

# COMP 250

Assignment Project Exam Help

## INTRODUC TER SCIENCE

<https://eduassistpro.github.io/>

Week 11-1: Ro  
Add WeChat edu\_assist\_pro

Giulia Alberini, Fall 2020

Slides adapted from Michael Langer's

# WHAT ARE WE GOING TO DO IN THIS VIDEO?



- **Rooted Trees**    **Assignment Project Exam Help**

- Terminology

- Implementation

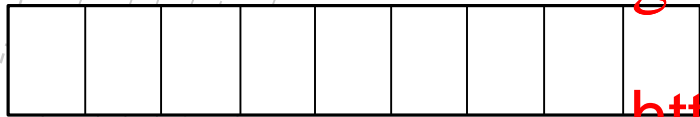
<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

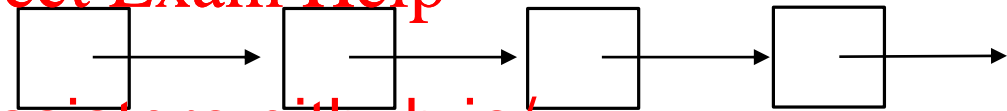
# DATA STRUCTURES

- Linear

array



Linked list

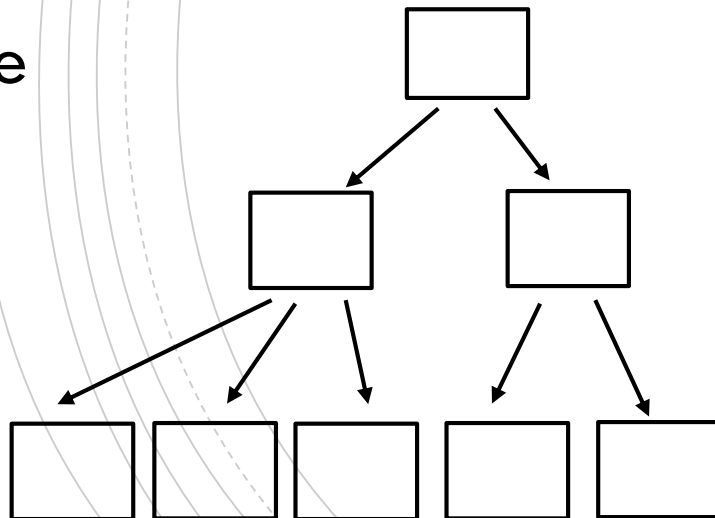


Assignment Project Exam Help

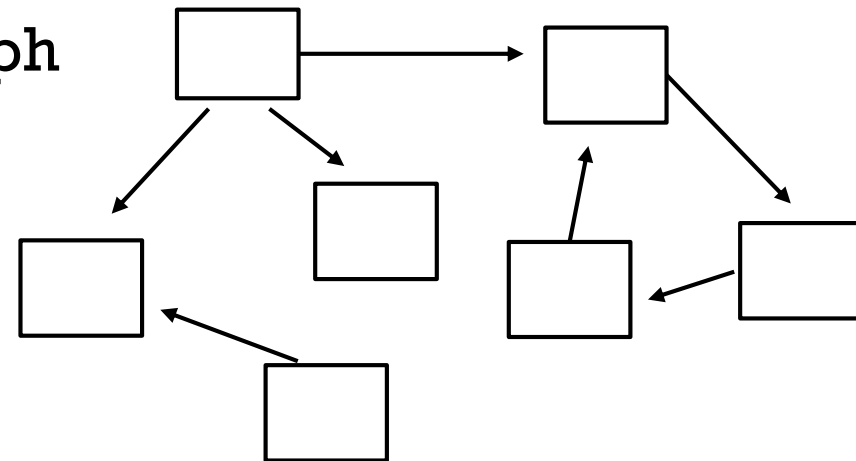
<https://eduassistpro.github.io/>

- Non-linear

tree



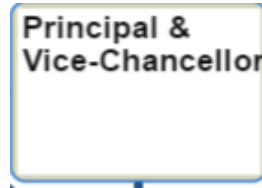
graph



Add WeChat edu\_assist\_pro

## TREE - EXAMPLE

- Organizational Hierarchy  
(McGill)

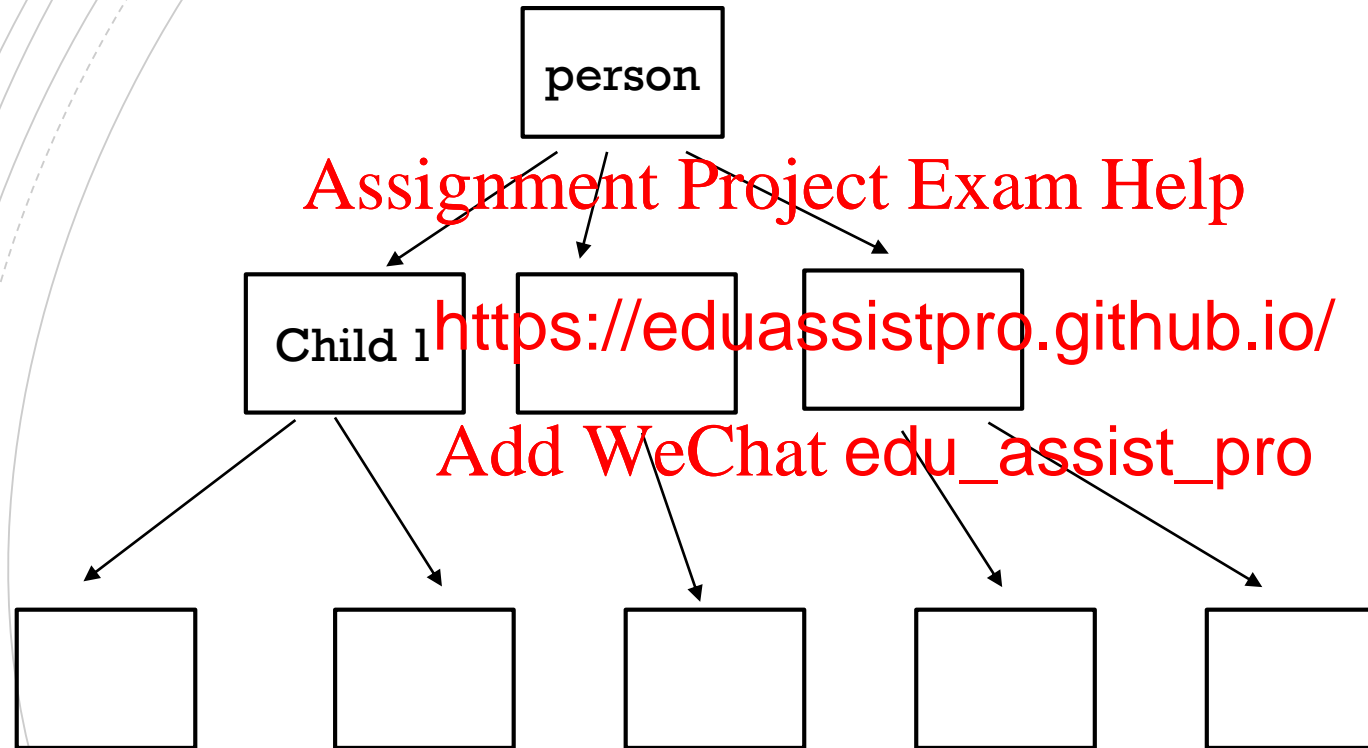


Assignment Project Exam Help

<https://eduassistpro.github.io/>

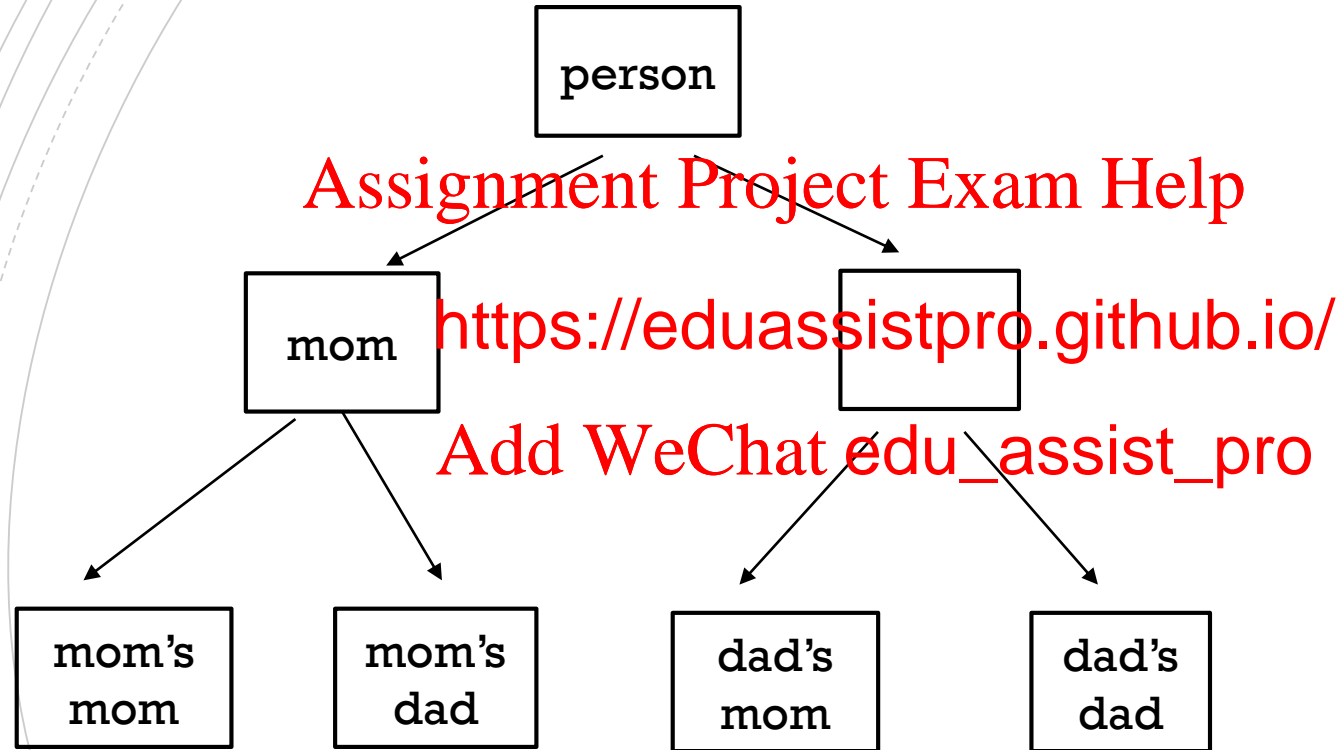
Add WeChat edu\_assist\_pro

## EXAMPLE 2: FAMILY TREE (DESCENDANTS)



Here we ignore spouses (partner).

## EXAMPLE 3: FAMILY TREE (ANCESTORS)



This is an example of a binary tree.

## EXAMPLE 4: UNIX FILE SYSTEM

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

## EXAMPLE 5: JAVA CLASSES E.G. GUI

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat  edu\_assist\_pro

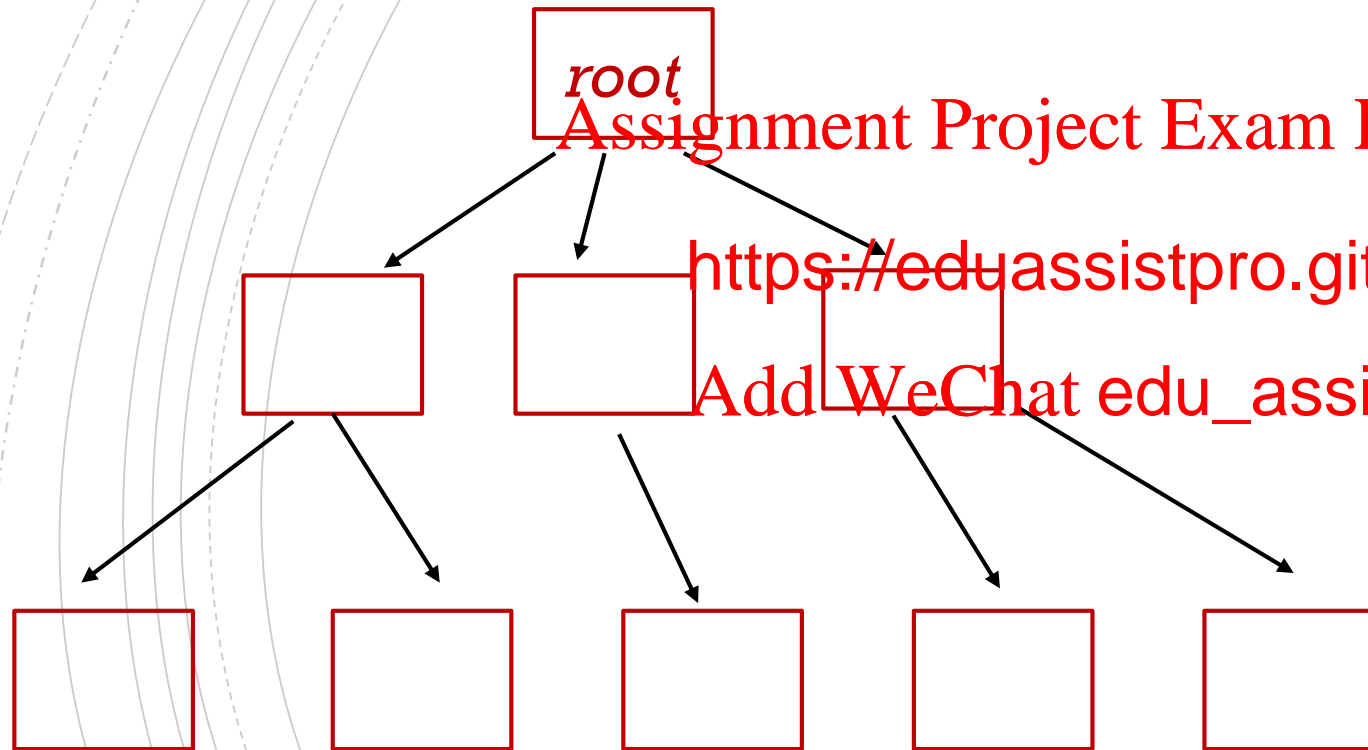


Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

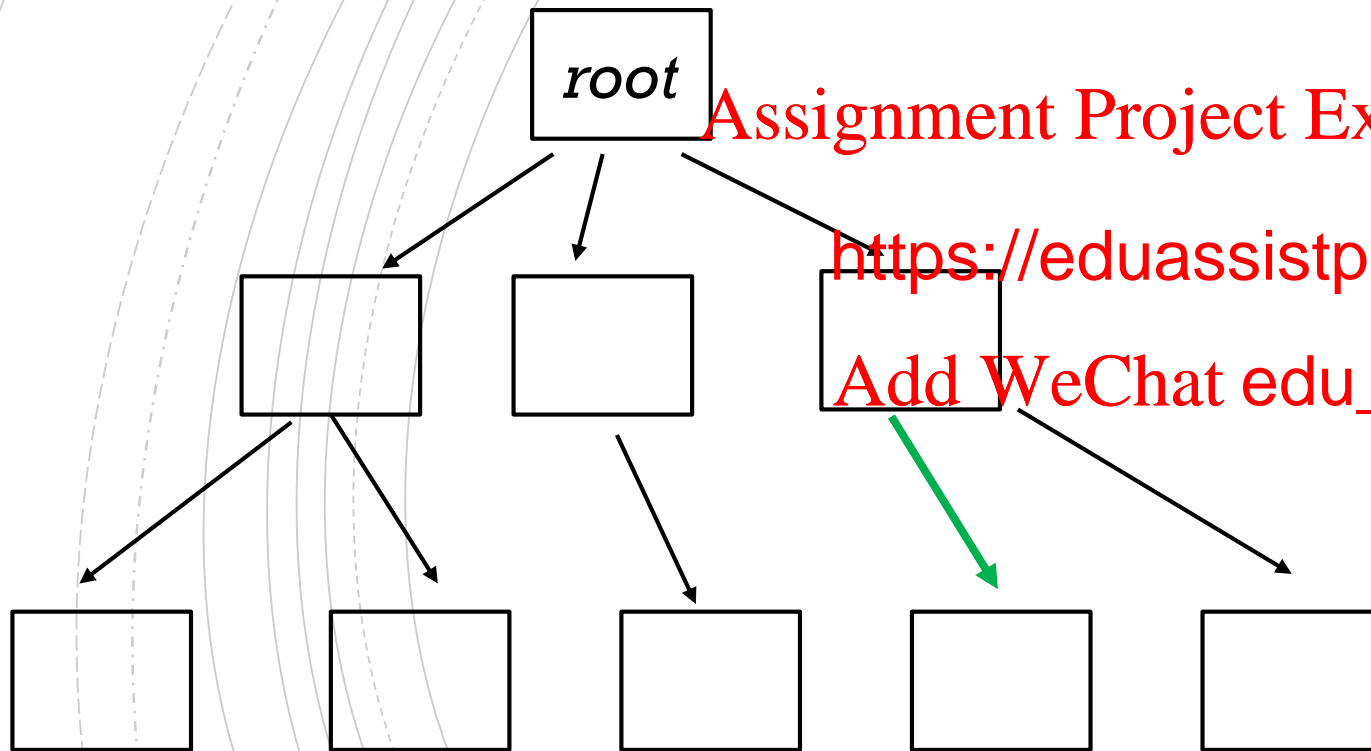
## (ROOTED) TREE TERMINOLOGY



A tree is a collection of nodes (*vertexes*)

The *root* is the top node in a tree

## (ROOTED) TREE TERMINOLOGY



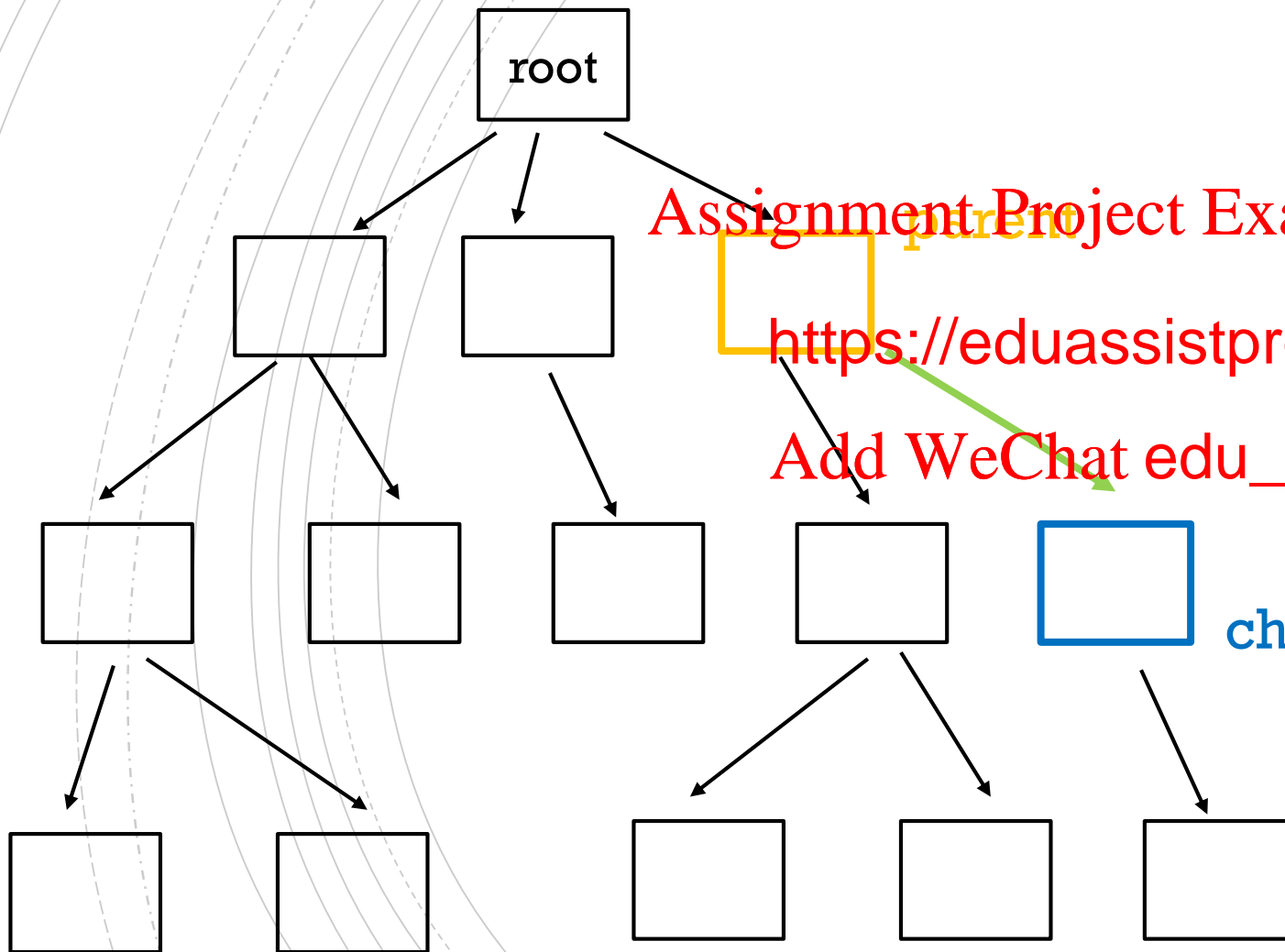
A **directed edge** is ordered pair of nodes  $(v_i, v_j)$  (from, to).

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

Trees can be *undirected* or *directed*. If directed, the edges are either all pointing away from the root or all pointing towards the root.

## (ROOTED) TREE TERMINOLOGY



A *child* is a node directly connected to another node when moving away from the root.

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

A *parent* is a node directly connected to another node when moving towards the root.

*child*

Every node except the root is a *child*, and has exactly one *parent*.

## EDGE DIRECTION

For some trees,

- edges are directed from parent to child
- edges are directed both from child and child to parent.
- edge direction is ignored e.g. common with non-rooted trees (see next slide)

*Most of definitions today will assume edges are from parent to child.*

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

## ASIDE: NON-ROOTED TREES

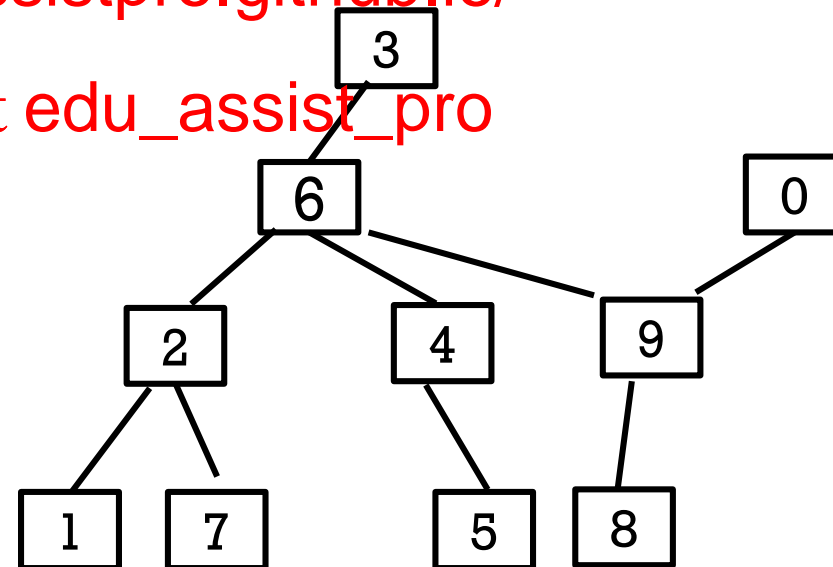
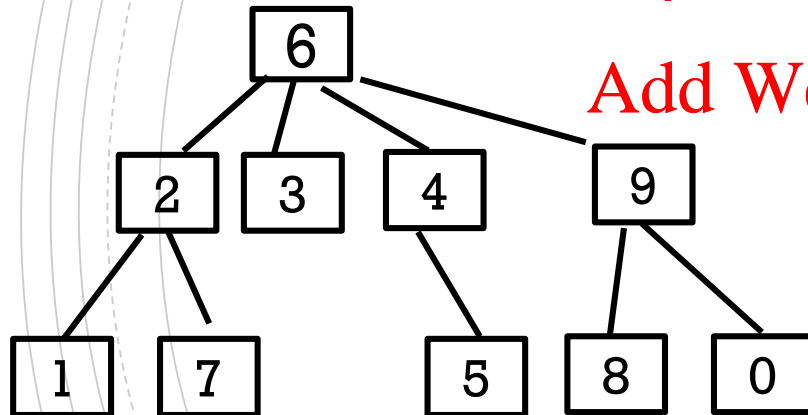
You will see non-rooted trees most commonly when edges are undirected, and there is no natural way to define the 'root'.

You will see examples in COMP 251.

e.g. the tree on the left is only rooted because I drew it that way. It is actually the same (no n the right.

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro



## NUMBER OF EDGES

- Q: If a (rooted) tree has  $n$  nodes, then how many edges does it have?

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

## NUMBER OF EDGES

- Q: If a (rooted) tree has  $n$  nodes, then how many edges does it have?

Assignment Project Exam Help

- A:  $n - 1$

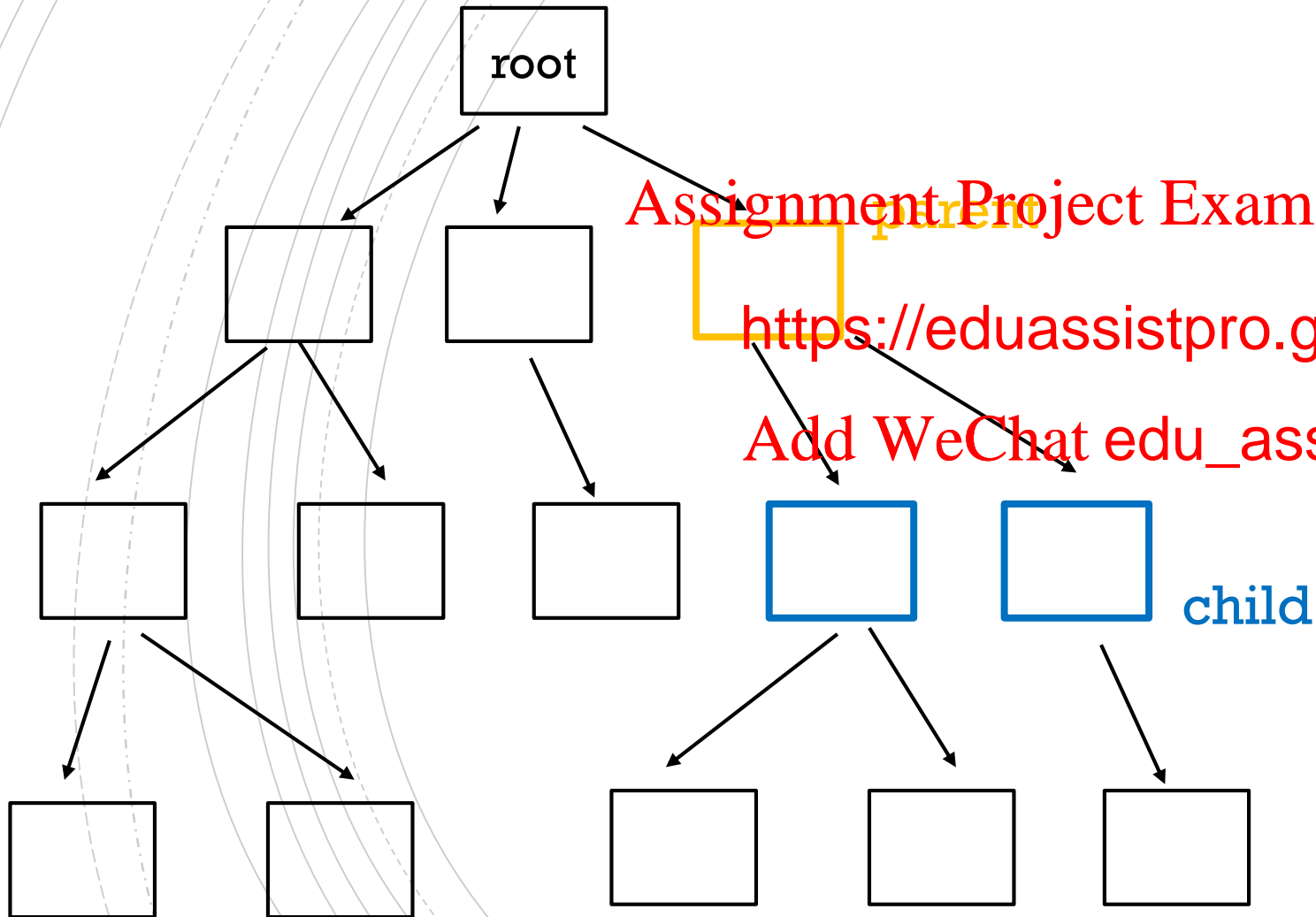
<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

Since every edge is of the form (parent, child) and each node except the root is a child and each child has exactly one parent.



## (ROOTED) TREE TERMINOLOGY



Assignment Project Exam Help

nodes are said to be **siblings**

<https://eduassistpro.github.io/> if they have the same **parent**.

Add WeChat edu\_assist\_pro

**child**

## RECURSIVE DEFINITION OF ROOTED TREE

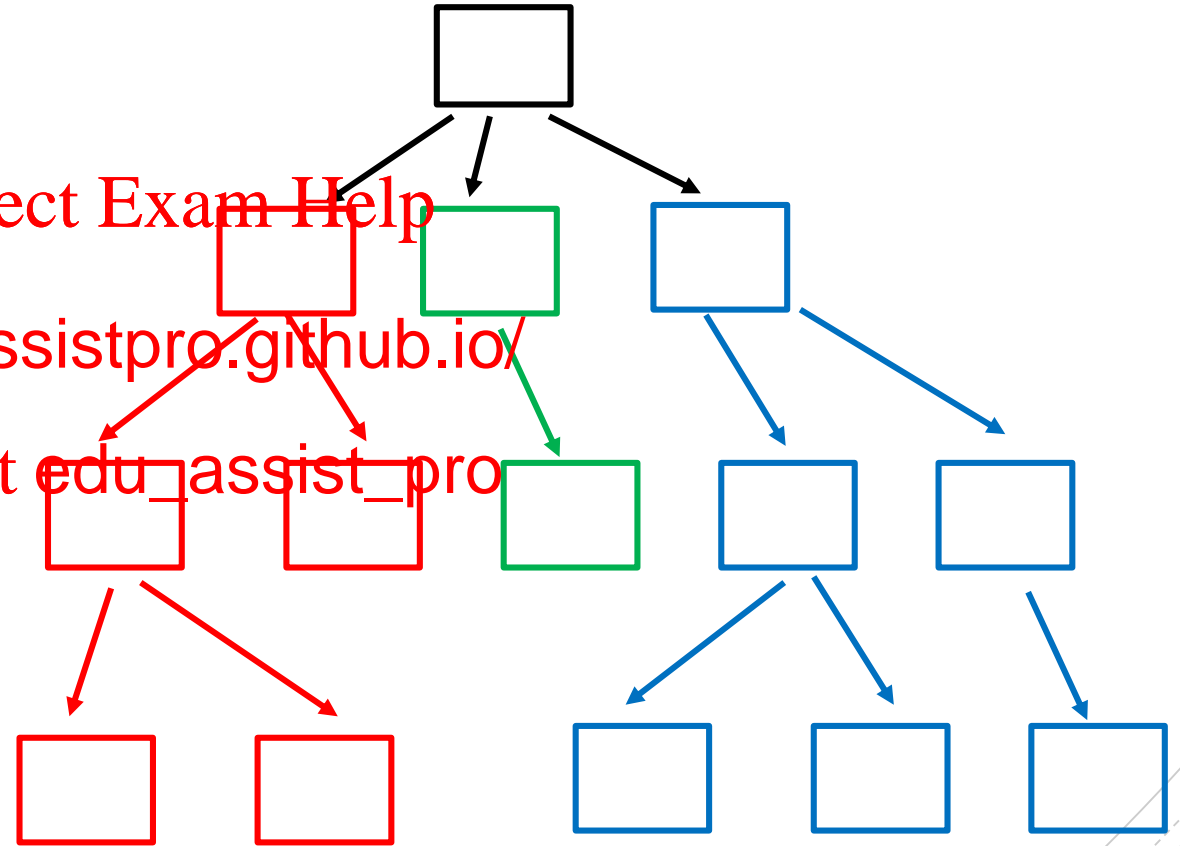
A tree  $T$  is a finite (& possibly empty) set of  $n$  nodes such that:

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

?



## RECURSIVE DEFINITION OF ROOTED TREE

A tree  $T$  is a finite (& possibly empty) set of  $n$  nodes such that:

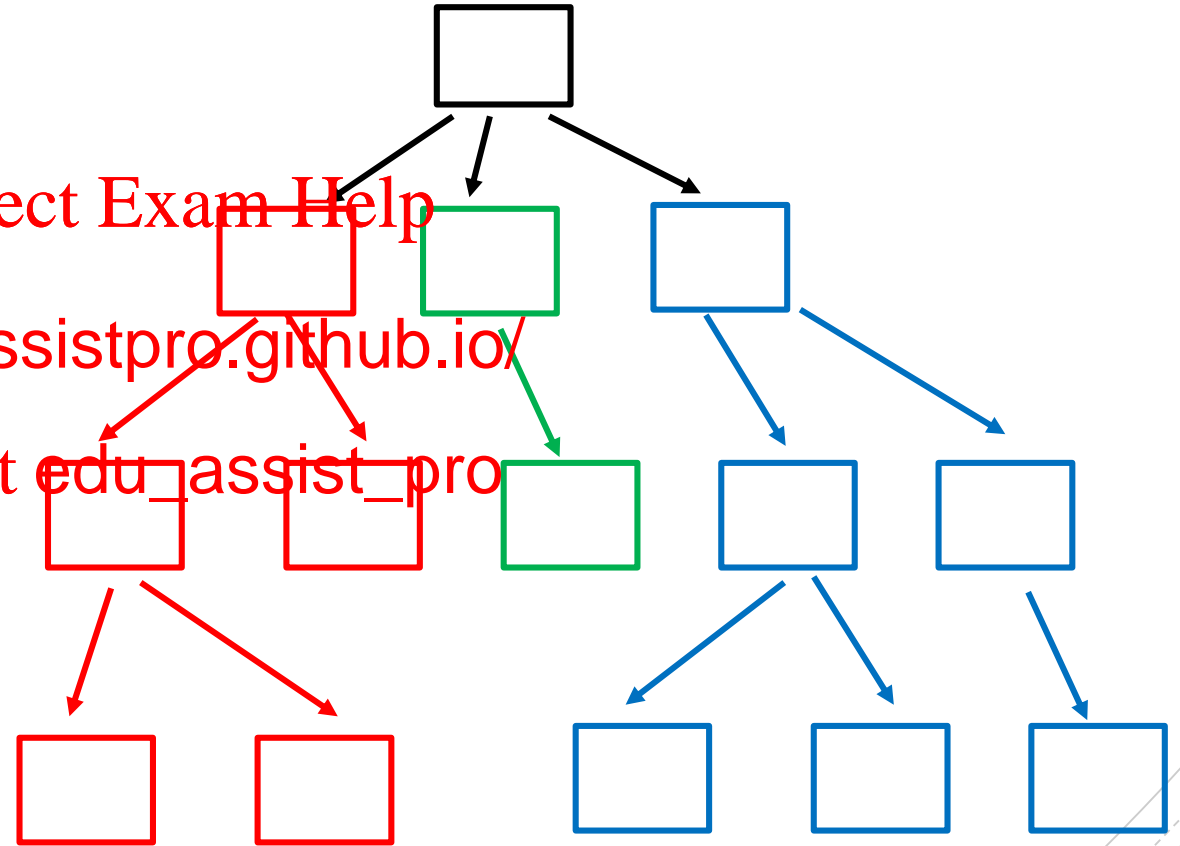
- if  $n > 0$  then one of the node

?

Assignment Project Exam Help

<https://eduassistpro.github.io/>

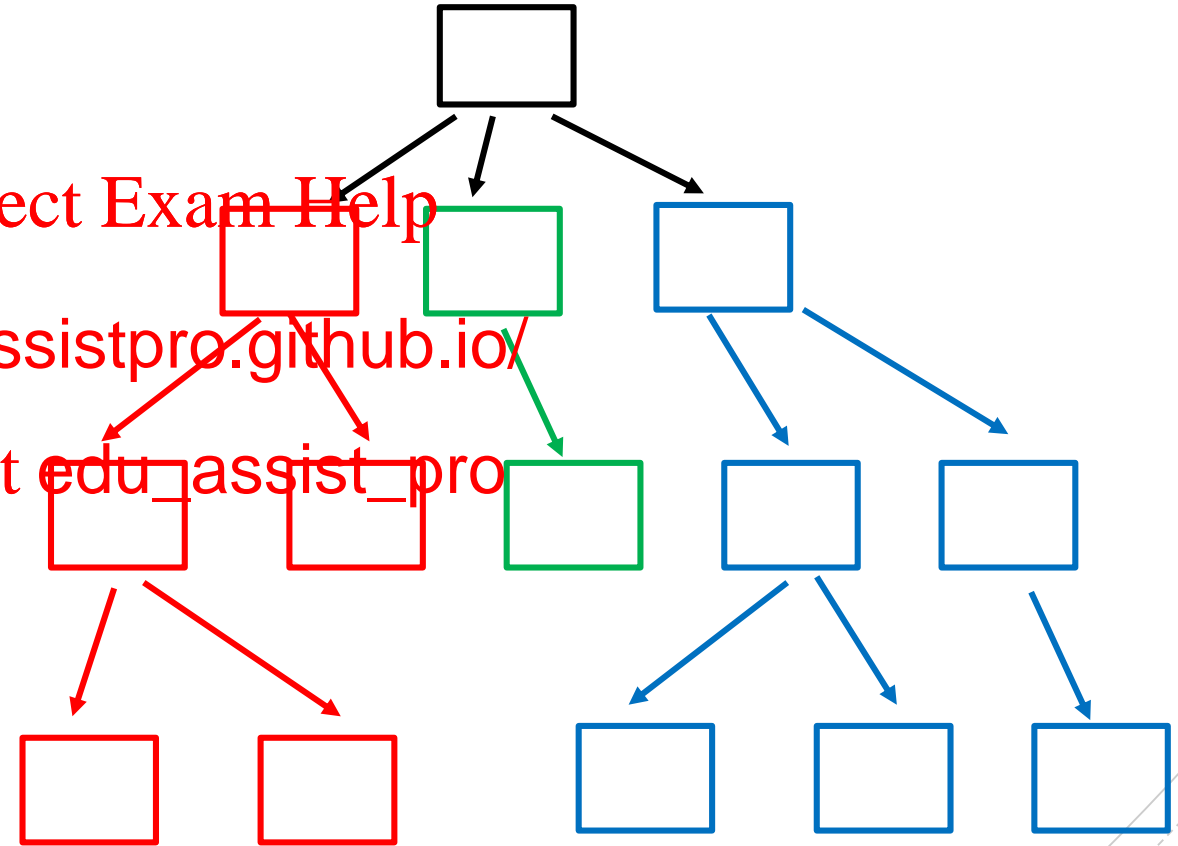
Add WeChat edu\_assist\_pro



## RECURSIVE DEFINITION OF ROOTED TREE

A tree  $T$  is a finite (& possibly empty) set of  $n$  nodes such that:

- if  $n > 0$  then one of the node
- if  $n > 1$  then the  $n - 1$  non-root nodes are partitioned into (non-empty) subsets  $T_1, T_2, \dots, T_k$ , each of which is a tree (called a “subtree”), and the roots of the subtrees are the children of root  $r$ .



Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

## ANOTHER DEFINITION

A recursive definition for tree can also be given using lists as follows:

**Assignment Project Exam Help**  
<https://eduassistpro.github.io/>  
**Add WeChat edu\_assist\_pro**

```
tree      =  (root tOfSubTrees )  
listOfSubTrees = tree | tOfSubTrees
```

**Note** that `listOfSubTrees` cannot be empty.

## TRY IT!

A recursive definition for tree can also be given using lists as follows:

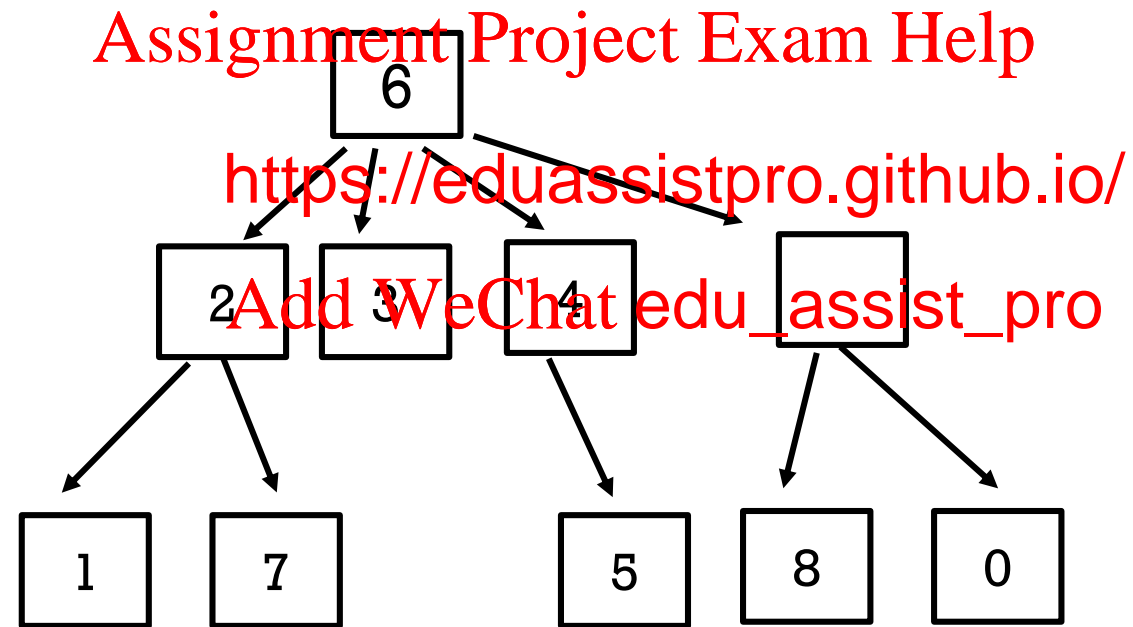
**Assignment Project Exam Help**  
`tree = (root tOfSubTrees )`  
`listOfSubTrees = tree | listOfSubTrees`  
**<https://eduassistpro.github.io/>**  
**Add WeChat edu\_assist\_pro**

- Draw the tree that corresponds to the following list, where the root elements are single digits.

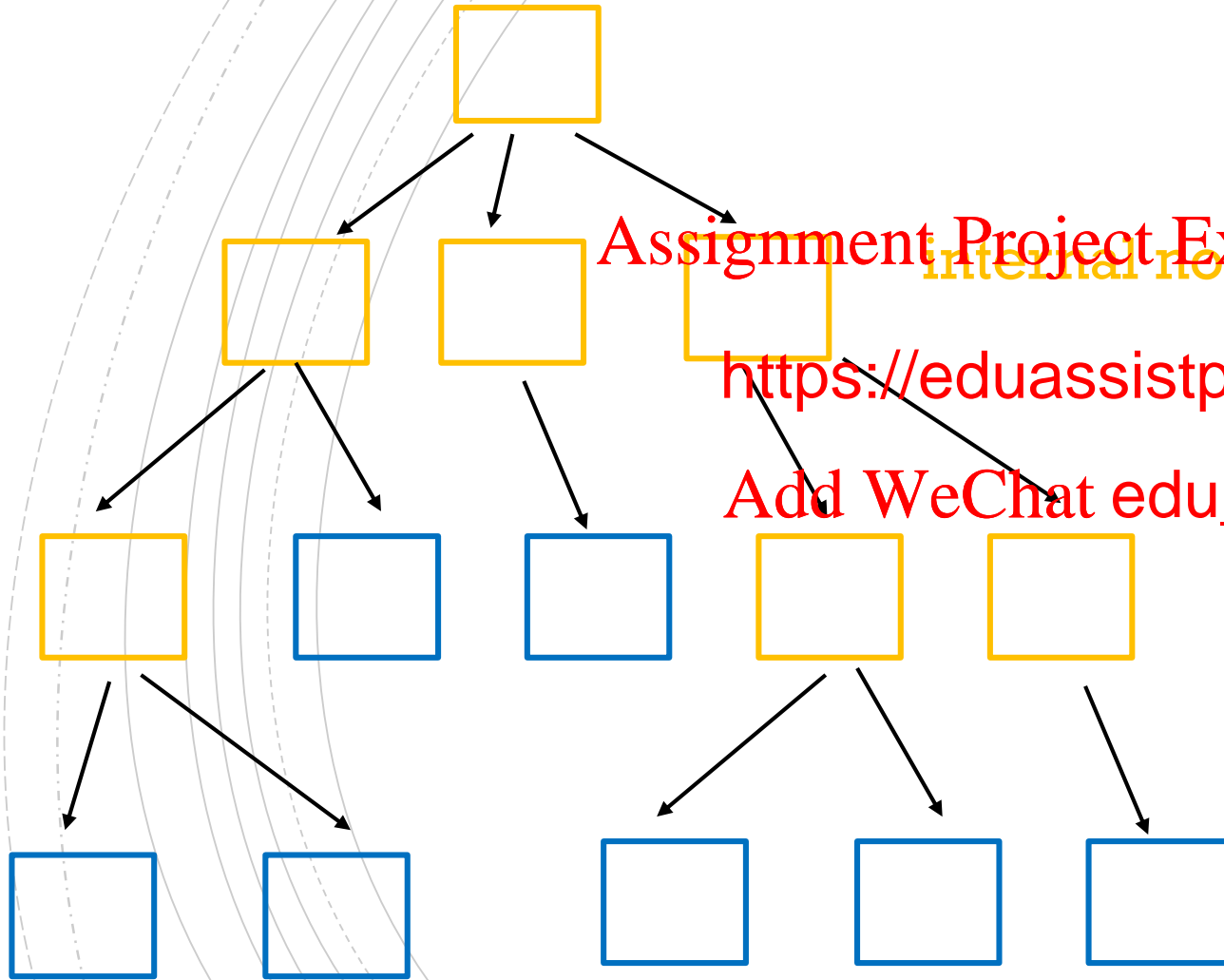
`( 6 ( 2 1 7 ) 3 ( 4 5 ) ( 9 8 0 ) )`

## SOLUTION

$(6 \ (2 \ 1 \ 7) \ 3 \ (4 \ 5) \ (9 \ 8 \ 0))$  represents the following tree:



# (ROOTED) TREE TERMINOLOGY



An *internal node* is a node with at least one child.

# Assignment Project Exam Help

# Project Exam

directories)

~~<https://eduassistpro.github.io/>~~

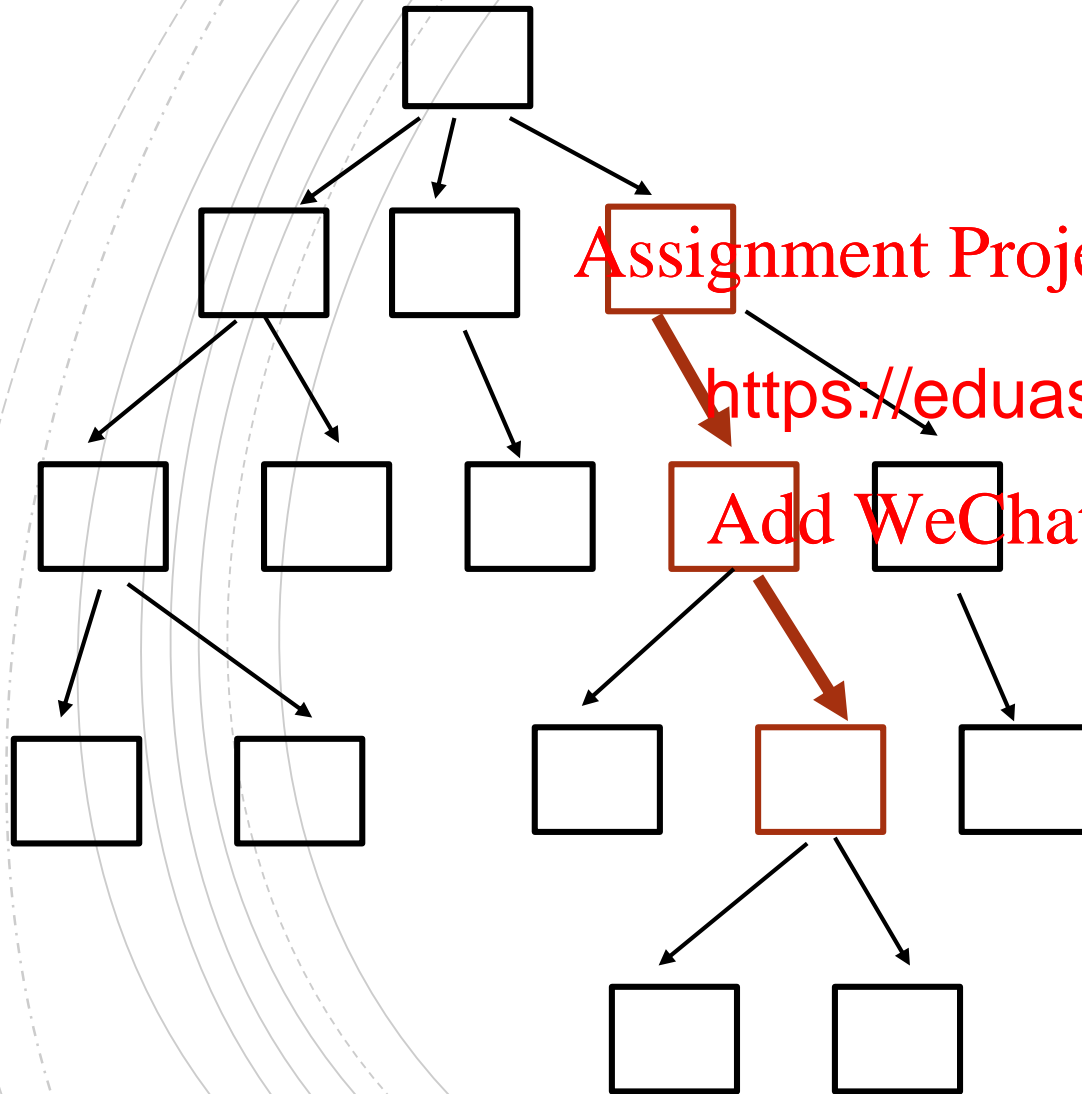
# Add WeChat edu\_assist\_pro

An *leaf (or external node)* is a node with no children.

leaves (external nodes)  
(e.g. files or empty directories)



# TREE TERMINOLOGY



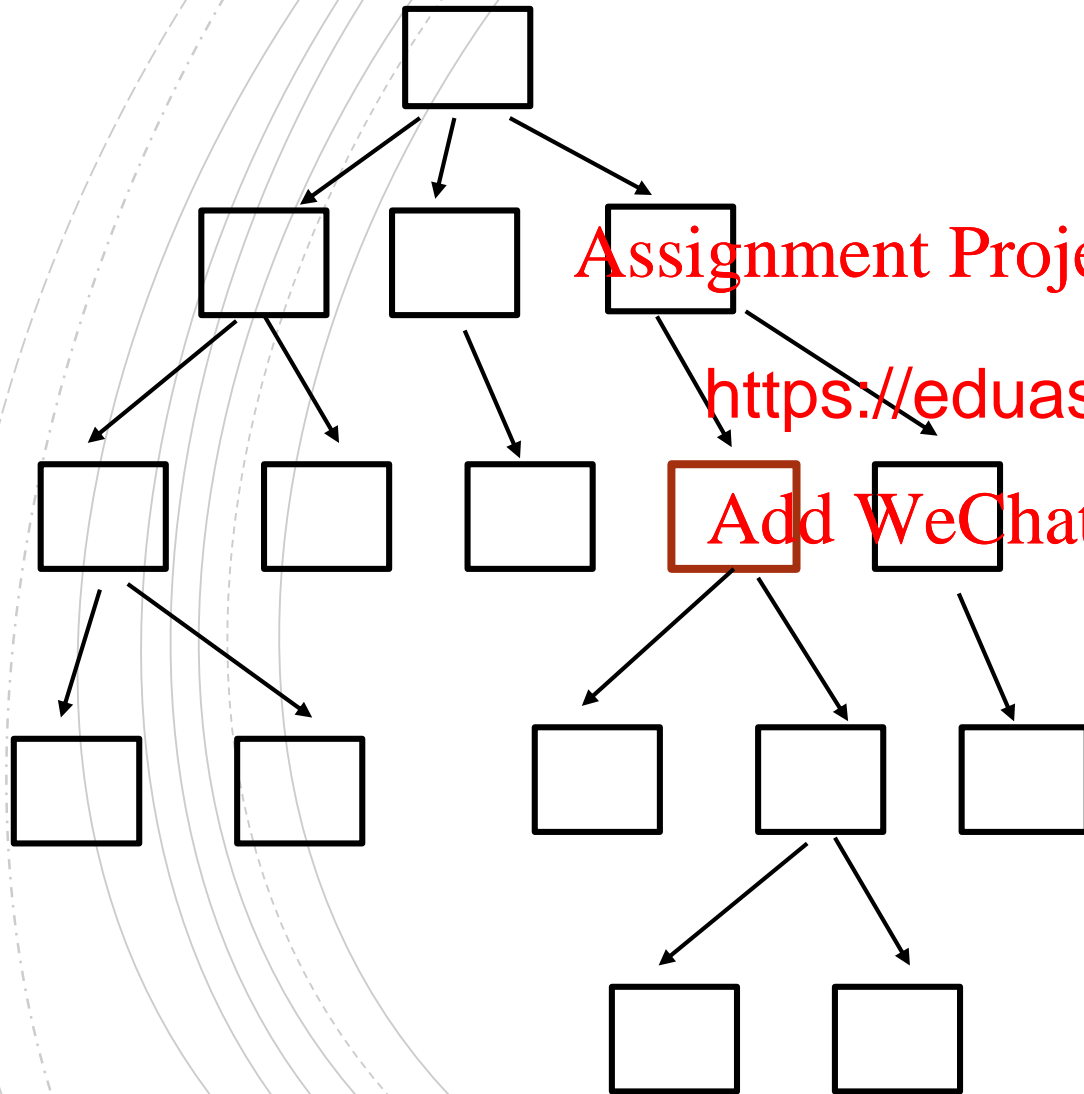
A **path** in a tree is a sequence of nodes  $(v_1, v_2, \dots, v_k)$  such that  $(v_i, v_{i+1})$  is an edge.

<https://eduassistpro.github.io/>

# Add WeChat edu\_assist\_pro

*length* of a path is *the number of edges in the path*  
(number of nodes in the path – 1)

# TREE TERMINOLOGY

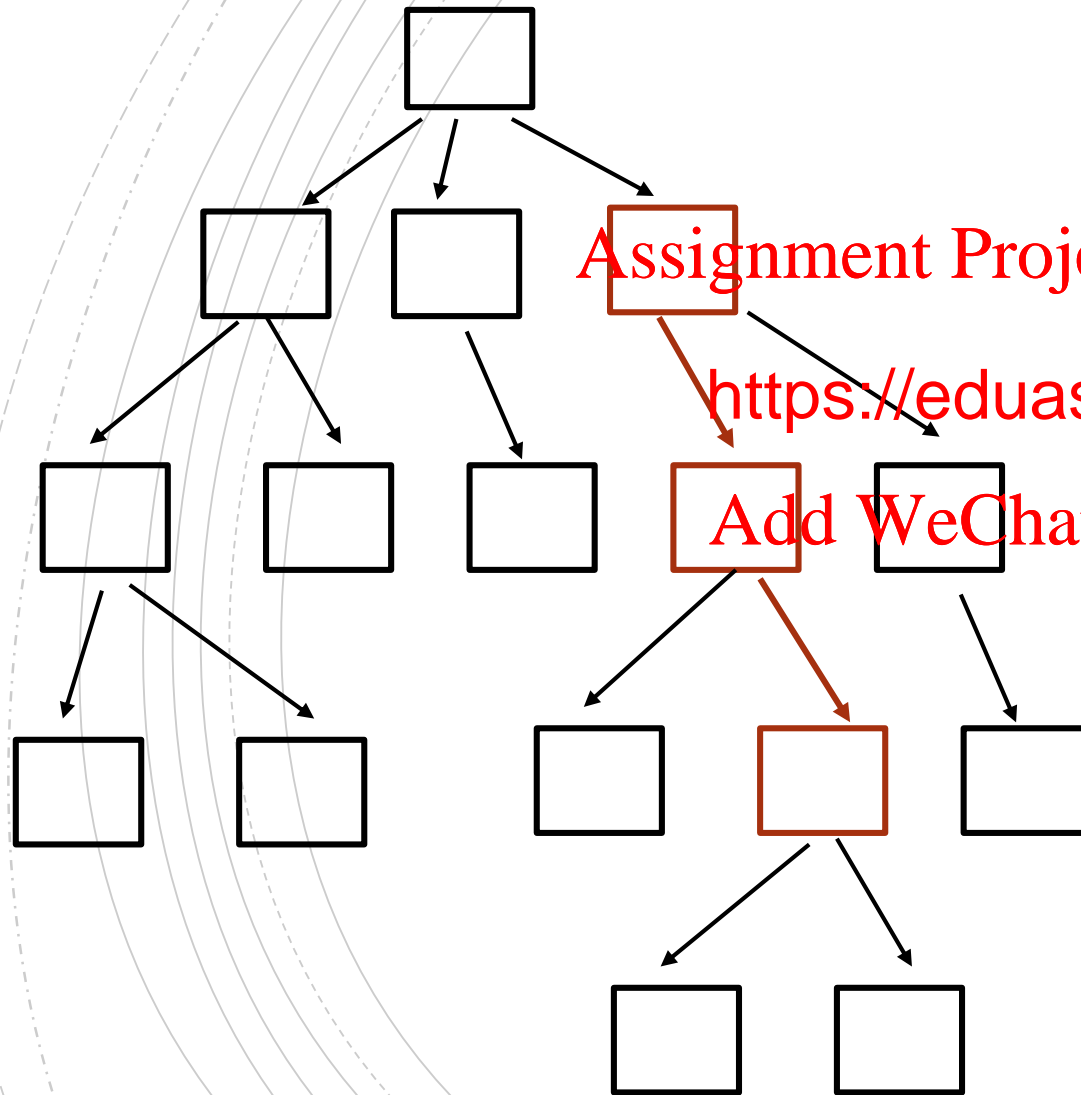


# Assignment Project Exam Help

path with just one node ( $v_1$ )  
length = 0, since it has no

Add WeChat edu\_assist\_pro

## QUICK QUESTION



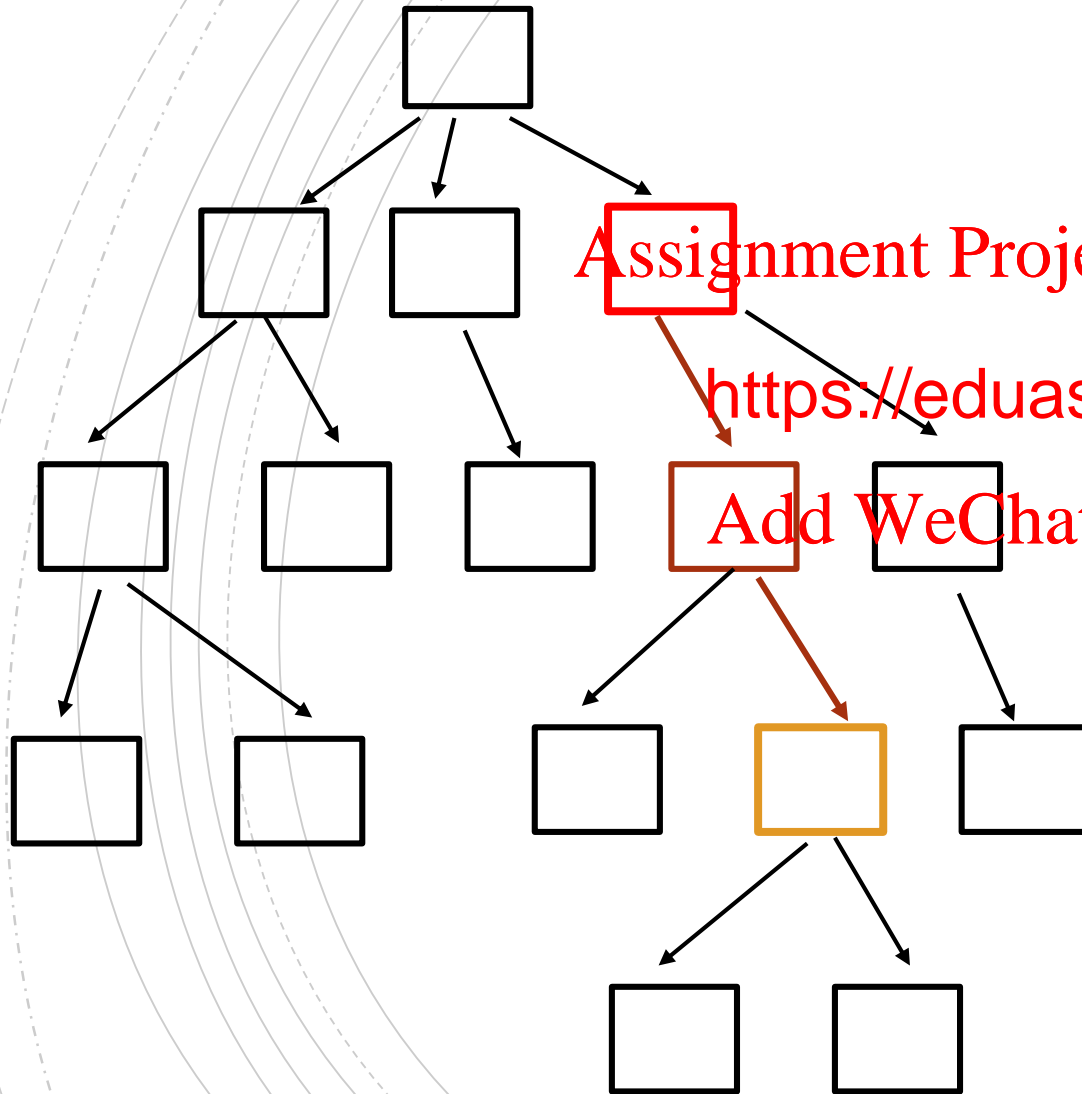
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

What is the path length?

# TREE TERMINOLOGY



# Assignment Project Exam Help

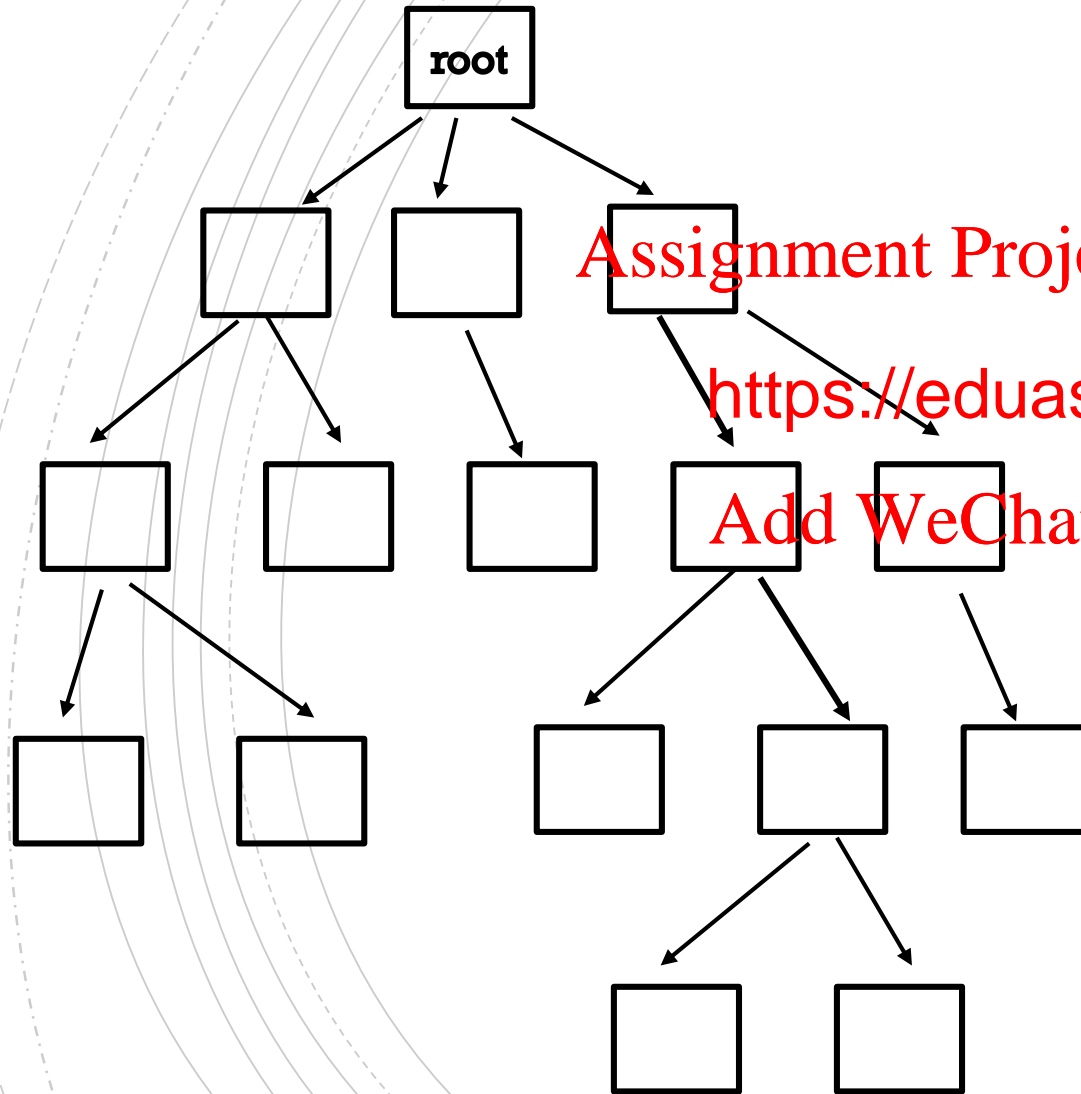
<https://eduassistpro.github.io/>

# Add WeChat edu\_assist\_ch

node  $v$  is an *ancestor* of node  $w$  if and only if there is a path from  $v$  to  $w$ .  
In each case, we also say that  $w$  is a *descendant* of node  $v$ .

## (ROOTED) TREE TERMINOLOGY

depth (level)  
0



Assignment Project Exam Help

<https://eduassistpro.github.io/>

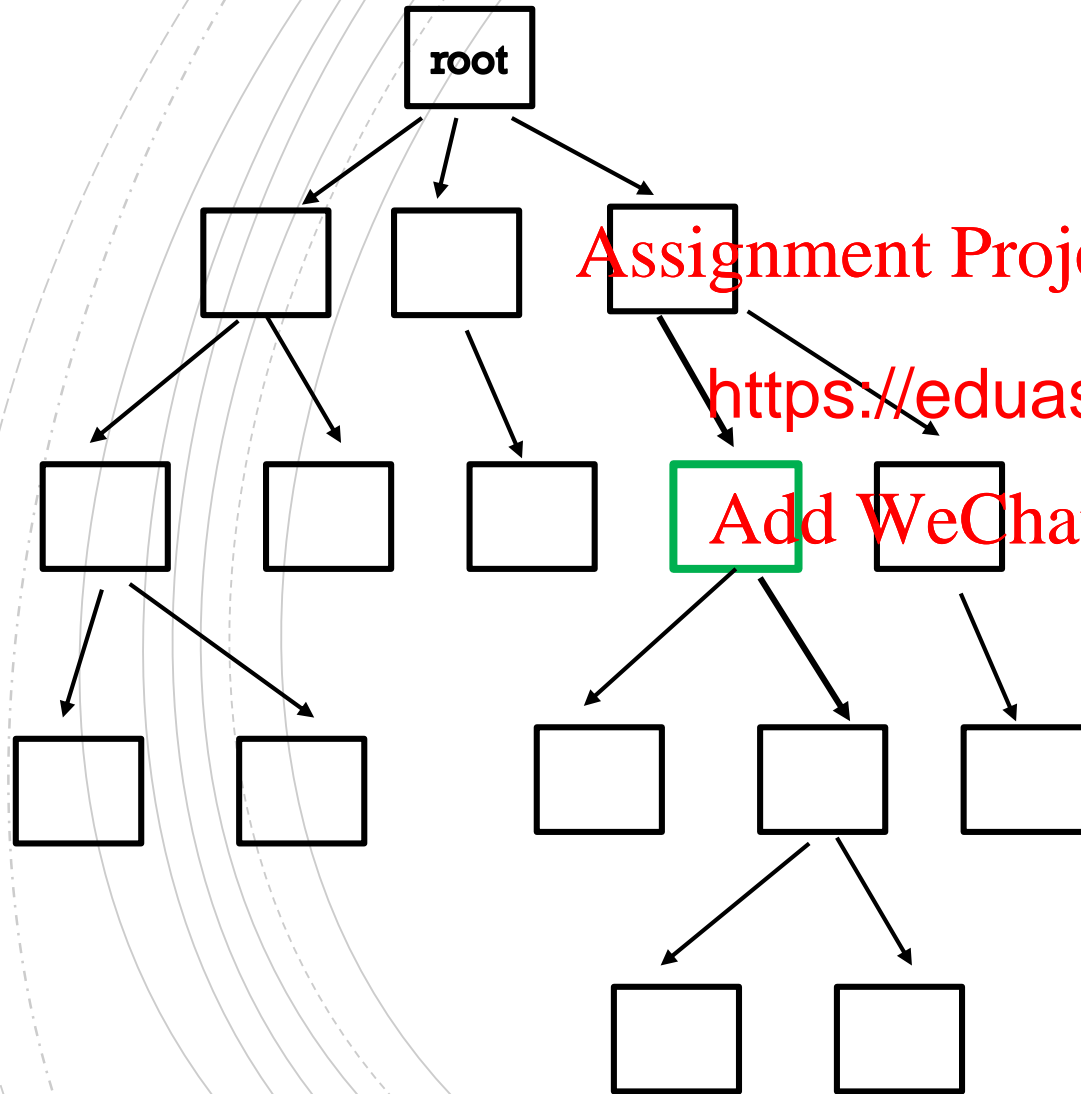
Add WeChat edu\_assist\_pro

The *depth* (or *level*) of a node is the length of the path *from the root to the node*.

3

4

## (ROOTED) TREE TERMINOLOGY



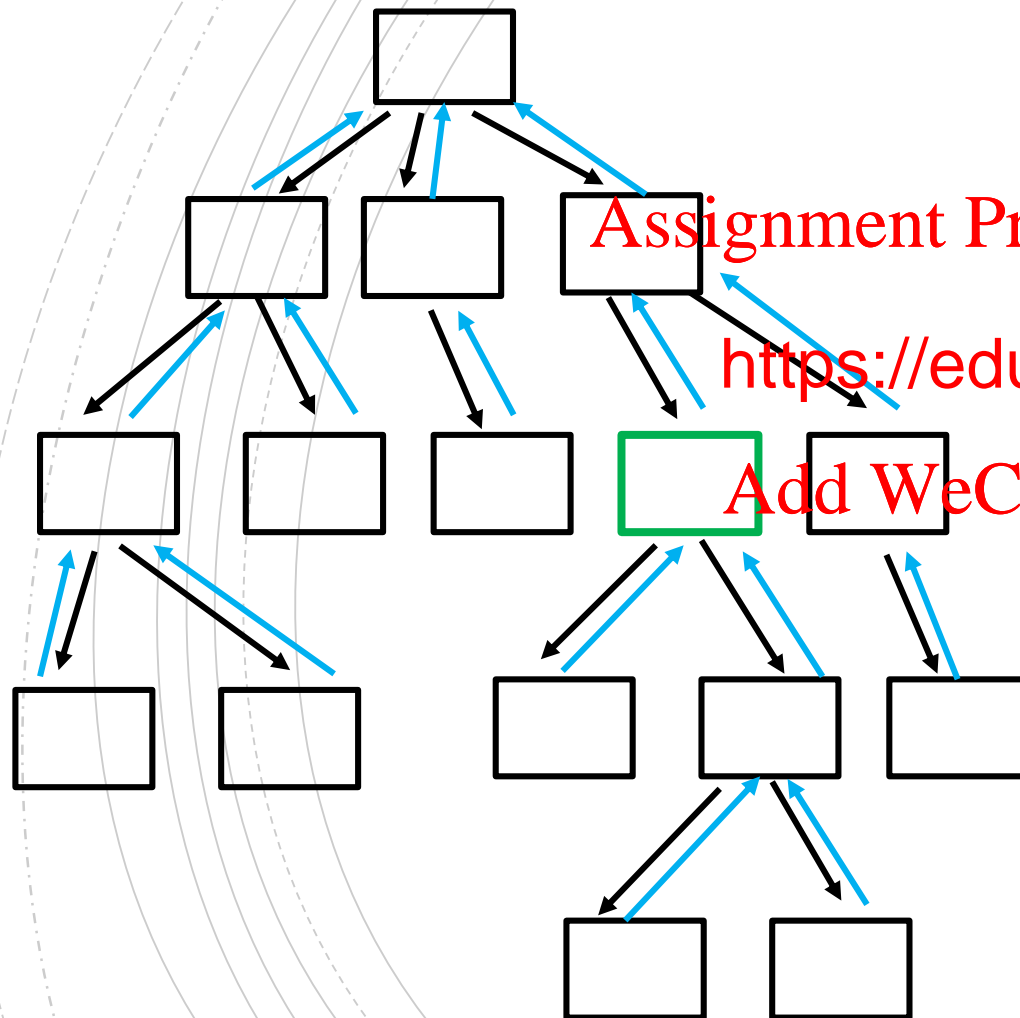
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assistpro

How can we compute  
the depth of a node **v**?

depth(v)



To do this efficiently we require nodes to have a **parent link**. This is analogous to a 'prev' link in a doubly linked list.

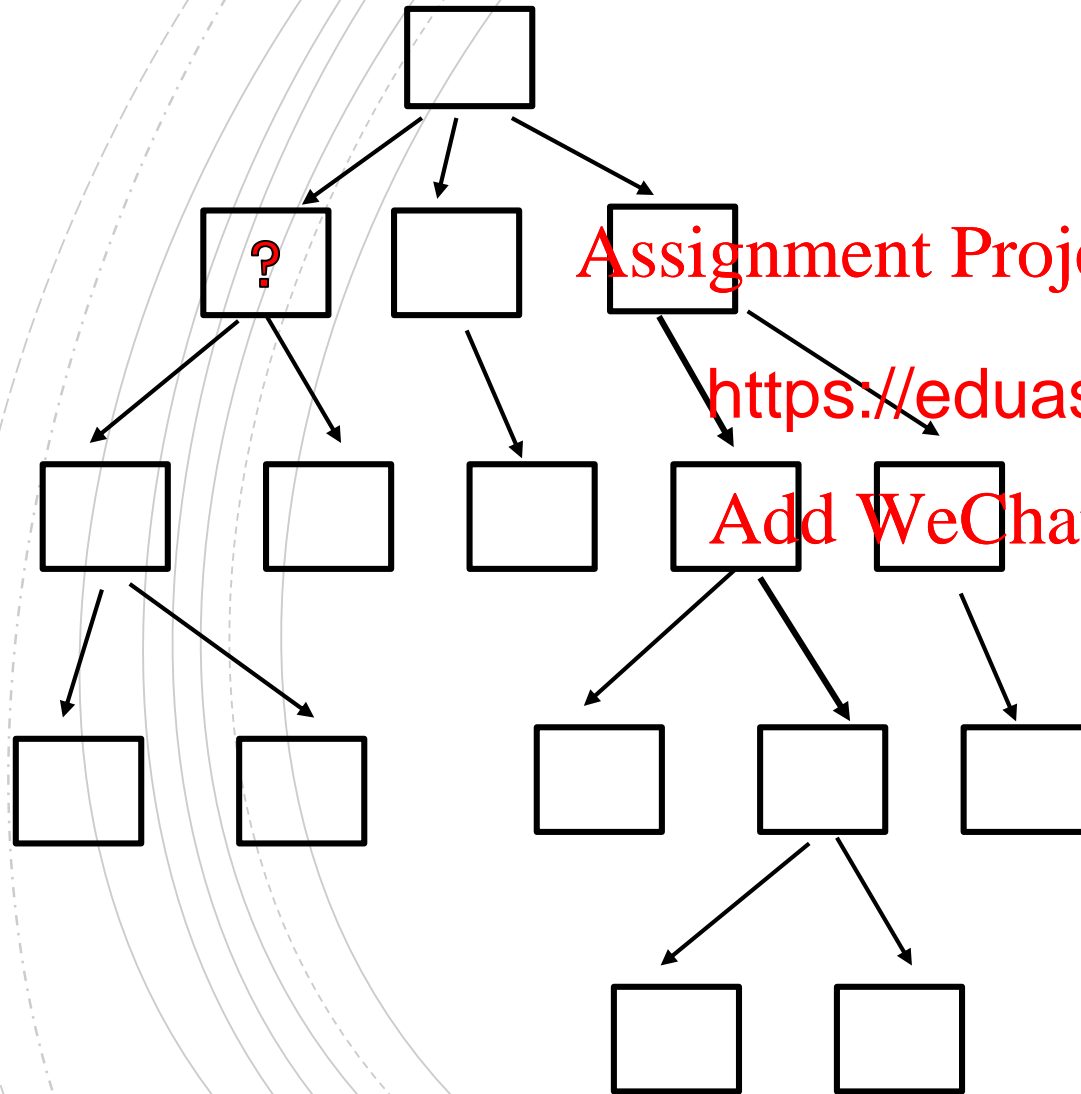
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

```
} {  
    if (v.parent == null) //root  
        return 0  
    else  
        return 1 + depth(v.parent)  
}
```

## (ROOTED) TREE TERMINOLOGY



Assignment Project Exam Help

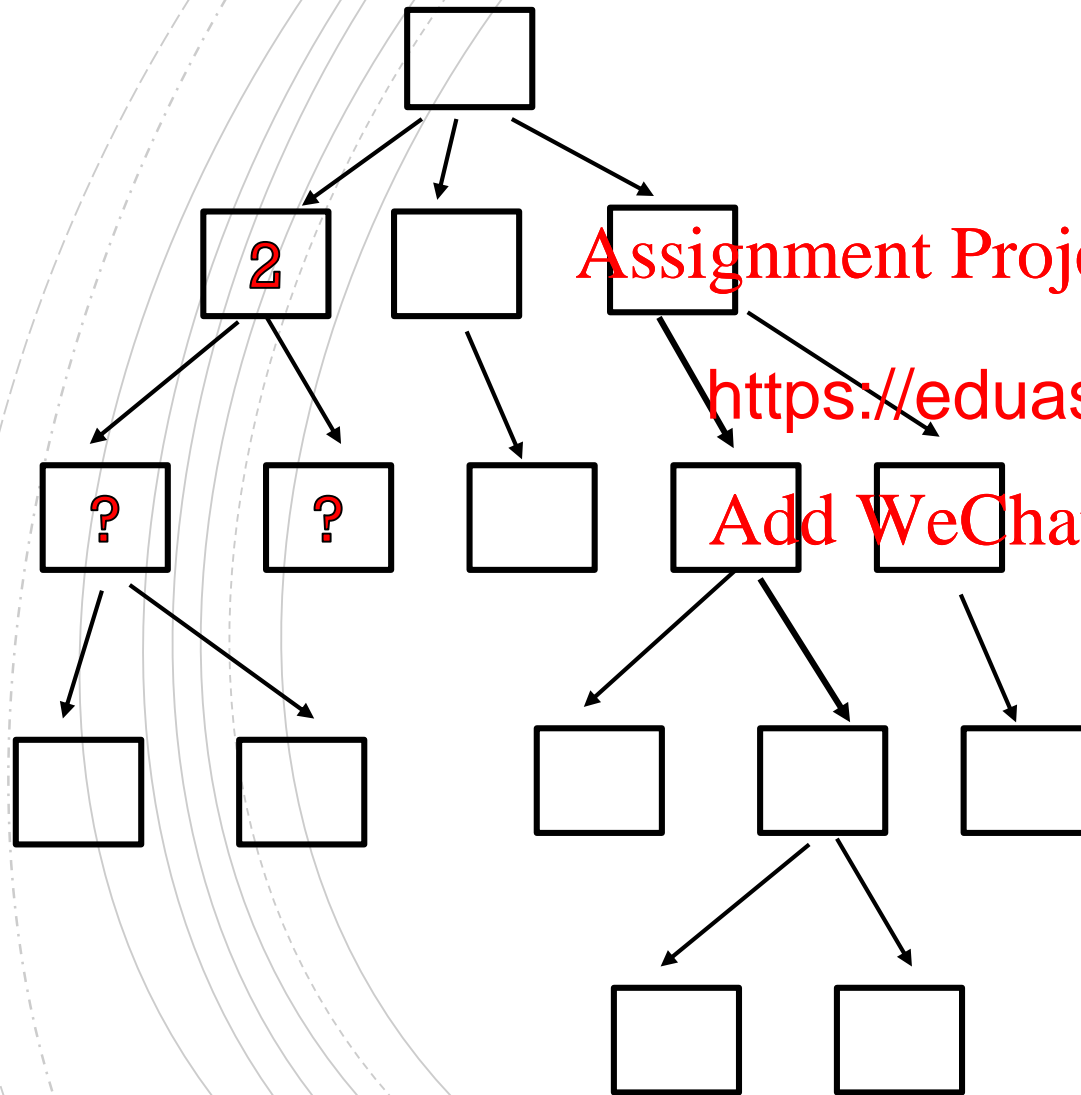
<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

The *height* of a node is the minimum length of a path from that node to a leaf.



# TREE TERMINOLOGY



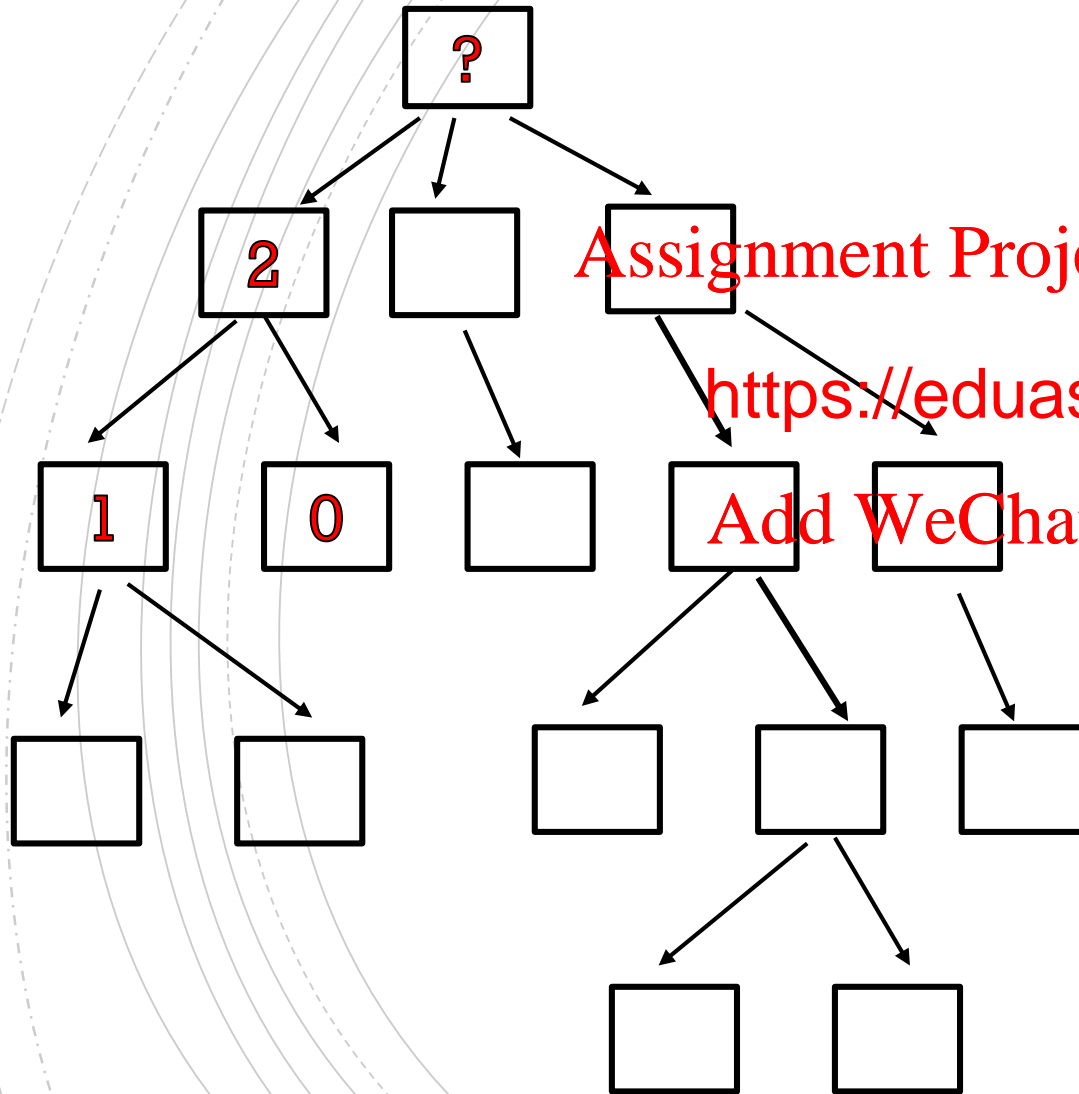
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

The *height* of a node is the minimum length of a path from that node to a leaf.

# TREE TERMINOLOGY



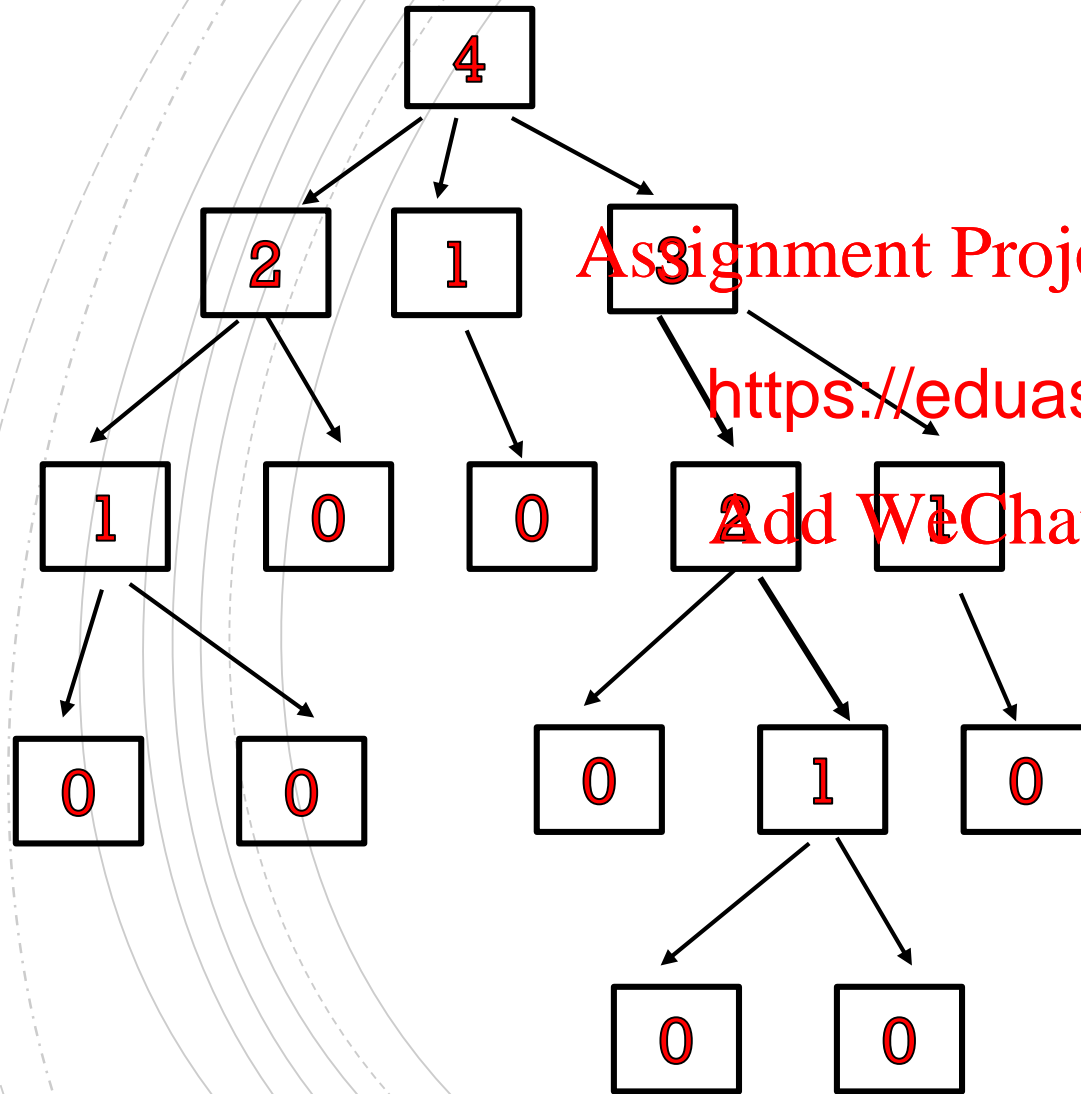
# Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

The *height* of a node is the maximum length of a path that node to a leaf.

# TREE TERMINOLOGY



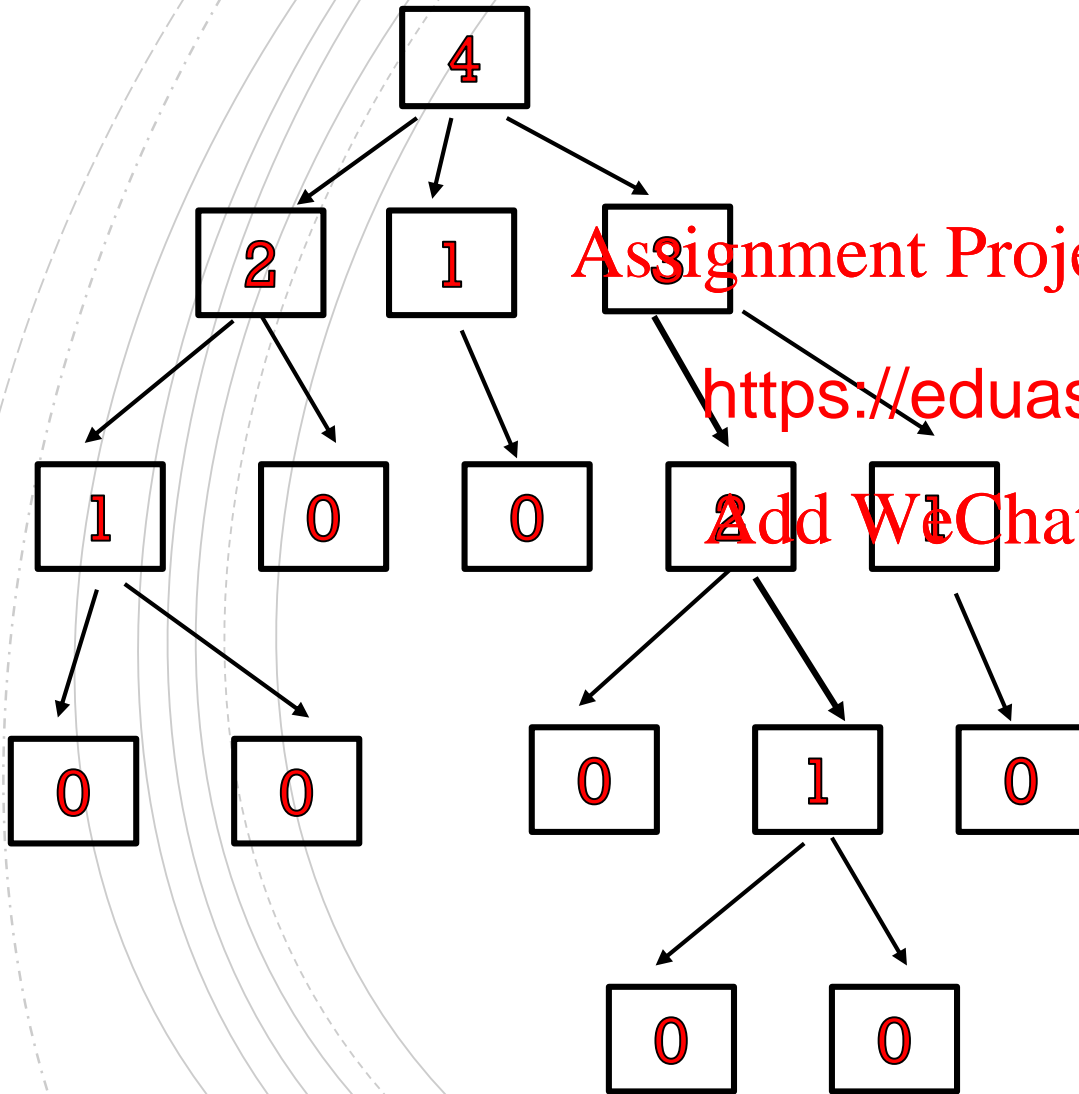
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

we can we compute the  
ht of a node v?

## height(v)



# Assignment Project Exam Help

<https://eduassistpro.github.io/>

## 2 Add WeChat edu\_assist\_pro

```
height(v) {
    if (v is a leaf)
        return 0
    h = 0
    for each child w of v
        h = max(h, height(w))
    return 1 + h
}
```

Assignment Project Exam Help

IM

ONS

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

## HOW TO IMPLEMENT A TREE IN JAVA?

Same idea as with linked lists:

- Create a data type to represent tree nodes.
- Represent a tree with a pointer to the root node.

# Assignment Project Exam Help

<https://eduassistpro.github.io/>

## Add WeChat edu\_assist\_pro

class TreeNode<T> {

//eduassistpro.github.io

WeChat edu\_assist\_pro

}

# HOW TO IMPLEMENT A TREE IN JAVA?

Same idea as with linked lists:

- Create a data type to represent tree nodes.
- Represent a tree with a pointer to the root node.

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

```
class TreeNode<T> {  
    All TreeNode<T>> children;  
  
    TreeNode<T> parent; // optional  
  
}
```

# HOW TO IMPLEMENT A TREE IN JAVA?

Same idea as with linked lists:

- Create a data type to represent tree nodes.
- Represent a tree with a pointer to the root node.

Assignment Project Exam Help

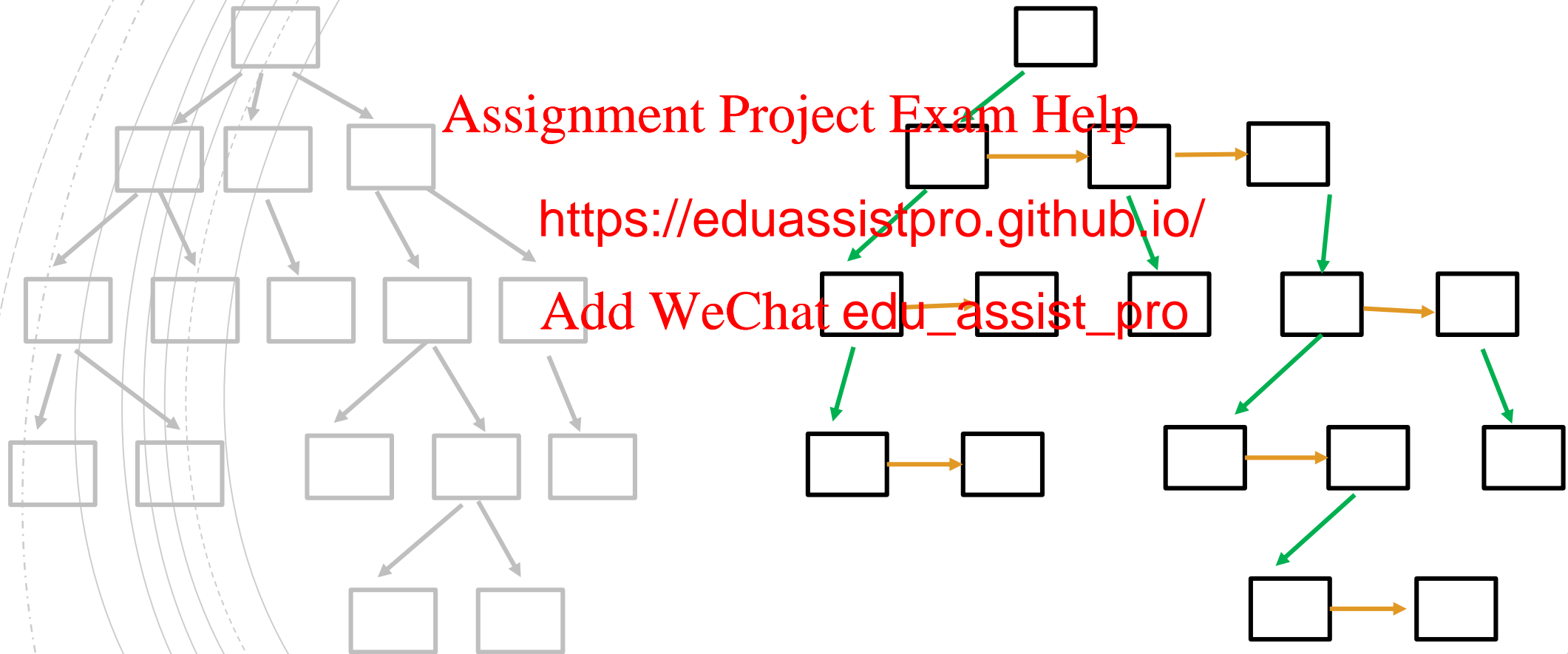
<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

```
class Tree<T>{  
    T root;  
  
    class TreeNode<T>{  
        T  
        ArrayList<TreeNode<T>> children;  
        TreeNode<T> parent; // optional  
    }  
}
```



## ANOTHER COMMON IMPLEMENTATION: 'first child, next sibling'

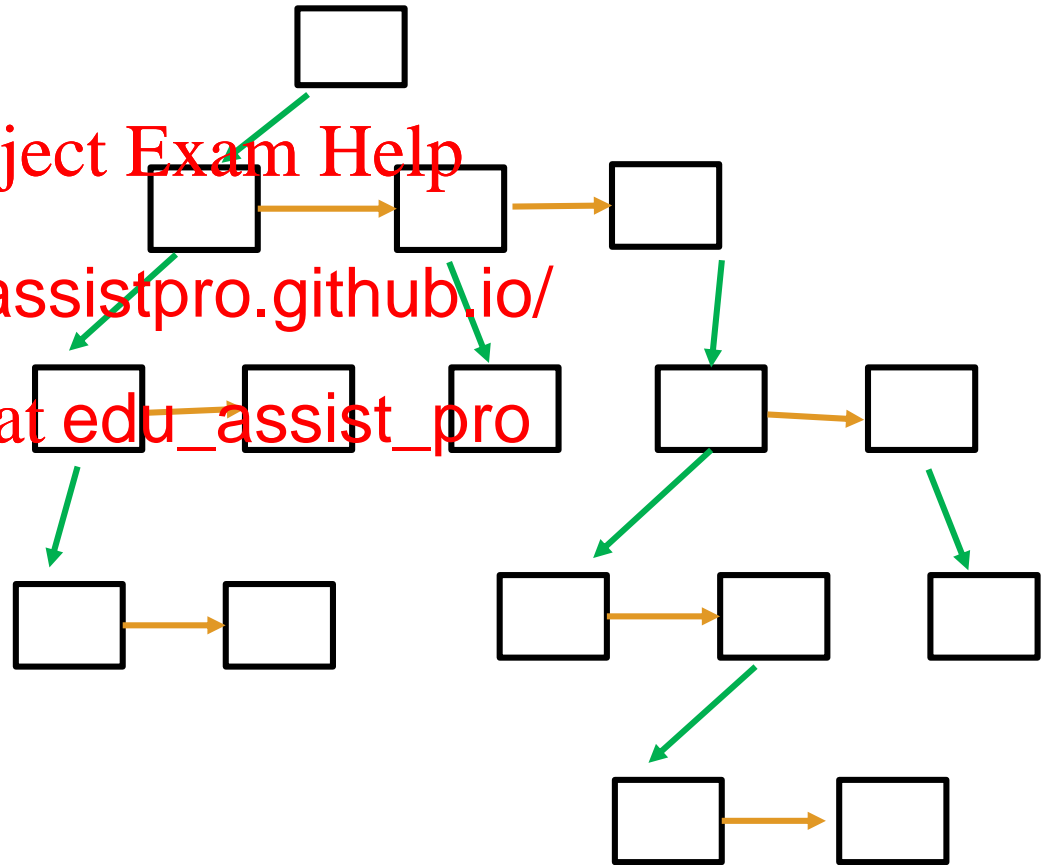


(similar to singly linked lists)

# Assignment Project Exam Help

~~<https://eduassistpro.github.io/>~~

Add WeChat edu\_assist\_pro

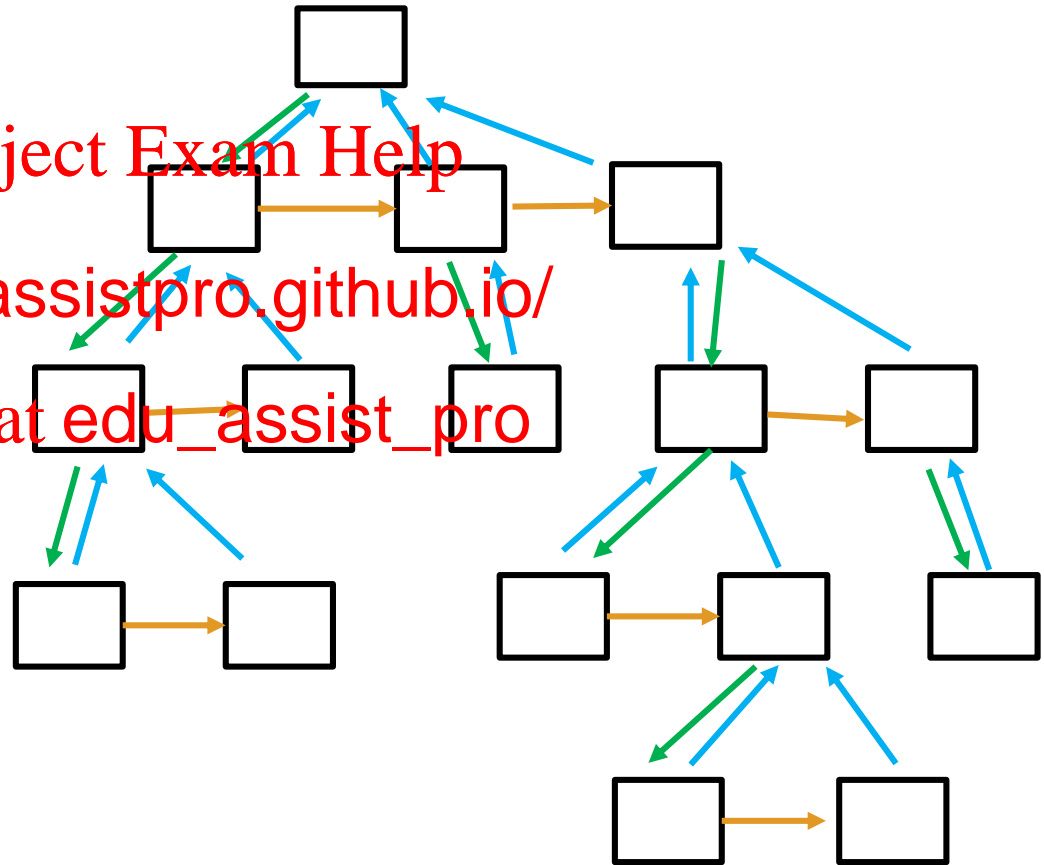


(similar to singly linked lists)

# Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

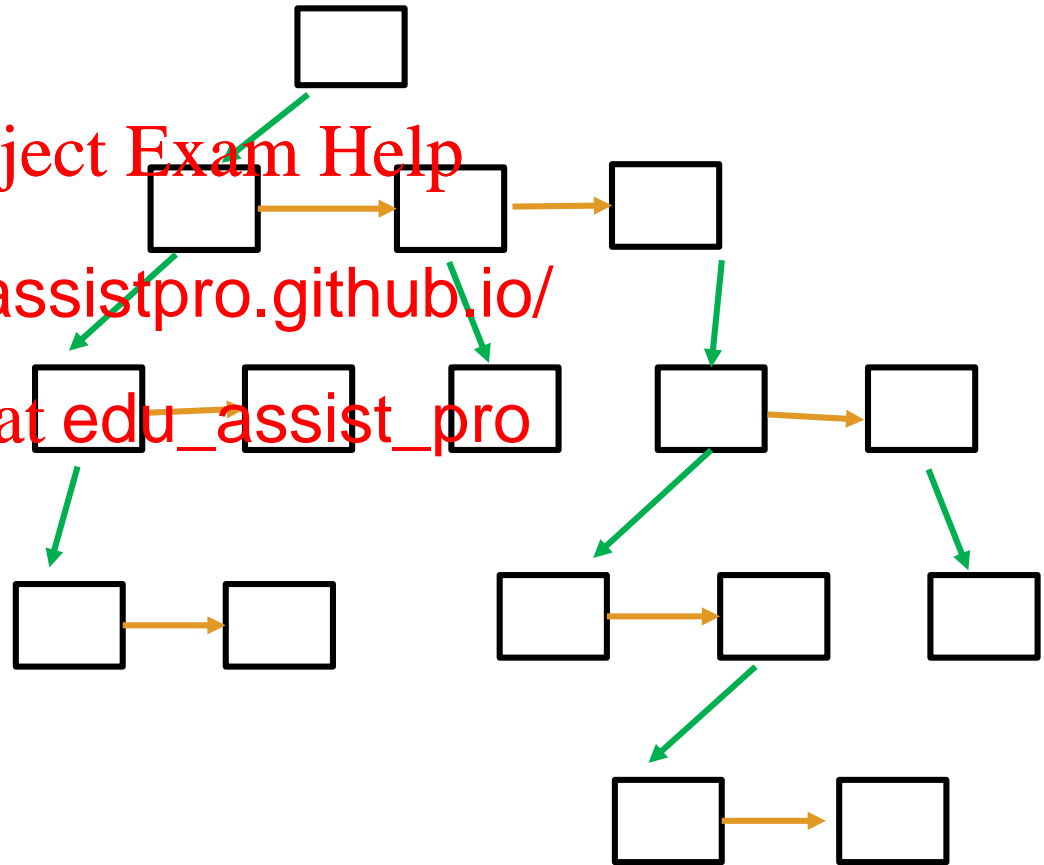


(NOT ILLUSTRATED ON THE RIGHT)

# Assignment Project Exam Help

~~<https://eduassistpro.github.io/>~~

Add WeChat edu\_assist\_pro



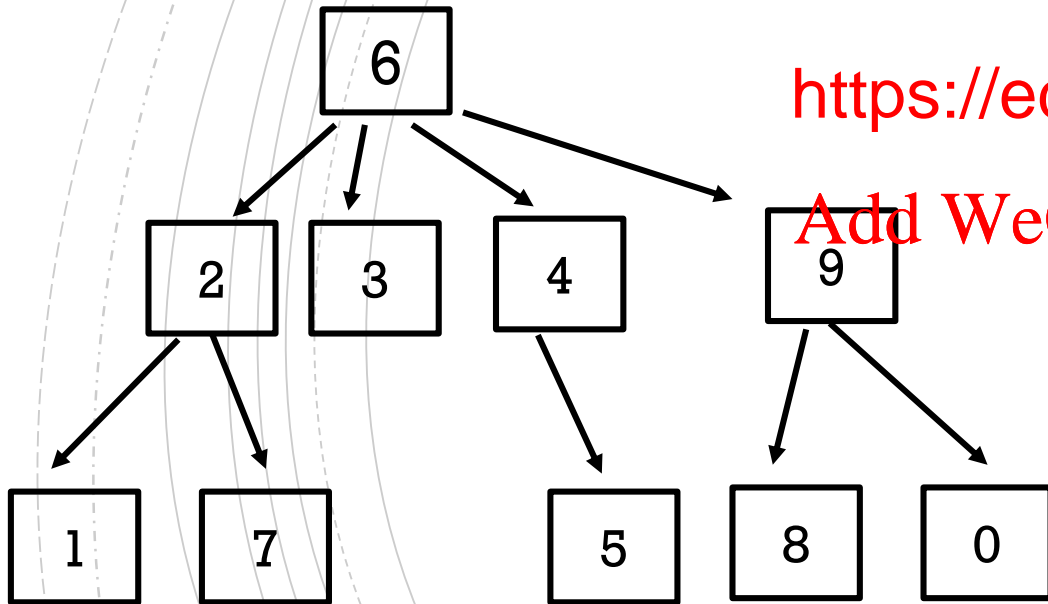
## ANOTHER EXERCISES

Write this tree using the first child, next sibling representation.

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro



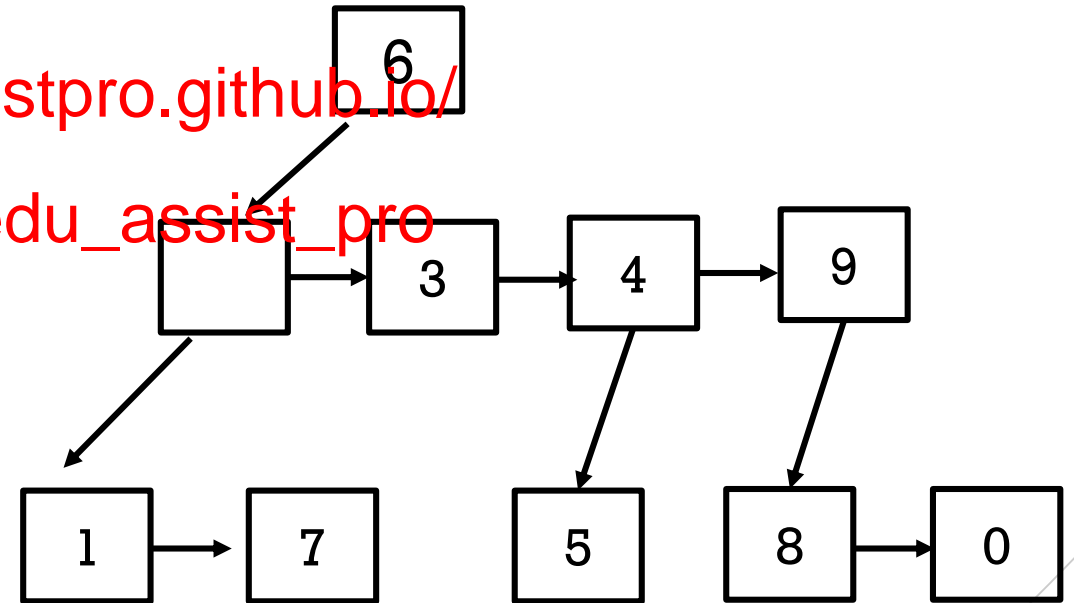
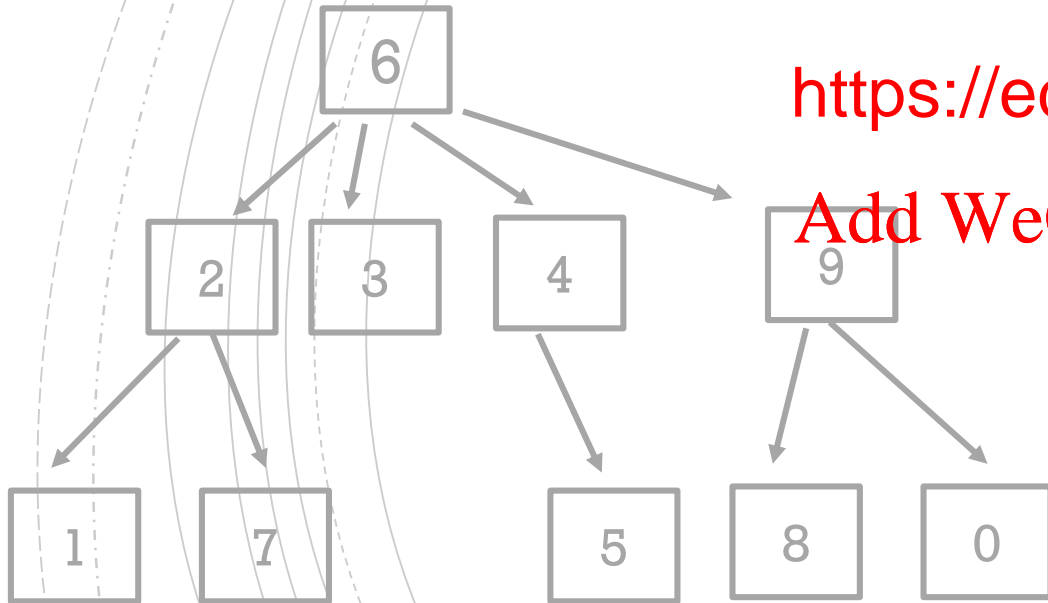
## SOLUTION

Write this tree using the first child, next sibling representation.

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro



An orange paint roller with a red handle, positioned horizontally. The roller is partially filled with orange paint, and there are orange paint splatters and drips around it. The text "Coming Soon" is written in white on the orange part of the roller.

# Coming Soon

## Assignment Project Exam Help

In the next

- Tree Tra <https://eduassistpro.github.io/>  
Add WeChat edu\_assist\_pro