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Outline

- Special "numbers" revisited
- Rounding

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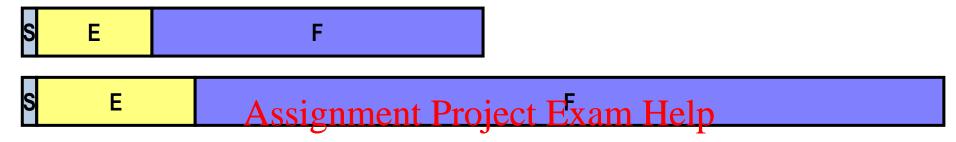
FP add/sub

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FP on MIPS

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• Integer multiplication & division

IEEE 754 Floating Point Review



Precision	Sign https:/	/eduassist	pro.github	Bias
Float	1 bit	8 bits	prorgitirad	127
Double	1 bit Add W	VerGilbat edu	u_assist_p	1 0 23

$$(-1)^S \times (1+F) \times 2^{(E-bias)}$$

- Numbers in normalized form, i.e., 1.xxxx...
- The standard also defines special symbols

Special Numbers Reviewed

Special symbols (single precision)

ExponerASS	gnmentcProject I	ExamjeHelpresented
0	https://eduassist	tpro.github.io/
0	Add Weehat ed	u_assistalipronumber
1-254	Anything	± floating point number
255	0	± infinity
255	Nonzero	NaN (Not a Number)

Representation for Not a Number

What do I get if I calculate

```
sqrt(-4.0) or 0/0?
```

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 If infinity is not an er

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 e either.
- Called Not a Numbe https://eduassistpro.github.io/
- Exponent = 255, Signifident cohzeedu_assist_pro
- Why is this useful?
 - Hope NaNs help with debugging?
 - They contaminate: op(NaN,X) = NaN

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Representation for Denorms (1/2)

- Problem: There's a gap among representable FP numbers around 0
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 Smallest representa
 - a = 1.00000000000000https://eduassistpro.github.io/
 - Second smallest representable pa edu_assistepro

$$a - 0 = 2^{-126}$$

$$b - a = 2^{-149}$$

-
$$\infty$$
 + ∞ + ∞

Normalization and implicit 1 is to blame!

Representation for Denorms (2/2)

- Solution: special symbol in exponent field
 - Use 0 in exponent field, nonzero for fraction Assignment Project Exam Help
 Denormalized numb
 - - https://eduassistpro.github.io/ Has no leading 1
 - Has implicit exponent at the birth edu_assist birth
 - Smallest positive float: 2e-149
 - 2nd smallest positive *float*: 2e-148





Small numbers and Denormalized

```
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0.000000000000000000011_2 \times 2^{-126}
0.00000000000000000000000001_2 \times 2^{-126}
Next smaller number is zero
```

Rounding

- When we perform math on real numbers, we must worry about rounding to fit the result in the significant field.
 Assignment Project Exam Help recision, and then rounds
 - The FP hardware car rectsion, and then rounds to get the proper valhttps://eduassistpro.github.io/
 - Rounding also occurs when equassist property a single precision value, or converting a floating point number to an integer

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IEEE Has Four Rounding Modes

- 1. Round towards +infinity
 - ALWAYS round "up": 2.001 -> 3
 - -2.001 -> -2 Assignment Project Examilimg(x) or [x]
- 2. Round towards -infi
 - ALWAYS round "do https://eduassistpro.github.io/
 - -1.999 -> -2

Add WeChat edu_assistx_ppo [x]

- 3. Truncate
 - Just drop the last bits (round towards 0)
- 4. Round to (nearest) even
 - Normal rounding, almost

Round to Even

- Round like you learned in grade school
- **Except** if the value is right on the borderline, in which case we round to the nearest Project Exam Help
 - -2.5 -> 2

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-3.5 -> 4

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- Insures *fairness*
 - This way, half the time we round up on tie, the other half time we round down
- This is the default rounding mode

FP Addition and Subtraction 1/2

- Much more difficult than with integers
- Cannot just add significands
- Recall how we do it: Project Exam Help
 - De-normalize to ma https://eduassistpro.github.io/
 - Add significands to get resulting on Add WeChat edu_assist_pro
 Normalize and check for under/ov

 - 4. Round if needed (may need to goto 3)
- Note: If signs differ, perform a subtract instead
 - Subtract is similar except for step 2

FP Addition and Subtraction 2/2

- Problems in implementing FP add/sub:
 - If signs differ for add (or same for sub), what is the sign of the result?
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- Question:
 - How do we integrat https://eduassistpro.githubnie/ic unit?
 - Answer: We don't! Add WeChat edu_assist_pro

MIPS Floating Point Architecture (1/4)

- Separate floating point instructions:
 - Single Precision:

 add.s, sub.s, mul.s, div.s

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 - Double Precision: https://eduassistpro.github.io/
 add.d, sub.d, mul deChat edu_assist_pro
- These instructions are *far more complicated* than their integer counterparts, so they can take much longer to execute.

MIPS Floating Point Architecture (2/4)

Observations

- It's inefficient to have different instructions take vastly differing amounts of time.
- Generally, a particul https://eduassistpro.gitlebarige from FP to int, or vice versa, within a program Soo edu_assist_proinstruction will be used on it.
- Some programs do no floating point calculations
- It takes lots of hardware relative to integers to make Floating Point fast

MIPS Floating Point Architecture (3/4)

- Pre 1990 Solution:
 - separate chip to do floating point (FP)
- Coprocessor 1: FP chi

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 - Contains 32 32-bit reg https://eduassistpro.github.io/
 - Usually registers specification with the control of the control
 - Separate load and store: lwc1 and swc1 ("load word coprocessor 1", "store ...")
 - Double Precision: by convention, even/odd pair contain one **DP FP number**: \$f0/\$f1,\$f2/\$f3,...,\$f30/\$f31 where the even register is the name

MIPS Floating Point Architecture (4/4)

- Pre 1990 Computers contains multiple separate chips:
 - Processor: handles all the normal stuff Assignment Project Exam Help
 - Coprocessor 1: hand

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– more coprocessors?

- Today, FP coprocessor integrat PU, or specialized or inexpensive chips may leave out FP HW
- Instructions to move data between main processor and coprocessors, e.g., mfc0, mtc0, mfc1, mtc1

17

Some More Example FP Instructions

```
abs.s $f0, $f2 # f0 = abs( f2 );
neg.s $f0, $f2 # f0 = - f2;
sqrt.s $f0, $f2 #AfoiganscpttProfect)Exam Help

c.lt.s $f0, $f2 # is
bclt label # branch WaChat edu_assist_pro
```

See 4th edition text 3.5 and App. B for a complete list of floating point instructions

Copying, Conversion, Rounding

```
mfc1 $t0, $f0  # copy $f0 to $t0
mtc1 $t0, $f0
               # copy $t0 to $f0
               # for Assignment Project Examt Halpble
cvt.d.s $f0 $f2
               # f0f1 ge
cvt.d.w $f0 $f2
                                          double
                      https://eduassistpro.github.io/
ceil.w.s $f0 $f2 # round to next higher integer
floor.w.s $f0 $f2 # round down to next lower integer
trunc.w.s $f0 $f2 # round towards zero
round.w.s $f0 $f2 # round to closest integer
```

Dealing with Constants

float a = 3.14;

```
    Option 1

                                     Option 2

    Declare constant 3.14 in data

    Compute hexadecimal IEEE

     segment of memarssignment Project Examelse pation for 3.14 (it is

    Load the address labe.

                        https://eduassistpro.github.jo/,

    Load to coprocessor

                        Add WeChat edu_assist_corprocessor
.data
                                           $t0 0x4048
                                     lui
PI: .float 3.14
                                     ori $t0 $t0 0xF5C3
.text
                                     mtc1 $t0 $f0
1a
      $t0 PI
Twc1 $f0 ($t0)
                                           Option 3, pseudoinstruction
                                           not available in MARS:
1.S $f0 PI # easiest
```

li.s \$f0, 3.14

Floating Point Register Conventions

(\$f0, \$f1), and (\$f2, \$f3)	Function return registers used to return float and double values from function calls.		
(\$f12, \$f13) and (\$f14, \$f15)	Two pairs of registers used to pass float and Assignment Project Exam Help double valued arguments to functions. Pai https://eduassistpro.gffffff.bc/cause the ues. To pass float double with the ues. To pass float and project Exam Help double with the ues. To pass float and passing the uest are used to pass float and passing the uest arguments are used to pass float and passing the uest arguments are used to pass float and passing the uest arguments are used to pass float and passing the uest arguments are used to pass float and passing the uest arguments are used to passing the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the unit of the uest are used to passing the uest ar		
\$f4, \$f6, \$f8, \$f10, \$f16, \$f18	Temporary registers		
\$f20, \$f22, \$f24, \$f26, \$f28, \$f30	, . ,		

Unfortunately no nice names (e.g., \$t#, \$s#) like with the main registers)

With double precision instructions, the high-order 32-bits are in the implied odd register.

Fahrenheit to Celsius

float f2c(float f) { return 5.0/9.0*(f-32.0); }



```
.text
                             .data
            Assignment Project Exam: Helps. 0
f2c:
          $t0 co
    la
          $f16 (https://eduassistpro.github.io/o
          $t0 const9
    la
    lwc1 $f18 ($Aold WeChat edu_assist_pro
    div.s $f16 $f16 $f18 # f16 = 5.0/9.0
          $t0 const32
    la
    lwc1 $f18 ($t0)
    sub.s $f18 $f12 $f18 # f18 = fahr-32.0
    mul.s $f0 $f16 $f18 # return f16*f18
    jr
          $ra
```

Debugging FP Code in MARS

- MARS displays floating point registers in hexadecimal
- This makes debugging floating point code tricky...
 Can use MARS "Floating Point Representation" tool to examine single precision
 - Alternatively syscall can https://eduassistpro.glehub.io/

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Service	Code in \$v0	Arguments
Print float	2	\$f12 = float to print
Print double	3	\$f12 = double to print
Print string	4	\$a0 = address of null-terminated string to print

```
.data
                .asciiz " "
spaceString:
newlineString:
                .asciiz "\n"
printSpace:
        li $v0, 4
        la $aAssignifient Project ExamilHeintspace syscall lwc1 $f12, 4($s0)
        jr $ra
printNewLine:
        1i $v0, 4 Add WeChat edu_assist_ipfoat
        la $a0, newlineString
        syscall
        jr $ra
printFloat: # in $f12
        1i $v0, 2
        syscall
        jr $ra
```

```
# print( float vec[4] )
                 printFloatVector:
                         addi $sp, $sp, -8
                         sw $ra, 0($sp)
                         sw $s0, 4($sp)
                         move $s0, $a0
                         lwc1 $f12, 0($s0)
                         jal printfloat
                           l printFloat
https://eduassistpro.github.jo/ce
                              $f12, 8($s0)
                         jal printSpace
                         lwc1 $f12, 12($s0)
                         jal printfloat
                         jal printNewLine
                         lw $ra, 0($sp)
                         lw $s0, 4($sp)
                         addi $sp, $sp, 4
                         jr $ra
```

REMEMBER: Floating Point Fallacy

FP add, subtract associative? FALSE!

```
x = -1.5 \times 10^{38} y = 1.5 \times 10^{38} z = 1.0

x + (y + z) Assignment Projects Examp Help

= -1. https://eduassistpro.github.io/

= 0.0

(x + y) + z = (-1.5 \times 10^{38}) + \text{Chatedu_assist_pro}

= (0.0) + 1.0

= 1.0
```

- Floating Point add, subtract are not associative!
 - Floating point result approximates real result!

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Casting floats ← ints

- (int) floating point expression
 - Coerces and converts it to the nearest integer (C uses truncation)

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 - i = (int) (3.14 https://eduassistpro.github.io/
- (float) expresadd We Chat edu_assist_pro
 - converts integer to nearest floating point

```
f = f + (float) i;
```

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int \rightarrow float \rightarrow int

Large values of integers don't have exact floating

• What about double?

point representations

float \rightarrow int \rightarrow float

```
if (f == (float)((int) f)) {
    printf("true");
    Assignment Project Exam Help
    https://eduassistpro.github.io/
```

- Does this always print t
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 No, it will not always pri
 - Small floating point numbers (<1) don't have integer representations
 - Same is true for large numbers
 - For other numbers, rounding errors

MIPS Integer Multiplication

- Syntax of Multiplication (signed): MULT reg1 reg2
- Result of multiplying 32 bit registers has 64 bits Assignment Project Exam Help
- MIPS splits 6 cial registers
 - upper half i https://eduassistpro.github.io/
 - Registers hi andd Wacchest edu_assisthes general purpose registers
 - Use MFHI reg to move from hi to register
 - Use MFLO reg to move from lo to another register
- Unusual syntax compared to other instructions!

MIPS Integer Multiplication Example

```
a = b * c;
Let b be $s2; let c be $s3;
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And let a be $s0 and $ bits)
https://eduassistpro.github.io/
mult $s2 $s3  # b*c Add WeChat edu_assist_pro
mfhi $s0  # get upper half of product
```

mflo \$s1

• We often only care about the low half of the product!

get lower half of product

MIPS Integer Division

- Syntax of Division (signed): DIV reg1 reg2
 - Divides register 1 by register 2
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 Puts remainder of di

 - Puts quotient of divi https://eduassistpro.github.io/
- Notice that this can bedds to the division operator (/) and modulo operator (%) in a high level language

31

MIPS Integer Division Example

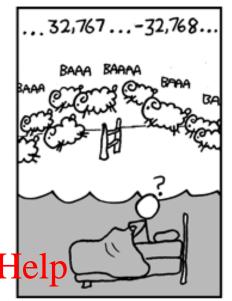
		Variable	Register
a	= c / d; Assignment Project Exam F	a John	\$s0
b	= C	b	\$s1
	https://eduassistpro.gitl	hub _c io/	\$s2
	Add WeChat edu_assis	st_pto	\$s3

```
div $s2 $s3 # lo=c/d, hi=c%d
mflo $s0 # get quotient
mfhi $s1 # get remainder
```

Unsigned Instructions and Overflow

 MIPS has versions of mult and div for unsigned operands:

multu, dassignment Project Exam Help





- Determines wheth https://eduassistpro.githubuo/tient are changed if the operands are sign gned.

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 Typically unsigned instructions r overflow
- (e.g., add vs addu)
- MIPS does not check overflow or division by zero on ANY signed/unsigned multiply, divide instruction
 - Up to the software to check "hi", "divisor"

Things to Remember

- Integer multiplication and division:
 - -mult, div, mfhi, mflo
- New MIPS registers (special Pole) that institute tions in two flavours

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 - Single Precision .s
 - Double Precision .d
- Add WeChat edu_assist_pro
- FP add and subtract are not associative...
- IEEE 754 NaN & Denorms (precision) review
- IEEE 754's Four different rounding modes

Review and More Information

- Textbook
 - Section 3.5 Floating Point

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 We saw the representation and addition and multiplication algorithm
 - We saw the representation and addition and multiplication algorithm material earlier in th https://eduassistpro.github.io/

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