## COMP3161/9164 22T3 Assignment 0 Proofs

Marks: 15% of overall marks for the course.

A mark of x (out of 100) on this assignment will

translate to .15x course marks.

Due date: Thursday, 6th of October 2022, 12 noon (Sydney Time)

#### 1 Task

In this as is not generally miton to the compilation of semantic techniques, including its syntax and sematics, and its compilation to various target lang

Prepare your antipos://eduassistpro.github.io/ typeset. Figure https://eduassistpro.github.io/ mathematics is formatted correctly. Some guidance will be posted on the course website.

Submit your PDF using the CSF give system, by typing the cossist\_progive cs3161 Proofs Proofs.pdf

or by using the CSE give web interface.

#### Part A (25 marks)

Consider the language of boolean expressions  $\mathcal{P}$  containing just literals (True, False), parentheses, conjunction ( $\land$ ) and negation ( $\neg$ ):

```
\mathcal{P} = \{ \text{True}, \text{False}, \neg \text{True}, \neg \text{False}, \text{True} \land \text{False}, \neg (\text{True} \land \text{False}), \dots \}
```

- 1. Write down a set of inference rules that define the set  $\mathcal{P}$ . The rules may be ambiguous. (5 marks)
- 2. The operator ¬ has the highest precedence, and conjunction is right-associative. Define a set of simultaneous judgements to define the language without any ambiguity. (5 marks)

3. Here is an abstract syntax  $\mathcal{B}$  for the same language:

$$\mathcal{B} ::= \mathsf{Not} \; \mathcal{B} \; | \; \mathsf{And} \; \mathcal{B} \; | \; \mathsf{True} \; | \; \mathsf{False}$$

Write an inductive definition for the *parsing* relation connecting your unambiguous judgements to this abstract syntax. (5 marks)

4. Here is a big-step semantics for the language B

- a) Show the evaluation of And (Not (And True False)) True with a derivation tree. (5 marks)
- b) Consider the following inference rule:

$$\frac{y \Downarrow \mathsf{False}}{\mathsf{And} \ x \ y \Downarrow \mathsf{False}}$$

A If we assume that x B holds, is this rule derivable? Is it admissible? And if Sold Halle hall Bholds Je Goes this half your answers. (5 marks)

Part B (20 marks) ps://eduassistpro.github.io/

- Show the full evaluation of the term (If True (If True False True) False). (5
  marks)
- 2. Define an equivalent big-step semantics for  $\mathcal{L}$ . (5 marks)
- 3. Prove that if  $e \Downarrow v$  then  $e \stackrel{\star}{\mapsto} v$ , where  $\Downarrow$  is the big-step semantics you defined in the previous question, and  $\stackrel{\star}{\mapsto}$  is the reflexive and transitive closure of  $\mapsto$ . Use rule induction on  $e \Downarrow v$ . (10 marks)

#### Part C (15 marks)

- 1. Define a recursive compilation function  $c: \mathcal{B} \to \mathcal{L}$  which converts expressions in  $\mathcal{B}$  to expressions in  $\mathcal{L}$ . (5 marks)
- 2. Prove that for all e,  $e \Downarrow v$  implies  $c(e) \Downarrow v$ , by rule induction on the assumption that  $e \Downarrow v$ . (10 marks)

#### Part D (40 marks)

1. Here is a term in  $\lambda$ -calculus:

$$(\lambda n. \lambda f. \lambda x. (n f (f x))) (\lambda f. \lambda x. f x)$$

- a) Fully  $\beta$ -reduce the above  $\lambda$ -term. Show all intermediate beta reduction steps. (5 marks)
- b) Identify an  $\eta$ -reducible expression in the above (unreduced) term. (5 marks)
- 2. Recall that in  $\lambda$ -calculus, booleans can be encoded as binary functions that return one of their arguments:

$$T \equiv (\lambda x. \lambda y. x)$$

$$\mathbf{F} \equiv (\lambda x. \ \lambda y. \ y)$$

Either via  $\mathcal{L}$  or directly, define a function  $d: \mathcal{B} \to \lambda$  which converts expressions in  $\mathcal{B}$  to  $\lambda$ -calculus. (5 marks)

- 3. Prove that for all e such that  $e \Downarrow v$  it holds that  $d(e) \equiv_{\alpha\beta\eta} v'$ , where v' is the  $\lambda$ -calculus encoding of v. (10 marks)
- 4. Suppose we added unary local function definitions to our language P. Here's an example project Exam Help

### https://eduassistpro.github.io/

We limit ourselves to non-recursive bindings (meani selves), and Arxi-prior whether (manife actuses assist pro).

- a) Extend the *abstract* syntax for  $\mathcal{B}$  from question A.3 so that it supports the features used in the above example. Use first-order abstract syntax with explicit strings. You don't have to extend the parsing relation. (5 marks)
- b) Define a scope-checking judgement, similar to the **ok** judgement from the lectures. It should check (a) that all names of variables and functions are used only within their scopes; and (b) that names used in variable (or function) position are indeed the names of variables (or functions). Hence, the following expressions should both be rejected:

The following are examples of things that should be accepted: nullary definitions, nested definitions, and shadowed definitions.

$$\begin{array}{lll} \text{let} & & & \text{let} \\ f(x) = & & f(x) = x \\ \text{let} & & f(x) = x \\ g(y) = \neg x \wedge y & & \text{in} \\ g(x) \wedge \neg g(x) & & f(x) = f(x) \\ \text{end} & & \text{in} \\ f(\text{False}) & & \text{end} \\ & & \text{end} \end{array}$$

Note that the latter example is *not* a recursive call. (10 marks)

#### 2 Late Penalty

You may submit up to five days (136 hours) late. Early day of lateness corresponds to a 5% reducible bluk. For Capacity your Xsaturdent is worth 88% and you submit it two days late, you get 78%. If you submit it more than five days late, you get 0%.

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