

Can you use a hashtable to implement skipTo()?

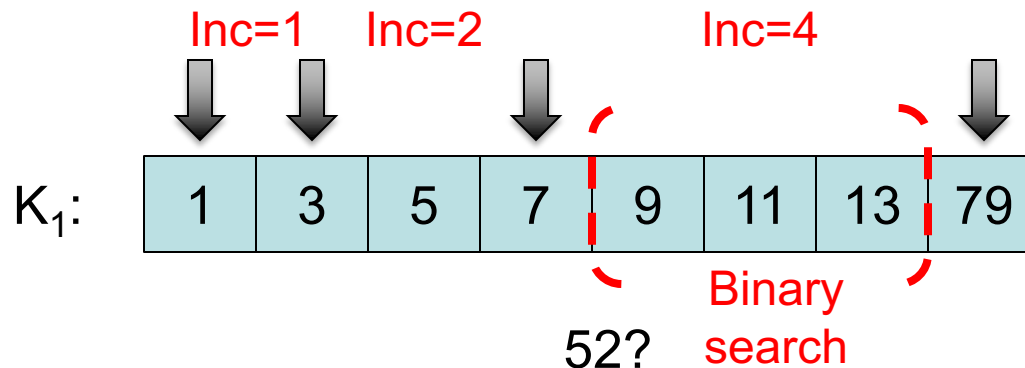
Better than next()

- What's the worst case for sequential merge-based intersection?
- {52, 1} → **Assignment Project Exam Help**
 - To the position of the first element in K₂'s list that is greater than or equal to 52. **skipTo(52)**
 - Essentially, **<https://eduassistpro.github.io/>** $2[i] \geq 52$ (K₂'s list is sorted).
 - Takes many sequential call of **Add WeChat edu_assist_pro**
 - Could use binary search in the rest of the list
 - Cost: $\lceil \log_2(N_{\text{remainder}}) \rceil$

K ₂ :	1	3	5	79
K ₁ :	52	54	56	58				

skipTo(id)

- Galloping search (gambler's strategy)
 - [Stage 1] Doubling the search range until you overshoot
 - [Stage 2] Perform binary search in the last range
- Performance analysis (worst case)
 - Let the destination be far away.
 - $\approx \log_2 n$ probes in Stage 1 + \approx probes in Stage 2
 - Total = $2 \lceil \log_2 (n+1) \rceil = O(\log_2 n)$



Total Cost

- Galloping search (gambler's strategy)
 - Cost of the i -th probe: $\approx 2 \log_2(n_i)$
 - Total cost of K_1 probes: $\approx 2 \log_2(\prod_{i=1}^{|K_1|} n_i)$
 - $\leq 2 \log_2((\sum_{i=1}^{|K_1|} \log_2(|K_2|/|K_1|)) \cdot |K_1|)$
- Asymptotic r merge when $|K_2|/|K_1| = O(1)$, resembles r merge when $|K_1| = O(1)$

What about list intersection using binary search?

Multiple Term Conjunctive Queries

- K_1 AND K_2 AND ... AND K_n
- SvS does not perform well if none of the associate <https://eduassistpro.github.io/>
- In addition, it is block [Add WeChat edu_assist_pro](#)
- Can you design non-blocking multiple sorted array intersection algorithm?

Generalization

- Generalize the 2-way intersection algorithm

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- 2-way: <https://eduassistpro.github.io/>

- $\{1, 2\} \rightarrow$ move k_1 's cursor
- skipTo(2)

K_1 :	1	3		
:	2	4	6	
K_3 :	3	9	27	81

- 3-way:
 - $\{1, 2, 3\} \rightarrow$ move k_1, k_2 's cursor
 - skipTo(3)

$$\text{eliminator} = \text{Max}_{1 \leq i \leq n} (k_i.\text{cursor})$$

Optimization

- Mismatch found even before accessing K_3 's cursor

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- Choice 1: c
cursors of other list

<https://eduassistpro.github.io/>

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- Choice 2: settle the

K_1 :	1	3		
K_2 :	2	4	6	
:	3	9	27	81

dispute within the first two lists → max
algorithm [Culpepper & Moffat, 2010]

- Better locality of access → fewer cache misses
- Similar to SvS

Pseudo-Code for the **Max** Algorithm (Wrong)

- Input: K_1, K_2, \dots, K_n in increasing size

```
(1)  $x := K_1[1]$ ;  $startAt := 2$  //x is the eliminator
(2) while  $x$  is defined do
(3)   for  $i = startAt$  to  $n$  do
(4)      $y := K_i.skipTo(x)$ 
(5)     if  $y > x$  then
(6)        $x := K_1$  //res //restart_2
(7)       if  $y > x$  then  $startAt := 2$  end if
(8)       break //match in all lists
(9)     elsif  $i = n$  then //y = x
(10)      Output  $x$ 
(11)       $x := K_1.next()$ 
(12)    end if
(13)  end for
(14) end while
```

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A



B



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C



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D



The original code has a bug when in restart_1 cases

Pseudo-Code for the **Max** Algorithm (Fixed)

- Input: K_1, K_2, \dots, K_n in increasing size

```
(1)  $x := K_1[1]$ ;  $startAt := 2$ 
(2) while  $x$  is defined do
(3)     for  $i = startAt$  to  $n$  do
(4)          $y := K_i.skipTo(x)$ 
(5)         if  $y > x$  th
(6)              $x := K_1$ 
(7)             if  $y > x$  then  $startAt := 2$  end if
(8)             break
(9)         elseif  $i = n$  then
(10)            Output  $x$ 
(11)             $x := K_1.next()$ 
(12)        end if
(13)    end for
(14) end while
```

(4.1) **if** $i = 1$ **then**
(4.2) **if** $y > x$ **then**
(4.3) $x := y$
(4.4) **break**

<https://eduassistpro.github.io/>
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References

- J. Shane Culpepper, Alistair Moffat: Efficient set intersection for projected indexing. ACM Trans. Inf. <https://eduassistpro.github.io/>
- F.K. Hwan e algorithm for merging two disjoint indexed sets. SIAM J. Comput. 1 1 (1972), pp. 31–39. [Add WeChat edu_assist_pro](#)
- Stefan Buettcher, Charles L. A. Clarke, Gordon V. Cormack, Information Retrieval: Implementing and Evaluating Search Engines, 2010 [Chapter 5]