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Introduction to Informa

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<https://eduassistpro.github.io/>

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Lecture 6: Scoring, Termination and the
Vector Space Model

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This lecture, IR Se .2-6.4.3

- Ranked retrieval
- Scoring documents
- Term frequency
- Collection sta <https://eduassistpro.github.io/>
- Weighting schemes
- Vector space scoring

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Ranked retrieval

- Thus far, our queries have all been Boolean.
 - Documents either match or don't.
- Good for expert users with precise understanding of their needs a <https://eduassistpro.github.io/>
 - Also good for applications: A can easily consume 1000s of results.
- Not good for the majority of users.
 - Most users incapable of writing Boolean queries (or they are, but they think it's too much work).
 - Most users don't want to wade through 1000s of results.
 - This is particularly true of web search.

Problem with Boolean search: feast or famine

- Boolean queries often result in either too few (=0) or too many (1000s) results.
- Query 1: “standard user dlink 650” → 200,000 hits
- Query 2: “standard user dlink 650 card found”: 0 hits
- It takes a lot of skill to come up with a query that produces a manageable number of hits.
 - AND gives too few; OR gives too many

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Ranked retrieval

- Rather than a set of documents satisfying a query expression, in **ranked retrieval models**, the system returns an ordering over the (top) documents in the collection with
<https://eduassistpro.github.io/>
- **Free text queries**: Rather than a language of operators and expressions, a query is just one or more words in a human language
- In principle, there are two separate choices here, but in practice, ranked retrieval models have normally been associated with free text queries and vice versa

Feast or famine: not a problem in ranked retrieval

- When a system produces a ranked result set, large result sets are not an issue
 - Indeed, the size of the result set is not an issue
 - We just show it
 - We don't over
- Premise: the ranking algorithm works

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Scoring as the basic ranked retrieval

- We wish to return in order the documents most likely to be useful to the searcher
- How can we rank-order the documents in the collection with <https://eduassistpro.github.io/>
- Assign a score – say in $[0, 1]$ document
- This score measures how well document and query “match”.

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Query-document scores

- We need a way of assigning a score to a query/document pair
- Let's start with a one-term query
- If the query term is in the document: score should be 0
- The more frequent the query term in the document, the higher the score (should be)
- We will look at a number of alternatives for this.

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Take 1: Jaccard coefficient

- Recall from Lecture 3: A commonly used measure of overlap of two sets A and B
- $\text{jaccard}(A, B) = \frac{|A \cap B|}{|A \cup B|}$
- $\text{jaccard}(A, A) = 1$
- $\text{jaccard}(A, B) = 0$ if $A \cap B = \emptyset$
- A and B don't have to be the same size.
- Always assigns a number between 0 and 1.

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Jaccard coefficient example

- What is the query-document match score that the Jaccard coefficient computes for each of the two documents below?
- Query: *ides of* <https://eduassistpro.github.io/>
- Document 1: *caesar died in*
- Document 2: *the long marc*

the term *Ides of March* is best known as the date that Julius Caesar was killed in 709 AUC or 44 B.C

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Issues with Jaccard

- 1 It doesn't consider *term frequency* (how many times a term occurs in a document)
 - 2 Rare terms in a collection are more informative than frequent terms. <https://eduassistpro.github.io/> doesn't consider this information
- We need a more sophisticated weighting for length

Recall (Lecture 1). Binary term-document incidence

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	1	0	0	0	1
Brutus	1	1	0	1	0	0
Caesar	1			1	1	1
Calpurnia	0			0	0	0
Cleopatra	1	0		0	0	0
mercy	1	0		1	1	1
worser	1	0	1	1	1	0

Each document is represented by a binary vector $\in \{0,1\}^{|V|}$

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Term-document co-occurrences

- Consider the number of occurrences of a term in a document:
 - Each document is a count vector in \mathbb{N}^N : a column below

<https://eduassistpro.github.io/>

	Antony and Cleopatra	Julius Caesar	Hamlet	Othello	Macbeth
Antony	157	73	0	0	0
Brutus	4	157	0	1	0
Caesar	232	227	0	2	1
Calpurnia	0	10	0	0	0
Cleopatra	57	0	0	0	0
mercy	2	0	3	5	1
worser	2	0	1	1	0

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Bag of words model

- Vector representation doesn't consider the ordering of words in a document
- *John is quicker than Mary and Mary is quicker than John* have the <https://eduassistpro.github.io/>
- This is called the bag of words
- In a sense, this is a step back. A positional index was able to distinguish these two documents.
- We will look at “recovering” positional information later in this course.
- For now: bag of words model

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Term frequency tf

- The term frequency $tf_{t,d}$ of term t in document d is defined as the number of times that t occurs in d .
- We want to use tf when computing query-document match scores.
- Raw term frequency is not a good measure of relevance:
 - A document with 10 occurrences of a term is more relevant than a document with 1 occurrence of the term.
 - But not 10 times more relevant.
- Relevance does not increase proportionally with term frequency.

NB: frequency = count in IR

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Log-frequency [Add WeChat edu_assist_pro](https://eduassistpro.github.io/)

- The log frequency weight of term t in d is

$$w_{t,d} = \begin{cases} 1 + \log_{10} \text{tf}_{t,d}, & \text{if } \text{tf}_{t,d} > 0 \\ 0, & \text{otherwise} \end{cases}$$

- $0 \rightarrow 0, 1 \rightarrow 1, \text{https://eduassistpro.github.io/} \rightarrow 4, \text{etc.}$
- Score for a document d over terms t in both q and d :
[Add WeChat edu_assist_pro](https://eduassistpro.github.io/)
- $\text{score} = \sum_{t \in q \cap d} (1 + \log \text{tf}_{t,d})$
- The score is 0 if none of the query terms is present in the document.

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Document frequency

- Rare terms are more informative than frequent terms
 - Recall stop words
- Consider a term *arachn* that is in the collection (e.g. <https://eduassistpro.github.io/>)
- A document containing this term is likely to be relevant to the query *arachn*
- → We want a high weight for rare terms like *arachnocentric*.

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Document frequency

- Frequent terms are less informative than rare terms
- Consider a query term that is frequent in the collection (e.g., *high*, *increase*, *line*)
- A document <https://eduassistpro.github.io/> is more likely to be relevant than a document that isn't
- But it's not a sure indicator
- → For frequent terms, we want high positive weights for words like *high*, *increase*, and *line*
- But lower weights than for rare terms.
- We will use document frequency (df) to capture this.

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idf weight

- df_t is the document frequency of t : the number of documents that contain t
 - df_t is an inverse measure of the informativeness of t
 - $df_t \leq N$
- We define the t frequency) of t by
$$idf_t = \log_{10} (N/df_t)$$
 - We use $\log (N/df_t)$ instead of N/df_t to “dampen” the effect of idf.

Will turn out the base of the log is immaterial.

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idf example, suppose million

term	df_t	idf_t
calpurnia	1	
animal	100	
sunday		
fly		
under		
the	1,000,000	

$$idf_t = \log_{10} (N/df_t)$$

There is one idf value for each term t in a collection.

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Effect of idf on ran

- Does idf have an effect on ranking for one-term queries, like
 - iPhone
- idf has no eff
 - idf affects the ranking of doc queries with at least two terms
 - For the query *capricious person*, idf weighting makes occurrences of *capricious* count for much more in the final document ranking than occurrences of *person*.

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Collection vs. Document Frequency

- The collection frequency of t is the number of occurrences of t in the collection, counting multiple occurrences.

- Example: <https://eduassistpro.github.io/>

Word	Collection frequency	Document frequency
<i>insurance</i>	10440	3997
<i>try</i>	10422	8760

- Which word is a better search term (and should get a higher weight)?

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tf-idf weighting

- The tf-idf weight of a term is the product of its tf weight and its idf weight.

$$w_{t,d} = \left(1 + \frac{N}{df_t}\right)$$

- Best known weighting scheme for information retrieval
 - Note: the “-” in tf-idf is a hyphen, not a minus sign!
 - Alternative names: tf.idf, tf x idf
- Increases with the number of occurrences within a document
- Increases with the rarity of the term in the collection

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Final ranking of documents for a query

$$\text{Score}(q, d) = \sum_{t \in q \cap d} \text{tf.idf}_{t,d}$$

<https://eduassistpro.github.io/>

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Binary \rightarrow count \rightarrow matrix

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	5.25	3.18	0	0	0	0.35
Brutus	1.21	6.1	0	1	0	0
Caesar	8.59			1.51	0.25	0
Calpurnia	0			0	0	0
Cleopatra	2.85	0		0	0	0
mercy	1.51	0		0.12	5.25	0.88
worser	1.37	0	0.11	4.15	0.25	1.95

Each document is now represented by a real-valued vector of tf-idf weights $\in \mathbb{R}^{|V|}$

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Documents as vect

- So we have a $|V|$ -dimensional vector space
- Terms are axes of the space
- Documents are points in this space
- Very high-dimensional vectors
<https://eduassistpro.github.io/>
dimensions when you apply web search engine
- These are very sparse vectors - most entries are zero.

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Queries as vectors

- Key idea 1: Do the same for queries: represent them as vectors in the space
- Key idea 2: Rank documents according to their proximity to q
<https://eduassistpro.github.io/>
- proximity = similarity of q and d
- proximity \approx inverse of distance
- Recall: We do this because we want to get away from the you're-either-in-or-out Boolean model.
- Instead: rank more relevant documents higher than less relevant documents

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Formalizing vector proximity

- First cut: distance between two points
 - (= distance between the end points of the two vectors)
- Euclidean distance?
- Euclidean distance <https://eduassistpro.github.io/>
- ... because Euclidean distance for vectors of different lengths.

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Why distance is a

The Euclidean distance between q

and \vec{d}_2 is large even though the

distribution of terms in the query q and the distribution of

terms in the document \vec{d}_2 are very similar.

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Use angle instead

- **Thought experiment:** take a document d and append it to itself. Call this document d' .
- “Semantically” d and d' have the same content
- The Euclidean distance between two documents can be quite large
- The angle between the two documents is 0, corresponding to maximal similarity.
- Key idea: Rank documents according to angle with query.

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From angles to cos

- The following two notions are equivalent.
 - Rank documents in decreasing order of the angle between query and document
 - Rank documents in increasing order of $\cos(\text{angle between query and document})$
- Cosine is a monotonically decreasing function for the interval $[0^\circ, 180^\circ]$

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From angles to cos

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<https://eduassistpro.github.io/>

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- But how – *and why* – should we be computing cosines?

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Length normalization

- A vector can be (length-) normalized by dividing each of its components by its length – for this we use the L_2 norm: $\frac{\vec{v}}{\|\vec{v}\|_2}$
- Dividing a vector by its L_2 norm (length) vector (on surface of unit sphere)
- Effect on the two documents d and d' (d appended to itself) from earlier slide: they have identical vectors after length-normalization.
 - Long and short documents now have comparable weights

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cosine(query, docu

Dot product

Unit vectors

$$\cos(\vec{q}, \vec{d}) = \frac{\vec{q} \cdot \vec{d}}{\|\vec{q}\| \|\vec{d}\|} = \frac{\sum_{i=1}^{|V|} q_i d_i}{\sqrt{\sum_{i=1}^{|V|} q_i^2} \sqrt{\sum_{i=1}^{|V|} d_i^2}}$$

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q_i is the tf-idf weight of term i in the query

d_i is the tf-idf weight of term i in the document

$\cos(\vec{q}, \vec{d})$ is the cosine similarity of \vec{q} and \vec{d} ... or, equivalently, the cosine of the angle between \vec{q} and \vec{d} .

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Cosine for length-n ed vectors

- For length-normalized vectors, cosine similarity is simply the dot product (or scalar product):

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$$\cos(\vec{q}, \vec{d}_i)$$

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for q, d length-normalized.

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Cosine similarity ill

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Cosine similarity among documents

How similar are

the novels

SaS: *Sense and*

Sensibility

PaP: *Pride and*

Prejudice, and

WH: *Wuthering*

Heights?

term	SaS	PaP	WH
affection	115	58	20
gossip	7	11	6
wuthering	0	0	38

Term frequencies (counts)

Note: To simplify this example, we don't do idf weighting in this example.

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3 documents exam Add WeChat edu_assist_pro

Log frequency weighting

After length normalization

term	SaS	PaP	WH	term	SaS	PaP	WH
affection	3.06				0.789	0.832	0.524
jealous	2.00				0.515	0.555	0.465
gossip	1.30	0	1.78	g	.335	0	0.405
wuthering	0	0	2.58		0	0	0.588

$\cos(\text{SaS}, \text{PaP}) \approx$

$$0.789 \times 0.832 + 0.515 \times 0.555 + 0.335 \times 0.0 + 0.0 \times 0.0 \\ \approx 0.94$$

$\cos(\text{SaS}, \text{WH}) \approx 0.79$

$\cos(\text{PaP}, \text{WH}) \approx 0.69$

Why do we have $\cos(\text{SaS}, \text{PaP}) > \cos(\text{SaS}, \text{WH})$?

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Computing cosine s

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tf-idf weighting has many variants

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<https://eduassistpro.github.io/>

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Columns headed 'n' are acronyms for weight schemes.

Why is the base of the log in idf immaterial?

Weighting may differ in queries vs documents

- Many search engines allow for different weightings for queries vs. documents
- SMART Notation: denotes the combination in use in an engine, with using the acronyms from <https://eduassistpro.github.io/>
- A very standard weighting
 - Document: logarithmic tf (l as first character), no idf and cosine normalization
 - Query: logarithmic tf (l in leftmost column), idf (t in second column), cosine normalization ...

A bad idea?

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tf-idf example: Inc.

Document: *car insurance auto insurance*
Query: *best car insurance*

Term	Query						Document				Pro d
	tf-raw	tf-wt	idf	tf-idf	tf	wt	tf-raw	tf-wt	n'lize		
auto	0	0	50000	2.3	0	0	1	1	0.52		0
best	1	1	50000	1.3	1.3	0.34	0	0	0	0	0
car	1	1	10000	2.0	2.0	0.52	1	1	1	0.52	0.27
insurance	1	1	1000	3.0	3.0	0.78	2	1.3	1.3	0.68	0.53

Exercise: what is N, the number of docs?

Doc length = $\sqrt{1^2 + 0^2 + 1^2 + 1.3^2} \approx 1.92$

Score = $0+0+0.27+0.53 = 0.8$

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Representation/feature perspective

- Inc.ltc
 - doc vector:
 - tf-vector
 - normalized
 - query vector
 - tf-idf-vector
 - normalized to unit length
 - score = similarity = inner product between the two vectors

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Summary – vector ranking

- Represent the query as a weighted tf-idf vector
- Represent each document as a weighted tf-idf vector
- Compute the dot product for the query vector and each document vector
- Rank documents with respect to query by score
- Return the top K (e.g., $K = 10$) to the user

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Resources for today

- IIR 6.2 – 6.4.3
- <http://www.n-retrieval-tutorial/cosine-similarity/>
<https://eduassistpro.github.io/>
 - Term weighting and cosine similarity tutorial for SEO folk!