#### **COMP3141**

Software System Design and Implementation

#### SAMPLE EXAM

Term 2, 2020

- Total Number of Parts: 5.
- Total Number of Marks: 125
- All parts are of equal value.
- Answer **all** questions.
- Excessively verbose answers may lose marks
- Failure to make the declaration or making a false declaration results in a 100% mark penalty.
- Ensure you are the person listed on the declaration.
- All questions must be attempted **individually** without assistance from anyone else.
- Late submissions will not be accepted.
- You may save mult ubmission will be considered.
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### Declaration Add WeChat edu\_assist\_pro

■ I, name, declare that these answers are **entirely my own**, and that I did not complete this exam with assistance from anyone else.

#### Part A (25 Marks)

Answer the following questions in a couple of short sentences. No need to be verbose.

1. (3 Marks) What is the difference between a partial function and partial application?

A partial function is a function not defined for its whole domain, whereas partial application is where a n-argument function is applied to fewer than n values.

2. (3 Marks) Name *two* methods of measuring program coverage of a test suite, and explain how they differ.

Function coverage measures whether or not a given function is executed by the test suite, whereas path coverage measures all possible execution paths. Function coverage is easier to compute than path coverage.

3. (3 Marks) How are multi-argument functions typically modelled in Haskell?
Mutliple argument functions are usually modelled by one-argument functions that in turn return functions to accept further arguments. For example, the add function $(+)$ :: Int $\rightarrow$ (Int $\rightarrow$ Int) takes an Int and returns a function.
4. (3 Marks) Is the type of getChar below a pure function? Why or why not?
getChar::IO Char
It is not a pure function, but not because it is impure, but because it is not a function. It is instead an IO procedure.
Assignment Project Exam Help 5. (3 Marks) What is a functional correctness specification?
A functional cor https://eduassistpro.githpletby.spoify the definition of data invariants and a refinement from an abst  Add WeChat edu_assist_pro
6. (3 Marks) Under what circumstances is performance important for an abstract model?
If we are testing using an abstract model (for example with QuickCheck), then we are still computing with it and thus intractable or uncomputable abstract models would not be suitable.
7. (3 Marks) What is the relevance of termination for the Curry-Howard correspondence?
The Curry-Howard correspondence assumes that function types are pure and total. Non-termination makes the logic the type system corresponds to inconsistent.
8. (4 Marks) Imagine you are working on some price tracking software for some company

8. (4 Marks) Imagine you are working on some price tracking software for some company stocks. You have already got a list of stocks to track pre-defined.

Your software is required to produce regular reports of the stock prices of these companies. Your co-worker proposes modelling reports simply as a list of prices:

Where each price in the list is the stock price of the company in the corresponding position of the *stocks* list. How is this approach potentially unsafe? What would be a safer representation?

It is not guaranteed that the prices will line up to the stocks, or that there will be a stock for every price and a price for every stock. An alternative would be:

which at least ensures that the right stocks are associated with the right price.

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# Part B (25 Marks) / eduassist pro.github.io/

The following questions pertain to the given Haskell

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foldr 
$$fz(x:xs) = fx(\text{foldr } fz(xs))$$
 -- (1)  
foldr  $fz[] = z$  -- (2)

1. (3 Marks) State the type, if one exists, of the expression foldr (:) ([]:: [Bool]).

```
[Bool] \to [Bool]
```

2. (4 Marks) Show the evaluation of foldr (:) [] [1, 2] via equational reasoning.

```
foldr (:) [] [1, 2]

= 1: (foldr (:) [] [2]) (1)

= 1:2: (foldr (:) [] []) (1)

= 1:2: [] (2)
```

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3. (2 1	Marks) In your own words, describe what the function foldr (:) [] does.		
It	It is the identity function on lists.		
4. (12	Marks) We shall prove by induction on lists that, for all lists xs and ys:		
	foldr(:) xs ys = ys ++ xs		
	i. (3 Marks) First show this for the base case where ys = [] using equational reasoning.  You Assign the Little Project + Electric Project + Elect		
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i	i. (9 Marks) Next, we have the case where $ys = (k: ks)$ for some item $k$ and list $ks$ .  a. (3 Marks) What is the <i>inductive hypothesis</i> about $ks$ ?		
	foldr (:) xs ks = ks ++ xs		
	b. (6 Marks) Using this inductive hypothesis, prove the above theorem for the inductive case using equational reasoning.		

```
foldr (:) xs (k: ks) = (:) k (foldr (:) xs ks) (1)

= k: (foldr (:) xs ks) simp

= k: (ks ++ xs) I.H

= (k: ks) ++ xs def. of (++)
```

5. (2 Marks) What is the time complexity of the function call foldr (:) [] xs, where xs is of size *n*?

```
\mathcal{O}(n)
```

6. (2 Marks) What is the time complexity of the function call foldr (\(\hat{a} a \) \(\hat{B} \) as the time complexity of the function call foldr (\(\hat{a} a \) \(\hat{B} \) \(\hat{B} \) as the p as the p are the p

#### Part C (25 Marks)

A *sparse vector* is a vector where a lot of the values in the vector are zero. We represent a sparse vector as a list of position-value pairs, as well as an Int to represent the overall length of the vector:

We can convert a sparse vector back into a dense representation with this expand function:

expand:: SVec 
$$\rightarrow$$
 [Float]  
expand (SV  $n$  vs) = map check [0.  $n - 1$ ]  
where  
check  $x = \mathbf{case}$  lookup  $x$  vs of  
Nothing  $\rightarrow$  0  
Just  $y \rightarrow y$ 

For example, the SVec value SV 5 [(0, 2.1), (4, 10.2)] is expanded into [2.1, 0, 0, 0, 10.2]

1. (16 Marks) There are a number of SVec values that do not correspond to a meaningful vector - they are invalid.

i. (6 Marks) Which two *data invariants* must be maintained to ensure validity of an SVec value? Describe the invariants in informal English.

For a value SV n vs, the list vs should contain only one value for a given position, and the positions of all values in vs should all be  $\geq 0$  and  $\leq n$ .

ii. (4 Marks) Give two examples of SVec values which violate these invariants.

Violates "only one value for a position": SV 2 [(1, 1.1), (1, 5.3)] Violates "all positions  $\geq 0$  and < n": SV 2 [(3, 1.1)]

Assignment Project Exam Help
iii. (6 Marks) Define a Haskell function werformed:: SVec → Bool which returns True iff

iii. (6 Marks) Define a Haskell function wellformed:: SVec → Bool which returns True iff the data inva

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You may find from a list.

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wellformed (SV n vs)  $= \mathbf{let} \text{ ps} = \text{map fst vs}$   $\mathbf{in} \text{ all } (\lambda x \to x \ge 0 \&\& x < n) \text{ ps}$  && nub ps == ps

2. (9 Marks) Here is a function to multiply a SVec vector by a scalar:

vsm:: SVec 
$$\rightarrow$$
 Float  $\rightarrow$  SVec  
vsm (SV  $n$  vs)  $s =$  SV  $n$  (map  $(\lambda(p, v) \rightarrow (p, v * s))$  vs)

i. (3 Marks) Define a function vsmA that performs the same operation, but for dense vectors (i.e. lists of Float).

$$vsmA xs s = map (* s) xs$$

ii. (6 Marks) Write a set of properties to specify *functional correctness* of this function. *Hint*: All the other functions you need to define the properties have already been mentioned in this part. It should maintain data invariants as well as refinement from the abstract model.

Data invariants:

wellformed xs  $\implies$  wellformed (vsm xs s)

Data refinement:

expand (vsm xs s) == vsmA (expand xs) s

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#### Part D (25 Marks)

1. (10 Marks) Imagine you are working for a company that maintains this library for a database of personal records, about their customers, their staff, and their suppliers.

**newtype** Person = ...

name:: Person  $\rightarrow$  String

salary:: Person → Maybe String

fire:: Person  $\rightarrow$  IO ()

company:: Person  $\rightarrow$  Maybe String

The salary function returns Nothing if given a person who is not a member of company staff. The fire function will also perform no-op unless the given person is a member of company staff. The company function will return Nothing unless the given person is a supplier.

Rewrite the above type signatures to enforce the distinction between the different types of person statically, within Haskell's type system. The function name must work with all kinds of people as input.

*Hint*: Attach *phantom* type parameters to the Person type.

```
data Staff
data Customer
data Supplier
newtype Person t = \dots
name:: Person t \to String
-- Maybe no longer needed here:
salary:: Person Staff \to String
fire:: Person Staff \to IO()
-- Maybe no longer needed here:
company:: Person Supplier \to String
```

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2. (15 Marks) Consid https://eduassistpro.github.io/

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```
Cons :: a \to \text{List } a \to \text{List } a

data Nat = Z \mid S Nat

data Vec (n :: \text{Nat}) a where

VNil :: Vec Z a

VCons :: a \to \text{Vec } n a \to \text{Vec } (S n) a
```

What is the difference between these types? In which circumstances would Vec be the better choice, and in which List?

Vec tracks its length in the type level, whereas List does not. Usually, one would only use Vec if one frequently needed to express static pre-conditions about the length of the list. This way, the type checker can ensure these preconditions are met automatically.

i. (5 Marks)

ii. (5 Marks) Here is a simple list function:

zip::List 
$$a \to \text{List } b \to \text{List } (a, b)$$
  
zip Nil ys = Nil  
zip xs Nil = Nil  
zip (Cons x xs) (Cons y ys) = Cons (x, y) (zip xs ys)

Define a new version of zip which operates on Vec instead of List wherever possible. You can constrain the lengths of the input.

# Assignmente Project, Exam Help zip VNil ys = VNil zip https://eduassistpro.githubyio/

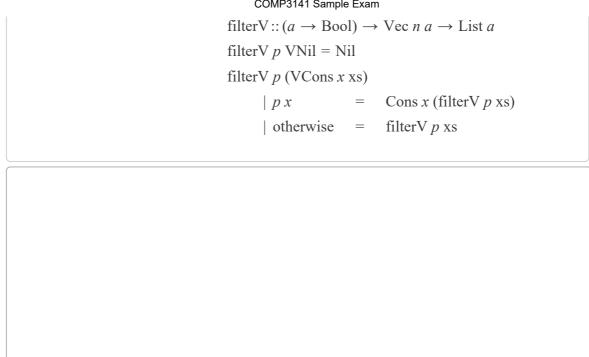
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iii. (5 Marks) Here is another list function:

filter:: 
$$(a \to Bool) \to List \ a \to List \ a$$
  
filter  $p \ Nil = Nil$   
filter  $p \ (Cons \ x \ xs)$   
 $| \ p \ x = Cons \ x \ (filter \ p \ xs)$   
 $| \ otherwise = filter \ p \ xs$ 

Define a new version of filter which operates on Vec instead of List wherever possible.

We can't return a Vec because we don't know how long it will be.



#### Part E (25 Marks)

sequenced does not matter. In addition to the normal applicative laws, a commutative applicative functo

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. (2 Marks) Is the Maybe Applicative instanc Add WeChat edu_			
Yes. If either $u$ or $v$ are Nothing, the result	es of the law. If		
both are not Nothing, then the result is <i>f</i> applied to their contents.			

ii. (3 Marks) We have seen two different Applicative instances for lists. Which of these instances, if any, are commutative? Explain your answer.

The ZipList instance obeys the law above - the size is the minimum of the two input lists, and each element is combined with *f* in the same order. The combinatorial instance does not. For example if u = [2, 3] and v = [4, 5] and f = (\*), then the left hand side of the law is [8, 10, 12, 15] and the right hand side gives us [8, 12, 10, 15] - they are different.

iii. (5 Marks) A *commutative* monad is the same as a commutative applicative, only specialised to monads. Express the commutativity laws above in terms of monads, using either **do** notation or the raw pure/bind functions.

do  $x \leftarrow u$   $y \leftarrow v$  pure (f x y) = do  $y \leftarrow v$ 

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2. (10 Marks) Translate the following logical formulae into types, and provide Haskell types that correspond to proofs of these formulae, if one exists. If not, explain why not.

i. (2 Marks)  $(A \lor B) \rightarrow (B \lor A)$ 

```
f:: (Either A B) \rightarrow (Either B A)
f(Left x) = Right x
f(Right x) = Left x
```

ii. (2 Marks)  $(A \lor A) \rightarrow A$ 

$$f:: (Either A A) \rightarrow A$$
  
 $f(Left x) = x$   
 $f(Right x) = x$ 

iii. (3 Marks)  $(A \land (B \lor C)) \rightarrow ((A \land B) \lor (A \land C))$ 

$$f:: (A, (Either B C)) \rightarrow (Either (A, B) (A, C))$$
  
 $f(a, Left x) = Left (a, x)$   
 $f(a, Right x) = Right (a, x)$ 

# Assignment Project Exam Help iv. (3 Marks) $\neg$ (( $A \rightarrow \bot$ ) $\lor$ A)

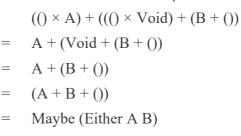
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This function cannot be implemented in ed lambda calculus as in the the weather attached assiste confrontive logics do not admit the law of the exclud

3. (5 Marks) Here is a Haskell data type:

Using known type isomorphisms, simplify this type as much as possible.

This is equivalent to (using plus for Either and times for products):



#### **END OF SAMPLE EXAM**

(don't forget to save!)

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