

## Assignment Project Exam Help

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School of Computer Science and En University of New South Wales

DYNAMIC PROGRAMMING

## Dynamic Programming

# As stephing pynnic pie of the problem from optical solutions for (carefully chosen) psmaller size subproblems.

- Sub opti opti size shttps://eduassistpro.github.
- Efficiency of DP comes from the fact that the sets of su to solve larger problems heavilly prortanged the assistance and its solution is stored in a table for maniple as SSIST\_DI larger problems.

• Instance: A list of activities  $a_i$ ,  $1 \le i \le n$  with starting times  $s_i$  and finishing times  $f_i$ . No two activities can take place simultaneously.

## A S Task: Find a subset of compatible activities of Tasking I total duration Help Remember, we used the Greedy Method to solve a somewhat similar problem

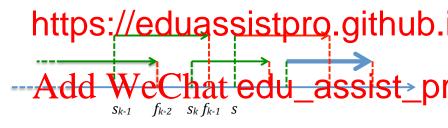
- Remember, we used the Greedy Method to solve a somewhat similar problem of finding a subset with the **largest possible number** of compatible acti lem.
- We shttps://eduassistpro.github.
- For every  $i \le n$  we solve the following subproble

  Subproblem (i) and a subschipped (i) and a subschipped (i) and a subschipped (i) and (i) such that (i) and (i) are subschipped (i) are subschipped (i) and (i) are subschipped (i) are subschipped (i) are subschipped (i) and (i) are subschipped (i) are subschipped (i) and (i) are subschipped (i) are subschipped (i) are subschipped (i) and (i) are subschipped (i) are subschipped (i) and (i) are subschipped (i) and (i) are subschipped (i) and (i) are subschipped (i) and (i) are subschipped (i) are subschipped (i) and (i) are subschipped (i) and (i) are su
  - $\bullet$   $\sigma_i$  consists of non-overlapping activitie
  - $\circ$   $\sigma_i$  ends with activity  $a_i$ ;
  - 3  $\sigma_i$  is of maximal total duration among all subsequences of  $S_i$  which satisfy 1 and 2.
- Note: the role of Condition 2 is to simplify recursion.

- Let T(i) be the total duration of the optimal solution S(i) of the subproblem P(i).
- For S(1) we choose  $a_1$ ; thus  $T(1) = f_1 s_1$ ;

  Security 1 associated that  $C(1) = f_1 s_1$ ;

  Stored them in a table, we let



• In the table, for every i, besides T(i), we also store  $\pi(i) = j$  for which the above max is achieved:

$$\pi(i) = \arg \max \{ T(j) : j < i \& f_j \le s_i \}$$

- Why does such a recursion produce optimal solutions to subproblems P(i)?
- As f the optimal solution of subproblem P(i) be the sequence f we claim: the truncated subsequence f to f the sequence f we claim: the truncated subsequence f to f the sequence f where f is an optimal f to f the sequence f and f is an optimal f to f and f is an optimal f is an opt
  - solu
  - wh https://eduassistpro.github.
  - If there were a sequence  $S^*$  of a larger total dur sequence  $S^*$  and also indire with activity  $\mathbf{CU}$  assist  $\hat{\mathbf{D}}$  by extending the sequence S with activity  $\mathbf{CU}$  assist  $\hat{\mathbf{D}}$  subproblem P(i) with a longer total duration than t sequence S, contradicting the optimality of S.
  - Thus, the optimal solution  $S = (a_{k_1}, a_{k_2}, \ldots, a_{k_{m-1}}, a_{k_m})$  for problem P(i)  $(= P(a_{k_m}))$  is obtained from the optimal solution  $S' = (a_{k_1}, a_{k_2}, \ldots, a_{k_{m-1}})$  for problem  $P(a_{k_{m-1}})$  by extending it with  $a_{k_m}$

the o

• Continuing with the solution of the problem, we now let

```
T_{max} = \max\{T(i) : i \le n\};
```

last =  $\arg \max\{T(i) : i \le n\}$ . **Selection in the primal sequence** when **Xive fur** problem from the table of partial solutions, because in the  $i^{in}$  slot of the table, besides T(i) we also store  $\pi(i) = j$ , (j < i) such that the optimal solution of P(i) extends

- Thu https://eduassistpro.github.
- Why is such solution optimal, i.e., why looking for optimal solutions of P(i) which must end with a<sub>i</sub> did not cause us to miss th such an additional requirement? hat edu\_assist\_pi
  Consider the optimal solution without such additio
  - assume it ends with activity  $a_k$ ; then it would have been obtained as the optimal solution of problem P(k).
- Time complexity: having sorted the activities by their finishing times in time  $O(n \log n)$ , we need to solve n subproblems P(i) for solutions ending in  $a_i$ ; for each such interval  $a_i$  we have to find all preceding compatible intervals and their optimal solutions (to be looked up in a table). Thus,  $T(n) = O(n^2)$ .

• Longest Increasing Subsequence: Given a sequence of n real numbers A[1..n], determine a subsequence (not necessarily contiguous) of maximum length in which the values in the subsequence are strictly

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- Solution: For each  $i \leq n$  we solve the following subproblems:
- \* \*\*Sub max https://eduassistpro.github.
- Recursion: Assume we have solved the subproblem that we have just in a table S he values  $\ell_j$  of maximum structures are the subject of  $\ell_j$  as S
- We now look for all A[m] such that m < i and such that A[m] < A[i].
- Among those we pick m which produced the longest increasing subsequence ending with A[m] and extend it with A[i] to obtain the longest increasing subsequence which ends with A[i]:

$$\begin{split} \ell_i &= \max \{ \ell_m \ : \ m < i \ \& \ A[m] < A[i] \} + 1 \\ \pi(i) &= \arg \max \{ \ell_m \ : \ m < i \ \& \ A[m] < A[i] \} \end{split}$$

## Assignment Project Exam Help We she in the 1th slot of the table the length \( \ell\_i \) of the longest increasing

- We store in the  $i^{th}$  slot of the table the length  $\ell_i$  of the longest increasing subsequence ending with A[i] and  $\pi(i) = m$  such that the optimal solu
- so, https://eduassistpro.github.
- The end point of such a sequence can be obtained as

end = 
$$\arg\max\{\ell_i : i \leq n\}$$

# As We can now reconstruct the longest monotonically increasing Henry $\pi$ and $\pi$ end, $\pi$ (end), $\pi$ ( $\pi$ (end)), . . .

- Aga https://eduassistpro.github. bec constructed as the solution for P(m).
- TimeAnd of ty: We Chat edu\_assist\_pr
- Exercise: (somewhat tough, but very useful) Design an algorithm for solving this problem which runs in time  $n \log n$ .

- Making Change. You are given n types of coin denominations of values (1, 1) (2, 1) (3, 1) (4, 1) integers. Assume (1, 1) so that you can make change for any given integer amount C with as few coins as possible, assuming that you have an unlimited supply of coins of each den
  - Soluhttps://eduassistpro.github.
  - If C A the lut Wse vial natseed uof dessist production of the lut with the lut wi
  - Assume we have found optimal solutions for every amount j < i and now want to find an optimal solution for amount i.

• We consider optimal solutions opt(i-v(k)) for every amount of the form i-v(k), where k ranges from 1 to n. (Recall  $v(1),\ldots,v(n)$  are all of the available denominations.)

## ssignment Project Exam Help Amore all of these optimal solutions which we find in the table we are constructing recursively!) we pick one which uses the fewest number of coins,

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- we https://eduassistpro.gitihub.i

# 

- Consider an optimal solution for amount  $i \leq C$ ; and say such solution includes at least one coin of denomination v(m) for some  $1 \le m \le n$ . But then removing such a coin must produce an optimal solution for the amount i - v(m) again by our cut-and-paste argument.

• However, we do not know which coins the optimal solution includes, so we try all the available coins and then pick m for which the optimal solution for

## Assignment From Exam Help • It is enough to store in the $i^{th}$ slot of the table such m and opt(i) because this

- ored in the slot of the table such m and opt(i) because this allo slot, t slot https://eduassistpro.github.
- $\bullet$  opt(C) is the solution we need.
- Time Amplexity of Welchart edu\_assist\_pr
- Note: Our algorithm is NOT a polynomial gth of the input, because the length of a representation of C is only  $\log C$ , while the running time is nC.
- But this is the best what we can do...

Integer Knapsack Problem (Duplicate Items Allowed) You have n types of items; all items of kind i are identical and of weight  $w_i$  and value  $v_i$ . You also have a knapsack of capacity C. Choose a combination of available items which all fit in the knapsack and whose value is plarge as possible. You can take any number of the STARMENT PROJECT EXAM Help

- Solu
- we https://eduassistpro.github.
- Assume we have solved the problem for all knapsacks of capacities j < i.
- We not look at optival selection in that edu\_assist\_production in the contract of the contra
- Chose the one for which  $opt(i w_m) + v_m$  is the largest;
- Add to such optimal solution for the knapsack of size  $i w_m$  item m to obtain a packing of a knapsack of size i of the highest possible value.

- \* https://eduassistpro.github.
  - Whi backtracking: if  $\pi(C) = k$  then the first object is alue  $v_k$ ; if  $\pi(C w_k) = m$  then the second object is
- Note that the light not be conquely attended; U\_assist\_property and solutions we pick arbitrarily among them.
- Again, our algorithm is **NOT** polynomial in the **length** of the input.

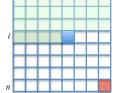
• Integer Knapsack Problem (Duplicate Items NOT Allowed) You have n items (some of which can be identical); item  $I_i$  is of weight  $w_i$  and value  $v_i$ . You also have a knapsack of capacity C. Choose a combination of available items which all fit in the kn prack and whose value is as large as possible.

Signment Project Exam Helt This Can example of a "2D" recursion; we will be filling a table of size n × 1 row by row; subproblems P(i, c) for all i - n and c - C will be of the form:

## <sup>chos</sup> https://eduassistpro.github.

- Fix now  $i \le n$  and  $c \le C$  and assume we have solved the subproblems for:

  - all j < i and all knapsacks of capacities fr</li>
     for ideal average the problem from assist problem.



- we now have two options: either we take item  $I_i$  or we do not;
- Assignment Project Exam Help

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- if  $opt(i-1, c-w_i) + v_i > opt(i-1, c)$ then  $opt(i, c) = opt(i-1, c-w_i) + v_i;$ else opt(i, c) = opt(i-1, c).
- Final solution will be given by opt(n, C).

• Balanced Partition You have a set of n integers. Partition these integers into two subsets such that you minimise  $|S_1 - S_2|$ , where  $S_1$  and  $S_2$  denote the sums of the elements in each of the two subsets.

# As Significant transmitted items not allowed) with the knapsak of size S/2 and with each integer $x_i$ of both size and value equal to $x_i$ .

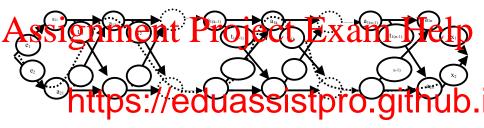
- \* Part https://eduassistpro.github.
- Why? Since  $S = S_1 + S_2$  we obtain

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i.e. 
$$S_2 - S_1 = 2(S/2 - S_1)$$
.

- Thus, minimising  $S/2 S_1$  will minimise  $S_2 S_1$ .
- So, all we have to do is find a subset of these numbers with the largest possible total sum which fits inside a knapsack of size S/2.

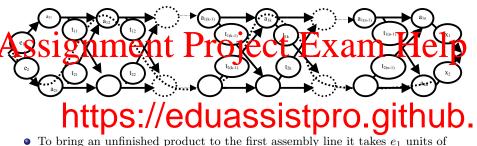
#### Dynamic Programming: Assembly line scheduling



**Instance:** Two assembly lines with workstations for

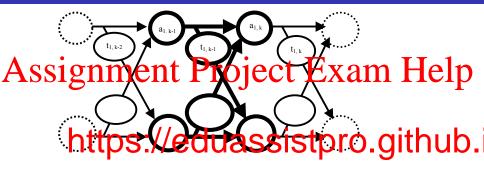
- On the intestmb Whole kit parket Complete; on the second assembly line the same job tak
- To move the product from station k-1 on the first assembly line to station k on the second line it takes  $t_{1,k-1}$  units of time.
- Likewise, to move the product from station k-1 on the second assembly line to station k on the first assembly line it takes  $t_{2,k-1}$  units of time.

## Dynamic Programming: Assembly line scheduling



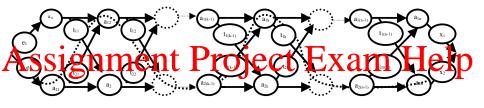
- To bring an unfinished product to the first assembly line it takes  $e_1$  units of time.
- To bring an unfinished product to the second assemble time. Add We Chat edu\_assist\_product to the second assemble to the second assembl
- To get a finished product from the first assembly line to the warehouse it takes  $x_1$  units of time;
- ullet To get a finished product from the second assembly line to the warehouse it takes  $x_2$  units.
- Task: Find a fastest way to assemble a product using both lines as necessary.

## Dynamic Programming: Assembly line scheduling



- For each  $k \le n$ , we solve subproblems P(1) edu\_assist\_problems P(1)
- P(1,k): find the minimal amount of time k jobs, such the  $k^{th}$  job is finished on the  $k^{th}$  workstation on the **first** assembly line;
- P(2, k): find the minimal amount of time m(2, k) needed to finish the first k jobs, such the  $k^{th}$  job is finished on the  $k^{th}$  workstation on the **second** assembly line.

## **Dynamic Programming**



- \* We shttps://eduassistpro.github.
- Rec

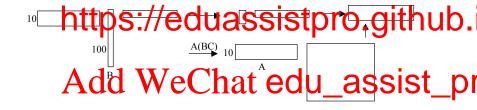
$$\begin{array}{c} m(1,k) = \min\{m(1,k-1) + a_{1,k}, \quad m \\ \text{And } m(2,k) = \min\{m($$

• Finally, after obtaining m(1,n) and m(2,n) we choose

$$opt = min\{m(1, n) + x_1, m(2, n) + x_2\}.$$

• This problem is important because it has the same design logic as the Viterbi algorithm, an extremely important algorithm for many fields such as speech recognition, decoding convolutional codes in telecommunications etc, covered

- For any three matrices of compatible sizes we have A(BC) = (AB)C.
- Assignment = 1000 beece Exam Help



- To evaluate (AB)C we need  $(10 \times 5) \times 100 + (10 \times 50) \times 5 = 5000 + 2500 = 7500$  multiplications;
- To evaluate A(BC) we need  $(100 \times 50) \times 5 + (10 \times 50) \times 100 = 25000 + 50000 = 75000$  multiplications!

• Problem Instance: A sequence of matrices  $A_1A_2...A_n$ ;

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- The t of bin https://eduassistpro.github.
  - recursion (why?):

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- One can show that the solution satisfies  $T(n) = \Omega(2^n)$ .
- Thus, we cannot do an exhaustive search for the optimal placement of the brackets.

• Problem Instance: A sequence of matrices  $A_1A_2...A_n$ ;

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- The s "gro https://eduassistpro.github."
- Note: this looks like it is a case of a "2D recursion, but we can ac with Aimple dinearly recursion. hat edu\_assist\_prediction."
- We group such subproblems by the value of j-i and perform a recursion on the value of j-i.
- At each recursive step m we solve all subproblems P(i,j) for which j-i=m.

• Let m(i,j) denote the minimal number of multiplications needed to compute the product  $A_iA_{i+1}...A_{j-1}A_j$ ; let also the size of matrix  $A_i$  be  $s_{i-1} \times s_i$ .

## Assiligation, in the claim notice of the principal (outermost elp

- Note that both k-i < j-i and j-(k+1) < j-i; thus we have the solutions of the subp
- Note https://eduassistpro.github.
- To multiplicate of the control of th

$$S_{i-1} = S_{i-1}$$

Total number of multiplications: S<sub>i-1</sub> S<sub>i</sub> S<sub>k</sub>

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- Not algo https://eduassistpro.github.
- k for which the minimum in the recursive definiti ieved can be stored to retrieve the obtimal placement of brassist\_problem.
- Thus, in the  $m^{th}$  slot of the table we are constructing we store all pairs (m(i,j),k) for which j-i=m.

• Assume we want to compare how similar two sequences of symbols S and  $S^*$  are.

# Assignment Project Exam Help • Example: how similar are the genetic codes of two viruses.

## Thi https://eduassistpro.github.

- A sequence s is a subsequence of a can be obtained by deleting some of the symbols of the arcel the remaining spirals | ECU\_assist\_pi
- Given two sequences S and  $S^*$  a sequence s is a **Longest** Common Subsequence of  $S, S^*$  if s is a common subsequence of both S and  $S^*$  and is of maximal possible length.

• Instance: Two sequences  $S = \langle a_1, a_2, \dots a_n \rangle$  and  $S^* = \langle b_1, b_2, \dots, b_m \rangle$ .

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- We first find the length of the longest common subsequence of  $S, S^*$ .
- "2D https://eduassistpro.github. $S_i = S_i = S_i$ " https://eduassistpro.github.
- Recursion: we fill the table row by row, so the ordering o lexicochapit; Orderly; eChat edu\_assist\_pr

$$c[i,j] = \begin{cases} 0, & \text{if } i = 0 \text{ or } j = 0; \\ c[i-1,j-1] + 1 & \text{if } i,j > 0 \text{ and } a_i = b_j; \\ \max\{c[i-1,j], c[i,j-1]\} & \text{if } i,j > 0 \text{ and } a_i \neq b_j. \end{cases}$$

Retrieving a longest common subsequence:

# Assignment Project Exam Help https://eduassistpro.github. Add WeChat edu\_assist\_properties.

• What if we have to find a longest common subsequence of three sequences  $S_1, S_2, S_3$ ?

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## https://eduassistpro.github.

LCS(LCS(
$$S_1, S_2$$
),  $S_3$ ) = LCS( $ABE$ 

LCS(LCS( $S_2, S_3$ ),  $S_1$ ) = LCS( $ACEF$ 

ACCIO( $S_1, S_2$ ),  $S_2$  = LCS( $ACEF$ 

ACCIO( $S_1, S_2$ ),  $S_3$  = LCS( $S_1, S_2$ )

But

$$LCS(S_1, S_2, S_3) = ACEG$$

• So how would you design an algorithm which computes correctly  $LCS(S_1, S_2, S_3)$ ?

• Instance: Three sequences  $S = \langle a_1, a_2, \dots a_n \rangle$ ,  $S^* = \langle b_1, b_2, \dots, b_m \rangle$  and  $\begin{array}{l} S^{**} = \langle c_1, c_2, \dots, c_k \rangle \\ \textbf{SSignment Project Exam Help} \\ \textbf{STasker ind a longest common subsequence of } S, S, S \end{array}$ 

- We a
- for a https://eduassistpro.github.  $S_j^* = \langle b_1, b_2, \dots, b_j \rangle \text{ and } S_l^{**} = \langle c_1, c_2, \dots, c \rangle$
- Recurrended WeChat edu\_assist\_preserved

$$d[i,j,l] = \begin{cases} 0, & \text{if } i = 0 \text{ or } j = 0 \text{ or } l = 0; \\ d[i-1,j-1,l-1] + 1 & \text{if } i,j,l > 0 \text{ and } a_i = b_j = c_l; \\ \max\{d[i-1,j,l],d[i,j-1,l],d[i,j,l-1]\} & \text{otherwise.} \end{cases}$$

#### Dynamic Programming: Shortest Common Supersequence

## $\begin{array}{l} \textbf{Instance:} \ \, \textbf{Two sequences} \ \, \textbf{Project} \ \, \textbf{Exam} \\ \textbf{SS1gnment} \ \, \textbf{Project} \ \, \textbf{Exam} \\ \textbf{Find a shortest common super-sequence} \end{array} \\ \begin{array}{l} \textbf{Sof } s, s^*, \text{ i.e., the shortest} \\ \textbf{Sof } s, s^*, \text{ i.e., the shor$

- possible sequence S such that both s and  $s^*$  are subsequences of S.
- \* sol https://eduassistpro.github.

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shortest super-sequence S = axbyacazda

#### Dynamic Programming: Edit Distance

• Edit Distance Given two text strings A of length n and B of length m, you want to transform A into B. You are allowed to insert a character, delete a character and to replace a distance with another one. An insertion color of the character and to replace the other colors and the character of the character

- Tas
- Not https://eduassistpro.github.
- If the equelices are signed as of DNA bases and the cost probabilities of the convergence of DNA bases and the cost as a signed probability that one sequence mutates into anot of DNA copying.
- Subproblems: Let C(i,j) be the minimum cost of transforming the sequence A[1..i] into the sequence B[1..j] for all  $i \leq n$  and all  $j \leq m$ .

#### Dynamic Programming: Edit Distance

• Subproblems P(i,j): Find the minimum cost C(i,j) of transforming the sequence A[1..i] into the sequence B[1..j] for all  $i \leq n$  and all  $j \leq m$ .

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## https://eduassistpro.github.

- $\cos t \, c_D + C(i-1,j)$  corresponds to the option if y  $A[1..i \ 1]$  it to B[1] and then delete A[i] cost C[1] to C[1
- B[1..j-1] and then append B[j] at the end;
- the third option corresponds to first transforming A[1..i-1] to B[1..j-1] and
  - if A[i] is already equal to B[j] do nothing, thus incurring a cost of only C(i - 1, j - 1):
  - $C(i-1, j-1) + c_R$ .

#### Dynamic Programming: Maximizing an expression

• Instance: a sequence of numbers with operations  $+, -, \times$  in between, for example

$$1 + 2 - 3 \times 6 - 1 - 2 \times 3 - 5 \times 7 + 2 - 8 \times 9$$

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- Wha
- May https://eduassistpro.github.
- maybe we could consider which the principal operations s

  A[i..k] AA[k+1j]. Here is what ever operation assist.

   Put when would such conversion by maximized if these could be provided in the country.
- But when would such expression be maximised if there coul negative values for A[i..k] and A[k+1..j] depending on the placement of brackets??
- Maybe we should look for placements of brackets not only for the maximal value but also for the minimal value!
- Exercise: write the exact recursion for this problem.

#### Dynamic Programming: Turtle Tower

A S state property in article is the maximal weight you can put on it without cracking its shell.

- \* top https://eduassistpro.github.
- Hint: Order turtles in an increasing order of the su their strength, and proceed by recursion.
- You can find a solution to this problem and of another in the class website (class resources, file "More Dynami

#### Dynamic Programming: Bellman Ford algorithm

- One of the earliest use of Dynamic Programming (1950's) invented by Bellman.
- Instance: A directed weighted graph G = (V, E) with weights which can be ASSIGNIFIED POSETIVE to the law of the and a vertex F Posetive to the law of the shortest path from vertex s to every other vertex t.
  - https://eduassistpro.github.
  - Thu
  - Subproblems: For very v (find every the least of a horse from at edu\_assist\_p) be
  - Our goal is to find for every vertex  $t \in G$  the value of opt(n-1,t) and the path which achieves such a length.
  - Note that if the shortest path from a vertex v to t is  $(v, p_1, p_2, \ldots, p_k, t)$  then  $(p_1, p_2, \ldots, p_k, t)$  must be the shortest path from  $p_1$  to t, and  $(v, p_1, p_2, \ldots, p_k)$  must also be the shortest path from v to  $p_k$ .

## Dynamic Programming: Bellman Ford algorithm

• Let us denote the length of the shortest path from s to v among all paths which contain at most i edges by  $\operatorname{opt}(i,v)$ , and let  $\operatorname{pred}(i,v)$  be the immediate predecessor of vertex v on such shortest path.

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- Final solutions: p(n-1, v) for all  $v \in G$ .
- Computation of t(i) was a time at | edu\_assist for present v, min is taken over all edges e(p,v) in edges are inspected.
- ullet Algorithm produces shortest paths from s to every other vertex in the graph.
- The method employed is sometimes called "relaxation", because we progressively relax the additional constraint on how many edges the shortest paths can contain.

#### Dynamic Programming: Floyd Warshall algorithm

• Let again G = (V, E) be a directed weighted graph where  $V = \{v_1, v_2, \dots, v_n\}$  and where weights  $w(e(v_p, v_q))$  of edges  $e(v_p, v_q)$  can be negative, but there are no negative weight cycles.

# Assignment inharided betain the shortest paths from everly vertex $v_p$ to every vertex $v_q$ (including back to $v_p$ ).

- $^{\circ}$   $^{\text{Let o}}_{\text{vert}}$   $^{\circ}$  https://eduassistpro.github.
- Then opt Add mWpeChatpedu\_assist $v_q$ ) or
- Thus, we gradually **relax** the constraint that the intermediary vertices have to belong to  $\{v_1, v_2, \ldots, v_k\}$ .
- Algorithm runs in time  $|V|^3$ .

#### Another example of relaxation:

• Compute the number of partitions of a positive integer n. That is to say the number of distinct multi-sets of positive integers  $\{n_1, \ldots, n_k\}$  which sum up to n, i.e., such that  $n_1 + \ldots + n_k = n$ .

As significant that the excent are swellowing of elements count as a single multi-set.

https://eduassistpro.gitmeb.

We are looking for nump(n, n) but the recursion is based on relaxation of the allowed size i of the parts of j for all

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## Assignment Project Exam Help

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