

Assignment Project Exam Help
Num ations

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*There are 10 types of this world
Those who understand binary and those who don't*

Agenda

- Bits, Bytes, and Words
- Number bases and base conversion
 - Positional notation
- Binary arithmetic and I/O
 - Signed numbers
 - Arithmetic and overflow
 - Packed Decimal, ASCII, Parity...

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From Lecture 1: Below Your Program

- High-level language program (in C)

```
swap (int v[], int k) {  
    int temp = v[k];  
    v[k] = v[k+1];  
    v[k+1] = temp;  
}
```

- Assembly language program

```
swap:  sll  
       add $2, $4, $2  
       lw  $15, 0($2)  
       lw  $16, 4($2)  
       sw  $16, 0($2)  
       sw  $15, 4($2)  
       jr  $31
```

- Machine (object) code (for MIPS)

```
000000 00000 00101 0001000010000000  
000000 00100 00010 0001000000100000  
... ..
```

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C compiler

assembler

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How do people represent

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Why Base 10? Why Base 2?

- **Decimal: Base 10**, a single number from 0-9
- **Binary: Base 2**, a single digit is called a **bit** (binary digit)
- A bit is the smallest unit of information, and can represent...
 - 1 / 0
 - True / False
 - Yes / No
 - On / Off
 - used in a two-state (Boolean) logic
- Can represent anything with a sequence of binary bits, but the bit patterns have *no* intrinsic meaning by themselves!

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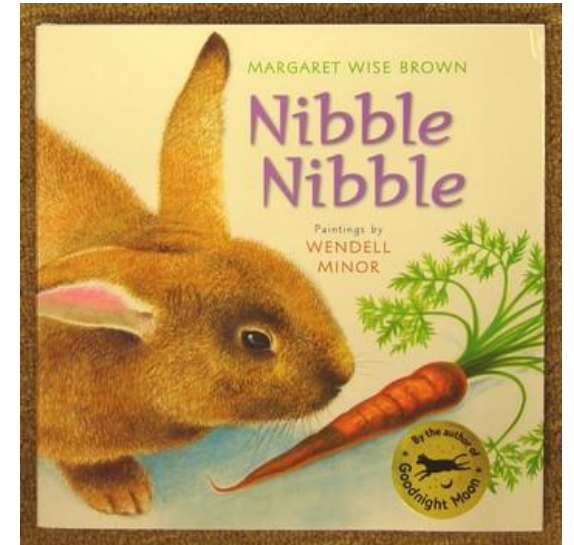
Nibbles to Words

- Typically store information in groups
 - a **byte** is a group of 8 bits
 - e.g. 01100101
 - a **nibble/nybble** (a s <https://eduassistpro.github.io/> 4 bits,
 - e.g. 0110
 - a **word** (MIPS) is a group of 4 bytes, or 32 bits
 - e.g. 01100101011001010110010101100101
- Least significant bit right most

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Numbers and Positional Notation

$a_n a_{n-1} \dots a_1 a_0 . a_{-1} a_{-2} \dots a_{-m}$
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$i = -m$
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$$N = a_n b^n + a_{n-1} b^{n-1} + \dots + a_1 b + a_0 + a_{-1} b^{-1} + \dots + a_{-m} b^{-m}$$

Examples

- 238_{10}

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- 10110_2

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Common Bases

Name of Base	Base	Digits used
Decimal	10	0,1,2,3,4,5,6,7,8,9
Binary	2	0,1
Octal	8	0,1,2,3,4,5,6,7
Hexadecimal	16	0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F

- We often write hex numbers preceded by 0x

$$1011_2 = 11_{10} = 13_8 = B_{16} = 0xB$$

How many bits are needed to represent a decimal number?



What is the largest decimal number with n digits?

$$10^n - 1$$

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What is the largest

$$2^m - 1$$

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- For base b , the largest number is $b^k - 1$

How many bits are needed to represent a decimal number?



How many digits necessary for numbers up to one million?

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How to Convey <https://eduassistpro.github.io/> **ase to Another?**

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Base Conversion – Decimal to Another Base

- Approach 1: Make a table

- Divide by b^i
- The quotient is the most significant bit
- Repeat with the rem

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- Approach 2:

- Divide by b
- Remainder of result is least significant bit
- Repeat with the quotient

Base Conversion – Decimal to Another Base



Example: What is 523_{10} in binary?

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Base Conversion – Decimal to Another Base



Example: What is 53241_{10} in hexadecimal?

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Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

Base Conversion – Other Base to Decimal

- Basic Approach: Direct expansion with positional weights

$$N = a_n b^n + a_{n-1} b^{n-1} + \dots + a_1 b + a_0$$

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- Advanced Approach <https://eduassistpro.github.io/>

$$N = a_n b^n + a_{n-1} b^{n-1} + \dots + a_1 b + a_0$$

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$$= (\dots((a_n b + a_{n-1})b + a_{n-2})b + \dots + a_1)b + a_0$$

Base Conversion – Other Base to Decimal



Examples: What is 1010101_2 in Decimal

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Base Conversion – Other Base to Decimal



Examples: What is $1AB_{16}$ in Decimal?

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Base Conversion – Base A to Base B

- Conversion from base a to base b

- First convert base a to decimal

- Then convert decimal to base b

- Special cases (easier)

- Binary to hexadecimal and back

- Example:

- $$\begin{aligned} &11010101101_2 \\ &= 011010101101_2 \\ &= 6AD_{16} \end{aligned}$$

- Binary to octal and back

- Example: 760_8 becomes 111110000_2

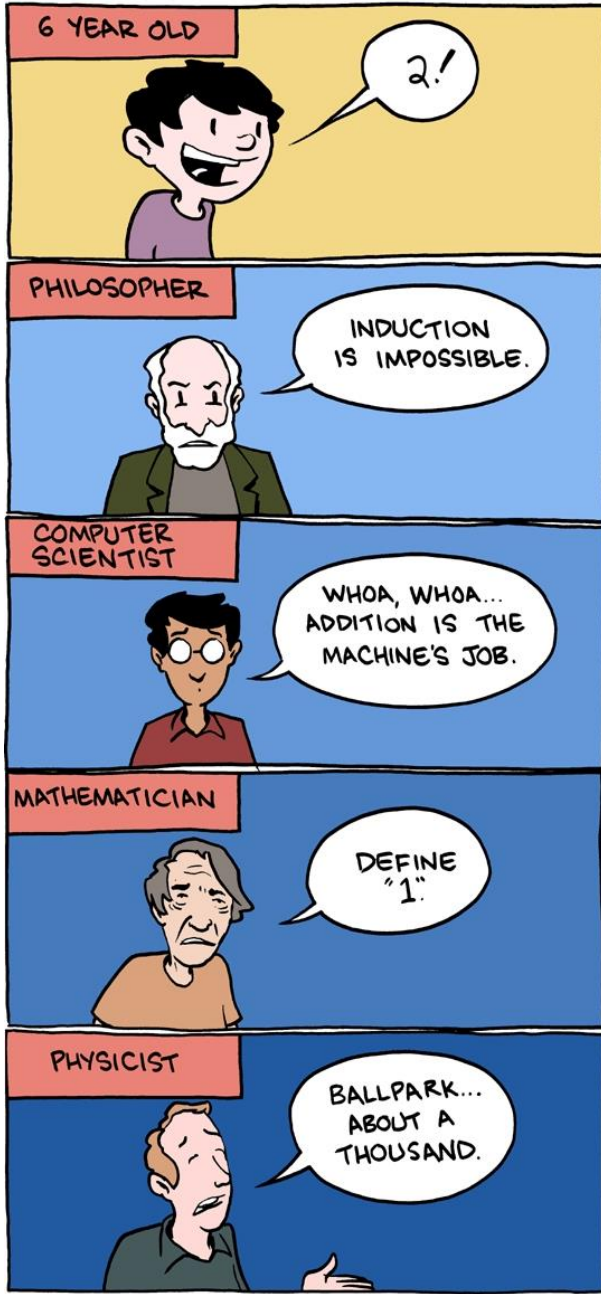
Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

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$$1 + 1 = ?$$



Questions



- What is the largest binary number with n bits?
- How do we add binary numbers?
- How many numbers?
- Why do programs always mix up Halloween and Christmas?
- How should we represent negative numbers?

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How to Re <https://eduassistpro.github.io/> **d Numbers?**

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Sign-and-Magnitude

- The first approach
- Use the most significant bit to represent the sign

+13 = 0000 1101

-13 = 1000 1101

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- Problems
 - Two representations for zero: 0000 0000 and 1000 0000
 - Cannot add a positive number and a negative number together

One's Complement

- ***Invert each bit!***

+13 = 0000 1101

-13 = 1111 0010

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- ***Problems:***

– Still two representations for zero 0 and 1111 1111

– Answer is off by 1

– Incorrect overflow

- What is $16 + (-13)$?

Two's Complement

- The gold standard
- Invert the bits and add one!

+13 = 0000 1101

What is -13?

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- Unique zero
0000 0000

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- MSB represents the sign.
 - 1 if negative
 - 0 if positive
- Negative numbers are defined as $-N = \mathbf{B}^n - N$

Two's Complement

- Easily implemented in hardware

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- Range from -2^{n-1} to

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- The complement of compleme, i.e., $-(-Y) = Y$.

Two's Complement

- $16 - 13 = ?$

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The Hitchhiker's Guide to the Galaxy

What is the question about the universe, and
everyt

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Binary Arithmetic

Addition	Subtraction	Multiplication
$0 + 0 = 0$	$0 - 0 = 0$	$0 * 0 = 0$
$0 + 1 = 1$		$0 * 1 = 0$
$1 + 0 = 1$	$1 - 0 = 1$	$1 * 0 = 0$
$1 + 1 = 0$ carry 1	$1 - 1 = 0$	$1 * 1 = 1$

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- Rules in base 10 are also valid in any other base
- Subtraction often done using addition and 2's complement
- Multiplication and division are similar. We will learn in a few lectures

Arithmetic overflow

- Typically use a fixed # of bits to represent numbers!
- *Arithmetic overflow* can occur during two's complement addition/subtraction

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Arithmetic overflow

- Example: $6_{10} + 5_{10}$ using 4 bits

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Arithmetic overflow

- Typically use a fixed # of bits to represent numbers!
- *Arithmetic overflow* can occur during two's complement addition/subtraction
 - Add 2 positive numbers and getting a negative result
 - Add 2 negative numbers and getting a positive result.
 - A minus B with $A < 0$ and $B > 0$ and getting positive result
 - A minus B with $A > 0$ and $B < 0$ and getting negative result
- Need to take extra care when implement it on the circuits

Packed Decimal

(Binary Coded Decimal, BCD)

- Replace each digit with its 4-bit equivalent

5372₁₀ in BCD is 0101 0011 0111 0010

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- Good

- User friendly? Yes!

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- BCD is easier for humans to parse

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- Bad

- Wastes storage space

- BCD is harder to implement in hardware

Parity

- Used to check for corrupt data in storage or transmission, with two kinds: even and odd

- Total # of bits with 1
 - Total # of bits with 1

- Examples:

Even Parity	Odd Parity
0010101001	1110101000
0000000000	0011110111
1010101011	0000000000



- Advantage of odd parity?
- Detecting multiple errors? Correcting errors?

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How to <https://eduassistpro.github.io/> **characters?**

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Character Data Codes

Name	bits per symbol	# of symbols	Comments
IBM-BCD	6	64	Capital letters: A-Z, 0-9, \$, etc. Not to confuse with Packed Decimal.
ASCII	7	128	All letters: a-z, A-Z, 0-9, \$, BEL, TAB, etc. See link below
USACII	8		n).
EBCDIC	8		s (odd parity)
UNICODE	16		etters of all languages.

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ASCII

American
Standard
Code for
Information
Interchange

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UNICODE

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The Martian

A
The c
Only one camera is wor
How can he communic

ars.
roken.
und
arth?

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48 4F 57 41 4C 49 56 45?
What was the Earth trying to say?

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48 4F 57 41
4C 49 56 45?

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Summary

- Definitions: Bits, Nibbles, Bytes, Words
- Representations: number bases, conversion
- Signed numbers with two's complement
- Other data representations
 - Packed Decimal (BCD)
 - ASCII and other character data codes
 - Parity

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Review and more information

- Textbook
 - Section 2.4, Signed and Unsigned Numbers
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There are 10 types of people in this world...

Those who understand binary and those who don't