

Multi-agent Decision Making

COMP 4418 – Assignment 2

Due 18 Nov. 2022, 23:55

Total Marks: 100

Worth: 10% of the course

Question 1 (20 marks) Consider the following preference profile of voters.

1 : $c \succ d \succ b \succ a$

2 : $d \succ c \succ b \succ a$

3 : $a \succ d \succ c \succ b$

1. Prove or disprove that the preference profile is single-peaked with respect to some order of alternatives.

2. Prove or disprove

3. Compute the

4. Compute the Top Cycle set for the preference profile.

Question 2 (20 marks) Consider a resource allocation problem with n agents having positive additive utilities over $m > n$ indivisible items. Prove or disprove the following statements.

- The allocation that maximizes utilitarian welfare is Pareto optimal.
- If an allocation is Pareto optimal, it is envy-free.
- If $n = 2$, envy-freeness and proportionality are equivalent.
- The sequential allocation algorithm, in which agents arrive in order $(1, 2, 3, \dots, n)^*$ and are given a most preferred unallocated item, is strategyproof.

Question 3 (20 marks) Consider the following school choice problem with five students 1, 2, 3, 4, 5 and five schools a, b, c, d , and e with each school having exactly one seat. The preferences of the students are as follows from left to right in decreasing order of preference.

1 : e, b, a, c, d

2 : b, a, c, d, e

3 : a, b, c, d, e

4 : a, b, c, d, e

5 : d, b, c, a, e

The priorities of the schools are as follows from left to right in decreasing order of priority.

$a : 2, 4, 3, 5, 1$

$b : 3, 2, 4, 5, 1$

$c : 3, 2, 4, 5, 1$

$d : 5, 2, 4, 3, 1$

$e : 1, 2, 3, 4, 5$

1. Find the outcome matching of the student proposing deferred acceptance algorithm, showing working out. Prove or disprove that the resultant matching is Pareto optimal for the students.
2. Suppose that initially, student 1 is allocated to school a , student 2 is allocated to school b , student 3 is allocated to school c , student 4 is allocated to school d , and student 5 is allocated to school e . Apply the Top Trading Cycles (TTC) Algorithm with respect to the students' preferences here and find the output, showing working out. Note that we ignore the schools' priorities here.
3. Give three reasons, with examples if necessary, why the deferred acceptance algorithm is pre
4. Give a reason, school ch

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Question 4 (40 marks) Consider the standard social choice problem where n voters have strict preferences over a set of m alternatives.

1. We can define the $\text{rank}/3$ predicate, where $\text{rank}(i, a, k)$ indicates voter i ranks outcome a as its k th most preferred outcome in his/her vote. Write down the ASP encoding for the preference profile in Question 1.
2. Write an ASP program `condorcet.lp` that takes in a preference profile as input, and outputs the Condorcet winner in the predicate `condorcetWinner/1`. If there is no Condorcet winner, there should be no instance of this predicate/the predicate should be empty.
3. Write an ASP program `condorcetborda.lp` that takes in a preference profile as input, and outputs the Condorcet winner if one exists, or the Borda winner if no Condorcet winner exists. If no Condorcet winner exists and there are multiple alternatives with a tied winning Borda score, the program should output the alternative that comes first in alphabetical order.
4. Consider the voting rule from the previous subquestion that selects the Condorcet winner if one exists, or the Borda winner if no Condorcet winner exists, breaking ties by alphabetical order. Write an ASP program `cbmanipulation.lp` that takes in a preference profile as input, and returns a different preference ordering that a voter can report to achieve a better outcome under the aforementioned voting rule.

The program should additionally return the misreporting voter's original (truthful) preference ordering. If no such misreport exists for any voter, the program should return UNSATISFIABLE.

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