

School of Computing and Information Systems
COMP30026 Models of Computation Problem Set 9

27 September – 1 October 2021

Content: regular expressions, NFAs, context-free grammars, the pumping lemma.

P9.1 Give regular expressions for the following languages over the alphabet $\Sigma = \{0, 1\}$.

- (i) $\{w \mid w \text{ has length at least 3 and its third symbol is 0}\}$
- (ii) $\{w \mid \text{every odd position of } w \text{ is a 1}\}$
- (iii) $\{w \mid w \text{ contains at least two 0s and at most one 1}\}$
- (iv) $\{\epsilon, 0\}$
- (v) The empty set

Bonus: Draw minimal NFAs for these languages, and those from T9.1

P9.2 String s is a *suffix* of string t iff there exists some string u (possibly empty) such that $t = us$. For any language L we can define the set of suffixes of strings in L :

$$\text{suffix}(L) = \{x \mid x \text{ is a suffix of some } y \in L\}$$

Let A be any regular language. Consider the language $L = \{x \mid x \text{ is a suffix of some } y \in A\}$. int: Think about how a DFA for A can be modified to accept L .

P9.3 In general it is difficult, given a regular expression, to find a regular expression for its complement. However, it can be done, and you have been given all the necessary tricks and algorithms. This question asks you to go through the required steps. Consider the regular language $(ba^*a)^*$. Assuming that you know how to find a regular expression for its complement, that is, for

$$L = \{w \in \{a, b\}^* \mid w \text{ is not in } (ba^*a)^*\}$$

To complete this task, go through the following steps.

- (a) Construct an NFA for $(ba^*a)^*$. Two states suffice.
- (b) Turn the NFA into a DFA using the subset construction method.
- (c) Do the “complement trick” to get a DFA D for L .
- (d) Reflect on the result: Wouldn’t it have been better/easier to apply the “complement trick” directly to the NFA?
- (e) Turn DFA D into a regular expression for L using the NFA-to-regular-expression translation shown in the lecture on regular expressions (not examinable).

P9.4 A *palindrome* is a string that reads the same forwards and backwards. Use the pumping lemma for regular languages and/or closure results to prove that the following languages are not regular:

- (a) $B = \{a^i b a^j \mid i > j \geq 0\}$
- (b) $C = \{w \in \{a, b\}^* \mid w \text{ is not a palindrome}\}$
- (c) $D = \{www \mid w \in \{a, b\}^*\}$

Assignment Project Exam Help

- # Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

Assignment Project Exam Help

