#### PROGRAMMING IN HASKELL

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Chapter 11 - The Countdown Problem

### **What Is Countdown?**

- ? A popular <u>quiz programme</u> on British television that has been running since 1982.

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- Based upon https://eduassistpro.gethsibnocalled "Des Chiffres et Des Lett edu\_assist\_pro
- Includes a numbers game that we shall refer to as the <u>countdown problem</u>.

# **Example**

Using the numbers

```
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and the arithmetiq.pperator edu_assist_pro
```

- +
- -
- \*
- ÷

construct an expression whose value is

#### Rules

- ? All the numbers, including intermediate results, must be positive naturals (1,2,3,...). Assignment Project Exam Help
- Each of the https://eduassistpro.githelbused at most once when constru edu\_assist\_pression.
- We <u>abstract</u> from other rules that are adopted on television for pragmatic reasons.

## For our example, one possible solution is

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Notes:

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- There are 780 solutions for this example.
- Changing the target number to gives an example that has no solutions.

# **Evaluating Expressions**

### Operators:

```
data Op = Assignment Broject Exam Help
```

Apply an opera

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```
apply :: Op \rightarrow Int \rightarrow Int \rightarrow Int apply Add x y = x + y apply Sub x y = x - y apply Mul x y = x * y apply Div x y = x `div` y
```

Decide if the result of applying an operator to two positive natural numbers is another such:

```
valid :: Op \rightarrow Int \rightarrow Int \rightarrow Bool valid Add _Assignment Project Exam Help valid Sub x y = x valid Mul _ = Thttps://eduassistpro.github.io/valid Div x y = x Add WeChat edu_assist_pro
```

#### **Expressions:**

data Expr = Val Int | App Op Expr Expr

Return the overall value of an expression, provided that it is a positive natural number:

```
eval (Val n) Assignment)Project Exam Help eval (App o l r) = [
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```

Either succeeds and returns a singleton list, or fails and returns the empty list.

# **Formalising The Problem**

Return a list of all possible ways of choosing zero or more elements from a list:

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choices :: [a] https://eduassistpro.github.io/

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For example:

> choices [1,2] [[],[1],[2],[1,2],[2,1]]

## Return a list of all the values in an expression:

```
values :: Expr → [Int]
values (Val n) = [n]
values (App _ l r) = values l ++ values r
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```

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Decide if an exp for a given list of source numbers and a tar edu\_assist\_pro

```
solution :: Expr \rightarrow [Int] \rightarrow Int \rightarrow Bool solution e ns n = elem (values e) (choices ns) && eval e == [n]
```

#### **Brute Force Solution**

Return a list of all possible ways of splitting a list into two non-empty parts:

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split :: [a] → [([a],[https://eduassistpro.github.io/

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For example:

```
> split [1,2,3,4]
[([1],[2,3,4]),([1,2],[3,4]),([1,2,3],[4])]
```

Return a list of all possible expressions whose values are precisely a given list of numbers:

The key function in this lecture.

### Combine two expressions using each operator:

```
combine :: Expr → Expr → [Expr]
combine | r =
  [App o | r | o ← [Add,Sub,Mul,Div]]
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```

Return a list of <a href="https://eduassistpro.github.io/">https://eduassistpro.github.io/</a> solve an instance of the countdownapedu\_assist\_pro

```
solutions :: [Int] \rightarrow Int \rightarrow [Expr]
solutions ns n = [e | ns' \leftarrow choices ns
, e \leftarrow exprs ns'
, eval e == [n]]
```

#### **How Fast Is It?**

System: 2.8GHz Core 2 Duo, 4GB RAM

Compiler: Assignment Project Exam Help

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Example: Asolutions [1.3 edu\_assist\_pro

One solution: 0.108 seconds

All solutions: 12.224 seconds

#### **Can We Do Better?**

- Many of the expressions that are considered will typically be invalid - fail to evaluate. Assignment Project Exam Help
- For our exa <a href="https://eduassistpro.github.jo/million">https://eduassistpro.github.jo/million</a> of the 33 million possible vexpre edu\_assistvation.
- Combining generation with evaluation would allow <u>earlier rejection</u> of invalid expressions.

# **Fusing Two Functions**

Valid expressions and their values:

```
Assignment Project Exam Help type Result = (Expr,Int)
```

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We seek to define twoction edu\_assists together the generation and evaluati essions:

```
results :: [Int] \rightarrow [Result]
results ns = [(e,n) | e \leftarrow exprs ns
, n \leftarrow eval e]
```

# This behaviour is achieved by defining

```
results [] = []
results [n] = [(Val n,n) | n > 0]
results ns =
[res | (ls,rs) ssignment Project Exam Help
, |x ← re
, ry ← rehttps://eduassistpro.github.io/
, res ← combine' |x ry]

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```

#### where

```
combine' :: Result → Result → [Result]
```

### Combining results:

New function t

https://eduassistpro.github.io/ problems:

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```
solutions' :: [Int] → Int → [Expr]
solutions' ns n =

[e | ns' ← choices ns

, (e,m) ← results ns'

, m == n]
```

#### **How Fast Is It Now?**

Example: solutions' [1,3,7,10,25,50] 765

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One solution: 0.014 secon Add Wechat edu\_assist\_pro

Around 10 times faster in both cases.

All solutions: 1.312 seconds

#### **Can We Do Better?**

Many expressions will be <u>essentially the same</u> using simple arithmetic properties, such as:

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Exploiting such properties would considerably reduce the search and solution spaces.

# **Exploiting Properties**

Strengthening the valid predicate to take account of commutativity and identity properties:

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```
https://eduassistpro.github.io/\\ valid :: Op \rightarrow Int dd^{Intv} e^{Bool}_{Add} e^{Dol}_{Add} e^{Dol}_
```

#### **How Fast Is It Now?**

Example: solutions" [1,3,7,10,25,50] 765

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https://eduassistpro.github.jo/Around 20

Valid: 250,000 expres edu\_assist\_pmes less.

Solutions: 49 expressions

Around 16 times less.

One solution: 0.007 seconds

Around 2 times faster.

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Around 11

All solutions: https://eduassistpro.githwle.jofaster.

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More generally, our program usually returns all solutions in a fraction of a second, and is around 100 times faster that the original version.