# Assignment Project Exam Help

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Recap: Induction

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Suppose we want t

Remember that t

Definition of https://eduassistpro.github.io/

O is a natural number.

For any natural number.

Tispalso a natural number assist\_pro

# **Recap: Induction**

Therefore, to show P(n) for all n, iPuffices to show: Exam Help

**2** assuming P(k) (the *inductive hypothesis*),

 $\Rightarrow P(k +$ 

#### **Example**

Induction

0000

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Show that  $f(n) = n^2$  for all  $n \in \mathbb{N}$ , where:

 $Add_{f(n)} = \begin{cases} Chat \ edu\_assist\_pro \\ 2n-1+f(n-1) & \text{if } n>0 \end{cases}$ 

(done on iPad)

#### Induction on Lists

# Hask Assignment Projects Exam Help

#### **Definition of Ha**

- © [] is a list. https://eduassistpro.github.io/

#### Induction on Lists

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#### **Definition of Ha**

- © [] is a list. https://eduassistpro.github.io/

This means, if we want to prove that a property

1s. it suffices

o show: Add WeChat edu\_assist\_pro

- P(x:xs) for all items x, assuming the inductive hypothesis P(xs).

## **Induction on Lists: Example**

```
Assignment Project Exam Help
sum (x:xs) = x + sum xs -- 2
```

```
foldr :: (a https://eduassistpro.github.io/
foldr f z (x:xs) = x f foldr f z xs
```

```
Add WeChat edu_assist_pro
Prove for all 1s.
```

```
sum ls == foldr (+) 0 ls
```

(done on iPad)

Induction

000

type Colour = (Int, Int, Int, Int) -- RGBA

### **Custom Data Types**

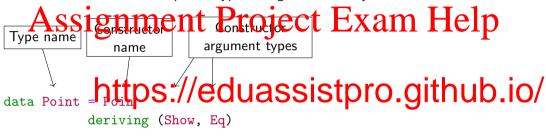
```
So face present the project of the p
```

```
movePoint :: Aid by echat edu_assist_pro
```

But these definitions allow Points and Vectors to be used interchangeably, increasing the likelihood of errors.

# **Product Types**

We can define our own compound types using the data keyword:



data Vector Actor FWt Cathat edu\_assist\_pro

```
movePoint :: Point -> Vector -> Point
movePoint (Point x y) (Vector dx dy)
= Point (x + dx) (y + dy)
```

#### Records

But this has so many

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#### Records

# 

But this has so many

Haskell lets us decition style on the previous hittps://eduassistpro.github.io/

```
Add , we chart edu_assist_pro

Add , opacityC :: Int

| deriving (Show, Eq)
```

Here, the code redC (Colour 255 128 0 255) gives 255.

### **Enumeration Types**

Similars singinment we Paroject that am a Helphefined values:

data LineStyl

https://eduassistpro.github.io/

deriving (Show, Eq)

data FillSty Addid We Cornat edu\_assist\_proderiving (Show, Eq)

Types with more than one constructor are called *sum types*.

## **Algebraic Data Types**

type Picture = [PictureObject]

## **Live Coding: Cool Graphics**

# Examples Assignment Project Exam Help

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### **Recursive and Parametric Types**

Assignment Project Exam Help Data types can be defined with parameters, such as the well known Maybertype, defined in the stan

https://eduassistpro.github.io/

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Types can also https://eduassistpro.github.io/could define them ourselves:

```
\overset{\scriptscriptstyle \text{data List a}}{Add}\overset{\scriptscriptstyle \text{=-Nil}}{We}\overset{\scriptscriptstyle \text{(List a)}}{Chat}\,edu\_assist\_pro
```

### **Recursive and Parametric Types**

Assignment Project Exam Help Data types can be defined with parameters, such as the well known Maybertype, defined in the stan

Types can also https://eduassistpro.github.io/could define them ourselves:

```
data List a = Nil | Cons a (List a)
We can even define four al Number Cwart is edulas assistro)

data Natural = Zero | Succ Natural
```

## **Types in Design**



# An Assignmenty Projectis Exam Help

Make illegal states unrepresentable.

Choose types that ttps://eduassistpro.github.io/

# Types in Design

#### Sage Advice

# An Assignmenty Projectis Exam Help

Make illegal states unrepresentable.

Choose types that ttps://eduassistpro.github.io/

#### **Example (Contact Details)**

 $\begin{array}{c} {}^{\tt data\ Contact}} A^{\tt Contact} A^{\tt Contact} & \\ {}^{\tt date\ We} & \\ \end{array} \\ \begin{array}{c} {}^{\tt data\ Contact}} & {}^{\tt date\ Unit} & \\ {}^{\tt data\ Contact}} & \\ {}^{\tt data\$ 

What failure state is eliminated here? Liam: also talk about other famous screwups

#### Partial Functions

Failure to follow Yaron's excellent advice leads to partial functions.

# A partial function is a function not defined for all possible inputs.

Examples: hea

Partial function https://eduassistpro.github.io/

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Partial function https://eduassistpro.github.io/ undefined cases a

To eliminate partiality, we must either:

```
• enlarge the Addidn, Wille Charge edu_assist_pro
 safeHead (x:xs) = Just x
 safeHead []
               = Nothing
```

#### Partial Functions

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# A partial function is a function not defined for all possible inputs.

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Partial function https://eduassistpro.github.io/

To eliminate partiality, we must either:

- enlarge the Adelhaln, Walls of have edu\_assist\_pro safeHead (x:xs) = Just xsafeHead [] = Nothing
- Or we must constrain the domain to be more specific:

```
safeHead' :: NonEmpty a -> a -- Q: How to define?
```

## Type Classes

# You Assignment Project Exam Help

- compare
- (==)
- https://eduassistpro.github.io/ • (+)
- show

that work on multiple types, and their corresponding constra Eq. Num and Shand WeChat edu assist pro

## Type Classes

# You Assignment Project Exam Help

- compare
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- https://eduassistpro.github.io/ • (+)
- show

that work on multiple types, and their corresponding constrating the contract of the contract

These constraints are called *type classes*, and can be t which certain operations are implemented.

#### Show

The Show type class is a set of types that can be converted to strings. It is defined like: classes is a set of types that can be converted to strings. It is defined like: show :: a String

https://eduassistpro.github.io/

#### Show

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```
clas Assignment Project Exam Help
```

Types are added to t

```
instance Shopttps://eduassistpro.github.io/show False = "False"
```

#### Show

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Types are added to t

```
instance Sho https://eduassistpro.github.io/
 show False = "False"
```

We can also define instances that depend on other instances: assist\_pro instance Show and the control of the co show (Just x) = "Just " ++ show x

show Nothing = "Nothing"

Fortunately for us, Haskell supports automatically deriving instances for some classes, including Show.

Assignment Project Exam Help
Type classes capalso overload based on the type returned, unlike similar features like
Java's interfaces

read :: Stattps://eduassistpro.github.io/
Some examples:

\* read "34" -:- Int Add WeChat edu\_assist\_pro

Assignment Project Exam Help
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read :: Stattps://eduassistpro.github.io/ Some examples:

- $\begin{array}{l} \bullet \text{ read "34"} & \text{ i.i. Int. We Chat edu\_assist\_pro} \\ \bullet \text{ read "22"} & \text{A:dG} \end{array}$

Assignment Project Exam Help
Type classes capalso overload based on the type returned, unlike similar features like
Java's interfaces

read :: Stattps://eduassistpro.github.io/

- read "34" :: Int we Chat edu\_assist\_pro
- show (read "34") :: String

Assignment Project Exam Help
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Java's interfaces

read :: Stattps://eduassistpro.github.io/
Some examples:

- read "34" :: Int we Chat edu\_assist\_pro
- show (read "34") :: String Type error!

## Semigroup

#### **Semigroups**

A seAssignmentanProject: Exampletelpation

https://eduassistpro.github.io/

# Semigroup

#### Semigroups

A seAssignmentan Project: Example telepation

Associativity is de

https://eduassistpro.github.io/

Haskell has a type of the programmer discipline:

Haskell has a type of the programmer discipline:

Haskell has a type of the programmer discipline:

class  $\operatorname{Semigroup} s$  where

```
(<>) :: s -> s -> s
-- Law: (<>) must be associative.
```

What instances can you think of?

## Semigroup

# Lets Assignment ix Project Exam Help

instance Semigroup Colour where Colour r1 g1 b1 a

\* colohttps://eduassistpro.github.io/

(mix b1 b2)

nere Add WeChat edu\_assist\_pro

Observe that associativity is satisfied.

#### Monoid



https://eduassistpro.github.io/ Add WeChat edu\_assist\_pro

#### Monoid

#### **Monoids**

A mais is a graph enterprovious field that  $x \cdot z = x$  and  $z \cdot y = y$  for all x, y.

```
Add WeChat edu assist pro
```

#### Monoid

#### **Monoids**

A majorisa gramment en equipped to be controlled by that  $x \cdot z = x$  and  $z \cdot y = y$  for all x, y.

class (Semigr

mempty:: https://eduassistpro.github.io/

instance Monoid Colour where

mempty = Copyright We Chat edu\_assist\_pro
For each of the semigroups discussed previously:

- Are they monoids?
- If so, what is the identity element?

## Monoid

## **Monoids**

A majorisa grannented provide sterilization and  $z \cdot y = y$  for all x, y.

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Are there any semigroups that are not monoids?

## Monoid

#### **Monoids**

A majerisa entrope property contains that  $x \cdot z = x$  and  $z \cdot y = y$  for all x, y.

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# The Assignment of Project Exam: Help

- The operation (+) is associative, with identity element 0
- The operati

https://eduassistpro.github.io/

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Haskell doesn't https://eduassistpro.github.io/class in the entire pr

A common technique is to teine a ceptrate type that is represented by the common type, but can have its own, different type class instance SSIST\_Pro

# The Assignment of Project Exam: Help

- The operation (+) is associative, with identity element 0
- The operati

Haskell doesn't https://eduassistpro.github.io/class in the entire pr

A common technique is to teine a ceptate type that is represent type, but earn have its own, different type lass instance. SSIST\_Pro

In Haskell, this is done with the newtype keyword.

A newtype declaration is much like a data declaration except that there can be only one constituting the like exactly of a current. Xam Help newtype Score = S Integer

instance Sembttos://eduassistpro.github.io/

```
instance Monoid Score where
mempty = SAdd WeChat edu_assist_pro
Here, Score is represented identically to Integ
incurred to convert between them.
```

In general, newtypes are a great way to prevent mistakes. Use them frequently!

```
Ord iA type class for inequality coparison that the last of the class for inequality coparison to the last of the class of the class for inequality coparison to the class of the class of
```

What laws should i

https://eduassistpro.github.io/

Ord iA type lass for inequality copyrisor Exam Help

(<=) :: a -> a -> Bool

What laws should i

For all x, y, an https://eduassistpro.github.io/

• Reflexivit x <= x</p>

Ord iA type class for inequality coparison ect Exam Help

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- \*\*Transitivity: If x <= y and y <= z then x < du\_assist\_pro

Ord iA System Help (<=) :: a -> a -> Bool

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Ord iA System Help

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- **1** Totality: Either  $x \le y$  or  $y \le x$

# Ord iA SSignment Project Exam Help

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For all x, y, an https://eduassistpro.github.io/

(<=) :: a -> a -> Bool

- Transitivity: If x <= y and y <= z then x </li>
   Antisymmetry: Old <= Ward C = haten edu\_assist\_pro</li>
- **1** Totality: Either  $x \le y$  or  $y \le x$

Relations that satisfy these four properties are called total orders. Without the fourth (totality), they are called partial orders.

Eq is a type class for equality or equivalence:



What laws should i

https://eduassistpro.github.io/

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What laws should i

For all x, y, and https://eduassistpro.github.io/

Eq is a type class for equality or equivalence:

```
clas Arssignment Project Exam Help
```

#### What laws should i

- For all x, y, and https://eduassistpro.github.io/
  - 2 Transitivity: If x == y and y == z then x == y

Eq is a type class for equality or equivalence:

```
clas Assignment Project Exam Help
```

#### What laws should i

- For all x, y, and https://eduassistpro.github.io/
  - 2 Transitivity: If x == y and y == z then x =
  - Symmetry: Atdd WeChat edu\_assist\_pro

Eq is a type class for equality or equivalence:

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#### What laws should i

- For all x, y, and https://eduassistpro.github.io/
  - 2 Transitivity: If x == y and y == z then x == y

Eq is a type class for equality or equivalence:

#### What laws should i

- For all x, y, and https://eduassistpro.github.io/
  - 2 Transitivity: If x == y and y == z then x =

Some argue that the Eq class should be only for equality, requiring stricter laws like:

If x == y then f x == f y for all functions f

But this is debated.

# **Types and Values**

# Assignment Project Exam Help

Haskell is actually

• The value https://eduassistpro.gith@tb.io/

# **Types and Values**

# Assignment Project Exam Help

Haskell is actually

- The value https://eduassistpro.githth.io/
  - and type *constructors* like Maybe, (->), []

# **Types and Values**

# Assignment Project Exam Help

Haskell is actually

- The value https://eduassistpro.githth.io/
  - The type- like String, and type constructors like Maybe, (->), []

This type level Aguage its What the control is type level land the control is type level land the control is type level land to the control in the control is type level land to the control in the control is type level land to the control in the control is type level land to the control in the control is type level land to the control in the control is type level land to the control in the control is type level land to the control in the

### **Kinds**

# Assignment Project Exam Help

Just as terms in the v
language are give
The most basic rittps://eduassistpro.github.io/

- Types such a
- Seeing as Maybe is parameterised by one argume

  given a type eg (ht) with etu natipe edu\_assist\_pro

### Lists

# Sup Assignment Project Exam Help

toString :: Int -> String

And we also have a fu

getNumbers: https://eduassistpro.github.io/

How can I compose toString with getNumbers to get a function f of type Seed ->

[String]?

## Lists

# Supples Signment Project Exam Help

```
toString :: Int -> String
```

And we also have a fu

getNumbers: https://eduassistpro.github.io/

How can I compose toString with getNumbers to get a function f of type Seed ->

[String]?

Answer: we use map: Add WeChat edu\_assist\_pro

f = map toString . getNumbers

# Maybe

# Supple Signment Project Exam Help to String :: Int -> String

And we also have a fu

tryNumber :: https://eduassistpro.github.io/
How can I compose

Maybe String?

# Maybe

# Supples ignment Project Exam Help to String :: Int -> String

And we also have a fu

tryNumber :: https://eduassistpro.github.io/
How can I compose
Maybe String?

We want a map fund double Chate edu\_assist\_pro

f = maybeMap toString . tryNumber

Let's implement it.

#### Functor

```
All of these functions are in the interface of a single type class, called Functor.

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fmap :: (a -> b) -> f a -> f b
```

https://eduassistpro.github.io/

#### **Functor**

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Unlike previous t
of kind \* -> \*https://eduassistpro.github.io/

## **Functor**

```
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Assignment Project Exam Help

fmap :: (a -> b) -> f a -> f b
```

Unlike previous t
of kind \* -> \*https://eduassistpro.github.io/

Instances for:

- Lists
- Add WeChat edu\_assist\_pro
- Tuples (how?)
- Functions (how?)

Demonstrate in live-coding

### **Functor Laws**

# Assignment Project Exam Help

#### Functor Laws

- - Add WeChat edu\_assist\_pro

### **Functor Laws**

# Assignment Project Exam Help

#### **Functor Laws**

- In Haskell's type system it's impossible to make a total first law but violated lesective. Chat edu\_assist\_pro

This is due to *parametricity*, a property we will return to in Week 8 or 9

## Homework

# Assignment Project Exam Help

- be due in https://eduassistpro.github.io/

  Last week's Do the first pr
- This week's quiz is also up, due next friday (the friday after the Add WeChat edu\_assist\_pro