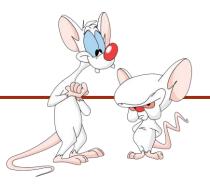
Assigned MPc1250Help INTRODUC https://eduassistpro.gtffR.SCIENCE

Week 10-14 Recursion 3 (Me _______ accordicksort)

Giulia Alberini, Fall 2020

WHAT ARE WE GOING TO DO IN THIS VIDEO?



Merge sort

Assignment Project Exam Help

Quick sort

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

TIME COMPLEXITY

	1	
$O(\log n)$	O(n)	$O(n^2)$
Assi	nment Project Exam	Help insertion/selectio
convert to binary	nttps://eduassistpro.gi	thub.10/
 binary search 	Add WeChat edu_ass - grade sch	ist_pro grade school
	addition	multiplication



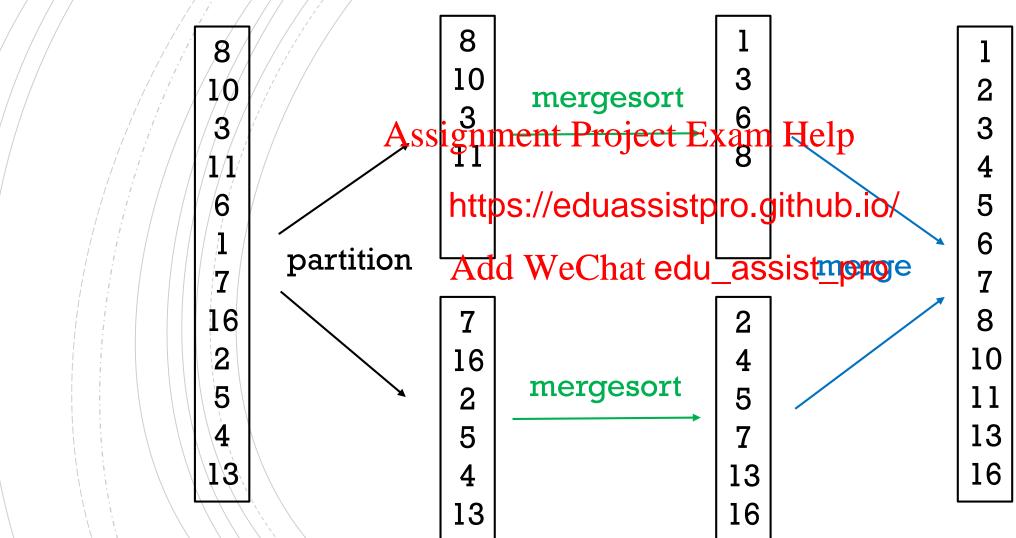
MERGE SORT

Merge Sort is a divide and conquer algorithm.

- GOAL: Sort an list Assignment Project Exam Help
- IDEA: https://eduassistpro.github.io/
 - Partition the list into two halves.
 Add WeChat edu_assist_pro
 Sort each half recursively

 - Merge the sorted half maintaining the order.

IDEA



IMPLEMENTATION

```
mergesort(list) {
      if (list.size() == 1)
            return list
                     Assignment Project Exam Help
      else {
          mid = (list.si https://eduassistpro.github.io/
          list1 = list.getElements(0, Add WeChat edu_assist_pro
          list2 = list.getElements(mi
                                                  size()-1)
          list1 = mergesort(list1)
          list2 = mergesort(list2)
          return merge(list1, list2)
```

IMPLEMENTATION

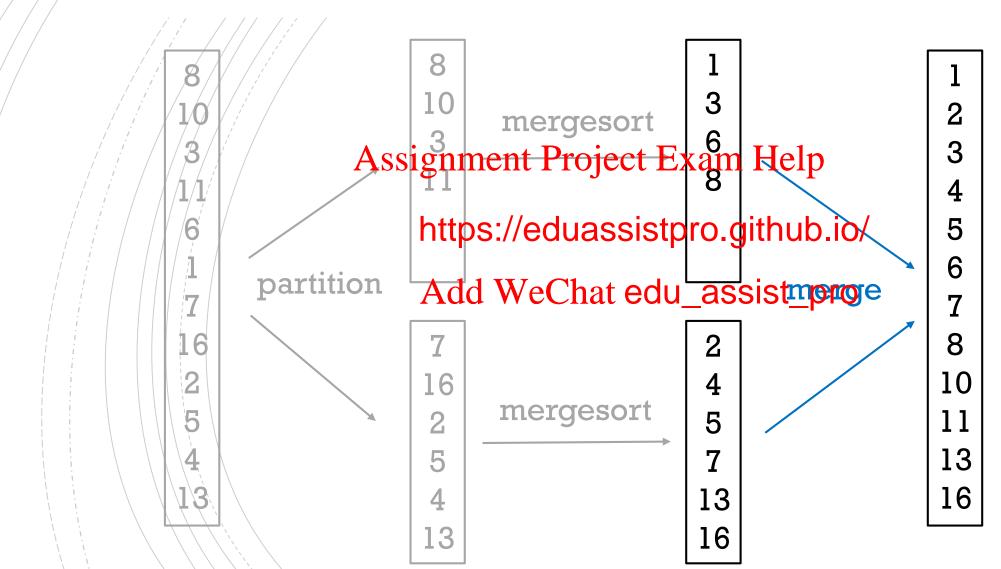
```
mergesort(list) {
     if (list.size() == 1)
          return list Assignment Project Exam Help
     else {
        mid = (list.si https://eduassistpro.github.io/
        list1 = mergesort(list1)
        list2 = mergesort(list2)
        return merge(list1, list2)
```

Base case

Partition

Recursive sort

Merge



Iterate through the elements of the two sorted list. Assignment Project Exam Help Depending on how the compare decide which element comes first in t merged list.

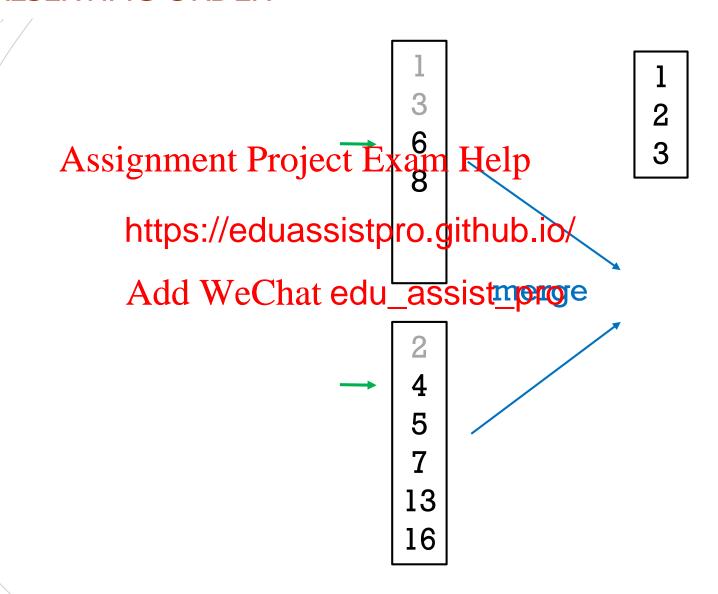
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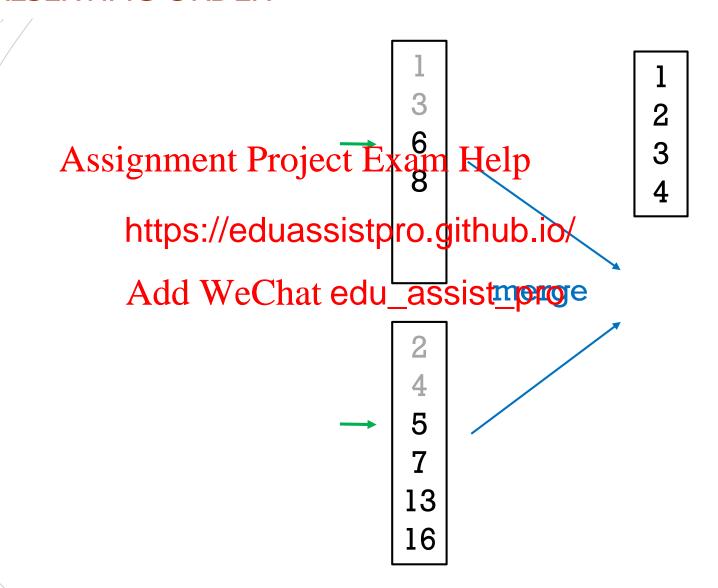
5 13 16

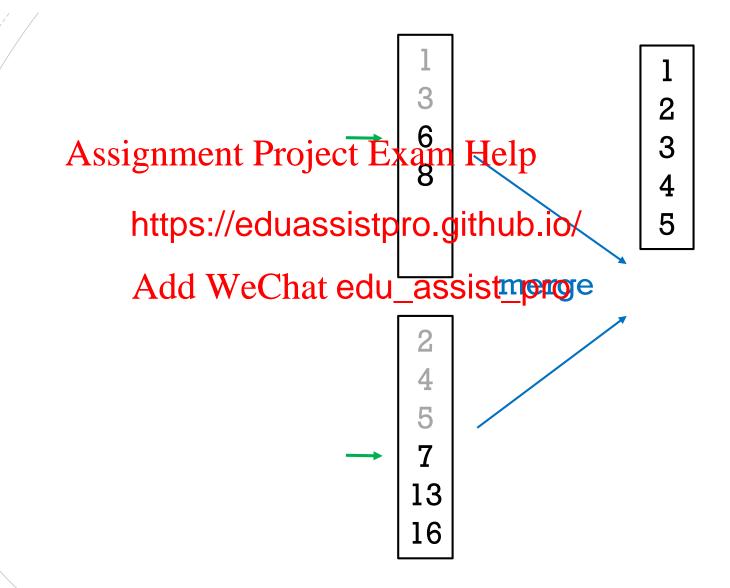
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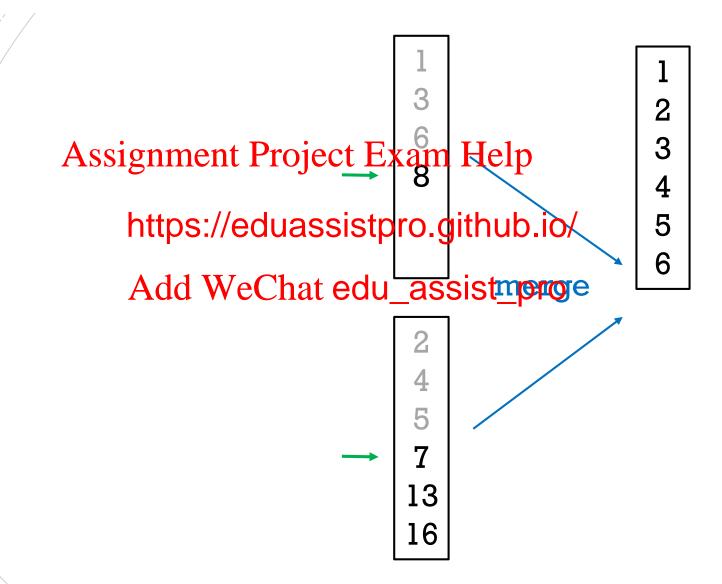
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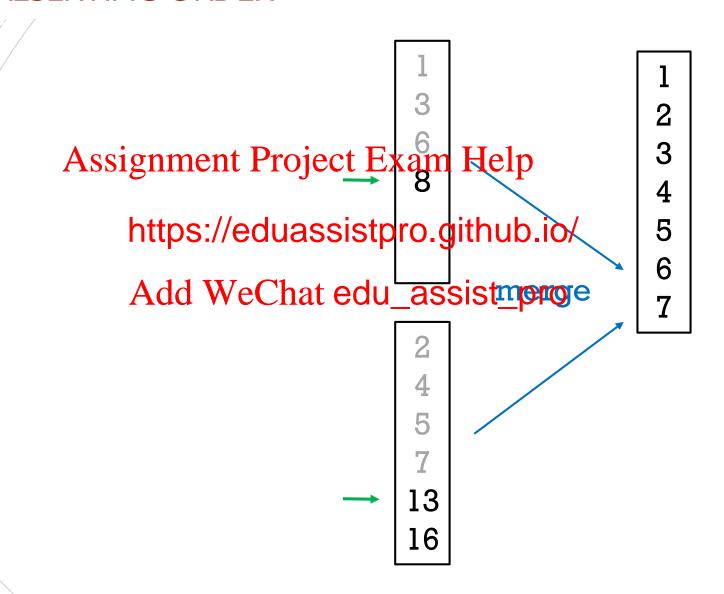
MERGING PRESERVING ORDER Assignment Project Exam https://eduassistpro.github.io/ Add WeChat edu_assistmerore 5 13 16

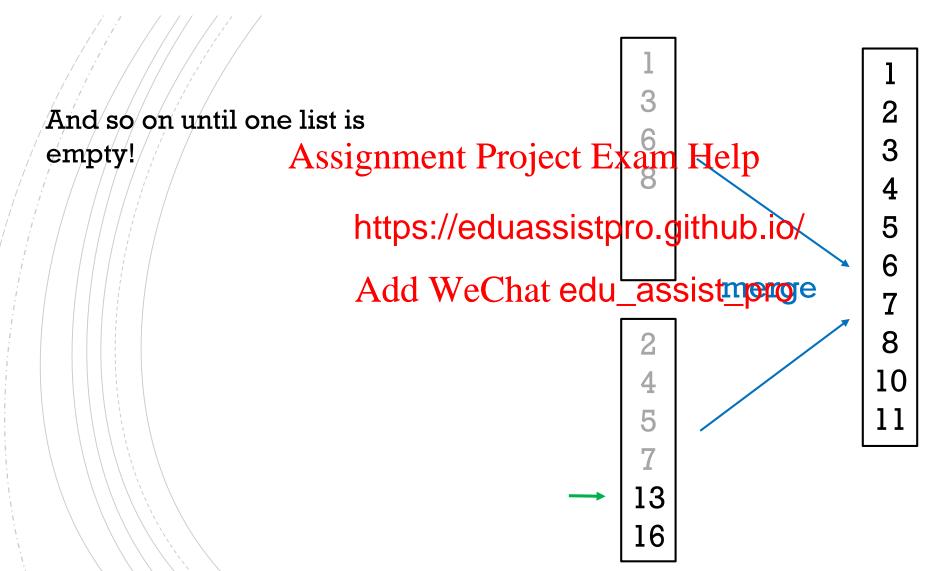


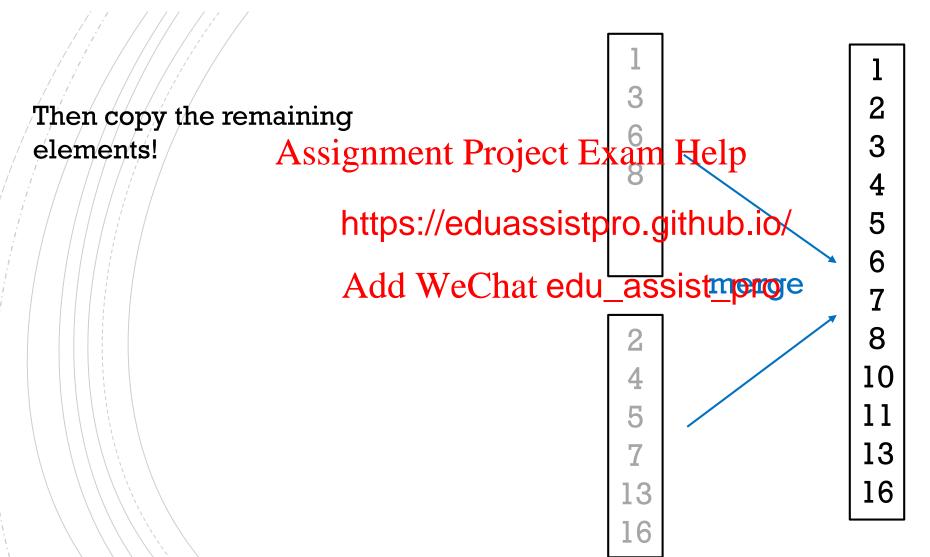












IMPLEMENTATION OF MERGE

```
merge(list1, list2) {
      list = ...initialize with empty list...
      while (!list1.isEmpty() && !list2.isEmpty()) {
            if (list Assignment Project Exam Help
                   list.a
                                                rst())
                          https://eduassistpro.github.io/
            else
                   list.addlast (list2
Add WeChat edu_assist_pro
      while (!list1.isEmpty())
             list.addlast(list1.removeFirst())
      while (!list2.isEmpty())
             list.addlast( list2.removeFirst())
      return list
```

IMPLEMENTATION OF MERGE

```
merge(list1, list2) {
      list = ...initialize with empty list...
      while (!list1.isEmpty() && !list2.isEmpty()) {
            if (list Assignment Project Exam Help
                   list.a
                                                rst())
                          https://eduassistpro.github.io/
            else
                   list.addlast(list2
Add WeChat edu_assist_pro
      while (!list1.isEmpty())
             list.addlast(list1.removeFirst())
      while (!list2.isEmpty())
             list.addlast( list2.removeFirst())
      return list
```

Pick elements to add until one of the two lists is empty

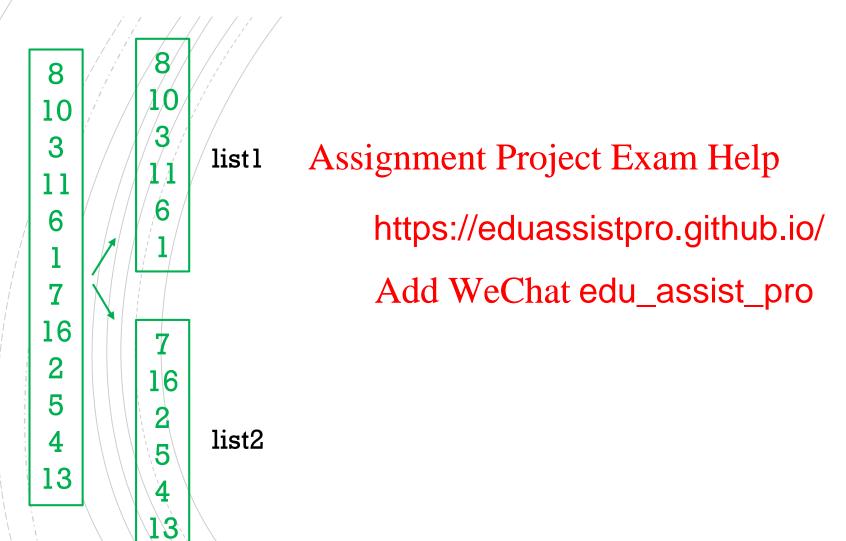
Then add the remaining elements

EXAMPLE OF EXECUTION

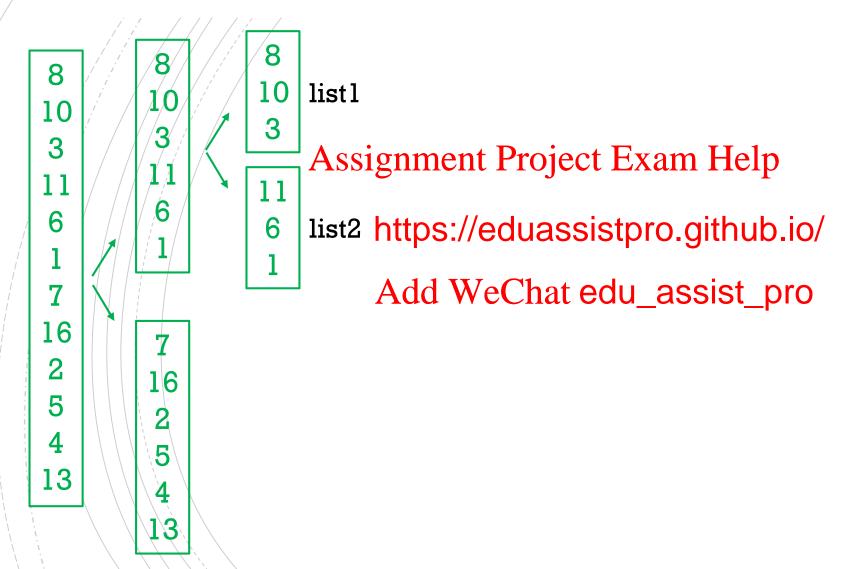
```
8
10
3
11
6
16
13
```

```
mergesort(list) {
      if (list.size() == 1)
         Assignment Project Exam Help
      else
         mid https://eduassistpro.github.io/
         listAdd Wethat edu_assist_pro
          list2 = list.get id+1, list.size()-1)
          list1 = mergesort(list1)
          list2 = mergesort(list2)
          return merge(list1, list2)
```

EXAMPLE OF EXECUTION

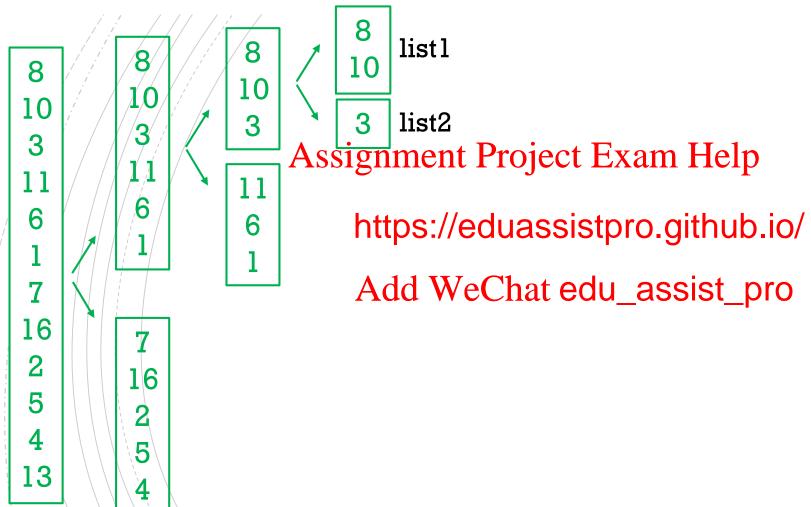


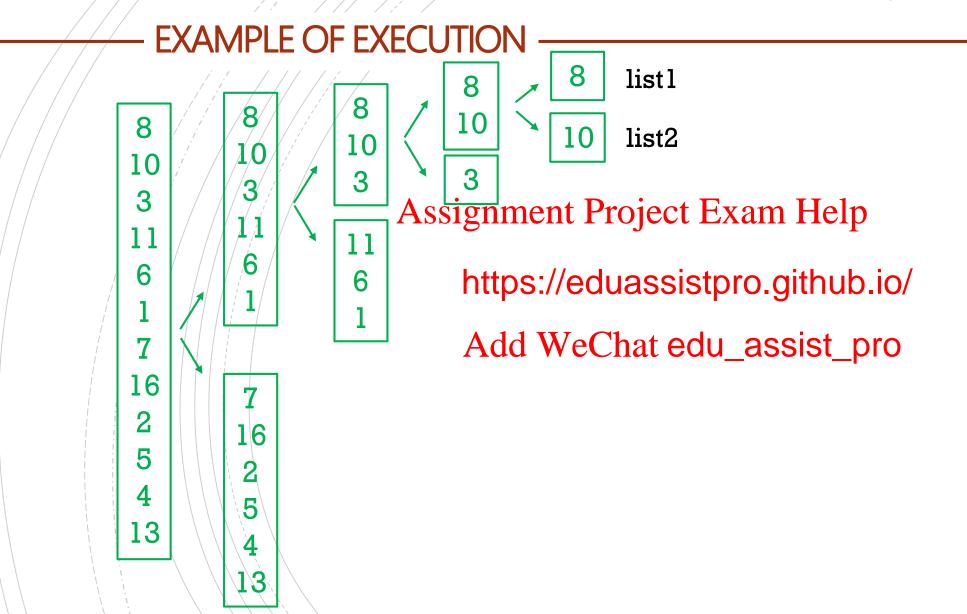
EXAMPLE OF EXECUTION

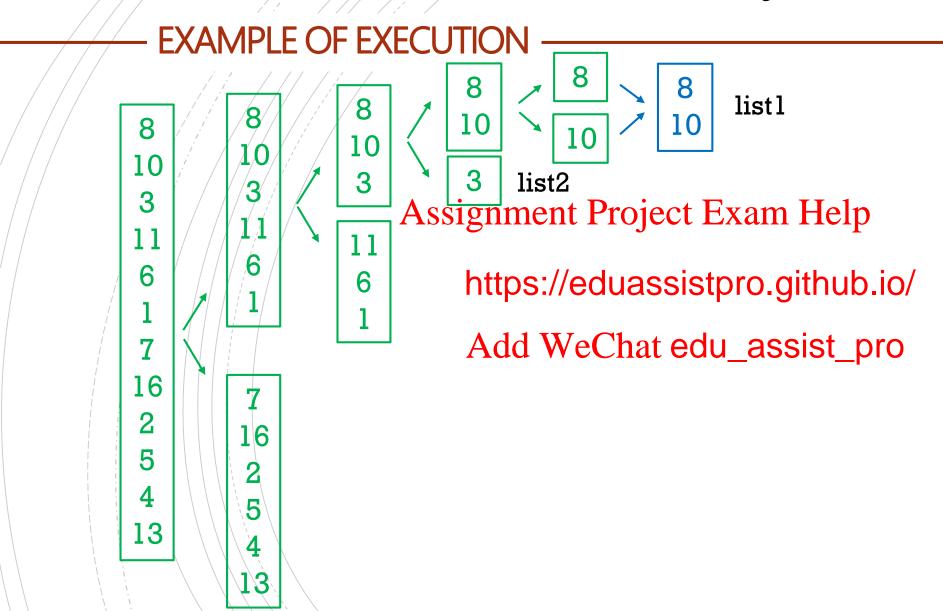


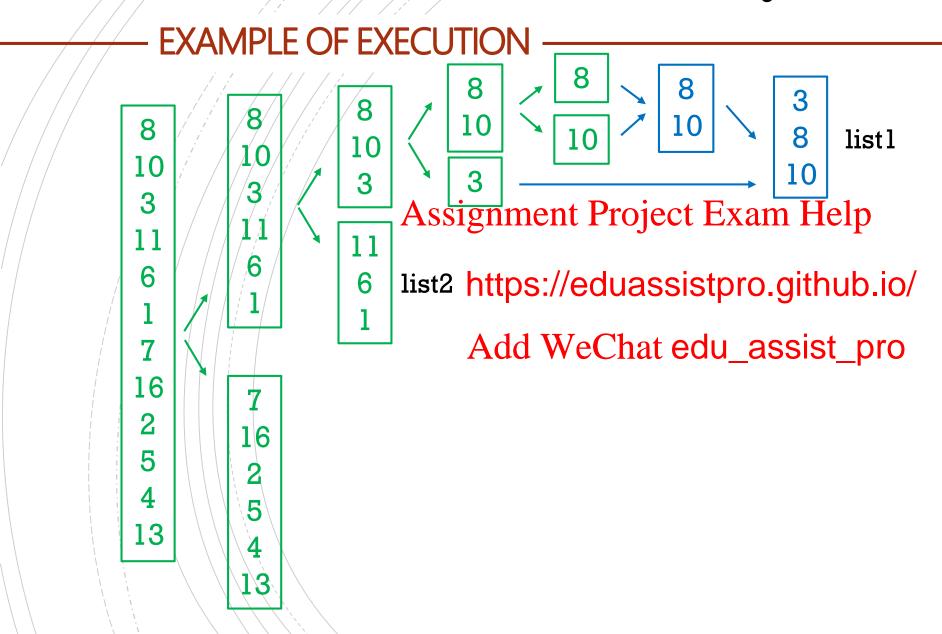


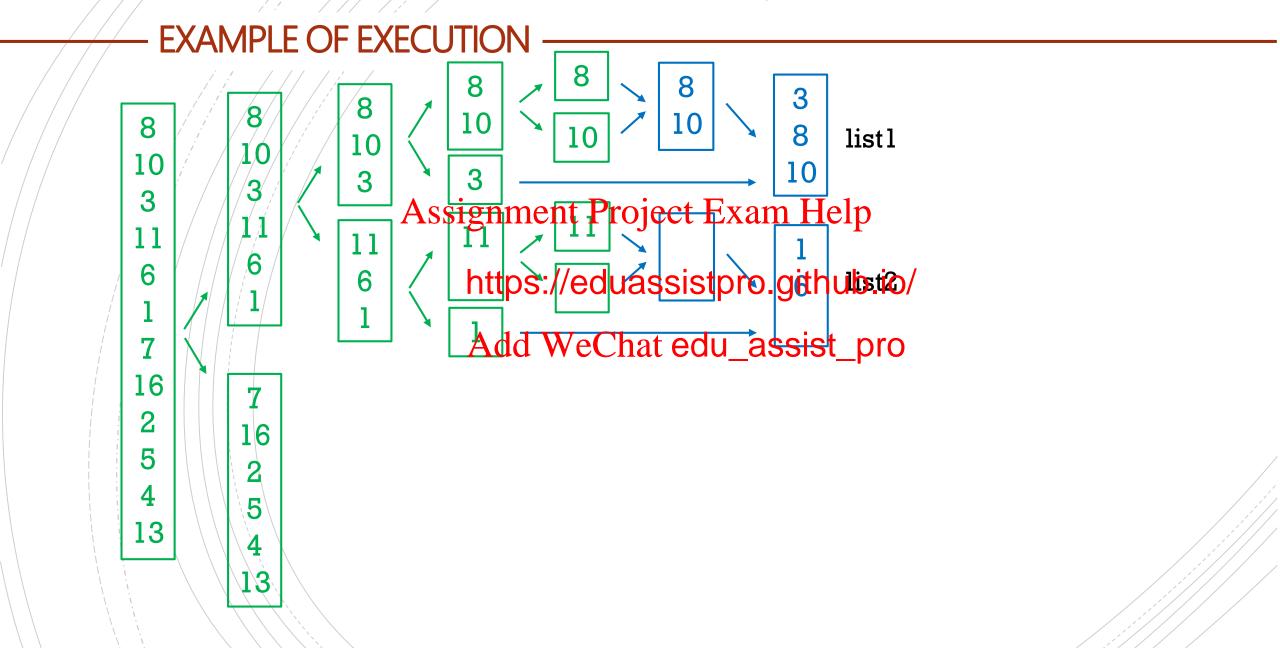
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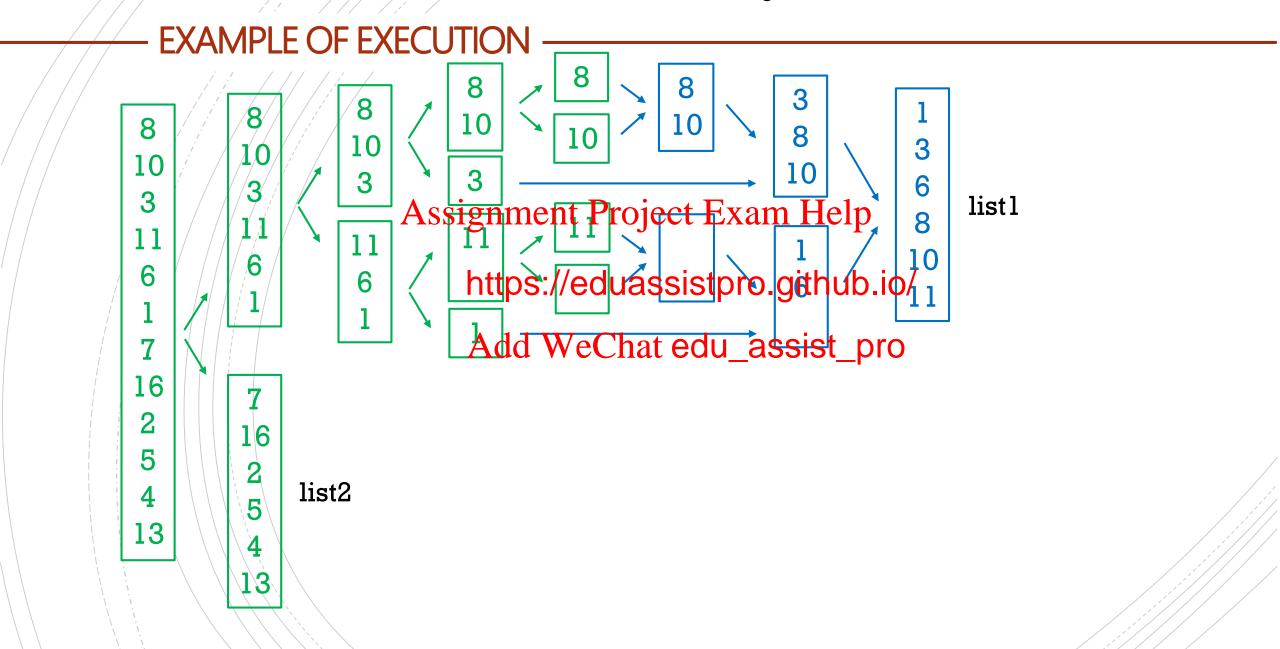


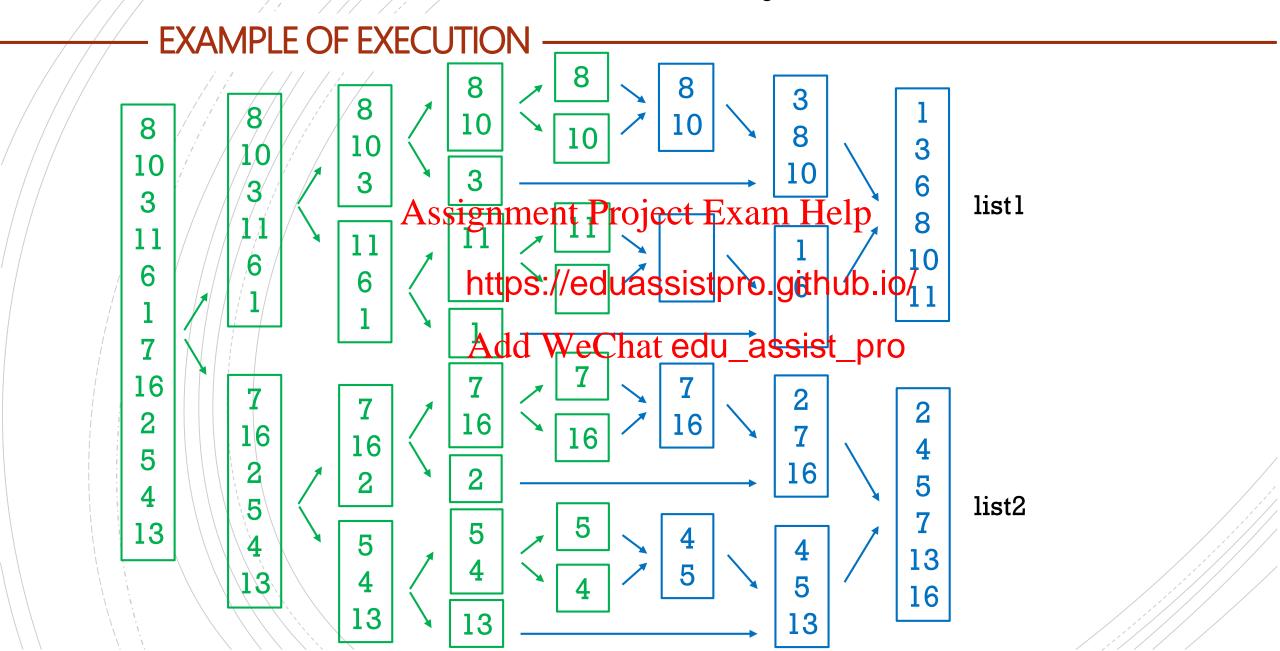


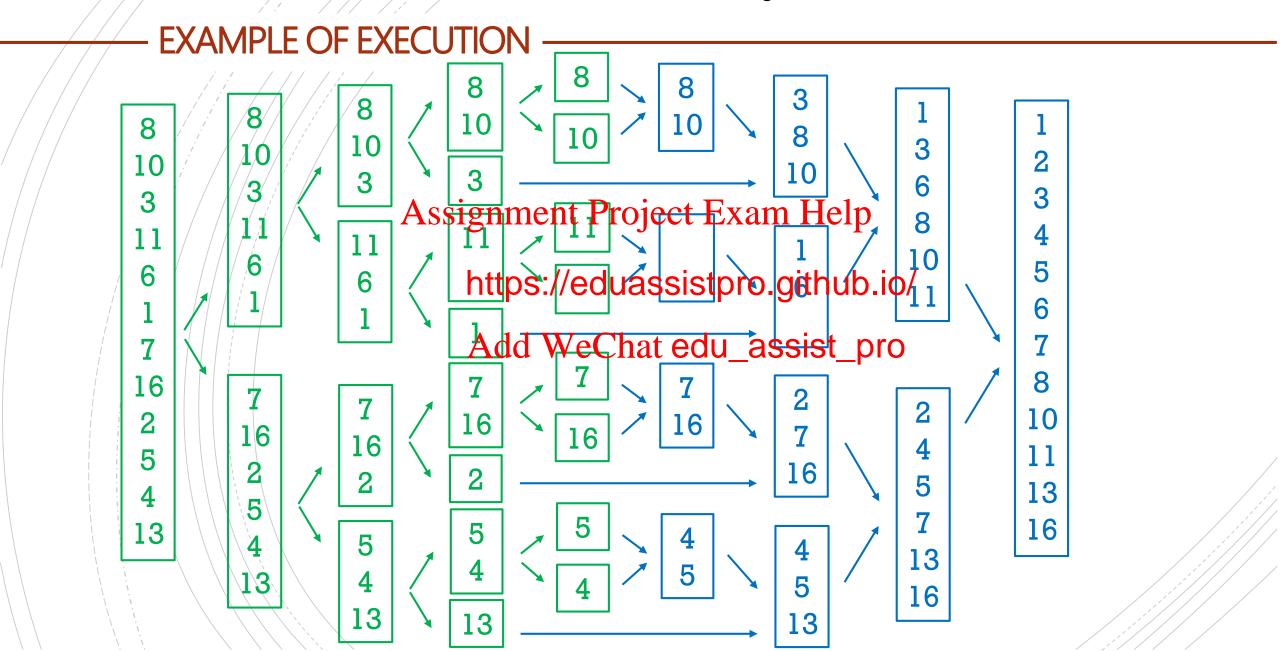


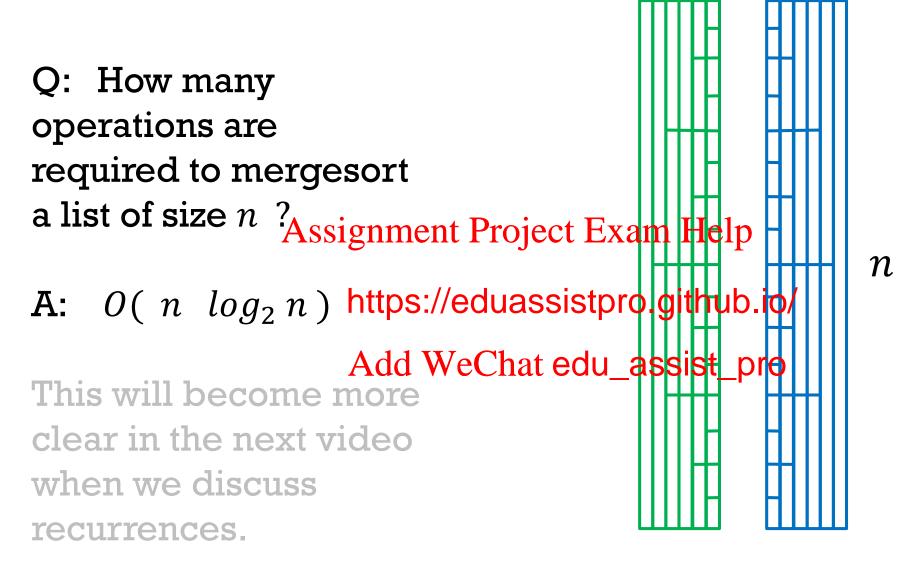












 log_2n log_2n

COMPLEXITY

$n \log_2 n$ is much closer to n than to n^2

$log_2 n$	Assignment Pr	roje at Eaga i Hel	$p n^2$
10	$2^{10} \approx 10^3$	uassistpro.githu hat edu_assist_	10 ⁶
20	$2^{20} \approx 10^6$	~10 ⁷	10^{12}
30	$2^{30} \approx 10^9$	~10 ¹⁰	10^{18}

COMPLEXITY

 $n \log_2 n$ is much closer to n than to n^2

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$log_2 n$	Assignment P	roje et Eag m He	$p n^2$
	10	$2^{10} \approx 10^3$		106
$30 \qquad 2^{30} \approx 10^9 \qquad \sim 10^{10} \qquad 10^{18}$	20	$2^{20} \approx 10^6$	~10 ⁷	10 ¹²
	30	$2^{30} \approx 10^9$	~10 ¹⁰	10 ¹⁸



QUICK SORT

- Quick Sort is a divide and conquer algorithm.
- GOAL: Sort a list. Assignment Project Exam Help
- IDEA:

Pick an element of the https://eduassistpro.github.io/

- Partition the list moving the westbat edu_assistion making sure that all the lower elements are on its left and all the larger elements are on its right.
- Sort the left part AND the right part of the list recursively.
- Keep doing it until there's nothing left to sort.

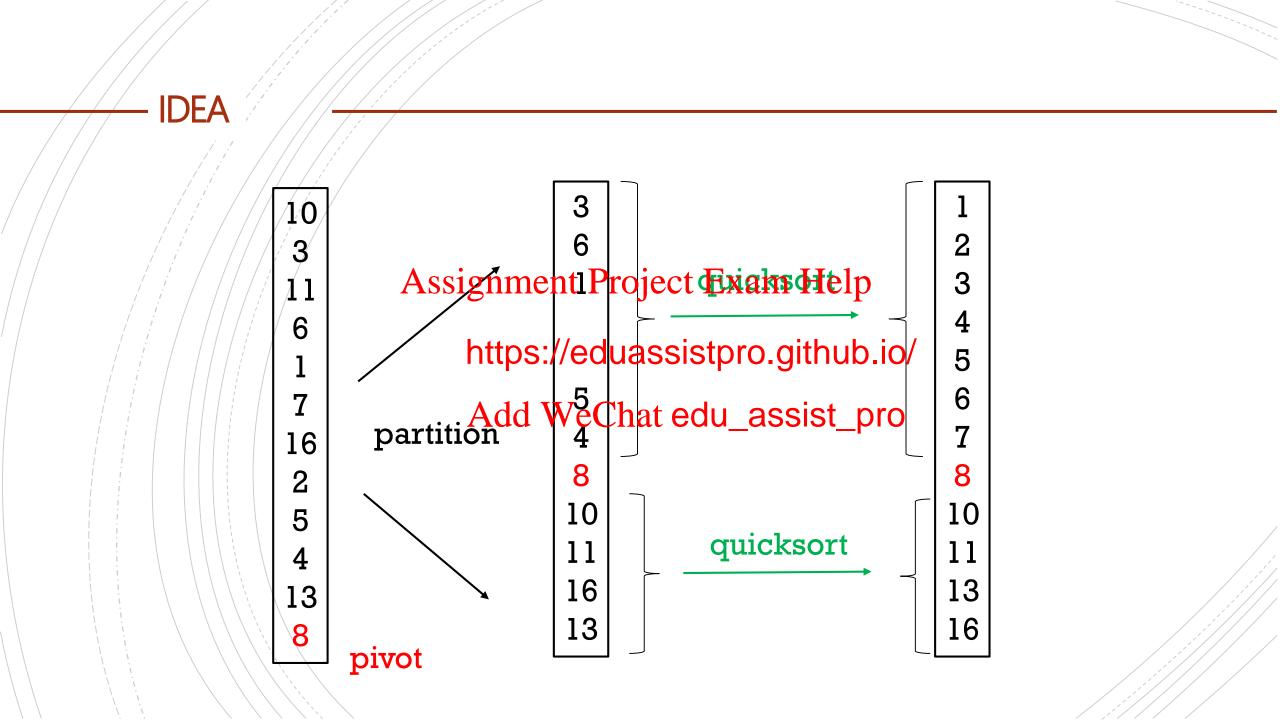
IDEA

IDEA:

- Pick an element of the array (the pivot).
 Assignment Project Exam Help
- Move the pivot to its c https://eduassistpro.github.io/This is the crucial sure that all the smalle and all the larger elements are charted edu_assist_process of the algorithm!
- Sort the left part AND the right part
- Keep doing it until there's nothing left to sort.

Recursive Step

Base case



THE PIVOT

Different versions of Quick Sort pick the pivot in different ways: Assignment Project Exam Help Always pick the first element as the pivot

- Always pick the last e https://eduassistpro.github.io/
- Pick a random element Add WeChat edu_assist_pro
- Pick the median as pivot

THE PIVOT

Different versions of Quick Sort pick the pivot in different ways:

Assignment Project Exam Help
Always pick the first element as the pivot

- Always pick the last e https://eduassistpro.github.io/
- Pick a random element dd WeChat edu_assist_pro
- Pick the median as pivot



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Add WeChat edu assist_pro 5

1. Pick the pivot.

Assignment Project Exam Help

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Add WeChat edu assist_pro 3

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu assist pro 3

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by 1, and place the element just behind the wall.
 - Otherwise, do nothing.

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.



5<3 false \rightarrow do nothing!

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.

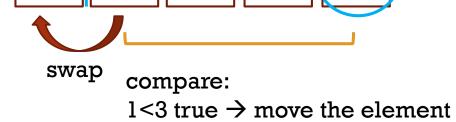
compare: 1<3 true

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.

compare:

1 < 3 true \rightarrow move the wall

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.



- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.

compare: 4<3 false \rightarrow do nothing

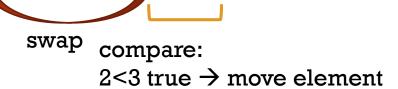
- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.

compare: 2<3 true

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.

compare: 2<3 true → move wall

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
 - Otherwise, do nothing.



- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/

swap

- If the element is smaller than the pivot, move the wall right by I, and place the element just behind the wall.
- Otherwise, do nothing.
- 4. Move the pivot next to the wall.

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements right part the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by 1, and place the element just behind the wall.
 - Otherwise, do nothing.
- 4. Move the pivot next to the wall.
- 5. Use Quick sort on left part and then on the right part

1. Pick the pivot.

Assignment Project Exam Help

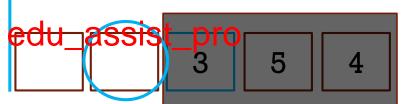
https://eduassistpro.github.io/

- 1. Pick the pivot.
- 2. Set the wall on the left

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assis

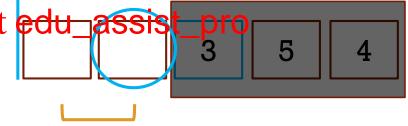


- 1. Pick the pivot.
- 2. Set the wall on the left

- Assignment Project Exam Help
 3. Go through all the elements of the list that are not the pivot https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by dq a We Chat edu_assis place the element just behind the wall.
 - Otherwise, do nothing.

- 1. Pick the pivot.
- 2. Set the wall on the left

- 3. Go through all the elements of the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by down eChat edu_assis place the element just behind the wall.
 - Otherwise, do nothing.



compare: 1<2 true

- 1. Pick the pivot.
- 2. Set the wall on the left

- Assignment Project Exam Help
 3. Go through all the elements of the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by ddan eChat edu_assis place the element just behind the wall.
 - Otherwise, do nothing.

compare: 1<2 true \rightarrow move wall

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by dd WeChat edu_assis place the element just behind the wall.
 - Otherwise, do nothing.

compare:

1<2 true \rightarrow element already in position.

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by 1, and place the element just behind the wall.
 - Otherwise, do nothing.
- 4. Move the pivot next to the wall.
- 5. Use Quick Sort on left part and then on the right part.

- In this case the left part and the right part are base cases.
- The left part has I element ignificantly in the left part ignifica
- The right part is empty → s https://eduassistpro.github.io/

Add WeChat edu_assis pro 5 4

It is left to sort the part of the list to the right of the first pivot.

Assignment Project Exam Help

https://eduassistpro.github.io/ right part

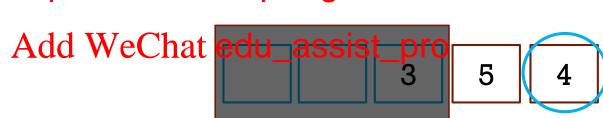
Add WeChat edu_assist_pro

5 4

1. Pick the pivot.

Assignment Project Exam Help

https://eduassistpro.github.io/



- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help

https://eduassistpro.github.io/

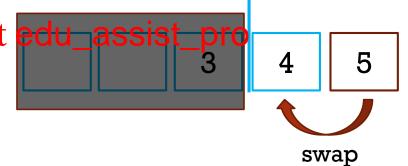


- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the Add WeChat pivot, move the wall right by 1, and place the element just behind the wall.
 - Otherwise, do nothing.



compare: 5 < 4 false \rightarrow do nothing!

- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the WeChat pivot, move the wall right by 1, and place the element just behind the wall.
 - Otherwise, do nothing.
- 4. Move the pivot next to the wall.



- 1. Pick the pivot.
- 2. Set the wall on the left Assignment Project Exam Help
- 3. Go through all the elements the list that are not the pivot. https://eduassistpro.github.io/
 - If the element is smaller than the pivot, move the wall right by 1, and place the element just behind the wall.
 - edu_assist_pro 4 5

- Otherwise, do nothing.
- 4. Move the pivot next to the wall.
- 5. Use Quick Sort on left part and then on the right part.

Once again, both the left part and the right part are base cases.

Assignment Project Exam Help

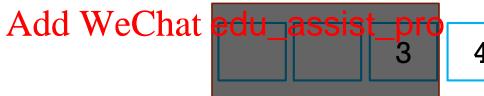
https://eduassistpro.github.io/



- Once again, both the left part and the right part are base cases.
- The array is sorted

Assignment Project Exam Help

https://eduassistpro.github.io/



QUICK SORT EXAMPLE

- Once again, both the left part and the right part are base cases.
- The array is sorted Assignment Project Exam Help
- The original array is sorted

https://eduassistpro.github.io/

Add WeChat edu_assist_pro 3 4 5

QUICK SORT - IMPLEMENTATION

What do we need to implement this algorithm?

- A method that swaps two elements
- A way to refer to parts of green Project Exam Help
- A method that places the https://eduassistpro.gitland moves the elements around so that all the lower elements ar and all the larger elements are on the right. Call it place And Elvide edu_assist_pro
- A method that implements the Quick Sort, that is:
 - Pick a pivot
 - placeAndDivide
 - quickSort left part
 - quickSort right part

PARTS OF THE LIST

What can we use to denote a part of the list?

- We can use the same ideaned Projectna agarte help keep track of the left and right index de ins and ends.
 - Consider for example https://eduassistpro.github.io/
 - The indices 0 and Add Nethertedu_assist_pro
 - The indices 0 and 2 denote the part of the list with the 3 left most elements.
 - The indices 1 and 3 denote the part of the list with the 3 middle elements.

quickSort – PSEUDO CODE

quickSort – PSEUDO CODE

```
quickSort(list, leftIndex, rightIndex) {
   // Base case:
   if (leftIndex Assignment Project Exam Help
      return; // do
   https://eduassistpro.github.io/
      i \(\rightarrow\) placeAndD\(\text{AddeWeCthat edu_assistreme}\) Index)
      // i = index where the pivot is placed
      quickSort(list, leftIndex, i-1)
      quickSort(list, i+1, rightIndex)
```

```
placeAndDivide(list, leftIndex, rightIndex) {
     // pick the right most element
     // place the wallAssignmentProject Exam Help
     wall \leftarrow leftIndex -1
     // go through all elehttps://eduassistpro.github.ie/pivot
      for(int i=leftIndex; i< rigthIndex</pre>
                         Add WeChat edu_assist_pro
```

```
placeAndDivide(list, leftIndex, rightIndex) {
       // pick the right most element
       pivot  \(\begin{align*} list.get(rigthIndex) \end{align*} \)
       // place the wallAssignmentProject Exam Help
       wall \leftarrow leftIndex -1
       // go through all elehttps://eduassistpro.github.ie/pivot
       for(int i=leftIndex; i< rigthIndex</pre>
              if(list.get(i) < pivot WeChat edu_assist_pro</pre>
                     wall++; // move wall
                     swap list.get(i) list.get(wall)// move element behind wall
```

```
placeAndDivide(list, leftIndex, rightIndex) {
       // pick the right most element
       pivot  \(\begin{align*} list.get(rigthIndex) \end{align*} \)
      // place the wallAssignmentProject Exam Help
       wall \leftarrow leftIndex -1
       // go through all elehttps://eduassistpro.github.ie/pivot
       for(int i=leftIndex; i< rigthIndex</pre>
              if(list.get(i) < pivot WeChat edu_assist_pro</pre>
                     wall++; // move wall
                     swap list.get(i) list.get(wall)// move element behind wall
       swap list.get(rigthIndex) list(wall+1) // move pivot next to wall
       return wall+1;
```

MERGESORT VS. QUICKSORT

Mergesort typically uses an extra list. More space can hurt performance for bists Project Exam Help

https://eduassistpro.github.io/

• We will discuss worst case per quicksort later in the course. Add WeChat edu_assist_pro

See stackoverflow if you want opinions on which is better.
The answer is, it depends ...



Assignment Project Exam Help In the next

• Recurre

https://eduassistpro.github.io/

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