#### Week 8

## Assignment Project Exam Help

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COMP 481: Functional and Logic Programming

#### Overview

- Wrapping an Existing Type Into a New Type
- Using `newtype` to Make Type Class Instances
- On `newtype` and Laziness
- Type Keywords Review Ssignment Project Exam Help
- Getting Back to Monoids
- The Monoid Laws
- A Few Monoids
  - Multiply and Sum
  - Any and All
  - The Ordering Monoid
  - <u>`Maybe` the Monoid</u>
- Folding with Monoids

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#### Programming Paradigms

There are two paradigms in programming that contrast each other, which you now know:

- procedural programming
  - uses functions and stores data within arrays
- object-oriented programming

Assignmendat Pastielde within a hierarched pobjects

Fun https://eduassistpro.github.jo/ programming.buttedu\_assist\_pro

- arranging data into arrays allows for fast access to it during execution
- access to data within a hierarchy of objects can be slow, because of stepping through pointers to get to it

## Arrays versus Records

Haskell has efficiency of arranging data apart from objects.

# Assignment Project Exam Help • th

- th o this point follows more lik https://eduassistpro.gitliub.io/ as another typing design we will learn
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(Unity 3D is in the process of implementing an Entity Component System for Data Oriented Technology Stack to pack data into arrays)

— Wrapping a https://eduassistpro.g@habN@w Type —

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### Two Behaviours

We have seen in the last chapter the two ways that lists can implement the `<\*>` operation:

- 1. with every nested function in the first list applied to every possible Asselement of the second list am Help
  - 2. ction of the first list applied to its https://eduassistpro.gគ្គមួយគ្នាស្រី

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The issue with ZipL it is implemented with the 
`data` keyword:

```
data ZipList a = ZipList { getZipList :: [a] }
```

# For object-oriented-like design, Haskell wraps and unwraps the nested `a` and `[a]` types each time in use of `zipList`.

this is not as efficient as it could be

## newtype

Alaskellalson has the chewtype keylpord for defining types so that its underlying type.

- th https://eduassistpro.githelbeided
  with implementations d applicatives
- this is because the ord only allows exactly one constructor
  - also, the constructor can have up to only one field (in a record, if desired)

## newtype with Functor Example (Simranjit Singh)

```
-- examples
                                             p1 = Score ("James", 1)
                        Assignment Project-Exam(Help, 4)
newtype Score a b =
                                                        "Drew", 8)
   Score { getScore :: (String https://eduassistpro.github.io/
       deriving Show
                             Add WeChatedu_assistp1pro
instance Functor (Score c) where
                                             ("James", 1)
   fmap f (Score (x, y)) = Score (x, f y)
                                             ghci> (+3) <$> p1
                                             Score {getScore = ("James",4)}
```

— Using `newty https://eduassistpro.gkhasso/nstances —

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# Swapping Parameters

To implement functor on a constructor with two parameters so that functions 'fmap' on its first parameter:

```
Assignment Project Exam Heip b) } deriving (Show)
```

```
inst https://eduassistpro.github.io/
fmap g (Pair (x, y x, y)
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```

note the swap in the constructor for `Pair b a` and the record `getPair :: (a, b)`

# Three Parameters

More parameters can be involved, and this time suppose we wanted to use the function on the second parameter:

```
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newtype Triple a c b = Triple { getTriple :: (a, b, c) } deriving (Sho

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instancel Functor (Trip edu_assist_pro

fmap g (Triple (x, ple (x, g y, z))
```

# Using `fmap`

Try `fmap` on a `Pair` and a `Triple` with some function. For example:

```
ghci> getPair (fmap reverse (Pair ("london calling", 3)))

Aussignment Project Exam Help
```

The https://eduassistpro.github.io/ The Haskellwitheairat edu\_assist\_pro

- they only allow us to implement another way to use `fmap` (as an example) with pairs and 3-tuples.
- we could create yet more `newtype` and implementations for pairs and 3-tuples if we wanted

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#### undefined

Haskell being lazy means it will only evaluate expressions until it absolutely must (e.g.: to print a result to output).

- only calculations that are necessary are performed, and no others
- Assignment Language Charles Value (a special keyword) wil

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```
ghci>AndefiredChat edu_assist_pro

*** Exception: Prelude.undefined

CallStack (from HasCallStack):
  error, called at libraries\base\GHC\Err.hs:75:14 in base:GHC.Err
  undefined, called at <interactive>:56:1 in interactive:Ghci3
```

# lgnoring undefined

however, notice how undefined can go unevaluated just fine when other calculations are the focus:

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ghci> head [1,2,3,unde Add WeChat edu\_assist\_pro

## `newtype versus `data`

'newtype' allows structures to be more lazy than 'data' because there is only exactly one constructor.

- Haskell must evaluate the parameters to determine which value constructor implementation matches with use of `data`
- the `newtype` value constructor implementation must only have the A sneyersion spevaluation that the deferred

```
data https://eduassistpro.gittoblb:ic3ool } deriving (Show)

helloMedd WeChat edu_assist_pro
helloMe (CoolBool _) = "hello!"
```

helloMe undefined
\*\*\* Exception: Prelude.undefined

# Demonstration of newtype Laziness

# Exit interactive session and reenter to define the next version:

```
newtype CoolBool = CoolBool { getCoolBool :: Bool } deriving
(Show)
```

```
helloMe :: CoolBool -> String

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```

ghci https://eduassistpro.github.io/

```
"hello!"dd WeChat edu_assist_pro
```

• the `(CoolBool \_)` did not need to evaluate `undefined`

#### Altogether, the difference between `data` and `newtype` is:

- make completely new types with `data`
- make other versions of types with `newtype`

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## type

The `type` keyword is just used to create synonyms.

```
• e.g.: `type IntList = [Int]`
```

Astingkendentribionsotolexeadathelipe function signatures

```
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[1,2,3,1d, WeChat edu_assist_pro
```

 recall we created another name for the list association `[(String,String)]` as a `PhoneBook`

#### The `newtype` will create a completely separate type:

```
newtype CharList = CharList { getCharList :: [Char] } deriving
(Show)
```

- 'CharList' values cannot have '++' applied with Assther Tokan' values because the two types are different
- twhttps://eduassistpro.gincatenated with `++`, since `++` is not even implemente
  - -Atd dos ble Chate edu\_assist \ [ [ ] apply \ ++ \ and convert back
  - `newtype` record syntax provides the field `getCharList` as conversion function
- none of the `[Char]` instance implementations are inherited to `CharList` for any of the involved type classes
  - you will need to derive or manually write them

newtype Implementations Three Kinds of Data Implementation

Consider using `newtype` over `data` when you only have one value constructor.

Abeighteecan Briggerules to follows:

- 1. https://eduassistpro.github.io/ 1. the type` synonym will do
- 2. If an aiready existit edu\_assist proper and implemented as an instance of a type class—the `newtype` keyword will do
- 3. If a completely new type is needed—the `data` keyword will do

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# Monoid Type Class

So we can implement instances of different type classes.

We have seen and learned of their usefulness:

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• `E `, etc.

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Thera is vertanotheredu\_assishatis fairly involved and powerful, called `Mo

- a `Monoid` describes a combination of
  - a binary function
  - with an identity value

# Monoid Example

#### An example:

```
ghci> [1,2,3] ++ []
[1,2,3]

Absirghtteft Project Exam Help
[1,2

https://eduassistpro.github.io/
```

- above the binary fun edu\_assist\_pro d the identity element is `[]`
  - notice the identity element leaves the other operand unchanged, regardless of which side it is applied

Can you think of other examples?

#### 'Monoid' implementation is as follows:

```
class Monoid m where
    mempty :: m
    mappend :: m -> m -> m
    mconcat :: [m] -> m
    Assignment Project Example Help
    mconcat = foldr Mappend mempty
```

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- `mempty` describes th constant that should act as the identity element hat edu\_assist\_pro
- 'mappend' is a misnomer, and should be some associative binary operator
- 'mconcat' is *implemented by default* to take a list and forms one monoid value using 'mappend' between its elements
  - `mconcat` can have its default implementation changed depending on `m`

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## Monoid Laws

The following three laws involving `Monoid` are not implemented in Haskell by default...

...so you will need to check your own implementations when you create instances!

The last law requires a 'Monoid' instance to ensure order of evaluation of 'mappend' operations do not matter:

Assignment dest law were at gepaway with writing

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Part of the reasonat edu\_assistia procee such laws hold:

 we then do not have to change our understanding of a computational result based on order of operations

#### Associativity

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Implementing a Monoid Instance

We saw the example of `[]` and `++` function as a `Monoid` instance, which has the following implementation:

instance Monoid [a] where Assignment Project Exam Help

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- the mider relation oedu\_assist`Monoid` requires a concrete type, so note the use
   t`[]`
- (requirement since version `build-4.11.0.0` for `Semigroup` to be a superclass of a `Monoid`, but we leave this for a bit later)

# Examples of Using Monoid Behaviour

```
ghci> [1,2,3] `mappend` [4,5,6]
[1,2,3,4,5,6]
ghci> ("one" `mappend` "two") `mappend` "three"
"onetwothree"
ghci> "one" `mappend` ("two" `mappend` "three")
"onetwothree" Project Exam Help
                                end` "three"
ghci
"one https://eduassistpro.github.io/
ghci>A"ping Wreependt edu_assist_pro
"ping"
ghci> mconcat [[1,2],[3,6],[9]]
[1,2,3,6,9]
ghci> mempty :: [a]
```

# Details on Examples (monoid behaviour)

- we needed a type annotation in the last expression, because Haskell would not be able to infer any type for it without giving `:: [a]`
- it is more general to write `[a]` than `[Int]` or `[String]`, ASSIginde (Int) could contain all its elements of any one type
- th https://eduassistppligithub.io/ `demonstrates ho

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The above examples demonstrated how `++` and `[]` satisfy the associativity and identity laws.

- there is no requirement to satisfy any commutativity laws
  - swapping order of elements in a `++` operation will be different
    - ghci> "tick" ++ "tock"

• "ticktock"
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#### https://eduassistpro.github.io/

- other moneids c edu\_assist\_pro 'mappend':
- to be commutative, the result of the binary operation must be the same, regardless of order, for **every** pair of possible operands

#### Commutativity

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#### Understand that both

- '+' and '0' is a monoid
- as well as `\*` and `1` are a different monoid.

#### Semigroup

Recap: we can treat the same kind of thing with different Amplementations of type classes by repurposing them with 'newtype'.

https://eduassistpro.github.io/ implementations for the two We mondidd Wethatt edu assistepras had an update since version `base-4.11.0.0`:

- any `Monoid` must also be a `Semigroup` instance
- `Semigroup` means that the associativity should be implemented and expected before implementing `Monoid`

```
We start with `Multiply`:
newtype Multiply a = Multiply { getMultiply :: a }
    deriving (Eq, Ord, Read, Show, Bounded)
instance Num a => Semigroup (Multiply a) where
     (Multiply x) \leftrightarrow (Multiply y) = Multiply (x * y)
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inst
                                ply a) where
     https://eduassistpro.github.io/
    mappend = (<>)
     Add WeChat edu_assist_pro
Now we can try the following operations using `<>`:
ghci> getMultiply $ Multiply 3 <> Multiply 9
ghci> getMultiply $ Multiply 3 <> mempty
ghci> getMultiply $ Multiply 3 <> Multiply 4 <> Multiply 2
ghci> getMultiply . mconcat . map Multiply $ [3,4,2]
```

# Implement 'Sum' as a Monoid Instance

Practice implementing `Sum` similarly to `Multiply`.

You will need to think about what the identity element is that corresponds to the operation of binary addition.

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• on it with the following: https://eduassistpro.github.io/

```
ghci> getSum $ Sum 2 edu_assist_pro

11

ghci> getSum $ mempty <> Sum 3

3

ghci> getSum . mconcat . map Sum $ [1, 2, 3]

6
```

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### Bool as a Monoid

We can work with `Bool` values and its common operations for our own monoids as well (like operators OR and AND).

 convince yourself of the `mempty` definition for the implementation where `<>` takes on the binary operation of OR:

#### And give the following a try:

```
ghci> getAny $ Any True <> Any False
True
Assignment Project Exam Help ghci> getAny $ mempty <> Any True
True https://eduassistpro.github.io/
ghci>AgetAnyWercoheat edu_assisfalgen False, False, True]
True
ghci> getAny $ mempty <> mempty
False
```

## Bool as a Different Monoid

#### Can you implement another `<>` for the AND operator?

• it should have the following results:

```
ghci> getAll $ mempty <> All True
Arsignment Project Exam Help
ghci https://eduassistpro.gfthub.io/
False
    Add WeChat edu_assist_pro
ghci> getAll . mconcat . map All $ [True, True, True]
True
ghci> getAll . mconcat . map All $ [True, True, False]
False
```

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— Thttps://eduassistpro.github.io/

### Comparing Integers

The following slides are merely a demonstration of how to mix restrictions on comparing between `String` values.

we have the three possible results of comparing integers:

```
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ghci> 2 'compare' 2

EQ Add WeChat edu_assist_pro

ghci> 3 `compare' 2

GT
```

(could implement for `Char` as well)

## Appending Ordering Values

Although it may not seem as if it would be possible to define 'Monoid' behaviour over the three ordering values, it is already done so:

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 you can check that the `mempty` acts like the identity on the other ordering values

#### Refined Comparison

#### The following might be a way we want to compare strings:

```
lengthCompare :: String -> String -> Ordering
lengthCompare x y =
      (length x `compare` length y) `mappend`
      (x `compare` y)
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```

- - Abdt of the two stath edu\_assist he length, they will be further compared alphabetically

```
ghci> lengthCompare "zen" "ants"
LT
ghci> lengthCompare "zen" "ant"
GT
```

Even More Refined Comparison We might want to design an a more refined scheme.

Further refine comparison to check between `x` and `y` by

Assiber of vowels before alphabetic comparison:

```
https://eduassistpro.github.io/
lengthCompare/Xethat edu_assist_pro
    (length x `compare mappend`
    (vowels x `compare` vowels y) `mappend`
    (x `compare` y)
where vowels = length . filter (`elem` "aeiou")
```

## Example of Orderings

See how the above refinement of ordering affects results with use of `lengthCompare`:

```
ghci> lengthCompare "zen" "anna"
LT
Assignment Project Exam Help
ghci
LT https://eduassistpro.github.io/
    Add WeChat edu_assist_pro
ghci> lengthCompare "z
GT
```

This is only one example of how to apply 'Monoids' in a non-trivial way toward creating your own orderings.

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#### Nested Monoids

Already implemented is the use of `Maybe` as a monoid (and a semigroup).

• the nested elements can also be instances of `Monoid` and `Semigroup`, so the implementations look like the following:

```
Anstigue Description (Value a) where

https://eduassistpro.github.io/
(Just x) <> (Just Add WeChat edu_assist_pro

instance Monoid a => Monoid (Maybe a) where

mempty = Nothing

mappend = (<>)
```

notice how `x <> y` nests in right evaluation of a `Just` element

### Ignoring Nothing

#### Give the following a try:

```
ghci> Nothing <> Just "andy"

Just "andy"

ghci> Just LT <> Nothing

Just LT

Abci grust (54m B) cjeuts E (54m 4) Help

Just

https://eduassistpro.github.io/
```

• we can use `Maybe` ted values for types previously defined to Work With edu\_assisteir own, such as `Sum`

#### The above implementation of `Maybe` is very useful:

- for working with binary computations in the nested elements when we do not care that some of the `Maybe` values are `Nothing`
- since they are absorbed during calculations as an identity

#### Only the First Element

```
And `Maybe` values with nested element not a monoid?
```

• grab the values without worrying about nested operations

Create `newtype First` as implementation of `Maybe`:

```
newtype First a = First { getFirst :: Maybe a }
deriving (Eq. Ord, Read, Show)
Assignment Project Exam Help
https://eduassistpro.github.io/
     First d Week hat edu_assist_pro
 instance Monoid (First a) where
     mempty = First Nothing
     mappend = (<>)
```

### Using 'First' as a Monoid

This way, we can work with the *first* element that is not `First Nothing` given some operations with `<>`:

```
ghci> getFirst $ First (Just 'a') <> First (Just 'b')
Just 'a'
Assignment Project Exam Help
ghci
Just https://eduassistpro.github.io/
    Add WeChat edu_assist_pro
ghci> getFirst $ First > First Nothing
Just 'a'
ghci> getFirst . mconcat . map First $ [Nothing, Just 9, Just 10]
Just 9
```

#### Last

Just 10

The `Data.Monoid` module already has a `Last` data type implemented that works similarly

Atalways evaluate to the right non-`Nothing` value:

```
https://eduassistpro.github.io/ghci
ghci>Agettast/eccange edu_assist[Nothing, Just 9, Just 10]
```

• note that Haskell cn imply the package prefix for unique names

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#### The `foldr` function:

- used to have different version found in the `Data.Foldable` module
- allows us similar operations on other types that act similar to lists
- it is now just implemented into the `Prelude` default version
- the default only used to work on lists

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Tre e we could practice folding:

• obhttps://eduassistpro.githeuheichnstance of `Foldable`

```
ghci>AddolareChat edu_assist_pro
foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b
```

Just a quick reminder demo:

```
ghci> foldr (*) 1 [1,2,3]
6
```

## Folding with Monoids

#### In this example, the first parameter is a binary operation:

- the second parameter is the starting accumulator value
- the third parameter is the list we want to fold

#### A few more examples:

```
Assignment Project Exam Help ghci
```

```
https://eduassistpro.github.io/ghci> foldl (||) False
True Add WeChat edu_assist_pro
```

#### When folding right, whatever <u>function</u> we pass must have:

- its first parameter as the next input list element
- its second parameter as the accumulator

## Folding with Nothing

Something that is a bit weird, but works, because of monoid behaviour:

```
ghci> foldl (||) False (Nothing)
False
Assignment Project Exam Help
    https://eduassistpro.github.io/
FalseAdd WeChat edu_assist_pro
ghci> foldl (&&) True (Nothing)
True
```

the above I just remember as the fold as acting on the identity

#### Foldable Trees

We make another type an instance of `Foldable` with the Area gata structure we had previously defined:

https://eduassistpro.github.jo/ (Tree a) deriving (Show)
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#### To make something foldable, we must implement a function called `foldMap`, which is described with the type:

Assignment Project Exam Help -> m) -> t a -> m

- th https://eduassistpro.github.io/
  - •A (11d-17m) (ana fuedu\_assisted element type `a` to an element that can b
  - the data structure `t a` we would like to fold
  - the final result of the fold 'm' for one monoid value

#### foldMap

### Implementing `foldMap` for `Tree`

We need to implement `foldMap` function for our trees:

```
instance Foldable Tree where
    foldMap g EmptyTree = mempty
    foldMap g (Node x l r) =
AssignfaldMap Brbject Exam Help
```

https://eduassistpro.github.io/

• the above implement in-order traversal

- a tree that is empty just evaluates to the monoid `mempty` value
  - this way, when the recursive `foldMap` reaches empty leaf nodes, they
    resolve as identity operations to the other parent nodes

#### A Test Tree

Testing trees out in an interactive ghci session is a bit much to type, but it is easiest to do in multiline syntax:

```
:{
testTree = Node 5
 (Node 3
A(Wigniferety/Tree)am Help
 (No
    https://eduassistpro.github.io/
 (Node 9
 (Node of the pty free hat edu_assist_pro
 (Node 10 EmptyTree EmptyTree)
 :}
```

(lines are blocked after `Node 5` with one space at the front)

### Folding `testTree`

Now you should be able to check:

```
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ghci

ghci

6480 https://eduassistpro.github.io/
```

- the first result is just the sum of all the nested node values together
- the second result is just the product of all of the nested node values together

#### Using Nested Monoids

#### But we want to see `foldMap` in action:

```
ghci> getAny $ foldMap (\x -> Any $ x == 3) testTree True
```

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- th the tree are by `<>` and not some fu https://eduassistpro.githerested elements themselves
- we converted edu\_assignch node to something that has monoid behaviour, i. e (we defined earlier)
- the result is whether some node in the tree contains the value `3`

# Applying Custom Nested Monoids

If instead we wanted to get the sum of all the elements, you can guess we would next use the monoid we defined Assignification in the elements.

Assignification is a sum of all the elements, and it is a sum of all the elements.

```
https://eduassistpro.github.io/
ghci https://eduassistpro.github.io/
42 Add WeChat edu_assist_pro
ghci> getMultiply $ fo (Multiply x)) testTree
64800
```

#### More Nested Monoids

We would likely not implement basic operations as those already defined to work with the fold functions.

Keep in mind the flexibility with each of the further implementations

As Mannie Televisite Exam Help

ghci https://eduassistpro.git/hub.is/ testTree
False
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The above checks whether any of the nodes in the `testTree` have a value above `15`, which it does not.

#### Conversion to Lists

We can even convert our tree into a list:

```
ghci> foldMap (\x -> [x]) testTree
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```

- https://eduassistpro.github.io/ Mon tion <>`performed on lists corkaterates that edu\_assist\_pro
- we could change the order of the traversal in the implementation of `foldMap` for our trees

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#### Monad Example (David Semke)

```
instance Monad Box where
import Data.Monoid
                                               return x = Box x
                                               Box x \gg f = f x
data Box a = Box a
                       Assignment Project Exam Help
   deriving (Show)
                            https://eduassistpro.github.io/
instance Functor Box where
   fmap f (Box x) = Box (f x)
                            Add WeChatedu_assista broBox (a `mappend` b)
instance Applicative Box where
                                            resultChars =
   pure x = Box x
                                               Box "day" >>= (combineIntoBox "good")
    (Box f) <^*> x = fmap f x
                                            resultAny = Box (Any False)
```

>>= combineIntoBox (Any True)

Thank You!

Assignment Project Exam Help Questions?

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