability to Prove Existence,
 Mathematical Intelligencer, Volume 34, Number 3, 2012.
 Assignment Project Exam Help
- Mathematical In , 1998
- Aleliunas, R. Kartps://eduassistpro.github.io/ Random walks, Aniversal traversal se_assist_pro complexity of maze problems. 20th Ann on Foundations of Computer Science (FOCS 1979): 218?223