

# Assignment Project Exam Help

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## Motivation

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We'll be looking at t

- used in funct
- increasing

Unlike many other languages, these abstractions are reified i  
in Haskell, where they are often left as mere "design patterns" in o  
languages.

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## Kinds

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Recall that terms in the type level language of Haskell are given *kinds*.

The most basic kind

- Types such as

- Seeing as `Maybe`

`Maybe`      `nd * -> *`

given a type (e.g. `Int`), it will return a type (

**Question:** What's the kind of `State`?

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## Functor

Recall the type class defined over type constructors called `Functor`.

```
class Functor f where  
  fmap :: (a -> b) -> f a -> f b
```

### Functor Laws

- 1 `fmap id == id`
- 2 `fmap f . fmap g == fmap (f . g)`

We've seen instances for lists, Maybe, tuples and fun

Other instances include:

- IO (how?)
- State s (how?)
- Gen

Demonstrate in live-coding

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## QuickCheck Generators

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Recall the Arbitrary class has a function:

```
arbitrary :: Gen
```

The type Gen  
function:

```
toString :: Int -> String
```

And we want a generator for String (i.e. Gen String)  
toString to arbitrary Ints.  
Then we use fmap!

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## Binary Functions

Suppose we want to look up a student's zID and program code using these functions:

```
lookupID :: Name -> Maybe ZID
lookupProgr
```

And we had a function

```
makeRecord :: ZID
```

How can we combine these functions to get a function of type  
Name -> Maybe StudentRecord?

```
lookupRecord :: Name -> Maybe StudentRecord
lookupRecord n = let zid      = lookupID n
                  program = lookupProgram n
                  in ?
```

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## Binary Map?

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We could imagine a binary version of the `maybeMap` function.

```
maybeMap2 :: (a -  
              -
```

But then, we might

```
maybeMap3 :: (a -> b -> c -> d)  
              -> Maybe a -> Maybe b -> Maybe c -> Maybe d
```

Or even a 4-ary version, 5-ary, 6-ary ..

this would quickly become impractical!

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## Using Functor

Using fmap gets us part of the way there:

```
lookupRecord :: Name -> Maybe (Program -> StudentRecord)
lookupRecord n = let zid      = lookupID n
```

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But, now we have a function inside a Maybe.

We need a function to take:

- A Maybe-wrapped fn Maybe (Program -> Stude
- A Maybe-wrapped argument Maybe Program

And apply the function to the argument, giving us a result of type  
Maybe StudentRecord?

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## Applicative

This is encapsulated by a subclass of Functor called Applicative:

```
class Functor f => Applicative f where
```

```
  pure :: a -> f a
```

```
  (<*>) :: f (a -> b) -> f (a -> b)
```

Maybe is an instance of Applicative

```
lookupRecord :: Name -> Maybe StudentRecord
```

```
lookupRecord n = let zid = lookupID n
                  program = lookupProgram zid
                  in fmap makeRecord zid <*> program
    -- or pure makeRecord <*> zid <*> program
```

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## Using Applicative

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In general, we can take a regular function application:

And apply that function to a list of values, using this pattern (where `<*>` is left-associative):

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`pure f <*> ma <*> mb <*> mc <*> md`

## Relationship to Functor

All law-abiding instances of `Applicative` are also instances of `Functor` by defining:

```
fmap f x = pure f <*> x
```

Sometimes this is written as an infix operator, `<$>`, which allows us to write:

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as:

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```
f <$> ma <*> mb <*> mc <*> md
```

**Proof exercise:** From the applicative laws (next slide), prove that this implementation of `fmap` obeys the functor laws.

## Applicative laws

```
-- Identity
```

```
pure id <*> v = v
```

```
-- Homomorphi
```

```
pure f <*> pure x = pur
```

```
-- Interchange
```

```
u <*> pure y = pure ($ y) <*> u
```

```
-- Composition
```

```
pure (.) <*> u <*> v <*> w = u <*> (v <*> w)
```

These laws are a bit complex, and we certainly don't expect you to memorise them, but pay attention to them when defining instances!

## Applicative Lists

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There are **two** ways to implement Applicative for lists.

`(<*>) :: [a -> b] -> [a`

- 1 Apply each of the functions in the list to all the result arguments.
- 2 Apply each function in the list of functions to the corresponding arguments.

**Question:** How do we implement pure?

The second one is put behind a newtype (ZipList) in the Haskell standard library.

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## Other instances

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- QuickCheck generators: Gen
- Recall from Wednesday Week 4:

```
data Concr
```

```
derivi
```

```
instance Arbitrary Concrete where
```

```
arbitrary = C <$> arbitrary <*> arbitrary
```

- Functions:  $((\rightarrow) x)$
- Tuples:  $((,) x)$  We can't implement pure without an extra constraint!
- IO and State  $s$ :

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## On to Monads

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- Functors are types for containers where we can map pure functions on their contents.

- Applicative functors are containers with a  $n$ -ary function.

The last and most common is the Monad.

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### Monads

Monads are types  $m$  where we can *sequentially compose*

$b$

$a \rightarrow m$

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## Monads

```
class Applicative m => Monad m where  
  (>-) :: m a -> (a -> m b) -> m b
```

Sometimes in old documentation the function return is included here, but it is just an alias for pure. It

Consider for:

- Maybe
- Lists
- $(x \rightarrow)$  (the `Reader` monad)
- $(x,)$  (the `Writer` monad, assuming a `Monoid` instance for `x`)
- Gen
- IO, State `s` etc.

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## Monad Laws

We can define a composition operator with ( $\gg$ ):

$(\leq\leq) :: (b \rightarrow m\ c) \rightarrow (a \rightarrow m\ b) \rightarrow (a \rightarrow m\ c)$

$(f \leq\leq g)\ x = g\ x \gg f$

### Monad Laws

$f \leq\leq (g \leq\leq x) == (f \leq\leq g) \leq\leq x$  *-- associativity*

$\text{pure} \leq\leq f == f$  *-- l*

$f \leq\leq \text{pure} == f$  *-- r*

These are similar to the monoid laws, generalised for multiple types inside the monad.  
This sort of structure is called a *category* in mathematics.

## Relationship to Applicative

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All Monad inst

in terms of >>

`mf <*> mx = mf >>= \f -> m`

n define <\*>

This implementation is already provided for Mon

`Control.Monad`

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## Do notation

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Working directly with the monad functions can be unpleasant.  
As we've seen, Haskell has some notation to increase niceness:

```
do x  
  z
```

```
do x  
  y
```

becomes

```
x >
```

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We'll use this for most of our examples.

## Examples

### Example (Dice Rolls)

Roll two 6-sided dice, if the difference is  $< 2$ , reroll the second die. Final score is the difference of the two

### Example (Part)

We have a list of student names in a database of type  $[(ZID, Name)]$ . Given a list of  $zID$ 's, return a  $Maybe [Name]$ , where  $Nothing$  if no student is found.

### Example (Arbitrary Instances)

Define a  $Tree$  type and a generator for search trees:

```
searchTrees :: Int -> Int -> Generator Tree
```

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## Homework

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- 1 Next project <https://eduassistpro.github.io/>
- 2 This week's

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