Week 7

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COMP 481: Functional and Logic Programming

Overview

- functor design
- IO actions as functors
- <u>functions as functors</u>
- functor laws
- breaking the functor laws

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- <u>`M</u>
- th https://eduassistpro.github.io/
- lists (a) applicative fuedu_assist_pro
- IO (as an applicative functor)
- <u>functions (as applicative values)</u>
- ZipList`Applicative Functor
- Applicative Laws
- Useful Functions for Applicatives

Interface-style Design

The Haskell programming language is:

- bigger on interface-style design
- than on classes- and subclass-hierarchy design A sasignother object-priented programming languages.
- https://eduassistpro.github.io/ act as many different kinds of things descriedu_assist_pro

A thing can be categorized into many type classes, not just one hierarchy.

Functor Type Class

Recall type classes such as:

- `Eq` for describing types with values we can check for equality, and
- 'Ord' for describing types with values that are orderable.

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The es demonstrate the https://eduassistpro.githiptions/

Add WeChat edu_assist_pro Recall the `Functor` escribes:

- types with nested values
- that can have a function applied
- and maintain the parent structure.

Functionality

`Functor` type class: types that can be mapped over.

Applying functions on elements of:

• an input set (a domain)...

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- (there could be repetition both in the input set and in the output set)
- thihttps://eduassistpro.giththetis/a singleton (lik
- but Actib Wyou harbed u_assisting the nested values

Realize that `Functors` allow you to begin to think of things such as lists, `Maybe`, binary trees, etc., as having similar possible behaviour.

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Functor versus Function

The `Functor` type class has only one method that must be implemented on any instances called `fmap`, which we have already seen.

Assigning the description cist fragam (Holp) -> f a -> f b

- se https://eduassistpro.githegontext of `f` to the nested val
- the function passed i edu_assist_probut the parameter function `(a -> b)`
 - `(a -> b)` is the function applied to the nested values, where as `f` maintains itself as parent context

Functors and Type Parameters

To describe an instance of `Functor` as a type constructor, it must be of kind `* -> *`:

 give one type parameter as input, and the type constructor will evaluate to one concrete type

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Then with a type so edu_assisth as `Either` that takes two type paramete

- we must additionally supply exactly one type parameter, `Either a`
 - cannot write `instance Functor Either where`
 - must write `instance Functor (Either a) where`

`Either a` as a Functor

To implement `fmap` with the `Either a` type constructor Avould then be deserbed as Help

fmap https://eduassistpro.github.io/

- in the above Either a edu_assist pro
 the context is alwa

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`IO` as a Functor

```
Notice that the `IO a` type has the one parameter `a`, where `IO` has been implemented as a Functor.
```

A description for how it is implemented already:

```
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inst
https://eduassistpro.github.io/
let_result <-
Add_weChat_edu_assist_pro
```

The input parameter `g` is NOT the parent context `f` (in this case `IO`)!

*Textbook Caveat

The textbook often uses the same letter `f` for both functor and function:

• 'g' is some function passed in as a parameter of 'fmap'

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• the context is an I/O action, suppose `IO String` (which is NOT `g`)

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Note that weturnat edu_assisparent context:

- this requires an I/O action in the process, so it must be bound with `<-` assignment (unless it is the last line of the `do` block)
- this must be done within a 'do' block as part of multiple I/O actions

`IO` Functor Example (1) This has many layers of concepts, so a few examples, first without, and then with:

```
main = do
     line <- getLine</pre>
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putStrLn $ "You said " ++ line' ++ " backwards!"
      https://eduassistpro.gtthub.ib/ "
 Then lo as a funct edu_assist_pro parameter is `String`:
 main = do
     line <- fmap reverse getLine</pre>
     putStrLn $ "You said " ++ line ++ " backwards!"
```

putStrLn \$ "Yes, you said " ++ line ++ " backwards!"

`Io` Functor Example (2)

See how the function 'reverse' passed in to 'fmap' must work with types 'String':

- input of `reverse` is String

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 - https://eduassistpro.github.io/
 - Abut we passed are edu_assisp`, which returns an `IO` context, so `fmap reverse edu_assisp`, which returns an `IO` context, is of type `IO String`
 - the `<-` operation removes the `IO` context and stores the nested `String` value in `line`

Point-free versus Nesting (1)

- if you are wanting to perform I/O action and then a function on the result...
- …instead consider using `fmap` and pass the function in together with the I/O action
- then the function passed in can be a composition using point-free notation, or a lambda function, etc.

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```
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. reverse . map toUpper) getLine
putstdLWieChat edu_assist_pro
```

The equivalent function passed to `fmap` written without using point-free is:

```
(\xs -> intersperse '-' (reverse (map toUpper xs)))
```

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Functions as Functors

The syntax we have seen for descriptions of functions is `a -> b`:

notice it is written similar to a binary operator

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- if https://eduassistpro.github.io/
 - this describes the s tructor

 Afa function that t edu_assisterpro
 - this is used to implement an instance of `Functor`

```
instance Functor ((->) r) where

fmap f g = (\x -> f (g x))
```

*Equivalent to Composition The textbook just demonstrates how the composition operator `.` is equivalent to `fmap` when implementing a function as a `functor`.

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- fu https://eduassistpro.githerojation of mathematics wh
- piping would be muc edu_assist pro a `do` block

Signature of `fmap`

The above is just function composition, which could be written more concisely as:

```
instance Functor ((->) r) where
    fmap = (.)
```

Ansimplementation textists in Control Monad Instances https://eduassistpro.github.io/ mo

```
fmap :: (a -> f b

AddayWeChat edu_assist_pro>) r b
     fmap :: (a \rightarrow b) \rightarrow (r \rightarrow a) \rightarrow (r \rightarrow b)
```

- then see in this instance, 'fmap' takes two functions as parameters
- the composition would be, mathematically `r -> a` then `a -> b`, so that altogether the result is `r -> b`

Demonstrations of Functions Functors

```
ghci> :t fmap (*3) (+100)
fmap (*3) (+100) :: (Num a) => a -> a
ghci> fmap (*3) (+100) 1
303
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    https://eduassistpro.github.io/
   Add WeChat edu_assist_pro
ghci> fmap (show . (*3)) (+100) 1
"303"
```

Note that the order of operations will first compose the functions and then apply the one resulting function.

*A Few More Examples

```
ghci> fmap (replicate 3) [1,2,3,4]
[[1,1,1],[2,2,2],[3,3,3],[4,4,4]]
ghci> fmap (replicate 3) (Just 4)
Just [4,4,4]
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ghci
                               blah")
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ghci>Add WeChat edu_assist_pro
Nothing
ghci> fmap (replicate 3) (Left "foo")
Left "foo"
```

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The Functor Laws

There are properties and behaviours of functors we call laws:

they are not checked by Haskell automatically

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 however, all the library functors implement them
- wehttps://eduassistpro.githuheighg our own functors

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- 1. the function 'id' mapped over a functor must return the same functor value
- 2. 'fmap' distributes across composition

Details of Functor Laws

- 1. the function 'id' mapped over a functor must return the same functor value
 - i.e.: `fmap id = id`
 - e.g.: `fmap id (Just 3)` vs `id (Just 3)`

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 2. fmap distributes across composition
 - •https://eduassistpro.github.io/

 - i.e.: `fmap (f . g) x = x)`
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 ultimately, nothing behaviour of other functions applied over it
 - for example, there is nothing about lists that changes how a function will operate on its elements

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Breaking Functor Laws

We will consider an example that breaks the laws, just to see what happens.

```
data CMaybe a = CNothing | CJust Int a deriving (Show)

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```

- th https://eduassistpro.github.io/
- the first field in the `C or will always have type `Int`
 - Add WeChat edu_assist_pro this is similar to M edu_assist_pro but will just be used as a counter
- the second field is of type `a` and will depend on the concrete type we choose later for `CMaybe a`

Using CMaybe

```
ghci> CNothing
Cnothing
ghci> CJust 0 "haha"
CJust 0 "haha"
Assignment Project Exam Help
ghci
CNOt https://eduassistpro.github.io/
ghci>Add WeChat edu_assist_pro
CJust 0 "haha" :: CMaybe String
ghci> CJust 100 [1,2,3]
CJust 100 [1,2,3]
```

CMaybe an Instance of Functor

Now we will implement `CMaybe a` as a functor.

- so `fmap`
 - applies the function passed in to the second field of `CJust`
 - and increments the first field,

Assigotherwise Parconothing x suleft lalohe:

```
https://eduassistpro.github.io/
```

```
fmap g (CJust counter x) = CJust (counter + 1) (g x)
```

(in ghci, no need for `let` with instance and can be multiline)

First Functor Law Broken

See how we can apply fmap now:

CJust 0 "haha"

```
ghci> fmap (++ "ha") (CJust 0 "ho")
CJust 1 "hoha"
ghci> fmap (++ "he") (fmap (++ "ha") (CJust 0 "ho"))
CJust 2 "hohahe"
Assignment Project Exam Help ghci> fmap (++ "blah") CNothing
CNot https://eduassistpro.github.io/
But the first law do edu_assist_pro
ghci> fmap id (CJust 0 "haha")
CJust 1 "haha"
ghci> id (CJust 0 "haha")
```

Second Functor Law Broken

And neither does the second law hold:

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```
ghci>https://eduassistpro.githuciQ/ 0 "ho")

CJust 2 "hohahe"
ghci> fmap ((++ "he") . edu_assist_pro
ghci> fmap ((++ "he") . edu_assist_pro
CJust 1 "hohahe"
```

Code Independent of Context

The functor laws are necessary to ensure they do not obfuscate the use of our other functions we may write.

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- i.e about how a function will be applied to https://eduassistpro.giffic/
- this makes pur code e edu_assist_pro
- in turn, many of the other "-ities" become supported, such as extensibility, maintainability, etc.

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Functions in Context

Functors can be taken to a more general context by partially applying the function passed in to 'fmap':

```
Assignment Project Exam Help fmap (*) Just 3
```

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The above results i assist or `Just (3 *)`.
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• the nested value becomes a partially applied function

Nested
Partially
Applied
Functions
(1)

```
ghci> :t fmap (++) (Just "hey")
fmap (++) (Just "hey") :: Maybe ([Char] -> [Char])
ghci> :t fmap compare (Just 'a')
ASSIGNMENT Project Exam Help
fmap compare (Just 'a') :: Maybe (Char -> Ordering)
https://eduassistpro.github.io/
fmap AmbareWacISTapedu_assistappo Ordering]
ghci> :t fmap (\x y z -> x + y / z) [3,4,5,6]
fmap (x y z -> x + y / z) [3,4,5,6] :: Fractional a => [a -> a -> a]
```

Nested Partially Applied Functions

In the expressions involving `compare` function

- Assignment oppore is `compare :: (Ord a) => a -> a -> Ordering`
- https://eduassistpro.github.io/ n for `compare` is inferred to be `Char`

 - -Add the eChat edu_assistapro
 - the combined partially-applied compare function and the functor together generate a list of functions of type 'Char -> Ordering'

Lists of Multiparameter Functions

- you may wonder how to work with the last expression
 - assign the expression result to a variable: `functions` (see below)

```
Assignment function is missing two parameters: `y` and `z` a ->` part of the type description
```

- •https://eduassistpro.gith(好b.fo/2) \$ functions`
- this adds `0.5 of the already Addsuble views edu_assist list [3,4,5,6]

```
functions = (fmap (\x y z -> x + y / z) [3,4,5,6])
ghci> fmap (\f -> f 1 2) functions
```

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— `Maybe`https://eduassistpro.githีแปกผู้tor —

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Applicative Functors (1)

We have seen how to use functions on the nested elements of functors.

• "functor value" just means some context with nested elements

Applicative functors go one sten more abstract and allow us to define operations between functor values.

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Consided the follow edu_assist_pro

- we have a functor full of nested partially applied functions
- we have another functor full of nested elements
- we want the corresponding nested functions and nested elements to be calculated together

Applicative Functors (2)

Consider such an operation:

```
ghci> Just (+3) <*> Just 9
Just 12
```

We need the Applicative type class:

function, and

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The `Applicative` ty
(remember, `f` is likely NOT a function!):

```
class (Functor f) => Applicative f where
  pure :: a -> f a
  <*> :: f (a -> b) -> f a -> f b
```

Maybe as an Applicative Functor

A function named with **all** special characters is automatically a binary operator.

Implementation for the `Maybe` type: Assignment Project Exam Help

inst https://eduassistpro.github.io/
pure = Just
Nothing V** Chat edu_assist_pro

(Just g) <*> something = fmap g something

• `pure = Just` is equivalent to `pure x = Just x`

Implementation of <*>

```
(Just g) <*> something = fmap g something
```

- the last line may be difficult to imagine what is happening, but recall the example we are working toward

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 • we want to get the function `g` out of the first functor `(Just g)`

 - *https://eduassistpro.githtub:fo/

 - (`something`conta t can have `g` applied to them)

 Add We Chat edu_assist properties of have the two functors in exactly this order with `<*>`
 - we cannot transpose the order for nested function and something

pure

These implementations are already part of Haskell, so give them a try:

```
Just (+3) <*> Just 9

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Just

Noth https://eduassistpro.github.io/
```

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- there are many kinds functors
- so, there are many kinds of results for `pure`
- `pure (+3)` takes advantage of Haskell's inference
 - what functor type will match with `Just 9`
 in order to match on the left an expression `Just (+3)`

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The order of operations using `<*>` is from left-to-right

- when writing larger expressions of more than two functor values
- this is called left-associative
- then partially applied functions leftmost need more parameters Assignment Project Exam Help

Using <*>

For https://eduassistpro.github.io/

```
pure (+) <*> Just 3 <*
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```

- notice that the above expression is similar in syntax as `(+) 3 5`
- the given expression is equivalent to
 - `(pure (+) <*> Just 3) <*> Just 5`
 - ...and result of `(pure (+) <*> Just 3)` is `Just (3+)`

Applicative Advantage

The advantage of applicative types:

 we can use functions on nested values within functors without having to worry about what those functors are

Assignment Project Exam Help • `pure g <*> x <*> y <*> ...`

- - ·https://eduassistpro.githusbeio/
 - each successive evaluedu_assist_pro
- `pure g <*> x` is equivalent to `fmap g x`
 - (this is one of the applicative laws we will discuss later)

fmap Synonym <\$>

```
Instead of writing `pure g <*> x <*> ...` we could just write `fmap g x <*> ...`
```

• however, there is an infix version of `fmap` to make expressions even Associate with less Exam Help

```
https://eduassistpro.github.io/
(<$> Atdfr@eChat edu_assist_pro
```

- so, we could instead write `g <\$> x <*> y <*> ...`
- note that `g` is a function (a variable one)

Type Descriptions with <\$> and <*>

Another example:

```
(++) <$> Just "Doctor Strange" **> Just "and the Multiverse of Madness"
```

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- recall the type for concatenation `(++) :: [a] -> [a] Add WeChat edu_assist_pro
- the `<\$>` operation results in a partially applied function of type Just ("Doctor Strange "++) :: Maybe ([Char] -> [Char])
- can you work out the type of the last functor in the example?

Example of <\$> (Simranjit Singh)

```
-- Presentation 3
-- Simranjit Singh

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    https://eduassistpro.github.io/

getList :: String -> [
getList xs = foldr (\n edu_assist_pro.github : acc) [] list
    where list = words xs
```

Example of <\$> (Simranjit Singh)

```
genNewList :: [Int] -> StdGen -> IO ()
 genNewList xs gen =
     do
         let
Assignme(rangement levgen) Help
randomR (1,3) gen :: (int, StdGen)
     https://eduassistpro.github.io/
$ (+75) <$> xs
      Add WeChatedu_assist(*5)ro$> xs
                   x == 3 = print $ (`div` 3) <$> xs
                   True
                     putStrLn "Something went terribly wrong"
         secretCalc randNumber
```

Example of <\$> (Simranjit Singh)

```
main = do
    gen <- getStdGen

putStrLn "Enter a list of numbers (no commas or brackets):"

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print(list edu_assist pro.github.io/

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    print(list edu_assist edu_assist eduale)

putStrLn "I have n et operation on your list"
    putStr "Your new list is: "
    genNewList list gen</pre>
```

Assignment Project Exam Help — Lists (https://eduassistpro.gifhGtQt/S) — Add WeChat edu_assist_pro

Lists as Applicative Functors

We have the implementation of lists as applicative functors:

```
instance Applicative [] where
    pure x = [x]
    fs <*> xs = [g x | g <- fs, x <- xs]
Assignment Project Exam Help</pre>
```

- nohttps://eduassistpro.gitกป่ยี.ศูผู*ays*
- also notice that the `gedu_assistably create ALL possible combinations of func
 - the type of `<*>` restricted to lists:
 `(<*>) :: [a -> b] -> [a] -> [b]`
 - since there are potentially many functions, the implementation needs list comprehensions (to facilitate all possible combinations)

Lists with `<*>` will remind you when you apply it that you will get every combination of result possible.

```
[(*0),(+100),(^2)] <*> [1,2,3]
```

The next example shows step-by-step evaluation of multiple operations:

```
ghci https://eduassistpro.github.io/
[(+1),(+2),(*1),(*2)] <
[4,5,4,4,4,6,6] hat edu_assist_pro
```

One more example:

```
ghci> (++) <$> ["ha", "he", "hm"] <*> ["?", "!", "."]
["ha?", "ha!", "ha.", "he?", "he!", "he.", "hm?", "hm!", "hm."]
```

Practice with Lists and <>

Nondeterministic Computation

We can think of lists as nondeterministic computations.

- a value such as `"what"` or `100` is deterministic
- a value such as `[1,2,3]` may decide among its three elements
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```
Notihttps://eduassistprepgiteus.io/comprehensions:
    Add WeChat edu_assist_pro
ghci> [ x*y | x <- [1,2,3], y <- [4,5,6] ]
[4,5,6,8,10,12,12,15,18]
ghci> (*) <$> [1,2,3] <*> [4,5,6]
```

[4,5,6,8,10,12,12,15,18]

filter and <\$>

Combining with `filter` is especially useful: Assignment Project Exam Help

ghci https://eduassistpro.github*i0[4,5,6]
[12,12,15,18]
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— IO (as https://eduassistpro.glthu6tio/r) —

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IO as Applicative **Functor**

We look at the implementation of 'IO' as an applicative functor:

```
instance Applicative IO where
    pure = return
    s <*> t = do
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```

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- pure = return` works ignoring the value passed in Add WeChat edu_assist_pro
 `<*>` for `IO` has desc
 IO (a -> b) -> IO a -> IO b`
- - implementation of `<*>` must then remove the `IO` context for both s and t parameter values
 - 'do' is needed to glue together multiple I/O actions into one
 - 'return' will place the result '(g x)' back into an 'IO' context

getLine and <*>

```
do

x <- (++) <$> getLine <*> getLine
putStrLn $ "two lines concatenated: " ++ x
```

- Assignment Project Exam, Help the nested result of a getLine I/O action is a `String`
 - *https://eduassistpro.gittingfragh `getLine` catenated values
- the result of (++) <\$ edu_assist_pro is of type `IO b` where `b` in this case is `String`
 - this is altogether one I/O action and we can assign the yield to `x` as a `String` value

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Functions as Applicative Functors

The implementation for functions as applicatives:

```
instance Applicative ((->) r) where

pure x = (\--> x)

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f<*> g = \x -> f x (g x)
```

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- the `pure` implement value of minimal context for the functordype chat edu_assist_pro
 - in this case, the result is a function that ignores its parameter and always evaluates to `x`
 - the type for `pure` is `pure :: a -> (r -> a)`

pure Behaviour

The default behaviour of 'pure' is kind of strange here:

```
(pure 3) "blah"
```

Asbignesuiteoftherabitive is actually Help

- ate a function that always https://eduassistpro.gatanleterlpassed in
- Ait is a partially appliedu_assist_pro will take "blah" as
- the result is `3`, as expected
- equivalently, because functions are left-associative, there is no need for parentheses: `pure 3 "blah"`

Function Composition

We look at a few examples:

```
ghci> :t (+) <$> (+3) <*> (*100)
(+) <$> (+3) <*> (*100) :: Num b => b -> b
```

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- https://eduassistpro.github.io/ ons (+3) and `(*100)`
 - About function hateedu_assistan Din the above we pass in `5`
 - `(5+3) = 8`
 - (5*100) = 500
 - add the results together (as if we had not passed in `5` yet)
 - the result of the entire function is `(5+3) + (5*100) = 508`

Here is another wild one to read:

```
ghci> (\x y z -> [x, y, z]) <$> (+3) <*> (*2) <*> (/2) $ 5 [8.0,10.0,2.5]
```

- A shigh the peraid is a function that takes three parameters
- fir https://eduassistpro.gitthelpanext of the list elements, which are each then functions
- Add WeChat edu_assist_pro

 each next operand in ression fills in one parameter
 - in the order `x`, `y`, `z`
- this results in a function equivalent to (x -> [(x+3),(x*2),(x/2)])
 - (arguably, the original expression is much more difficult to read)

*
<\$> and <*>

Operations First

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— `ZipL https://eduassistpto.github.io/

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Corresponding Elements

We will often want corresponding elements between lists to operate together, rather than combinations.

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`Zip mplementation of applicative fun https://eduassistpro.gittehtron.Applicative`):

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```
instance Applicative ZipList where
  pure x = ZipList (repeat x)
  fs <*> xs = ZipList (zipWith (\f x -> f x) fs xs)
```

ZipList

 we can see that `zipWith` applies each function element of `fs` to its corresponding element of `xs`

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- for reates an infinite list, whereas `rehttps://eduassistpro.gith@an finite list
 - we want "minimal finite list, because `zipWith` will Atop on the shorter edu_assist be any length, even infinite...)
 - for example:`take 2 \$ zipWith (\x y -> x + y) [1,2..] [3,4..]`

The `zipList` type is not implemented as an instance of `Show`, so we must use the `getZipList` function to return results as a list:

import Control.Applicative

Assignments Projects Exams Help, 3]

[101 https://eduassistpro.github.io/

[('d','c','r'),('o','a','a'),('g','t','t')]

getZipList

Multiple Lists and Zip Functions

```
(,,) is a constructor for a triple, equivalent to (\x y z -> (x, y, z)).
```

Abeignance un Rions for Zigning Halpe lists, four lists, etc.:

- `z
- https://eduassistpro.github.io/
- · ··Add WeChat edu_assist_pro
- `zipWith7`

```
ghci> zipWith3 (x y z -> x + y + z) [1,2,3] [4,5,6] [7,8,9] [12,15,18]
```

Multi-Parameter with **ZipList**

Equivalently:

```
:{
getZipList $ (\x y z -> x + y + z)
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```

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It is a bit more writing, because of the redundant `ZipList` constructors.

ZipList Example (David Semke)

```
import Control.Applicative
-- Multiply the first number in list1 by 1,
    the second by 2, the third by 3, ...
list1 = take 10 (repeat 1)
Assignment: Project Examziptist Int
incrementMult (ZipList xs) =
    https://eduassistpro.githubkeo(length xs) [1, 2...]
   in mults <*> ZipLi
    Add WeChat edu_assist_pro
listzip = ZipList list1
result = getZipList $ incrementMult listzip
ghci> getZipList $ incrementMult $ ZipList result
```

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Applicative Laws (1)

- 1. `pure id <*> v = v`
- Assignment Project Examplele* > (v <*> w)`
- 3. https://eduassistpro.github.io/
- 4. \(\frac{Add WeChat edu_assist_pro }{u < * > pure y = \quad > u

Applicative Laws: Examples

```
1. (trivial)

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2. (+2)] <*> [1]) :: [Int]

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3. [Int]

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4. pure ($ 4) <*> [
```

Applicative Laws (2)

- `(.)` is the operation of composition
- so for Law 2, note that it only makes sense when both `u` and `v` have Assignmented inside Exam Help
- th ou would like to apply to el https://eduassistpro.github.co/r parameter (a function)
 - And twe know harh edu_assists rested inside as elements in its context that should be applied (from the LHS of the equation of law (4))
 - so, the RHS will be fine to apply these functions with `(\$ y)`

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— Useful Fhttps://eduassistpro.gphicatives —

liftA2

The `Control.Applicative` module has a function called Assignment Project Exam Help

- ap s we have practiced so far
- th https://eduassistpro.gislas.follio/s:

```
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liftA2 :: (Applicative b -> c) -> f a -> f b -> f c
liftA2 g x y = g <$> x <*> y
```

Using liftA2

The name of the function `liftA2` is fitting:

- consider type description as `(a -> b -> c) -> (f a -> f b -> f c)`
- we see `liftA2` can promote a regular binary function and make that function operate within the context of two applicatives

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```
ghci>Acock Statedu_assist_pro
Just [3,4]
```

```
ghci> liftA2 (:) (Just 3) (Just [4])
Just [3,4]
```

Now we would like to apply a similar operation to the above demonstration, but repeatedly:

```
sequenceA :: (Applicative f) => [f a] -> f [a]
sequenceA [] = pure []
sequenceA (x:xs) = (:) <$> x <*> sequenceA xs
```

A staise carrein an empty distinx default context as `pure []`

- e first element within the context of https://eduassistpro.githuleric/ xs)`
 - `xs` is a list of funct

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sequenceA [Just 1, Jus

```
(:) <$> Just 1 <*> sequenceA [Just 2]
```

- (:) <\$> Just 1 <*> ((:) <\$> Just 2 <*> sequenceA [])
- (:) <\$> Just 1 <*> ((:) <\$> Just 2 <*> Just [])
- (:) <\$> Just 1 <*> Just [2]

Just [1,2]

*sequenceA

*Equivalent to sequenceA

We can also implement the same `sequenceA` function with `foldr` instead:

```
sequenceA :: (Applicative f) => [f a] -> f [a]
Assignment Project Example p
```

- https://eduassistpro.github.io/
 `(liftA2 (:)) ing on accumulator and next element both processedu assisentext of the functor `f`
 - it may help you to imagine the prefix `:` acting on the accumulator regardless of the functor context
- result is a nested list within the context of the passed in functor

*Using sequenceA

Take a moment to convince yourself of the following examples that the result matches the passed in context:

```
ghci> sequenceA [(+3),(+2),(+1)] 3
[6,5,4]
Assignment Project Exam Help
ghci
[[1, https://eduassistpro.git/j.lp,lp,lp,[3,5],[3,6]]

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ghci> sequenceA [[1,2,
```

• in short, `sequenceA [(+3),(+2),(+1)]` has resulting context as a function that takes one parameter

*Compare with sequenceA

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(\xshttps://eduassistpro.gitKtblid/

[] Similar to Nothing

```
ghci> sequenceA [Just 3, Just 2, Just 1]
Just [3,2,1]

ghci> sequenceA [Just 3, Nothing, Just 1]
Alsthignment Project Exam Help
```

- ap Maybe` values results in a list ne https://eduassistpro.github.io/
- usefulf we are intereedu_assist mayte `values where we only care about the result when none of the input elements are `Nothing`

*Multiple Predicates

Suppose we have a number that we would like to check if it satisfies a list of predicates:

```
Ansignment-Project, Fxam, Jobalp

[Tru
https://eduassistpro.github.io/
ghci> and $ map (\f -> edu_assist_pro
True

True
```

 recall that `and` returns `True` only when all of the elements in a list are `True` *sequenceA Refactor

We can achieve the same result as above with the `sequenceA` function:

```
ghci> sequenceA [(>4),(<10),odd] 7</pre>
[True, True, True]
Assignment Project Exam Help
ghci
True https://eduassistpro.github.io/
```

- Add WeChat edu_assist_pro
 `sequenceA [(>4),(<10),odd] ates a function that takes one parameter `7` and feeds it to the predicates
- it results in the list of `Boo1` values
- the type for `[(>4),(<10),odd] `is `(Num a) => [a -> Bool] `
- the type of `sequenceA [(>4),(<10),odd]` is `(Num a) => a -> [Bool]`

*Mixed Function Types

Note that lists must have the same type for each element.

- we cannot make a list such as `[ord, (+3)]`
 - `ord` takes a character and returns a number
 - `(+3)` takes a number and returns a number

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The quenceA `we consider is with the https://eduassistpro.github.io/

```
ghci> sequenceA [[1,2,3],[4,5,6]]
[[1,4],[1,5],[1,6],[2,4],[2,5],[2,6],[3,4],[3,5],[3,6]]
```

```
ghci> [[x, y] | x <- [1,2,3], y <- [4,5,6]]
[[1,4],[1,5],[1,6],[2,4],[2,5],[2,6],[3,4],[3,5],[3,6]]
```

*Using sequenceA with IO

One last useful application of `sequenceA` is on the context of `io`:

```
Assignment Project Exam Help ghci>sequence [getLine, getLine, getLine]

what https://eduassistpro.github.io/doin

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["what","doing","?"]
```

Finally

Altogether, we have used `<\$>` and `<*>` for:

- Assignmenteles of total total Help
- nohttps://eduassistpro.github.io/
- sets of computations edu_assist fante

Thank You!

Assignment Project Exam Help Questions?

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