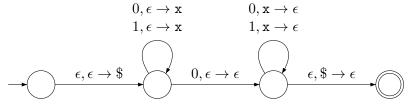
The University of Melbourne School of Computing and Information Systems COMP30026 Models of Computation

Selected Problem Set Solutions, Week 10

P10.1 Here is a PDA for $\{w \mid \text{the length of } w \text{ is odd and its middle symbol is } 0\}$



P10.3 For the case $v \neq \epsilon$ we define

$$\delta((q_p, q_d), v, x) = \{ ((r_p, r_d), y) \mid (r_p, y) \in \delta_P(q_p, v, x) \land r_d = \delta_D(q_d, v) \}$$

But we must also allow transitions that don't consume input, so:

 $\begin{array}{c} \textbf{Assignment} & \textbf{Project Exam Help} \\ \textbf{P10.5 We are looking at the context-free grammar} & \textbf{Exam Help} \\ \end{array}$

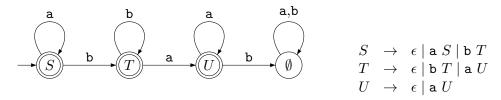
https://eduassistpro.github.io/

(a) The grammar is ambiguous. For example, a

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- (b) $L(G) = a^*b^*a^*$.
- (c) To find an unambiguous equivalent context-free grammar it helps to build a DFA for a*b*a*. (If this is too hard, we can always construct an NFA, which is easy, and then translate the NFA to a DFA using the subset construction method, which is also easy.) Below is the DFA we end up with. The states are named S, T, and U to suggest how they can be made to correspond to variables in a context-free grammar. The DFA translates easily to the grammar on the right. The resulting grammar is a so-called regular grammar, and it is easy to see that it is unambiguous—there is never a choice of rule to use.



P10.6 Here is a context-free grammar that will do the job (S is the start symbol):

$$\begin{array}{ccc} S & \rightarrow & \epsilon \mid \mathtt{a} \; A \\ A & \rightarrow & \mathtt{a} \; A \mid \mathtt{b} \; B \\ B & \rightarrow & \epsilon \mid \mathtt{a} \; A \mid \mathtt{b} \; B \end{array}$$